

# CSC 261/461

## Database Systems

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# Relational Algebra

## CARTESIAN PRODUCT Operation

- ▶ This operation is used to combine tuples from two relations.
- ▶ Denoted by  $R(A_1, A_2, \dots, A_n) \times S(B_1, B_2, \dots, B_m)$
- ▶ Result is a relation Q with  $n + m$  attributes:  
$$Q(A_1, A_2, \dots, A_n, B_1, B_2, \dots, B_m)$$
- ▶ The resulting relation state has one tuple for each combination of tuples - one from R and one from S.
- ▶ The two operands do NOT have to be "type compatible"



# Example

## Example

**EMPNames**

Fname	Lname	Ssn
Alicia	Zelaya	999887777
Jennifer	Wallace	987654321
Joyce	English	453453453

**DEPENDENT**

<u>Essn</u>	<u>Dependent_name</u>	Sex	Bdate	Relationship
333445555	Alice	F	1986-04-05	Daughter
333445555	Theodore	M	1983-10-25	Son
333445555	Joy	F	1958-05-03	Spouse
987654321	Abner	M	1942-02-28	Spouse
123456789	Michael	M	1988-01-04	Son
123456789	Alice	F	1988-12-30	Daughter
123456789	Elizabeth	F	1967-05-05	Spouse



# Example

## Example

**EMP\_DEPENDENTS**

Fname	Lname	Ssn	Essn	Dependent_name	Sex	Bdate	...
Alicia	Zelaya	999887777	333445555	Alice	F	1986-04-05	...
Alicia	Zelaya	999887777	333445555	Theodore	M	1983-10-25	...
Alicia	Zelaya	999887777	333445555	Joy	F	1958-05-03	...
Alicia	Zelaya	999887777	987654321	Abner	M	1942-02-28	...
Alicia	Zelaya	999887777	123456789	Michael	M	1988-01-04	...
Alicia	Zelaya	999887777	123456789	Alice	F	1988-12-30	...
Alicia	Zelaya	999887777	123456789	Elizabeth	F	1967-05-05	...
Jennifer	Wallace	987654321	333445555	Alice	F	1986-04-05	...
Jennifer	Wallace	987654321	333445555	Theodore	M	1983-10-25	...
Jennifer	Wallace	987654321	333445555	Joy	F	1958-05-03	...
Jennifer	Wallace	987654321	987654321	Abner	M	1942-02-28	...
Jennifer	Wallace	987654321	123456789	Michael	M	1988-01-04	...
Jennifer	Wallace	987654321	123456789	Alice	F	1988-12-30	...
Jennifer	Wallace	987654321	123456789	Elizabeth	F	1967-05-05	...
Joyce	English	453453453	333445555	Alice	F	1986-04-05	...
Joyce	English	453453453	333445555	Theodore	M	1983-10-25	...
Joyce	English	453453453	333445555	Joy	F	1958-05-03	...
Joyce	English	453453453	987654321	Abner	M	1942-02-28	...
Joyce	English	453453453	123456789	Michael	M	1988-01-04	...
Joyce	English	453453453	123456789	Alice	F	1988-12-30	...
Joyce	English	453453453	123456789	Elizabeth	F	1967-05-05	...

# Operations of RA

## JOIN

- ▶ Denoted by  $\bowtie$
- ▶ The sequence of CROSS PRODUCT followed by SELECT is used quite to identify and select related tuples from two relations
- ▶ A special operation, called JOIN combines them into a *single* operation
- ▶ very important because it allows us combine data from various relations
- ▶ The general form of a join operation is:

$$R \bowtie_{\langle \text{joincondition} \rangle} S$$



# Operations of RA

## JOIN

- ▶ Consider the following JOIN:  
 $R(A_1, A_2, \dots, A_n) \bowtie_{R.A_i=S.B_j} S(B_1, B_2, \dots, B_m)$
- ▶ Result is a relation Q with  $n + m$  attributes:  $Q(A_1, A_2, \dots, A_n, B_1, B_2, \dots, B_m)$ , in that order.
- ▶ The result has one tuple for each combination of tuples - one from R and one from S, but only if they satisfy the join condition  $r[A_i] = s[B_j]$



# Example

## Example

### EMPLOYEE

Fname	Minit	Lname	<u>Ssn</u>	Bdate	Address	Sex	Salary	Super_ssn	Dno
John	B	Smith	123456789	1965-01-09	731 Fondren, Houston, TX	M	30000	333445555	5
Franklin	T	Wong	333445555	1955-12-08	638 Voss, Houston, TX	M	40000	888665555	5
Alicia	J	Zelaya	999887777	1968-01-19	3321 Castle, Spring, TX	F	25000	987654321	4
Jennifer	S	Wallace	987654321	1941-06-20	291 Berry, Bellaire, TX	F	43000	888665555	4
Ramesh	K	Narayan	666884444	1962-09-15	975 Fire Oak, Humble, TX	M	38000	333445555	5
Joyce	A	English	453453453	1972-07-31	5631 Rice, Houston, TX	F	25000	333445555	5
Ahmad	V	Jabbar	987987987	1969-03-29	980 Dallas, Houston, TX	M	25000	987654321	4
James	E	Borg	888665555	1937-11-10	450 Stone, Houston, TX	M	55000	NULL	1

### DEPARTMENT

Dname	<u>Dnumber</u>	Mgr_ssn	Mgr_start_date
Research	5	333445555	1988-05-22
Administration	4	987654321	1995-01-01
Headquarters	1	888665555	1981-06-19

### DEPT\_MGR

Dname	Dnumber	Mgr_ssn	...	Fname	Minit	Lname	Ssn	...
Research	5	333445555	...	Franklin	T	Wong	333445555	...
Administration	4	987654321	...	Jennifer	S	Wallace	987654321	...
Headquarters	1	888665555	...	James	E	Borg	888665555	...

Figure 6.6

# Operations of RA

## THETA JOIN

- ▶ The general case of JOIN operation is called a Theta-join:

$$R \bowtie_{\theta} S$$

- ▶ The join condition is called **theta**
- ▶ Theta can be any boolean expression on attributes of R and S:

Example:

$$R.A_i < S.B_j \text{ AND } (R.A_k = S.B_i \text{ OR } R.A_p < S.B_q)$$





# Example

## EQUIJOIN

- ▶ join conditions with equality comparisons only
- ▶ In the result we always have one or more pairs of attributes that have identical values in every tuple.



# Operations of RA

## NATURAL JOIN

- ▶ denoted by \*
- ▶ created to get rid of the second attribute in an EQUIJOIN condition.
  - ▶ one of each pair of attributes with identical values is redundant
- ▶ each pair of corresponding join attributes have the same name in both relations
  - ▶ If not, a renaming operation is applied first.



# Example

## Example

### PROJECT

Pname	<u>Pnumber</u>	Plocation	Dnum
ProductX	1	Bellaire	5
ProductY	2	Sugarland	5
ProductZ	3	Houston	5
Computerization	10	Stafford	4
Reorganization	20	Houston	1
Newbenefits	30	Stafford	4

### DEPARTMENT

Dname	<u>Dnumber</u>	Mgr_ssn	Mgr_start_date
Research	5	333445555	1988-05-22
Administration	4	987654321	1995-01-01
Headquarters	1	888665555	1981-06-19

(a)

### PROJ\_DEPT

Pname	<u>Pnumber</u>	Plocation	Dnum	Dname	Mgr_ssn	Mgr_start_date
ProductX	1	Bellaire	5	Research	333445555	1988-05-22
ProductY	2	Sugarland	5	Research	333445555	1988-05-22
ProductZ	3	Houston	5	Research	333445555	1988-05-22
Computerization	10	Stafford	4	Administration	987654321	1995-01-01
Reorganization	20	Houston	1	Headquarters	888665555	1981-06-19
Newbenefits	30	Stafford	4	Administration	987654321	1995-01-01



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# Example

## Example

**DEPARTMENT**

Dname	Dnumber	Mgr_ssn	Mgr_start_date
Research	5	333445555	1988-05-22
Administration	4	987654321	1995-01-01
Headquarters	1	888665555	1981-06-19

**DEPT\_LOCATIONS**

Dnumber	Dlocation
1	Houston
4	Stafford
5	Bellaire
5	Sugarland
5	Houston

(b)

**DEPT\_LOCS**

Dname	Dnumber	Mgr_ssn	Mgr_start_date	Location
Headquarters	1	888665555	1981-06-19	Houston
Administration	4	987654321	1995-01-01	Stafford
Research	5	333445555	1988-05-22	Bellaire
Research	5	333445555	1988-05-22	Sugarland
Research	5	333445555	1988-05-22	Houston



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# Operations of RA

## OUTER JOIN

- ▶ LEFT OUTER JOIN  $R \bowtie_{\text{L}} S$ : keeps every tuple in  $R$ ; if no matching tuple is found in  $S$ , then the attributes of  $S$  are filled with NULL.
- ▶ RIGHT OUTER JOIN  $R \bowtie_{\text{R}} S$ : keeps every tuple in  $S$  in the result.
- ▶ FULL OUTER JOIN  $R \bowtie_{\text{F}} S$ : keeps all tuples in both relations: when no matching tuples are found, fills with NULL.



# Example

## Example

### EMPLOYEE

Fname	Minit	Lname	<u>Ssn</u>	Bdate	Address	Sex	Salary	Super_ssn	Dno
John	B	Smith	123456789	1965-01-09	731 Fondren, Houston, TX	M	30000	333445555	5
Franklin	T	Wong	333445555	1955-12-08	638 Voss, Houston, TX	M	40000	888665555	5
Alicia	J	Zelaya	999887777	1968-01-19	3321 Castle, Spring, TX	F	25000	987654321	4
Jennifer	S	Wallace	987654321	1941-06-20	291 Berry, Bellaire, TX	F	43000	888665555	4
Ramesh	K	Narayan	666884444	1962-09-15	975 Fire Oak, Humble, TX	M	38000	333445555	5
Joyce	A	English	453453453	1972-07-31	5631 Rice, Houston, TX	F	25000	333445555	5
Ahmad	V	Jabbar	987987987	1969-03-29	980 Dallas, Houston, TX	M	25000	987654321	4
James	E	Borg	888665555	1937-11-10	450 Stone, Houston, TX	M	55000	NULL	1

### DEPARTMENT

Dname	<u>Dnumber</u>	Mgr_ssn	Mgr_start_date
Research	5	333445555	1988-05-22
Administration	4	987654321	1995-01-01
Headquarters	1	888665555	1981-06-19

### RESULT

Fname	Minit	Lname	Dname
John	B	Smith	NULL
Franklin	T	Wong	Research
Alicia	J	Zelaya	NULL
Jennifer	S	Wallace	Administration
Ramesh	K	Narayan	NULL
Joyce	A	English	NULL
Ahmad	V	Jabbar	NULL
James	E	Borg	Headquarters

## Example

**SSN\_PNOS**

Essn	Pno
123456789	1
123456789	2
666884444	3
453453453	1
453453453	2
333445555	2
333445555	3
333445555	10
333445555	20
999887777	30
999887777	10
987987987	10
987987987	30
987654321	30
987654321	20
888665555	20

**SMITH\_PNOS**

Pno
1
2

**SSNS**

Ssn
123456789
453453453

**R**

A	B
a1	b1
a2	b1
a3	b1
a4	b1
a1	b2
a3	b2
a2	b3
a3	b3
a4	b3
a1	b4
a2	b4
a3	b4

**S**

A
a1
a2
a3

**T**

B
b1
b4

