non-sparse with scaled  $\beta$  vs. sparse with constant  $\beta$ 

