

FÍSICA II

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1)  $x(t) = 6 * 10^{-2} \cos(9,42t + 1,04)m$

a) Amplitude =  $6 * 10^{-2} = 0,06m$

b)  $9,42 \text{ rad/s}$

c)  $T = \frac{1}{f} = \frac{1}{1,499} = 0,667s$

d)  $f = \frac{\omega}{2\pi} = \frac{9,42}{2\pi} \cong 1,499Hz$

e)  $1,04 \text{ rad}$

f)  $x(0) = 0,06 * \cos(9,42 * 0 + 1,04) m$

$x(0) = 0,06 * \cos(1,04) = 0,06 * 0,506 = \mathbf{0,0304m}$

$v(0) = -9,42 * 0,06 * \sin(9,42 * 0 + 1,04)$

$v(0) = -0,5652 * \sin(1,04) = -0,5652 * 0,8624 = \mathbf{-0,4874m/s}$

$a(0) = -9,42^2 * 0,0304 = \mathbf{-2,69m/s^2}$

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2) a)

$\omega = \frac{2\pi}{2} = \pi \text{ rad/s}$

$k = \omega^2 * m = m\pi^2$

$\omega = \frac{2\pi}{T} = \frac{2\pi}{3} = 2,0943 \text{ rad/s}$

$k = (m + 2)2,0943^2$

$9,8696m \cong 4,38649m + 8,77298$

$5,4831m \cong 8,77298 \rightarrow m \cong \frac{8,77298}{5,4831} \cong \mathbf{1,6kg}$

b)  $\omega^2 = \frac{k}{1,6} \rightarrow \pi^2 = \frac{k}{1,6} \rightarrow k = \pi^2 * 1,6 \cong \mathbf{15,79N/m}$

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3) a)  $E_{pe} = \frac{kx^2}{2} \rightarrow 0,4 = k * \frac{0,1^2}{2} \rightarrow k = \frac{0,4}{0,005} = \mathbf{80N/m}$

b)  $\omega^2 = \frac{k}{m} \rightarrow \omega = \sqrt{\frac{80}{0,1}} = \mathbf{28,284 \text{ rad/s}}$

c) 400j – Se a energia potencial máxima é 400, a energia total, desprezado o atrito é 400.

$$4) a) \gamma = \frac{b}{2m} = \frac{1,6}{2*0,1} = \frac{1,6}{0,2} = 8 \text{ s}^{-1} \quad \omega_0 = \sqrt{\frac{k}{m}} = \sqrt{\frac{10}{0,1}} = 10 \text{ rad/s}$$

$\gamma < \omega_0$  – Subcrítica

$$b) x(t) = Ae^{-\gamma t} \cos(\omega + \varphi_0) \quad \omega = \sqrt{\omega_0^2 - \gamma^2} = \sqrt{100 - 64} = 6 \text{ rad/s}$$

$$0,200 = A * \cos(\varphi_0) \quad \varphi_0 = \arctg\left(-\frac{\gamma}{\omega}\right) \cong -0,674 \text{ rad}$$

$$\frac{0,2}{\cos(-0,674)} = A \cong 0,256 \text{ m}$$

$$x(t) = \mathbf{0,256} \, e^{-8t} \mathbf{\cos(6 - 0,674) \, m}$$

$$c) A_n = A_0 e^{-n\gamma T} \quad T = \frac{2\pi}{6} \cong 1,047 \text{ s} \quad E_n = E_0 e^{-2n\gamma T}$$

$$A_5 = 0,256 e^{-5*8*1,047} = 0,256 * e^{-41,88} \cong 0$$

$$E_0 = \frac{1}{2} * 10 * 0,2^2 = 0,2 \text{ J} \quad E_5 = 0,2 e^{-2*41,88} \cong 0$$