Discrepancy in energy after simulation

$dt = 0.02, N = 1000, n = 2000$

Discrepancy in energy between U_0 and U_n

delta accuracy of the Barnes-Hut method