SCHOOL OF ENGINEERING COLLEGE OF BASIC AND APPLIED SCIENCES

FAEN 201: CALCULUS II INTERIM ASSESSMENT II

Answer all questions. Time Duration: 1 hour 20 minutes.

- 1. a. Show that the following limits do not exist i) $\lim_{(x,y)\to(0,0)} \frac{2x^2-y^2}{x^2+2y^2}$

 - ii) $\lim_{(x,y)\to(0,0)} \frac{3xy}{5x^4+2x^4}$
 - b. If $w = (y-2x)^3 \sqrt{y-2x}$, show that

$$w_{xx} - 4w_{yy} = 0.$$

2. a. If $w = f(x^2 + y^2)$, show that

$$y\left(\frac{\partial\omega}{\partial x}\right)-x\left(\frac{\partial\omega}{\partial y}\right)=0.$$

(*Hint*: Let $u = x^2 + y^2$)

b. Find the extrema of the function

$$f(x,y) = x^2 - 6x\cos y + 9; \ 0 \le y \le 2\pi$$

and classify them.

3. a. Find the scalar field, f(x,y) having the gradient

$$\left(\frac{1}{x^2} + \frac{1}{y^2}\right)\mathbf{i} + \left(\frac{1 - 2x}{y^3}\right)\mathbf{j}.$$

b. Use Green's theorem to evaluate

$$\int_C \sqrt{1+x^3} \mathrm{d}x + 2xy \mathrm{d}y$$

where C is the triangle with vertices (0,0),(1,0) and (1,3) oriented counterclockwise.