LogLogistic

Parametrisation

The LogLogistic distribution has cumulative distribution function

$$F(y) = \frac{1}{1 + (y/\beta)^{-\alpha}}$$

where

 $\alpha > 0$ is the shape parameter.

 $\beta > 0$ is the scale parameter.

Link-function

The parameter β is linked to the linear predictor as:

$$\beta = \exp(\eta)$$

Hyperparameters

The α parameter is represented as

$$\theta = \log \alpha$$

and the prior is defined on θ .

Specification

- \bullet family = loglogistic
- Required arguments: y (to be given in a format by using inla.surv() function)

Hyperparameter spesification and default values

doc The log-logistic likelihood (survival version)

hyper

theta

hyperid 80001

name log alpha

short.name alpha

initial 1

fixed FALSE

prior loggamma

param 25 25

to.theta function(x) log(x)

from.theta function(x) exp(x)

survival TRUE

discrete FALSE

link default log neglog

pdf loglogistic

Example

In the following example we estimate the parameters in a simulated case

```
rloglogistic = function(n, beta, alpha = 1)
{
    p = runif(n)
    return (beta* (((1-p)/p)^(-1/alpha)))
}

n = 1000
alpha = 2
x = runif(n)
eta = 1+x
beta = exp(eta)
y = rloglogistic(n, beta = beta, alpha = alpha)
event = rep(1,n)
data = list(y=y, event=event, x=x)
formula=inla.surv(y,event) ~ x
r=inla(formula, family ="loglogistic", data=data, verbose=T)
```

Notes

- Loglogistic model can be used for right censored, left censored, interval censored data.
- A general frame work to represent time is given by inla.surv
- If the observed times y are large/huge, then this can cause numerical overflow in the likelihood routines giving error messages like

```
file: smtp-taucs.c hgid: 891deb69ae0c date: Tue Nov 09 22:34:28 2010 +0100 Function: GMRFLib_build_sparse_matrix_TAUCS(), Line: 611, Thread: 0 Variable evaluates to NAN/INF. This does not make sense. Abort...
```

If you encounter this problem, try to scale the observatios, time = time / max(time) or similar, before running inla().