Classical Cryptography

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Example and definitions of a cryptosystem

Caesar Cipher - the oldest cryptosystem

A shift cipher – attributed to Julius Caesar (100-44 BC)

MEET ME AFTER THE TOGA PARTY

PHHW PH DIWHU WKH WRJD SDUWB

Shift the alphabet 23 places to the right and substitute letters

abcdefghijklmnopqrstuvwxyz

DEFGHIJKLMNOPQRSTUVWXYZABC

Communication over an insecure medium

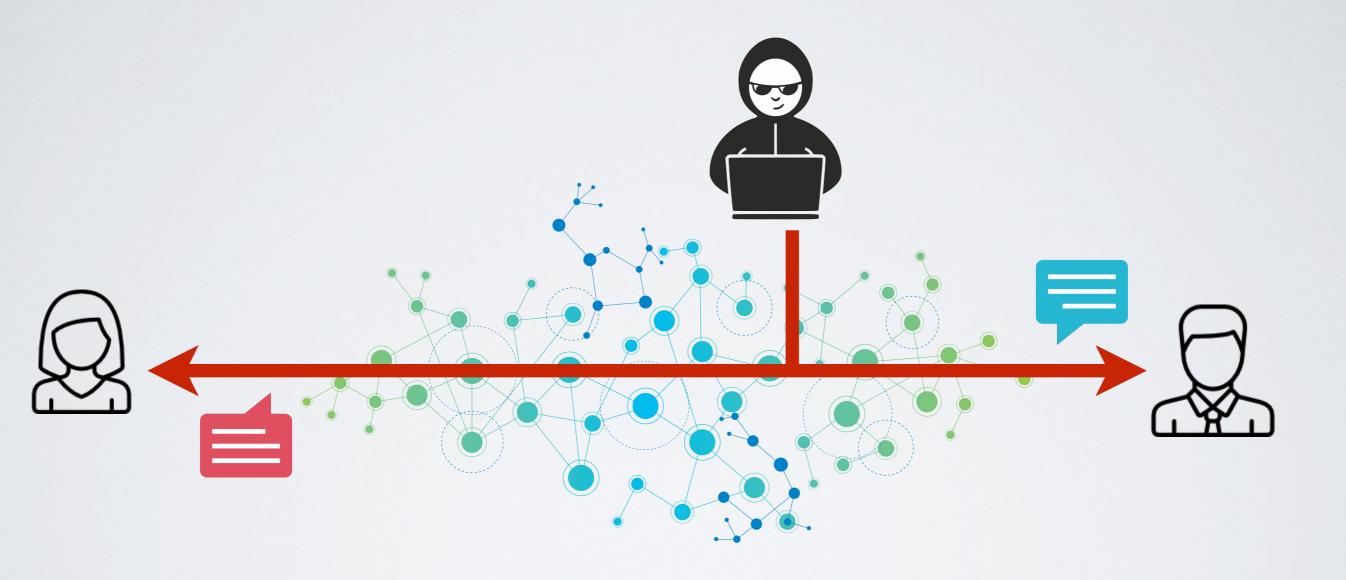


Threat | - Interception



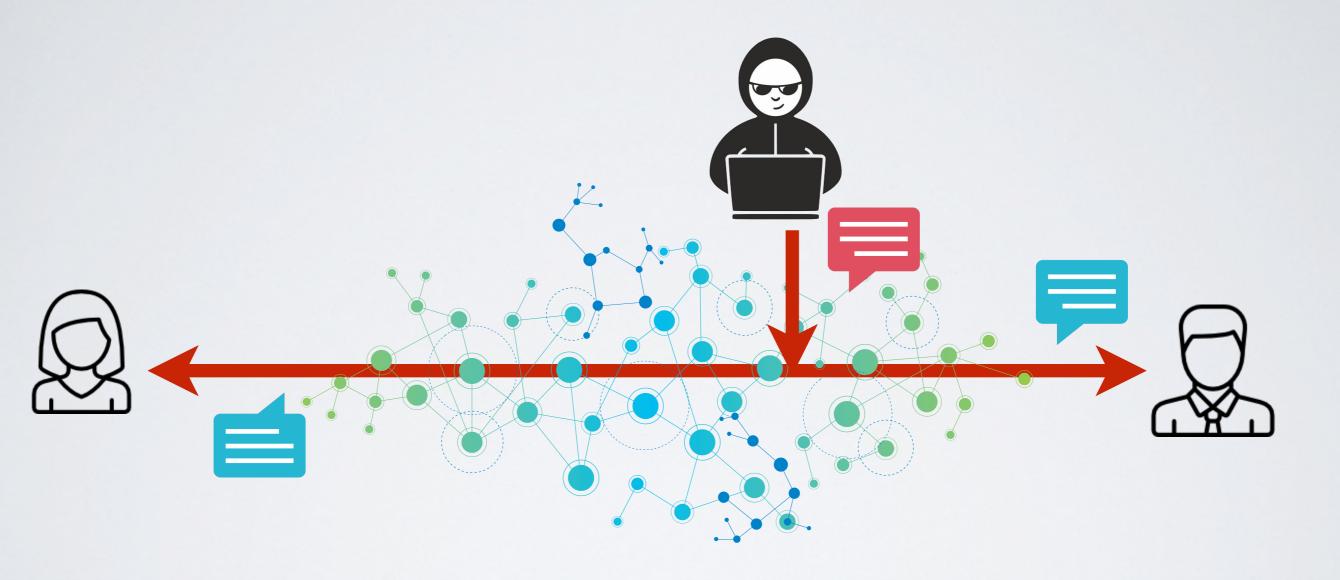
• Interception : an attacker can <u>read</u> messages

Threat 2 - Modification



Modification : an attacker can modify messages

Threat 3 - Fabrication



• Fabrication : an attacker can inject messages

Threat 4 - Interruption



• Interruption : an attacker can block messages

Confidentiality and Integrity of communications



→ Implement a virtual trusted channel over an insecure medium

Definitions

Plaintext

The message in its clear form (the original message)

Ciphertext

The message in its ciphered form (the encrypted message)

Encryption

Transform a plaintext into ciphertext

Decryption

Transform a ciphertext into a plaintext

Definitions

Cryptographic algorithm

The method to do encryption and decryption

Cryptographic key

An input variable used by the algorithm for the transformation

N-bit security entropy (a.k.a. the key space)
The number of bits necessary to encode the number of possible keys (could be different than the key length)

Representing data as numbers

Cryptographic algorithms are mathematical operations

→ messages and keys must be represented as numbers for instance : ASCII encoding

Back to Caesar Cipher

Algorithm: shift the alphabet of a certain number of positions

Key: the number of positions to shift

Key space : 25 possible rotations (~ 5 bits security)

Encoding:

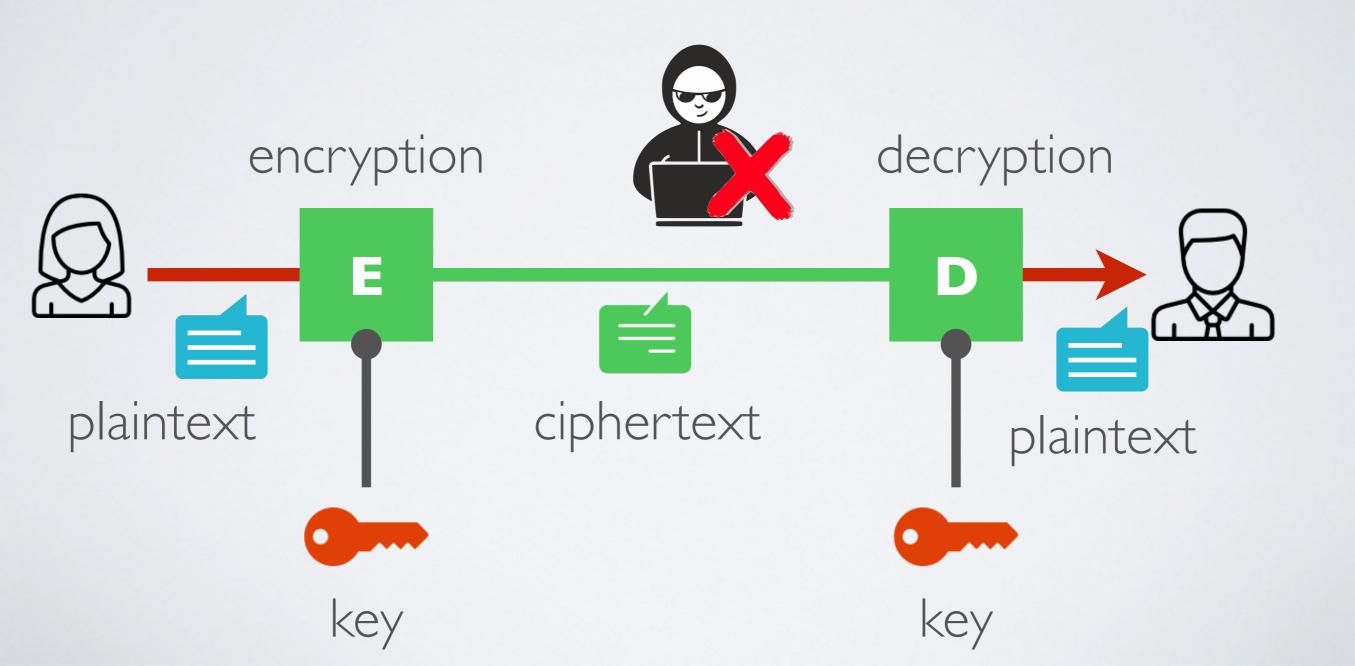
```
a b c d e f g h i j k l m n o p q r s t u v w x y z
0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25
```

Encrypting and decrypting one character is obtained as follows:

$$c = E(k,p) = (p + k) \mod 26$$

$$p = D(k,c) = (c - k) \mod 26$$

The big picture



Breaking the cipher

The Kerckhoffs' principle (1883)

"The enemy knows the system" - the security of a communication should not rely on the fact that the algorithms are secrets

→ A cryptosystem should be secure even if everything about the system, except the key, is public knowledge

No security by obscurity

Breaking the cipher - the attacker's model

- Exhaustive Search (a.k.a brute force)
 Try all possible n keys (in average it takes n/2 tries)
- Ciphertext only
 You know one or several <u>random ciphertexts</u>
- Known plaintext
 You know one or several pairs of <u>random plaintext</u> and their corresponding ciphertexts
- Chosen plaintext
 You know one or several pairs of chosen plaintext and their corresponding ciphertexts
- Chosen ciphertext
 You know one or several pairs of plaintext and their corresponding chosen ciphertexts
- **→** A good crypto system resists all attacks

Breaking Caesar cipher

| Exhaustive search | Yes |
|-------------------|--|
| ciphertext only | Statistical Analysis |
| known plaintext | Look at the first letter and get the shift |
| chosen plaintext | Choose "A" and get the shift |
| chosen ciphertext | Choose "A" and get the shift |

Statistical Cryptanalysis

→ Monoalphabetic ciphers do not change the relative frequency of letters in a message

Evolution of cryptosystems

A brief history of cryptography

| ~ 2000 years ago | Substitution ciphers (a.k.a mono alphabetic ciphers) |
|---------------------|---|
| few centuries later | Transposition ciphers |
| Renaissance | Polyalphabetic ciphers |
| 1844 | Mechanization |
| 1976 | Public key cryptography |

Substitution ciphers (a.k.a mono alphabetic ciphers)

→ Improvement over Caesar cipher

Algorithm: allow an arbitrary permutation of the alphabet

Key: set of substitutions

Key space : 26! possible substitutions ($4 \times 10^{26} \sim 89$ bits)

```
abcdefghijklmnopqrstuvwxyz
DKVQFIBJWPESCXHTMYAUOLRGZN
```

if we wish to replace letters WI RF RWAJ UH YFTSDVF SFUUFYA

Breaking substitution ciphers

| Exhaustive search | Doable with a computer |
|-------------------|--------------------------------|
| ciphertext only | Statistical analysis |
| known plaintext | Match letters together |
| chosen plaintext | Choose ABCDE and match letters |
| chosen ciphertext | Choose ABCDE and match letters |

Polyalphabetic ciphers (a.k.a Renaissance Cipher)

→ Vigenere cipher

Algorithm: combine the message and the key

Key: a word

Key space: the length of the word

wearediscoveredsaveyourself

+ deceptivedeceptive (mod 26)
ZICVTWQNGRZGVTWAVZHCQYGLMGJ

Advantage: Encryption of a letter is context dependent

Breaking Polyalphabetic Ciphers

| exhaustive search | Small key length only |
|-------------------|--|
| ciphertext only | Statistical analysis for small key length and significant amount of ciphertext |
| known plaintext | Subtract plaintext from ciphertext |
| chosen plaintext | Choose AAAAA and match letters |
| chosen ciphertext | Choose AAAAA and match letters |

OTP - One Time Pad

→ Improvement over Vigenere cipher

Algorithm: combine the message and the key

Key: an infinite random string

Key space: infinite

whatanicedaytoday

yksuftgoarfwpfwel

ZZZJUCLUDTUNNWGQS

Advantage: this is the perfect cipher!

Disadvantage: hard to use in practice, how to transmit the key?

The impossibility of breaking OTP

The ciphertext bears no statistical relationship to the plaintext

→ No statistical analysis

For any plaintext and ciphertext, there exists a key mapping one to the other, and all keys are equally probable

→ A ciphertext can be decrypted to any plaintext of the same length

Transposition Cipher

Algorithm: switch letters around a permutation

Key: a set of permutation

Key space: the set of permutations

helloworld LOLHERDLWO

Breaking Transposition ciphers

| brute force | Small key length only |
|-------------------|--------------------------------|
| ciphertext only | Hard for large permutations |
| known plaintext | Match letters together |
| chosen plaintext | Choose ABCDE and match letters |
| chosen ciphertext | Choose ABCDE and match letters |

The seeds of modern cryptography

. Diffusion

Mix-up symbols
Transposition Cipher

2. Confusion

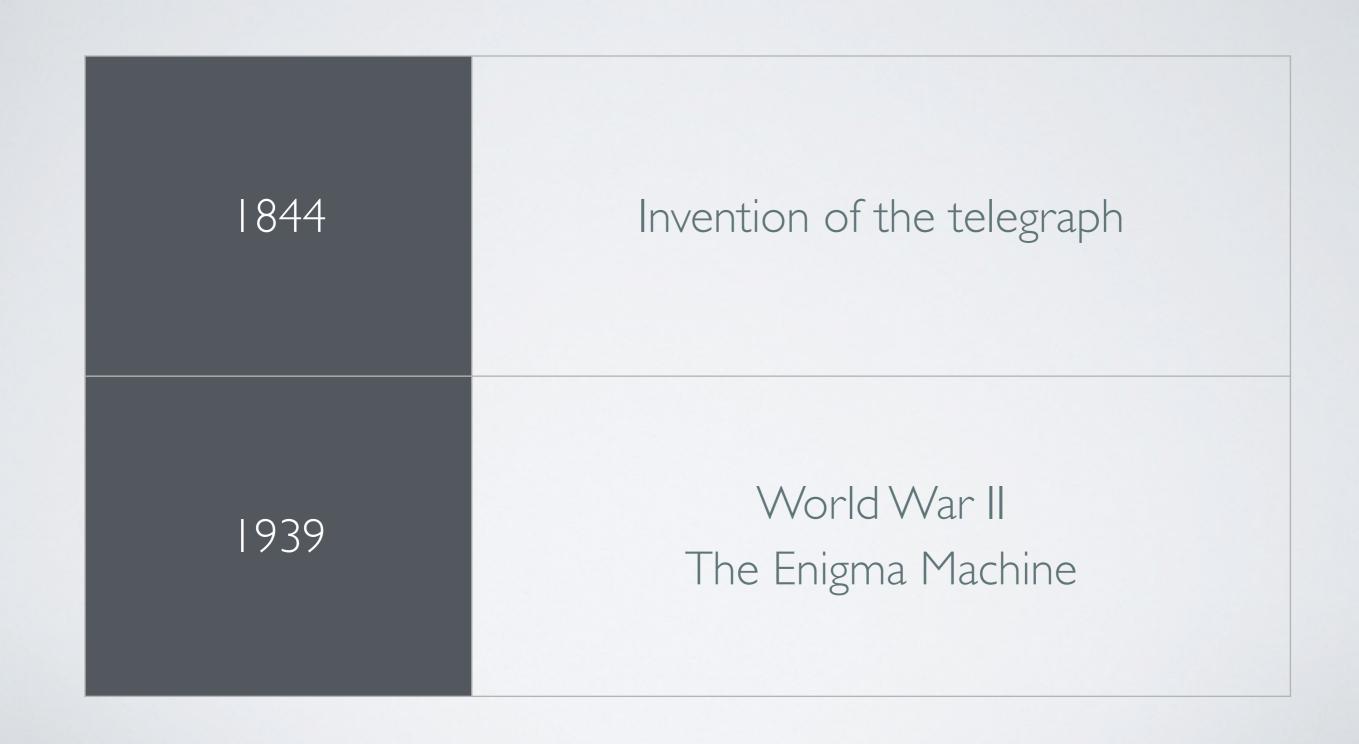
Replace a symbol with another Polyaphabetic Cipher

3. Randomization

Repeated encryption of the same text are different OTP

Mechanization

Mechanization



The cryptography toolbox

Cryptography is not just a about confidentiality

Integrity

digital signatures, hash functions

Non-repudiation

contract-signing

Anonymity

electronic cash, electronic voting

. . .

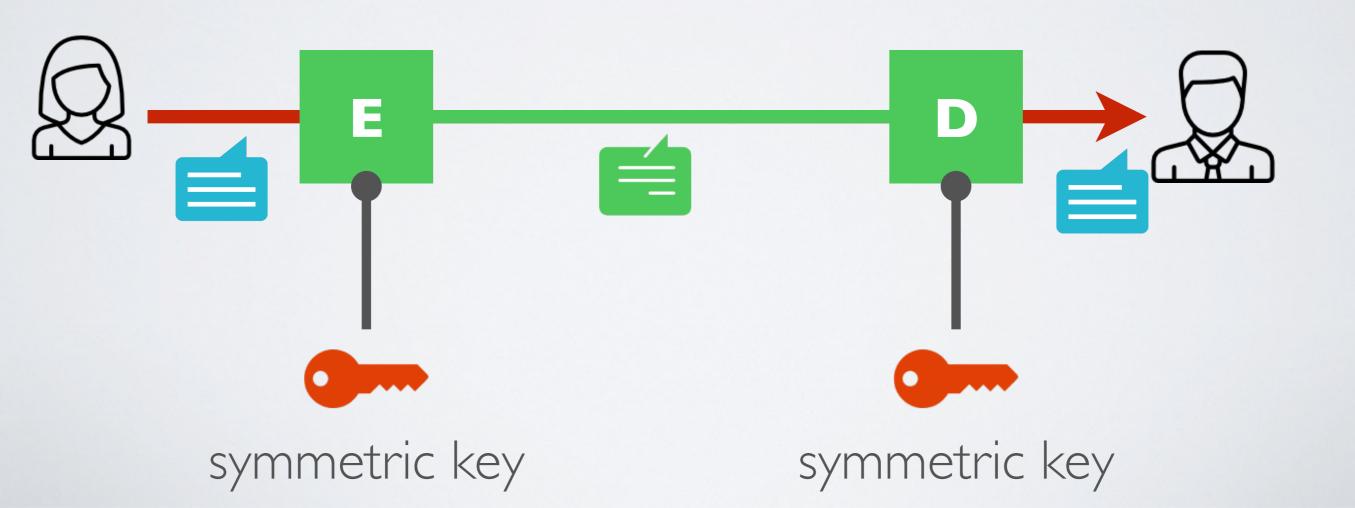
Availability

The crypto toolbox

- Symmetric cryptography schemes
- Asymmetric cryptography schemes
- Message digests
- Digital signatures
- Certificates

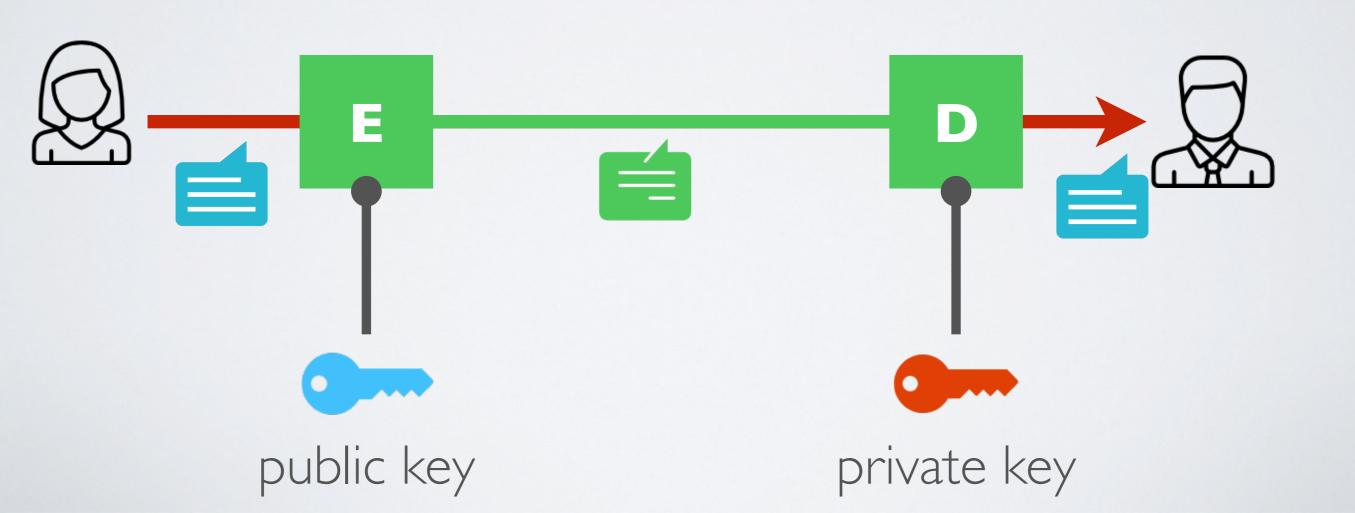
Symmetric encryption

The same key is used for encryption and decryption



Asymmetric encryption a.k.a Public Key Cryptography

- → The public key for encryption
- → The private key for decryption



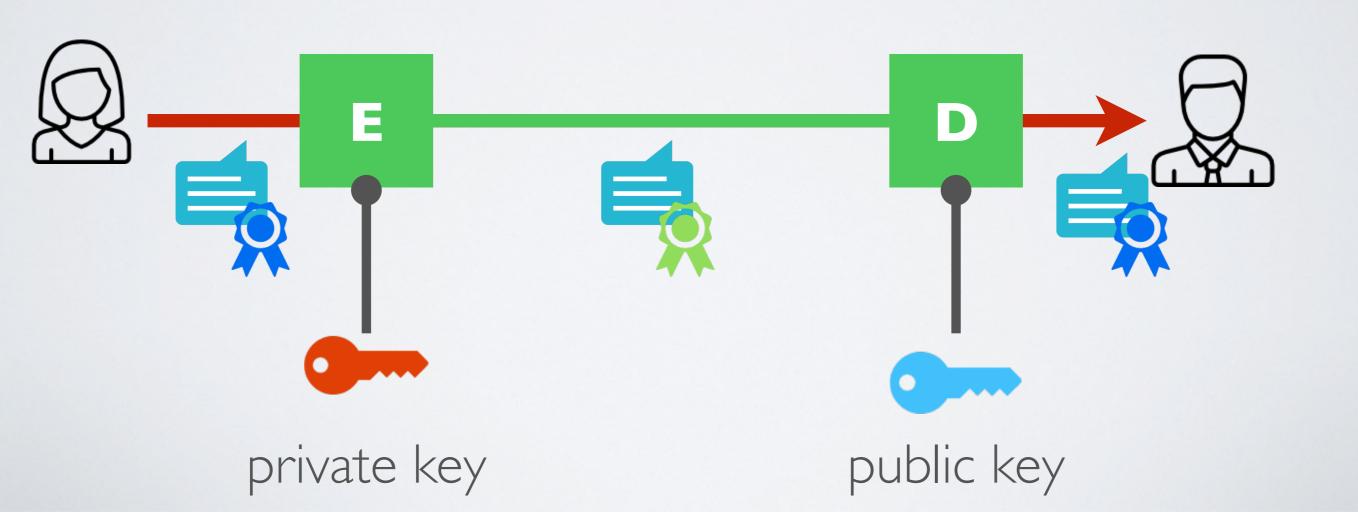
Message digests

Message digests are meant for creating fingerprints of messages

- Un-keyed message digest: hashes, checksum
- Keyed message digests : MACs

Digital Signature

- → The private key for encryption
- → The public key for decryption



Certificates - Public Key Infrastructure

Certificates are meant for verifying someone's identity

- Binding between a public key and an owner
- Certified by a certification authority