What Is Bayesian Classification?

- A statistical classifier
 - Perform probabilistic prediction (i.e., predict class membership probabilities)
- ☐ Foundation Based on Bayes' Theorem
- Performance
 - A simple Bayesian classifier, *naïve Bayesian classifier*, has comparable performance with decision tree and selected neural network classifiers
- Incremental
 - Each training example can incrementally increase/decrease the probability that a hypothesis is correct—prior knowledge can be combined with observed data
- Theoretical Standard
 - Even when Bayesian methods are computationally intractable, they can provide a standard of optimal decision making against which other methods can be measured

Bayes' Theorem: Basics

Total probability Theorem:

$$p(B) = \sum_{i} p(B|A_i)p(A_i)$$

Bayes' Theorem:

$$p(H|X) = \frac{p(X|H)P(H)}{p(X)} \propto p(X|H)P(H)$$

What we should choose

posteriori probability

What we just see

likelihood

What we knew previously

prior probability

X: a data sample ("evidence")

Prediction can be done based on Bayes' Theorem:

H: X belongs to class C

Classification is to derive the maximum posteriori

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Naïve Bayes Classifier: Making a Naïve Assumption

- Practical difficulty of Naïve Bayes inference: It requires initial knowledge of many probabilities, which may not be available or involving significant computational cost
- A Naïve Special Case
 - Make an additional <u>assumption</u> to simplify the model, but achieve comparable performance.

attributes are conditionally independent (i.e., no dependence relation between attributes)

$$p(X|C_i) = \prod_k p(x_k|C_i) = p(x_1|C_i) \cdot p(x_2|C_i) \cdot \cdots \cdot p(x_n|C_i)$$

Only need to count the class distribution w.r.t. features

Naïve Bayes Classifier: Categorical vs. Continuous Valued Features

□ If feature x_k is categorical, $p(x_k = v_k | C_i)$ is the # of tuples in C_i with $x_k = v_k$, divided by $|C_{i,D}|$ (# of tuples of C_i in D)

$$p(X|C_i) = \prod_k p(x_k|C_i) = p(x_1|C_i) \cdot p(x_2|C_i) \cdot \cdots \cdot p(x_n|C_i)$$

 $\hfill \square$ If feature x_k is continuous-valued, $p(x_k=v_k|C_i)$ is usually computed based on Gaussian distribution with a mean μ and standard deviation σ

$$p(x_k = v_k | C_i) = N(x_k | \mu_{C_i}, \sigma_{C_i}) = \frac{1}{\sqrt{2\pi}\sigma_{C_i}} e^{-\frac{(x - \mu_{C_i})^2}{2\sigma^2}}$$

Naïve Bayes Classifier: Training Dataset

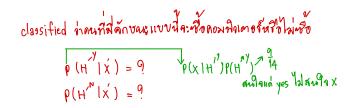
Class:

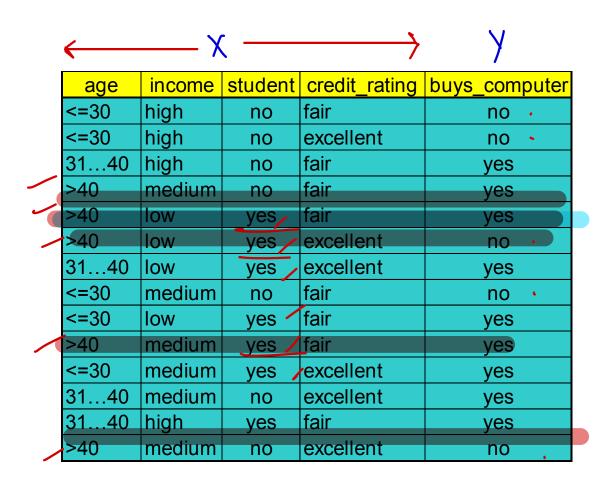
C1:buys_computer = 'yes'

C2:buys_computer = 'no' 5

Data to be classified:

X = (age <=30, Income = medium,
Student = yes, Credit_rating = Fair)</pre>





Naïve Bayes Classifier: An Example

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P(C<sub>i</sub>): P(buys_computer = "yes") = 9/14 = 0.643
P(buys_computer = "no") = 5/14 = 0.357
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Compute P(X|C_i) for each class P(age = "<=30"|buys_computer = "yes") = 2/9 = 0.222

P(age = "<=30"|buys_computer = "no") = 3/5 = 0.6

P(income = "medium" | buys_computer = "yes") = 4/9 = 0.444

P(income = "medium" | buys_computer = "no") = 2/5 = 0.4

P(student = "yes" | buys_computer = "yes") = 6/9 = 0.667

P(student = "yes" | buys_computer = "no") = 1/5 = 0.2

P(credit_rating = "fair" | buys_computer = "yes") = 6/9 = 0.667

P(credit_rating = "fair" | buys_computer = "no") = 2/5 = 0.4

age	income	student	credit_rating	buys_computer
<=30	high	no	fair	no
<=30	high	no	excellent	no
3140	high	no	fair	yes
>40	medium	no	fair	yes
>40	low	yes	fair	yes
>40	low	yes	excellent	no
3140	low	yes	excellent	yes
<=30	medium	no	fair	no
<=30	low	yes	fair	yes
>40	medium	yes	fair	yes
<=30	medium	yes	excellent	yes
3140	medium	no	excellent	yes
3140	high	yes	fair	yes
>40	medium	no	excellent	no

X = (age <= 30, income = medium, student = yes, credit_rating = fair)</p>

$$P(X|C_i)$$
: $P(X|buys_computer = "yes") = 0.222 x 0.444 x 0.667 x 0.667 = 0.044$

$$P(X|buys_computer = "no") = 0.6 \times 0.4 \times 0.2 \times 0.4 = 0.019$$

$$P(X|C_i)*P(C_i): P(X|buys_computer = "yes") * P(buys_computer = "yes") = 0.028$$

 $P(X|buys_computer = "no") * P(buys_computer = "no") = 0.007$

Therefore, X belongs to class ("buys_computer = yes")

$$\hat{x} = age = 42, student = yes?$$

$$P(H_1^7|\hat{x}) = ? \quad 42 \text{ yes a}$$

$$P(H_2|\hat{y}| (age = 42, student = yes)) = P(age = 42|popy)P(student|popy)P(popy)$$

$$\frac{3}{9} \quad \times \quad \frac{6}{9} \quad \times \quad \frac{9}{14}$$

$$P(H_{puy} = N | (age = 41, student = yes) = 0.143$$

Lazy Learner: Instance-Based Methods เพื่อใช้งังมุล train มา เก็บเทโบละสุ เพื่อมี ปลรอ เข้ามาถึงทำ , เก็บสนสุดท้ายจริง ๆ ส่องทำ

- Instance-based learning:
 - Store training examples and delay the processing ("lazy evaluation") until a new instance must be classified
- Typical approaches
 - k-nearest neighbor approach
 - Instances represented as points in a Euclidean space.
 - Locally weighted regression
 - Constructs local approximation
 - Case-based reasoning
 - Uses symbolic representations and knowledge-based inference

The k-Nearest Neighbor Algorithm

- All instances correspond to points in the n-D space
- \square The nearest neighbor are defined in terms of Euclidean distance, dist(X_1, X_2)
- Target function could be discrete- or real- valued
- For discrete-valued, k-NN returns the most common value among the k training examples nearest to x_q
- Vonoroi diagram: the decision surface induced by 1-NN for a typical set of training examples

