### Bioinformatics III

#### Eighth Assignment

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## Exercise 8.1: Data Preprocessing

(a) **Data matrix:** The supplement contains the data matrix.py-file with the outline of a Data-Matrix-class in which you should complete.

#### Listing 1: Data Matrix class script

```
o import pandas as pd
  from scipy import stats
  class DataMatrix:
       \mathbf{def} \ \ \underset{"""}{\text{--init}} \ \text{--} \ (\ \text{self} \ , \ \ \text{file-path} \ ) :
5
            : param \ file\_path: \ path \ to \ the \ input \ matrix \ file
           self.file_path = file_path
           self.df = None
10
           # read the matrix in the input file, remove rows with empty values and
                 merge duplicate rows
            self.read_data()
       def read_data(self):
15
           Reads data from a given matrix file, where the first line gives the
               names of the columns and the first column
            gives the names of the rows. Removes rows with empty or non-numerical
               values and merges rows with the same
           name into one.
20
           # Read the file in a pandas DataFrame
           self.df = pd.read_csv(self.file_path, index_col=False, sep='\t')
           # Drop all NAN before setting the first columns as index, as some
                index\ label\ might\ be\ NaN/empty
            self.df.dropna(axis=0, how="any", inplace=True)
25
           \# Change the first column's name
           new_columns = self.df.columns.values
new_columns[0] = "Index"
30
           self.df.columns = new_columns
           # Sort values for later use (to_tsv)
           self.df = self.df.sort_values('Index')
           # Group by index: remove duplicate rows by meaning the rows values
           # Set 'Index' as index automatically
           self.df = self.df.groupby('Index').mean()
```

```
# Print to console to have a nice overview
           \# print(self.df)
40
      def get_rows(self):
           : return: \ dictionary \ with \ keys = row \ names, \ values = \ list \ of \ row \ values
45
           rows = \{\}
           for index, row in self.df.iterrows():
50
               rows[index] = list(row)
           return rows
      def get_columns(self):
55
           :return: dictionary with keys = column names, values = list of column
               v\,a\,l\,u\,e\,s
           cols = \{\}
           for name, values in self.df.iteritems():
60
               cols[name] = list(values)
           return cols
      def not_normal_distributed(self, alpha, rows):
65
           Uses the Shapiro-Wilk test to compute all rows (or columns) that are
               not normally distributed.
           :param alpha: significance threshold
           :param\ rows:\ True\ if\ the\ Shapiro-Wilk\ p-values\ should\ be\ computed\ for
               the rows, False if for the columns
           : return: dictionary \ with \ keys = row/columns \ names, \ values = Shapiro-
70
               Wilk p-value
           ret = \{\}
           if rows:
75
               tmp = self.get_rows()
           else:
               tmp = self.get_columns()
           for key, value in tmp.items():
80
               shapiro = stats.shapiro(tmp[key])
               pvalue = shapiro[1]
               if pvalue < alpha:</pre>
                    ret[key] = pvalue
85
           return ret
      def to_tsv(self, file_path):
90
           Writes the processed matrix into a tab-separated file, with the same
               column order as the input matrix and
           the rows in lexicographical order.
           : param \ file\_path: \ path \ to \ the \ output \ file
95
           self.df.to\_csv(file\_path, sep='\t')
```

(b) Process expression and methylation data: In the function exercise 1() in main.py, use your DataMatrix-class to read in the expression and methylation tables given in the supple-

ment and write the processed matrices into files. <sup>1</sup>

#### Listing 2: Main programm

```
o from data_matrix import DataMatrix
  from network import CorrelationNetwork
  from correlation import CorrelationMatrix
  from cluster import CorrelationClustering
5 def dict_to_file(dict, path):
       :param dict: Dictionnary you want to write to file
      :param path: Path or filename
10
       : return:\ nada
      fout = path
      fo = open(fout, "w")
      for k, v in dict.items():
15
           fo.write(\mathbf{str}(k) + \dot{\dot{x}} = \dot{x} + \mathbf{str}(v) + \dot{x} = \dot{x}
      fo.close()
20 def exercise_1():
      # Read data
      data_expression = DataMatrix("./expression.tsv")
      data_methylation = DataMatrix("./methylation.tsv")
      # Uses the Shapiro-Wilk test to test if the data follow a normal
25
           distribution
      ALPHA = 0.05
      not_normal_expression_genes = data_expression.not_normal_distributed(ALPHA
           , True)
       dict_to_file(not_normal_expression_genes, "./not_normal_expression_genes.
          txt")
      print("Number_of_genes_whose_data_does_not_follow_a_normal_distribution_(
30
          EXPRESSION): _" , len(not_normal_expression_genes))
      not_normal_expression_sample = data_expression.not_normal_distributed(
          ALPHA, False)
       dict_to_file (not_normal_expression_sample, "./not_normal_expression_sample
           . txt")
      print ("Number_of_sample_whose_data_does_not_follow_a_normal_distribution_(
          EXPRESSION): _" , len(not_normal_expression_sample))
35
      \verb|not_normal_methylation_genes| = \verb|data_methylation.not_normal_distributed| (
          ALPHA, True)
       dict_to_file(not_normal_methylation_genes, "./not_normal_methylation_genes
           . txt")
      print("Number_of_genes_whose_data_does_not_follow_a_normal_distribution_(
          METHYLATION): _", len(not_normal_methylation_genes))
      not_normal_methylation_sample = data_methylation.not_normal_distributed(
40
          ALPHA, False)
       dict_to_file (not_normal_methylation_sample, "./
           not_normal_methylation_sample.txt")
      print("Number_of_sample_whose_data_does_not_follow_a_normal_distribution_(
          METHYLATION): _" , len(not_normal_methylation_sample))
      # Write processed matrix to file
45
      data_expression.to_tsv("schmitt_schowing_expression.tsv")
      data_methylation.to_tsv("schmitt_schowing_methylation.tsv")
```

<sup>&</sup>lt;sup>1</sup>The files are attached with the source files in the email.

```
50 def exercise_3():
       #
       data_expression = DataMatrix("./expression.tsv")
data_methylation = DataMatrix("./methylation.tsv")
55
       NETWORK.THRESHOLD = 0.75
       # Expression
       cm = CorrelationMatrix(data\_expression, "Pearson", True)
60
       cn = CorrelationNetwork(cm,NETWORK_THRESHOLD)
       cn.to_sif("./schmitt_schowing_expression_network_pearson.sif")
       cm = CorrelationMatrix(data_expression, "Spearman", True)
       cn = CorrelationNetwork (cm, NETWORK_THRESHOLD)
65
       cn.to_sif("./schmitt_schowing_expression_network_spearman.sif")
       cm = CorrelationMatrix(data_expression, "Kendall", True)
       cn = CorrelationNetwork(cm, NETWORK.THRESHOLD)
       cn.to_sif("./schmitt_schowing_expression_network_kendall.sif")
70
       cm = CorrelationMatrix(data_methylation, "Pearson", True)
       cn = CorrelationNetwork(cm,NETWORK_THRESHOLD)
       cn.to_sif("./schmitt_schowing_methylation_network_pearson.sif")
75
       cm = CorrelationMatrix(data_methylation, "Spearman", True)
       cn = CorrelationNetwork(cm, NETWORK_THRESHOLD)
       cn.to_sif("./schmitt_schowing_methylation_network_spearman.sif")
80
       cm = Correlation Matrix (\, data\_methylation \,, \,\, "Kendall" \,, \,\, True)
       cn = CorrelationNetwork(cm, NETWORK_THRESHOLD)
       cn.to_sif("./schmitt_schowing_methylation_network_kendall.sif")
85
   \mathbf{def} exercise_4():
       # TODO
       # correlation matrix -> columns and not rows
       data_expression = DataMatrix("./expression.tsv")
data_methylation = DataMatrix("./methylation.tsv")
       # With the expression data
95
       cm = CorrelationMatrix(data_expression, "Kendall", False)
       cc = CorrelationClustering(cm)
       cc.trace_to_tsv("schmitt_schowing_expression_cluster_kendall.tsv")
100
       cm = CorrelationMatrix(data_expression, "Pearson", False)
       cc = CorrelationClustering(cm)
       cc.trace_to_tsv("schmitt_schowing_expression_cluster_pearson.tsv")
       cm = CorrelationMatrix(data_expression, "Spearman", False)
       cc = CorrelationClustering (cm)
105
       cc.trace_to_tsv("schmitt_schowing_expression_cluster_spearman.tsv")
       # With the methylation data
       cm = CorrelationMatrix(data_methylation, "Kendall", False)
       cc = CorrelationClustering (cm)
110
       \verb|cc.trace_to_tsv| ("schmitt_schowing_methylation_cluster_kendall.tsv")|
       cm = CorrelationMatrix(data_methylation, "Pearson", False)
       cc = CorrelationClustering (cm)
```

```
cc.trace_to_tsv("schmitt_schowing_methylation_cluster_pearson.tsv")

cm = CorrelationMatrix(data_methylation, "Spearman", False)

cc = CorrelationClustering(cm)

cc.trace_to_tsv("schmitt_schowing_methylation_cluster_spearman.tsv")

# only execute the following if this module is the entry point of the program,

not when it is imported into another file

if __name__ == '__main__':

exercise_1()

exercise_3()

exercise_4()
```

For each input file, report the number of genes and samples whose data does not follow a normal distribution with  $\alpha = 0.05$ .

Number of genes whose data does not follow a normal distribution (EXPRESSION): 73

Number of sample whose data does not follow a normal distribution (EXPRESSION): 19

Number of genes whose data does not follow a normal distribution (METHYLATION): 66

Number of sample whose data does not follow a normal distribution (METHYLATION): 19

#### Exercise 8.2: Correlation Measures

Listing 3: Correlation matrix

```
o from itertools import combinations
  from scipy import stats
  \mathbf{def} \ \mathrm{rank}(x):
        :param x: a list of values
        : return: \ ranking \ of \ the \ input \ list
        Note: not used because of laziness
        " " "
       return stats.rankdata(x)
  def pearson_correlation(x, y):
15
        : param \ x: \ a \ list \ of \ values
        :param\ y:\ a\ list\ of\ values
        : return: \ Pearson \ correlation \ coefficient \ of \ X \ and \ Y \\ """
20
       return stats.pearsonr(x, y)[0]
   \mathbf{def} spearman_correlation(x, y):
25
        :param \ x: \ a \ list \ of \ values
        :param\ y:\ a\ list\ of\ values
        : return: \ Spearman \ correlation \ coefficient \ of \ X \ and \ Y
30
       return stats.spearmanr(x, y)[0]
   def kendall_correlation(x, y):
        :param x: a list of values
        : param \ y: \ a \ list \ of \ values
        :return: Kendall-B correlation coefficient of X and Y
40
       return stats.kendalltau(x, y)[0]
   class CorrelationMatrix(dict):
        This class behaves like a dictionary, where the correlation between two
            elements 1 and 2 is accessible via
        cor\_matrix \textit{[(element\_1\,,\ element\_2)]} \ or \ cor\_matrix \textit{[(element\_2\,,\ element\_1)]} \ since
            the matrix is symmetrical.
        It also stores the row (or column) names of the input DataMatrix.
       \label{eq:def_def} \textbf{def} \ \_\texttt{init}\_\texttt{-} \ (\ \texttt{self} \ , \ \ \texttt{data\_matrix} \ , \ \ \texttt{method} \ , \ \ \texttt{rows} \,) :
50
             :param data_matrix: a DataMatrix (see data_matrix.py)
             :param method: string specifying the correlation method, must be 'Pearson', 'Spearman' or 'Kendall'
             :param rows: True if the correlation matrix should be constructed for the
             rows, False if for the columns
            # initialise the dictionary
            super().__init__(self)
```

```
# if rows = True, then compute the correlation matrix for the row data
           if rows:
60
               data = data_matrix.get_rows()
           \# if rows = False, then compute the correlation matrix for the column data
           {f else}:
               data = data_matrix.get_columns()
65
           # sorted list of row names (or column names) in the input data matrix
           self.names = list(sorted(data.keys()))
           # compute the correlation between all pairs of rows (or columns)
           for name_1, name_2 in combinations(data.keys(), 2):
70
               # use the specified correlation method
               if method == 'Pearson':
                   correlation = pearson_correlation(data[name_1], data[name_2])
               elif method = 'Spearman':
                   correlation = spearman_correlation(data[name_1], data[name_2])
75
               elif method = 'Kendall':
                   correlation = kendall_correlation(data[name_1], data[name_2])
                   raise ValueError('The_correlation_method_not_supported_must_be_
                       either_Pearson,_Spearman_or_Kendall.')
80
               # add the correlation symmetrically
               self[(name_1, name_2)] = correlation
self[(name_2, name_1)] = correlation
```

### Exercise 8.3: Gene Co-Expression Networks

### (a) Network construction

Listing 4: Correlation network

```
o import collections
  import pandas as pd
  import math
  class CorrelationNetwork:
      def __init__(self , correlation_matrix , threshold):
    """
           Constructs a co-expression network from a correlation matrix by adding
                edges \ between \ nodes \ with \ absolute
           correlation \ bigger \ than \ the \ given \ threshold \, .
           : param \ \ correlation\_matrix: \ a \ \ CorrelationMatrix \ \ (see \ \ correlation.py)
           :param threshold: a float between 0 and 1
10
           interactions = []
           for tup, corr in correlation_matrix.items():
15
               correlation = str(round(corr, 2))
               node0 = tup[0]
               node1 = tup[1]
               tmp = [node0, node1, correlation]
20
               tmp.sort(reverse=True)
               interactions.append(tmp)
          # create set of unique node connections (src, dest, corr)
           set_interractions = set(tuple(i) for i in interactions)
25
          # Sort the set
           set_interractions = sorted(set_interractions)
          \# Make a dataframe
30
           df_interractions = pd.DataFrame.from_records(set_interractions)
          \# Set columns names
           df_interractions.columns = ['src', 'dest', 'corr']
35
          # Creating a dictionary with the structure as below:
             dict (src, corr): [dest]
           self.dc_interact = collections.defaultdict(list)
          \# Fill the dictionary with unique src-correlation id and a dest.
40
               list
           for index, row in df_interractions.iterrows():
               # Skip too small correlations (threshold vs absolute value)
               if math.fabs(float(row['corr'])) < threshold:
                   continue
45
               \# If the correlation is big enough, add it to the dictionary
               tmp_tuple = (row['src'], row['corr'])
               self.dc_interact[tmp_tuple].append(row['dest'])
      def to_sif(self, file_path):
           Write the network into a simple interaction file (SIF).
           Column 0: label of the source node
           Column 1: interaction type
           Columns \ 2+: \ label \ of \ target \ node(s)
           : param \ file\_path: \ path \ to \ the \ output \ file
```

# (b) Network visualisation<sup>2</sup>

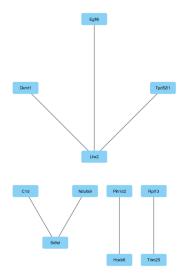


Figure 1: Expression network with Kendall correlation

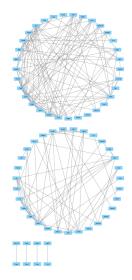


Figure 2: Expression network with Pearson correlation

<sup>&</sup>lt;sup>2</sup>The files are attached with the source files in the email.

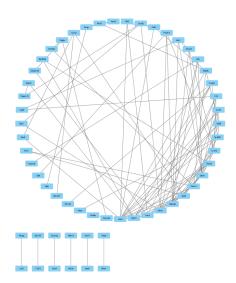


Figure 3: Expression network with Spearman correlation

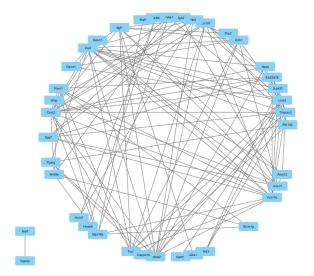


Figure 4: Methylation network with Kendall correlation

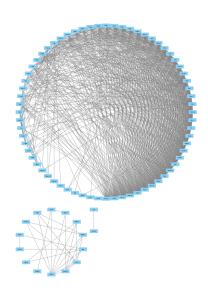


Figure 5: Methylation network with Pearson correlation

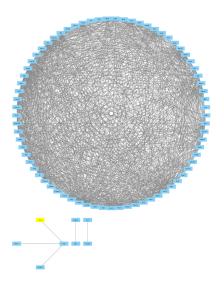


Figure 6: Methylation network with Spearman correlation

(c)  ${f Discussion:} Briefly\ comment\ on\ the\ similarities\ and\ difference\ between\ the\ networks.$  Explain and discuss your results.

We observe that the number of highly correlated gene is much higher when we look at the methylation in opposition as when we look at the expression.

### Exercise 8.4: Hierarchical Clustering

### (a) Implementation:

Listing 5: Hierarchical clustering

```
o import itertools
  class Cluster(frozenset):
      This class behaves like a frozenset, meaning it only contains unique items
           like a set but you cannot add or remove
      items, which makes it hashable and thus suitable for dictionary keys or as
           elements of a normal set.
      You can use the modified union method to merge two clusters as follows:
      merged\_cluster = cluster\_1.union(cluster\_2)
      The to string method was modified as well to help with the trace_to_tsv()
      method in exercise 8.4.
      \mathbf{def} \ \ \_\_str_{--}(self):
10
          :return: string with the sorted elements of the current cluster:
          element_1, element_2,...
          return ', _'. join(sorted(self))
15
      def union(self , iterable):
          : param \ iterable: \ a \ Cluster \,, \ list \,, \ set \,, \ iterator \,, \dots
          :return: a new Cluster containing all elements in the current cluster
             and the iterable
20
          return Cluster(list(self) + list(iterable))
  class CorrelationClustering:
      def __init__(self , correlation_matrix):
          Initialises and executes hierarchical clustering based on a
              correlation\ matrix.
          :param correlation_matrix: a CorrelationMatrix (see correlation.py)
          30
          \# \ distance \ metric
          self.d = correlation\_matrix
          # list of tuples: [(cluster 1 to merge, cluster 2 to merge, linkage
              value between the two clusters),...
          self.trace = []
          # cluster the elements in the correlation matrix
          self.cluster()
40
      def cluster (self):
          Hierarchically clusters the elements in the input correlation matrix
          and stores each step in the trace.
          # Create a set of unique correlation (a, b, corr) but not (b, a, corr)
45
          \# set of nodes (experiments)
          set_experiment = set(i for i in self.d.names)
          all_individual_clusters = []
          for element in set_experiment:
50
              tmp_cluster = Cluster([element])
              all_individual_clusters.append(tmp_cluster)
```

```
\# while we have more than one cluster
55
           while len(all_individual_clusters) > 1:
               # Compute linkage for all pair
               all_pairs = list(itertools.combinations(all_individual_clusters,
                   2))
               index_max_linkage = 0
60
               max\_linkage = 0
               for i in range(len(all_pairs)):
                   tmp_linkage = self.average_linkage(all_pairs[i][0], all_pairs[
                       i ] [1])
                   if tmp_linkage > max_linkage:
                       max_linkage = tmp_linkage
65
                       index_max_linkage = i
               # Now we have the two clusters to merge: merge them and remove
                   them from the list
               # First add them to the trace
               self.trace.append([all_pairs[index_max_linkage][0], all_pairs[
70
                   index_max_linkage | [1], max_linkage |)
               new_cluster = all_pairs[index_max_linkage][0].union(all_pairs[
                   index_max_linkage [[1])
               \# Remove the two clusters that are gonna be merged from the list
               all_individual_clusters.remove(all_pairs[index_max_linkage][0])
               all_individual_clusters.remove(all_pairs[index_max_linkage][1])
75
               # Append the new cluster resulting from the merging of the two old
                    ones
               all_individual_clusters.append(new_cluster)
80
       def average_linkage(self, cluster_1, cluster_2):
           :return: average linkage between cluster 1 and cluster 2
85
           sum_{\text{-}} = 0
           for key1 in cluster_1:
               for key2 in cluster_2:
                   sum_{-} += abs(self.d[(key1, key2)])
90
           return 1/(len(cluster_1) * len(cluster_2)) * sum_
       def trace_to_tsv(self, file_path):
95
           Writes\ the\ clustering\ trace\ into\ a\ tab-separated\ file\ .\ Each\ line
               represents a step in the clustering, in which
           two clusters are merged.
           Column 0: comma-separated names in cluster 1
           Column 1: comma-separated names in cluster 2
           Column 2: linkage value
100
           : param \ file\_path: \ path \ to \ the \ output \ file
           f = open(file_path, "w") # opens file
105
           # At each step we have the two merged cluster and their linkage value
           # The linkage value is rounded to 4 digits to make it nice
           for step in self.trace:
               [2], 4)) + "\n")
110
           f.close()
```

- (b) **Application:** In the function exercise 4() in main.py (listing 2), use your implementation to hierarchically cluster the expression and methylation data tables with the Pearson, Spearman and Kendall correlation coefficient. This should give you a total of 6 TSV files
- (c) **Discussion:** Can hierarchical clustering be used to differentiate between blood cells and skin tissues? Are there differences between the correlation coefficients or data type? Why?

Let's first recall the two different types of cells. In this experiment we have the samples HSC, MPP1, MPP2, CLP, CMP, GMP, MEP, CD4, CD8, B cell, Eryth, Granu and Mono that are from blood cells, whereas the samples TBSC, ABSC, MTAC, CLDC, EPro and EDif from skin tissues. In the listing 7 at line 15, one of the last merge, we can see that the two merged cluster are from samples from different cells (blood or skin) meaning that the clustering is working well<sup>3</sup>. We can assume here that the genes in a skin cell or in a blood cell are not expressed and/or methylated in the same way as the function of the cells are not the same.

Listing 6: Hierarchical clustering example with methylation data and Pearson correlation

```
o GMP
          Granu
                   0.9988
  MPP2
          CMP
                   0.9985
  CD8
          CD4
                   0.9981
  CLP
          CMP. MPP2
                           0.9972
  GMP,
       Granu
                   CLP
                       CMP, MPP2
                                    0.9965
                CMP, GMP, Granu, MPP2
                                             0.9961
5 Mono
          CLP,
  MPP1
          HSC
                   0.9956
  TBSC
          ABSC
                   0.9955
  CLP, CMP, GMP,
                  Granu, MPP2, Mono
                                            HSC, MPP1
                                                             0.9919
  EPro
          EDif
                   0.9918
 CD4,
                   CLP, CMP, GMP, Granu, HSC, MPP1, MPP2, Mono
                                                                      0.9901
  MEP
          CD4, CD8, CLP, CMP, GMP, Granu, HSC, MPP1, MPP2, Mono
                                                                      0.9889
  MTAC
          ABSC, TBSC
                            0.9889
                                     Granu, HSC, MEP, MPP1, MPP2, Mono
  B_cell
          CD4, CD8, CLP, CMP, GMP,
                                                                              0.9871
                   ABSC, MTAC, TBSC
                                            0.9795
  EDif,
15 CLDC
          ABSC, EDif, EPro, MTAC, TBSC
                                             0.9768
          CD4, CD8, CLP, CMP, GMP,
                                            HSC, MEP, MPP1, MPP2, Mono
                                                                              ABSC,
  B_cell .
                                     Granu.
                               TBSC
      CLDC, EDif, EPro, MTAC,
                                          0.9155
          ABSC, B_cell, CD4, CD8, CLDC, CLP, CMP, EDif, EPro, GMP, Granu, HSC,
      MEP, MPP1, MPP2, MTAC, Mono, TBSC
                                           0.8979
```

<sup>&</sup>lt;sup>3</sup>Notice that here, the ABSC sample is not present due to a too small correlation with the others, and therefore, is not present in the dendrogram.

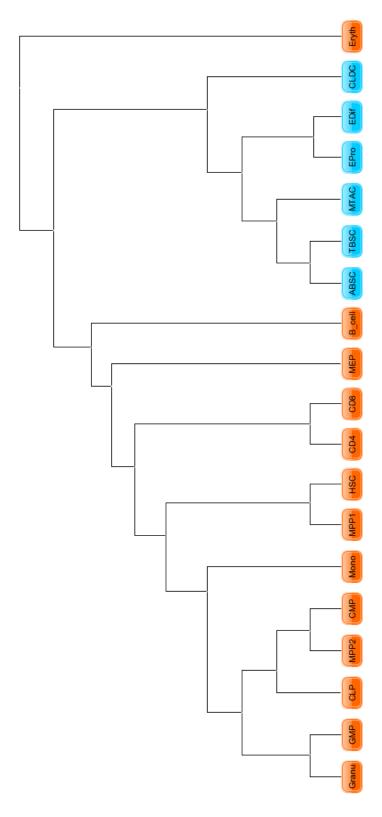


Figure 7: Dendrogram of the clustering in listing 7. The blue nodes are skin cells, and the orange one blood cells.

Listing 7: Hierarchical clustering example with expression data and Pearson correlation. The clustering is also separating the skin and blood cells very well.

```
o CLP
            MPP2
                      0.9904
  CMP
            GMP
                      0.9857
  MPP1
            {\rm CLP},\ {\rm MPP2}
                               0.9832
                      0.9733
  \operatorname{TBSC}
            ABSC
                     CLP, MPP1, MPP2 0.9712 0.9709
  CMP, GMP
5 CD8
            CD4
  EPro
            EDif
                      0.947
            CLP, CMP, GMP, MPP1, MPP2
                                                  0.9432
  HSC
  Mono
            Granu
                      0.9381
  B_cell
            CLP, CMP, GMP, HSC, MPP1, MPP2
            B_cell, CLP, CMP, GMP, HSC, MPP1, MPP2
10 MEP
                                                            0.9036
  MTAC
            ABSC, TBSC
                               0.8931
  CD4, CD8
                      Granu, Mono
                                         0.8842
                     ABSC, MTAC, TBSC
  {\rm EDif}\,,\ {\rm EPro}\,
                                                  0.872
            B_cell, CLP, CMP, GMP, HSC, MEP, MPP1, MPP2 0.8686
8, Granu, Mono B_cell, CLP, CMP, Eryth, GMP, HSC, MEP, MPP1, MPP2
  Eryth
15 CD4, CD8, Granu, Mono
              0.8549
            ABSC, EDif, EPro, MTAC, TBSC
                                                  0.8402
  B_cell, CD4, CD8, CLP, CMP, Eryth, GMP, Granu, HSC, MEP, MPP1, MPP2, Mono
               ABSC, CLDC, EDif, EPro, MTAC, TBSC
                                                                0.6466
```