## LibADMM: A Library of Alternating Direction Method of Multipliers for Compressed Sensing

Version 1.0

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https://github.com/canyilu/LibADMM

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June, 2016

TABLE 1: Applicability of the LibADMM package

Model	Problem		Function	Description and Reference
Sparse models		$r(\mathbf{x}) = \ \mathbf{x}\ _1$	11	$\ell_1$ [14]
	$\min_{\mathbf{x}} r(\mathbf{x})$	$r(\mathbf{x}) = \sum_{g \in \mathcal{G}} \ \mathbf{x}_g\ _2$	groupl1	Group Lasso [17]
		$r(\mathbf{x}) = \ \mathbf{x}\ _1 + \lambda_2 \ \mathbf{x}\ _2^2$	elasticnet	Elastic net [19]
	s.t. $\mathbf{A}\mathbf{x} = \mathbf{b}$	$r(\mathbf{x}) = \ \mathbf{x}\ _1 + \lambda_2 \sum_{i=2}^{p}  x_i - x_{i-1} $	fusedl1	Fused Lasso [15]
		$r(\mathbf{x}) = \ \mathbf{A}\mathrm{Diag}(\mathbf{x})\ _*$	tracelasso	Trace Lasso [12]
		$r(\mathbf{x}) = \frac{1}{2} \ \mathbf{x}\ _{ksp}^2$	ksupport	k support norm [6]
	$\min_{\mathbf{x}, \mathbf{e}} \ l(\mathbf{e}) + \lambda r(\mathbf{x})$ s.t. $\mathbf{A}\mathbf{x} + \mathbf{e} = \mathbf{b}$	$l(\mathbf{e}) = \ \mathbf{e}\ _1$ $l(\mathbf{e}) = \frac{1}{2} \ \mathbf{e}\ _2^2$	11R	Reg. $\ell_1$
			groupl1R	Reg. Group Lasso
			elasticnetR	Reg. Elastic net
			fusedl1R	Reg. Fused Lasso
			tracelassoR	Reg. Trace Lasso
			ksupportR	Reg. $k$ support norm
	$\min_{\mathbf{L},\mathbf{S}} \ \mathbf{L}\ _* + \lambda l(\mathbf{S}), \text{ s.t. } \mathbf{X} = \mathbf{L} + \mathbf{S}$		rpca	Robust PCA [2]
Low-rank	$\min_{\mathbf{X}} \ \mathbf{X}\ _*, \text{ s.t. } \mathcal{P}_{\Omega}(\mathbf{X}) = \mathcal{P}_{\Omega}(\mathbf{M})$		lrmc	Low-rank matrix completion [1]
	$\min_{\mathbf{X}, \mathbf{E}} \ \mathbf{X}\ _* + \lambda l(\mathbf{E}), \text{ s.t. } \mathcal{P}_{\Omega}(\mathbf{X}) + \mathbf{E} = \mathbf{M}$		lrmcR	Reg. Low-rank matrix completion
	$\min_{\mathbf{X}, \mathbf{E}} \ \mathbf{X}\ _* + \lambda l(\mathbf{E}), \text{ s.t. } \mathbf{A} = \mathbf{B}\mathbf{X} + \mathbf{E}$		lrr	Low-rank representation [8]
	$\min_{\mathbf{Z}, \mathbf{L}, \mathbf{E}} \ \mathbf{Z}\ _* + \ \mathbf{L}\ _* + \lambda l(\mathbf{E})$		latlrr	Latent low-rank representation [9]
	s.t. $XZ + LX - X = E$			
matrix models	$\min_{\mathbf{X},\mathbf{E}} \ \mathbf{X}\ _* + \lambda_1 \ \mathbf{X}\ _1 + \lambda_2 l(\mathbf{E})$		lrsr	Low-rank and sparse representation [18]
	s.t. $\mathbf{A} = \mathbf{B}\mathbf{X} + \mathbf{E}$			
	$\min_{\mathbf{L}_i, \mathbf{S}_i} \ \mathbf{L}\ _* + \lambda \sum_{i=1}^m \ \mathbf{S}_i\ _{1,i}$		rmsc	Robust multi-view spectral clustering [16]
	s.t. $\mathbf{X}_i = \mathbf{L} + \mathbf{S}_i, i = 1, \dots, m, \mathbf{L} \ge 0, \mathbf{L}1 = 1$			
	$\min_{\mathbf{Z}_i, \mathbf{E}_i} \sum_{i=1}^K (\ \mathbf{Z}_i\ _* + \lambda l(\mathbf{E}_i)) + \alpha \ \mathbf{Z}\ _{2,1}$		mlap	Multi-task low-rank affinity pursuit [4]
	s.t. $\mathbf{X}_i = \mathbf{X}_i \mathbf{Z}_i + \mathbf{E}_i, i = 1, \cdots, K$			, ,
		$\ \mathbf{S}\ _1, \text{ s.t. } \mathbf{A} = \mathbf{L} + \mathbf{S}, 0 \le \mathbf{L} \le 1$	igc	Improved graph clustering [3]
	$\min_{\mathbf{P}} \langle \mathbf{P}, \mathbf{L} \rangle + \lambda   \mathbf{P}  _1$	, s.t. $0 \leq \mathbf{P} \leq \mathbf{I}, \text{Tr}(\mathbf{P}) = k$	sparsesc	Sparse spectral clustering [13]
Low-rank tensor models	$\min_{\mathcal{L}, \mathcal{S}} \ \sum_{i=1}^k lpha_i \ \mathcal{L}_{i(i)}\ _* + \ \mathcal{S}\ _1,  ext{ s.t. } \mathcal{X} = \mathcal{L} + \mathcal{S}$		trpca_snn	Tensor robust PCA based on
	$\lim_{\mathcal{L},\mathcal{S}} \angle_{i=1}^{\alpha_i}   \mathcal{L}_{i}  $	$ i\rangle \parallel * + \parallel \boldsymbol{\mathcal{S}} \parallel 1, \text{ s.t. } \boldsymbol{\mathcal{A}} = \boldsymbol{\mathcal{L}} + \boldsymbol{\mathcal{S}}$	cipca_siii	sum of nuclear norm [5]
	$\boxed{\min_{\boldsymbol{\mathcal{X}}} \; \sum_{i=1}^{k} \alpha_{i} \ \boldsymbol{\mathcal{X}}_{i(i)}\ _{*}, \; \text{s.t. } \mathcal{P}_{\Omega}(\boldsymbol{\mathcal{X}}) = \mathcal{P}_{\Omega}(\boldsymbol{\mathcal{M}})}$		lrtc_snn	Low-rank tensor completion based on
				sum of nuclear norm [10]
	$ \begin{aligned} & \min_{\boldsymbol{\mathcal{X}},\boldsymbol{\mathcal{E}}} \ \sum_{i=1}^k \alpha_i \ \boldsymbol{\mathcal{X}}_{i(i)}\ _* + \lambda l(\boldsymbol{\mathcal{E}}) \\ & \text{s.t.} \ \mathcal{P}_{\Omega}(\boldsymbol{\mathcal{X}}) + \boldsymbol{\mathcal{E}} = \boldsymbol{\mathcal{M}} \end{aligned} $		lrtcR_snn	Reg. low-tank tensor completion based on
				sum of nuclear norm
	$\min_{\mathcal{L}, \mathcal{S}} \ \mathcal{L}\ _* + \lambda \ \mathcal{S}\ _1, \text{ s.t. } \mathcal{X} = \mathcal{L} + \mathcal{S}$		trpca_tnn	Tensor Robust PCA based on
				tensor nuclear norm [11]
	$\min_{m{\mathcal{X}}} \ m{\mathcal{X}}\ _*, \text{ s.t. } \mathcal{P}_{\Omega}(m{\mathcal{X}}) = \mathcal{P}_{\Omega}(m{\mathcal{M}})$		lrtc_tnn	Low-rank tensor completion based on
				tensor nuclear norm [11]
	$\min_{\mathcal{X}, \mathcal{E}} \ \mathcal{X}\ _* + \lambda l(\mathcal{E}), \text{ s.t. } \mathcal{P}_{\Omega}(\mathcal{X}) + \mathcal{E} = \mathcal{M}$		lrtcR_tnn	Reg. low-rank tensor completion based on
				tensor nuclear norm [11]

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