

**UNIVERSITY OF GHANA**

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**BSC. MATERIALS SCIENCE AND ENGINEERING  
END OF FIRST SEMESTER EXAMINATIONS: 2016/2017  
DEPARTMENT OF MATERIALS SCIENCE AND ENGINEERING**

**MTEN 307: PHASE EQUILIBRIA OF MATERIALS (2 Credits)**

**TIME ALLOWED: TWO (2) HOURS**

**ANSWER ALL QUESTIONS.**

1.

- a. Using the Clausius – Clapeyron relationship, derive an expression for the pressure on the system ( $P$ ) in terms of the temperature of the system for an evaporation phase equilibrium. Take the heat of vaporization to be  $\Delta H_{vap}$ .
- b. The following phases are known to exist in a system at constant pressure:  
*Cordierite* ( $2MgO \cdot 2Al_2O_3 \cdot 5SiO_2$ )  
*Mullite* ( $3Al_2O_3 \cdot 2SiO_2$ )  
*Forsterite* ( $2MgO \cdot SiO_2$ )  
*Protoenstatite* ( $MgO \cdot SiO_2$ )  
*Periclase* ( $MgO$ )
  - i. What are the components of the system?
  - ii. Could all of the above-listed phases coexist at equilibrium? Explain your answer.
- c. Classify the following systems as monovariant, divariant, or invariant. Explain your answers
  - i. Beta quartz in equilibrium with beta tridymite at the transition temperature.
  - ii. Graphite at room temperature.
  - iii. Ice in equilibrium with its vapor and liquid water.
  - iv. Liquid phase in a binary system
- d. From Figure 1 (Page 2), indicate whether the following statement is true or false.
  - i.  $L$  is denser than  $S_2$ .

- ii.  $S_1$  is denser than  $S_2$  and the transformation from  $S_1 \rightarrow S_2$  is endothermic.
- iii.  $L$  is less dense than  $S_2$
- iv.  $V$  is more dense than  $L$ .

30 Marks

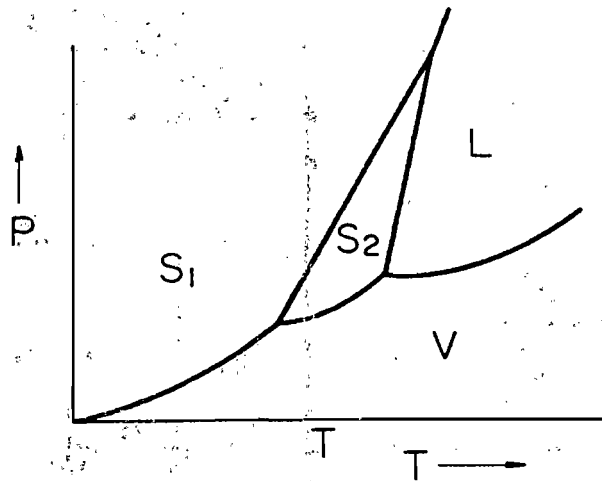
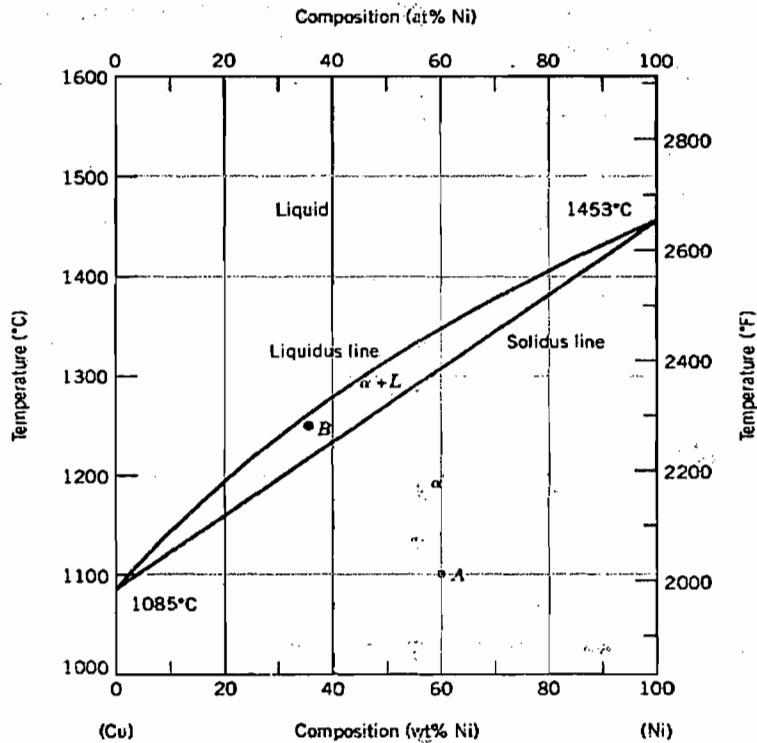
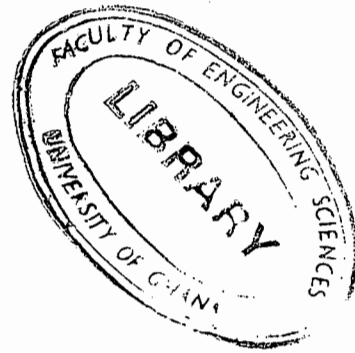


Figure 1

2. Use Figure 2 (Page 3), to answer the following questions.
  - a. What name would you give to describe the binary system in Figure 2?
  - b. Under what conditions is such a system possible?
  - c. What are the melting points of copper and nickel?
  - d. Conduct an isoplethal study of a melt with composition 20 wt% Ni considering only the temperatures at which the equilibrium phase(s) change(s) for your calculations. Present your results in a tabulated format.
  - e. Sketch the microstructure of the system at each of the temperatures indicated in 2(d) above.

25 Marks



**Figure 2**

3. Construct the binary phase diagram which represents the following conditions in the system A-B:
  - i. Component A melts at 1850 °C.
  - ii. Component B melts at 1700 °C.
  - iii. Compound  $A_4B$  melts incongruently at 1500 °C.
  - iv. Compound AB melts congruently at 1600 °C.
  - v. A eutectic is formed between  $A_4B$  and AB at 1400 °C.
  - vi. A eutectic is formed between AB and B at 1450 °C

**15 Marks**

4. Use Figure 4 to answer the following questions. Use and attach the extra print out of this figure where necessary.
  - a. Construct Alkemade lines and indicate slopes of boundary lines.
  - b. What are the two compatibility triangles in the system?
  - c. Write and name the respective invariant reactions at points E and D.
  - d. Make a sketch of the isothermal sections at 600 °C and label.
  - e. For a melt of composition A=20%, B= 15% and C = 65%

- i. What crystalline phase will be first to form upon cooling?
- ii. What is the composition of the final crystals?
- iii. What is the composition of the final liquid to solidify?

30 Marks

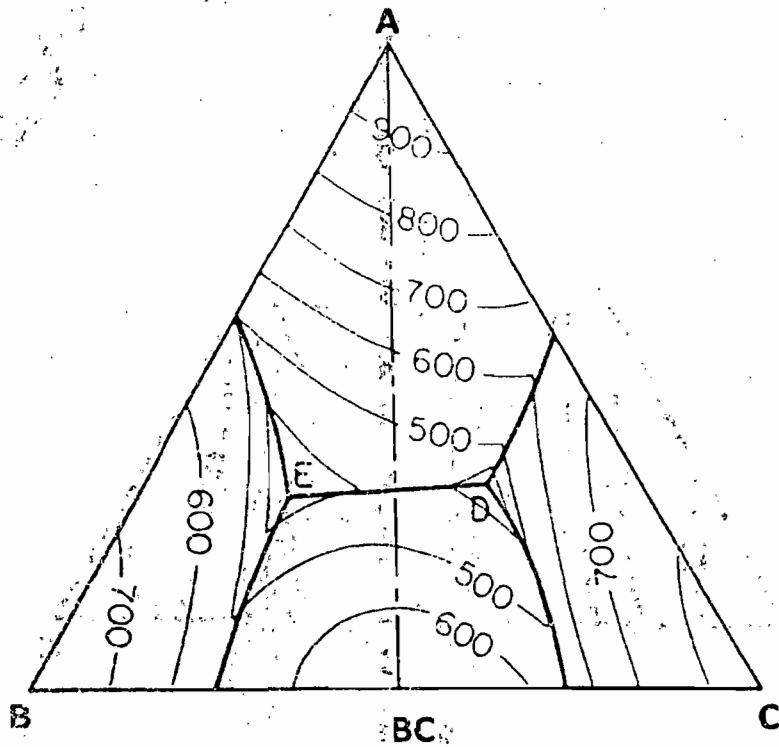


Figure 3

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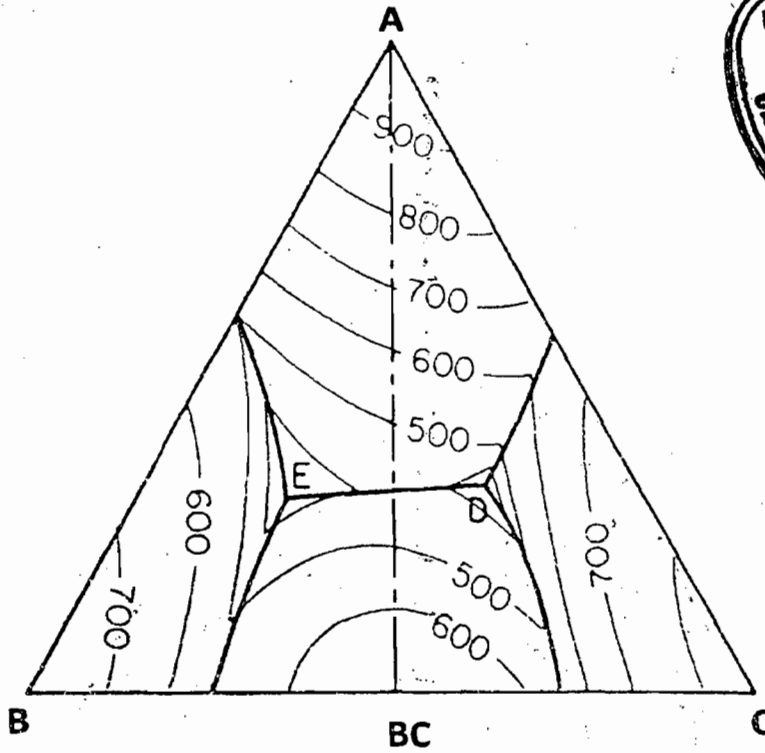


Figure 3

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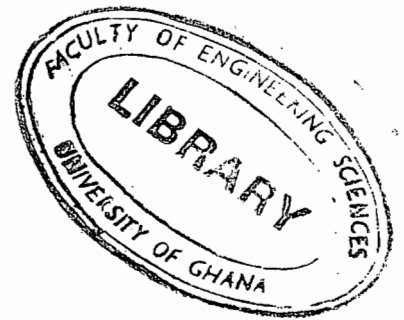
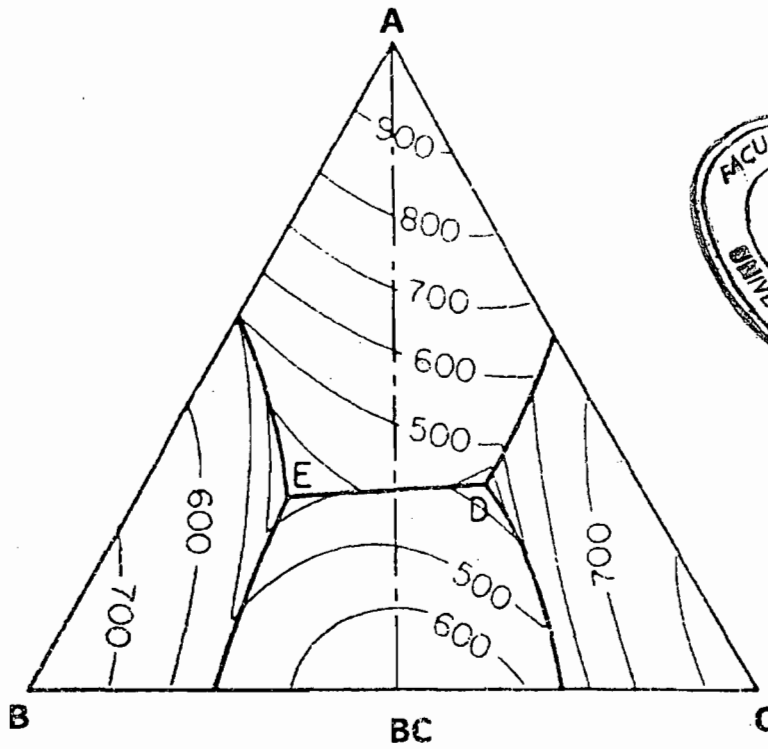


Figure 3