

CSC 261/461

Database Systems

Eustrat Zhupa

November 7, 2018



UNIVERSITY of
ROCHESTER

Relational Algebra

CARTESIAN PRODUCT Operation

- ▶ This operation is used to combine tuples from two relations.
- ▶ Denoted by $R(A1, A2, \dots, An) \times S(B1, B2, \dots, Bm)$
- ▶ Result is a relation Q with $n + m$ attributes:
 $Q(A1, A2, \dots, An, B1, B2, \dots, Bm)$
- ▶ The resulting relation state has one tuple for each combination of tuples.
- ▶ The two operands do NOT have to be "type compatible"

[1]



UNIVERSITY of
ROCHESTER

Example

Example

EMPNames

Fname	Lname	Ssn
Alicia	Zelaya	999887777
Jennifer	Wallace	987654321
Joyce	English	453453453

DEPENDENT

<u>Essn</u>	<u>Dependent_name</u>	Sex	Bdate	Relationship
333445555	Alice	F	1986-04-05	Daughter
333445555	Theodore	M	1983-10-25	Son
333445555	Joy	F	1958-05-03	Spouse
987654321	Abner	M	1942-02-28	Spouse
123456789	Michael	M	1988-01-04	Son
123456789	Alice	F	1988-12-30	Daughter
123456789	Elizabeth	F	1967-05-05	Spouse



Example

Example

EMP_DEPENDENTS

Fname	Lname	Ssn	Essn	Dependent_name	Sex	Bdate	...
Alicia	Zelaya	999887777	333445555	Alice	F	1986-04-05	...
Alicia	Zelaya	999887777	333445555	Theodore	M	1983-10-25	...
Alicia	Zelaya	999887777	333445555	Joy	F	1958-05-03	...
Alicia	Zelaya	999887777	987654321	Abner	M	1942-02-28	...
Alicia	Zelaya	999887777	123456789	Michael	M	1988-01-04	...
Alicia	Zelaya	999887777	123456789	Alice	F	1988-12-30	...
Alicia	Zelaya	999887777	123456789	Elizabeth	F	1967-05-05	...
Jennifer	Wallace	987654321	333445555	Alice	F	1986-04-05	...
Jennifer	Wallace	987654321	333445555	Theodore	M	1983-10-25	...
Jennifer	Wallace	987654321	333445555	Joy	F	1958-05-03	...
Jennifer	Wallace	987654321	987654321	Abner	M	1942-02-28	...
Jennifer	Wallace	987654321	123456789	Michael	M	1988-01-04	...
Jennifer	Wallace	987654321	123456789	Alice	F	1988-12-30	...
Jennifer	Wallace	987654321	123456789	Elizabeth	F	1967-05-05	...
Joyce	English	453453453	333445555	Alice	F	1986-04-05	...
Joyce	English	453453453	333445555	Theodore	M	1983-10-25	...
Joyce	English	453453453	333445555	Joy	F	1958-05-03	...
Joyce	English	453453453	987654321	Abner	M	1942-02-28	...
Joyce	English	453453453	123456789	Michael	M	1988-01-04	...
Joyce	English	453453453	123456789	Alice	F	1988-12-30	...
Joyce	English	453453453	123456789	Elizabeth	F	1967-05-05	...

Operations of RA

JOIN

- ▶ Denoted by \bowtie
- ▶ The sequence of CROSS PRODUCT followed by SELECT is used quite to identify and select related tuples from two relations
- ▶ A special operation, called JOIN combines them into a *single* operation
- ▶ very important because it allows us combine data from various relations
- ▶ The general form of a join operation is:

$$R \bowtie_{\langle \text{joincondition} \rangle} S$$



Operations of RA

JOIN

- ▶ Consider the following JOIN:
$$R(A_1, A_2, \dots, A_n) \bowtie_{R.A_i=S.B_j} S(B_1, B_2, \dots, B_m)$$
- ▶ Result is a relation Q with $n + m$ attributes: $Q(A_1, A_2, \dots, A_n, B_1, B_2, \dots, B_m)$, in that order.
- ▶ The result has one tuple for each combination of tuples - one from R and one from S, but only if they satisfy the join condition $r[A_i] = s[B_j]$

[2]

Example

Example

EMPLOYEE

Fname	Minit	Lname	Ssn	Bdate	Address	Sex	Salary	Super_ssn	Dno
John	B	Smith	123456789	1965-01-09	731 Fondren, Houston, TX	M	30000	333445555	5
Franklin	T	Wong	333445555	1955-12-08	638 Voss, Houston, TX	M	40000	888665555	5
Alicia	J	Zelaya	999887777	1968-01-19	3321 Castle, Spring, TX	F	25000	987654321	4
Jennifer	S	Wallace	987654321	1941-06-20	291 Berry, Bellaire, TX	F	43000	888665555	4
Ramesh	K	Narayan	666884444	1962-09-15	975 Fire Oak, Humble, TX	M	38000	333445555	5
Joyce	A	English	453453453	1972-07-31	5631 Rice, Houston, TX	F	25000	333445555	5
Ahmad	V	Jabbar	987987987	1969-03-29	980 Dallas, Houston, TX	M	25000	987654321	4
James	E	Borg	888665555	1937-11-10	450 Stone, Houston, TX	M	55000	NULL	1

DEPARTMENT

Dname	Dnumber	Mgr_ssn	Mgr_start_date
Research	5	333445555	1988-05-22
Administration	4	987654321	1995-01-01
Headquarters	1	888665555	1981-06-19

DEPT_MGR

Dname	Dnumber	Mgr_ssn	...	Fname	Minit	Lname	Ssn	...
Research	5	333445555	...	Franklin	T	Wong	333445555	...
Administration	4	987654321	...	Jennifer	S	Wallace	987654321	...
Headquarters	1	888665555	...	James	E	Borg	888665555	...

Operations of RA

THETA JOIN

- ▶ The general case of JOIN operation is called a Theta-join:

$$R \bowtie_{\text{theta}} S$$

- ▶ The join condition is called **theta**
- ▶ Theta can be any boolean expression on attributes of R and S:

Example:

$$R.A_i < S.B_j \text{ AND } (R.A_k = S.B_i \text{ OR } R.A_p < S.B_q)$$



Example

EQUIJOIN

- ▶ Join conditions with equality comparisons only
- ▶ In the result we always have one or more pairs of attributes that have identical values in every tuple.

$DEPT_MGR \leftarrow DEPARTMENT \bowtie_{Mgr_ssn=Ssn} EMPLOYEE$

DEPT_MGR

Dname	Dnumber	Mgr_ssn	...	Fname	Minit	Lname	Ssn	...
Research	5	333445555	...	Franklin	T	Wong	333445555	...
Administration	4	987654321	...	Jennifer	S	Wallace	987654321	...
Headquarters	1	888665555	...	James	E	Borg	888665555	...



Operations of RA

NATURAL JOIN

- ▶ denoted by *
- ▶ created to get rid of the second attribute in an EQUIJOIN condition.
 - ▶ one of each pair of attributes with identical values is redundant
- ▶ each pair of corresponding join attributes have the same name in both relations
 - ▶ If not, a renaming operation is applied first.

[3]



UNIVERSITY of
ROCHESTER

Example

Example

PROJECT

Pname	<u>Pnumber</u>	Plocation	Dnum
ProductX	1	Bellaire	5
ProductY	2	Sugarland	5
ProductZ	3	Houston	5
Computerization	10	Stafford	4
Reorganization	20	Houston	1
Newbenefits	30	Stafford	4

DEPARTMENT

Dname	<u>Dnumber</u>	Mgr_ssn	Mgr_start_date
Research	5	333445555	1988-05-22
Administration	4	987654321	1995-01-01
Headquarters	1	888665555	1981-06-19

$PROJ_DEPT \leftarrow PROJECT * \rho_{(Dname, Dnum, Mgr_ssn, Mgr_start_date)}(DEPARTMENT)$

(a)

PROJ_DEPT

Pname	<u>Pnumber</u>	Plocation	Dnum	Dname	Mgr_ssn	Mgr_start_date
ProductX	1	Bellaire	5	Research	333445555	1988-05-22
ProductY	2	Sugarland	5	Research	333445555	1988-05-22
ProductZ	3	Houston	5	Research	333445555	1988-05-22
Computerization	10	Stafford	4	Administration	987654321	1995-01-01
Reorganization	20	Houston	1	Headquarters	888665555	1981-06-19
Newbenefits	30	Stafford	4	Administration	987654321	1995-01-01

Example

Example

DEPARTMENT

Dname	Dnumber	Mgr_ssn	Mgr_start_date
Research	5	333445555	1988-05-22
Administration	4	987654321	1995-01-01
Headquarters	1	888665555	1981-06-19

DEPT_LOCATIONS

Dnumber	Dlocation
1	Houston
4	Stafford
5	Bellaire
5	Sugarland
5	Houston

DEPT_LOCS ← *DEPARTMENT* * *DEPT_LOCATIONS*?

(b)

DEPT_LOCS

Dname	Dnumber	Mgr_ssn	Mgr_start_date	Location
Headquarters	1	888665555	1981-06-19	Houston
Administration	4	987654321	1995-01-01	Stafford
Research	5	333445555	1988-05-22	Bellaire
Research	5	333445555	1988-05-22	Sugarland
Research	5	333445555	1988-05-22	Houston



UNIVERSITY OF
ROCHESTER

Operations of RA

OUTER JOIN

- ▶ LEFT OUTER JOIN $R \bowtie\!\!\!\lrcorner S$: keeps every tuple in R; if no matching tuple is found in S, then the attributes of S are filled with NULL.
- ▶ RIGHT OUTER JOIN $R \bowtie\!\!\!\rceil S$: keeps every tuple in S in the result, fill in with NULLs in R.
- ▶ FULL OUTER JOIN $R \bowtie\!\!\!\bowtie S$: keeps all tuples in both relations: when no matching tuples are found, fills with NULL.

[4]



UNIVERSITY of
ROCHESTER

Example

Example

EMPLOYEE

Fname	Minit	Lname	<u>Ssn</u>	Bdate	Address	Sex	Salary	Super_ssn	Dno
John	B	Smith	123456789	1965-01-09	731 Fondren, Houston, TX	M	30000	333445555	5
Franklin	T	Wong	333445555	1955-12-08	638 Voss, Houston, TX	M	40000	888665555	5
Alicia	J	Zelaya	999887777	1968-01-19	3321 Castle, Spring, TX	F	25000	987654321	4
Jennifer	S	Wallace	987654321	1941-06-20	291 Berry, Bellaire, TX	F	43000	888665555	4
Ramesh	K	Narayan	666884444	1962-09-15	975 Fire Oak, Humble, TX	M	38000	333445555	5
Joyce	A	English	453453453	1972-07-31	5631 Rice, Houston, TX	F	25000	333445555	5
Ahmad	V	Jabbar	987987987	1969-03-29	980 Dallas, Houston, TX	M	25000	987654321	4
James	E	Borg	888665555	1937-11-10	450 Stone, Houston, TX	M	55000	NULL	1

DEPARTMENT

Dname	<u>Dnumber</u>	Mgr_ssn	Mgr_start_date
Research	5	333445555	1988-05-22
Administration	4	987654321	1995-01-01
Headquarters	1	888665555	1981-06-19

RESULT

Fname	Minit	Lname	Dname
John	B	Smith	NULL
Franklin	T	Wong	Research
Alicia	J	Zelaya	NULL
Jennifer	S	Wallace	Administration
Ramesh	K	Narayan	NULL
Joyce	A	English	NULL
Ahmad	V	Jabbar	NULL
James	E	Borg	Headquarters

Division

Division

The division operator denoted as $R \div S$.

- ▶ If $R(Z) \div S(X)$, where $X \subseteq Z$, and $Y = Z - X$.
- ▶ Result is a relation $T(Y)$ including a tuple t if:
 - ▶ t_R appears in R with $t_R[Y] = t$
 - ▶ $t_R[X] = t_S$ for every tuple t_S in S .
- ▶ Otherwise, For a tuple t to appear in the result, values in t must be in R combined with all tuples in S .



Example

SSN_PNOS

Essn	Pno
123456789	1
123456789	2
666884444	3
453453453	1
453453453	2
333445555	2
333445555	3
333445555	10
333445555	20
999887777	30
999887777	10
987987987	10
987987987	30
987654321	30
987654321	20
888665555	20

SMITH_PNOS

Pno
1
2

SSNS

Ssn
123456789
453453453

R

A	B
a1	b1
a2	b1
a3	b1
a4	b1
a1	b2
a3	b2
a2	b3
a3	b3
a4	b3
a1	b4
a2	b4
a3	b4

S

A
a1
a2
a3

T

B
b1
b4



RA Operations

Generalized Projection

The generalized projection operation:

$$\pi_{F_1, F_2, \dots, F_n}(R)$$

- F_1, F_2, \dots, F_n are functions over the attributes of R and may involve arithmetic operations and constant values.

$$\pi_{Ssn, Salary - Deduction, 2000 * Years_service, 0.25 * Salary}(EMPLOYEE)$$



RA Operations

Aggregate Functions

We can define an AGGREGATE FUNCTION operation, using the symbol \mathcal{F} :

$$\langle \text{grouping_attributes} \rangle \mathcal{F} \langle \text{function_list} \rangle (R)$$

- ▶ $\langle \text{grouping_attributes} \rangle$ is a list of attributes
- ▶ $\langle \text{function_list} \rangle$ is a list of $(\langle \text{function} \rangle, \langle \text{attribute} \rangle)$ pairs.
- ▶ $\langle \text{function} \rangle$ is one of SUM , AVERAGE , MAXIMUM , MINIMUM , COUNT.



Example

R

(a)

Dno	No_of_employees	Average_sal
5	4	33250
4	3	31000
1	1	55000

(b)

Dno	Count_ssn	Average_salary
5	4	33250
4	3	31000
1	1	55000

(c)

Count_ssn	Average_salary
8	35125

Figure 8.10

The aggregate function operation.

- a. $\text{PR}(\text{Dno}, \text{No_of_employees}, \text{Average_sal})(\text{Dno} \bowtie \text{COUNT Ssn}, \text{AVERAGE Salary}(\text{EMPLOYEE}))$.
- b. $\text{Dno} \bowtie \text{COUNT Ssn}, \text{AVERAGE Salary}(\text{EMPLOYEE})$.
- c. $\bowtie \text{COUNT Ssn}, \text{AVERAGE Salary}(\text{EMPLOYEE})$.





UNIVERSITY of
ROCHESTER

