from sympy import *

TÀI LIỆU ĐƯỢC SỬ DỤNG CHO MÔN THI TOÁN TOÁN HỌC TÍNH TOÁN

Họ tên : Tạ Công Hiếu MSSV : 0011168 # VD2, 3: import numpy as np f = lambda x, y: y - x # VD2: f = lambda x, y: np.array([x * y[0] - y[1],y[0] + y[1] - 1])# VD3: f = lambda x, y: np.array([y[1], y[2], x *y[2] - y[0]X = [0, 0.2, 0.3, 0.5] # VD2: X = [1, 1.1, 1.3, 1.5]# VD3: X = [-1, -0.8, -0.6, -0.5]6 y = 2# VD2: y = [-1, 2]# VD3: y = [1, 0,8 for n in range(3): h = X[n+1] - X[n]y = y + h * f(X[n], y)print(y) $_{3}$ (-3*Y[0] + 4*Y[1] - Y[2]) 4 [(Y[i+1] - Y[i-1]) / 2 / h for i in range(1, 10)] 5 (3*Y[10] - 4*Y[9] + Y[8]) / 2 / h6 (Y[2] - 2*Y[1] + Y[0]) / h**2[(Y[i+1] - 2*Y[i] + Y[i-1]) / h**2 for i in range(1, 10)](Y[10] - 2*Y[9] + Y[8]) / h**2sum([(X[i] - X[i-1]) * (Y[i] + Y[i-1]) / 2 for i in range(1, 11)]) sum([(X[2*i] - X[2*i-2]) * (Y[2*i] + 4*Y[2*i-1] + Y[2*i-2]) / 6]for i in range(1, 6)]) Mã 2:

Nguyễn Đức Thịnh 1 thinhnd@huce.edu.vn

```
g = lambda x: root(x**2 + 3, 3)
x = symbols('x')
_{4} plot(g(x), (x, 1, 4))
5 plot(abs(g(x).diff()), (x, 1, 4))
q = 0.38
7 \times 0 = 2.5
                                             # x_{n-1}
8 for _ in range(3):
      x = N(g(x0), 6)
      ss = N(q / (1-q) * abs(x - x0), 6)
      x = 0x
      print(x, ss)
                                    Mã 3:
f = lambda x: x**3 + 2*x - 1
2 f(0), f(2)
  a, b = 0, 2
  for _ in range(5):
      c = (a + b) / 2
      if f(c) == 0:
          print(f'Nghiệm đúng: {c}')
      elif f(a) * f(c) < 0:
          b = c
10
      else:
          a = c
      ss = b - a
                     # \varepsilon_n
13
      print(a, b)
                                    Mã 4:
import numpy as np
B = np.array([[-0.21, -0.28, 0.05],
                  [0.19, 0.01, -0.26],
                  [0.39, -0.12, -0.06]
   = [-0.9, 3.8, -2.9]
```

q = np.linalg.norm(B, np.inf)

```
q
                            # x^{(k-1)}
8 \times 0 = [0, 2, -1]
9 for _ in range(3):
      x = B.dot(x0) + g # x^{(k)}
10
      ss = q / (1-q) * np.linalg.norm(x - x0, np.inf) # \varepsilon_k
11
      x0 = x
12
      print(x, ss)
13
14 x = [0, 2, -1]
15 for _ in range(4):
      for i in range(3):
16
           x[i] = B[i].dot(x) + g[i]
17
      print(x)
                                      Mã 5:
                             # VD2, 3: import numpy as np
  f = lambda x, y: y - x # VD2: f = lambda x, y: np.array([x * y[0] - y[1],
     y[0] + y[1] - 1]
                             # VD3: f = lambda x, y: np.array([y[1], y[2], x *
     y[2] - y[0])
 X = [0, 0.2, 0.3, 0.5] \# VD2: X = [1, 1.1, 1.3, 1.5]
                               VD3: X = [-1, -0.8, -0.6, -0.5]
                              # VD2: y = [-1, 2]
    = 2
                             # VD3: y = [1, 0, -2]
  for n in range(len(X) - 1):
      h = X[n+1] - X[n]
      k1 = h * f(X[n])
                        , у)
10
      k2 = h * f(X[n] + h/2, y + k1/2)
11
      k3 = h * f(X[n] + h/2, y + k2/2)
12
      k4 = h * f(X[n] + h , y + k3)
13
      y = y + (k1 + 2*k2 + 2*k3 + k4)/6
14
      print(y)
15
                                      Mã 6:
f = lambda x: x**3 - x**2 - 3
2 from sympy import *
x = symbols('x')
4 plot(f(x), (x, 1, 4))
```

```
_{5} plot(_{abs}(f(x).diff(x, 2)), (x, 1, 4))
_{6} M = 22.5
7 t = symbols('t')
8 df = lambda x: f(t).diff().subs(t, x)
9 m = min(abs(df(1)), abs(df(4)))
10 \times 0 = 4.
                                              # x_{n-1}
11 for _ in range(3):
      x = N(x0 - f(x0) / df(x0), 6)
      ss = N(M / 2 / m * (x - x0)**2, 6) # \varepsilon_0
13
      x0 = x
      print(x, ss)
                                      Mã 7:
 A = [[-15.4, 1, 6.3], [-4.2, 10.8, 3.3], [-2.4, 5.3, 15.9]]
  b = [30, 25, -10]
3 m = lambda i, j: -A[i][j] / A[i][i] if i!= j else 0
4 import numpy as np
_{5} B = np.array([ [ m(i, j) for j in range(3)] for i in range(3) ])
6 g = [ b[i] / A[i][i] for i in range(3) ]
                                      Mã 8:
d = lambda k, i: Y[i] if k == 0 else d(k-1, i+1) - d(k-1, i)
[d(k, i) \text{ for } i \text{ in } range(4-k)] \text{ for } k \text{ in } range(4)]
3 from sympy import *
4 \times, t = symbols('x t')
_{5} P = 0
                                           # Y[3]
6 for k in range(4):
      prod = d(k, 0) / factorial(k) # d(k, 3-k)
      for i in range(k):
                                          #t+i
           prod *= t - i
```

```
P += prod
10
11 P
12 P.subs(t, (x - X[0]) / 1).expand() # X[3]
X = [-0.7, 1.7, -4.9, 3.1, -1.3]
Y = [-2.9, -1.1, -2.9, 1.5, 0.8]
Z = [7.1, 5.8, -3.1, -1, -8.7]
4 from sympy import *
s x, y = symbols('x y')
6 cs = [1 + 0*x, x, y]
V = [ [cs_i.subs(\{x: X_k, y: Y_k\}) ]  for (X_k, Y_k)  in zip(X, Y)]  for
     cs_i in cs ]
8 import numpy as np
9 A = [ [np.dot(V_i, V_j) for V_j]
                                   in V] for V_i in V ]
10 b = [np.dot(Z, V_i) for V_i in V]
hs = np.linalg.solve(
      np.array(A, dtype=float)
12
      np.array(b, dtype=float) )
13
P = hs.dot(cs)
[P.subs(\{x: X_k, y: Y_k\}) for (X_k, Y_k) in zip(X, Y)]
errors = [Z_k - P.subs(\{x: X_k, y: Y_k\})] for (X_k, Y_k, Z_k) in zip
np.linalg.norm( np.array(errors, dtype=float) )
                                  Mã 10:
X = [-1, 0, 1, 2]
_{2} Y = [4, 3, 2, 7]
3 def L(i, x):
      prod = 1
      for j in range(4):
5
          if j != i:
              prod *= (x - X[j]) / (X[i] - X[j])
```

```
return prod
9 from sympy import *
x = symbols('x')
11 L(0, x)
12 L(0, x).expand()
13 P = 0
14 for i in range(4):
     P += Y[i] * L(i, x)
P.expand()
                                  Mã 11:
1 from sympy import *
_{2} f = lambda x: sin(x)
a, b = 0, pi
4 import numpy as np
5 X = np.linspace(np.float32(0), np.float32(b), 11)
_{6} Y = [ f(x) for x in X ]
7 sum( [(X[i] - X[i-1]) * (Y[i] + Y[i-1]) / 2 for i in range(1, 11)]
8 plot(f(x).diff(x, 2), (x, a, b))
9 M2 = 1
10 N(M2 * (b-a)**3 / 12 / 10**2, 6)
sum([(X[2*i] - X[2*i-2]) * (Y[2*i] + 4*Y[2*i-1] + Y[2*i-2]) / 6
    for i in range(1, 6)] )
plot(f(x).diff(x, 4), (x, a, b))
13 M4 = 1
N(M4 * (b-a)**5 / 180 / 10**4, 6)
                                  Mã 12:
X = [1, 1.3, 1.7, 2.]
```

Nguyễn Đức Thịnh 6 thinhnd@huce.edu.vn

```
_{2} Y = [3.5, 4., 4.6, 5.2]
3 from sympy import *
4 x = symbols('x')
5 cs = [1 + 0*x, x, log(x)]
V = [ [cs_i.subs(x, X_k) for X_k in X] for cs_i in cs ]
7 import numpy as np
8 A = [ [np.dot(V_i, V_j) for V_j in V] for V_i in V ]
 b = [np.dot(Y, V_i) for V_i in V]
hs = np.linalg.solve(
      np.array(A).astype(float),
11
      np.array(b).astype(float) )
12
P = hs.dot(cs)
14 [P.subs(x, X_k) for X_k in X]
errors = [Y_k - P.subs(x, X_k)] for (X_k, Y_k) in zip(X, Y)
np.linalg.norm(np.array(errors).astype(float))
```

Mã 13: