#### 1

# Modern Digital Synchronization Techniques for Reliable Communication

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Abstract—A brief description about the de implementation of Modern Digital Synchronizat niques for reliable communication.

#### 1. TIME OFFSET: GARDNER TED

Let the *m*th sample in the *r*th received time slot be

$$Y_k(m) = X_k + V_k(m), \quad k = 1, \dots, N, m = 1, \dots, I_{r_k}.$$
(1.1)

where  $X_k$  is the transmitted symbol in the kth time slot and  $V_k(m) \sim \mathcal{N}(0, \sigma^2)$ . The decision variable for the kth symbol is [2]

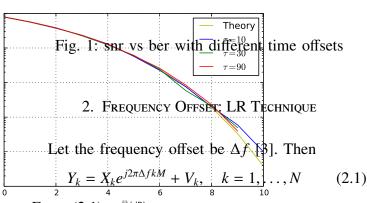
$$U_{k} = Y_{k-1} \left(\frac{M}{2}\right) \left[Y_{k}(M) - Y_{k-1}(M)\right]$$
 (1.2)

#### A. Plots

The codes for generating the plots are available at

Fig. 1 shows the variation of the bit error rate respect to the snr with different timing offsets.  $\Delta f$  when the SNR = 10 dB.

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From (2.1),  $\frac{Eb}{N0}$  (dB)

$$Y_k X_k^* = |X_k|^2 e^{j2\pi\Delta f k M} + X_k^* V_k$$
 (2.2)

$$\implies r_k = e^{j2\pi\Delta fkM} + \bar{V}_k \tag{2.3}$$

where

$$r_k = Y_k X_k^*, \bar{V}_k = X_k^* V_k, |X_k|^2 = 1$$
 (2.4)

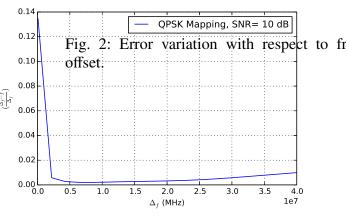
The autocorrelation can be calculated as

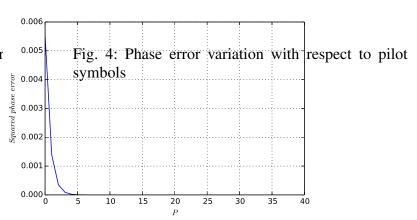
$$R(k) \stackrel{\Delta}{=} \frac{1}{N-k} \sum_{i=k+1}^{N} r_i r_{i-k}^*, 1 \le k \le N-1$$
 (2.5)

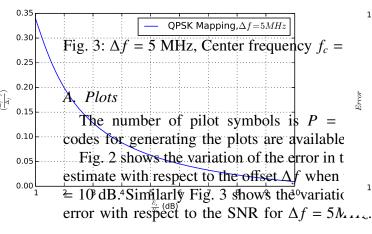
Where N is the length of the received signal. For large centre frequency, the following yields a good approximation for frequency offset upto 40 MHz.

$$\Delta \hat{f} \approx \frac{1}{2\pi M} \frac{\sum_{k=1}^{P} \operatorname{Im}(R(k))}{\sum_{k=1}^{P} k \operatorname{Re}(R(k))}, \quad P\Delta f M << 1 \quad (2.6)$$

where P is the number of pilot symbols.







# 3. Phase Offset: Feed Forward Maximum Likelihood (FF-ML)technique

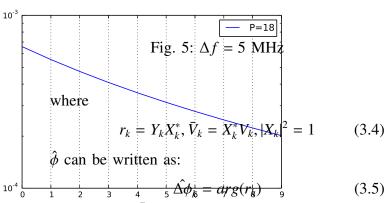
Let the phase offset be  $\Delta \phi$  [4]. Then

$$Y_k = X_k e^{j\Delta\phi} + V_k, \quad k = 1, \dots, N$$

From (3.1),

$$Y_k X_k^* = |X_k|^2 e^{j\Delta\phi} + X_k^* V_k$$

$$\implies r_k = e^{j\Delta\phi} + \bar{V}_k$$



This equation gives the final estimation of phase

$$\hat{\Delta\phi}_f^{(p)}(l) = \hat{\Delta\phi}_f^{(p)}(l-1) + \alpha SAW[\hat{\Delta\phi}_f^{(p)}(l) - \hat{\Delta\phi}_f^{(p)}(l-1)]$$
(3.6)

Where SAW is a saw tooth non-linearity and  $\alpha \le 1$ 

## A. Plots

(3.1)

The codes for generating the plots are available at

(3.2) Fig. 4 shows the variation of the phase error in the offset estimate with respect to the pilot symbols.

 $\Delta f$  when the SNR = 10 dB. Similarly Fig. 5 shows the variation of the error with respect to the SNR for pilot symbols P = 18.

### REFERENCES

- [1] U. Mengali and A. N. D'Andrea:'synchronization Techniques for Digital Receivers,' New York: Plenum, 1997.
- [2] F. M. Gardner: A BPSK/QPSK timing-error detector for sampled receivers, IEEE TRANSACTIONS ON COMMUNICA-TIONS, VOL.COM-34,NO.5,MAY 1986
- [3] M. Luise and R. Reggiannini: Carrier frequency recovery in all-digital modems for burst mode transmissions, IEEE Trans. Commun., vol. 43, no. 2/3/4, pp. 1169-1178, Feb/Mar/Apr 1995
- [4] E. Casini, R. De Gaudenzi, and A. Ginesi: 'DVB-S2 modem algorithms design and performance over typical satellite channels,' International Journal of Satellite Communications and Networking 2004, vol. 22(3), pp. 281-318, 2004.