



UNIVERSITY OF GHANA

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**BACHELOR OF SCIENCE IN ENGINEERING
SECOND SEMESTER EXAMINATIONS: 2014/2015**

CPEN 204: DATA STRUCTURES AND ALGORITHMS (3 Credits)

INSTRUCTION: Answer *ALL* questions from Sections A and B.

TIME ALLOWED: TWO-AND-HALF (2½) HOURS

SECTION A [20 marks]

Answer all questions in this section

Given the following structure definition and declarations in a C programme, **find error(s), if any, in statements A1-A5 and correct them.**

```
struct Utility
{
    char companyName[20];
    int year;
    double quantity;
    double consumption;
}; struct Utility water, electricity;
```

A1. water.quantity=205.2;

A2. water.quantity.consumption=48.3;

A3. electricity.companyName = 'GidCo';

A4. strcpy (water.companyName, "ACQUA");

A5. electricity.year = 2014;

Given these structure definition and declarations, **find error(s), if any, in statements A6-A10, and correct them.**

```
struct Xxx
{
    int aa; double *bb; char *cc[30]
};
struct Yyy
{
    int *dd; double ee;
}; struct Xxx mm, nn; struct Yyy pp, qq;
```

- A6. mm=pp;
 A7. strcpy(nn.cc, "Test");
 A8. Xxx.aa = 15;
 A9. Yyy.ee = 43.8;
 A10. mm=nn;

SECTION B [80 marks]

Answer all questions in this section.

- B1. Figure 1 shows a queue of at most 12 elements implemented using array $Q[1..13]$ with $head[Q] = 7$.

| | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 |
|---|---|---|---|---|---|---|----|---|---|----|----|----|----|
| Q | | | | | | | 60 | 6 | 4 | 50 | 3 | 70 | |

Figure 1

- Illustrate the configuration of the queue after each of the following operations has been performed successively on it: ENQUEUE (Q, 3), ENQUEUE (Q, 1), ENQUEUE (Q, 4), DEQUEUE (Q), ENQUEUE (Q, 8), and DEQUEUE (Q).
[6 marks]
- Find the value of $tail[Q]$ after each of the operations in B1.(a) has been performed.
[3 marks]
- Using diagrams, show how a **doubly linked list** L can be used to represent the dynamic set $\{1, 4, 9, 16\}$.
[5 marks]
- Show the configuration of L after performing the following operation:
LIST-INSERT (L, x), where $key[x] = 25$.
[2 marks]
- Using diagrams describe a *sentinel* and show how this sentinel can turn the *doubly linked list* L in question B1.c) into a *circular, doubly linked list* with a *sentinel*.
[4 marks]

B2.

- Explain the concept of *computational complexity* of algorithms. [3 marks]
- Show how *big-O* notation can be used to estimate the following: [12 marks]
 - A constant function
 - A polynomial $f(x) = a_n x^n + a_{n-1} x^{n-1} + \dots + a_1 x + a_0$,
where $a_0, a_1, \dots, a_{n-1}, a_n$ are real numbers.
 - The summation of the first N positive integers.

- iv. The factorial of a positive integer N .
 - v. The logarithm of a factorial of a positive integer N .
 - vi. The logarithm of a positive integer N .
- c) Using your estimation in B2. b), derive a *big-O* estimate for $f(n)=3n\log(n!)+(n^2+3)\log(n!)$. [5 marks]

B3.

- a) Write a C++ programme to implement a *recursive function* *recurFact*. *recurFact* takes as a parameter a positive integer N and returns the *factorial of the positive integer N ($N!$)*. State the *base case* and the *general case* for *recurFact*. [7 marks]
- b) Write another C++ programme to implement function *iteraFact*. *iteraFact* takes as a parameter a positive integer N and uses *iteration* to calculate and returns the factorial of the positive integer N . [7 marks]
- c) Analyse the *computational complexity* of each programme in questions B3.a) and B3.b). Which programme is efficient and why? [6 marks]

B4.

- a) Given the following list $A = [1,3,5,7,11,13,17,19,23, 31,33,37]$, systematically show how each of the following algorithms will locate the element 19 in the list:
 - i. Linear search [5 marks]
 - ii. Binary search [5 marks]
- b) Briefly describe the *divide-and-conquer* strategy as a problem solving technique. [4 marks]
- c) Briefly explain the difference between *quicksort* and *merge sort* algorithms. [6 marks]