Bioinformatics III

Third Assignment

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Exercise 3.1:

(a) Given the states of the features, you want to infer if two proteins are likely to physically interact. In practice, log-likelihood ratios are used in binary classification:

$$log \frac{P(C|S)}{P(\bar{C}|S)}$$

Derive a term that uses observable probabilities such as $P(S_i|C)$ to calculate the loglikelihood ratio from training data. How does the actual classification work?

First we have:

$$P(S_i|C) = \frac{P(C|S_i)P(S_i)}{P(C)}$$

And:

$$P(S_i|\bar{C}) = \frac{P(\bar{C}|S_i)P(S_i)}{P(\bar{C})}$$

Then we develop the desired final output

$$\frac{P(S_i|C)}{P(S_i|\bar{C})} \Longleftrightarrow \frac{P(S_i|C)P(C)}{P(S_i|\bar{C})P(\bar{C})} = \frac{P(C|S_i)P(S_i)}{P(\bar{C}|S_i)P(S_i)} = \frac{P(C|S_i)}{P(\bar{C}|S_i)}$$

$$log \frac{P(C|S)}{P(\bar{C}|S)} = log \prod_{i}^{n} \frac{P(S_i|C)P(C)}{P(S_i|\bar{C})P(\bar{C})} = \sum_{i}^{n} log \frac{P(S_i|C)P(C)}{P(S_i|\bar{C})P(\bar{C})} = \Lambda(C|S)$$

$$O(C|S) = \Lambda(C|S)O(C)$$

The posterior odd is calculated by the odds of an event $(\frac{p(event)}{1-p(event)})$ multiplied by the likelihood of that event¹.

To do the classification, we must interate through the data and calculate all the priors and likelihood. The prior P(C) is made from an educated guess

 $^{^1}$ Slides V4 - 4

(b) Shortly discuss: What are the practical advantages of the logarithm and the likelihood ratio within this framework? State two reasons why this particular type of classifier may perform poorly on a real world dataset.

The logarithm increase is a monotonically increasing function of x hence, for any positive value the maximum value of a function f(x), the maximum of f(x) is equal to the maximum of log(f(x)). This simplifies the calculation because we don't need the second derivative. A likelihood function is not concave but the log-likelihood is. Also, as seen in part A, with the log-likelihood we can turn a log of products into a sum of logs. The main inconvenient is that this method assume that all the features are independent and do not take in account the eventual correlations between them.

(c) Use the file training1.tsv to build a model. This basically means to determine all necessary priors and likelihoods from part (a). The file layout is explained in README.txt. Report P(C) and P(C

) as well as the ten S_i (feature number, variant and log-ratio) with the highest absolute log-likelihood ratios. Examine and comment on the results of the training-phase. Which features seem to be the most helpful?

Prior probability P(C) = 0.78Prior probability $P(\bar{C}) = 0.22$

Table 1: 10 S_i with the highest absolute log-likelihood ratio

Feature	Variant	log-ratio	
33	0	-3.7214026458194964	
11	3	-2.565631943311438	
87	1	-2.4686396773241284	
53	1	-2.3351082846996056	
99	1	-2.3061207478263537	
59	1	-2.2779498708596573	
80	2	-2.2779498708596573	
86	3	-2.2550655770260692	
91	3	-2.2173252490432223	
97	1	-2.2099451417455995	

The log likelihood ratio explains that if you have the variant X you have log(likelohood) more chance to have a complex (C). If negative, it diminishes this chance. To interpret the results above, if for the feature 33 you have variant 0, you have 3.7 more chance that it doesn't make a complex than with variant 1,2 or 3. So here the feature 33 is the most helpful. For the train and test 1 and 2 we obtain only 0's as a prediction which is not satisfying according to the real outputs.

Listing 1: bayes.py

```
o import math
  import copy
  \# For all features, compute the probability (prior) to have 0, 1, 2 or 3
      depending on the output (0 or 1)
  def priors(features, output_indexes):
      priors = \{\}
      # Start to 1 to match the instructions
      feature\_nb = 1
      for feature in features:
           P_Si_Output = \{\}
          # Values of the feature for a certain output (0 or 1)
10
          S = [feature[i] for i in output_indexes]
          \# for all possible feature values \rightarrow [0,1,2,3], set dynamically here
           for value in set (feature):
               # Prob of having this 'value' when output is 0 or 1 (depend on
                   output_{-}indexes)
               P_Si_Output [value] = S.count(value) / float(len(S))
15
           priors [feature_nb] = P_Si_Output
           feature_nb += 1
      return priors
20
  def log_likelihood(Prior_C, Prior_not_C, P_S_C, P_S_notC):
       log_like = [[0.0]*4 \text{ for } log_like = [[0.0]*4]
```

```
#For each feature
25
       \# Careful, in P_S_C it's a dict \rightarrow start at 1 as "feature 1"
       # in log_like it's a list of list \rightarrow feature 1 == [0]
       for feat in P_S_C:
            for val in [0,1,2,3]:
                p = math.log((P_S_C[feat][val] * Prior_C)/P_S_notC[feat][val] *
30
                     Prior_not_C)
                 \log_{-1} \text{like} [\text{feat} -1][\text{val}] = p
       return log_like
   # Returns the N max likelihood ratios
35 def getNMaxLikelihoodRatio(likelihoods, N):
       \# As we have to loop N times, we'll need to set the max value to zero
       # in order not to pick it more than once.
       "likelihoods_copy = copy.deepcopy(likelihoods)
       t = []
       for out in range(N):
40
            # Will contain (feature number, variant, absolute likelihood ratio)
            info = (0,0,0)
            max = 0
            for feat in range(len(likelihoods_copy)):
45
                 for val in range(len(likelihoods_copy[feat])):
                     if abs(likelihoods_copy[feat][val]) > max:
                         max = abs(likelihoods_copy[feat][val])
                          # Max is calculated with the abs, but the real value is
                          info = (feat, val, likelihoods_copy[feat][val])
50
                          likelihoods\_copy[feat][val] = 0.0
            t.append(info)
       return t
55
   # Read data file
   def readFile(filename):
       lines = []
       with open(filename) as f:
            for line in f:
                line = line.split(' \ ')
                map(str.strip , line)
65
                lines.append(line)
       # Convert all the elements in float instead of chars lines = [[float(i) for i in line] for line in lines]
       return lines
70
   lines = readFile("data/training1.tsv")
  \# Number of features
   nb_{\text{-}}features = len(lines[0]) - 1
75 print("Nb_features:_", nb_features)
   \# \ Get \ the \ data \ by \ columns: \ https://stackoverflow.com/questions/44360162/how-to-access-a-column-in-a-list-of-lists-in-python 
   data_columns = list(zip(*lines))
# Problem, columns are now tuples
so data_columns = [list(elem) for elem in data_columns]
   # Features only
   features = data_columns[1:]
85 # Output only
   outputs = list (data_columns [0])
   # Indexes according to outputs (1 or 0, first column)
```

```
interaction_indexes = [i for i,x in enumerate(outputs) if x == 1]
   no_interaction_indexes = [i for i,x in enumerate(outputs) if x == 0]
   # Prior probabilities
95 Prior_C = outputs.count(1) / float(len(outputs))
print("Prior_probability_of_having_a_connection:_", Prior_C)
   Prior_not_C = 1 - Prior_C
   \textbf{print} \, (\, "\, Prior\_probability\_of\_not\_having\_a\_connection:\_" \, , \, \, Prior\_not\_C \, )
100 # For each feature and possible value, calculate the probability according to
        the output
   \# P\_S\_C = Probability of having S (feature) according to output 1
   P_S_C = priors(features, interaction_indexes)
105 \# P\_S\_notC = Probability of having <math>S (feature) according to output 0
   P_S_notC = priors(features, no_interaction_indexes)
   \#\ Print\ every\ probabilities\ for\ every\ feature\ 's\ values
   \# print ("Features's values's probabilities if connection: \n")
110 # for p in P_S_C:
# print("Feature", p,
          for val in P_-S_-C[p]:
   #
               print("\tValue: ", val, "prob: ", P_S_C[p][val])
   #
115 # print ("Features's values's probabilities if no connection: \n")
   # for p in P_S_notC:
# print("Feature", p, ":")
          for val in P_S_notC[p]:
   #
               print("\t Value:", val, "prob:", P_S_notC[p][val])
120
   # Now we compute the log likelihood for every features and possible output
   log_like = log_likelihood(Prior_C, Prior_not_C, P_S_C, P_S_notC)
125 \#print(log_like)
   \# Get the N (ABSOLUTE) max log-likelihood ratios.
   maxLikelihoods = getNMaxLikelihoodRatio(log_like, 10)
130 # Nice printing
   for _ in maxLikelihoods:
        \mathbf{print}\left(\ _{-}\right)
   # Part D
135
   lines = readFile("data/test1.tsv")
   data\_columns = \dot{\mathbf{list}}(\dot{\mathbf{zip}}(*lines))
   data_columns = [list(elem) for elem in data_columns]
   features = data_columns[1:]
140 outputs = list (data_columns[0])
   print("Real_test_outputs:_")
   print(outputs)
145 predictiontmp = []
   for f in range(len(features)):
        tmp\_output = 0
        for v in [0,1,2,3]:
             tmp_output += log_like[f][v]
150
        predictiontmp.append(tmp_output)
   prediction = \begin{bmatrix} 0 & \textbf{if} & x < 0 & \textbf{else} & 1 & \textbf{for} & x & \textbf{in} & prediction tmp \end{bmatrix}
   print(prediction)
```

Exercise 3.2: Classify real-world network examples

(a) If one of the nodes has a degree of 1, then $\tilde{C}_{i,j}^{(3)}$ is infinite. What is the maximal finite value that the edge-clustering coefficient can take? For which configuration does this occur? Give an example!

The edge-clustering coefficient cannot be more than 2. In the layout below we see that the clustering coefficient for the link between node 2 and 3 is equal to $\tilde{C}_{2,3}^{(3)} = \frac{1+1}{\min(2-1,6-1)} = \frac{2}{1}$. We see that no matter the degree of node 3, if we connect more node to node 2 the coefficient will decrease even if the number of possible triplet increase.

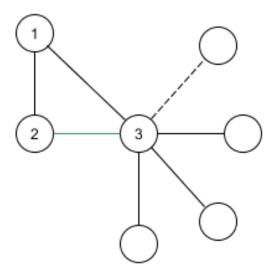


Figure 1:

(b) (1) Give the links that you deleted from the network in (iii) by printing the names of the two nodes and their current edge-clustering coefficient in the order of their deletion. Of course, add the output to the PDF/sheet that you hand in. Implement this part as a script or class-based, there are no specifications you need to adjust to.

Table 2: Output - Order of removed links

110	2. Output	Oraci or it	JIIIOVCA IIIIK
	Tyrion	Sansa	$0.33\bar{3}$
	Joffrey	Hound	0.5
	Eddard	Robert	0.5
	Eddard	Jon	0.5
	Joffrey	Jaime	1.0
	Hound	Mountain	1.0
	Cersei	Tyrion	1.0
	Jaime	Cersei	1.0
	Catelyn	Baelish	1.0
	Sansa	Baelish	1.0
	Eddard	Catelyn	1.5
	Sansa	Arya	1.5
	Eddard	Sansa	1.0
	Catelyn	Arya	1.0
	Joffrey	Cersei	2.0
	Cersei	Robert	1.0
	Samwell	Jon	2.0
	Joffrey	Robert	∞
	Shae	Tyrion	∞
	Eddard	Arya	∞
	Hound	Arya	∞
	Varys	Baelish	∞
	Jaime	Tyrion	∞
	Cersei	Mountain	∞
	Catelyn	Sansa	∞
	Samwell	Jeor	∞
	Jon	Jeor	∞

#print(net)

Implementation of the network decomposition:

Listing 2: testNetwork.py: decompose the network, output in table 2 o from GenericNetwork import GenericNetwork import sys net = GenericNetwork ("GoT.txt") $nb_links = net.nb_links$ removed_links_list = [None] * nb_links print (net) # for all the links for current_link in range(nb_links): $min_coeff = sys.maxsize$ # Iterate through all the links for node_a in net.nodes: 15 for node_b in net.nodes: node1 = net.getNode(node_a) $node2 = net.getNode(node_b)$ # if the two nodes are different and are linked, check if the 20 coeff is smaller or equal than nim_coeff if (node1 != node2 and node1.hasLinkTo(node2) and net. edgeClusterCoeff(node1, node2) <= min_coeff): # We have a temp minimal cluster coeff between node1 and node2 min_coeff = net.edgeClusterCoeff(node1, node2) $\verb|removed_links_list[current_link]| = (\verb|node1|, \verb|node2|, \verb|min_coeff|)|$ # Nodes to remove (for now, they will be after the loops) 25 $buffer_node1 = node1$ $buffer_node2 = node2$ # Here we have the minimal cluster with (node1, node2, coeff) in $removed_links_list$ 30 # To be sure that there is no mistakes if (buffer_node1 . hasLinkTo(buffer_node2)) : net.removeLink(buffer_node1, buffer_node2) print("Link_removed:_", buffer_node1, "_", buffer_node2, "_", min_coeff) 35 print("Warning:_node_", buffer_node1, "_and_", buffer_node2, "_have_no

Implementation of the other classes. New functions have been added directly in the Network classes.

Listing 3: Node.py

```
o # Node class, assignment 1
  class Node:
      def __init__(self , identifier):
           Sets\ node\ id\ and\ initialize\ empty\ node\ list\ that\ references\ its
           connected nodes
5
           self.id = identifier
           self.nodelist = []
      def hasLinkTo(self, node):
10
           Returns True if this node is connected to node asked for,
           False\ otherwise
          return (node in self.nodelist)
15
      def addLinkTo(self, node):
           Adds link from this node to parameter ode (only if there is no link
               connection already),
           does not automatically care for a link from parameter node to this
              node
20
           if (~self.hasLinkTo(node)):
               self.nodelist.append(node)
      def degree (self):
25
           Returns degree of this node
          return len (self.nodelist)
      30
           Returns id of node as string
          return str(self.id)
35
      def getNodeSet(self):
          return set (self.nodelist)
      Remove node from neighbours list
40
      def removeNode(self, node):
           self.nodelist.remove(node)
                           Listing 4: AbstractNetwork.py
o from Node import Node
  import sys
  {\bf class}\ {\bf AbstractNetwork:}
       """Abstract network definition, can not be instantiated"""
5
      \mathbf{def}_{n,n} = \inf_{n \in \mathbb{N}} (self, amount_nodes, amount_links):
           Creates empty nodelist and call createNetwork of the extending class
           self.nodes = \{\}
10
           self.__createNetwork__(amount_nodes, amount_links)
```

```
\mathbf{def} \ \_\mathtt{createNetwork} \_\mathtt{(self, amount\_nodes, amount\_links)} :
15
            Method overwritten by subclasses, nothing to do here
            raise NotImplementedError
       def appendNode(self, node):
20
            Appends node to network
            self.nodes[node.id] = node
25
       def maxDegree(self):
            Returns the maximum degree in this network
            return max([x.degree() for x in self.nodes.values()])
30
       def size (self):
            Returns network size
35
            return len (self.nodes)
       def __str__(self):
            Any string-representation of the network (something simply is enough)
40
            # will contain: {identifier : neighbours} -> dict are printed pretty
                 nicely
            self.networkdict = {}
            for n in self.nodes.values():
                 \# n is a node \rightarrow contains identifier and neighbours
45
                 nblist = []
                 for elem in n.nodelist:
                      nblist.append(elem.id)
                 self.networkdict[n.id] = nblist
50
            \label{eq:niceprint} \begin{array}{ll} \mbox{niceprint} = \mbox{str}(("\n".join("\{\}\t\t\{\}".\mbox{format}(k,\ v)\ \mbox{for}\ k,\ v\ \mbox{in}\ \mbox{self}\,. \\ \mbox{networkdict.items}())) + "\n\n") \end{array}
            \mathbf{return} \ \mathtt{niceprint}
       def getNode(self , identifier):
55
            Returns node according to key
            if identifier not in self.nodes:
                 self.nodes[identifier] = Node(identifier)
60
            return self.nodes[identifier]
       def degreeSum(self):
65
            :return: sum of all degrees of the network (a bit unefficient )
            sum = 0
            for key, node in self.nodes.items():
70
                sum += node.degree()
            return sum
       def removeLink(self, node1, node2):
            if node1.hasLinkTo(node2) and node2.hasLinkTo(node1):
75
                 node1.removeNode(node2)
                 node2.removeNode(node1)
```

```
else:
                 print("Cannot_remove_link_between_", str(node1), "_and_", str(
                      node2))
80
       \mathbf{def}\ \operatorname{nbTriangle}\left(\,\operatorname{self}\;,\;\operatorname{node1}\;,\;\operatorname{node2}\,\right):
            if(not node1.hasLinkTo(node2)):
                 return 0
            else:
                 # Intersection is part of "set"
85
                 intersect = set (node1.nodelist).intersection(node2.nodelist)
                 return len(intersect)
       \mathbf{def}\ \mathtt{edgeClusterCoeff}\,(\,\mathtt{self}\;,\;\,\mathtt{node1}\;,\;\,\mathtt{node2}\,):
            if(node1.degree()-1 == 0 \text{ or } node2.degree()-1 == 0):
90
                 return sys.maxsize
            else:
                 return (self.nbTriangle(node1, node2) + 1) / float(min(node1.
                      degree() - 1, node2.degree() - 1))
                                Listing 5: GenericNetwork.py
o from AbstractNetwork import AbstractNetwork
  from Node import Node
  # from standard library module
  from itertools import islice
5 import sys
  class GenericNetwork(AbstractNetwork):
       def __init__(self, filename):
10
            Create a network from a file
            self.nodes = \{\}
15
            self.nb_links = 0
            # We first need to create all Nodes (unique)
            allEntries = []
            pairs = []
20
            with open(filename) as f:
                 # Run through the entire file to make a set of entries
                 for line in f:
                      line = line.rstrip()
                      line_tab = line.split('-')
                      pairs.append(line_tab)
                      allEntries.extend(line_tab)
30
                 allUniqueEntries = set(allEntries)
                 for n in allUniqueEntries:
                      self.appendNode(Node(n))
                 for pair in pairs:
35
                      self.nb_links += 1
                      self.getNode(pair [0]).addLinkTo(self.getNode(pair [1]))self.getNode(pair [1]).addLinkTo(self.getNode(pair [0]))
```

(2) Use the links deleted in (1) in reverse order, i.e., the link that was deleted last is now used first to construct the communities.

Table 3: Inclusion of links, "x[number]" means two subgraphs have been merged. To visualize which subgraphs are merged, refer to figure 2. Colours are added to ease the visualisation in the beginning but then subgraph's number are used to indicate which ones are concerned by the merge.

Link	Merge	Graph	Sub.Gr
Jon - Jeor		[(Jon - Jeor)]	1
Samwell - Jeor		[(Jon - Jeor),(Samwell - Jeor)]	2
Catelyn - Sansa		[(Catelyn - Sansa)]	3
Cersei - Mountain		[(Cersei - Mountain)]	4
Jaime - Tyrion		[(Jaime - Tyrion)]	5
Varys - Baelish		[(Varys - Baelish)]	6
Hound - Arya		[(Hound - Arya)]	7
Eddard - Arya		[(Hound - Arya),(Eddard - Arya)]	8
Shae - Tyrion		[(Jaime - Tyrion),(Shae - Tyrion)]	9
Joffrey - Robert		[(Joffrey - Robert)]	10
Samwell - Jon		[(Jon - Jeor),(Samwell - Jeor),(Samwell - Jon)]	11
Cersei - Robert	x1 (4+10)	[(Cersei - Mountain), (Joffrey - Robert), (Cersei - Robert)]	12
Joffrey - Cersei		[(Cersei - Mountain),(Joffrey - Robert), (Cersei - Robert),(Joffrey - Cersei)]	13
Catelyn - Arya	x2 (3+8)	[(Catelyn - Sansa),(Hound - Arya),(Eddard - Arya), (Catelyn - Arya)]	14
Eddard - Sansa		[(Catelyn - Sansa),(Hound - Arya),(Eddard - Arya), (Catelyn - Arya),(Eddard - Sansa)]	15
Sansa - Arya		[(Catelyn - Sansa),(Hound - Arya),(Eddard - Arya), (Catelyn - Arya),(Eddard - Sansa),(Sansa - Arya)]	16
Eddard - Catelyn		[(Catelyn - Sansa),(Hound - Arya),(Eddard - Arya),(Catelyn - Arya), (Eddard - Sansa),(Sansa - Arya), (Eddard - Catelyn)]	17
Sansa - Baelish	x3 (17+6)	[(Varys - Baelish),(Sansa - Baelish),(Catelyn - Sansa), (Hound - Arya),(Eddard - Arya),(Catelyn - Arya), (Eddard - Sansa),(Sansa - Arya),(Eddard - Catelyn)]	18
Catelyn - Baelish		[(Varys - Baelish),(Sansa - Baelish),(Catelyn - Sansa), (Hound - Arya),(Eddard - Arya),(Catelyn - Arya), (Eddard - Sansa),(Sansa - Arya),(Eddard - Catelyn), (Catelyn - Baelish)]	19
Jaime - Cersei	x4 (9+13)	[(Jaime - Tyrion),(Shae - Tyrion), (Cersei - Mountain),(Joffrey - Robert), (Cersei - Robert), (Jeoffrey, Cersei)]	20
Cersei - Tyrion		[(Jaime - Tyrion),(Shae - Tyrion),(Cersei - Mountain), (Joffrey - Robert), (Cersei - Robert),(Joffrey - Cersei), (Cersei - Tyrion)]	21

Link	Merge	Graph	Subgraph
Hound - Mountain	x5 (21 + 19)	[(Varys - Baelish),(Sansa - Baelish),(Catelyn - Sansa), (Hound - Arya),(Eddard - Arya),(Catelyn - Arya), (Eddard - Sansa),(Sansa - Arya),(Eddard - Catelyn), (Catelyn - Baelish),(Jaime - Tyrion),(Shae - Tyrion), (Cersei - Mountain),(Joffrey - Robert), (Cersei - Robert), (Joffrey - Cersei),(Cersei - Tyrion), (Hound - Mountain)]	22
Joffrey - Jaime		[(Varys - Baelish),(Sansa - Baelish),(Catelyn - Sansa), (Hound - Arya),(Eddard - Arya),(Catelyn - Arya), (Eddard - Sansa),(Sansa - Arya),(Eddard - Catelyn), (Catelyn - Baelish),(Jaime - Tyrion),(Shae - Tyrion), (Cersei - Mountain),(Joffrey - Robert), (Cersei - Robert), (Joffrey - Cersei),(Cersei - Tyrion),(Joffrey - Jaime)]	23
Eddard - Jon	x6 (23 + 2)	[(Varys - Baelish),(Sansa - Baelish),(Catelyn - Sansa), (Hound - Arya),(Eddard - Arya),(Catelyn - Arya), (Eddard - Sansa),(Sansa - Arya),(Eddard - Catelyn), (Catelyn - Baelish),(Jaime - Tyrion),(Shae - Tyrion), (Cersei - Mountain),(Joffrey - Robert), (Cersei - Robert), (Joffrey - Cersei),(Cersei - Tyrion),(Joffrey - Jaime), (Jon - Jeor),(Samwell - Jeor),(Samwell - Jon)]	24
Eddard - Robert		[(Varys - Baelish),(Sansa - Baelish),(Catelyn - Sansa), (Hound - Arya),(Eddard - Arya),(Catelyn - Arya), (Eddard - Sansa),(Sansa - Arya),(Eddard - Catelyn), (Catelyn - Baelish),(Jaime - Tyrion),(Shae - Tyrion), (Cersei - Mountain),(Joffrey - Robert), (Cersei - Robert), (Joffrey - Cersei),(Cersei - Tyrion),(Joffrey - Jaime), (Jon - Jeor),(Samwell - Jeor),(Samwell - Jon), (Eddard - Robert)]	25
Joffrey - Hound		[(Varys - Baelish),(Sansa - Baelish),(Catelyn - Sansa), (Hound - Arya),(Eddard - Arya),(Catelyn - Arya), (Eddard - Sansa),(Sansa - Arya),(Eddard - Catelyn), (Catelyn - Baelish),(Jaime - Tyrion),(Shae - Tyrion), (Cersei - Mountain),(Joffrey - Robert), (Cersei - Robert), (Joffrey - Cersei),(Cersei - Tyrion),(Joffrey - Jaime), (Jon - Jeor),(Samwell - Jeor),(Samwell - Jon), (Eddard - Robert),(Joffrey - Hound)]	26
Tyrion - Sansa		[(Varys - Baelish),(Sansa - Baelish),(Catelyn - Sansa), (Hound - Arya),(Eddard - Arya),(Catelyn - Arya), (Eddard - Sansa),(Sansa - Arya),(Eddard - Catelyn), (Catelyn - Baelish),(Jaime - Tyrion),(Shae - Tyrion), (Cersei - Mountain),(Joffrey - Robert), (Cersei - Robert), (Joffrey - Cersei),(Cersei - Tyrion),(Joffrey - Jaime), (Jon - Jeor),(Samwell - Jeor),(Samwell - Jon), (Eddard - Robert),(Joffrey - Hound),(Tyrion - Sansa)]	27

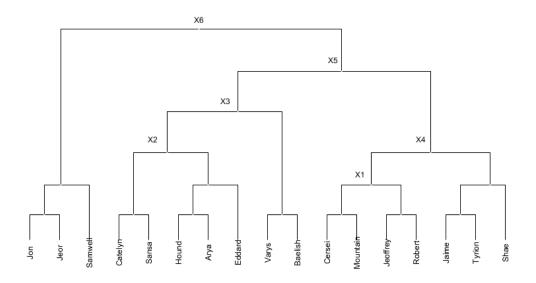


Figure 2: Dendogram

(c) Visualisation of the communities

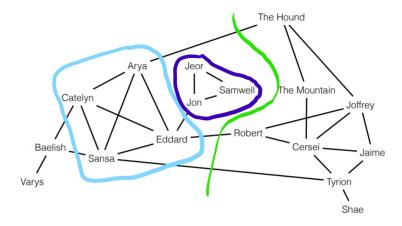


Figure 3: Visualisation of the network

Here we can identify many communities. The two biggest are the ones we can have by separating the network in the middle (In green). All the nodes have more links inside the communities than outside.

Table 4: The two big communities of the network separated by the green line. All the nodes not cited below have $k_{out} = 0$.

Node	k_{in}	k_{out}
Arya	3	1
Eddard	3	1
Sansa	3	1
The Hound	2	1
Robert	2	1
Tyrion	3	1

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Here is two disjointed examples:

Table 5: Stark community in light blue. Each member have a k_{in} bigger than the k_{out} so the strong criterion applies.

Node	k_{in}	k_{out}
Catelyn	3	1
Arya	3	1
Eddard	3	2
Sansa	3	2

Table 6: Jon's community in dark blue, the strong criterion applies too.

Node	k_{in}	k_{out}
Jon	2	1
Jeor	2	0
Samwell	2	0