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Modern Digital Synchronization Techniques for Reliable Communication

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Abstract—A brief description about the de implementation of Modern Digital Synchronizat niques for reliable communication.

1. TIME OFFSET: GARDNER TED

Let the *m*th sample in the *r*th received time slot be

$$Y_k(m) = X_k + V_k(m), \quad k = 1, ..., N, m = 1,$$

where X_k is the transmitted symbol in the kth time slot and $V_k(m) \sim \mathcal{N}(0, \sigma^2)$. The decision variable for the kth symbol is [2]

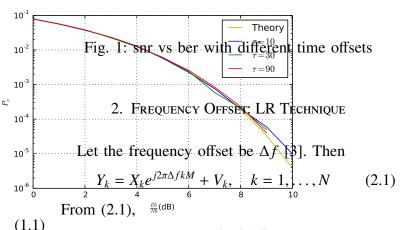
$$U_k = \frac{1}{N} \sum_{i=1}^{N} Y_{k-i} \left(\frac{M}{2} \right) (Y_{k-i+1}(M) - Y_{k-i}(M)) \quad (1.2)$$

A. Plots

The codes for generating the plots are available at

Fig. 1 shows the variation of the bit error rate respect to the snr with different timing offsets. Δf when the SNR = 10 dB.

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 $Y_k X_k^* = |X_k|^2 e^{j2\pi\Delta f k M} + X_k^* V_k$ (2.2)

$$\implies r_k = e^{j2\pi\Delta fkM} + \bar{V}_k \tag{2.3}$$

where

$$r_k = Y_k X_k^*, \bar{V}_k = X_k^* V_k, |X_k|^2 = 1$$
 (2.4)

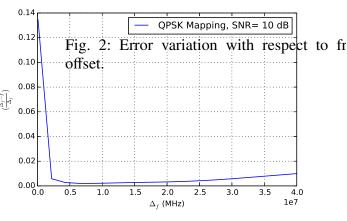
The autocorrelation can be calculated as

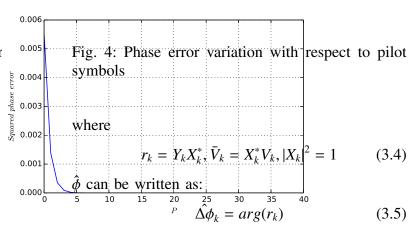
$$R(k) \stackrel{\Delta}{=} \frac{1}{N-k} \sum_{i=k+1}^{N} r_i r_{i-k}^*, 1 \le k \le N-1$$
 (2.5)

Where N is the length of the received signal. For large centre frequency, the following yields a good approximation for frequency offset upto 40 MHz.

$$\Delta \hat{f} \approx \frac{1}{2\pi M} \frac{\sum_{k=1}^{P} \text{Im}(R(k))}{\sum_{k=1}^{P} k \text{Re}(R(k))}, \quad P\Delta f M << 1 \quad (2.6)$$

where P is the number of pilot symbols.



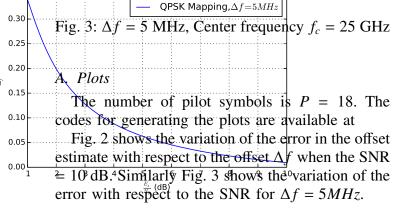


This equation gives the final estimation of phase

$$\hat{\Delta\phi}_{f}^{(p)}(l) = \hat{\Delta\phi}_{f}^{(p)}(l-1) + \alpha SAW[\hat{\Delta\phi}^{(p)}(l) - \hat{\Delta\phi}_{f}^{(p)}(l-1)]$$
(3.6)

$$SAW[\phi] = \left[\phi\right]_{-\pi}^{\pi} \tag{3.7}$$

Where SAW is sawtooth non-linearity and $\alpha \leq 1$. l counts the number of pilot-based estimates. $\hat{\Delta \phi}_f^{(p)}(l)$ is the final unwrapped pilot estimate.



3. Phase Offset: Feed Forward Maximum Likelihood (FF-ML)technique

Let the phase offset be $\Delta \phi$ [4]. Then

$$Y_k = X_k e^{j\Delta\phi} + V_k, \quad k = 1, ..., N$$
 (3.1)

From (3.1),

0.35

$$Y_k X_k^* = |X_k|^2 e^{j\Delta\phi} + X_k^* V_k \tag{3.2}$$

$$\implies r_k = e^{j\Delta\phi} + \bar{V}_k \tag{3.3}$$

A. Plots

The codes for generating the plots are available at

Fig. 4 shows the variation of the phase error in the offset estimate with respect to the pilot symbols. Δf when the SNR = 10 dB. Similarly Fig. 5 shows the variation of the error with respect to the SNR for pilot symbols P = 18.

References

- U. Mengali and A. N. D'Andrea: synchronization Techniques for Digital Receivers, New York: Plenum, 1997.
- [2] F. M. Gardner: A BPSK/QPSK timing-error detector for sampled receivers, IEEE TRANSACTIONS ON COMMUNICA-TIONS, VOL.COM-34,NO.5,MAY 1986

