

## Backbone detection algorithms

This repository aims to convey several backbone detection algorithms in an unique script, thereby allowing users to easily analyze the same dataset in multiple ways, according with their preferences/needs. At the moment, we list three different approaches.

- The evolving activity-driven model (EADM) is the first and unique method that considers time-varying individual properties. The EADM proposes an approach based on the configuration model which offers reliable estimates when the size of the network is hundreds of nodes and beyond. We realize two different versions of the same method: the ‘EADM’ and the ‘EADM\_Accuracy’. The ‘EADM’ is optimized for tackling very large networks (having even millions of nodes). The ‘EADM\_Accuracy’ can be applied only to smaller networks (up to ten-thousands nodes) and allows to evaluate the accuracy of the method. We implemented versions for both directed and undirected networks. More details about this method can be found in [citation].
- The temporal fitness model (TFM) is the most accurate method to reconstruct the backbone network of small systems. It puts forward a maximum likelihood approach which provide very reliable estimation of individual properties, which are set to be constant in time. Nevertheless, the maximum likelihood approach requires to solve a system of  $N$  independent equations (one for each node in the network) and it is computationally demanding. We suggest to use it for networks having at most thousands nodes. It can be applied only to undirected networks. More details in [1].
- The statistically validated network (SVN) was the first method able to filter the backbone network considering temporal patterns. It is particular useful when individual properties are constant in time and for large networks, when both the EADM and the TFM are useless. Versions are available for both directed and undirected networks. More details in [2].

We prepared two codes: ‘Filtering\_methods\_u.py’ for undirected networks and ‘Filtering\_methods\_d.py’ for directed networks. Here, we describe an example of running the code for an undirected network. We use the Primary School dataset from the Sociopattern project [1].

1. To import all the functions in the script (you may have to manually install some packages), type: `From Filtering_methods_u.py import *`
2. To run the code with default options, type: `Backbone_detection()`

Here we list the input parameters, their purposes and how to modify them:

- `path_in`: path to the directory containing the dataset to be analyzed. Default: `path_in = 'DATASET/Example_PrimarySchool/'`.

- `name_file`: name of the file in which the edgelist and its timestamp are listed. For directed networks, make sure that the IDs of nodes generating links come first, the IDs of nodes receiving links come in the column immediately after. Default: `name_file = 'primaryschool.csv'`.
- `column_time`: it indicates the column containing the timestamp. Only the first three columns in the file will be considered. Default: `column_time=0`.
- `sep`: how the columns in the edgelist file are separated. Default: `sep='\t'`.
- `dt`: time step which determines the evolution of the temporal network. It must be a list. Default: `dt=[20., 60.*1., 60.*5., 60.*15.]`. These resolutions correspond to 20 seconds, 1 minute, 5 minutes, and 15 minutes, respectively.
- `multiedges`: if you want to retain multiple connections happening within the same time step, write 'yes', otherwise 'no' to allow only one link per time step. It must be a list and its length should be equal to `dt`. The TFM does not work if multiedges are present. Default: `multiedges = ['no']`.
- `directory_out`: it determines where all output file will be stored. Default: `directory_out = 'Output'`.
- `remove_nights`: if you want to remove time steps in which no connections happen, write 'yes', otherwise 'no' to consider the whole observation window. Default: `remove_nights='yes'`.
- `alpha`: value of the significance threshold. All links having a p-value lower than the significance threshold will be included in the backbone network. Default: `alpha = 0.01`.
- `Bonferroni_corr`: write 'yes' if you want to correct alpha according to the Bonferroni correction, otherwise write 'no' and the significance threshold is set to be equal to alpha. Default: `Bonferroni_corr = 'yes'`.
- `model`: choose what filtering approach you want to apply to the temporal dataset. For undirected networks, options are: 'EADM', 'EADM\_Accuracy', 'TFM', and 'SVN'. Default: `model = 'EADM'`. For directed networks, options are: 'EADAM', 'EADAM\_Accuracy', and SVN. Default: `model = 'EADAM'`.

#### Output files:

- `links_model.txt`: it stores the time step chosen (first column) and the number of significant links detected (second column). `model` is a string equal to the respective input parameter.
- `edgelist_dt[i]_model.txt`: it returns the edgelist representing all significant links in the network. `dt[i]` is a string equal to `i` element of the list `dt`, which is the input parameter

determining the length of the time step. *model* is a string equal to the respective input parameter.

- `relative_error_model.txt`: it computes the accuracy of the method in describing the overall system evolution through the relative error. *model* is a string equal to the respective input parameter. The accuracy of the approach can be computed only for ‘EADM\_Accuracy’ and ‘TFM’. Details are available in [citation].

## References

- [1] Teruyoshi Kobayashi, Taro Takaguchi, and Alain Barrat. The structured backbone of temporal social ties. *Nature communications*, 10(1):220, 2019.
- [2] Ming-Xia Li, Vasyl Palchykov, Kaski Kimmo Jiang, Zhi-Qiang, János Kertész, Salvatore Micciché, Michele Tumminello, Wei-Xing Zhou, and Rosario N. Mantegna. Statistically validated mobile communication networks: the evolution of motifs in European and Chinese data. *New Journal of Physics*, 16(8):083038, 2014.