### UNIVERSIDADE FEDERAL DO ABC

Tabela de Derivadas, Integrais e Identidades Trigonométricas

# Derivadas

### Regras de Derivação

- (cf(x))' = cf'(x)
- Derivada da Soma

$$(f(x) + g(x))' = f'(x) + g'(x)$$

• Derivada do Produto

$$(f(x)g(x))' = f'(x)g(x) + f(x)g'(x)$$

• Derivada do Quociente

$$\left(\frac{f(x)}{g(x)}\right)' = \frac{f'(x)g(x) - f(x)g'(x)}{g(x)^2}$$

• Regra da Cadeia

$$(f(g(x))' = (f'(g(x))g'(x)$$

#### Funções Simples

- $\frac{d}{dx}c = 0$
- $\frac{d}{dx}x = 1$
- $\frac{d}{dx}cx = c$
- $\frac{d}{dx}x^c = cx^{c-1}$
- $\frac{d}{dx}\left(\frac{1}{x}\right) = \frac{d}{dx}\left(x^{-1}\right) = -x^{-2} = -\frac{1}{x^2}$
- $\frac{d}{dx}\left(\frac{1}{x^c}\right) = \frac{d}{dx}\left(x^{-c}\right) = -\frac{c}{x^{c+1}}$
- $\frac{d}{dx}\sqrt{x} = \frac{d}{dx}x^{\frac{1}{2}} = \frac{1}{2}x^{-\frac{1}{2}} = \frac{1}{2\sqrt{x}}$

### Funções Exponenciais e Logarítmicas

- $\frac{d}{dx}e^x = e^x$
- $\frac{d}{dx} \ln(x) = \frac{1}{x}$
- $\frac{d}{dx}a^x = a^x \ln(a)$

# Funções Trigonométricas

- $\frac{d}{dx} \sin x = \cos x$
- $\frac{d}{dx}\cos x = -\sin x$ ,
- $\frac{d}{dx} \operatorname{tg} x = \sec^2 x$
- $\frac{d}{dx} \sec x = \operatorname{tg} x \sec x$
- $\frac{d}{dx} \cot x = -\csc^2 x$
- $\frac{d}{dx}$  cossec x = -cossec x cotg x

## Funções Trigonométricas Inversas

- $\frac{d}{dx}$  arcsen  $x = \frac{1}{\sqrt{1-x^2}}$
- $\frac{d}{dx} \arccos x = \frac{-1}{\sqrt{1-x^2}}$
- $\frac{d}{dx}$  arctg  $x = \frac{1}{1+x^2}$
- $\frac{d}{dx} \operatorname{arcsec} x = \frac{1}{|x|\sqrt{x^2-1}}$
- $\frac{d}{dx}$  arccotg  $x = \frac{-1}{1+x^2}$
- $\frac{d}{dx}$  arccossec  $x = \frac{-1}{|x|\sqrt{x^2-1}}$

### Funções Hiperbólicas

- $\frac{d}{dx} \operatorname{senh} x = \cosh x = \frac{e^x + e^{-x}}{2}$
- $\frac{d}{dx} \cosh x = \operatorname{senh} x = \frac{e^x e^{-x}}{2}$
- $\frac{d}{dx} \operatorname{tgh} x = \operatorname{sech}^2 x$
- $\frac{d}{dx}$  sech  $x = \operatorname{tgh} x$  sech x
- $\frac{d}{dx} \operatorname{cotgh} x = -\operatorname{cossech}^2 x$

## Funções Hiperbólicas Inversas

- $\frac{d}{dx}$  csch x = coth x cossech x
- $\frac{d}{dx}$  arcsenh  $x = \frac{1}{\sqrt{x^2+1}}$
- $\frac{d}{dx}$  arccosh  $x = \frac{1}{\sqrt{x^2 1}}$
- $\frac{d}{dx}$  arctgh  $x = \frac{1}{1-x^2}$
- $\frac{d}{dx}$  arcsech  $x = \frac{-1}{x\sqrt{1-x^2}}$
- $\frac{d}{dx}$  arccoth  $x = \frac{1}{1-x^2}$
- $\frac{d}{dx}$  arccossech  $x = \frac{-1}{|x|\sqrt{1+x^2}}$

### Regras de Integração

•  $\int cf(x) dx = c \int f(x) dx$ 

•  $\int [f(x) + g(x)] dx = \int f(x) dx + \int g(x) dx$ 

•  $\int f'(x)g(x) dx = f(x)g(x) - \int f(x)g'(x) dx$ 

### Funções Racionais

•  $\int x^n dx = \frac{x^{n+1}}{n+1} + c$  para  $n \neq -1$ 

 $\bullet \int \frac{1}{x} \, \mathrm{d}x = \ln|x| + c$ 

 $\bullet \int \frac{du}{1+u^2} = \arctan u + c$ 

 $\bullet \int \frac{1}{\alpha^2 + x^2} \, dx = \frac{1}{\alpha} \arctan(x/\alpha) + c$ 

 $\bullet \int \frac{du}{1-u^2} = \left\{ \begin{array}{l} \operatorname{arctgh}\, u+c, \ \operatorname{se}\, |u| < 1 \\ \operatorname{arccotgh}\, u+c, \ \operatorname{se}\, |u| > 1 \end{array} \right. = \\ \left. \frac{1}{2} \ln \left| \frac{1+u}{1-u} \right| + c \right.$ 

### Funções Logarítmicas

 $\bullet \int \ln x \, dx = x \ln x - x + c$ 

•  $\int \log_a x \, dx = x \log_a x - \frac{x}{\ln a} + c$ 

#### Funções Irracionais

 $\bullet \ \int \frac{du}{\sqrt{1-u^2}} = \arcsin u + c$ 

 $\bullet \ \int \frac{du}{u\sqrt{u^2 - 1}} = \mathrm{arcsec} \ u + c$ 

 $\bullet \ \int \frac{du}{u\sqrt{1-u^2}} = -\mathrm{arcsech} \ |u| + c$ 

 $\bullet \ \int \frac{du}{u\sqrt{1+u^2}} = -\mathrm{arccosech} \ |u| + c$ 

 $\bullet \ \int \frac{1}{\sqrt{\alpha^2 - x^2}} \, dx = \arcsin \frac{x}{\alpha} + c$ 

•  $\int \frac{-1}{\sqrt{a^2 - x^2}} \, dx = \arccos \frac{x}{a} + c$ 

#### Funções Trigonométricas

•  $\int \cos x \, dx = \sin x + c$ 

•  $\int \sin x \, dx = -\cos x + c$ 

•  $\int \operatorname{tg} x \, dx = \ln|\operatorname{sec} x| + c$ 

•  $\int \csc x \, dx = \ln|\csc x - \cot x| + c$ 

•  $\int \sec x \, dx = \ln|\sec x + \operatorname{tg} x| + c$ 

•  $\int \cot x \, dx = \ln|\sin x| + c$ 

•  $\int \sec x \operatorname{tg} x \, dx = \sec x + c$ 

•  $\int \csc x \cot x \, dx = -\csc x + c$ 

•  $\int \sec^2 x \, dx = \operatorname{tg} x + c$ 

•  $\int \sin^2 x \, dx = \frac{1}{2}(x - \sin x \cos x) + c$ 

•  $\int \cos^2 x \, dx = \frac{1}{2}(x + \sin x \cos x) + c$ 

## Funções Hiperbólicas

•  $\int \sinh x \, dx = \cosh x + c$ 

•  $\int \cosh x \, dx = \sinh x + c$ 

•  $\int \operatorname{tgh} x \, dx = \ln(\cosh x) + c$ 

•  $\int \operatorname{csch} x \, dx = \ln \left| \operatorname{tgh} \frac{x}{2} \right| + c$ 

•  $\int \operatorname{sech} x \, dx = \operatorname{arctg}(\sinh x) + c$ 

•  $\int \coth x \, dx = \ln|\sinh x| + c$ 

# Identidades Trigonométricas

1. 
$$sen(90^{\circ} - \theta) = cos \theta$$

$$2. \cos(90^{\circ} - \theta) = \sin \theta$$

$$3. \ \frac{\sin \theta}{\cos \theta} = \operatorname{tg} \theta$$

$$4. \sin^2 \theta + \cos^2 \theta = 1$$

5. 
$$\sec^2 \theta - \operatorname{tg}^2 \theta = 1$$

6. 
$$\csc^2 \theta - \cot^2 \theta = 1$$

7. 
$$\sin 2\theta = 2 \sin \theta \cos \theta$$

8. 
$$\cos 2\theta = \cos^2 \theta - \sin^2 \theta = 2\cos^2 \theta - 1$$

9. 
$$sen 2\theta = 2 sen \theta cos \theta$$

10. 
$$sen(\alpha \pm \beta) = sen \alpha cos \beta \pm cos \alpha sen \beta$$

11. 
$$\cos(\alpha \pm \beta) = \cos \alpha \sin \beta \pm \sin \alpha \cos \beta$$

12. 
$$tg(\alpha \pm \beta) = \frac{tg \alpha \pm tg \beta}{1 \mp tg \alpha tg \beta}$$

13. 
$$\sin \alpha \pm \sin \beta = 2 \sin \frac{1}{2} (\alpha \pm \beta) \cos \frac{1}{2} (\alpha \pm \beta)$$

14. 
$$\cos \alpha + \cos \beta = 2 \cos \frac{1}{2} (\alpha + \beta) \cos \frac{1}{2} (\alpha - \beta)$$

15. 
$$\cos \alpha - \cos \beta = 2 \sin \frac{1}{2} (\alpha + \beta) \sin \frac{1}{2} (\alpha - \beta)$$