

## LogLogistic likelihoods

### Parametrisation

The LogLogistic distribution has cumulative distribution function

$$F_0(y) = \frac{1}{1 + \lambda y^{-\alpha}}, \quad y > 0$$

or

$$F_1(y) = \frac{1}{1 + (\lambda y)^{-\alpha}}, \quad y > 0$$

where

$\alpha > 0$  is a shape parameter, and

$\lambda > 0$  is a scale parameter.

The subscript indicated variant 0 and 1.

### Link-functions

The parameter  $\lambda$  is linked to the linear predictor, by default as

$$\lambda = \exp(\eta)$$

### Hyperparameters

The  $\alpha$  parameter is represented as

$$\theta = \log \alpha$$

and the prior is defined on  $\theta$ .

### Specification

- `family` equals `loglogistic` (regression) or `loglogisticsurv` (survival)
- `variant=0` (default) or 1 (choosing between parameterisation  $F_0$  or  $F_1$ ).
- Required arguments:  $y$  (regression) or an `inla.surv`-object using `inla.surv()`

### Hyperparameter spesification and default values

#### Regression:

**doc** The loglogistic likelihood

#### hyper

##### theta

**hyperid** 80001

**name** log alpha

**short.name** alpha

**initial** 1

**fixed** FALSE

**prior** loggamma

**param** 25 25

```
to.theta function(x) log(x)
from.theta function(x) exp(x)
```

**status** changed:Oct.25.2017

**survival** TRUE

**discrete** FALSE

**link** default log neglog

**pdf** loglogistic

### **Survival:**

**doc** The loglogistic likelihood (survival)

**hyper**

**theta**

```
hyperid 80011
name log alpha
short.name alpha
initial 1
fixed FALSE
prior loggamma
param 25 25
to.theta function(x) log(x)
from.theta function(x) exp(x)
```

**status** changed:Oct.25.2017

**survival** TRUE

**discrete** FALSE

**link** default log neglog

**pdf** loglogistic

### **Example**

In the following example we estimate the parameters in a simulated case

```
rloglogistic = function(n, beta, alpha = 1)
{
  p = runif(n)
  return (beta* (((1-p)/p)^(-1/alpha)))
}
```

```
n = 1000
alpha = 2
x = runif(n)
eta = 1+x
beta = exp(eta)
```

```
y = rloglogistic(n, beta = beta, alpha = alpha)
event = rep(1,n)
data = list(y=y, event=event, x=x)
formula=inla.surv(y,event) ~ x
r=inla(formula, family ="loglogistic", data=data, verbose=T)
```

Notes