

Homework 2 : Radar Imaging

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1 Characteristic of the mission and Introduction

The characteristic and parameters of the mission are encoded at the beginning of our code as seen on figure 1.

```
1 %% initialization
2 clc
3 C = 3e8; % speed of light
4 B = 170e6; % bandwidth
5 kr = 1.597256e12; % chirp rate
6 fc = 5.42876e9;
7 lambda = C / fc;
8 fs = 24485000; % sampling freq
9 ts = 1/fs;
10 beam_width = 0.1920;
11 prf = 307.292; % pulse repetition frequency
```

Figure 1: Parameters

It is also asked to provide the resolution in range and azimuth, as dictated by the following equations $\rho_r = \frac{C}{2B}$ and $\rho_y = \frac{\lambda}{2L_s}R$.¹ This range and azimuth resolution will dictate what is the minimal size of cell we should consider in our projection as seen on figure 2

2 Focusing by Time Domain Back Projection (TDBP)

2.1 Creating the back projection grid

As stated previously, our pixel size and therefore back projection grid must be generated by keeping in mind the range and azimuth resolution that limits our system.

¹ L_s is the length of the array, in our case, it is a synthetic array, therefore it is dictated by the speed of the plane and the number of sample generated.

```

54 %% Range/azimuth resolution
55 Range_resolution = C / (2*B);
56
57 R0 = plane_position(3,1);
58 p1 = plane_position(1,1); % position of the first sensor
59
60 p2 = plane_position(1,2); % position of the second sensor
61 dis = norm(p2 - p1); % distance of 2 consecutive sensor/position of the plane of SAR
62 % we want the total distance of our Synthetic aperture array ,
63
64 tpr = 1/prf;
65 v = dis / tpr; % speed of the plane
66 Ls = v*tpr*3000;
67 Azimuth_resolution = (lambda/(2*Ls))*R0;
68
69 %% creating pixels :
70
71 dx_r = 0.75 * Range_resolution;
72 dx_a = 0.75 * Azimuth_resolution;
73
74
75 x_mesh = plane_position(2,1) : -dx_a : plane_position(2,1000); % plane_position(2,sensor_num);
76 y_mesh = plane_position(1,1) +5*dx_r : -dx_r : plane_position(1,1) -5*dx_r;
77
78 [pixel_x,pixel_y] = meshgrid(x_mesh,y_mesh);% creat the pixel , pixel_x contains the x positions of each pixel , same goes for y
79 pixel_size = size(pixel_x);
80 pixel_size_x = pixel_size(1,1);
81 pixel_size_y = pixel_size(1,2)

```

Figure 2: We extract the final and initial positions of the plane and compute both resolutions. with that we create pixels

It is good as a rule of thumb to use 0.75 times the resolution in azimuth and range to determine the size of our pixels.

2.2 Change of spatial reference system

From then, as explain on appendix B in the provided document, we convert our initial reference system, the position data of the plane from latitude , longitude and altitude (LLA) to an intermediate referential that yields Northing , Easting and altitude (ENU). To do this transformation we needed to use a reference , we settled on using the mean value of longitude and latitude. Finally we convert this into our final referential by applying a rotation matrix to the ENU coordinates so that the East and North axis should be in a way that the East axis aligns in the direction of the trajectory. From there we determine an azimuth, range , altitude reference system. This procedure can be visualised on figure 3.

```

12 %% changing the coordinates to Range/Azimuth
13
14
15 lat0 = mean(geom(2,:));
16 lon0 = mean(geom(3,:));
17 h0 = 0;
18
19 [row_num col_num] = size(geom);
20 ENU = zeros(3,col_num); % new matrix of positions
21 spheroid = wgs84Ellipsoid;
22 for n = 1:1:col_num % creating new matrix of position by parsing the data
23     lat = geom(2,n); %take the second row of the geom which is lat
24     lon = geom(3,n); %take the second row of the geom which is lon
25     h = geom(4,n); %take the second row of the geom which is alt
26     [east,northing,z] = geodetic2enu(lat,lon,h,lat0,lon0,h0,spheroid); % LLA to ENU
27     ENU(1,n) = easting;
28     ENU(2,n) = northing;
29     ENU(3,n) = z;
30 end
31
32 theta_temp = zeros(1,col_num); % initialise the azimuth
33 for n = 1:1:col_num
34     theta_temp(n) = atan(ENU(2,n)/ENU(1,n)); % computing angle for the rotation matrix
35 end
36 theta = mean(theta_temp); % mean value of the angle
37 % we take the mean value of theta between he positionion to rotate our axis
38 % to have x along the east and y along the north . x=range , y azimuth
39 RangeAzimuth = zeros(2,col_num);
40 rotation_matrix = [cos(theta) -sin(theta) ; sin(theta) cos(theta)]; % rotation matrix
41 for n=1:1:col_num
42
43     A = [ENU(2,n) ; ENU(1,n)];
44
45     R = rotation_matrix*A; % rotating the axis
46     RangeAzimuth(1,n) = -R(1,1);
47     RangeAzimuth(2,n) = R(2,1);
48 end
49
50 plane_position = [RangeAzimuth ; ENU(3,:)]; % Range azimuth matrix contain range and azimuth , enu values is just the z , maka a matrix
51 sensor_num = size(plane_position);

```

Figure 3: Transformation of our spacial reference system from LLA to ENU to Range/Azimuth/ height.

2.3 Distance Computations

In this section, now that the coordinates system has been redefined , we can compute the distance from each pixel to each element of our virtual array (each slow time position of the plane) as

showcased on figure 4

```

82 % Distance Computation
83 temp_distance = zeros(1,sensor_num); % initialise matrix
84 distance = zeros(pixel_size_x*pixel_size_y,sensor_num); % matrix of projecting ( size of the grid on the ground)
85 % each row is pixel , each column is a distance to an antenna
86 counter = 1;
87 for n = 1 : 1 : pixel_size_x
88     for m = 1 : 1 : pixel_size_y
89         x_position = pixel_x(n,m);
90         y_position = pixel_y(n,m);
91         pixel_position = [x_position;y_position;0];
92
93         for k = 1 : 1 : sensor_num
94             temp_distance(1,k) = norm(pixel_position - plane_position(:,k)); % calculate distance between pixel and antenna
95         end
96         distance(counter,:) = temp_distance; % each row is pixel , each column is a distance to an antenna
97         counter = counter + 1; % stops at teh end of the for loop
98     end
99 end
100

```

Figure 4: Calculating the distance from each pixel , to each of the 3884 "virtual antennas" created by the trajectory of our plane .

2.4 Focus pixel on the ground

This section is to artificially create the range compressed data that would have been receiving on the plane. Now that all the slow time distance to all pixel have been computed , we can find their corresponding double travel time (we are talking in fast time ,to go from the plane to the pixel and back) and map it to have the corresponding slow time.Also we can create the focus pixel as described on part 4.See figure 5

```

103 % focused pixel in ground
104 step = size(distance); % step(1) number of rows , all the pixel we have
105 A = zeros(1,step(1)); % as many column as pixels
106 for n = 1 : 1 : step(1) % number of pixel
107     sum_temp = 0;
108     for m = 1 : 1 : step(2) %number of the satellite
109         D_row = distance(n,m);
110         time = D_row * 2 / C; % 2 bc back and forth
111         mapped_time = floor(time/ts)*1; %maps to lower integer , this gives you the time index on the data that you should evaluate
112         R = dat(mapped_time,m); %find the corresponding value in the data file
113         sum_temp = sum_temp + R * exp(2 * pi * distance(1,m) / lambda) * exp(-2 * 4 * pi * kr * (distance(1,m)^2) / C^2 ); % summ all the contribution using the formula
114     end
115     A(1,n) = sum_temp; %everything saved here
116 end
117
118

```

Figure 5: Creating Focused pixel

2.5 Frequency to distance conversion

The idea of this section , is to compute a FFT in fast time of the signal received by the plane , by doing so and coupled by that fact that we are using a chirp there is a clear correspondence between the frequency domain and the spacial (distance) domain². So to say,the values of a pixel at distance r_1 is mapped in our signal at a frequency $f_1 = K_r \frac{2r_1}{C}$, with K_r being the chip rate , the speed at which the chip change in frequency with respect to time. Therefore for each virtual antenna, we can compute the FFT in fast time and transform the frequency axis into a distance axis, by applying the equation stated previously , and project to each pixel the corresponding signal value. By doing so and by adding the contribution of each virtual antenna we get our final desired "picture". In order to do so we will also use some zero padding (adding zeros at the end of our signal) while doing the FFT to "artificially" increase the number of possible indices in the frequency domain. It is important to keep in mind that no matter what the highest index corresponds to the sampling frequency f_s .

²See Appendix A of homework.

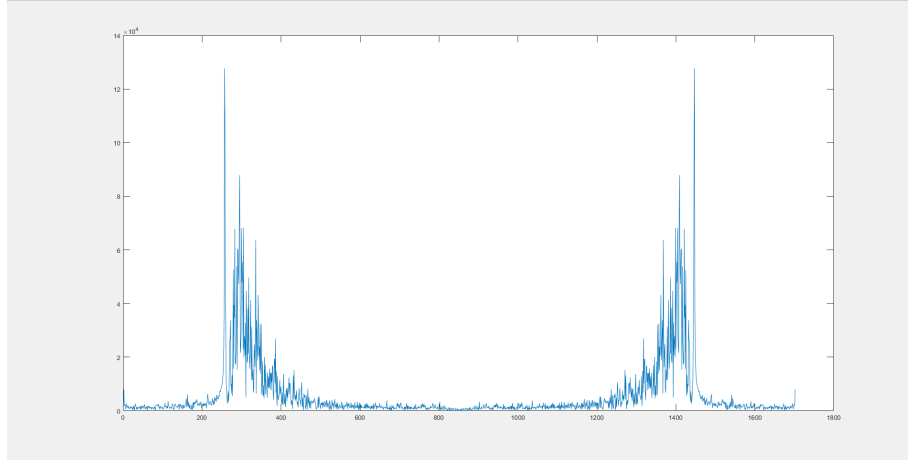


Figure 6: FFT in fast time of our received signal, without zero padding, the signal being real is symmetrical, so only the first half matters.

```

118 % frequency axis to range axis
119
120 % computing range axis
121 Data=dat;
122 % we have 3884 datas sets , but eah as 1702 samples in fast time
123 % let's 0 pad
124 FftData= zeros (16384,3884);
125 for n=1:1:3884
126     FftData(:,n)= fft(Data(:,n),16384); % as proposed in the document
127 end
128 dn =0:fs/16384:fs-1/16384; % freq axis
129
130
131 dt = dn./kr; % time axis
132
133 dr = dt.* C/2; % range axis
134
135 plot(dr,FttData(:,1));
136
137
138

```

Figure 7: FFT in fast time with zero padding and range transformation.

2.6 Selecting a random pixel

To start off the TDBP we need to pick a target pixel in a random position on our grid, see figure 8.

```

139 % place the target in a random position
140
141 clc
142 %rand_x_pixel = floor(pixel_size_x*rand()+1); % pick a reandom pixel index
143 %rand_y_pixel = floor(pixel_size_y*rand()+1); % pick a reandom pixel index
144 rand_x_pixel = 4;
145 rand_y_pixel = 120;
146 x_position = pixel_x(rand_x_pixel,rand_y_pixel); % random point coordinates
147 y_position = pixel_y(rand_x_pixel,rand_y_pixel); % random point coordinates
148

```

Figure 8: Picking a random pixel from the grid

2.7 Range compressed data simulation

Now, the range compressed data is "artificially" generated according to the formula on point 5.2. In this formula W is the antenna pattern, we decided to go for a sinc antenna pattern for our implementation. That sinc has as argument all the angle divided by the beam width. See figure 9.

```

149 % range compressed data computation
150 % calculating R0 = distance from the random target to the trajectory of
151 theta = -pi/2*pi/16384:pi - 1/16384;
152
153 row_num = (rand_x_pixel - 1) * pixel_size_y + rand_y_pixel;
154 target_dis = distance(row_num, :);
155 R_tow_r = zeros(3384,16384);
156
157 for n = 1 : 1 : 3384
158     R_tow_r_temp = sinc(theta./beam_width).*sinc((dr - target_dis(1,n))/Range_resolution)*exp(-j*4*pi*target_dis(1,n)/lambda);
159     R_tow_r(n,:) = R_tow_r_temp;
160 end
161 plot(dr,abs(R_tow_r(1,:)))
162
163

```

Figure 9: Generating the range compressed data

2.8 Time Domain back projection

For this section, we created two different implementation that also using different interpolation functions.

2.8.1 First implementation

As explain in section 2.5 , the idea is that for each slow time we find the corresponding ranged compressed data with the frequency/range mapping. Knowing the distance , we know the range , we therefore also know at what frequency to look at. Then having found the corresponding value , we find all the other pixels at the same distance from the SAR as the current one. We repeat this for each 3384 slow time and add each contribution. Then we should have a 2D SINC function around the main pixel position.

```

165 % TDBP
166
167 distance;
168
169 grid = zeros(pixel_size_x,pixel_size_y); % creating the grids
170
171 target_dis;
172 f = FftData(:,1)';
173 plot(dr,abs(f));
174 % find the corresponding index of the range_compressed_signal
175 for l = 1:1:3384
176
177     for n = 1 : 1 : 16384
178         if dr(1,n) > target_dis(1,1)
179             n;
180             break
181         end
182     end
183
184     f = FftData(:,1)'; % choosing the fft of the corresponding slow time
185     amp = abs(f(1,n))*exp(j*4*pi*distance(row_num ,1)/lambda); % finding the value of the ranged cpmressed data
186
187     neighbor = [rand_x_pixel+1 rand_y_pixel;rand_x_pixel+1 rand_y_pixel+1;rand_x_pixel rand_y_pixel+1;
188               rand_x_pixel-1 rand_y_pixel+1;rand_x_pixel-1 rand_y_pixel;rand_x_pixel-1 rand_y_pixel-1;
189               rand_x_pixel rand_y_pixel-1;rand_x_pixel+1 rand_y_pixel-1]; %neighbors of the selected pixel
190     neighbor_pos = zeros(8,3);
191
192     for n = 1:1:8
193         neighbor_pos(n,1) = pixel_x(neighbor(n,1),neighbor(n,2));
194         neighbor_pos(n,2) = pixel_y(neighbor(n,1),neighbor(n,2));
195     end
196     neighbor_pos; % position of the neighbors
197     dif = plane_position(:,1)-neighbor_pos; % vector representing the distance of each neighbor to the plane position
198     neighbor_dis = zeros(8,1);
199     for m = 1:1:8
200         neighbor_dis(m,1) = norm(dif(m,:));
201     end
202     neighbor_dis; % distance of each neighbor to the plane position
203     comp_nei_dist =abs(neighbor_dis - target_dis(1,1)); %subtracting the distance of neighbor from the target distance
204

```

Figure 10: TDBP1.1

```

204 - comp_nei_dist = abs(neighbor_dis - target_dis(1,1)); %subtracting the distance of neighbor from the target distance
205 - % finding 2 minimum values
206 - [x1_min ind1_min] = min(comp_nei_dist);
207 - comp_nei_dist(ind1_min,1) = 10;
208 -
209 - [x2_min, ind2_min] = min(comp_nei_dist);
210 - ind = ind2_min;
211 - % now that we have find 2 pixels with the most similar distance from the
212 - % plane position we should continue for each pixel in 2 for loop
213 - for k = 1 : 1 : max(pixel_size_x,pixel_size_y)
214 -
215 -
216 -     if k ==1
217 -         new_neighbor = neighbor(ind1_min,1);
218 -     end
219 -
220 -     rand_x_pixel_n1 = new_neighbor(1,1); % new x pixel
221 -     rand_y_pixel_n1 = new_neighbor(1,2); % new y pixel
222 -     row_num = (rand_x_pixel_n1 - 1) * rand_y_pixel_n1 + rand_y_pixel_n1; % corresponding distance from all the place position
223 -     target_dis_1 = distance(row_num , :); % selecting the corresponding distance
224 -     % find the corresponding index of the range_compressed_signal
225 -     for n = 1 : 1 : 16384
226 -         if dr(1,n) > target_dis_1(1,1)
227 -             n;
228 -             break
229 -         end
230 -     end
231 -     f = FftData(:,1)';
232 -     amp = abs(f(1,n))*exp(2*pi*distance(row_num,1)/lambda); % finding the value of the ranged compressed data
233 -
234 -
235 -     neighbor_1 = [rand_x_pixel_n1+1 rand_y_pixel_n1;rand_x_pixel_n1+1 rand_y_pixel_n1+1;rand_x_pixel_n1 rand_y_pixel_n1+1;
236 -     rand_x_pixel_n1-1 rand_y_pixel_n1+1;rand_x_pixel_n1-1 rand_y_pixel_n1;rand_x_pixel_n1-1 rand_y_pixel_n1-1;
237 -     rand_x_pixel_n1 rand_y_pixel_n1-1;rand_x_pixel_n1+1 rand_y_pixel_n1-1];
238 -     neighbor_1; % new neighbors
239 -     neighbor_pos_1 = zeros(8,3);
240 -     for n = 1:1:8
241 -         neighbor_pos_1(n,1) = pixel_x(neighbor_1(n,1),neighbor_1(n,2));
242 -         neighbor_pos_1(n,2) = pixel_y(neighbor_1(n,1),neighbor_1(n,2));
243 -     end

```

Figure 11: TDBP1.2

```

243 -
244 - end
245 - neighbor_pos_1; % new neighbors position
246 - dif_1 = plane_position(:,1)-neighbor_pos_1;% vector representing the distance of each neighbor to the plane position
247 - neighbor_dis_1 = zeros(8,1);
248 - for m = 1:1:8
249 -     neighbor_dis_1(m,1) = norm(dif_1(m,:)); % calculating the distance
250 - end
251 - if k == 1
252 -     comp_nei_dist_1 = abs( neighbor_dis_1 - target_dis(1,1)); %subtracting the distance of neighbor from the target distance
253 -
254 - else
255 -     comp_nei_dist_1 =abs( neighbor_dis_1 - temp_dis); %subtracting the distance of neighbor from the prevouse target distance
256 -     % check wheather the distance is too different from the main
257 -     % distance
258 -     o = abs( neighbor_dis_1 - target_dis(1,1));
259 -     if o>1
260 -         break
261 -     end
262 - end
263 - % find the the most similar distance
264 - [x1_min ind1_min] = min(comp_nei_dist_1);
265 -
266 - temp_dis = neighbor_dis_1(ind1_min,1);
267 - comp_nei_dist_1(ind1_min,1) = 10000;
268 - [x2_min ind2_min] = min(comp_nei_dist_1);
269 -
270 - new_neighbor = neighbor_1(ind2_min,1);
271 - grid(rand_x_pixel_n1,rand_y_pixel_n1) = grid(rand_x_pixel_n1,rand_y_pixel_n1) + amp;
272 -
273 - % check whether we have reached to the boundry of the pixel
274 - if new_neighbor(1,1) == 1
275 -     break
276 - elseif new_neighbor(1,1) == pixel_size_x
277 -     break
278 - elseif new_neighbor(1,2) == 1
279 -     break
280 - elseif new_neighbor(1,2) == pixel_size_y
281 -     break
282 - end

```

Figure 12: TDBP1.3

```

282 -         end
283 -
284 -
285 -     end
286 -     for k = 1 : 1 : max(pixel_size_x,pixel_size_y)
287 -
288 -         if k ==1
289 -             new_neighbor = neighbor(ind,:);
290 -         end
291 -
292 -         rand_x_pixel_n2 = new_neighbor(1,1);% new x_pixel
293 -         rand_y_pixel_n2 = new_neighbor(1,2);% new y_pixel
294 -         row_num = (rand_x_pixel_n2 - 1) * rand_y_pixel_n2 + rand_y_pixel_n2; % corresponding distance from all the place position
295 -         target_dis_2 = distance(row_num , :);% selecting the corresponding distance
296 -         for n = 1 : 1 : 16384
297 -             if dr(1,n) > target_dis_2(1,1)
298 -                 n;
299 -                 break
300 -             end
301 -         end
302 -
303 -         f = FttData(:,1)';
304 -         amp = abs(f(1,n)) * exp(2*pi*distance(row_num ,1)/lambda);% obtaining the corresponding value
305 -
306 -         target_dis_2 = [rand_x_pixel_n2+1 rand_y_pixel_n2;rand_x_pixel_n2+1 rand_y_pixel_n2+1;rand_x_pixel_n2 rand_y_pixel_n2+1;
307 -             rand_x_pixel_n2-1 rand_y_pixel_n2+1;rand_x_pixel_n2-1 rand_y_pixel_n2;rand_x_pixel_n2-1 rand_y_pixel_n2-1;
308 -             rand_x_pixel_n2 rand_y_pixel_n2-1;rand_x_pixel_n2+1 rand_y_pixel_n2-1];
309 -         target_dis_2; % new neighbor
310 -         neighbor_pos_2 = zeros(8,3);
311 -         for n = 1:1:8
312 -             neighbor_pos_2(n,1) = pixel_x(target_dis_2(n,1),target_dis_2(n,2));
313 -             neighbor_pos_2(n,2) = pixel_y(target_dis_2(n,1),target_dis_2(n,2));
314 -         end
315 -         neighbor_pos_2; %position of the neighbor
316 -         dif_2 = plane_position(:,1)-neighbor_pos_2; %vector representing the distance of each neighbor to the plane position
317 -
318 -         neighbor_dis_2 = zeros(8,1);
319 -         for m = 1:1:8
320 -             neighbor_dis_2(m,1) = norm(dif_2(m,:));
321 -         end

```

Figure 13: TDBP1.4

```

321 -         end
322 -         neighbor_dis_2; % distance of the neighbors
323 -         if k == 1
324 -             comp_nei_dist_1 = abs( neighbor_dis_2 - target_dis(1,1));%subtracting the distance of neighbor from the target distance
325 -
326 -         else
327 -             comp_nei_dist_1 = abs( neighbor_dis_2 - temp_dis);
328 -             % check wheather the distance is too different from the main
329 -             % distance
330 -             o = abs( neighbor_dis_2 - target_dis(1,1));
331 -             if o>1
332 -                 break
333 -             end
334 -         end
335 -         % find the the most similar distance
336 -         [x1_min ind1_min] = min(comp_nei_dist_1);
337 -
338 -         temp_dis = neighbor_dis_2(ind1_min,1);
339 -         comp_nei_dist_1(ind1_min,1) = 10000;
340 -         [x2_min ind2_min] = min(comp_nei_dist_1);
341 -
342 -         new_neighbor = target_dis_2(ind2_min,:);
343 -         grid(rand_x_pixel_n2,rand_y_pixel_n2) = grid(rand_x_pixel_n2,rand_y_pixel_n2) + amp;
344 -
345 -         % check whether we have reached to the boundry of the pixel
346 -         if new_neighbor(1,1) == 1
347 -             break
348 -         elseif new_neighbor(1,1) == pixel_size_x
349 -             break
350 -         elseif new_neighbor(1,2) == 1
351 -             break
352 -         elseif new_neighbor(1,2) == pixel_size_y
353 -             break
354 -         end
355 -
356 -     end
357 -
358 -
359 - end
360 -

```

Figure 14: TDBP1.5

2.8.2 Second implementation

In this section we will use the interp1 function.

We start off by finding the slow time at which the SAR see the selected pixel, therefore the angle of the target with respect to the positions of the SAR is computed. If the object is at a bigger angle than the beamwidth, we can consider that it is not seen by the plane.

```

376 %% find the times that the SAR see target
377 c1c
380
381 i = 1;
382
383 for m = 1 : 1 : 3884
384
385     z = plane_position(3,m);
386     l = [plane_position(1,m),plane_position(2,m)];
387     k = [y_position,x_position];
388
389     if (atan(norm(l-k)/z)) < (beam_width/2)
390
391         target_seen_slowtime(i)=m;
392         i=i+1;
393     end
394 end
395
396
397

```

Figure 15: Is the target seen by the SAR position.

The next step is to find all the pixels seen by the SAR in each individual slow time. By basing our calculation on the geometry we can easily extract the distance and azimuth that the plane observe at each slow time. Because we know the size of the pixel in the azimuth axis (Y) we can compute how many pixels the radar can pickup at each specific slow time but also the pixel that change in each consecutive slow time. We end up storing the totality of pixels seen by the radar along its trajectory.

```

398 %% find the seen pixels in the slow time according to the angle by plane
399
400
401
402 for m = 1:1:3884
403
404     z = plane_position(3,m);
405     az_seen = tan(beam_width/2)*z*2; % distance seen in each slow time
406     az_seen_pixel = floor(az_seen/dx_a); % number of pixel seen in each slow time
407
408     start_seen_pixel = round(az_seen_pixel/2);
409     step_size_pixel = round((plane_position(2,1) - plane_position(2,2))/dx_a); % number of pixel added in each slow time
410
411     seen_pixel = zeros(3884,pixel_size_y);
412     cnt = 0;
413     % which pixels are seen in each slow time
414     for n = 1:1:3884
415         if n < start_seen_pixel / step_size_pixel
416             cnt = cnt + 1 ;
417             for m = 1:1:start_seen_pixel + step_size_pixel * (n-1)
418                 seen_pixel(n,m) = m;
419             end
420         else
421             if az_seen_pixel + n * 5 < pixel_size_y
422                 for m = (n - cnt) * step_size_pixel : 1 : az_seen_pixel + (n - cnt) * step_size_pixel
423                     seen_pixel(n,m) = m;
424                 end
425             else
426                 for m = (n - cnt) * step_size_pixel : 1 : pixel_size_y
427                     seen_pixel(n,m) = m;
428                 end
429             end
430         end
431     end
432
433 end
434
435
436

```

Figure 16: Determining which pixels from the grid are seen by the SAR

From that we can reevaluate the matrix of distance by only containing the pixels that are actually seen by the SAR. This matrix is a sub matrix of our original distance matrix. Now that that new matrix contains only the pixels of interest, we can proceed with the TDBP, once again in each slow time and only for the pixels seen by the SAR at that slow time moment we interpolate the ranged compressed signal ³ onto a matrix containing all the distance between the radar and the pixels. We then proceed to do that for each slow time positions and sum the contribution on each pixel respectively.

³because after doing the FFT and making the transformation to a distance axis , this range compressed data has a X axis corresponding to a distance, if a specific pixel is in between two represented "x"axis distances , we need to interpolate between those two indices


```

439 % new distance matrix accordig to the rows
439 temp_distance = zeros(1,sensor_num); % initialise matrix
440 distance_l = zeros(pixel_size_x*pixel_size_y,sensor_num); % matrix of projecting ( size of the grid on the ground)
441 % each row is pixel , each column is a distance to an antenna
442 counter = 1;
443 for n = 1 : 1 : pixel_size_y
444     for m = 1 : 1 : pixel_size_x
445         x_position = pixel_x(m,n);
446         y_position = pixel_y(m,n);
447         pixel_position = [x_position;y_position;0];
448
449         for k = 1 : 1 : sensor_num
450             temp_distance(1,k) = norm(pixel_position - plane_position(:,k)); % calculate distance between pixel and antenna
451         end
452         distance_l(counter,:) = temp_distance; % each row is pixel , each column is a distance to an antenna
453         counter = counter + 1 ; % stops at teh end of the for loop
454     end
455 end
456

```

Figure 17: Reevaluating the distance matrix.

```

457 % TDBP
458 clc
459 seen_step = size(target_seen_slowtime);
460 seen_step = seen_step(1,2);
461
462
463 grid = zeros(size(distance_l));
464 t = size(grid);
465 t = t(1,1);
466 for i = 1 : 1 : seen_step
467     slow_time = target_seen_slowtime(1,i);
468     temp = seen_pixel(i,:);
469     temp(temp==0) = [];
470     siz = size(temp);
471     siz = siz(1,2);
472     xp = distance_l(temp(1,1):temp(1,siz),:); % distance matrix of seen pixels in selected slow times
473     v = FttData(:,slow_time); % values of ranged compressed signal in seen slow time
474     x = dr; % range complex axis
475     vq = interp1(x,v,xp); % do interpolation
476     vq_size = size(vq);
477     vq_size = vq_size(1,1);
478     % add zeros to the begining and the end of the distance matrix for
479     % coherent summation
480     if temp(1,1) == 1
481         v_q = [vq ; zeros(t-vq_size,3884)];
482         grid = grid + v_q ;
483     else
484         if siz < pixel_size_y
485             v_q = [zeros(temp(1,1) , 3884); vq ; zeros(t -temp(1,1) - vq_size )];
486             grid = grid + v_q ;
487         else
488             v_q = [zeros(t -vq_size ,3884);vq];
489             grid = grid + v_q ;
490         end
491     end
492 end
493 end
494
495

```

Figure 18: Applying the TDBP but only considering the "seen" pixels.

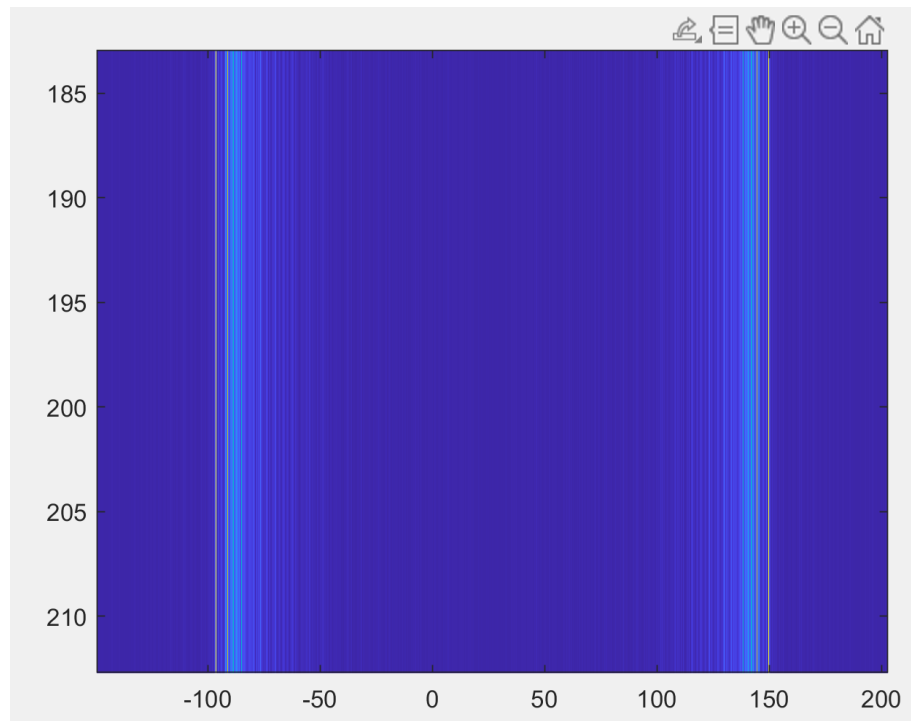


Figure 19: Range compressed pulse using imagesc.