

T2K 3.010×10^{20} -POT 3-Flavour Muon-Neutrino Disappearance Analysis

Costas Andreopoulos^a, Thomas Dealtry^{a,b}, Lorena Escudero Sánchez^c, Nick Grant^d, and Alfons Weber^{a,b}

^aParticle Physics Dept., Rutherford Appleton Laboratory, STFC
Harwell Oxford Campus

Oxfordshire OX11 0QX, UK

^bSubdepartment of Particle Physics, University of Oxford
Denys Wilkinson Building, Keble Road

Oxfordshire OX1 3RH, UK

^cInstituto de Física Corpuscular
CSIC and University of Valencia

Valencia, Spain

^dPhysics Dept., Lancaster University
Lancaster, LA1 4YB, UK

Abstract

We report the results of the *VaLOR* (Valencia-Lancaster-Oxford-Rutherford) 3-flavour ν_μ -disappearance analysis on the combined Run 1+2+3 dataset. This analysis is an update of the work presented in Refs. [1], [2] and [3] with improved methods and an enlarged dataset. The Run 1+2+3 dataset corresponds to an integrated J-PARC neutrino beam exposure of 3.010×10^{20} POT.

This analysis predicts 204.75 ± 16.75 (syst) 1 μ -like ring events in SuperK in the absence of any oscillation, but only 58 were observed. The observed deficit has a strong energy dependence; the ratio of observed to expected, under the no-oscillation hypothesis, is $\sim 30\% < 0.5$ GeV, $\sim 10\%$ between 0.5 and 1 GeV and $\sim 75\% > 1$ GeV.

A ν_μ -disappearance analysis was performed in a framework of 3-flavour oscillations including matter effects in constant-density matter. Two versions of the oscillation fit were performed: one (the ‘2+N’ fit) allows all 48 systematics considered in this analysis to float, while the other (the ‘2+8’ fit) allows only the 8 most dominant systematics to float (the dominant systematics are those identified as having an effect on the measured oscillation parameters that is greater than 25% of the expected statistical error, for at least one set of true oscillation parameters in the area of interest).

The ‘2+N’ 3-flavour ν_μ -disappearance fit to the observed reconstructed energy spectrum of 1 μ -like ring events of the combined Run1+2+3 dataset, assuming the first octant ($\sin^2 2\theta_{23} \leq 0.5$), with $\sin^2 2\theta_{23}$ constrained to the physical region, yields $|\Delta m_{32}^2| = 2.441 \times 10^{-3} \text{ eV}^2/\text{c}^4$ and $\sin^2 \theta_{23} = 0.514$ as the best-fit values (p-value = 0.80). For the ‘2+N’ fits for $\sin^2 2\theta_{23}$, assuming both the first ($\sin^2 2\theta_{23} \leq 0.5$) and second octant ($\sin^2 2\theta_{23} \geq 0.5$), the best-fit values are almost identical. All fits used 2012 PDG values for $\sin^2 2\theta_{13}$, $\sin^2 2\theta_{12}$ and Δm_{21}^2 [21], and assumed $\delta_{CP}=0$ and the normal mass hierarchy.

Confidence regions obtained using both the constant- $\Delta\chi^2$ method and the method of Feldman and Cousins are shown for both the ‘2+N’ and ‘2+8’ fits. Using the results of the ‘1+N’ fits, and the constant- $\Delta\chi^2$ method, the 90% CL allowed region, for the ‘2+N’ fit for $\sin^2 \theta_{23}$, can be summarized as $2.19 \times 10^{-3} \text{ eV}^2/\text{c}^4 < |\Delta m_{32}^2| < 2.72 \times 10^{-3} \text{ eV}^2/\text{c}^4$ and $0.397 < \sin^2 \theta_{23} < 0.630$. The corresponding limits for the ‘2+N’ fit assuming the first octant, can be summarized as $2.19 \times 10^{-3} \text{ eV}^2/\text{c}^4 < |\Delta m_{32}^2| < 2.72 \times 10^{-3} \text{ eV}^2/\text{c}^4$ and $\sin^2 2\theta_{23} > 0.958$. The corresponding limits for the ‘2+N’ fit assuming the second octant, can be summarized as $2.19 \times 10^{-3} \text{ eV}^2/\text{c}^4 < |\Delta m_{32}^2| < 2.72 \times 10^{-3} \text{ eV}^2/\text{c}^4$ and $\sin^2 2\theta_{23} > 0.931$.

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131 **1. Introduction**

132 In this technical note, we report the results of a 3-flavour ν_μ -disappearance analysis, performed by the Valencia-
133 Lancaster-Oxford-Rutherford (VaLOR) group, on the combined Run1+2+3 (3.010×10^{20} POT) dataset. This dataset
134 was collected in three run periods: in January 2010 - June 2010 (Run1, 0.323×10^{20} POT), in November 2010 - March
135 2011 (Run2, 1.108×10^{20} POT) and, following the recovery work from the damage of the 2011 Tohoku earthquake, in
136 March 2012 - June 2012 (Run3, 1.579×10^{20} POT).

137 This analysis is an update of the work presented in Refs. [1], [2] and [3] with improved methods and an enlarged
138 dataset. It benefits from an updated flux tuning based on recent NA61 data [9][20], as well as from T2K fits of
139 flux and cross-section parameters to ND280 measurements of muon momentum-angle distributions of ν_μ CCQE-like
140 and CCnonQE-like events whose vertices are in the FGD [14]. Details of our updated method for predicting the
141 reconstructed energy spectrum of single μ -like ring events in SuperK are presented in Sec. 2.

142 The oscillation analysis is performed using neutrino oscillation probabilities computed in a 3-flavour framework
143 including constant-density matter effects. Details of our oscillation probability calculations, estimates of the numerical
144 accuracy of our calculations and comparisons with calculations used by the alternative T2K oscillation analyses, are
145 given in Appendices A and B.

146 We consider a total of 48 efficiency, energy scale, neutrino flux, neutrino cross-section, initial-state nuclear en-
147 vironment and final-state rescattering systematics. These systematic parameters and their effects on the extrapolated
148 single μ -like ring event reconstructed energy spectrum are described in Sec. 3. Further details of them are also given
149 in Appendices E and F.

150 As in our previous analyses, the oscillation fit was made using the likelihood-ratio method [24]. The oscillation
151 fitting method is presented in detail in Sec. 4.1, while the chosen goodness-of-fit test, suitable for the Run 1+2+3
152 statistics, is described in Sec. 4.2. The fitter performance was tested in detail using toy MC experiments and the results
153 of these tests are presented in Sec. 4.3 and in Appendix H. The effect of systematic parameters on the oscillation fit
154 was studied in detail. The results of this study are summarised in Sec. 4.4 and are shown, in more detail, in Appendix
155 G.

156 We considered two versions of the fit: the first version allows all 48 systematic parameters to float and is denoted
157 the ‘2+N’ fit, while the second version allows only the 8 most dominant systematics to float (the ‘2+8’ fit). These
158 8 dominant systematic parameters are those having an effect on the oscillation parameters greater than 25% of the
159 expected statistical error, for at least one set of true oscillation parameters in the parameter range of interest. Results
160 are presented both for ‘2+N’ and ‘2+8’ fits. Further details of our fit labeling scheme are given in Sec. 4.1.6.

161 The confidence regions were constructed, as in our previous analyses, using the Feldman-Cousins method [26]
162 both for ‘2+N’ and ‘2+8’ fits. Systematic errors were included in the oscillation contours using the Cousins-Highland
163 method (Bayesian integration) [27]. Contours constructed with the constant- $\Delta\chi^2$ method are also shown for both fits
164 for comparison. In Sec. 4.5 we summarise both of these methods and clearly explain the exact methodology used for
165 incorporating systematic errors.

166 Sensitivity studies are shown in Appendix C, and were performed using the complete VaLOR analysis with an
167 integrated exposure of 3.010×10^{20} POT and for a grid of oscillation points around the 2012 MINOS [31] 90% CL
168 region.

169 The results of the measurement of $\sin^2 2\theta_{23} / \sin^2 2\theta_{23}$ and $|\Delta m_{32}^2|$ using the Run1+2+3 dataset are given in Sec.
170 5.1 of this note for both ‘2+N’ and ‘2+8’ fits, while the goodness-of-fit tests are presented in Sec. 5.2. The best-
171 fit spectra for all ‘2+N’ and ‘2+8’ fits to the Run 1+2, Run 3 and Run 1+2+3 datasets are shown in Sec. 5.3. The
172 Feldman-Cousins and constant- $\Delta\chi^2$ confidence regions are shown, for both fits, in Sec. 5.5. Comparisons of our
173 results obtained with different fits and with different methods for constructing confidence regions are presented in Sec.
174 5.6. In that section, we also show comparisons of our T2K Run 1+2+3 results with MINOS and SuperK results, as
175 well as with the expected T2K sensitivity for an integrated exposure of 3.010×10^{20} POT. We present the VaLOR group
176 prospective on the choice of primary result for the Run1+2+3 disappearance analysis in Sec. 5.7. Finally, a summary
177 is given in Sec. 6.

178 **2. Predictions of single μ -like ring event reconstructed energy spectrum in SuperK**

179 **2.1. Methodology**

180 In this analysis, the oscillation parameters are determined by fitting the reconstructed energy (E_r) spectrum of
181 1-ring μ -like events observed at SuperK with the predicted spectrum. The predicted number $N_{SK;r}$ of 1-ring μ -like
182 events in the r^{th} reconstructed energy bin is computed as follows:

$$N_{SK;r} = \sum_m \sum_t \sum_{r'} P_{m;t} \cdot T_{r;r';f_{\Delta E}} \cdot S_{m;t;r';\vec{f}} \cdot N_{SK;m;r;t}^{MC}. \quad (1)$$

In Eq. 1, $N_{SK;m;r;t}^{MC}$ is the input SuperK Monte Carlo (MC) template containing the number of events in the 1-ring μ -like MC sample with true reaction mode m , and found in the true energy bin t and the reconstructed energy bin r' . The construction of the nominal MC templates is discussed in Sec. 2.2. Both flux-tuning weights based on NA61 hadro-production data (see Sec. 2.3) and flux and cross-section tuning weights based on ND280 data (see Sec. 2.4) are applied to the nominal MC templates. $S_{m;t;r';\vec{f}}$ is an overall, multiplicative, systematic error factor depending on the reaction mode m , the true energy bin t , the reconstructed energy bin r' and a vector of nuisance (systematic) parameters \vec{f} . A complete description of the nuisance parameters considered in this analysis is given in Sec. 3. $T_{r;r';f_{\Delta E}}$ is a transfer function describing the migration of events between the reconstructed energy bins r and r' due to uncertainty in the SuperK reconstructed energy scale, expressed here in terms of the nuisance parameter $f_{\Delta E}$. Finally, $P_{m;t}$ is the 3-flavour oscillation probability applied in the true energy bin t of the SuperK MC template which corresponds to mode m . Application of the term $P_{m;t}$ is discussed in Sec. 2.5.

2.2. Construction of nominal SuperK Monte Carlo templates

The nominal SuperK 1-ring μ -like MC templates $N_{SK;m;r;t}^{MC}$ are constructed by applying the 1-ring μ -like selection cuts to the official SuperK MC samples. Details of the MC samples are given in Sec. 2.2.1. The calculation of the normalization of each MC sample is described in Sec. 2.2.2. The official 1-ring μ -like selection cuts are listed in Sec. 2.2.3. The list of MC templates used in this analysis is shown in Sec. 2.2.4, while the true and reconstructed energy binning of the templates is discussed in Sec. 2.2.5.

The nominal SuperK MC templates used in this analysis are shown in Appendix I.3.

2.2.1. Input Monte Carlo samples

This analysis uses the official 2011c SuperK MC sample [17], which was generated and processed at the Kamioka cluster. The following versions of software packages were used:

- JNUBEAM flux 2011a
- NEUT v5.1.4.1
- SKDETSIM-v12p80
- ATMPD-ap11c
- SKOFL-11c

Five MC samples were generated. Four of the samples (ν_μ , $\bar{\nu}_\mu$, ν_e and $\bar{\nu}_e$) were generated using the nominal JNUBEAM flux without oscillations. A fifth sample of ν_e interactions was also generated with the ν_μ flux. This fifth sample will be denoted the ‘oscillated ν_e ’ sample (it corresponds to the ‘signal- ν_e ’ sample in the ν_e -appearance analysis). Samples neglected would make a negligible contribution to the single μ -like ring sample as explained in the following subsections. All samples were generated including the neutrino flux estimates up to 30 GeV. The flux histograms used for neutrino event generation had 50 MeV bins.

2.2.2. Normalization of Monte Carlo samples

The normalization (integrated exposure in terms of POT) of each event sample is calculated from the number of events with a MC truth interaction vertex within the 22.5 kt fiducial volume.

$$N = \int dS dIdE \cdot \frac{d^3\Phi_{SK}}{dS dIdE_\nu} \cdot \sigma_{H_2O} \cdot \frac{N_A}{A} \cdot \rho \cdot L \quad (2)$$

where $d^3\Phi_{SK}/dS dIdE$ is the number of flux particles, for the given neutrino species, per neutrino energy bin dE_ν , per unit area dS and per POT, σ_{H_2O} is the total interaction cross section in water for the given neutrino species, I is the beam intensity in terms of POT, N_A is Avogadro’s number, A is the mass number for water, ρ is the water density and L is the neutrino path length in the water volume. The results of this calculation are shown in Tab. 1 for all 5

Sample	Number of events /22.5 kt fiducial /10 ²¹ POT	Number of events generated	Number of events in fiducial volume	POT normalization
ν_μ	1418.68	1000000	634998	4.4760×10^{23}
$\bar{\nu}_\mu$	48.6039	504000	319640	6.5762×10^{24}
ν_e	28.312	1000000	633715	2.2383×10^{25}
$\bar{\nu}_e$	2.98885	504000	319689	1.0696×10^{26}
Oscillated ν_e	1490.15	504000	320252	2.1491×10^{23}

Table 1: Statistics and normalization of input SuperK MC samples.

222 SuperK MC samples along with the generated statistics, the numbers of events within the 22.5 kt fiducial volume and
 223 the derived POT normalization of each sample in terms of POT.

224 After being generated from a MC sample corresponding to a calculated integrated beam exposure I, each MC
 225 template is normalized to the integrated beam exposure of the Run1+2+3 dataset (3.010×10^{20} POT) by scaling the bin
 226 contents of the template with $3.010 \times 10^{20}/I$.

227 2.2.3. Single μ -like ring event selection cuts

228 The SuperK MC templates contain events from the ν_μ , $\bar{\nu}_\mu$, ν_e , $\bar{\nu}_e$ and oscillated ν_e samples passing the standard
 229 SuperK selection cuts for 1 μ -like ring events. These cuts are:

- 230 • the number of PMT hits in the highest-charge OD cluster is less than or equal to 15, and the event passes the
 231 flasher rejection cuts (`evclass == 1`),
- 232 • the reconstructed vertex is at least 2 metres away from the ID wall (`wall > 200`),
- 233 • the visible energy in the event is above 30 MeV (`evis > 30`),
- 234 • there is exactly 1 reconstructed ring in the event (`nring == 1`),
- 235 • the reconstructed ring is μ -like (`ip[0] = 3`),
- 236 • the reconstructed muon momentum is above 200 MeV (`amomm[0] > 200`), and
- 237 • there is at most 1 decay e^- in the event (`nmue <= 1`).

238 2.2.4. List of Monte Carlo templates

239 For each SuperK MC sample, a number of different MC templates is constructed corresponding to different true
 240 reaction modes. The template granularity depends on the type of oscillation analysis and the specific systematic
 241 parameters considered in the analysis. 12 MC templates were used for our 2010 Run1+2 2-flavour disappearance
 242 analysis [2], while 15 MC templates were used for our 2010 Run1+2 3-flavour disappearance analysis [3]. This
 243 analysis uses the following 28 MC templates:

- 244 • ν_μ CCQE
- 245 • ν_μ CC1 π ,
- 246 • ν_μ CC coherent,
- 247 • ν_μ CC other,
- 248 • ν_μ (and $\rightarrow \nu_e, \nu_\tau$) NC1 π^\pm ,
- 249 • ν_μ (and $\rightarrow \nu_e, \nu_\tau$) NC other,
- 250 • $\bar{\nu}_\mu$ CCQE,
- 251 • $\bar{\nu}_\mu$ CC1 π ,
- 252 • $\bar{\nu}_\mu$ CC coherent,

- 253 • $\bar{\nu}_\mu$ CC other,
- 254 • $\bar{\nu}_\mu$ (and $\rightarrow \bar{\nu}_e, \bar{\nu}_\tau$) NC1 π^\pm ,
- 255 • $\bar{\nu}_\mu$ (and $\rightarrow \bar{\nu}_e, \bar{\nu}_\tau$) NC other,
- 256 • ν_e CCQE,
- 257 • ν_e CC1 π ,
- 258 • ν_e CC coherent,
- 259 • ν_e CC other,
- 260 • ν_e (and $\rightarrow \nu_\mu, \nu_\tau$) NC1 π^\pm ,
- 261 • ν_e (and $\rightarrow \nu_\mu, \nu_\tau$) NC other,
- 262 • $\bar{\nu}_e$ CCQE,
- 263 • $\bar{\nu}_e$ CC1 π ,
- 264 • $\bar{\nu}_e$ CC coherent,
- 265 • $\bar{\nu}_e$ CC other,
- 266 • $\bar{\nu}_e$ (and $\rightarrow \bar{\nu}_\mu, \bar{\nu}_\tau$) NC1 π^\pm ,
- 267 • $\bar{\nu}_e$ (and $\rightarrow \bar{\nu}_\mu, \bar{\nu}_\tau$) NC other,
- 268 • Oscillated ν_e CCQE,
- 269 • Oscillated ν_e CC1 π ,
- 270 • Oscillated ν_e CC coherent and
- 271 • Oscillated ν_e CC other

272 In the standard 3-flavour oscillation framework, oscillations of ν_e and ν_μ can yield ν_τ , while oscillations of $\bar{\nu}_e$ and
 273 $\bar{\nu}_\mu$ can yield $\bar{\nu}_\tau$. In this analysis, we neglect contributions from ν_τ -CC and $\bar{\nu}_\tau$ -CC as their energy threshold is around
 274 3.5 GeV and their effect is negligible. Accordingly, this analysis uses no ν_τ -CC and $\bar{\nu}_\tau$ -CC MC templates (and, in fact,
 275 no ν_τ and $\bar{\nu}_\tau$ SuperK MC samples are available).

276 It should be emphasized here that the ν_μ NC MC templates for a mode m are proxies for the NC MC templates for
 277 the mixture of $\nu_e + \nu_\mu + \nu_\tau$ resulting from 3-flavour ν_μ oscillations for that mode m . The same applies to the $\bar{\nu}_\mu$, ν_e and
 278 $\bar{\nu}_e$ NC MC templates. These NC MC templates are unchanged under standard 3-flavour oscillations (see also Sec. 2.5).

279 Also it should be noted that there are no explicit NC MC templates made from the oscillated ν_e sample. If they were
 280 used, the oscillated ν_e (i.e. ν_e coming from ν_μ oscillations) would be double counted since they are already included
 281 in the ν_μ NC MC templates.

282 2.2.5. Binning of Monte Carlo templates

283 Each of the 28 MC templates has 6132 2-dimensional bins (= 84 true energy bins \times 73 reconstructed energy bins).
 284 The 84 true energy bins are arranged as follows:

- 285 • 6 50-MeV bins from 0-0.3 GeV,
- 286 • 28 25-MeV bins from 0.3-1 GeV,
- 287 • 40 50-MeV bins from 1-3 GeV,
- 288 • 5 100-MeV bin from 3-3.5 GeV,
- 289 • 1 bin from 3.5-4 GeV,

- 290 • 1 bin from 4-5 GeV,
 291 • 1 bin from 5-7 GeV,
 292 • 1 bin from 7-10 GeV and
 293 • 1 bin from 10-30 GeV.

294 The 73 reconstructed energy bins are the following:

- 295 • 60 50-MeV bins from 0-3 GeV,
 296 • 4 250-MeV bins from 3-4 GeV,
 297 • 4 500-MeV bins from 4-6 GeV,
 298 • 4 1000-MeV bins from 6-10 GeV and
 299 • 1 bin from 10-30 GeV.

300 The same reconstructed neutrino energy binning is used for the fit of the 1-ring μ -like reconstructed energy spectrum.
 301 A study was performed to decide the optimum binning scheme balancing the needs for accuracy and speed. Details
 302 are given in Appendix I.1-I.2.

303 2.3. Applying flux tuning based on NA61 data

304 In this analysis, the nominal MC templates, which were constructed using a MC event sample generated with 11a
 305 flux, are reweighted to the *2011b_v3.2_run1-3c* flux which was tuned on NA61 hadroproduction measurements [9][20].
 306 The reweighted MC templates are denoted the *NA61-tuned* MC templates in this document. The applied weights, as a
 307 function of the true neutrino energy, were obtained from [18] and are shown in Figs. 1-4. The effect of this flux tune
 308 on the predicted reconstructed energy spectrum of single μ -like ring events is discussed in Sec. 2.6 (see Figs. 8 and 10,
 309 and Tabs. 2 and 3)

310 2.4. Applying flux and cross-section (BANFF) tuning based on ND280 data

311 This analysis uses the flux and cross-section parameter tuning performed by the beam and ND280 flux extrapolation
 312 task force (BANFF). The BANFF fit combines constraints on the beam flux from the beam monitors and NA61,
 313 constraints on interaction cross sections from external data (e.g. MiniBooNE) and ND280 measurements of ν_μ CCQE-
 314 like and CCnonQE-like events with vertices in the FGD fiducial volume. This fit provides estimates of flux and
 315 cross-section parameters and their correlations; it also reduces the uncertainties in parameters that are expected to have
 316 some cancellation between the ND280 and SuperK compared with their uncertainties from external data. Version 8 of
 317 the BANFF fit is used in this analysis [14]. A list of BANFF parameters and their best-fit values is shown in Tab. 6.

318 This analysis reweights the NA61-tuned MC templates to the BANFF best-fit parameters ¹ ². The MC templates
 319 obtained are referred to, in this document, as the *BANFF-tuned* MC templates. The effect of the BANFF tune on the
 320 predicted reconstructed energy spectrum of single μ -like ring events is discussed in Sec. 2.6 (see Figs. 9 and 11, and
 321 Tabs. 2 and 3).

322 2.5. Applying neutrino oscillations

323 Oscillation probabilities are computed in a 3-flavour framework including matter effects in constant density matter
 324 (assuming an Earth crust density of 2.6 g/cm³). Custom oscillation probability calculation code was developed within
 325 the VaLOR analysis framework. Details and estimates of the numerical accuracy of this code were first presented in [3]
 326 and, for completeness of the present VaLOR analysis paper, they are given again in Appendix A. Comparisons between
 327 the VaLOR oscillation probability calculation code and Prob3++ [44], which is typically used by the alternative T2K
 328 oscillation analyses, are shown in Appendix B.

¹The BANFF group performed its fit using an NA61-tuned flux (*2011b_v3.2_run1-3c*), the same one used for reweighting our nominal MC templates in Sec. 2.3.

²Reweighting the MC templates to the BANFF best-fit parameters is, in effect, a “special” systematic variation. Therefore, more details on are presented in the section detailing the systematic parameters considered in this analysis (Sec. 3).

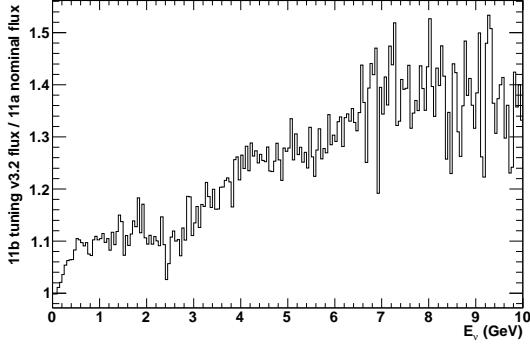


Figure 1: ν_μ 2011b_v3.2_run1-3c flux tuning weights applied to nominal ν_μ and oscillated- ν_e MC templates.

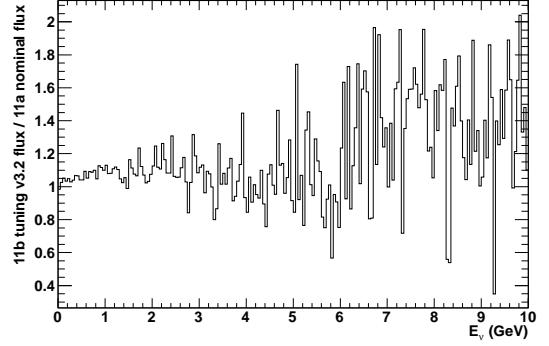


Figure 2: $\bar{\nu}_\mu$ 2011b_v3.2_run1-3c flux tuning weights applied to nominal $\bar{\nu}_\mu$ MC templates.

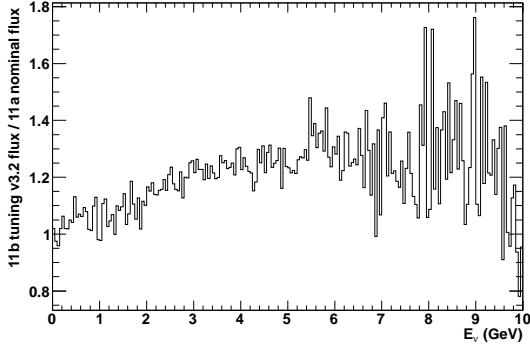


Figure 3: ν_e 2011b_v3.2_run1-3c flux tuning weights applied to nominal ν_e MC templates.

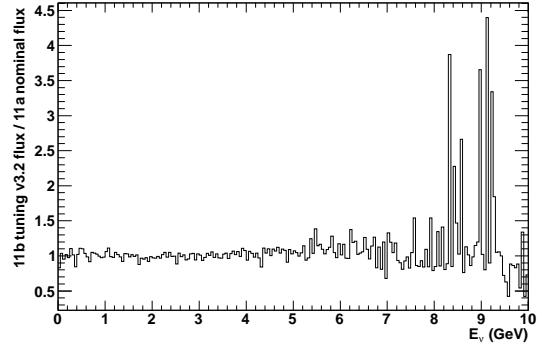


Figure 4: $\bar{\nu}_e$ 2011b_v3.2_run1-3c flux tuning weights applied to nominal $\bar{\nu}_e$ MC templates.

329 Oscillations are applied as a function of true energy to the ν_μ CCQE, ν_μ CC1 π , ν_μ CC coherent, ν_μ CC other,
330 $\bar{\nu}_\mu$ CCQE, $\bar{\nu}_\mu$ CC1 π , $\bar{\nu}_\mu$ CC coherent, $\bar{\nu}_\mu$ CC other, ν_e CCQE, ν_e CC1 π , ν_e CC coherent, ν_e CC other, $\bar{\nu}_e$ CCQE, $\bar{\nu}_e$
331 CC1 π , $\bar{\nu}_e$ CC coherent, $\bar{\nu}_e$ CC other, oscillated ν_e CCQE, oscillated ν_e CC1 π , oscillated ν_e CC coherent and oscillated
332 ν_e CC other MC templates.

333 The MC templates constructed from the unoscillated MC samples are weighted with the corresponding survival
334 probability: The ν_μ templates are weighted with $P(\nu_\mu \rightarrow \nu_\mu)$, the $\bar{\nu}_\mu$ templates with $P(\bar{\nu}_\mu \rightarrow \bar{\nu}_\mu)$, the ν_e templates
335 with $P(\nu_e \rightarrow \nu_e)$ and the $\bar{\nu}_e$ templates with $P(\bar{\nu}_e \rightarrow \bar{\nu}_e)$. The MC templates made from the oscillated ν_e MC sample
336 are weighted with $P(\nu_\mu \rightarrow \nu_e)$ (the sample was generated assuming 100% of ν_μ oscillate to ν_e).

337 We neglect contributions from ν_τ -CC and $\bar{\nu}_\tau$ -CC as their energy threshold is around 3.5 GeV and their effect is
338 negligible.

339 The same $\sin^2 2\theta_{23}$ and $|\Delta m_{32}^2|$ parameters are used for both ν_μ and $\bar{\nu}_\mu$ oscillations.

340 Oscillations are not applied to the NC MC templates ν_μ NC1 π^\pm , ν_μ NC other, $\bar{\nu}_\mu$ NC1 π^\pm , $\bar{\nu}_\mu$ NC other, ν_e
341 NC1 π^\pm , ν_e NC other, $\bar{\nu}_e$ NC1 π^\pm , $\bar{\nu}_e$ NC other since, as explained in Sec. 2.2.4, they serve as proxies for the mixtures
342 of $\nu_e + \nu_\mu + \nu_\tau$ NC and $\bar{\nu}_e + \bar{\nu}_\mu + \bar{\nu}_\tau$ NC MC templates which are unchanged under 3-flavour oscillations.

343 2.6. Nominal and tuned-MC single μ -like ring spectrum predictions

344 In this section, we present the expected numbers of events and single μ -like ring reconstructed energy spectra in
345 SuperK for various oscillation scenarios. We also present estimates of the effect of the NA61 and BANFF tunings
346 and of assumptions made in the 3-flavour neutrino oscillation framework used in this analysis. Unless explicitly stated
347 otherwise, the normal hierarchy is assumed, 2012 PDG values are used for $\sin^2 2\theta_{13}$, $\sin^2 2\theta_{12}$ and Δm_{21}^2 and $\delta_{CP}=0$.
348 All plots were generated for an integrated exposure of 3.010×10^{20} POT.

349 The expected number of single μ -like ring events is shown in Fig. 5 as a function of the oscillation parameters
350 $\sin^2 2\theta_{23}$ and $|\Delta m_{32}^2|$. The expected number of events ranges from ~ 58.5 at maximal mixing and at the 2012 MINOS

best-fit $|\Delta m_{32}^2|$ ($2.39 \times 10^{-3} \text{ eV}^2/c^4$) [31], to more than ~ 76 for oscillation parameter values still within the 2012 MINOS 90% confidence region. This illustrates the great sensitivity of T2K in measuring the θ_{23} mixing angle.

Predicted single μ -like ring SuperK reconstructed energy spectra are shown in Fig. 6 for no oscillations, and in Fig. 7 for oscillations with $\sin^2 2\theta_{23} = 1.0$ and $|\Delta m_{32}^2| = 2.4 \times 10^{-3} \text{ eV}^2/c^4$.

MC tunes derived using NA61 and ND280 data are applied to the nominal MC templates as described earlier in this section. In Fig. 8, the fractional difference is shown in the expected number of single μ -like ring events, as a function of oscillation parameters $\sin^2 2\theta_{23}$ and $|\Delta m_{32}^2|$, obtained when this analysis switches from the nominal MC to the NA61-tuned MC templates. The fractional difference in the expected number of single μ -like ring events when switching from the NA61-tuned MC templates to the BANFF-tuned MC templates is also shown in Fig. 9. From these figures it can be seen that, for oscillation parameters in the 2012 MINOS 90% confidence region, $\sim 11.5\text{--}12.5\%$ more single μ -like ring events are obtained with the NA61-tuned MC than with the nominal MC. In the same part of the parameter space, $\sim 1.8\text{--}2.0\%$ fewer events are expected with the BANFF-tuned MC than with the NA61-tuned MC. The effects of the NA61 and BANFF tunes on the total expected number of single μ -like ring events and on the numbers in each of the 28 component reaction modes are shown in Tab. 2 for no oscillations, and in Tab. 3 for oscillations with $\sin^2 2\theta_{23} = 1.0$ and $|\Delta m_{32}^2| = 2.4 \times 10^{-3} \text{ eV}^2/c^4$. Finally, the effect of the NA61 and BANFF tunes on the reconstructed energy spectrum of single μ -like ring events is shown in Figs. 10 and 11 respectively. In each case, spectra are shown for both no oscillations and for oscillations with $\sin^2 2\theta_{23} = 1.0$ and $|\Delta m_{32}^2| = 2.4 \times 10^{-3} \text{ eV}^2/c^4$.

The effect of the choice of octant of θ_{23} ³ on the energy spectrum of single μ -like ring events is shown in Fig. 12, for oscillations with $\sin^2 2\theta_{23} = 0.95$ (the 2012 PDG 90% lower limit) and $|\Delta m_{32}^2| = 2.4 \times 10^{-3} \text{ eV}^2/c^4$. It follows from Eq. 3 that the effect of changing from the first to second octant is to increase the depth of the oscillation dip, which is why the spectra are almost identical above the oscillation maximum. The fractional difference in the total expected number of single μ -like ring events when switching between the first and second octant is shown in Fig. 13.

When making a fit to obtain the best-fit values of $\sin^2 2\theta_{23}$ and $|\Delta m_{32}^2|$, we fix the non-23 oscillation parameters: $\sin^2 2\theta_{13}$, $\sin^2 2\theta_{12}$, Δm_{21}^2 are fixed to the 2012 PDG values and δ_{CP} is fixed to 0 (see Sec. 4.1.2). The maximum possible effect of this assumption on the expected number of single μ -like ring events is shown in Fig. 14. In each bin of $\sin^2 2\theta_{23}$ and $|\Delta m_{32}^2|$, a large number of toy MC experiments was generated with randomized values of the non-23 parameters. The random values of $\sin^2 2\theta_{13}$, $\sin^2 2\theta_{12}$ and Δm_{21}^2 were drawn from Gaussian distributions with means equal to the 2012 PDG values and standard deviations equal to the 1σ errors, while the values of δ_{CP} were drawn from a uniform distribution between $-\pi$ and $+\pi$. These four non-23 parameters were taken to be uncorrelated. The maximum fractional deviation from the default case was recorded and plotted in Fig. 14. From this figure, it can be seen that the effect of the non-23-sector oscillation parameters is small: the maximum fractional deviation from the default assumption is of the order of $\sim 1\%$ in the part of the parameter space covered by the 2012 MINOS 90% confidence region.

All the results in this analysis assume the normal mass hierarchy. The effect of this assumption on the expected number of single μ -like ring events is shown in Fig. 15 as a function of the oscillation parameters $\sin^2 2\theta_{23}$ and $|\Delta m_{32}^2|$. The effect is large and potentially misleading, and some clarifications are in order. This analysis can assume a given hierarchy (in our case, normal) without loss of generality of its results. Fig. 15 reveals that $|\Delta m_{32}^2|$ is a poor choice as the atmospheric mass-squared difference when both mass hierarchies need to be considered, since $|\Delta m_{32}^2|$ is the largest mass-squared difference for the inverted hierarchy but the second-largest for the normal hierarchy. The large difference shown in Fig. 15 is caused by the change in value of Δm_{31}^2 when switching from the normal to inverted hierarchy.

³It should be noted that, in the earlier versions of this note, the first octant ($\sin(\theta) \leq 0.5$) was assumed for all the PMNS oscillation angles. In this version, the first octant is assumed for all mixing angles unless explicitly stated otherwise. The octant choice does however make a difference; by making some approximations to the 3-flavour $P(\nu_\mu \rightarrow \nu_\mu)$ formula (neglecting $\sin^2\left(\frac{\Delta m_{21}^2 L}{4E}\right)$ and $\sin^2\left(\frac{2\Delta m_{31}^2 L}{4E}\right)$), we get

$$P(\nu_\mu \rightarrow \nu_\mu) \approx 1 - (\cos^4(\theta_{13}) \sin^2(2\theta_{23}) + \sin^2(\theta_{23}) \sin^2(2\theta_{13})) \sin^2\left(\frac{\Delta m_{31}^2 L}{4E}\right). \quad (3)$$

The minimum of Eq. 3 occurs at

$$\sin^2(\theta_{23}) = \frac{1}{2(1 - \sin^2(\theta_{13}))}, \quad (4)$$

and so, when $\theta_{13} \neq 0$, moves from $\sin^2(\theta_{23}) = 0.5$ to $\sin^2(\theta_{23}) > 0.5$. More discussion of this effect can be found in Appendix E of [5]. It should be noted that when $\sin^2(2\theta_{23}) = 1.000$, the oscillation probability is identical, no matter the value of θ_{13} , and no matter which octant is chosen. For both $\sin^2(\theta_{12})$ and $\sin^2(\theta_{13})$ we always assume the first octant.

392 Other choices exist for the atmospheric mass-squared difference, and these are explained in Sec. 4.1.1. An example
 393 of an alternative choice is shown vividly in Fig. 5 in [3]; this technical note describes a repeat, in a 3-flavour framework,
 394 of our official Run1+2 disappearance analysis [2] which was originally performed in a 2-flavour framework.

395 The reader may also be interested in comparisons of oscillated single μ -like ring spectra, obtained in a 3-flavour
 396 framework with spectra obtained in a 2-flavour framework. Many such comparisons were presented in [3].

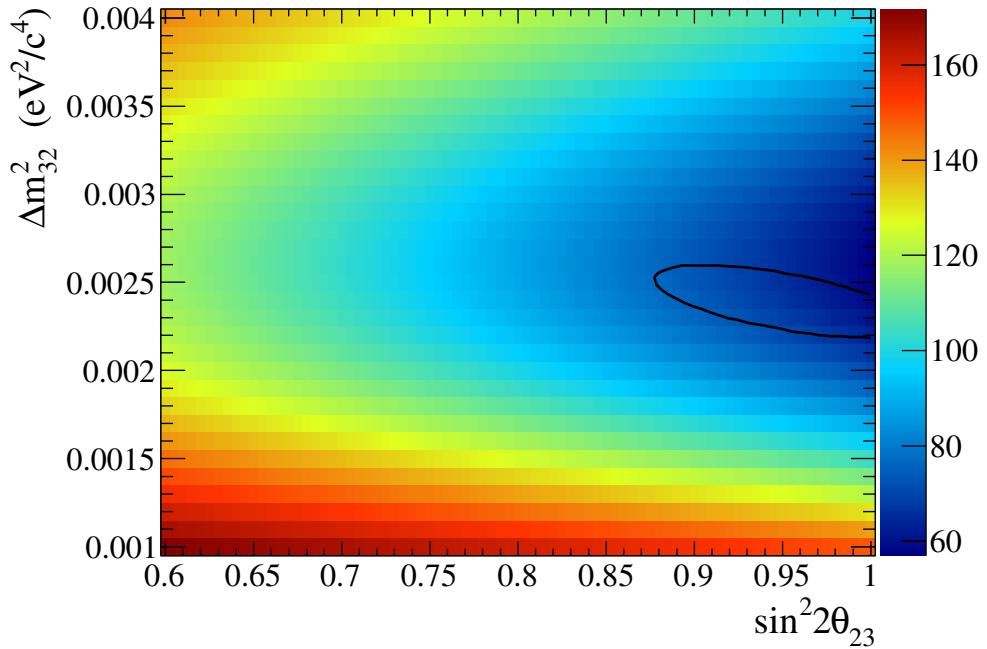


Figure 5: Predicted number of 1-ring μ -like events, as a function of $\sin^2 2\theta_{23}$ and $|\Delta m_{32}^2|$, for an exposure of 3.010×10^{20} POT. The number of events was calculated using the BANFF-tuned MC templates. 2012 PDG values are used for $\sin^2 2\theta_{13}$, $\sin^2 2\theta_{12}$ and Δm_{21}^2 and $\delta_{CP}=0$. The numbers shown were generated assuming the normal hierarchy. The 2012 MINOS 90% confidence region is superimposed for reference.

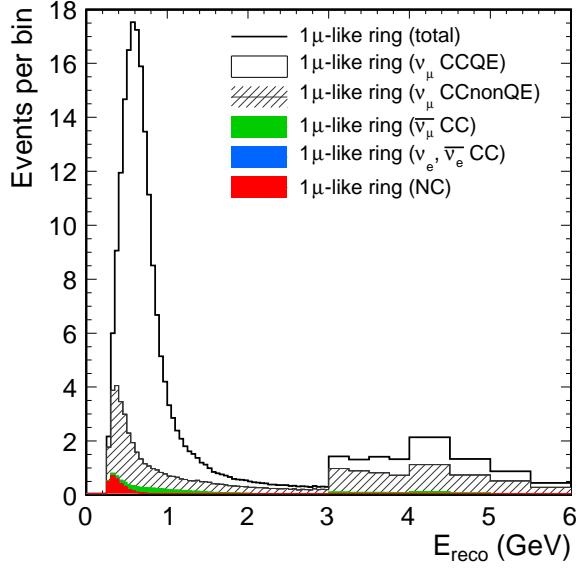


Figure 6: Predicted reconstructed-energy spectrum of 1-ring μ -like events, and contributions from various true neutrino reaction modes, for no oscillations and for an exposure of 3.010×10^{20} POT. The 28 components of the spectrum are calculated separately in the actual analysis, but, for this plot, are grouped into just 5 categories: ν_μ CCQE, ν_μ CCnonQE, $\bar{\nu}_\mu$ CC, $\nu_e/\bar{\nu}_e$ CC and NC. The spectrum was generated using the BANFF-tuned MC templates.

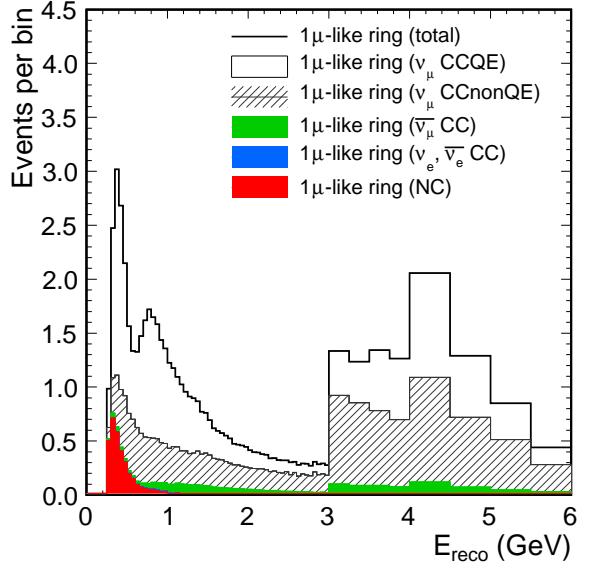


Figure 7: Predicted reconstructed-energy spectrum of 1-ring μ -like events, and contributions from various true neutrino reaction modes, for oscillations with $\sin^2 2\theta_{23}=1.0$ and $|\Delta m_{32}^2|=2.4 \times 10^{-3} \text{ eV}^2/\text{c}^4$ and for an exposure of 3.010×10^{20} POT. The spectrum was generated using the BANFF-tuned MC templates. 2012 PDG values are used for $\sin^2 2\theta_{13}$, $\sin^2 2\theta_{12}$ and Δm_{21}^2 and $\delta_{CP}=0$. The spectrum shown was generated assuming the normal hierarchy. Note that the vertical axis is zoomed in by a factor of 4 compared with Fig. 6.

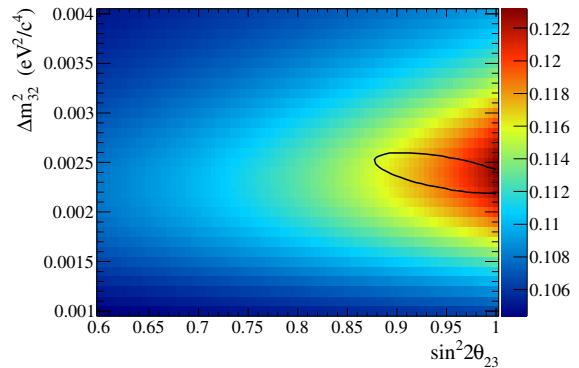


Figure 8: Fractional difference in the predicted number of 1-ring μ -like events as a result of applying the 2011b v3.2 flux tuning to the nominal MC templates. This number is shown as a function of $\sin^2 2\theta_{23}$ and $|\Delta m_{32}^2|$ for an exposure of 3.010×10^{20} POT. The 2012 PDG parameters are used for $\sin^2 2\theta_{13}$, $\sin^2 2\theta_{12}$ and Δm_{21}^2 , and $\delta_{CP}=0$. The numbers shown were generated assuming the normal hierarchy. The MINOS 2012 90% CL region is superimposed for reference.

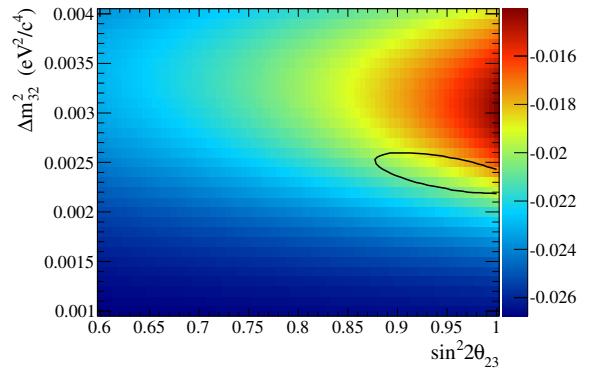


Figure 9: Fractional difference in the predicted number of 1-ring μ -like events as a result of applying the BANFF flux and cross-section tuning to the 2011b v3.2 flux tuned MC templates. This number is shown as a function of $\sin^2 2\theta_{23}$ and $|\Delta m_{32}^2|$ and for an exposure of 3.010×10^{20} POT. The 2012 PDG values are used for $\sin^2 2\theta_{13}$, $\sin^2 2\theta_{12}$ and Δm_{21}^2 , and $\delta_{CP}=0$. The numbers shown were generated assuming the normal hierarchy. The MINOS 2012 90% CL region is superimposed for reference.

	N_{SK} (nominal MC)	N_{SK} (NA61-tuned MC)	N_{SK} (BANFF-tuned MC)
Total	190.986142	210.464599	204.747590
ν_μ CCQE	151.820154	166.353705	155.044970
ν_μ CC 1π	25.717606	28.879686	34.945661
ν_μ CC coherent	0.898432	1.005621	0.950276
ν_μ CC other	3.584984	4.315475	4.198557
ν_μ/ν_τ NC $1\pi^{+/-}$	1.492903	1.696744	1.625483
ν_μ/ν_τ NC other	1.294522	1.521644	1.466497
$\bar{\nu}_\mu$ CCQE	4.118572	4.459811	3.981437
$\bar{\nu}_\mu$ CC 1π	1.336699	1.445418	1.762408
$\bar{\nu}_\mu$ CC coherent	0.194978	0.211123	0.202799
$\bar{\nu}_\mu$ CC other	0.236537	0.253912	0.247794
$\bar{\nu}_\mu/\bar{\nu}_\tau$ NC $1\pi^{+/-}$	0.084582	0.091984	0.090422
$\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other	0.073460	0.079580	0.077614
ν_e CCQE	0.015774	0.016972	0.016260
ν_e CC 1π	0.009050	0.009932	0.013125
ν_e CC coherent	0.000403	0.000434	0.000434
ν_e CC other	0.002568	0.003048	0.003051
ν_e NC $1\pi^{+/-}$	0.042494	0.048652	0.049421
ν_e NC other	0.049084	0.057414	0.057684
$\bar{\nu}_e$ CCQE	0.000822	0.000827	0.000790
$\bar{\nu}_e$ CC 1π	0.000599	0.000601	0.000745
$\bar{\nu}_e$ CC coherent	0.000073	0.000073	0.000073
$\bar{\nu}_e$ CC other	0.000214	0.000219	0.000219
$\bar{\nu}_e$ NC $1\pi^{+/-}$	0.005755	0.005805	0.005916
$\bar{\nu}_e$ NC other	0.005876	0.005918	0.005954
Oscillated ν_e CCQE	0.000000	0.000000	0.000000
Oscillated ν_e CC 1π	0.000000	0.000000	0.000000
Oscillated ν_e CC coherent	0.000000	0.000000	0.000000
Oscillated ν_e CC other	0.000000	0.000000	0.000000

Table 2: Calculated numbers of 1-ring μ -like events without oscillations using the nominal MC templates, the NA61-tuned MC templates and the BANFF-tuned MC templates. The total numbers of events and the numbers of events from each mode considered in this analysis are shown. These numbers were calculated for an exposure of 3.010×10^{20} POT.

	N_{SK} (nominal MC)	N_{SK} (NA61-tuned MC)	N_{SK} (BANFF-tuned MC)
Total	52.890886	59.406174	58.367775
ν_μ CCQE	30.122383	33.277415	30.285520
ν_μ CC 1π	12.736216	14.628739	16.931486
ν_μ CC coherent	0.365047	0.420613	0.399710
ν_μ CC other	3.187277	3.862403	3.771051
ν_μ/ν_τ NC $1\pi^{+/-}$	1.492903	1.696744	1.625483
ν_μ/ν_τ NC other	1.294522	1.521644	1.466497
$\bar{\nu}_\mu$ CCQE	2.023300	2.190691	1.891082
$\bar{\nu}_\mu$ CC 1π	0.958303	1.032827	1.228001
$\bar{\nu}_\mu$ CC coherent	0.104487	0.112894	0.108444
$\bar{\nu}_\mu$ CC other	0.209999	0.225107	0.220043
$\bar{\nu}_\mu/\bar{\nu}_\tau$ NC $1\pi^{+/-}$	0.084582	0.091984	0.090422
$\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other	0.073460	0.079580	0.077614
ν_e CCQE	0.014633	0.015752	0.015068
ν_e CC 1π	0.008572	0.009421	0.012426
ν_e CC coherent	0.000375	0.000404	0.000404
ν_e CC other	0.002530	0.003005	0.003007
ν_e NC $1\pi^{+/-}$	0.042494	0.048652	0.049421
ν_e NC other	0.049084	0.057414	0.057684
$\bar{\nu}_e$ CCQE	0.000785	0.000790	0.000755
$\bar{\nu}_e$ CC 1π	0.000583	0.000585	0.000724
$\bar{\nu}_e$ CC coherent	0.000070	0.000070	0.000070
$\bar{\nu}_e$ CC other	0.000212	0.000217	0.000217
$\bar{\nu}_e$ NC $1\pi^{+/-}$	0.005755	0.005805	0.005916
$\bar{\nu}_e$ NC other	0.005876	0.005918	0.005954
Oscillated ν_e CCQE	0.079970	0.087419	0.082883
Oscillated ν_e CC 1π	0.024965	0.027318	0.035271
Oscillated ν_e CC coherent	0.001860	0.002039	0.001949
Oscillated ν_e CC other	0.000644	0.000723	0.000672

Table 3: Calculated numbers of 1-ring μ -like events using the nominal MC templates, the NA61-tuned MC templates and the BANFF-tuned MC templates. The total numbers of events and the numbers of events from each mode considered in this analysis are shown. These numbers were calculated for an exposure of 3.010×10^{20} POT and oscillations with $\sin^2 2\theta_{23}=1.0$ and $|\Delta m_{32}^2|=2.4 \times 10^{-3} \text{ eV}^2/c^4$. The 2012 PDG parameters are used for $\sin^2 2\theta_{13}$, $\sin^2 2\theta_{12}$ and Δm_{21}^2 and $\delta_{CP}=0$. The normal hierarchy is assumed.

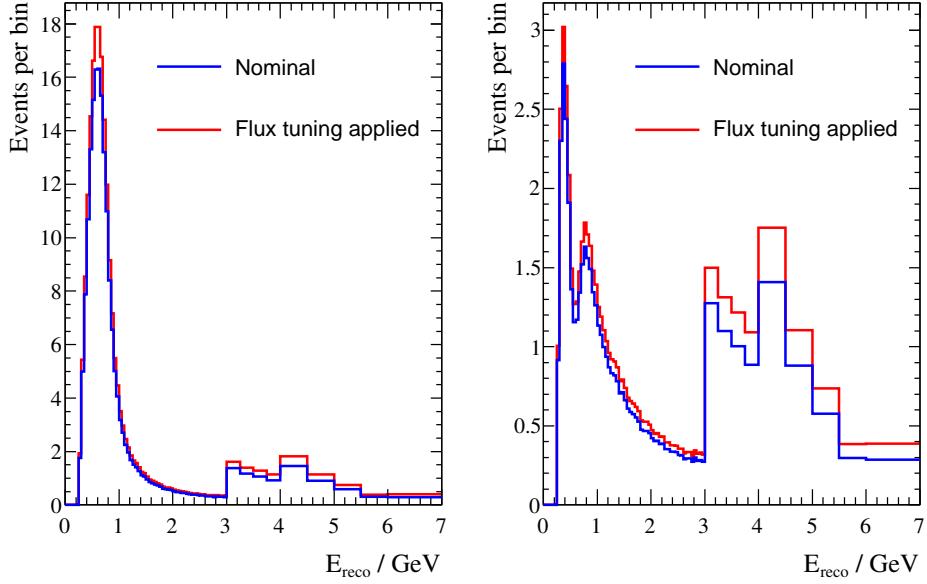


Figure 10: Reconstructed-energy spectrum of 1-ring μ -like events, for an exposure of 3.010×10^{20} POT, both with and without the effect of the `2011b_v3.2_run1-3c` flux tuning of the nominal MC templates. The spectra are shown both for no oscillations (left) and for oscillations with $\sin^2 2\theta_{23}=1.0$, $|\Delta m_{32}^2|=2.4 \times 10^{-3} \text{ eV}^2/c^4$, the 2012 PDG values for $\sin^2 2\theta_{13}$, $\sin^2 2\theta_{12}$ and Δm_{21}^2 , and $\delta_{CP}=0$ (right). Results shown for the normal hierarchy.

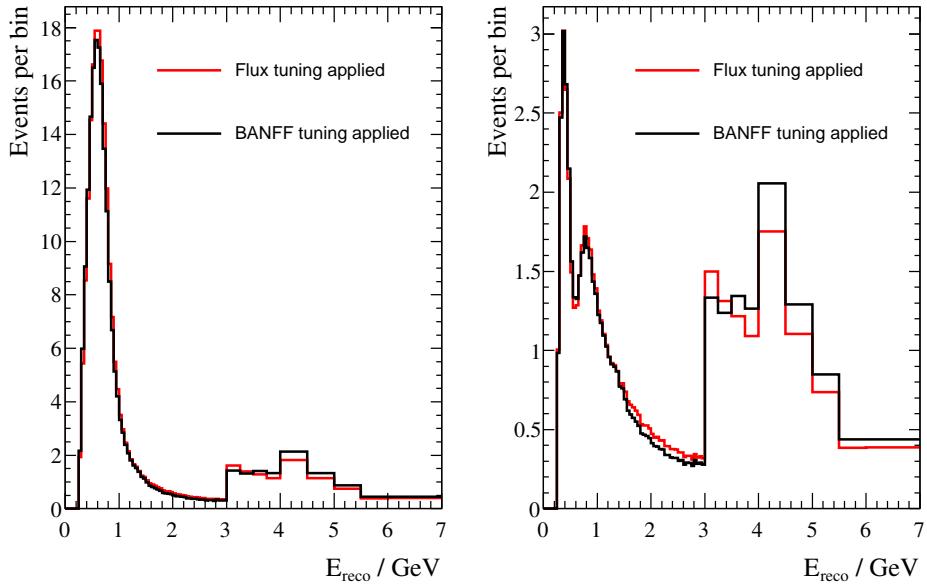


Figure 11: Reconstructed-energy spectrum of 1-ring μ -like events, for an exposure of 3.010×10^{20} POT, both with and without the effect of BANFF flux and cross-section tuning on the NA61-tuned `2011b_v3.2_run1-3c` flux MC templates. The spectra are shown both for no 23-sector oscillations (left) and for oscillations with $\sin^2 2\theta_{23}=1.0$ and $|\Delta m_{32}^2|=2.4 \times 10^{-3} \text{ eV}^2/c^4$ (right). In all spectra, the 2012 PDG parameters are used for $\sin^2 2\theta_{13}$, $\sin^2 2\theta_{12}$ and Δm_{21}^2 and $\delta_{CP}=0$. Results shown for the normal hierarchy.

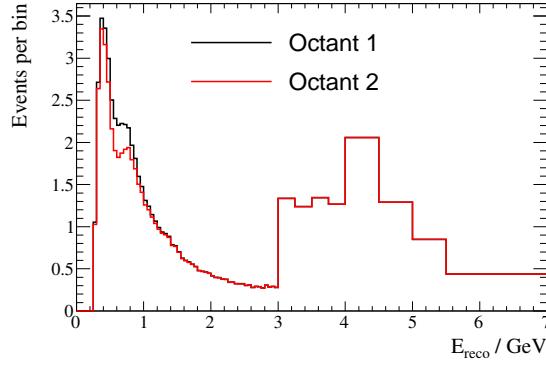


Figure 12: Predicted reconstructed-energy spectrum of 1-ring μ -like events, for an exposure of 3.010×10^{20} POT, for θ_{23} both in the first octant and second octant. The spectra are shown oscillations with $\sin^2 2\theta_{23}=0.95$, $|\Delta m_{32}^2|=2.4 \times 10^{-3} \text{ eV}^2/c^4$, the 2012 PDG values for $\sin^2 2\theta_{13}$, $\sin^2 2\theta_{12}$ and Δm_{21}^2 , and $\delta_{CP}=0$ (right). Results shown for the normal hierarchy.

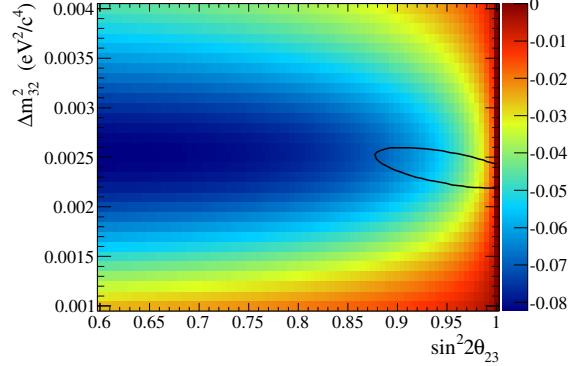


Figure 13: Fractional difference in the predicted number of 1-ring μ -like events between assuming that θ_{23} is in the first octant and assuming it is in the second octant. The fractional difference is shown as function of $\sin^2 2\theta_{23}$ and $|\Delta m_{32}^2|$, for an exposure of 3.010×10^{20} POT. The number of events was calculated using the BANFF-tuned MC templates. The 2012 PDG values are used for $\sin^2 2\theta_{13}$, $\sin^2 2\theta_{12}$ and Δm_{21}^2 , and $\delta_{CP}=0$. Results shown for the normal hierarchy. The 2012 MINOS 90% confidence region is superimposed for reference.

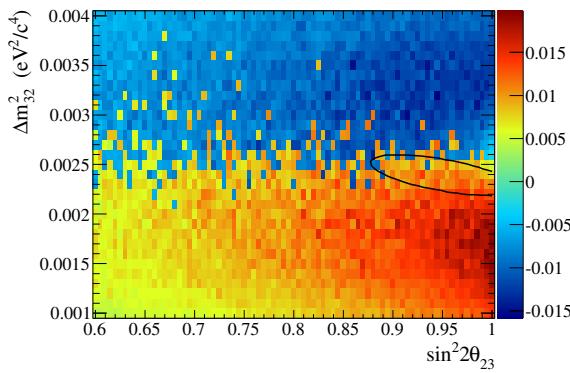


Figure 14: Maximum value of the fractional difference in the predicted number of 1-ring μ -like events between varying each of $\sin^2 2\theta_{13}$, $\sin^2 2\theta_{12}$, Δm_{21}^2 and δ_{CP} within their allowed ranges and their nominal values (these are the 2012 PDG values for $\sin^2 2\theta_{13}$, $\sin^2 2\theta_{12}$ and Δm_{21}^2 , and $\delta_{CP}=0$). The fractional difference is shown as function of $\sin^2 2\theta_{23}$ and $|\Delta m_{32}^2|$, for an exposure of 3.010×10^{20} POT. The number of events was calculated using the BANFF-tuned MC templates. The normal hierarchy was assumed. The 2012 MINOS 90% confidence region is superimposed for reference.

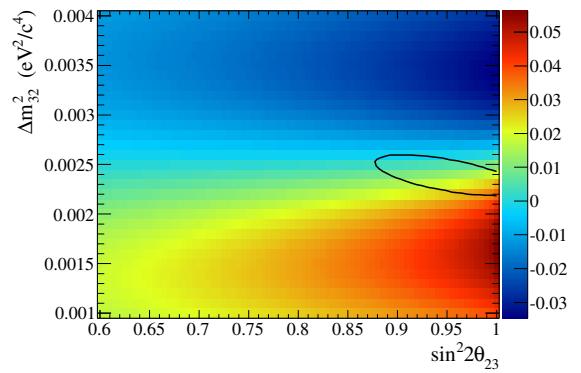


Figure 15: Fractional difference in the predicted number of 1-ring μ -like events between assuming the normal hierarchy and assuming the inverted hierarchy. The fractional difference is shown as function of $\sin^2 2\theta_{23}$ and $|\Delta m_{32}^2|$, for an exposure of 3.010×10^{20} POT. The number of events was calculated using the BANFF-tuned MC templates. The 2012 PDG values are used for $\sin^2 2\theta_{13}$, $\sin^2 2\theta_{12}$ and Δm_{21}^2 , and $\delta_{CP}=0$. The 2012 MINOS 90% confidence region is superimposed for reference.

397 **3. Systematic effects in the prediction of the single μ -like ring event reconstructed energy spectrum**

398 **3.1. Input systematic parameters**

399 This analysis considers 48 systematic parameters which can be grouped into 4 categories:

- 400 1. SuperK detector parameters (Sec. 3.1.1)
 401 2. Correlated flux and cross-section parameters tuned by the BANFF group to ND280 data (Sec. 3.1.2)
 402 3. Uncorrelated cross-section parameters (Sec. 3.1.3)
 403 4. Intranuclear and secondary interactions (Sec. 3.1.4).

404 A summary of all systematic parameters considered in this analysis is given in Tab. 4. These systematic parameters
 405 are applied to the MC templates as shown in Tab. 5.

406 **3.1.1. SuperK detector systematics**

407 The SuperK detector systematics are unchanged from the 2010 analyses [10]. They can be broken down into two
 408 categories:

- 409 1. Reconstructed energy scale
 410 The effect of the uncertainty in the reconstructed energy scale is calculated by scaling the bin edges of the MC
 411 templates and, assuming uniform distribution of events within the bins, calculating the number of events gained
 412 from / lost to neighbouring bins. The systematic parameter $f_{E;r}^{SK}$ controls the energy scale and its uncertainty is
 413 estimated to be 2.3% [10]. The effect of the energy scale uncertainty is propagated to all MC templates as shown
 414 in Tab. 5.

- 415 2. Detector efficiencies
 416 Uncertainty in the efficiencies comes from the uncertainties in the fiducial volume and reduction chain, and the
 417 OD, ring-counting, PID, momentum and decay-electron cuts. The efficiency errors used in this analysis [10] are
 418 listed below.

- 419 • $\nu_\mu, \bar{\nu}_\mu$ CCQE:
 420 An energy-dependent ring-counting efficiency error and an energy-independent “other” efficiency error
 421 (due to all sources of uncertainty other than ring-counting) are taken into account. For the ring-counting
 422 efficiency, we assume correlated errors in 3 E_{reco} bins: 0 - 0.4 GeV, 0.4 - 1.1 GeV and > 1.1 GeV. The
 423 following error matrix is used:

$$424 \begin{pmatrix} (1.7\%)^2 & 0.59 * 1.7\% * 3.5\% & 0.33 * 1.7\% * 9.3\% \\ & (3.5\%)^2 & 0.61 * 3.5\% * 9.3\% \\ & & (9.3\%)^2 \end{pmatrix}$$

425 For the “other” efficiency, we assume an energy-independent error of 1.8%.

- 426 • $\nu_\mu, \bar{\nu}_\mu$ CCnonQE:
 427 A single 20% energy-independent error is assumed. This error was calculated by combining the quoted
 428 energy-independent ring-counting (19.9%) and other (1.7%) errors in quadrature.
 429 • NC:
 430 A single 111% energy-independent error is assumed. This error was calculated by combining the quoted
 431 energy-independent ring-counting (48.2%), PID (100%) and other (1.7%) errors in quadrature.
 432 • $\nu_e, \bar{\nu}_e$ CC:
 433 A single $\sim 100\%$ energy-independent error is assumed.

434 The ν_μ and $\bar{\nu}_\mu$ CCQE ring-counting efficiency is controlled by the systematic parameters $f_{CCQERC0;r}^{SK}$ ($E_{reco} <$
 435 0.4 GeV), $f_{CCQERC1;r}^{SK}$ ($0.4 \text{ GeV} \leq E_{reco} \leq 1.1 \text{ GeV}$) and $f_{CCQERC2;r}^{SK}$ ($E_{reco} > 1.1 \text{ GeV}$), while the “other”
 436 efficiency is controlled by parameter $f_{CCQERoth;r}^{SK}$. The ν_μ and $\bar{\nu}_\mu$ CCnonQE, the NC and the $\nu_e, \bar{\nu}_e$ CC effi-
 437 ciencies are controlled by the systematic parameters $f_{CCnQE;r}^{SK}, f_{NC;r}^{SK}$ and $f_{\nu_e;r}^{SK}$ respectively. These systematic
 438 parameters are applied to the MC templates as specified in Tab. 5.

SuperK detector systematics

$f_{E;r}^{SK}$	Reconstructed energy scale	2.3%
$f_{CCQErci;r}^{SK}$	$\nu_\mu, \bar{\nu}_\mu$ CCQE ring-counting efficiency. Three correlated systematic parameters are included (i=0,1,2) corresponding to different reconstructed energy ranges. See Sec.3.1.1.	1.7% (< 0.4 GeV) 3.5% (0.4-1.1 GeV) 9.3% (> 1.1 GeV)
$f_{CCQEoth;r}^{SK}$	$\nu_\mu, \bar{\nu}_\mu$ CCQE other (all but ring-counting) efficiency. Includes fiducial volume, reduction chain, OD cut, PID cut, momentum cut and decay electron cut efficiencies.	1.8%
$f_{CCnonQE;r}^{SK}$	$\nu_\mu, \bar{\nu}_\mu$ CCnQE efficiency	20%
$f_{NC;r}^{SK}$	NC efficiency	111%
$f_{\nu_e;r}^{SK}$	$\nu_e, \bar{\nu}_e$ efficiency	100%

Correlated flux and cross-section (BANFF) systematics

$f_{i;t,r}^{banff}$	Flux and cross-section parameters tuned by BANFF group on ND280 data. Twenty-three correlated parameters are included (i=0,...,22). See Sec. 3.1.2.
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Uncorrelated cross-section systematics

$f_{pF;t,r}$	Fermi momentum (CCQE only)	225 ± 30 MeV
$f_{bindE;t,r}$	Binding energy for ^{16}O (CCQE only)	27 ± 9 MeV
$f_{SF;t,r}$	Nuclear environment modeling; switch from Fermi Gas (RFG) to Spectral Function (SF) model (CCQE only).	0 (RFG) - 1 (SF)
$f_{\pi-less\Delta;t,r}$	Fraction of π -less Δ decays in resonance neutrino-production events	20%
$f_{CCothShape;t,r}$	Parameterizes the uncertainty in CC multipion, CC DIS and CC resonant η , K and photon production.	40%
$f_{Wshape;t,r}$	Modifies the shape of the initial pion momentum distribution (before final-state interactions) in resonance interactions.	87.8 ± 45.3
$f_{CCcoh;t}$	CC coherent cross-section	100%
$f_{NC1\pi^\pm;t}$	NC1 π^\pm cross-section	30%
$f_{NCoth;t}$	NC other (all but single π^\pm) cross-section	30%
$f_{CC\nu_e;t}$	ν_e / ν_μ CC cross-section ratio	3%
$f_{CC\bar{\nu};t}$	$\bar{\nu} / \nu$ CC cross-section ratio	40%

FSI+SI systematics

$f_{i;r}^{FSI}$	FSI (final state interaction / intranuclear hadron transport) and SI (secondary interaction / detector hadron transport) systematic parameters. Six correlated parameters are included (i=0,...,5) corresponding to different modes and reconstructed energy bins. See Sec. 3.1.4.
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Table 4: Summary table of systematic parameters included the VaLOR ν_μ -disappearance analysis. The nuisance parameter symbols used in this paper are shown in the first column. An index r in the nuisance parameter symbol denotes dependence on reconstructed energy while an index t denotes dependence on true energy. An index i is used where multiple systematic parameters, typically correlated between themselves, are grouped together; in these cases we refer you to the main text for the exact parameter definition and for the input covariance matrix. Wherever practical, the physics parameter affected by the systematic parameter is shown in the second column and the size of the uncertainty is shown in the third column.

	ν_μ CCQE	ν_μ CC1 π	ν_μ CC coherent	ν_μ CC other	ν_μ NC1 π^\pm	ν_μ NC other	$\bar{\nu}_\mu$ CCQE	$\bar{\nu}_\mu$ CC1 π	$\bar{\nu}_\mu$ CC coherent	$\bar{\nu}_\mu$ CC other	$\bar{\nu}_\mu$ NC1 π^\pm	$\bar{\nu}_\mu$ NC other	ν_e CCQE	ν_e CC1 π	ν_e CC coherent	ν_e CC other	ν_e NC1 π^\pm	ν_e NC other	$\bar{\nu}_e$ CC coherent	$\bar{\nu}_e$ CC other	$\nu_{e,\nu}$ CCQE	$\nu_{e,\nu}$ CC1 π	$\nu_{e,\nu}$ CC coherent	$\nu_{e,\nu}$ CC other		
$f_{E;r}^{SK}$	✓	✓																								
$f_{CCQERC0;r}^{SK}$	✓	✓																								
$f_{CCQERC1;r}^{SK}$	✓																									
$f_{CCQERC2;r}^{SK}$	✓																									
$f_{CCQEoth;r}^{SK}$	✓																									
$f_{CCnQE;r}^{SK}$		✓	✓	✓																						
$f_{NC;r}^{SK}$					✓	✓																				
$f_{\nu_e;r}^{SK}$																										
$f_{0;t,r}^{banff}$	✓	✓	✓	✓	✓	✓																				
$f_{1;t,r}^{banff}$	✓	✓	✓	✓	✓	✓																				
$f_{2;t,r}^{banff}$	✓	✓	✓	✓	✓	✓																				
$f_{3;t,r}^{banff}$	✓	✓	✓	✓	✓	✓																				
$f_{5;t,r}^{banff}$	✓	✓	✓	✓	✓	✓																				
$f_{6;t,r}^{banff}$	✓	✓	✓	✓	✓	✓																				
$f_{7;t,r}^{banff}$	✓	✓	✓	✓	✓	✓																				
$f_{8;t,r}^{banff}$	✓	✓	✓	✓	✓	✓																				
$f_{9;t,r}^{banff}$	✓	✓	✓	✓	✓	✓																				
$f_{10;t,r}^{banff}$	✓	✓	✓	✓	✓	✓																				
$f_{11;t,r}^{banff}$																	✓	✓	✓	✓	✓	✓	✓	✓	✓	
$f_{12;t,r}^{banff}$																	✓	✓	✓	✓	✓	✓	✓	✓	✓	
$f_{13;t,r}^{banff}$																	✓	✓	✓	✓	✓	✓	✓	✓	✓	
$f_{14;t,r}^{banff}$																	✓	✓	✓	✓	✓	✓	✓	✓	✓	
$f_{15;t,r}^{banff}$																	✓	✓	✓	✓	✓	✓	✓	✓	✓	
$f_{16;t,r}^{banff}$	✓																									
$f_{17;t,r}^{banff}$	✓	✓	✓	✓	✓	✓											✓	✓	✓	✓	✓	✓	✓	✓	✓	
$f_{18;t,r}^{banff}$	✓																✓									
$f_{19;t,r}^{banff}$	✓																									
$f_{20;t,r}^{banff}$	✓																									
$f_{21;t,r}^{banff}$	✓																									
$f_{22;t,r}^{banff}$	✓																									
$f_{pF;t,r}$	✓																									
$f_{SF;t,r}$	✓																									
$f_{\pi-less\Delta;t,r}$	✓		✓	✓													✓	✓	✓	✓	✓	✓	✓	✓	✓	
$f_{bindE;t,r}$	✓																✓									
$f_{CCothShape;t,r}$		✓																✓								
$f_{Wshape;t,r}$		✓	✓														✓	✓								
$f_{CCcoh;t}$	✓																	✓								
$f_{NC1\pi^\pm;t}$			✓															✓								
$f_{NCoth;t}$				✓														✓								
$f_{CC\nu_e;t}$																		✓	✓	✓	✓	✓	✓	✓	✓	✓
$f_{CC\bar{\nu}_e;t}$																	✓	✓	✓	✓	✓	✓	✓	✓	✓	
$f_{0;r}^{FSI}$	✓																									
$f_{1;r}^{FSI}$	✓																									
$f_{2;r}^{FSI}$	✓																									
$f_{3;r}^{FSI}$	✓	✓	✓														✓	✓	✓	✓	✓	✓	✓	✓	✓	
$f_{4;r}^{FSI}$																	✓	✓	✓	✓	✓	✓	✓	✓	✓	
$f_{5;r}^{FSI}$																	✓	✓								

Table 5: A ✓ symbol denotes that the given MC template is modified when the given systematic parameter is tweaked. The table lists all 48 systematic parameters considered in this analysis (first column) and all 28 MC templates used for constructing the single μ -like ring event reconstructed energy spectrum p.d.f (first row).

Parameter	Definition	Best-fit value (tune v8)
$f_{0;t,r}^{banff}$	ν_μ flux normalisation, E = 0.0 - 0.4 GeV	0.995
$f_{1;t,r}^{banff}$	ν_μ flux normalisation, E = 0.4 - 0.5 GeV	1.007
$f_{2;t,r}^{banff}$	ν_μ flux normalisation, E = 0.5 - 0.6 GeV	1.002
$f_{3;t,r}^{banff}$	ν_μ flux normalisation, E = 0.6 - 0.7 GeV	0.963
$f_{4;t,r}^{banff}$	ν_μ flux normalisation, E = 0.7 - 1.0 GeV	0.901
$f_{5;t,r}^{banff}$	ν_μ flux normalisation, E = 1.0 - 1.5 GeV	0.910
$f_{6;t,r}^{banff}$	ν_μ flux normalisation, E = 1.5 - 2.5 GeV	0.936
$f_{7;t,r}^{banff}$	ν_μ flux normalisation, E = 2.5 - 3.5 GeV	0.967
$f_{8;t,r}^{banff}$	ν_μ flux normalisation, E = 3.5 - 5.0 GeV	0.988
$f_{9;t,r}^{banff}$	ν_μ flux normalisation, E = 5.0 - 7.0 GeV	0.997
$f_{10;t,r}^{banff}$	ν_μ flux normalisation, E = 7.0 - 30.0 GeV	1.004
$f_{11;t,r}^{banff}$	$\bar{\nu}_\mu$ flux normalisation, E = 0.0 - 0.7 GeV	0.980
$f_{12;t,r}^{banff}$	$\bar{\nu}_\mu$ flux normalisation, E = 0.7 - 1.0 GeV	0.958
$f_{13;t,r}^{banff}$	$\bar{\nu}_\mu$ flux normalisation, E = 1.0 - 1.5 GeV	0.947
$f_{14;t,r}^{banff}$	$\bar{\nu}_\mu$ flux normalisation, E = 1.5 - 2.5 GeV	0.953
$f_{15;t,r}^{banff}$	$\bar{\nu}_\mu$ flux normalisation, E = 2.5 - 30.0 GeV	0.985
$f_{16;t,r}^{banff}$	CCQE axial mass normalisation, x_{MAQE}	1.049
$f_{17;t,r}^{banff}$	Resonant axial mass normation, x_{MARES}	1.011
$f_{18;t,r}^{banff}$	CCQE normalisation, E = 0.0 - 1.5 GeV	0.951
$f_{19;t,r}^{banff}$	CCQE normalisation, E = 1.5 - 3.5 GeV	0.708
$f_{20;t,r}^{banff}$	CCQE normalisation, E = 3.5 - 30.0 GeV	1.347
$f_{21;t,r}^{banff}$	CC1 π normalisation, E = 0.0 - 2.5 GeV	1.370
$f_{22;t,r}^{banff}$	CC1 π normalisation, E = 2.5 - 30.0 GeV	1.016

Table 6: BANFF parameters and best-fit values (v8 tune) [14].

442 3.1.2. Correlated flux and cross-section (BANFF) systematics

443 The postfit uncertainties of all BANFF flux and cross-section parameters and their correlations are taken into
444 account. A list of the BANFF parameters is given in Tab. 6. The BANFF postfit covariance matrix is shown in Fig.
445 16, while both postfit and prefit 1σ fractional errors for all parameters are shown in Fig. 17. These fractional errors are
446 computed from the square roots of the diagonal elements of the corresponding input covariance matrix.

447 Version 8 of the BANFF matrix is used.

448 Only the ν_μ and $\bar{\nu}_\mu$ flux parameters are included in the BANFF fit. The ν_e and $\bar{\nu}_e$ flux parameters have a negligible
449 effect as shown by the results of the systematic study⁴ in Tab. 7.

450 Only those cross-section parameters that are expected to have some cancellation between the ND280 and SuperK
451 are included in the BANFF fit. The other cross-section parameters included in this analysis are taken to be uncorrelated
452 with the flux parameters and to have no cancellation between the near and far detectors. These uncorrelated cross-
453 section parameters are described in Sec. 3.1.3.

⁴The study was performed with an older version of the BANFF matrix (v5)

454 The BANFF parameters are applied to the MC templates as specified in Tab. 5. All but two of the BANFF cross-
 455 section parameters are simple normalization factors. The parameters $f_{16;t,r}^{banff}$ and $f_{17;t,r}^{banff}$ ⁵ parameterize the effect of
 456 the uncertainty of the axial masses used for modeling CC quasi-elastic (M_A^{QE})⁶ and resonance neutrino-production
 457 (M_A^{RES}) events respectively; these have a more complicated, often non-linear, dependence on the true and recon-
 458 structed neutrino energy. Event reweighting methods were used to obtain the fractional changes of the number of
 459 events, in bins of true and reconstructed neutrino energy, for a range of values (-3.0 σ , -2.5 σ , -2.0 σ , ..., +3.0 σ) of the
 460 $f_{17;t,r}^{banff}$ and $f_{18;t,r}^{banff}$ parameters. In our p.d.f. calculation, cross-section splines using a polynomial of order 3 are used
 461 to interpolate between these event weights to obtain the fractional change for any value of these systematic parameters
 462 in the (-3.0 σ , +3.0 σ) range.

Systematic	$\sin^2(2\theta_{23}) = 1.0$		$\sin^2(2\theta_{23}) = 0.9$	
	$\delta \sin^2(2\theta_{23})$	$\delta \Delta m_{32}^2 $	$\delta \sin^2(2\theta_{23})$	$\delta \Delta m_{32}^2 $
Statistical	0.17	0.00014	0.05	0.00022
$\bar{\nu}_\mu$ flux 0.0-0.4 GeV	$1 \cdot 10^{-6}$	$4 \cdot 10^{-7}$	$5 \cdot 10^{-5}$	$4 \cdot 10^{-7}$
$\bar{\nu}_\mu$ flux 0.4-0.5 GeV	$1 \cdot 10^{-6}$	$3 \cdot 10^{-7}$	$4 \cdot 10^{-5}$	$4 \cdot 10^{-7}$
$\bar{\nu}_\mu$ flux 0.5-0.6 GeV	$< 1 \cdot 10^{-6}$	$2 \cdot 10^{-7}$	$4 \cdot 10^{-5}$	$2 \cdot 10^{-7}$
$\bar{\nu}_\mu$ flux 0.6-0.7 GeV	$< 1 \cdot 10^{-6}$	$1 \cdot 10^{-7}$	$5 \cdot 10^{-5}$	$2 \cdot 10^{-7}$
$\bar{\nu}_\mu$ flux 0.7-1.0 GeV	$2 \cdot 10^{-6}$	$4 \cdot 10^{-7}$	$12 \cdot 10^{-5}$	$6 \cdot 10^{-7}$
$\bar{\nu}_\mu$ flux 1.0-1.5 GeV	$2 \cdot 10^{-6}$	$11 \cdot 10^{-7}$	$12 \cdot 10^{-5}$	$17 \cdot 10^{-7}$
$\bar{\nu}_\mu$ flux 1.5-2.5 GeV	$1 \cdot 10^{-6}$	$9 \cdot 10^{-7}$	$4 \cdot 10^{-5}$	$15 \cdot 10^{-7}$
$\bar{\nu}_\mu$ flux 2.5-3.5 GeV	$< 1 \cdot 10^{-6}$	$2 \cdot 10^{-7}$	$4 \cdot 10^{-5}$	$2 \cdot 10^{-7}$
$\bar{\nu}_\mu$ flux 3.5-5.0 GeV	$< 1 \cdot 10^{-6}$	$2 \cdot 10^{-7}$	$4 \cdot 10^{-5}$	$2 \cdot 10^{-7}$
$\bar{\nu}_\mu$ flux 5.0-7.0 GeV	$< 1 \cdot 10^{-6}$	$2 \cdot 10^{-7}$	$4 \cdot 10^{-5}$	$2 \cdot 10^{-7}$
$\bar{\nu}_\mu$ flux 7.0-30.0 GeV	$< 1 \cdot 10^{-6}$	$2 \cdot 10^{-7}$	$4 \cdot 10^{-5}$	$2 \cdot 10^{-7}$
ν_e flux 0.0-0.5 GeV	$< 1 \cdot 10^{-6}$	$2 \cdot 10^{-7}$	$4 \cdot 10^{-5}$	$2 \cdot 10^{-7}$
ν_e flux 0.5-0.7 GeV	$< 1 \cdot 10^{-6}$	$2 \cdot 10^{-7}$	$4 \cdot 10^{-5}$	$2 \cdot 10^{-7}$
ν_e flux 0.7-0.8 GeV	$< 1 \cdot 10^{-6}$	$2 \cdot 10^{-7}$	$4 \cdot 10^{-5}$	$2 \cdot 10^{-7}$
ν_e flux 0.8-1.5 GeV	$< 1 \cdot 10^{-6}$	$2 \cdot 10^{-7}$	$4 \cdot 10^{-5}$	$2 \cdot 10^{-7}$
ν_e flux 1.5-2.5 GeV	$< 1 \cdot 10^{-6}$	$2 \cdot 10^{-7}$	$4 \cdot 10^{-5}$	$2 \cdot 10^{-7}$
ν_e flux 2.5-4.0 GeV	$< 1 \cdot 10^{-6}$	$2 \cdot 10^{-7}$	$4 \cdot 10^{-5}$	$2 \cdot 10^{-7}$
ν_e flux 4.0-30.0 GeV	$< 1 \cdot 10^{-6}$	$2 \cdot 10^{-7}$	$4 \cdot 10^{-5}$	$2 \cdot 10^{-7}$
$\bar{\nu}_e$ flux 0.0-2.5 GeV	$< 1 \cdot 10^{-6}$	$2 \cdot 10^{-7}$	$4 \cdot 10^{-5}$	$2 \cdot 10^{-7}$
$\bar{\nu}_e$ flux 2.5-30.0 GeV	$< 1 \cdot 10^{-6}$	$2 \cdot 10^{-7}$	$4 \cdot 10^{-5}$	$2 \cdot 10^{-7}$

Table 7: Maximum deviation from input values of oscillation parameters for a 2+0 fit and a single parameter ± 1 sigma deviation from nominal. This uses an old version of the BANFF matrix (v5) with a different parameter set. The ν_e and $\bar{\nu}_e$ flux parameters have negligible effect, and they were removed for BANFF v8. Similarly, the first four and last four $\bar{\nu}_\mu$ flux parameters have negligible effect, and these were combined for BANFF v8. Made for oscillations with $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \text{e-}05 \text{ eV}^2/c^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/c^4$ and for an exposure of 3.010×10^{20} POT.

3.1.3. Uncorrelated cross-section systematics

In addition to the BANFF cross-section systematics, another 11 cross-section systematics are taken into account; these additional systematics are considered to be uncorrelated between themselves and to have no cancellation between the near and far detectors [12] [13].

⁵ $f_{16;t,r}^{banff}$ and $f_{17;t,r}^{banff}$ are not the *value* of M_A , but instead a multiplicative factor describing how M_A moves away from nominal; $M_A \rightarrow x_{MAM} M_A$.

⁶An alternative way to treat the quasielastic axial mass was suggested [19]; use $1/(M_A^{QE})^2$ instead of M_A^{QE} . This is because $1/(M_A^{QE})^2$ has a more linear response than M_A^{QE} . Distributions of the predicted number of events in SuperK are shown in [23] for 20000 toy experiments with all BANFF matrix parameters randomly thrown for each of these two definitions of M_A^{QE} . Both are Gaussian, suggesting that there is no effect of the M_A^{QE} response on the far detector phase space. The shift is thought to be due to the different parameter ranges used: $M_A^{QE} = 1.21 \pm 0.45$ while $1/(M_A^{QE})^2 = 0.683 \pm 0.320$, which translates to $M_A^{QE} = 1.21_{-0.21}^{+0.45}$. Therefore it was decided to use M_A^{QE} , to be consistent with the 2012 ν_e analyses.

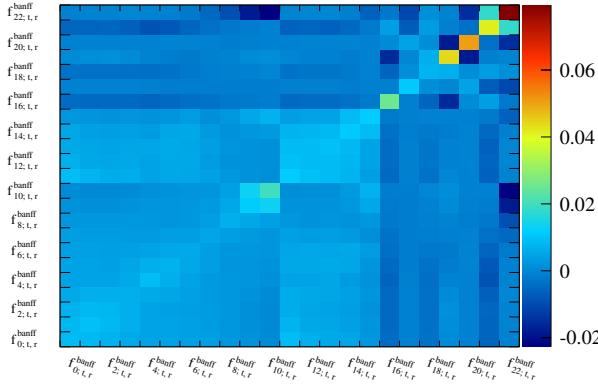


Figure 16: The input BANFF postfit covariance matrix. The meaning of each parameter is given in the text.

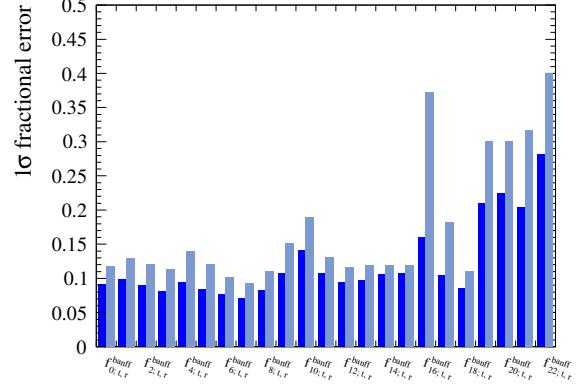


Figure 17: Postfit (dark blue) and prefit (light blue) 1σ fractional errors for BANFF parameters (computed from the square root of the diagonal elements of the corresponding input covariance matrix). The meaning of each parameter is given in the text.

467 Three of these additional systematics relate to the initial-state nuclear environment modeling for CCQE. Neutrino
 468 Monte Carlo generators typically use Relativistic Fermi Gas (RFG) models, with or without extensions to take nucleon-
 469 nucleon correlation into account, and with some, often simplistic, prescription for the treatment of off-shell kinematics.
 470 The RFG model implementation depends on two parameters, the Fermi momentum level (225 MeV for ^{16}O) and
 471 the nucleon binding energy (27 MeV for ^{16}O), which are extacted from quasi-elastic electron scattering data. The
 472 systematic parameter $f_{pF;t,r}$ takes into account the effect of a 30 MeV 1σ uncertainty in the Fermi momentum level
 473 for ^{16}O , while parameter $f_{bindE;t,r}$ takes into account the effect of a 9 MeV 1σ uncertainty in the nucleon binding
 474 energy for for ^{16}O . The implementation details of the nuclear model can have a significant effect and, therefore, the
 475 effect of switching between two such models was also included as a systematic uncertainty. This analysis considers
 476 the effect of switching between the RFG model and a better-motivated Spectral Function (SF) model. The latter does
 477 not assume a fixed binding energy and includes the correlations between nucleon momentum and binding energy. The
 478 systematic parameter $f_{SF;t,r}$ includes the effect of switching between the two models.

479 Simple, energy-independent, generator-level uncertainties are considered for the CC coherent, NC, ν_e CC and $\bar{\nu}$
 480 CC cross sections, as the effect of these processes in the single μ -like ring sample is small. This analysis uses a 100%
 481 uncertainty for the CC coherent cross-section, a 30% uncertainty for both the NC $1\pi^\pm$ and NC “other” (all but single
 482 π^\pm) cross section, a 3% uncertainty on the ν_e / ν_μ CC cross-section ratio and a 40% uncertainty on the $\bar{\nu} / \nu$ CC cross-
 483 section ratio. The effect of the variation of the above cross sections is included in the analysis through the systematic
 484 parameters $f_{CCcoh;t}$, $f_{NC1\pi^\pm;t}$, $f_{NCoth;t}$, $f_{CC\nu_e;t}$ and $f_{CC\bar{\nu};t}$ respectively.

485 The treatment of Δ resonances in the nuclear environment has been controversial in the neutrino Monte Carlo
 486 generator community. Certain models include a 20%-level of π -less Δ decays in order to include the effect of $\Delta + N \rightarrow$
 487 $N + N$ scattering, in which the Δ interacts before it can decay. In contrast, other models include no π -less Δ decays
 488 on the basis that this would amount to double counting since, whatever the size of the effect, it is already included in
 489 hadron-nucleus scattering data to which the intranuclear cascade Monte Carlos are tuned. This analysis uses NEUT, in
 490 which 20% of Δ s have a π -less decay by default, and takes the uncertainty in this branching fraction to be 100%. The
 491 systematic parameter $f_{\pi-less\Delta;t,r}$ includes the effect of varying the fraction of π -less Δ decays to the corresponding
 492 MC templates.

493 The $f_{CCothShape;t,r}$ systematic parameterizes the uncertainty in CC multi-pion, CC deep inelastic scattering and
 494 CC η , K and photon production. From MINOS data, this is known to be $\approx 10\%$ at 4 GeV. Using this as a reference
 495 point, the uncertainty is estimated as $0.4/E_\nu$, where E_ν is in GeV. It might appear that this error could diverge at low
 496 energy, but this does not happen since the threshold is ≈ 0.6 GeV and there are very few interactions below 1 GeV.

497 The $f_{Wshape;t,r}$ parameter modifies the shape of the initial pion momentum distribution (before final-state interac-
 498 tions) by changing the distribution of the pion/nucleon invariant mass while keeping the total cross section constant.
 499 As the W shape parameter decreases, the pion momentum shifts to lower values, and this increases the probability of
 500 pion absorption in a final-state interaction. If such an absorption occurs, the event is migrated from CC1 π (its true
 501 initial state) and appears to be CCQE.

502 The effect of the $f_{CCcoh;t}$, $f_{NC1\pi^\pm;t}$, $f_{NCoth;t}$, $f_{CC\nu_e;t}$ and $f_{CC\bar{\nu};t}$ systematic parameters is a simple normalisation
 503 change for the corresponding MC templates and thus easily implemented. Systematic parameters $f_{pF;t,r}$, $f_{SF;t,r}$,
 504 $f_{bindE;t,r}$, $f_{\pi-less\Delta;t,r}$, $f_{CCothShape;t,r}$ and $f_{Wshape;t,r}$ have a complicated, often non-linear, dependance on true
 505 and reconstructed energy. These are treated in a similar way to the BANFF parameters $f_{17;t,r}^{banff}$ and $f_{18;t,r}^{banff}$ (see Sec.
 506 3.1.2). Event reweighting methods were used to obtain the fractional changes of the number of events, in bins of true
 507 and reconstructed neutrino energy, for a range of values (-3.0 σ , -2.5 σ , -2.0 σ , ..., +3.0 σ) of the systematic parameters.
 508 Again cross-section splines with polynomials of order 3 were used to interpolate between these event weights to obtain
 509 the fractional change for any value of these systematic parameters in the (-3.0 σ , +3.0 σ) range.
 510

Some of these systematics are special cases:

- 511 • $f_{SF;t,r}$ is discrete; it can be either off (RFG) or on (SF). Splines are generated with off as nominal, and on as
 512 +1.0 sigma. Linear interpolation is done only between the weights for 0 and 1.
- 513 • For $f_{Wshape;t,r}$ only ± 1.0 sigma errors are evaluated using event reweighting. All other errors are extrapolated
 514 or interpolated from these ± 1.0 weights.
- 515 • For $f_{pi-lessDelta;t,r}$ only ± 1.0 sigma errors are evaluated using event reweighting. Weights for tweaks more
 516 positive than $+1\sigma$ are extrapolated from the $+1\sigma$ weight. Weights more negative than -1σ are taken to be the
 517 same as the -1σ weight; this is done since 20% of deltas have a pileless decay by default in NEUT, and the error is
 518 20%. For this reason, it is unphysical to tweak $f_{pi-lessDelta;t,r}$ to be more negative than -1σ .

519 The cross-section splines have 41 bins in reconstructed energy:
 520

- 521 • 1 bin from 0-0.3 GeV
- 522 • 14 50-MeV bins from 0.3-1.0 GeV
- 523 • 20 100MeV bins from 1.0-3.0 GeV
- 524 • 2 500-MeV bins from 3.0-4.0 GeV
- 525 • 1 bin from 4.0-5.0 GeV
- 526 • 1 bin from 5.0-7.0 GeV
- 527 • 1 bin from 7.0-10.0 GeV
- 528 • 1 bin from 10.0-30.0 GeV

529 For the ν_μ , $\bar{\nu}_\mu$ and oscillated ν_e samples, they have 11 bins in true energy:
 530

- 531 • 1 bin from 0-0.4 GeV
- 532 • 3 100-MeV bins from 0.4-0.7 GeV
- 533 • 1 bin from 0.7-1.0 GeV
- 534 • 1 bin from 1.0-1.5 GeV
- 535 • 2 1-GeV bins from 1.5-3.5 GeV
- 536 • 1 bin from 3.5-5.0 GeV
- 537 • 1 bin from 5.0-7.0 GeV
- 538 • 1 bin from 7.0-30.0 GeV

539 For the ν_e sample, they have 7 bins in true energy:
 540

- 541 • 1 bin from 0-0.05 GeV
- 542 • 1 bin from 0.5-0.7 GeV

- 540 ● 1 bin from 0.7-0.8 GeV
 541 ● 1 bin from 0.8-1.5 GeV
 542 ● 1 bin from 1.5-2.5 GeV
 543 ● 1 bin from 2.5-4.0 GeV
 544 ● 1 bin from 4.0-30.0 GeV

545 Finally, for the $\bar{\nu}_e$ sample, they have 2 bins in true energy:

- 546 ● 1 bin from 0-2.5 GeV
 547 ● 1 bin from 2.5-30.0 GeV

548 An example of a cross-section spline is shown in Fig. 18.

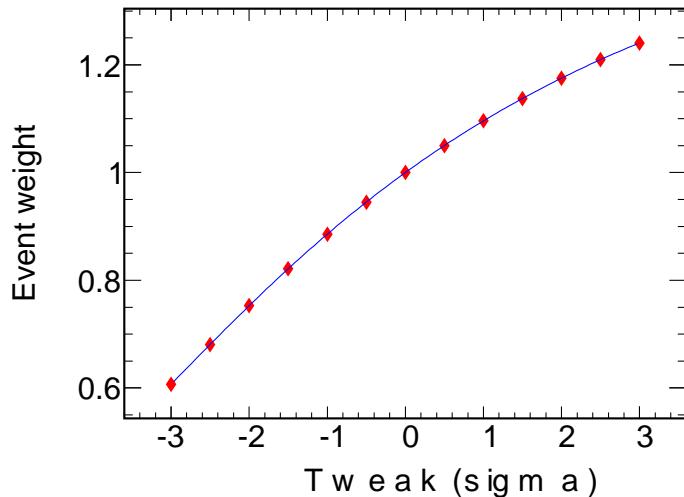


Figure 18: Example of a cross-section spline; this shows the event weights obtained by tweaking M_A^{QE} for ν_μ -CCQE events in the bin with reconstructed energy 0.75-0.8 GeV and true energy 0.6-0.7 GeV.

549 The 11 uncorrelated cross-section systematics considered in this analysis are summarised in Tab. 4. These cross-
 550 section systematics are applied to the MC templates as shown in Tab. 5.

551 3.1.4. FSI+SI systematics

552 Intranuclear hadron transport, or final-state interactions (FSI), have significant effects in the T2K energy range and
 553 result in event topologies, for scattering on nuclear targets, which are drastically different compared with those created
 554 in neutrino scattering on free nucleons. Elastic and inelastic hadron rescattering, secondary pion production, single and
 555 double charge exchange and absorption followed by multi-nucleon knockout are typically modelled in neutrino event
 556 generators using intranuclear cascades.

557 Uncertainties due to FSI were estimated by simultaneously varying the NEUT parameters that scale the interaction
 558 probabilities for quasi-elastic scattering, absorption, charge exchange and pion production using the method described
 559 in Sec. 2 in [12]. The NIWG group produced 16 parameter sets that span the 1σ surface in the parameter space; this
 560 was done by varying the NEUT parameters when running the pion scattering simulations, and comparing the results
 561 with external pion-carbon scattering data. These 16 parameter sets are shown in Tab. 2 in [12].

562 Uncertainties due to secondary pion interactions (SI) were also evaluated. The NIWG group adapted the NEUT
 563 nuclear cascade model to simulate SI in the SuperK detector simulation (SKDETSIM) and to allow variations in the
 564 interaction probabilities. Details of this are given in [15]. The original 11c SKMC files do not contain all the truth
 565 information required for reweighting SI, and a second production was made. The two productions contain independent

Parameter	Definition
$f_{0;r}^{FSI}$	$\nu_\mu \& \bar{\nu}_\mu$ CCQE, $E_{reco} < 0.4$ GeV
$f_{1;r}^{FSI}$	$\nu_\mu \& \bar{\nu}_\mu$ CCQE, $0.4 \text{ GeV} \leq E_{reco} \leq 1.1 \text{ GeV}$
$f_{2;r}^{FSI}$	$\nu_\mu \& \bar{\nu}_\mu$ CCQE, $E_{reco} > 1.1 \text{ GeV}$
$f_{3;r}^{FSI}$	$\nu_\mu \& \bar{\nu}_\mu$ CCnonQE
$f_{4;r}^{FSI}$	$\nu_e, \bar{\nu}_e$ CC
$f_{5;r}^{FSI}$	All NC

Table 8: FSI+SI systematic parameters.

566 steps (SKDETSIM was rerun on the NEUT files), and there are small differences in the numbers of events between the
 567 productions. The second production was used only to produce the FSI+SI covariance matrix, which is shown in Fig.
 568 19. The 1σ fractional errors in the 6 FSI+SI parameters are shown in Fig. 20; these are computed from the square roots
 569 of the diagonal elements of the input covariance matrix.

570 Since the same model is used for FSI and SI, it is possible to evaluate the uncertainties in both FSI and SI simul-
 571 taneously. This was done by reweighting a single μ -like ring selected SK MC with the 16 FSI parameter sets using
 572 T2KReweight. The reweighting method for FSI is described in Sec. 8 in [11]. Variations in the SI interaction prob-
 573 abilities were included for each FSI parameter set. Subsequently a covariance matrix was calculated using equation
 574 1 in [12]; the quantity p in that equation is the average event weight for a FSI parameter set, and the sum is over the
 575 parameter sets.

576 The covariance matrix was made with a 6-bin scheme, as shown in Tab. 8. For $\nu_\mu, \bar{\nu}_\mu$ CCQE, the FSI+SI binning
 577 scheme is identical to that used by SuperK for calculating the $\nu_\mu, \bar{\nu}_\mu$ CCQE ring-counting efficiency error matrix.

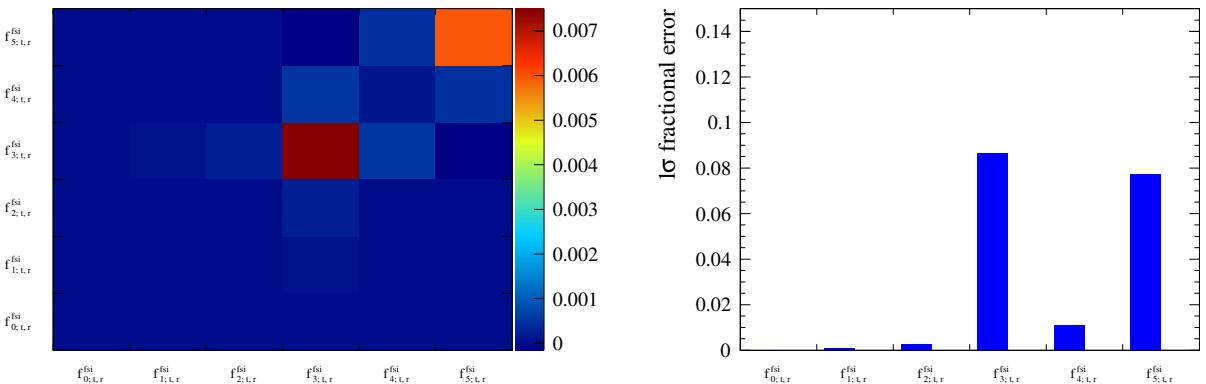


Figure 19: The input FSI+SI covariance matrix. The meaning of each parameter is given in Tab. 8.

Figure 20: 1σ fractional error for FSI+SI parameters (computed from the square roots of the diagonal elements of the input covariance matrix). The meaning of each parameter is given in Tab. 8.

578 3.2. Evaluation of systematic effects on the single μ -like ring reconstructed energy spectrum

579 In this section, we present the effects of the systematics described in Secs. 3.1.2, 3.1.3 and 3.1.4 on the expected
 580 number of single μ -like ring events and the reconstructed energy spectrum in SuperK. These effects are shown both for
 581 no oscillations and for oscillations with $\sin^2 2\theta_{23} = 1.0$ and $|\Delta m_{32}^2| = 2.4 \times 10^{-3} \text{ eV}^2/c^4$. For the oscillation cases, the
 582 2012 PDG values are used for $\sin^2 2\theta_{13}$, $\sin^2 2\theta_{12}$ and Δm_{21}^2 , and $\delta_{CP}=0$. The normal mass hierarchy is assumed. All
 583 results are generated for an integrated exposure of 3.010×10^{20} POT and the BANFF-tuned MC templates are used.

584 The effects of systematic uncertainties on the expected number of events, both for no oscillations and for oscillations
 585 with the typical parameter values given above, is summarised in Tab. 9. In this table, systematic parameters are grouped

Source of uncertainty	$\delta N_{SK}/N_{SK}$ (no oscillation)	$\delta N_{SK}/N_{SK}$ (oscillations with typical parameter values)
SuperK detector	5.57%	10.08%
BANFF (prefit)	24.14%	21.84%
BANFF (postfit)	4.38%	4.15%
Uncorrelated XSec	3.64%	6.26%
FSI+SI	1.87%	3.48%
Total (BANFF prefit)	25.11%	25.10%
Total (BANFF postfit)	8.18%	13.04%

Table 9: Effect of 1σ systematic parameter variation on the number of 1-ring μ -like events, computed for no oscillations and for oscillations with $\sin^2 2\theta_{23}=1.0$ and $|\Delta m_{32}^2|=2.4\times 10^{-3} \text{ eV}^2/c^4$. For the oscillation scenario, the 2012 PDG values are used for $\sin^2 2\theta_{13}$, $\sin^2 2\theta_{12}$ and Δm_{21}^2 , and $\delta_{CP}=0$. The normal mass hierarchy is assumed. The numbers shown were calculated for an exposure of 3.010×10^{20} POT and BANFF-tuned MC templates were used.

586 into a few categories and all parameter correlations are taken into account. Entries for both the BANFF prefit and postfit
 587 errors are provided. The effects of each parameter individually are presented in Tab. 10 in which the correlations
 588 between parameters are necessarily ignored.

589 The effects of the combined systematic uncertainties on the reconstructed energy spectrum of single μ -like ring
 590 events is shown in Fig. 21, for the typical oscillation scenario used. This plot shows the total error envelope for the 1
 591 μ -like ring event reconstructed energy spectrum; this is calculated as the $\pm 1\sigma$ spread of bin contents from 100k toy MC
 592 experiments generated with randomized systematic parameters. In Fig. 21, all systematic parameters were considered
 593 and their correlations were taken into account.

594 Error envelopes from the effects of certain groups of systematic parameters are shown in Figs. 22 (SuperK detector
 595 systematics only), 23 (BANFF systematics only), 24 (uncorrelated cross-section systematics only), and 25 (FSI+SI
 596 systematics only).

597 Detailed studies showing the effects of individual systematics on the expected number of single μ -like ring events
 598 are shown in Appendix E, while their effects on the reconstructed energy spectrum of the single μ -like ring sample are
 599 shown in Appendix F.

Source of uncertainty	$\delta N_{SK}/N_{SK}$ (no oscillation)		$\delta N_{SK}/N_{SK}$ (oscillations with typical params)	
	BANFF prefit	BANFF postfit	BANFF prefit	BANFF postfit
$f_{E;r}^{SK}$	0.00	0.00	0.00	0.00
$f_{CCQEoth;r}^{SK}$	1.41	1.41	0.97	0.97
$f_{CCQERC0;r}^{SK}$	0.06	0.06	0.11	0.11
$f_{CCQERC1;r}^{SK}$	2.22	2.22	0.83	0.83
$f_{CCQERC2;r}^{SK}$	0.96	0.96	2.30	2.30
$f_{CCnQE;r}^{SK}$	0.41	0.41	7.75	7.75
$f_{NC;r}^{SK}$	0.18	0.18	5.84	5.84
$f_{\nu_e;r}^{SK}$	0.02	0.02	0.26	0.26
$f_{0;t,r}^{banff}$	0.35	0.28	0.81	0.68
$f_{1;t,r}^{banff}$	1.01	0.82	0.65	0.54
$f_{2;t,r}^{banff}$	1.91	1.51	0.12	0.10
$f_{3;t,r}^{banff}$	2.22	1.69	0.29	0.23
$f_{4;t,r}^{banff}$	3.69	2.71	2.38	1.79
$f_{5;t,r}^{banff}$	1.05	0.80	1.89	1.49
$f_{6;t,r}^{banff}$	0.66	0.46	1.77	1.29
$f_{7;t,r}^{banff}$	0.32	0.22	0.99	0.70
$f_{8;t,r}^{banff}$	0.40	0.33	1.32	1.08
$f_{9;t,r}^{banff}$	0.20	0.14	0.65	0.48
$f_{10;t,r}^{banff}$	0.05	0.04	0.17	0.13
$f_{11;t,r}^{banff}$	0.06	0.05	0.03	0.03
$f_{12;t,r}^{banff}$	0.06	0.05	0.05	0.04
$f_{13;t,r}^{banff}$	0.09	0.08	0.16	0.14
$f_{14;t,r}^{banff}$	0.10	0.08	0.27	0.23
$f_{15;t,r}^{banff}$	0.08	0.07	0.24	0.22
$f_{16;t,r}^{banff}$	21.40	8.35	15.99	6.66
$f_{17;t,r}^{banff}$	2.80	1.86	6.65	4.31
$f_{18;t,r}^{banff}$	7.86	6.46	4.23	3.52
$f_{19;t,r}^{banff}$	1.41	1.06	3.94	2.96
$f_{20;t,r}^{banff}$	0.37	0.31	1.19	1.03
$f_{21;t,r}^{banff}$	3.67	2.14	4.90	2.84
$f_{22;t,r}^{banff}$	1.69	1.02	5.38	3.67
$f_{pF;t,r}$	0.06	0.06	0.11	0.11
$f_{bindE;t,r}$	0.39	0.39	0.18	0.18
$f_{SF;t,r}$	2.49	2.49	0.67	0.67
$f_{\pi-less\Delta;t,r}$	3.16	3.16	5.47	5.47
$f_{CCothShape;t,r}$	0.28	0.28	0.82	0.82
$f_{Wshape;t,r}$	0.11	0.11	0.39	0.39
$f_{CCcoh;t}$	0.56	0.56	0.88	0.88
$f_{NC1\pi^\pm;t}$	0.26	0.26	0.92	0.92
$f_{NCoth;t}$	0.23	0.23	0.82	0.82
$f_{CC\nu_e;t}$	0.00	0.00	0.00	0.00
$f_{CC\bar{\nu};t}$	1.19	1.19	2.33	2.33
$f_{0;t,r}^{FSI}$	0.00	0.00	0.00	0.00
$f_{1;t,r}^{FSI}$	0.05	0.05	0.02	0.02
$f_{2;t,r}^{FSI}$	0.03	0.03	0.07	0.07
$f_{3;t,r}^{FSI}$	1.83	1.83	3.37	3.37
$f_{4;t,r}^{FSI}$	0.00	0.00	0.00	0.00
$f_{5;t,r}^{FSI}$	0.13	0.13	0.45	0.45

Table 10: Effects of 1σ systematic parameter variations on the number of 1-ring μ -like events, computed for no oscillations and for oscillations with $\sin^2 2\theta_{23}=1.0$ and $|\Delta m_{32}^2|=2.4 \times 10^{-3} \text{ eV}^2/c^4$. Correlations are ignored for this table. For the oscillation scenario, the 2012 PDG values are used for $\sin^2 2\theta_{13}$, $\sin^2 2\theta_{12}$ and Δm_{21}^2 , and $\delta_{CP}=0$. The normal mass hierarchy is assumed. The numbers shown were calculated for an exposure of 3.010×10^{20} POT and BANFF-tuned MC templates were used.

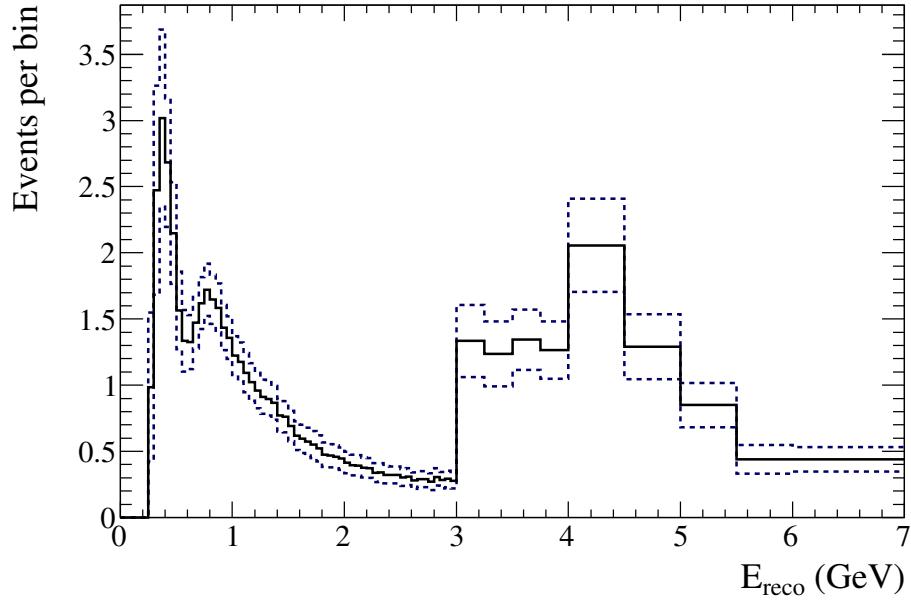


Figure 21: Total error envelope of the 1 μ -like ring event reconstructed energy spectrum, for oscillations with $\sin^2 2\theta_{23}=1.0$ and $|\Delta m_{32}^2|=2.4 \times 10^{-3}$ eV^2/c^4 . The 2012 PDG values are used for $\sin^2 2\theta_{13}$, $\sin^2 2\theta_{12}$ and Δm_{21}^2 , and $\delta_{CP}=0$. The normal mass hierarchy is assumed. The numbers shown were calculated for an exposure of 3.010×10^{20} POT. BANFF-tuned MC templates were used. The error envelope was calculated as the $\pm 1\sigma$ spread of bin contents using an ensemble of 100k toy MC experiments generated with randomized systematic parameters. All systematic parameters were considered and their correlations were taken into account.

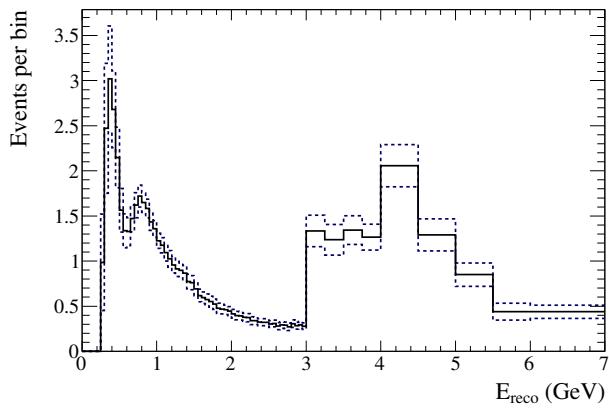


Figure 22: As in Fig. 21, but considering only SuperK detector systematics.

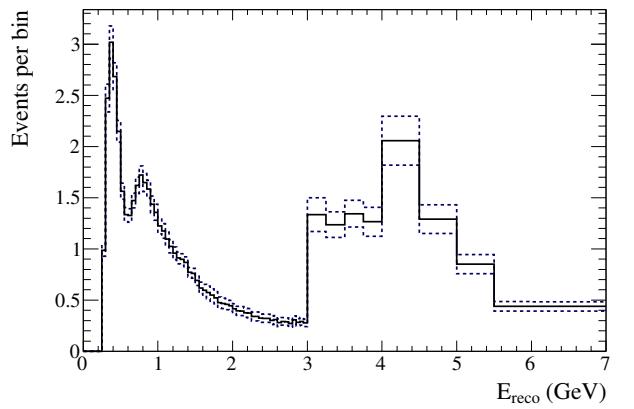


Figure 23: As in Fig. 21, but considering only BANFF systematics.

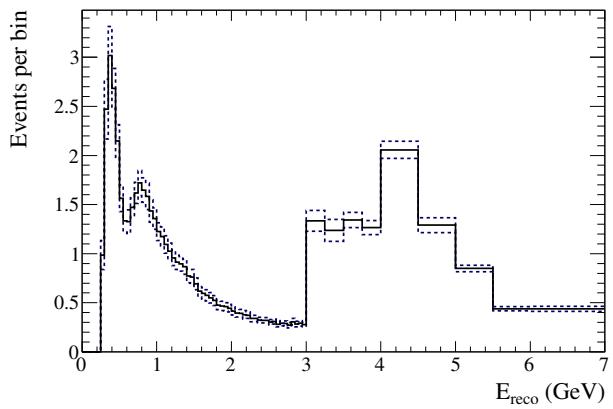


Figure 24: As in Fig. 21, but considering only uncorrelated cross-section systematics.

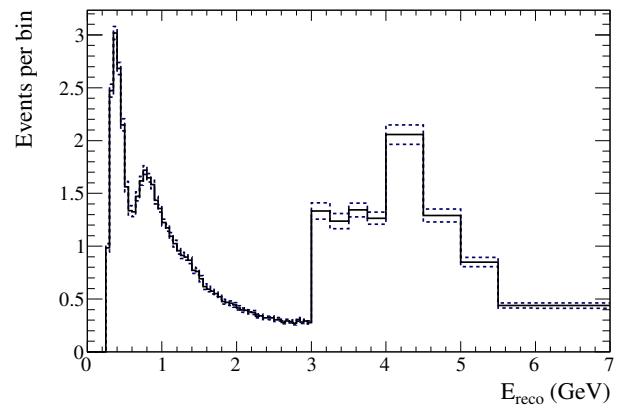


Figure 25: As in Fig. 21, but considering only FSI+SI cross-section systematics.

Parameter	Best-fit	1σ error
Δm_{21}^2	7.5×10^{-5} eV $^2/c^4$	$\sim 3\%$
$\sin^2(2\theta_{12})$	0.857	$\sim 3\%$
$\sin^2(2\theta_{13})$	0.098	$\sim 13\%$

Table 11: 2012 PDG best-fit values and 1σ range for the measured non-23-sector oscillation parameters [21].

600 4. Neutrino oscillation fitting

601 4.1. Fitting methodology

602 4.1.1. Choice of 23-sector oscillation parameters

603 Several choices exist for the 23-sector oscillation parameters that could be fitted, and they have been presented in
 604 the context of the VaLOR joint 3-flavour oscillation analysis [22]. The mixing parameter typically fitted is $\sin^2 2\theta_{23}$,
 605 but $\sin^2 \theta_{23}$ is a more natural choice in the context of a 3-flavour analysis, especially one with any sensitivity to resolve
 606 the octant degeneracy. The mass-squared difference typically fitted is $|\Delta m_{32}^2|$; this is the largest squared-mass splitting
 607 for the inverted mass hierarchy but the second largest for the normal mass hierarchy. It is therefore not correct to
 608 compare results obtained under the different mass hierarchy hypotheses. Other choices include fitting for a mass-
 609 squared difference whose absolute value is the same for both mass hierarchies, such as $\Delta m^2 = \left(m_3^2 - \frac{m_1^2 + m_2^2}{2}\right)$
 610 [37], or fitting for $|\Delta m_{32}^2|$ for the inverted hierarchy and $|\Delta m_{31}^2|$ for the normal hierarchy [38]. All these choices are
 611 implemented in the VaLOR oscillation analysis framework, and our analysis can switch between them.

612 For the Run 1+2+3 datasets, it was agreed that all official T2K ν_μ -disappearance analyses will continue to fit the
 613 usual parameters $\sin^2 2\theta_{23}$ and $|\Delta m_{32}^2|$.

614 The PRL referees requested that we present the result in terms of $\sin^2 \theta_{23}$ and $|\Delta m_{32}^2|$, so the result for this
 615 variable has been added to the note. The fact that the center of symmetry (point of maximal disappearance) is not
 616 at $\sin^2 \theta_{23} = 0.5$ makes this a sensible choice.

617 4.1.2. Treatment of non-23-sector oscillation parameters

618 In a 3-flavour ν_μ -disappearance fit, it is also necessary to make a choice for the non-23 oscillation parameters.
 619 Possible options for these parameters include

- 620 1. All 6 parameters, i.e. $\sin^2(2\theta_{12})$, $\sin^2(2\theta_{13})$, $\sin^2(2\theta_{23})$, Δm_{21}^2 , $|\Delta m_{32}^2|$ and δ_{CP} can float freely.
- 621 2. All 6 parameters can float freely, but deviations in values of $\sin^2(2\theta_{12})$, $\sin^2(2\theta_{13})$ and Δm_{21}^2 from values
 measured by other experiments are penalised.
- 623 3. $\sin^2(2\theta_{23})$ and $|\Delta m_{32}^2|$ can float freely, but $\sin^2(2\theta_{12})$, $\sin^2(2\theta_{13})$, Δm_{21}^2 and δ_{CP} are fixed.

624 In the present analysis, option 3 is used. When finding the best-fit values of $\sin^2(2\theta_{23})$ and $|\Delta m_{32}^2|$, the values of
 625 Δm_{21}^2 , $\sin^2(2\theta_{12})$ and $\sin^2(2\theta_{13})$ are fixed to the 2012 PDG best-fit values [21] shown in Tab. 11, and δ_{CP} is fixed to
 626 0.

627 4.1.3. Treatment of systematic parameters

628 In this analysis, 48 nuisance (systematic) parameters are taken into account in the prediction of the single μ -like
 629 ring event reconstructed energy spectrum (see Sec. 3). **The VaLOR group produces oscillation results including all
 nuisance parameters in the fit.**

631 At the time of the muon-neutrino disappearance analysis of the Run1+2 dataset, the authors of this analysis (at
 632 that time referred to as the Rutherford/Oxford analysis [2]) took the view that, due to low statistics, and in the interest
 633 of simplicity and robustness, fitting for all the numerous systematic parameters considered in the analysis was not
 634 warranted. It was shown that fitting for no systematics obtained results which were very similar to the ones obtained by
 635 fitting for all systematics. It was argued that better services would be provided to the community by focussing our paper
 636 on the power of the off-axis technique rather than on statistical gymnastics. Most T2K collaborators shared this view,
 637 and the Rutherford/Oxford result was chosen as the primary result shown in the first muon-neutrino disappearance
 638 paper [7]. Similar views may be expressed in the context of the present analysis. Due to a two-fold increase of
 639 the integrated exposure since the time of the Run1+2 analysis, fitting some of the dominant systematic parameters is
 640 now justified. However, again, we express concerns that fitting for all 48 systematic parameters considered in this
 641 analysis is not warranted, especially in view of the small effect many of them have compared with the effect of some

642 of the approximations made in this analysis. We have therefore sought to reduce the dimensionality of our fit while
 643 accounting for the full systematic effects on our measurements of $\sin^2 2\theta_{23}$ and $|\Delta m_{32}^2|$. **In addition to the result**
 644 **obtained by fitting all systematics, the VaLOR group produces alternative oscillation results by allowing only the**
 645 **most important systematics to float in the fit.** A detailed study to select the systematic parameters to include in the
 646 fit for the alternative result is presented in Sec. 4.4. We give the VaLOR group viewpoint on which is the preferred
 647 result to show publicly in Sec. 5.7, after presenting all the results in detail.

648 4.1.4. Allowed range of fit parameters

649 The search for the minimum value of $-2 \ln \lambda(\sin^2 2\theta_{23}, |\Delta m_{32}^2|; \mathbf{a})$ (see Eq. 5) is performed in the range $0 \leq$
 650 $\sin^2 2\theta_{23} \leq 1$ and $1 \times 10^{-3} eV^2/c^4 \leq |\Delta m_{32}^2| \leq 6 \times 10^{-3} eV^2/c^4$. Values of $\sin^2 2\theta_{23} > 1$ are not permitted;
 651 although it is numerically allowed and, occasionally, it yields better fits to data, it has no physical interpretation within
 652 the context in which we attempt to interpret the data and causes p.d.f.s to have pathological behaviour.

653 Systematic parameters included in the oscillation fit are constrained in the range $[-5\sigma_s, +5\sigma_s]$ where σ_s is the one
 654 standard deviation error assigned to each systematic parameter⁷. Values of systematic parameters that give a negative
 655 predicted number of events in any reconstructed energy bin are not allowed. If this scenario arises, the number of
 656 events is changed to $+1E-8$ in that bin. This is done for the sum of all the interaction modes rather than for each mode
 657 separately.

658 4.1.5. Minimization method

659 The VaLOR disappearance analysis uses a binned likelihood-ratio method. Measurements of the oscillation pa-
 660 rameters $\sin^2 2\theta_{23}$ and $|\Delta m_{32}^2|$ are obtained by comparing the observed and predicted SuperK reconstructed energy
 661 spectra for 1-ring μ -like events. Let N be the number of reconstructed energy bins and \mathbf{a} be a $1 \times N_s$ - dimensional
 662 array of systematic (nuisance) parameters that affect the SuperK reconstructed energy spectrum prediction (e.g param-
 663 eters that control the beam, neutrino interaction simulations and the detector response). Best-fit values are obtained by
 664 minimizing:

$$-2 \ln \lambda(\sin^2 2\theta_{23}, |\Delta m_{32}^2|; \mathbf{a}) = 2 \cdot \sum_{i=0}^{N-1} \left(n_i^{obs} \cdot \ln(n_i^{obs}/n_i^{exp}) + (n_i^{exp} - n_i^{obs}) \right) + (\mathbf{a} - \mathbf{a}_0)^T \cdot \mathbf{C}^{-1} \cdot (\mathbf{a} - \mathbf{a}_0) \quad (5)$$

665 where \mathbf{a}_0 is an $1 \times N_s$ - dimensional array with the default values of the systematics parameters, \mathbf{a}^T is the transpose
 666 of \mathbf{a} , \mathbf{C} is the systematic parameter covariance matrix of dimension $N_s \times N_s$, n_i^{obs} is the observed number of events
 667 in the i^{th} bin, and $n_i^{exp} = n_i^{exp}(\sin^2 2\theta_{23}, |\Delta m_{32}^2|; \mathbf{a})$ is the corresponding expected number of events.

668 The likelihood-ratio method used in this analysis, is equivalent to the extended maximum likelihood method
 669 used in the alternative T2K oscillation analysis (see [1, 24] for more details). The advantage of the likelihood ra-
 670 tio method, compared with the extended maximum-likelihood method, is that in the large-sample limit, the quantity
 671 $-2 \ln \lambda(\sin^2 2\theta_{23}, |\Delta m_{32}^2|; \mathbf{a})$ in Eq.5 has a χ^2 distribution and it can therefore be used as a goodness-of-fit test. In this
 672 note $-2 \ln \lambda(\sin^2 2\theta_{23}, |\Delta m_{32}^2|; \mathbf{a})$ and $\chi^2(\sin^2 2\theta_{23}, |\Delta m_{32}^2|; \mathbf{a})$ are used interchangeably.

673 The minimization is performed with Minuit [25], using the Migrad method. If Migrad does not converge, the
 674 starting values of the oscillation parameters are re-initialised: the new initial values are randomly drawn from uniform
 675 distributions in the ranges $0.80 \leq \sin^2 2\theta_{23} \leq 0.98$, $2 \cdot 10^{-3} \leq |\Delta m_{32}^2| \leq 3 \cdot 10^{-3}$ and the fit is retried. This is repeated
 676 10 times. If the fits still fail to converge, the Simplex algorithm is used. The Hesse algorithm is called after a successful
 677 fit to improve Minuit's estimates of the errors on the fitted parameters.

678 4.1.6. Brief note on out fit labeling scheme

679 In the following sections, the different fits are labeled as ' $I_{osc}+I_{syst}$ ', where I_{osc} and I_{syst} represent, respectively,
 680 the number of oscillation and systematic parameters which are allowed to float in the fit. If the symbol N is shown in
 681 place of I_{syst} , all of the systematic parameters are allowed to float. If an actual number is shown in place of I_{syst} , this
 682 is the number of systematics that is allowed to float.

⁷Such an error is defined for all but one of the systematic parameters considered in this analysis. The exception is the systematic parameter f_{SF} which parameterizes the uncertainty on nuclear modelling, switching between the Relativistic Fermi Gas (RFG) and Spectral Function (SF) models. The allowed range of the parameter f_{SF} in the oscillation fit is [0,1].

683 Accoring to the above scheme, ‘2+N’ denotes a fit of $\sin^2 2\theta_{23}$, $|\Delta m_{32}^2|$ and all nuisance parameters, ‘2+8’ denotes
 684 a fit of $\sin^2 2\theta_{23}$, $|\Delta m_{32}^2|$ and the 8 most important systematic parameters, ‘0+N’ denotes a fit of all nuisance parameters
 685 with all oscillation parameters fixed, etc.

686 4.2. Goodness-of-fit tests

687 In our ν_μ -disappearance analysis of the Run1+2 datasets, p-values were computed using both a) the rate of single
 688 μ -like ring events and b) the rate and reconstructed energy distribution of single μ -like ring events using the likelihood-
 689 ratio method [28]. The choice is not unique.

690 D. Karlen has pointed out that, if the statistics are low, ”the use of the distribution is not helpful in forming
 691 the p-value. This is directly related to the well known problem that is difficult to define a general goodness-of-fit for
 692 sparsely populated distributions. Large bins (or in the extreme a single bin = rate-only) are necessary for small statistics
 693 samples” [29].

694 It was decided by the oscillation analysis group that, for all ν_μ -disappearance analyses, p-values will be calculated
 695 using the rate and the reconstructed energy distribution, and that the distribution will use a very coarse binning scheme
 696 to ensure that there are sufficient numbers of events in each bin: this scheme has 5 bins from 0-0.4, 0.4-0.7, 0.7-1.0,
 697 1.0-2.0 and 2.0-30.0 GeV.

698 4.3. Toy Monte Carlo study of fitter performance

699 The performance of the fitter was evaluated using an ensemble of 10k toy MC experiments, generated with input
 700 oscillation parameters $\sin^2 2\theta_{23} = 0.9$ and $|\Delta m_{32}^2| = 2.4 \times 10^{-3} \text{ eV}^2/\text{c}^4$ and an exposure of 3.010×10^{20} POT. A further
 701 10k toy MC experiments with the same input oscillation parameters and an exposure of 3.010×10^{22} POT (100 \times
 702 Run1+2+3 exposure) were also used. These simulated experiments included statistical fluctuations and fluctuations of
 703 the 8 dominant systematic parameters only (see Sec. 4.4). The toy MC experiments were fitted using MINUIT and
 704 HESSE errors, with a ‘2+8’ fit being used. Residual and pull distributions were studied for oscillation and systematic
 705 parameters. No issue was identified regarding the fitter performance, which was as expected. The results are presented
 706 in Appendix H⁸.

707 4.4. Systematic analysis

708 This section describes a study into the effect of systematic uncertainties in the joint estimation of the $\sin^2 2\theta_{23}$ and
 709 $|\Delta m_{32}^2|$ using the fitting procedure described in Sec. 4.1.5. Only a summary is given here, and the full study is shown
 710 in Appendix G.

711 To quantify the effect of each systematic, toy MC datasets are generated with no statistical fluctuations and with the
 712 systematic parameter in question varied by $\pm 1\sigma$. A ‘2+0’ fit is performed on each dataset. For correlated systematic
 713 parameters, σ is defined as the square root of the corresponding covariance matrix diagonal element. The effect of
 714 the systematic parameter on the oscillation parameters, for the given systematic parameter variation and the input true
 715 oscillation point, is taken to be the difference between the best-fit and true oscillation points.

716 Figs. 26-29 show the so-called “star plots”, which have arrows plotted for each systematic parameter from the true
 717 input point to the best-fit points for both the $+1\sigma$ and the -1σ fits. These figures show only the “dominant” systematic
 718 parameters, which are defined as those having an effect on $\sin^2 2\theta_{23}$ and $|\Delta m_{32}^2|$ greater than 25% of the expected
 719 statistical error at one or more true oscillation points in the area of interest in the parameter space. The statistical error
 720 was evaluated using 10k toy MC datasets with no systematic fluctuations at each input point, with each dataset being
 721 fitted with the ‘2+0’ method. The maximum deviation found between the true input and best-fit oscillation parameters
 722 for all true oscillation points tested is summarised in Tab. 12. The dominant systematic parameters are highlighted in
 723 red in that table.

724 The purpose of this study was to identify the dominant systematics in order to reduce the dimensionality of the fit.
 725 As shown in Tab. 12, only 8 (out of a total of 48) systematic parameters have an effect which is larger than 25% of the
 726 expected statistical error anywhere in the oscillation parameter space of interest. These systematic parameters are:

- 727 • $f_{E;r}^{SK}$: SuperK reconstructed energy scale systematic.

⁸Fitter performance tests have not been repeated for the fit in terms of $\sin^2 \theta_{23}$, however they are available for similar analyses using the same code, in reference [5] for the joint oscillation analysis, fitting for $\sin^2 \theta_{23}$ to Run 1-3 POT, and in reference [6] for the disappearance-only analysis, fitting for $\sin^2 \theta_{23}$ to Run 1-4a POT. Both of these analyses use a (slightly) different systematic parameter representation, and also fit for some non-23-sector oscillation parameters. No problems have been found with the fitter performance in these cases.

- 728 • $f_{CCnonQE;r}^{SK}$: ν_μ , $\bar{\nu}_\mu$ SuperK CCnonQE efficiency systematic. This is a combined systematic parameter which
 729 includes the uncertainty on all fiducial volume, ring-counting, reduction chain, OD cut, PID cut, momentum cut
 730 and decay electron cut efficiencies.
- 731 • $f_{NC;r}^{SK}$: SuperK NC efficiency systematic. This is a combined systematic parameter which includes all sources
 732 of uncertainty listed above for $f_{CCnonQE;r}^{SK}$.
- 733 • $f_{16;t,r}^{bannf}$: CCQE axial mass systematic.
- 734 • $f_{18;t,r}^{bannf}$: CCQE normalisation systematic in the true energy range 0 - 1.5 GeV.
- 735 • $f_{bindE;t,r}$: ^{16}O binding energy systematic.
- 736 • $f_{SF;t,r}$: ^{16}O nuclear environment modeling systematic. Switches from Fermi Gas (RFG) to Spectral Function
 737 (SF) model.
- 738 • $f_{\pi-less\Delta;t,r}$: Systematic parameter taking into account the uncertainty in the fraction of π -less Δ decays is
 739 resonance neutrino-production events.

740 When performing a '2+8' fit, it should be noted that correlations are respected; the 21 BANFF parameters which are
 741 not fitted move as a result of changing the 2 BANFF parameters which are fitted, and all BANFF parameters contribute
 742 to the fit penalty term. Also, it should be noted that all parameter correlations are taken into account when the toy MC
 743 experiments are generated, and this is true for all fit methods.

744 It was decided to perform a '2+8' oscillation fit in addition to the '2+N' fit. This was done with the underlying
 745 assumption that, if the results of the two fits were identical, the '2+8' fit would be the preferred one to present outside
 746 T2K due to its simplicity, robustness, economy of assumptions and ease of explanation. It is physically correct and
 747 accounts for the full systematic error on our measurements.

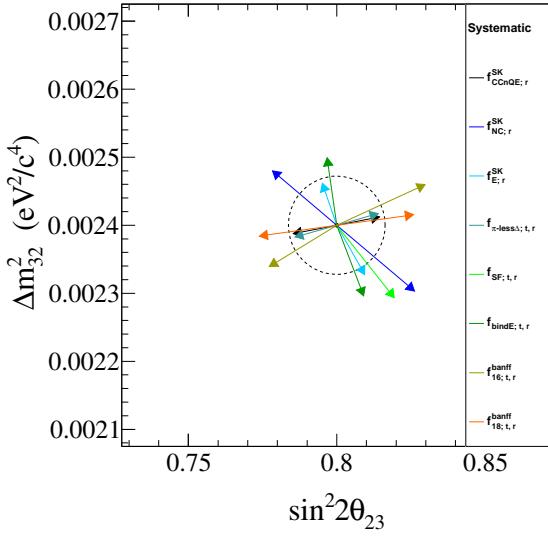


Figure 26: Effects of variation by $\pm 1\sigma$ of the 8 dominant systematic parameters on the oscillation parameters $\sin^2 2\theta_{23}$ and $|\Delta m_{32}^2|$. The method used for estimating the systematic shift is described in Sec. 4.4. The ellipse shown is one quarter the size of the statistical error. The true 23-sector oscillation parameters used are $\sin^2 2\theta_{23} = 0.80$ and $|\Delta m_{32}^2| = 2.4 \times 10^{-3} eV^2/c^4$. The 2012 PDG values are used for $\sin^2 2\theta_{13}$, $\sin^2 2\theta_{12}$ and Δm_{21}^2 , and $\delta_{CP}=0$. The normal mass hierarchy is assumed.

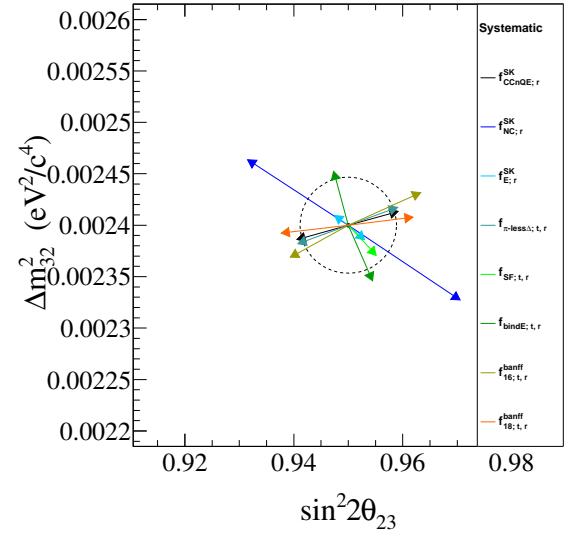


Figure 27: As in Fig. 26, but for true 23-sector oscillation parameters $\sin^2 2\theta_{23} = 0.95$ and $|\Delta m_{32}^2| = 2.4 \times 10^{-3} eV^2/c^4$.

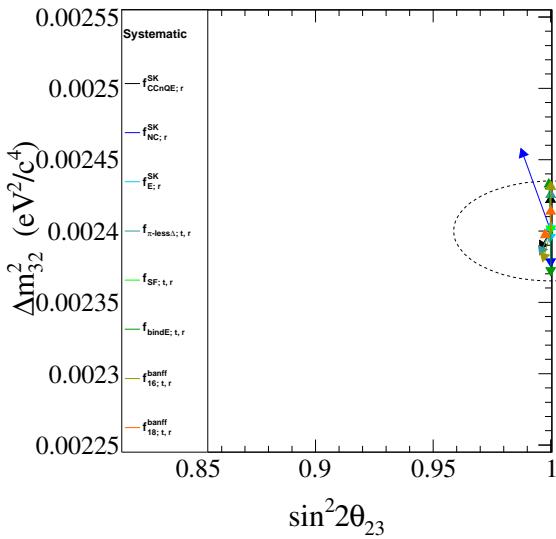


Figure 28: As in Fig. 26, but for true 23-sector oscillation parameters $\sin^2 2\theta_{23} = 1.00$ and $|\Delta m_{32}^2| = 2.4 \times 10^{-3} eV^2/c^4$.

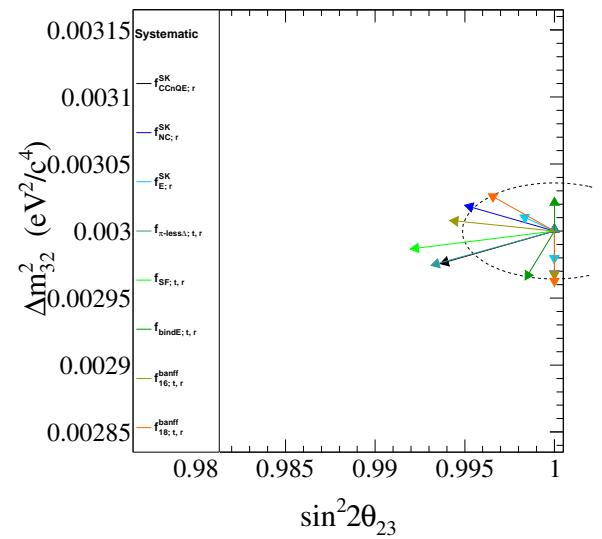


Figure 29: As in Fig. 26, but for true 23-sector oscillation parameters $\sin^2 2\theta_{23} = 1.00$ and $|\Delta m_{32}^2| = 3.0 \times 10^{-3} eV^2/c^4$.

748 **4.5. Construction of confidence regions**

749 In this analysis, we present confidence regions for all variations of the oscillation fit ('2+N' and '2+8'). Confidence
 750 regions are shown with both the constant $\Delta\chi^2$ (see Sec. 4.5.1) and the Feldman and Cousins (see Sec. 4.5.2) methods.
 751 A definite recommendation on the preferred methodology for constructing confidence regions was provided by the
 752 T2K ν_μ contour committee [30] and it will be reiterated in Sec. 5.7.

753 The two methods have been described in detail in past T2K technical notes and presentations. For completeness, we
 754 summarise both of these methods here and provide definite statements on the exact methodology used for incorporating
 755 systematic errors.

756 The methods differ in the calculation of the critical values of $\Delta\chi^2$, which are used to identify the areas of the
 757 parameter space to be included in the allowed region for a given confidence level. This allowed region is

$$\chi^2(\sin^2 2\theta_{23}, |\Delta m_{32}^2|; \mathbf{a}) < \chi^2_{min} + \Delta\chi^2_{critical} \quad (6)$$

758 However, the procedure followed for constructing the χ^2 surface itself, as a function of $\sin^2 2\theta_{23}$ and $|\Delta m_{32}^2|$, is
 759 common to both methods. Assuming that N systematic parameters are allowed to float in the oscillation fit, the values
 760 of $\chi^2(\sin^2 2\theta_{23}, |\Delta m_{32}^2|; \mathbf{a})$ are calculated via a '0+N' fit at *each* point of the $(\sin^2 2\theta_{23}, |\Delta m_{32}^2|)$ 2-dimensional grid,
 761 i.e. by fixing the oscillation parameters to the true values for the given grid point and minimising χ^2 with respect to the
 762 N systematic parameters.

763 The following grid spacing is used in all confidence region construction methods: $\delta \sin^2 2\theta_{23} = 5 \times 10^{-3}$ and
 764 $\delta |\Delta m_{32}^2| = 1 \times 10^{-4} eV^2/c^4$. The $|\Delta m_{32}^2|$ binning is the same as that used in our Run 1+2 analysis, while the $\sin^2 2\theta_{23}$
 765 bin size is reduced by 50% since sensitivity studies showed that the contour was expected to shrink in $\sin^2 2\theta_{23}$ by a
 766 similar factor.

767 **4.5.1. Constant $\Delta\chi^2$ method**

768 The constant $\Delta\chi^2$ method for quoting uncertainties on parameters measured jointly ($\sin^2 2\theta_{23}$, $|\Delta m_{32}^2|$ in our
 769 analysis) is described in [21] (pp. 390-401). It is a fully frequentist treatment using the Gaussian approximation. One
 770 finds the best-fit point and calculates the confidence contours as lines of *constant* $\Delta\chi^2$ from this point⁹.

771 **4.5.2. Feldman and Cousins method**

772 The work of Feldman and Cousins [26] uses the freedom which is inherent in the Neyman construction of confidence
 773 regions to address cases (in particular, cases with Poisson processes with background and Gaussian errors near
 774 a physical boundary) where classical construction of confidence regions produces overcoverage, undercoverage, or in
 775 extreme cases, an empty region.

776 Using the Feldman and Cousins method, construction of the confidence region proceeds as follows: a number of
 777 toy MC experiment fits is performed for each point of the $(\sin^2 2\theta_{23}, |\Delta m_{32}^2|)$ 2-dimensional grid. For each grid point,
 778 the critical value of $\Delta\chi^2$ ($\Delta\chi^2_{critical}$) is found such that α of the toy MC experiments have $\Delta\chi^2_{MC} < \Delta\chi^2_{critical}$, where
 779 α is the desired confidence level. The value of $\Delta\chi^2_{MC}$ for each toy MC experiment is calculated as

$$\Delta\chi^2_{MC} = \chi^2(\text{true}) - \chi^2(\text{MC, best fit}) \quad (7)$$

780 where "true" means that the χ^2 was computed using the true values of the oscillation parameters at that grid point, and
 781 "best-fit" means that the χ^2 was computed using the actual best-fit values for that MC experiment. The χ^2 values are
 782 calculated using Eq. 5.

783 The Feldman and Cousins confidence regions for a fit to an actual dataset are drawn such that grid points with
 784 $\Delta\chi^2_{data} < \Delta\chi^2_{critical}$ are included within the contour, where $\Delta\chi^2_{data}$ is given by

$$\Delta\chi^2_{data} = \chi^2(\text{true}) - \chi^2(\text{data, best fit}) \quad (8)$$

785 The principal difference between the Feldman and Cousins and the constant $\Delta\chi^2$ methods is that the former de-
 786 termines the value of $\Delta\chi^2_{critical}$ individually for each grid point, whereas the latter uses the same value for all grid
 787 points.

⁹For 1 fit parameter, the critical values of $\Delta\chi^2$ used are 1.00 (68% CL), 2.71 (90% CL), 3.84 (95% CL), 6.63 (99% CL). For 2 parameters fitted simultaneously, the critical values of $\Delta\chi^2$ used are 2.30 (68% CL), 4.61 (90% CL), 5.99 (95% CL), 9.21 (99% CL).

Parameter	$\frac{\delta_{syst} \sin^2 2\theta_{23}}{\delta_{stat} \sin^2 2\theta_{23}}$	$\frac{\delta_{syst} \Delta m_{32}^2 (eV^2/c^4)}{\delta_{stat} \Delta m_{32}^2 (eV^2/c^4)}$
$f_{E;r}^{SK}$	0.3486	0.3058
$f_{CCQEoth;r}^{SK}$	0.0872	0.0544
$f_{CCQERC0;r}^{SK}$	0.0106	0.0099
$f_{CCQERC1;r}^{SK}$	0.1398	0.1109
$f_{CCQERC2;r}^{SK}$	0.0686	0.0741
$f_{CCnQE;r}^{SK}$	0.3107	0.2134
$f_{NC;r}^{SK}$	1.1500	0.6091
$f_{\nu_e;r}^{banff}$	0.0130	0.0167
$f_{0;t,r}^{banff}$	0.0756	0.0682
$f_{1;t,r}^{banff}$	0.0883	0.1495
$f_{2;t,r}^{banff}$	0.0949	0.1248
$f_{3;t,r}^{banff}$	0.0946	0.0693
$f_{4;t,r}^{banff}$	0.2048	0.1899
$f_{5;t,r}^{banff}$	0.1053	0.0881
$f_{6;t,r}^{banff}$	0.0538	0.0452
$f_{7;t,r}^{banff}$	0.0130	0.0114
$f_{8;t,r}^{banff}$	0.0100	0.0077
$f_{9;t,r}^{banff}$	0.0051	0.0031
$f_{10;t,r}^{banff}$	0.0042	0.0029
$f_{11;t,r}^{banff}$	0.0043	0.0045
$f_{12;t,r}^{banff}$	0.0051	0.0061
$f_{13;t,r}^{banff}$	0.0103	0.0094
$f_{14;t,r}^{banff}$	0.0083	0.0079
$f_{15;t,r}^{banff}$	0.0034	0.0022
$f_{16;t,r}^{banff}$	0.5979	0.4068
$f_{17;t,r}^{banff}$	0.1557	0.1067
$f_{18;t,r}^{banff}$	0.4188	0.2891
$f_{19;t,r}^{banff}$	0.0610	0.0707
$f_{20;t,r}^{banff}$	0.0048	0.0059
$f_{21;t,r}^{banff}$	0.2142	0.1333
$f_{22;t,r}^{banff}$	0.0422	0.0462
$f_{pF;t,r}$	0.0526	0.0592
$f_{bindE;t,r}$	0.3108	0.3597
$f_{SF;t,r}$	0.4914	0.4249
$f_{\pi-less\Delta;t,r}$	0.3358	0.2342
$f_{CCothShape;t,r}$	0.0249	0.0181
$f_{Wshape;t,r}$	0.0653	0.0414
$f_{CCcoh;t}$	0.0348	0.0301
$f_{NC1\pi^\pm;t}$	0.1282	0.0941
$f_{NCoth;t}$	0.1083	0.0858
$f_{CC\nu_e;t}$	0.0052	0.0022
$f_{CC\bar{\nu}_e;t}$	0.1032	0.0750
$f_{0;t,r}^{FSI}$	0.0056	0.0020
$f_{1;t,r}^{FSI}$	0.0049	0.0024
$f_{2;t,r}^{FSI}$	0.0054	0.0022
$f_{3;t,r}^{FSI}$	0.1223	0.0944
$f_{4;t,r}^{FSI}$	0.0059	0.0100
$f_{5;t,r}^{FSI}$	0.0550	0.0473

Table 12: Maximum deviations, as a fraction of statistical error at the oscillation parameter grid point, from the input values of 2+0 fits to datasets with ± 1 sigma individual systematic variations at a range of oscillation points. The 8 most important systematics are highlighted in red.

788 The Feldman and Cousins method does not specify how systematics are to be included in the confidence region
 789 construction and different choices exist. To construct a 2-dimensional ($\sin^2 2\theta_{23}$, $|\Delta m_{32}^2|$) confidence region, where all
 790 N systematic parameters are included in the p.d.f. and all N systematics are allowed to float in the fit, this analysis
 791 uses the following methodology: the value of $\Delta\chi_{critical}^2$ at each true ($\sin^2 2\theta_{23}$, $|\Delta m_{32}^2|$) grid point is calculated from
 792 an ensemble of toy MC experiments, each one of which is generated with the true oscillation parameters of that point
 793 and with all N systematics randomised. For each toy MC experiment, a ‘2+N’ fit is performed to obtain the value
 794 of $\chi^2(MC, \text{best fit})$ used in Eq. 7. A separate ‘0+N’ fit, with the oscillation parameters fixed to the true values, is
 795 performed to obtain the value of $\chi^2(\text{true})$, i.e. χ^2 is *independently* minimised, for *each* toy MC experiment, with
 796 respect to the systematic parameters. If only a subset M ($M < N$) of the N systematics is allowed to float in the fit,
 797 all N systematics are again randomized in the generation of the datasets, and ‘2+M’ and ‘0+M’ fits are performed to
 798 obtain $\chi^2(MC, \text{best fit})$ and $\chi^2(\text{true})$ respectively

799 In Fig. 30, we show a Monte Carlo estimation using the Feldman-Cousins method of the $\Delta\chi_{critical}^2$ values used for
 800 calculation of the 68% and 90% CL confidence regions for the 3.010×10^{20} -POT 3-flavour ν_μ -disappearance analysis
 801 for both the ‘2+8’ and ‘2+N’ fit variants. The surfaces were generated using an ensemble of toy MC experiments which
 802 included both randomized systematic variations and statistical fluctuations. Slices of the 2-dimensional distributions
 803 shown in Fig. 30, are shown in Figs. 31 and 32. From these $\Delta\chi_{critical}^2$ distributions, we anticipate that the confidence
 804 regions produced using the Feldman-Cousins method will be narrower along $|\Delta m_{32}^2|$ at maximal mixing than those
 805 made with the $\Delta\chi_{critical}^2$ method. The Feldman-Cousins contours will also be wider along $\sin^2 2\theta_{23}$ for values of
 806 $|\Delta m_{32}^2|$ near the best fit.

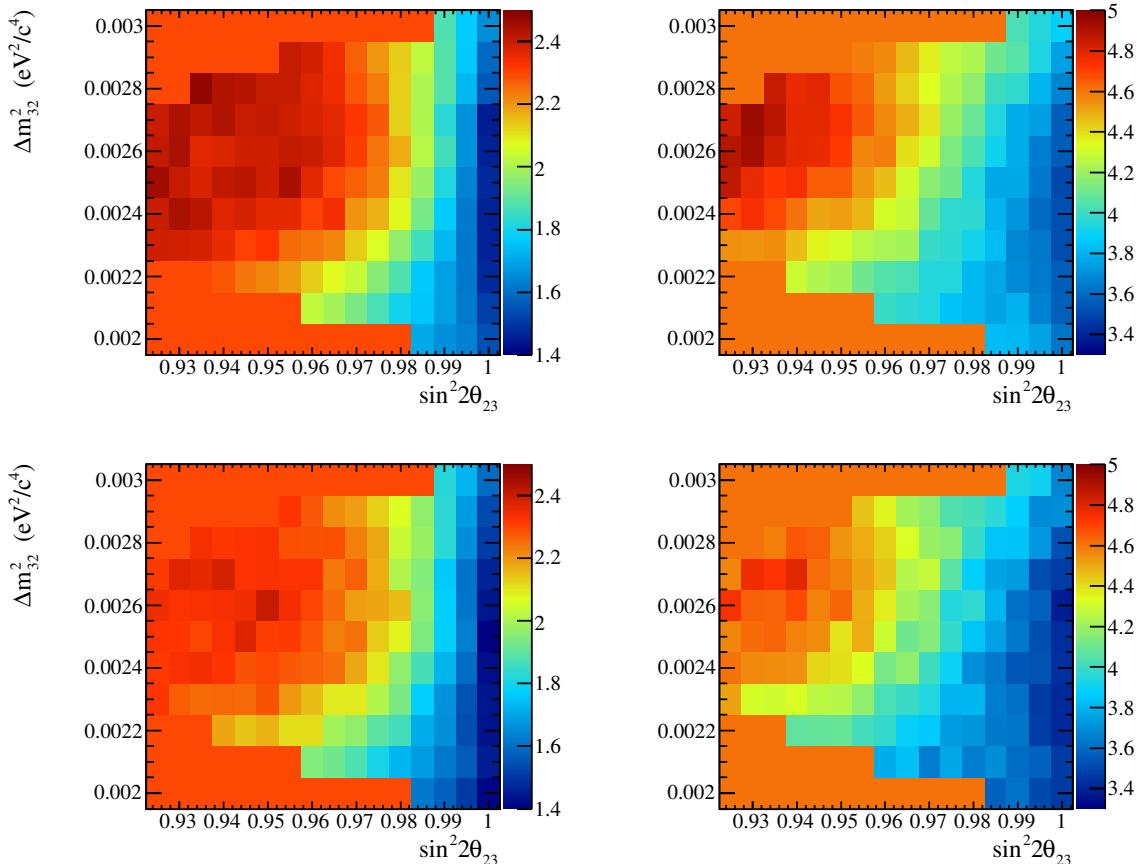


Figure 30: Monte Carlo estimation, according to the method of Feldman and Cousins, of $\Delta\chi_{critical}^2$ values $\Delta\chi_{68}^2$ (left) and $\Delta\chi_{90}^2$ (right) as functions of $\sin^2 2\theta_{23}$ and $|\Delta m_{32}^2|$, for calculation of the 68% and 90% CL confidence regions for the 3.010×10^{20} -POT 3-flavour ν_μ -disappearance analysis. The top row shows $\Delta\chi_{critical}^2$ surfaces calculated using the ‘2+8’ fit, whereas the bottom row shows surfaces calculated using the ‘2+N’ fit. The surfaces were generated from an ensemble of toy-MC experiments including both randomized systematic variations and statistical fluctuations. As expected from [26], the values of $\Delta\chi_{critical}^2$ decrease as the physical boundary at $\sin^2 2\theta_{23} = 1$ is approached.

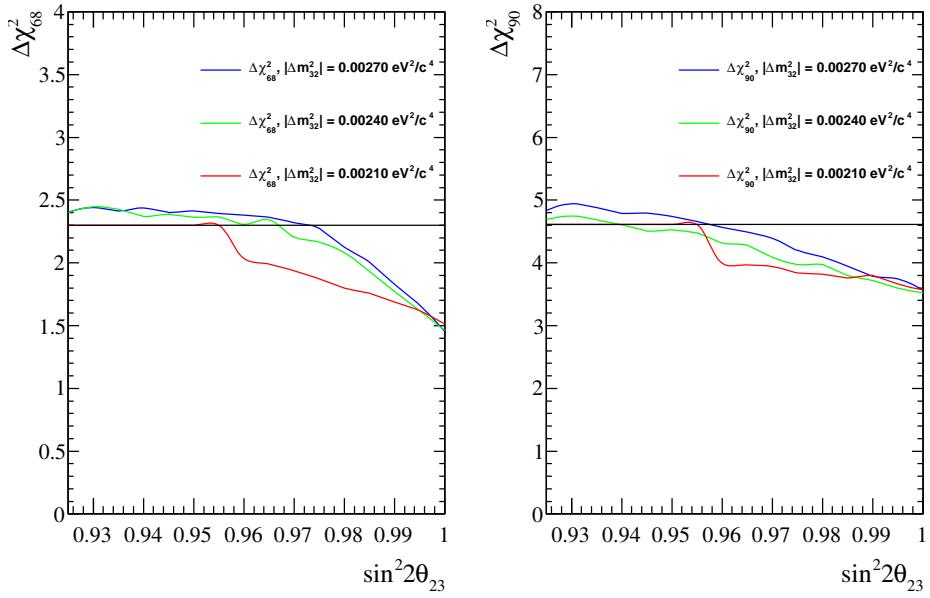


Figure 31: Monte Carlo estimation, according to the method of Feldman and Cousins, of $\Delta\chi^2_{critical}$ values $\Delta\chi^2_{68}$ (left) and $\Delta\chi^2_{90}$ (right), as functions of $\sin^2 2\theta_{23}$ for 3 different values of $|\Delta m^2_{32}|$ ($2.1 \times 10^{-3} \text{ eV}^2/\text{c}^4$, $2.4 \times 10^{-3} \text{ eV}^2/\text{c}^4$ and $2.7 \times 10^{-3} \text{ eV}^2/\text{c}^4$). The $\Delta\chi^2_{critical}$ values were calculated from an ensemble of toy-MC experiments, for an exposure of 3.010×10^{20} POT, including both randomized systematic variations and statistical fluctuations. The ‘2+8’ fit was used. For comparison, the canonical value used in the constant $\Delta\chi^2_{critical}$ method is also shown as a horizontal line.

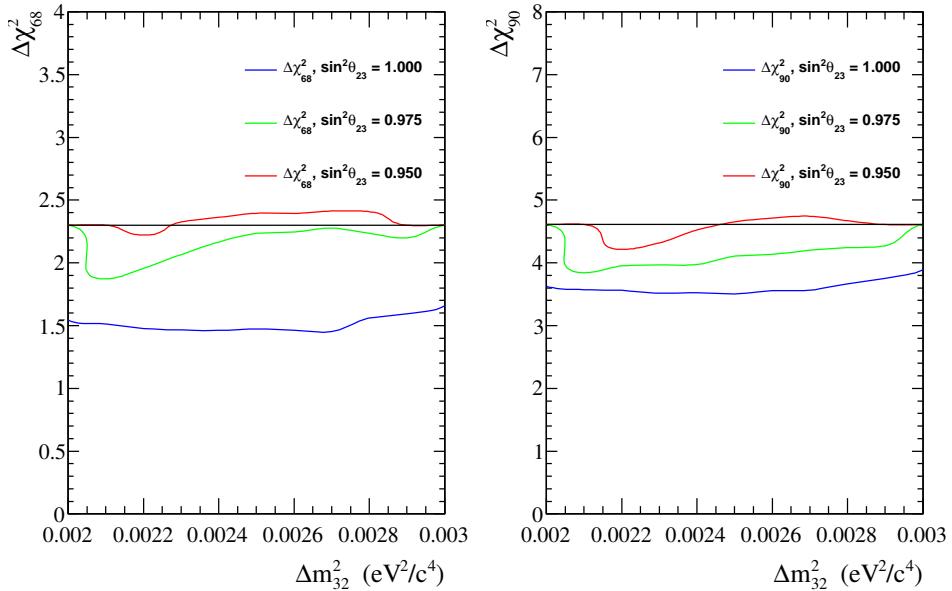


Figure 32: Monte Carlo estimation, according to the method of Feldman and Cousins, of $\Delta\chi^2_{critical}$ values $\Delta\chi^2_{68}$ (left) and $\Delta\chi^2_{90}$ (right), as functions of $|\Delta m^2_{32}|$ for 3 different values of $\sin^2 2\theta_{23}$ (0.950, 0.975 and 1.000). The $\Delta\chi^2_{critical}$ values were calculated from an ensemble of toy MC experiments, for an exposure of 3.010×10^{20} POT, including both randomized systematic variations and statistical fluctuations. The ‘2+8’ fit was used. For comparison, the canonical value used in the constant $\Delta\chi^2_{critical}$ method is also shown as a horizontal line.

807 **5. Results of the disappearance analysis with the Run 1+2+3 (3.010×10^{20} POT) dataset**

808 *5.1. Best-fit oscillation parameters and systematic parameter pulls*

809 ‘2+N’ and ‘2+8’ 3-flavour ν_μ -disappearance fits were performed using the method described in section 4 on the
 810 combined 3.010×10^{20} POT Run 1+2+3 dataset and, separately, on the 1.431×10^{20} POT Run 1+2 and the 1.579×10^{20}
 811 POT Run 3 datasets. The first octant is assumed for θ_{23} ($\sin(\theta_{23}) \leq 0.5$) and the fit is for $\sin^2 2\theta_{23}$ and $|\Delta m_{32}^2|$ unless
 812 explicitly stated otherwise.

813 Using the ‘2+N’ fit for $\sin^2 \theta_{23}$, this analysis found $|\Delta m_{32}^2| = 2.441 \times 10^{-3} \text{ eV}^2/c^4$ and $\sin^2 2\theta_{23} = 0.514$ to be the best-fit values for the Run 1+2+3 dataset.

814 Using the ‘2+N’ fit, this analysis found $|\Delta m_{32}^2| = 2.443 \times 10^{-3} \text{ eV}^2/c^4$ and $\sin^2 2\theta_{23} = 1.000$ to be the best-fit values for the Run 1+2+3 dataset. Similar best-fit values were obtained from separate ‘2+N’ fits to subsets of the full dataset. A ‘2+N’ fit to the Run 1+2 dataset gave best-fit values of $|\Delta m_{32}^2| = 2.588 \times 10^{-3} \text{ eV}^2/c^4$ and $\sin^2 2\theta_{23} = 0.986$, while a fit to the Run 3 dataset gave $|\Delta m_{32}^2| = 2.383 \times 10^{-3} \text{ eV}^2/c^4$ and $\sin^2 2\theta_{23} = 1.000$.

815 Using the ‘2+N’ fit, assuming that θ_{23} is in the second octant, yields a best-fit point almost identical to that assuming the first octant; we found $|\Delta m_{32}^2| = 2.441 \times 10^{-3} \text{ eV}^2/c^4$ and $\sin^2 2\theta_{23} = 0.999$.

816 The ‘2+8’ fits produced results that are nearly identical to those from the ‘2+N’ fits. Running the ‘2+8’ fit on the
 817 combined Run 1+2+3 dataset, we found $|\Delta m_{32}^2| = 2.442 \times 10^{-3} \text{ eV}^2/c^4$ and $\sin^2 2\theta_{23} = 1.000$ as the best-fit values. A
 818 ‘2+8’ fit to the Run 1+2 dataset gave best-fit values of $|\Delta m_{32}^2| = 2.589 \times 10^{-3} \text{ eV}^2/c^4$ and $\sin^2 2\theta_{23} = 0.986$, while a
 819 ‘2+8’ fit to the Run 3 dataset gave $|\Delta m_{32}^2| = 2.385 \times 10^{-3} \text{ eV}^2/c^4$ and $\sin^2 2\theta_{23} = 1.000$.

820 The results of the fits are summarized in Tabs. 13 and 14, for fits to $\sin^2 \theta_{23}$ and $\sin^2 2\theta_{23}$ respectively. In these tables are the best-fit oscillation parameters, the observed and expected number of single μ -like ring events, and the values of χ^2 per degree of freedom at the best-fit. The ‘2+N’ and ‘2+8’ fits give nearly identical best-fit values for the combined Run 1+2+3 dataset and, in fact, for all running periods¹⁰. Also the best-fit values are nearly identical between assuming the first octant and second octants for θ_{23} for the combined Run 1+2+3 dataset.

821 Using Eq. 4 and the value $\sin^2(2\theta_{13}) = 0.098$ used in this analysis, the point of maximal disappearance occurs at
 822 $\sin^2(2\theta_{23}) = 0.999$ for the second octant, whilst the point of maximal disappearance is $\sin^2(2\theta_{23}) = 1.000$ for the first octant. The result of the 2-flavour fit without the physical boundary show that the fit favours a high amount of disappearance, more than is physically allowed in the 2-flavour framework. Therefore it is not surprising that the ‘2+N’ best-fit points’ in the 3-flavour framework, are different, and sit at the point of maximal disappearance, for the given octant assumption.

823 The pull for each systematic parameter f included in the fit, is calculated as

$$\frac{f_{bf} - f_{nom}}{\sigma_{bf}}, \quad (9)$$

824 where f_{bf} is the best-fit value of the systematic parameter, f_{nom} is the nominal value of the parameter (corresponding to no systematic variation), and σ_{bf} is the Hesse error output from Minuit.

825 The pulls of all 48 systematic parameters allowed to float in the ‘2+N’ fit are shown in Fig. 33 for the fit to the Run
 826 1+2+3 dataset using $\sin^2 \theta_{23}$, in Fig. 34 for the fit to the Run 1+2+3 dataset assuming the first octant for θ_{23} , in Fig. 35
 827 for the fit to the Run 1+2+3 dataset assuming the second octant, and in Figs. 36-37 for the fits to the Run 1+2 and Run
 828 3 datasets. From these figures, it is apparent that most systematic parameters barely move from their nominal values.
 829 The pulls for the 8 dominant systematic parameters allowed to float in the ‘2+8’ fit are shown in Fig. 38 for the fit to
 830 the Run 1+2+3 dataset, and in Figs. 39-40 for the fits to the Run 1+2 and Run 3 datasets. The systematic parameter
 831 pulls shown in Fig. 34 for the ‘2+N’ fit are similar to those in Fig. 38 for the ‘2+8’ fit. The systematic parameter pulls
 832 shown in Fig. 35 for the ‘2+N’ fit assuming the second octant are similar to those in Fig. 34 for the ‘2+N’ fit assuming
 833 the first octant. For the ‘2+N’ case, we note that, although all 48 systematic parameters are allowed to float in the fit,
 834 only 6 of them move by more than $\pm 0.1\sigma$, for either octant assumption, and when fitting for $\sin^2 \theta_{23}$.

¹⁰It is interesting to know what the best-fit values would have been, had $\sin^2(2\theta_{23})$ been allowed to enter into the unphysical region. This question can not be answered in a 3-flavour framework due to the existence of a $\sqrt{1 - \sin^2(2\theta_{23})}$ term in the oscillation probabilities, so we performed fits in a simple 2-flavour framework. In the presence of the physical boundary, a ‘2+8’ fit to the Run 1+2+3 dataset yields the following best-fit values: $\sin^2(2\theta_{23}) = 1.000$ and $|\Delta m_{32}^2| = 2.47 \times 10^{-3} \text{ eV}^2/c^4$. If we do not constrain $\sin^2(2\theta_{23})$ within the physical region, the same fit yields the following best-fit values: $\sin^2(2\theta_{23}) = 1.025$ and $|\Delta m_{32}^2| = 2.47 \times 10^{-3} \text{ eV}^2/c^4$.

Analysis	$\sin^2 \theta_{23}$	Δm_{32}^2	N_{obs}	N_{exp}	χ^2_{bf}/ndf	p-value
3-flavour $\sin^2 2\theta_{23}$ 1st octant	0.500	$2.443 \cdot 10^{-3}$	58	57.97	56.04/71	0.83
3-flavour $\sin^2 2\theta_{23}$ 2nd octant	0.516	$2.441 \cdot 10^{-3}$	58	57.92	56.03/71	0.82
3-flavour $\sin^2 \theta_{23}$	0.514	$2.441 \cdot 10^{-3}$	58	57.92	56.03/71	0.80

Table 13: Summary of best-fit parameters for the combined Run 1+2+3 datasets for '2+N' fits with $\sin^2 2\theta_{23}$ converted to $\sin^2 \theta_{23}$ (with both θ_{23} octant assumptions), and a '2+N' fit with $\sin^2 \theta_{23}$. The quoted best-fit χ^2 values (χ^2_{bf}) were computed from Eq. 5 with the reconstructed energy binning used in each fit.

Analysis	Run period	$\sin^2 2\theta_{23}$	Δm_{32}^2	N_{obs}	N_{exp}	χ^2_{bf}/ndf	p-value
2012 / 3-flavour 1st octant / '2+N'	Run 1+2+3	1.000	$2.443 \cdot 10^{-3}$	58	57.97	56.04/71	0.83
2012 / 3-flavour 2nd octant / '2+N'	Run 1+2+3	0.999	$2.441 \cdot 10^{-3}$	58	57.92	56.03/71	0.82
2012 / 3-flavour 1st octant / '2+8'	Run 1+2+3	1.000	$2.442 \cdot 10^{-3}$	58	57.92	56.15/71	0.82
2012 / 3-flavour 1st octant / '2+N'	Run 3	1.000	$2.383 \cdot 10^{-3}$	27	29.58	56.28/71	0.83
2012 / 3-flavour 1st octant / '2+8'	Run 3	1.000	$2.385 \cdot 10^{-3}$	27	29.60	56.32/71	0.63
2012 / 3-flavour 1st octant / '2+N'	Run 1+2	0.986	$2.588 \cdot 10^{-3}$	31	29.04	38.96/71	0.82
2012 / 3-flavour 1st octant / '2+8'	Run 1+2	0.986	$2.589 \cdot 10^{-3}$	31	29.04	39.06/71	0.68
2010 / 2-flavour / '2+0'	Run 1+2	0.98	$2.65 \cdot 10^{-3}$	31	29.18	61.578/198	-

Table 14: Summary of best-fit parameters for the oscillation fits to the Run 1+2, Run 3, and combined Run 1+2+3 datasets. Best-fit values are given for both θ_{23} octants. The 2010 result is taken from the analysis presented in [2]. The quoted best-fit χ^2 values (χ^2_{bf}) were computed from Eq. 5 with the reconstructed energy binning used in each fit. The table also shows the p-values obtained from the goodness-of-fit test of Sec. 4.2 for the '2+N' and '2+8' oscillation fits to the Run 1+2, Run 3, and combined Run 1+2+3 datasets. Again values are given for both θ_{23} octants.

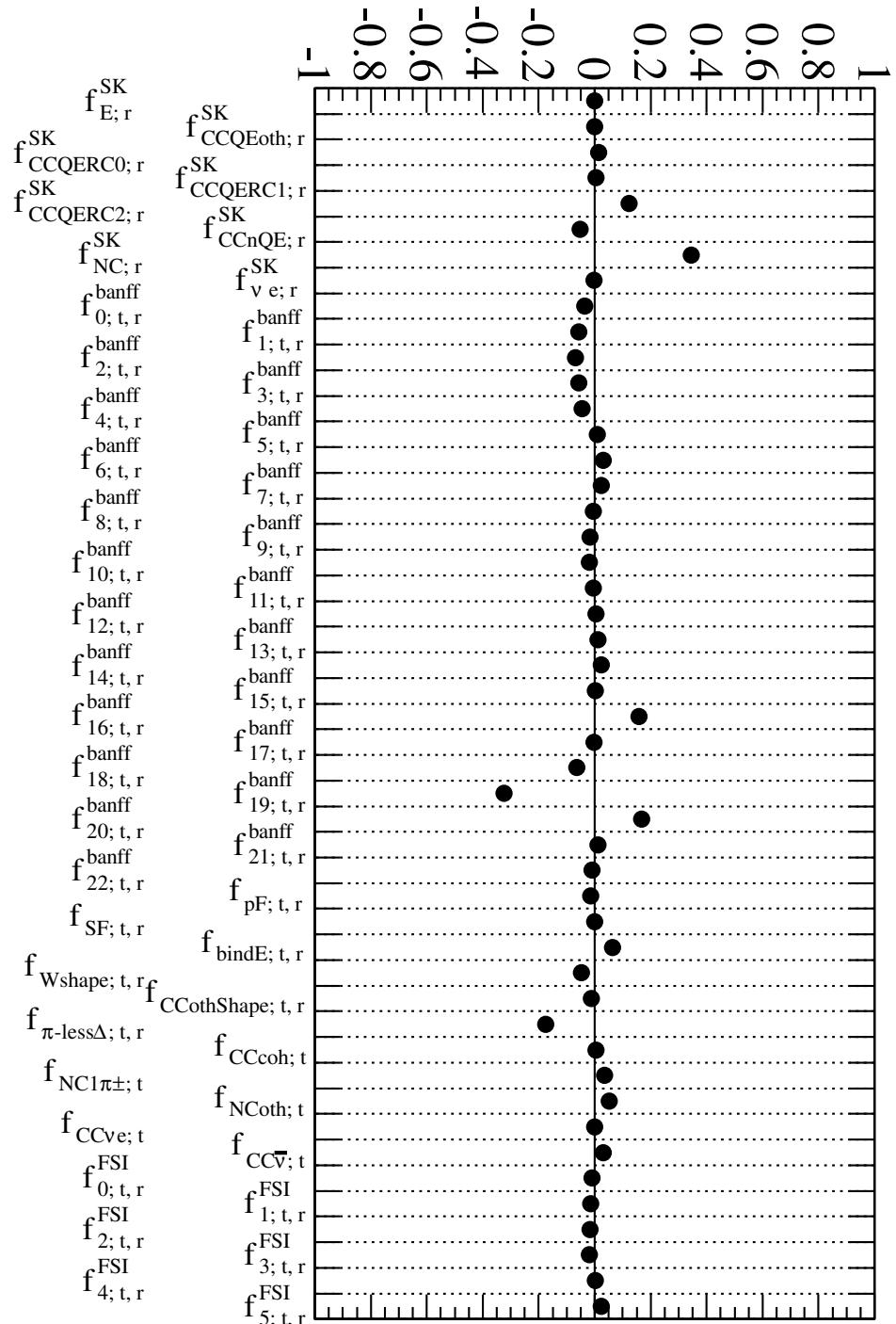


Figure 33: Systematic parameter pulls for the '2+N' $\sin^2 \theta_{23}$ fit to the Run 1+2+3 dataset.

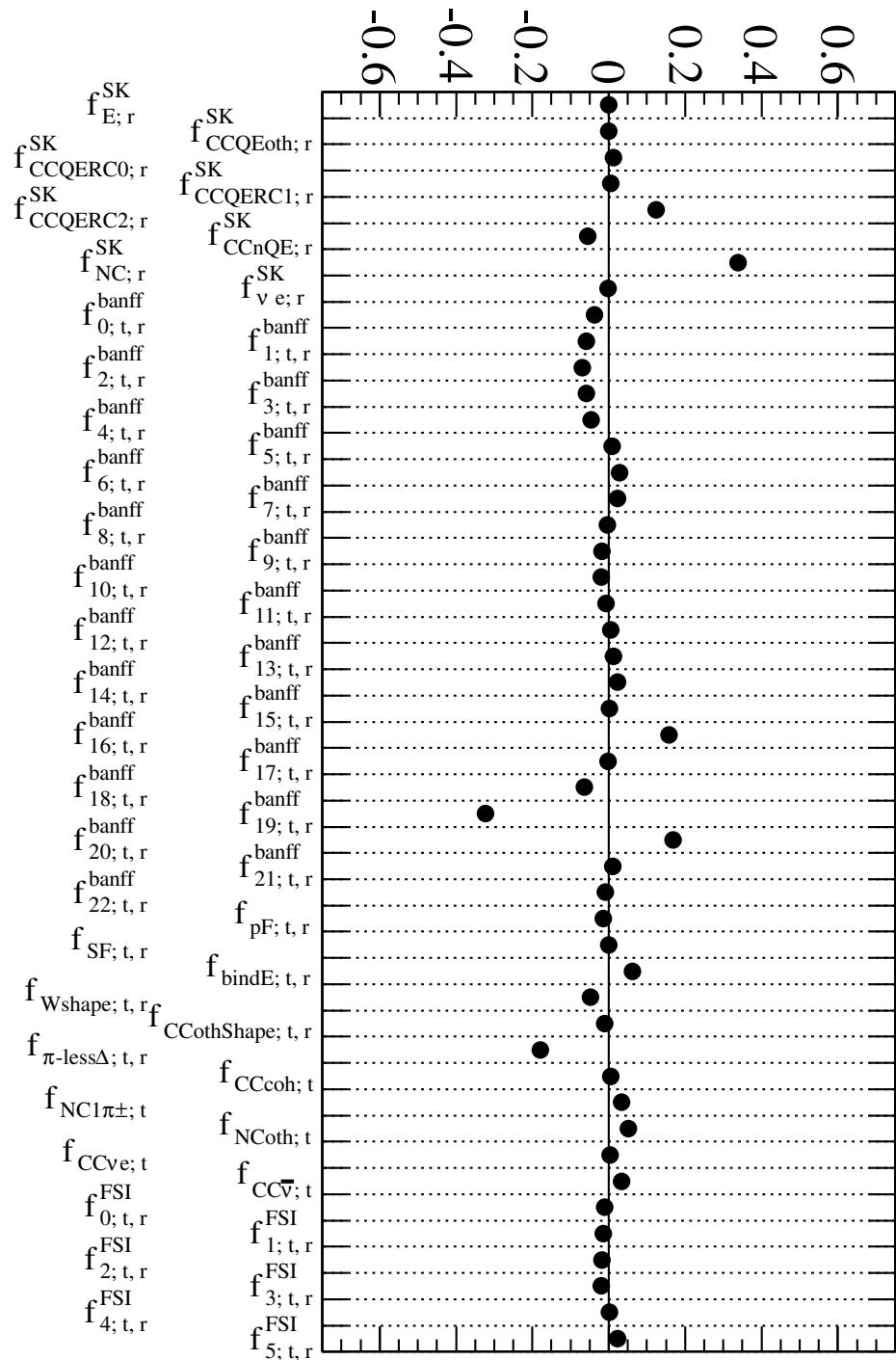


Figure 34: Systematic parameter pulls for the ‘2+N’ fit to the Run 1+2+3 dataset, assuming θ_{23} is in the first octant.

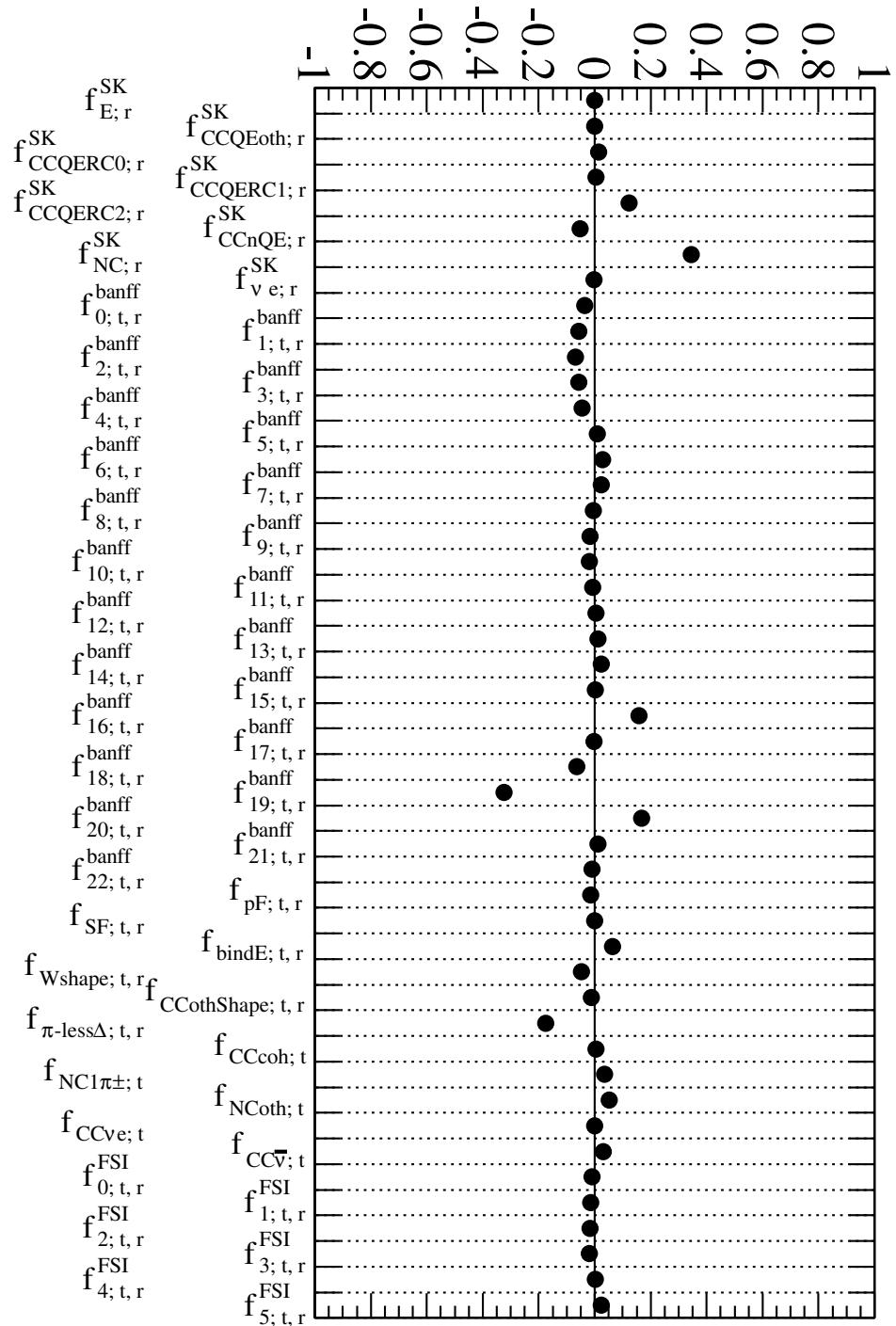


Figure 35: Systematic parameter pulls for the '2+N' fit to the Run 1+2+3 dataset, assuming θ_{23} is in the second octant.

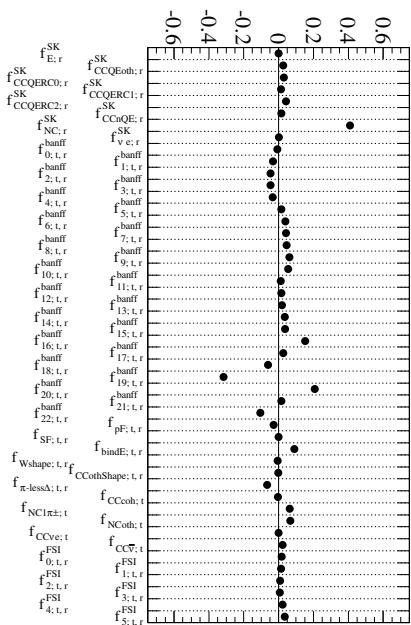


Figure 36: Systematic parameter pulls for the ‘2+N’ fit to the Run 1+2 dataset.

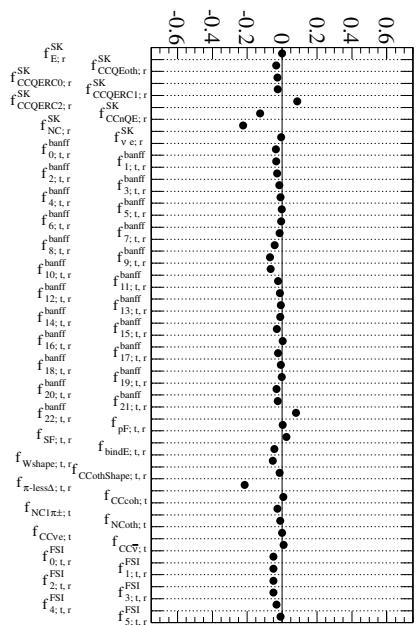


Figure 37: Systematic parameter pulls for the ‘2+N’ fit to the Run 3 dataset.

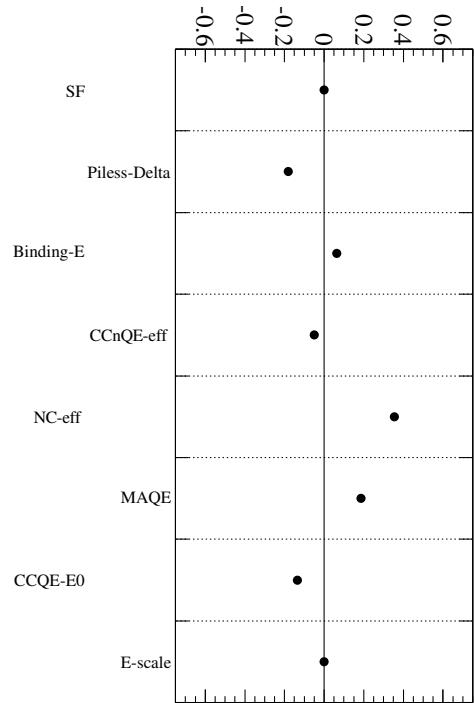


Figure 38: Systematic parameter pulls for the '2+8' fit to the Run 1+2+3 dataset.

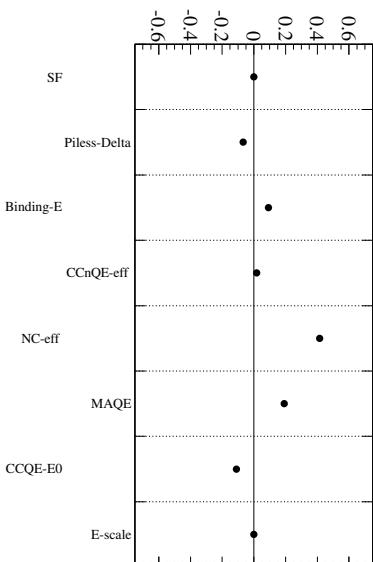


Figure 39: Systematic parameter pulls for the ‘2+8’ fit to the Run 1+2 dataset.

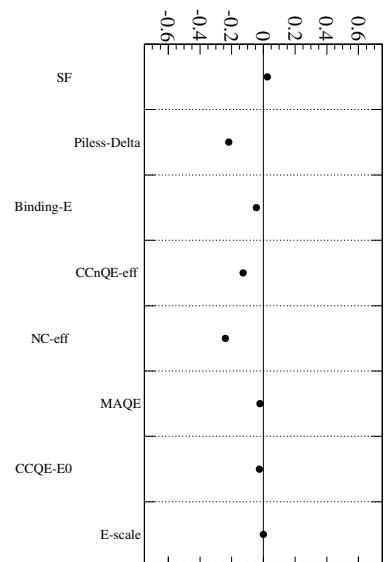


Figure 40: Systematic parameter pulls for the ‘2+8’ fit to the Run 3 dataset.

849 **5.2. Goodness-of-fit tests**

850 Goodness-of-fit tests were performed as described in Sec. 4.2, and the p-values for all ‘2+N’ and ‘2+8’ $\sin^2 2\theta_{23}$
 851 fits to the Run 1+2+3, Run 1+2 and Run 3 datasets are shown in Tab. 14. The χ^2 distributions from which the p-values
 852 were calculated are shown for the ‘2+N’ fit for $\sin^2 \theta_{23}$ in Fig. 41, for the ‘2+N’ fit assuming the first and second
 853 octants for θ_{23} for Run 1+2+3 data in Figs. 42 and 43 respectively, and for the ‘2+8’ fit for Run 1+2+3 data in Fig. 44.
 854 All fits have a high degree of plausibility.

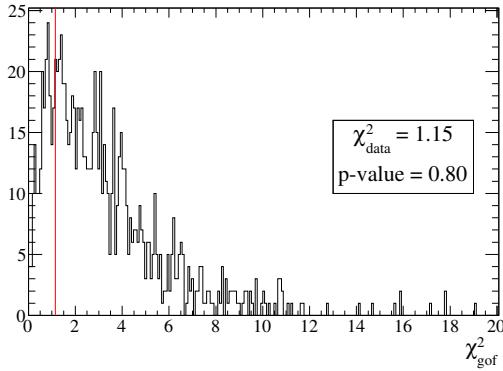


Figure 41: Distribution of χ^2_{gof} , the goodness-of-fit (gof) χ^2 , from 1k toy MC experiments generated at the ‘2+N’ $\sin^2 \theta_{23}$ Run 1+2+3 best-fit oscillation point. The χ^2_{gof} value for the Run 1+2+3 data (χ^2_{data}) is highlighted.

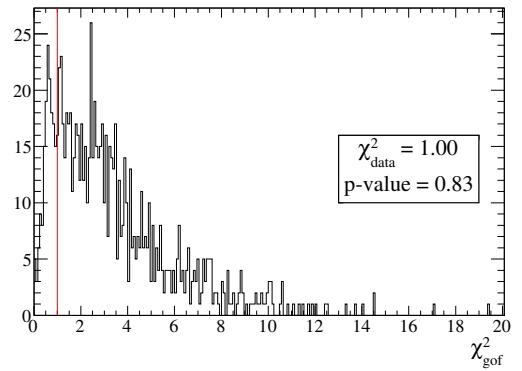


Figure 42: As in Fig. 41, but for the ‘2+N’ fit to the Run 1+2+3 dataset assuming θ_{23} is in the first octant.

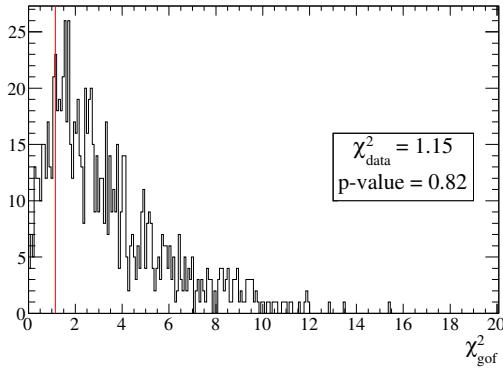


Figure 43: As in Fig. 41, but for the ‘2+N’ fit to the Run 1+2+3 dataset assuming θ_{23} is in the second octant.

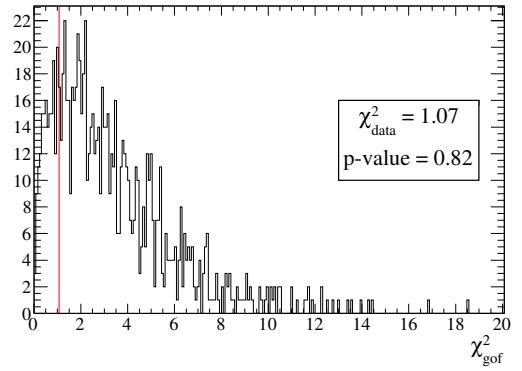


Figure 44: As in Fig. 41, but for the ‘2+8’ fit to the Run 1+2+3 dataset.

855 **5.3. Best-fit single μ -like ring reconstructed energy spectra**

856 The reconstructed neutrino energy distribution of the single μ -like ring events in the Run 1+2+3 dataset is shown in
 857 Fig. 45 along with the ‘2+N’ $\sin^2 \theta_{23}$ best-fit prediction and the prediction made under the no-oscillation hypothesis.
 858 Also shown is the ratio between the data and the no-oscillation spectrum and the ratio between the ‘2+N’ $\sin^2 \theta_{23}$ best-
 859 fit spectrum and the no-oscillation spectrum; in both of these ratios, the characteristic energy-dependent deficit can
 860 be clearly seen. The equivalent spectra for the Run 1+2+3 (assuming θ_{23} is in the first octant), Run 1+2+3 (assuming
 861 θ_{23} is in the second octant), Run 1+2 and Run 3 datasets are also shown in Figs. 46, 47, 48 and 49 respectively. All
 862 these distribution are shown in the 73-bin scheme in reconstructed neutrino energy that was used in the fitting procedure
 863 (see Sec. 2.2.5).

864 ‘2+8’ fits were also made to the Run 1+2+3, Run 1+2 and Run 3 datasets. The best-fit and no-oscillation spectra
 865 are compared with the data in Figs. 50, 51 and 52. The ratios of the data and best-fit spectra to the no-oscillation
 866 spectra are also shown in these figures, and the energy-dependent deficits are once more clearly visible.

867 Since the reconstructed energy binning used in the fit is relatively fine, it can be beneficial to see the above distributions
 868 using a coarser binning. The best-fit spectra obtained for the Run 1+2+3 dataset from the ‘2+N’ fit for $\sin^2 \theta_{23}$,
 869 the ‘2+N’ fit with θ_{23} in the first octant, the ‘2+N’ fit with θ_{23} in the second octant and the ‘2+8’ fit with θ_{23} in
 870 the first octant are shown using a coarse binning¹¹ in Figs. 53, 55, 57 and 59 respectively. It is also interesting to see
 871 the 28 components of the best-fit spectrum, each of which is calculated separately in this analysis. These components
 872 are shown for the ‘2+N’ and ‘2+8’ fits in Figs. 54, 56, 58 and 60 respectively. In these plots, the components of the
 873 spectrum are grouped into 5 categories: ν_μ CCQE, ν_μ CCnonQE, $\bar{\nu}_\mu$ CC, $\nu_e/\bar{\nu}_e$ CC and NC.

874 The ‘2+N’ best-fit predictions for $\sin^2 \theta_{23}$ and θ_{23} assuming the second octant are compared for the Run 1+2+3
 875 dataset only in Fig. 61, using the 73 reconstructed energy bins used in the fit, and in Fig. 62, using the coarser binning
 876 described above. The two best-fit spectra are nearly identical. In the 73-bin scheme used for the fit, the spectra never
 877 differ by more than 0.1% in the area below 3 GeV, and they are nearly identical in the area of the first oscillation
 878 maximum.

879 The ‘2+N’ best-fit predictions for both θ_{23} octant assumptions are compared for the Run 1+2+3 dataset only in Fig.
 880 63, using the 73 reconstructed energy bins used in the fit, and in Fig. 64, using the coarser binning described above.

881 Finally, the ‘2+N’ and ‘2+8’ best-fit predictions are compared for the Run 1+2+3 dataset only in Fig. 65, using the
 882 73 reconstructed energy bins used in the fit, and in Fig. 66, using the coarser binning described above. The two best-fit
 883 spectra are nearly identical. In the 73-bin scheme used for the fit, the spectra never differ by more than 1.5% in the
 884 area below 3 GeV, and they are nearly identical in the area of the first oscillation maximum.

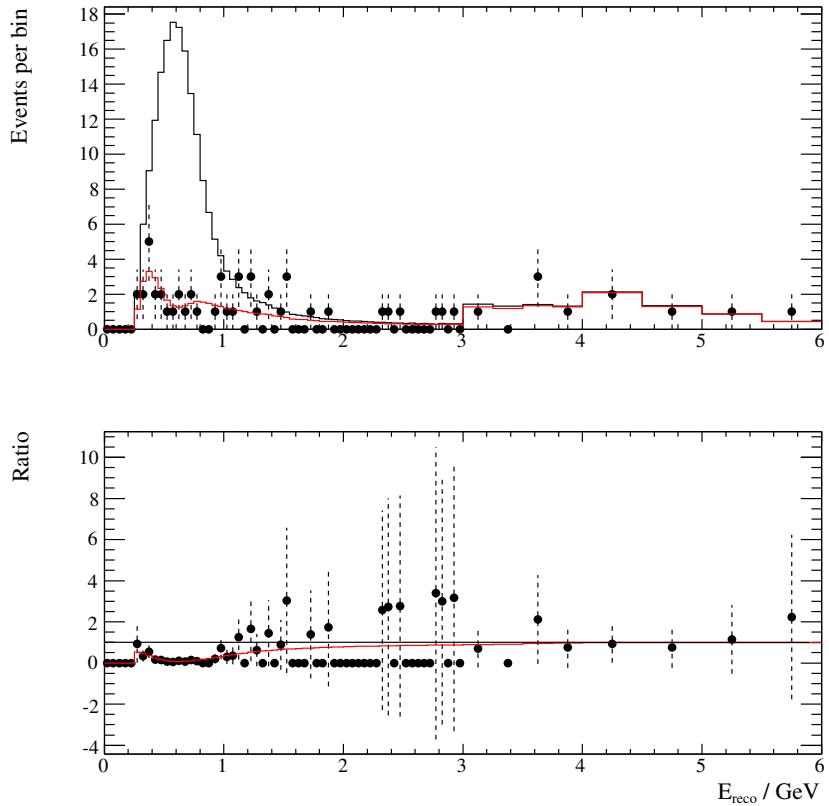


Figure 45: Best-fit reconstructed energy spectrum (top) obtained from the ‘2+N’ $\sin^2 \theta_{23}$ fit to the combined Run 1+2+3 dataset. The Run 1+2+3 dataset and the prediction obtained from the no-oscillation hypothesis are also shown. The spectra are shown using the 73 bins used in the fit (see Sec. 2.2.5). The ratio of the data and best-fit distribution to the no-oscillation hypothesis is shown in the bottom plot. The characteristic energy-dependent deficit can be clearly seen.

¹¹ 16 reconstructed energy bins arranged as follows: 1 0.3-GeV bin in 0 - 0.3 GeV, 8 0.1-GeV bins in 0.3 - 1.1 GeV, 1 0.15-GeV bin in 1.1 GeV - 1.25 GeV, 1 0.25-GeV bin in 1.25 - 1.5 GeV, 1 0.5-GeV bin in 1.5 - 2 GeV, 2 1-GeV bin in 2-4 GeV, 1 2-GeV bin in 4-6 GeV and 1 bin above 6 GeV.

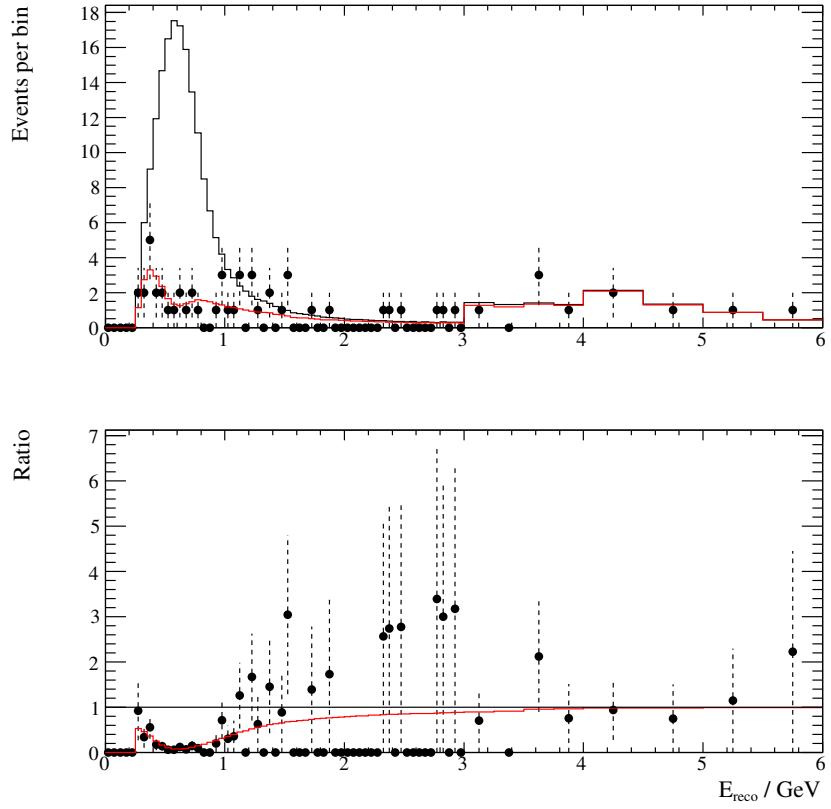


Figure 46: Best-fit reconstructed energy spectrum (top) obtained from the ‘2+N’ fit to the combined Run 1+2+3 dataset. The Run 1+2+3 dataset and the prediction obtained from the no-oscillation hypothesis are also shown. The spectra are shown using the 73 bins used in the fit (see Sec. 2.2.5). The ratio of the data and best-fit distribution to the no-oscillation hypothesis is shown in the bottom plot. The characteristic energy-dependent deficit can be clearly seen.

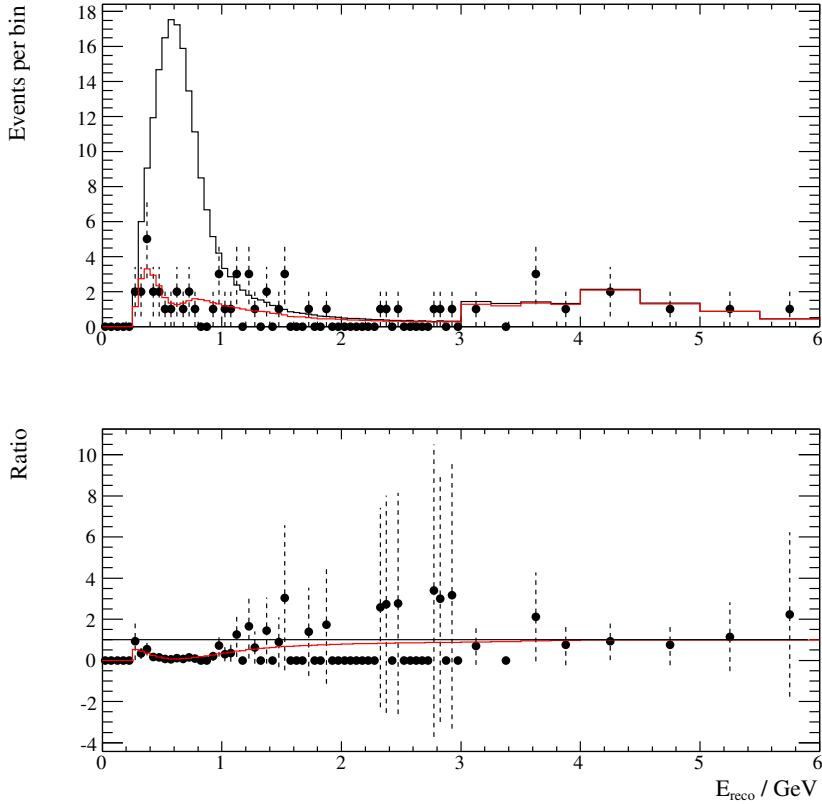


Figure 47: Best-fit reconstructed energy spectrum (top) obtained from the ‘2+N’ fit to the combined Run 1+2+3 dataset, assuming θ_{23} is in the second octant. The Run 1+2+3 dataset and the prediction obtained from the no-oscillation hypothesis are also shown. The spectra are shown using the 73 bins used in the fit (see Sec. 2.2.5). The ratio of the data and best-fit distribution to the no-oscillation hypothesis is shown in the bottom plot. The characteristic energy-dependent deficit can be clearly seen.

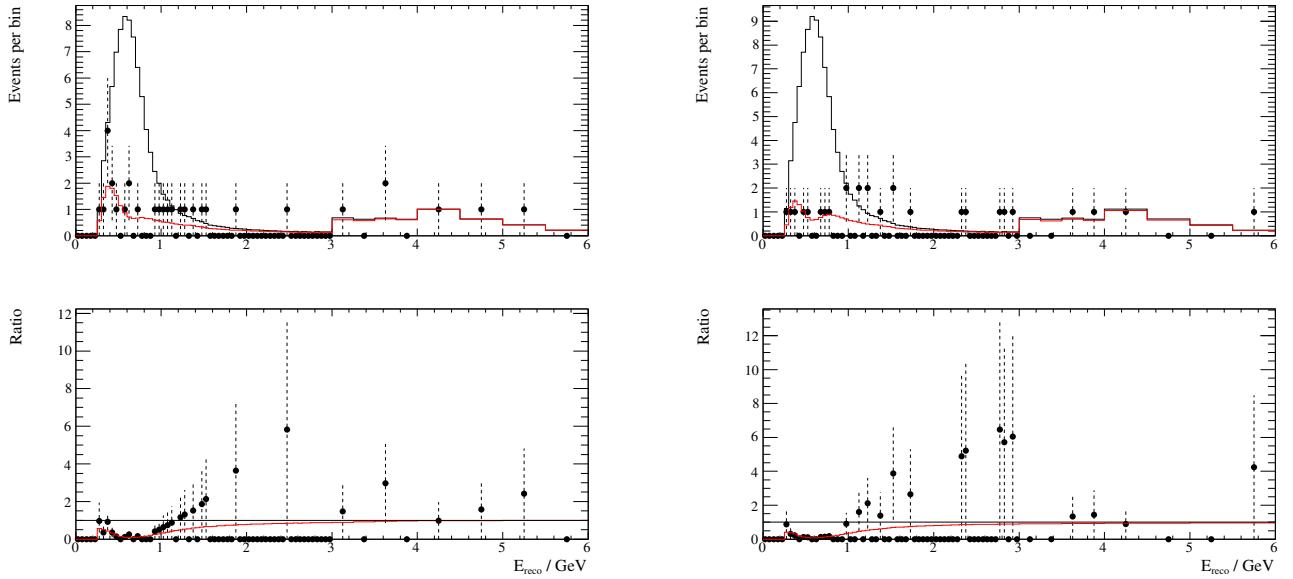


Figure 48: As in Fig. 46, but for the Run 1+2 dataset only.

Figure 49: As in Fig. 46, but for the Run 3 dataset only.

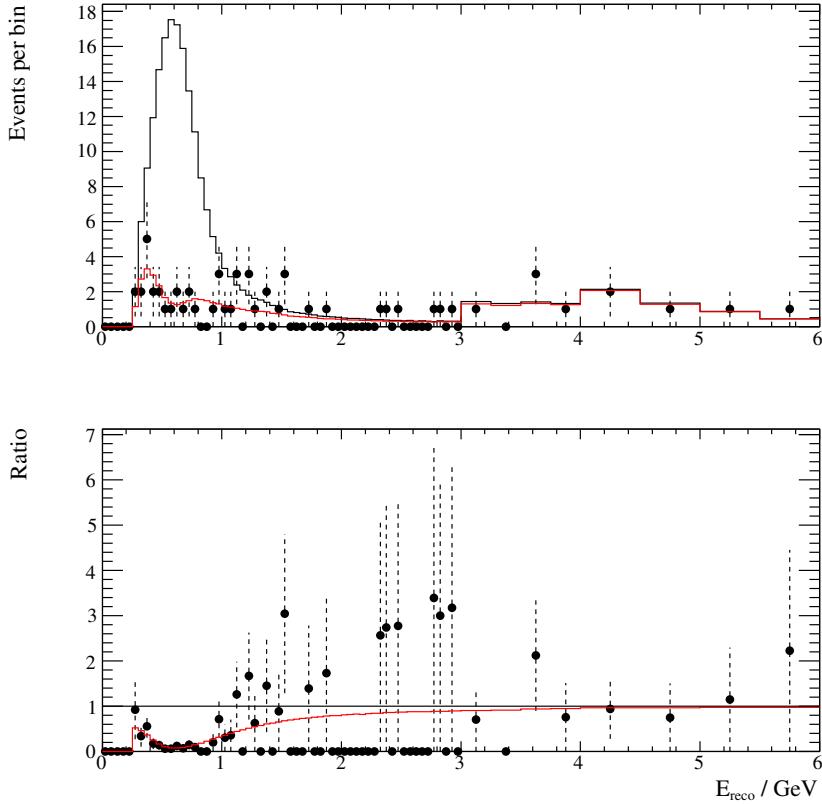


Figure 50: Best-fit reconstructed energy spectrum (top) obtained from the ‘2+8’ fit to the combined Run 1+2+3 dataset. The Run 1+2+3 dataset and the prediction obtained from the no-oscillation hypothesis are also shown. The spectra are shown using the 73 bins used in the fit (see Sec. 2.2.5). The ratio of the data and best-fit distribution to the no-oscillation hypothesis is shown in the bottom plot. The characteristic energy-dependent deficit can be clearly seen.

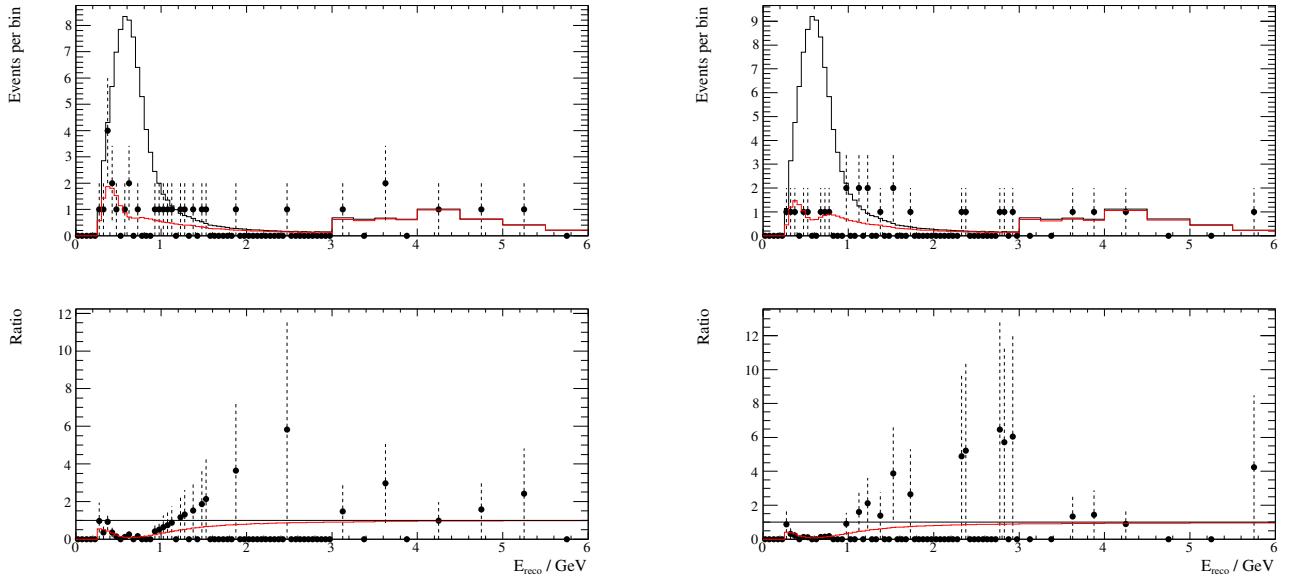


Figure 51: As in Fig. 50, but for the Run 1+2 dataset only.

Figure 52: As in Fig. 50, but for the Run 3 dataset only.

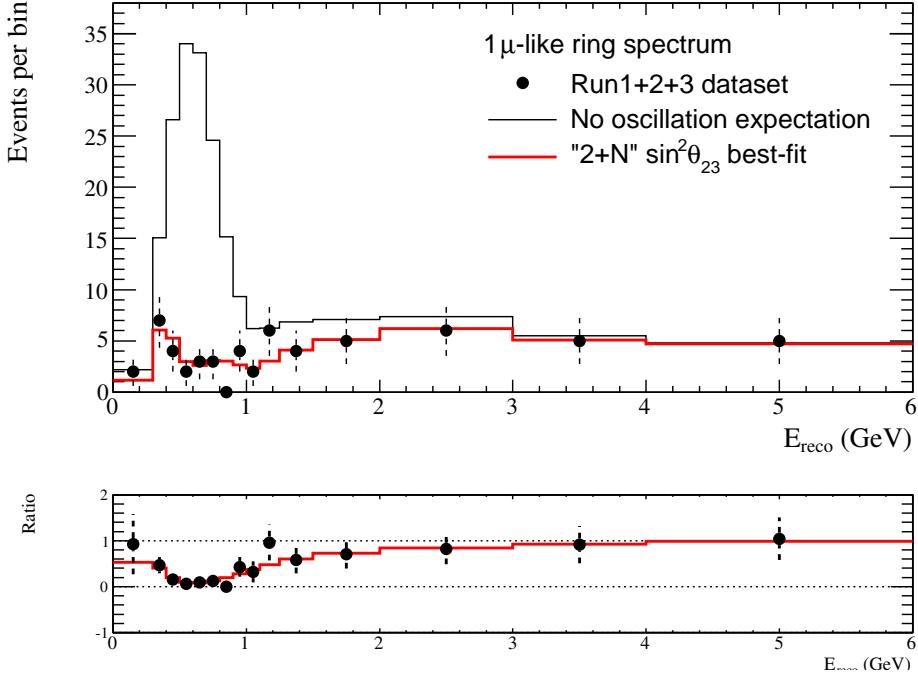


Figure 53: Best-fit reconstructed energy spectrum using the coarse binning scheme (see Sec. 5.3) obtained from the ‘2+N’ $\sin^2 \theta_{23}$ fit to the Run 1+2+3 dataset. Also shown are the spectrum obtained under the no-oscillation hypothesis and the ratios of the data and best-fit spectrum to it.

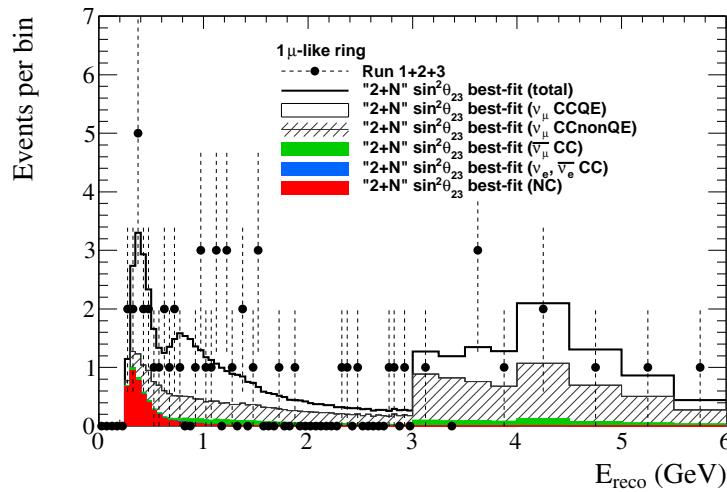


Figure 54: Best-fit reconstructed energy spectrum in the 73-bin scheme used in the fit (see Sec. 2.2.5) and its components obtained from the ‘2+N’ $\sin^2 \theta_{23}$ fit to the Run 1+2+3 dataset. The 28 components, each of which is calculated separately, are grouped into just 5 categories: ν_μ CCQE, ν_μ CCnQE, $\bar{\nu}_\mu$ CC, $\nu_e/\bar{\nu}_e$ CC and NC.

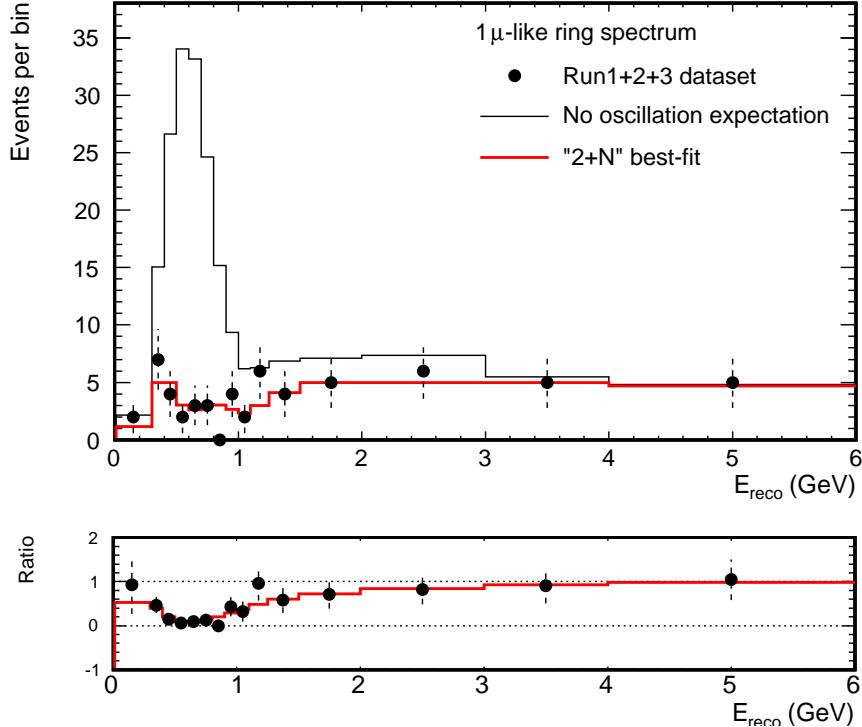


Figure 55: Best-fit reconstructed energy spectrum using the coarse binning scheme (see Sec. 5.3) obtained from the ‘2+N’ fit to the Run 1+2+3 dataset. Also shown are the spectrum obtained under the no-oscillation hypothesis and the ratios of the data and best-fit spectrum to it.

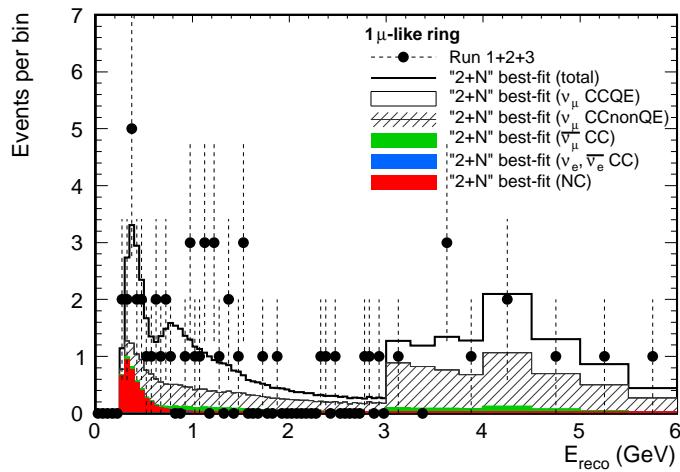


Figure 56: Best-fit reconstructed energy spectrum in the 73-bin scheme used in the fit (see Sec. 2.2.5) and its components obtained from the ‘2+N’ fit to the Run 1+2+3 dataset. The 28 components, each of which is calculated separately, are grouped into just 5 categories: ν_μ CCQE, ν_μ CCnonQE, ν_μ CC, $\nu_e/\bar{\nu}_e$ CC and NC.

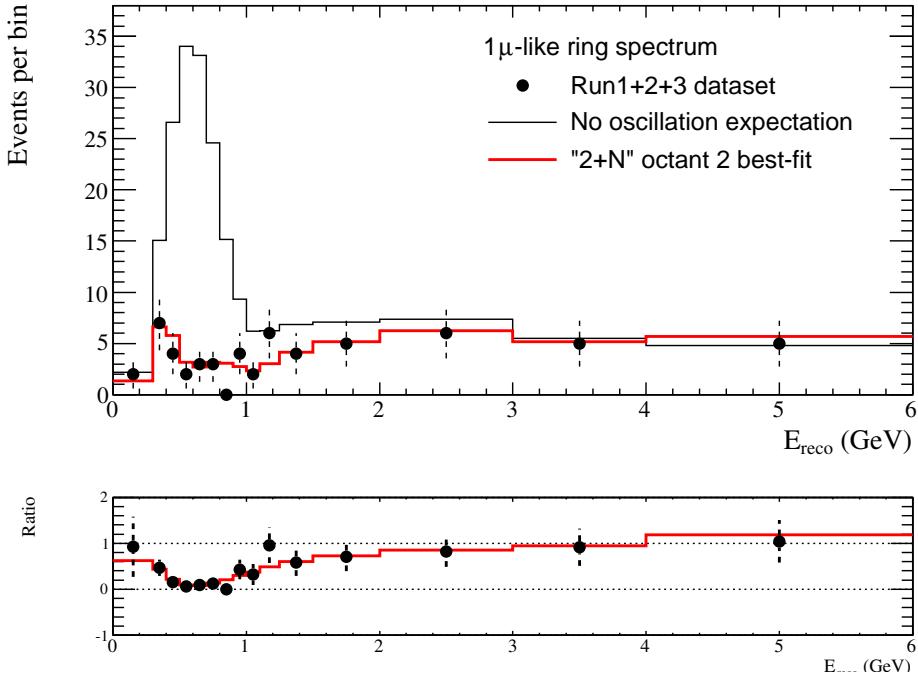


Figure 57: Best-fit reconstructed energy spectrum using the coarse binning scheme (see Sec. 5.3) obtained from the ‘2+N’ fit to the Run 1+2+3 dataset, assuming θ_{23} is in the second octant. Also shown are the spectrum obtained under the no-oscillation hypothesis and the ratios of the data and best-fit spectrum to it.

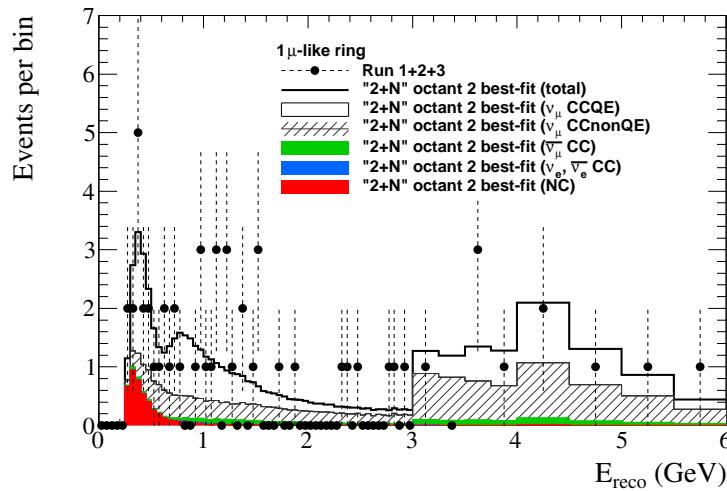


Figure 58: Best-fit reconstructed energy spectrum in the 73-bin scheme used in the fit (see Sec. 2.2.5) and its components obtained from the ‘2+N’ fit to the Run 1+2+3 dataset, assuming θ_{23} is in the the second octant. The 28 components, each of which is calculated separately, are grouped into just 5 categories: ν_μ CCQE, ν_μ CCnQE, $\bar{\nu}_\mu$ CC, $\nu_e/\bar{\nu}_e$ CC and NC.

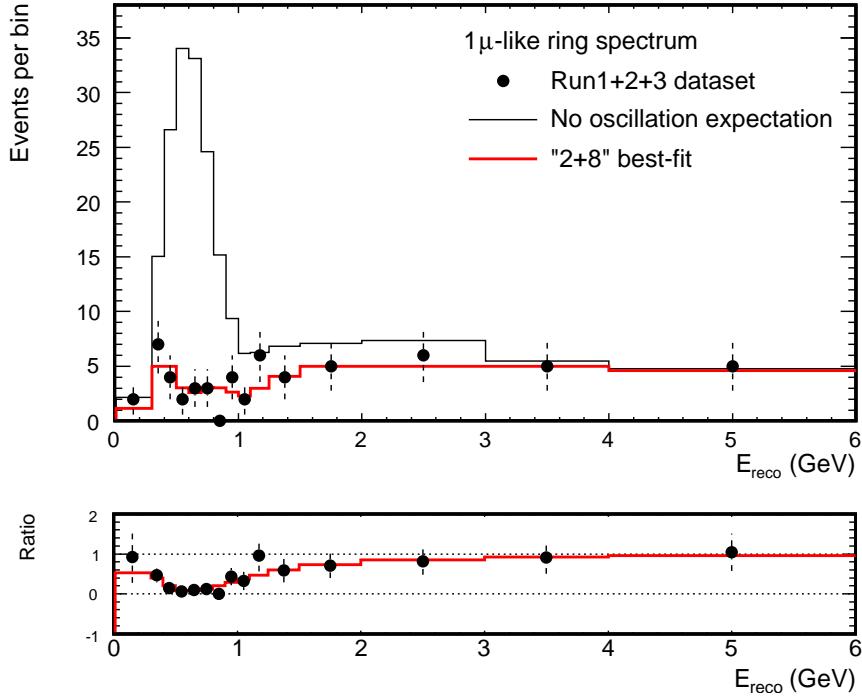


Figure 59: Best-fit reconstructed energy spectrum using the coarse binning scheme (see Sec. 5.3) obtained from the ‘2+8’ fit to the Run 1+2+3 dataset. Also shown are the spectrum obtained under the no-oscillation hypothesis and the ratios of the data and best-fit spectrum to it.

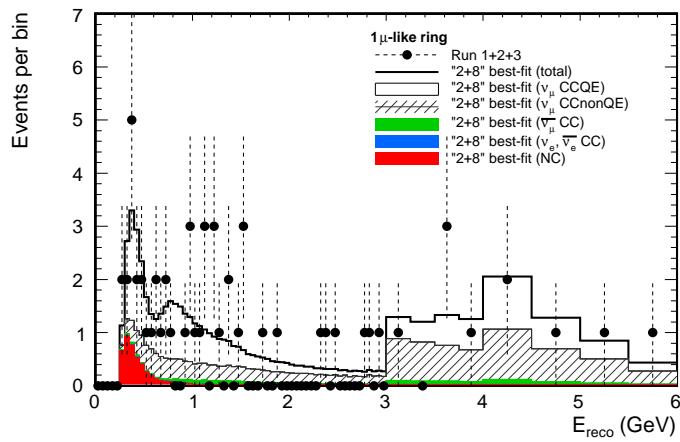


Figure 60: Best-fit reconstructed energy spectrum in the 73-bin scheme used in the fit (see Sec. 2.2.5) and its components obtained from the ‘2+8’ fit to the Run 1+2+3 dataset. The 28 components, each of which is calculated separately, are grouped into just 5 categories: ν_μ CCQE, ν_μ CCnQE, ν_μ CC, $\nu_e/\bar{\nu}_e$ CC and NC.

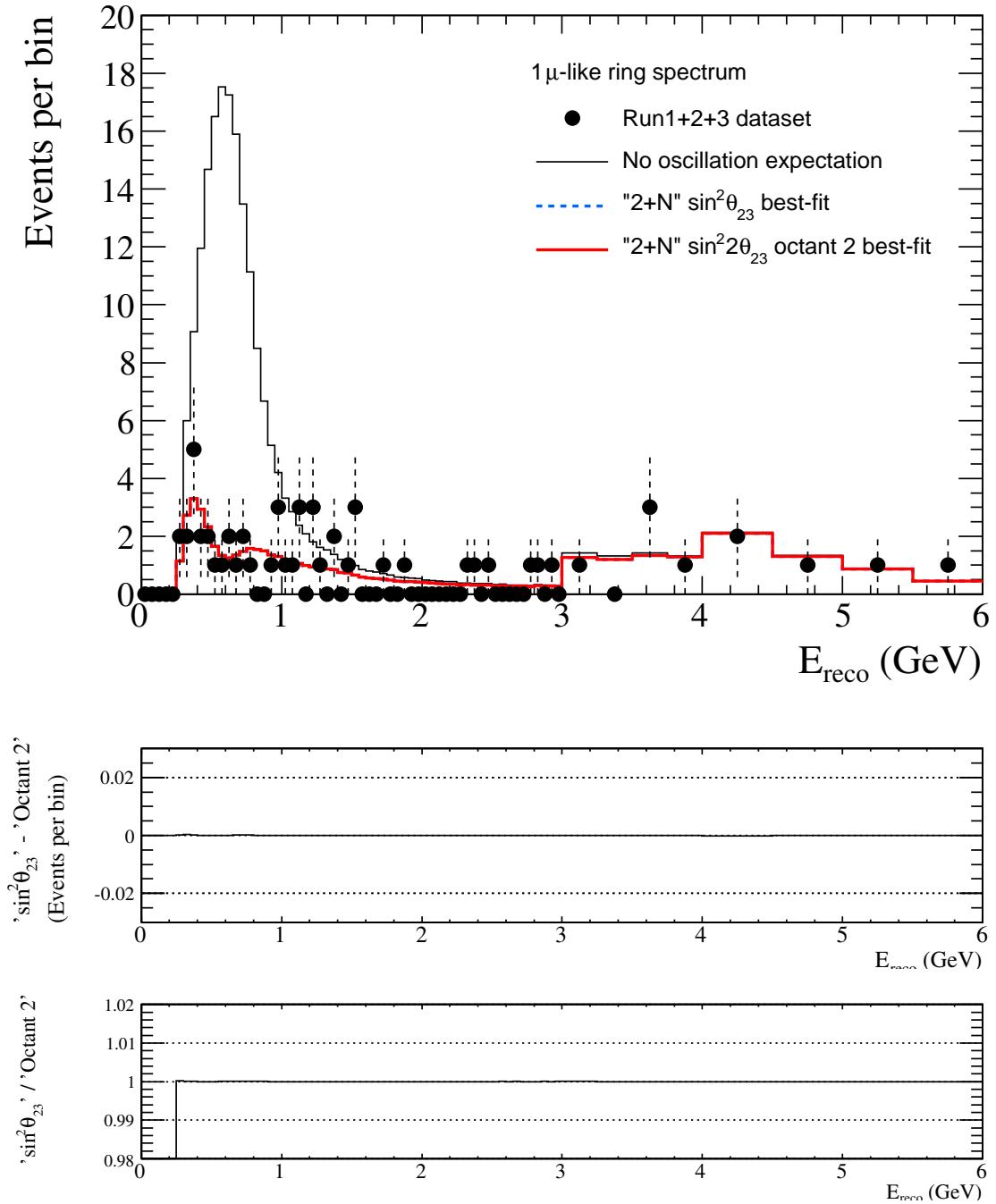


Figure 61: Comparison between best-fit reconstructed energy spectra obtained from the ‘2+N’ fits to the Run 1+2+3 datasets, for the $\sin^2 \theta_{23}$ fit, and the $\sin^2(2\theta_{23})$ fit assuming the second octant. The spectra are shown using the 73 bins used in the fit (see Sec. 2.2.5). Also shown are the absolute difference between the ‘ $\sin^2 \theta_{23}$ ’ and ‘ $\sin^2(2\theta_{23})$ ’ octant 2’ best-fit spectra and the ratio between them.

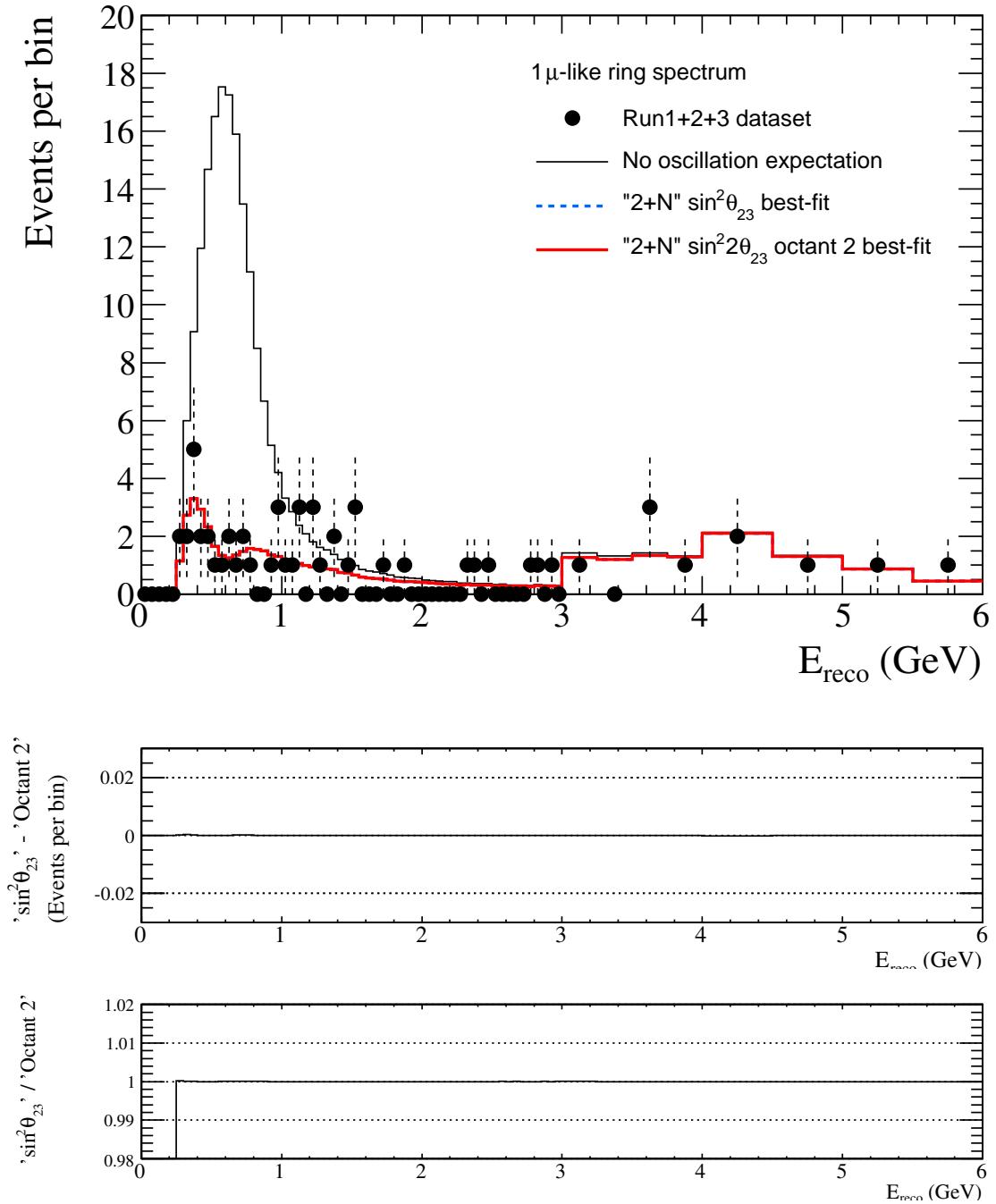


Figure 62: Comparison between best-fit reconstructed energy spectra obtained from the '2+N' fits to the Run 1+2+3 datasets, for the $\sin^2 \theta_{23}$ fit, and the $\sin^2(2\theta_{23})$ fit assuming the second octant. scheme (see Sec. 5.3). Also shown are the absolute difference between the ' $\sin^2 \theta_{23}$ ' and ' $\sin^2(2\theta_{23})$ octant 2' best-fit spectra and the ratio between them.

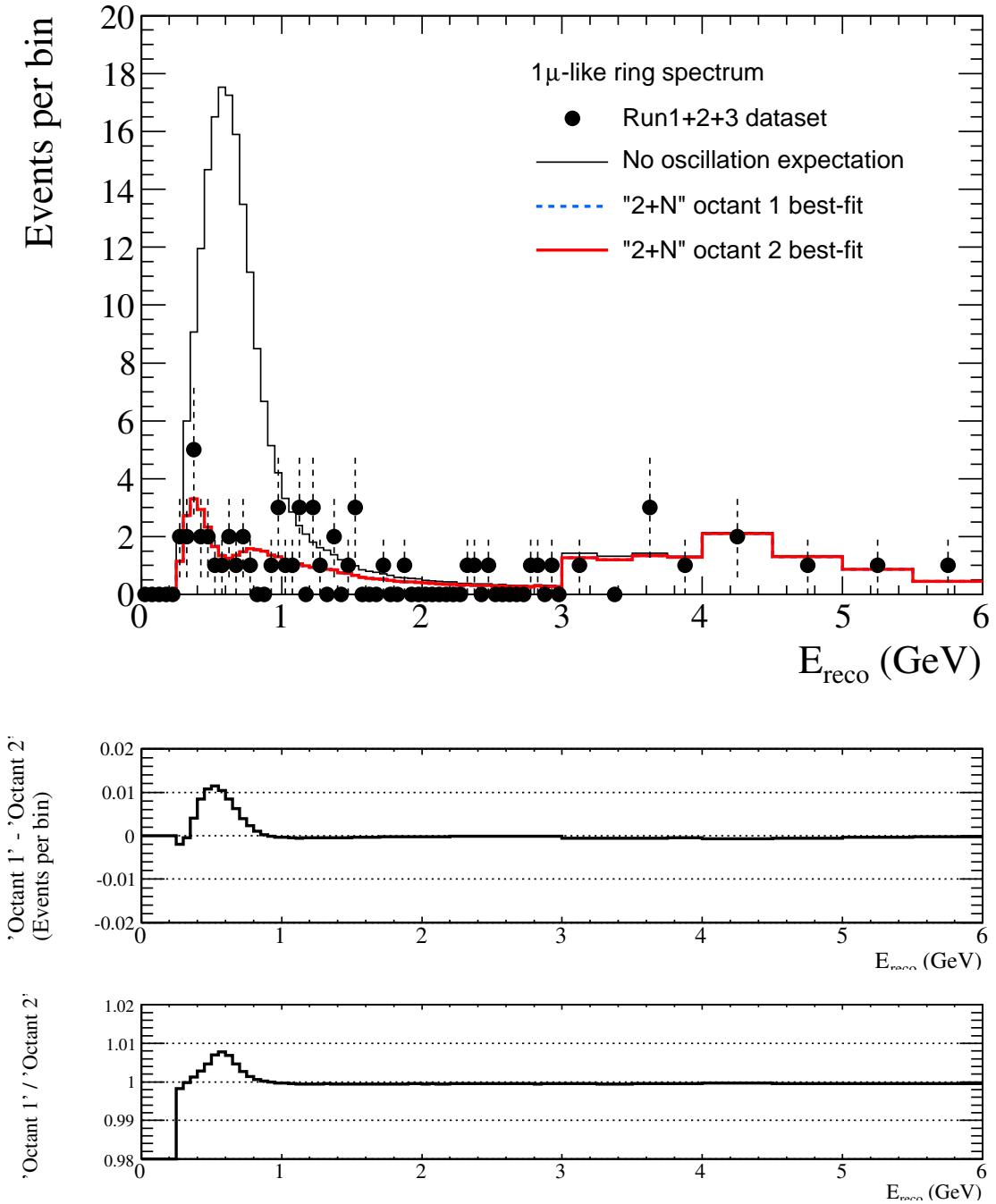


Figure 63: Comparison between best-fit reconstructed energy spectra obtained from the '2+N' fits to the Run 1+2+3 datasets, for both θ_{23} octant assumptions. The spectra are shown using the 73 bins used in the fit (see Sec. 2.2.5). Also shown are the absolute difference between the ' θ_{23} octant 1' and ' θ_{23} octant 2' best-fit spectra and the ratio between them.

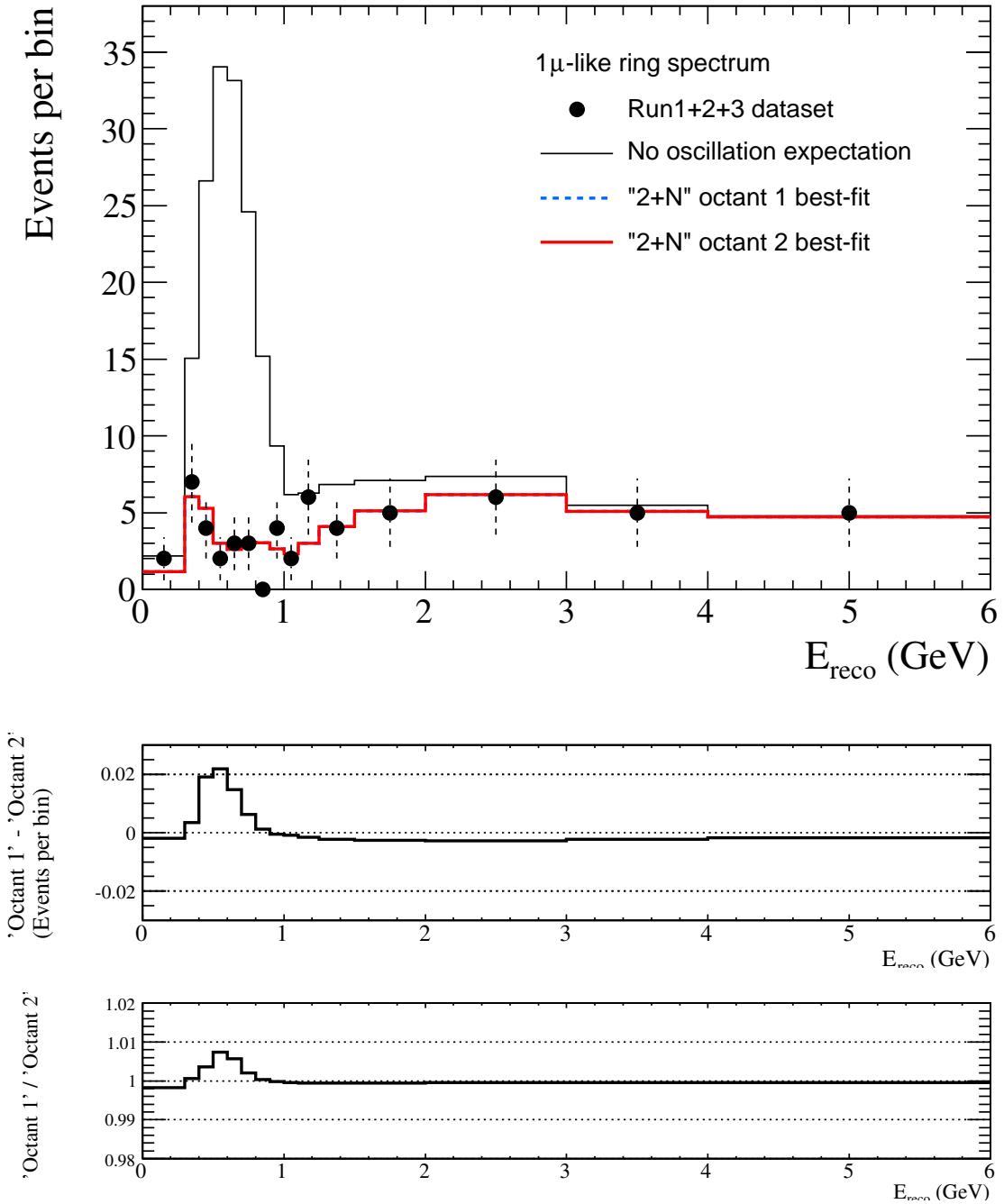


Figure 64: Comparison between best-fit reconstructed energy spectra obtained from the '2+N' fits to the Run 1+2+3 datasets, for both θ_{23} octant assumptions, using the coarse binning scheme (see Sec. 5.3). Also shown are the absolute difference between the ' θ_{23} octant 1' and ' θ_{23} octant 2' best-fit spectra and the ratio between them.

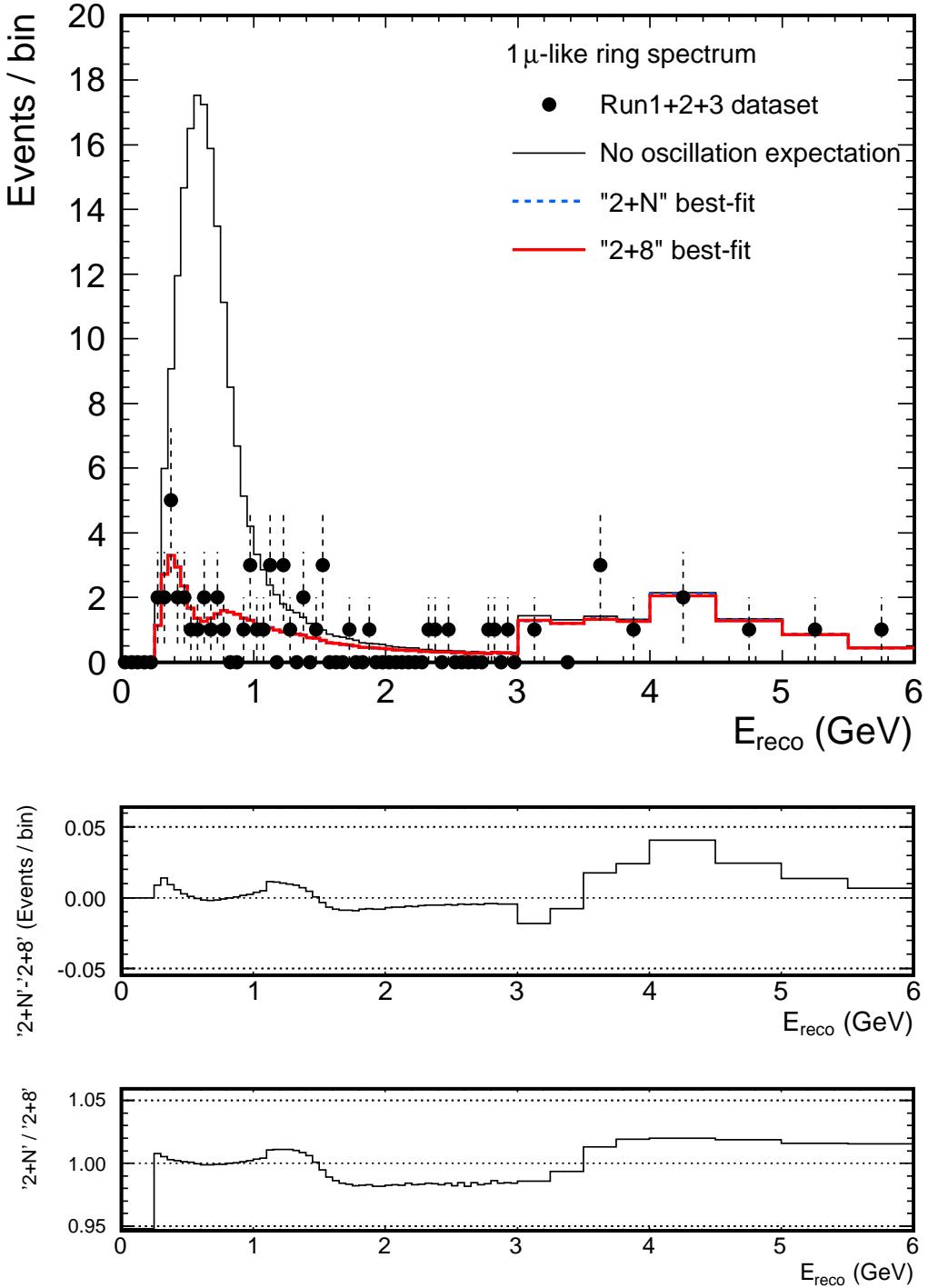


Figure 65: Comparison between best-fit reconstructed energy spectra obtained from the '2+N' and '2+8' fits to the Run 1+2+3 datasets. The spectra are shown using the 73 bins used in the fit (see Sec. 2.2.5). Also shown are the absolute difference between the '2+N' and '2+8' best-fit spectra and the ratio between them.

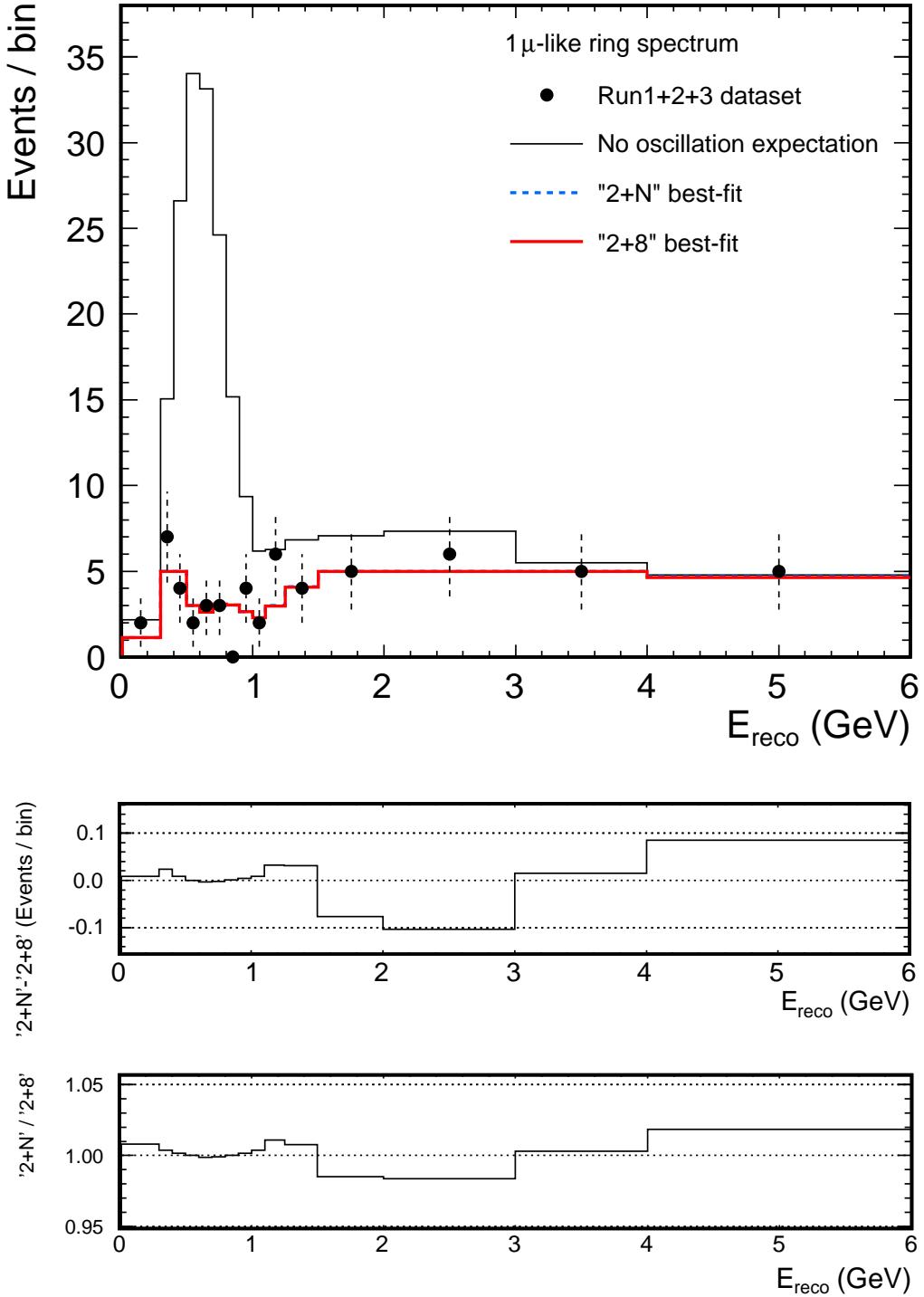


Figure 66: Comparison between best-fit reconstructed energy spectra obtained from the ‘2+N’ and ‘2+8’ fits to the Run 1+2+3 datasets using the coarse binning scheme (see Sec. 5.3). Also shown are the absolute difference between the ‘2+N’ and ‘2+8’ best-fit spectra and the ratio between them.

885 **5.4. Confidence limits**

886 The first step in calculating confidence limits for a single oscillation parameter is to calculate the values of $\Delta\chi^2$
 887 for each value of that oscillation parameter. For each value of $\sin^2 2\theta_{23}$, a ‘1+N’ fit is done with $|\Delta m_{32}^2|$ and all
 888 the systematic parameters allowed to float and $\sin^2 2\theta_{23}$ fixed. Then $\Delta\chi^2$ is calculated for that value of $\sin^2 2\theta_{23}$ by
 889 subtracting the ‘2+N’ best-fit value of χ^2 over the whole 2D oscillation parameter grid (which is listed in Tab. 14).
 890 The 68% and 90% confidence intervals in $\sin^2 2\theta_{23}$ are found using the constant- $\Delta\chi^2$ method, as described in Sec.
 891 4.5.1, and are given by the values for which χ^2 increases from the minimum by 1.00 and 2.71 respectively. Then this
 892 procedure is repeated for $|\Delta m_{32}^2|^{12}$.

893 The constant- $\Delta\chi^2$ method is used for the 1D confidence limits since there is a problem in using the Feldman-
 894 Cousins method. There is no obvious way of choosing the true value(s) of $|\Delta m_{32}^2|$ as inputs to the toy MC experiments
 895 to find the critical values of $\Delta\chi^2$ for the 1D confidence interval in $\sin^2 2\theta_{23}$. The same difficulty arises when choosing
 896 the true values of $\sin^2 2\theta_{23}$ to find the critical values of $\Delta\chi^2$ for the 1D confidence interval in $|\Delta m_{32}^2|$.

897 The $\Delta\chi^2$ distributions for $\sin^2 \theta_{23}$ and $|\Delta m_{32}^2|$ for the ‘1+N’ fit to the Run 1+2+3 dataset are shown in Figs.
 898 67 and 68 respectively, along with the 68% and 90% constant- $\Delta\chi^2$ critical values. These provide the 68% errors
 899 $\sin^2 \theta_{23} = 0.514 \pm 0.082$ and $|\Delta m_{32}^2| = 2.44^{+0.17}_{-0.15} \times 10^{-3} \text{ eV}^2/\text{c}^4$, and the limits of $0.397 < \sin^2 \theta_{23} < 0.630$ and
 900 $2.19 \times 10^{-3} \text{ eV}^2/\text{c}^4 < |\Delta m_{32}^2| < 2.72 \times 10^{-3} \text{ eV}^2/\text{c}^4$ at 90% C.L.

901 The $\Delta\chi^2$ distributions for $\sin^2 2\theta_{23}$ and $|\Delta m_{32}^2|$ for the ‘1+N’ fit to the Run 1+2+3 dataset are shown in Figs. 69
 902 and 70 respectively, along with the 68% and 90% constant- $\Delta\chi^2$ critical values. Results are shown for θ_{23} in both the
 903 first and second octants. For the first octant, these provide the 68% errors $\sin^2 2\theta_{23} = 1.000^{+0.000}_{-0.019}$ and $|\Delta m_{32}^2| =$
 904 $2.44^{+0.17}_{-0.15} \times 10^{-3} \text{ eV}^2/\text{c}^4$, and the limits of $\sin^2 2\theta_{23} > 0.958$ and $2.19 \times 10^{-3} \text{ eV}^2/\text{c}^4 < |\Delta m_{32}^2| < 2.72 \times 10^{-3} \text{ eV}^2/\text{c}^4$
 905 at 90% C.L. For the second octant, these provide the 68% errors $\sin^2 2\theta_{23} = 0.999^{+0.001}_{-0.036}$ and $|\Delta m_{32}^2| =$
 906 $2.44^{+0.17}_{-0.15} \times 10^{-3} \text{ eV}^2/\text{c}^4$, and the limits of $\sin^2 2\theta_{23} > 0.931$ and $2.19 \times 10^{-3} \text{ eV}^2/\text{c}^4 < |\Delta m_{32}^2| < 2.72 \times 10^{-3} \text{ eV}^2/\text{c}^4$
 907 at 90% C.L. The 1D limits for the second octant are identical to those for the first octant for $|\Delta m_{32}^2|$, but much wider
 908 for $\sin^2 2\theta_{23}$. This can be understood from Eq. 3 since the center of symmetry (point of maximal disappearance) is in
 909 the second octant.

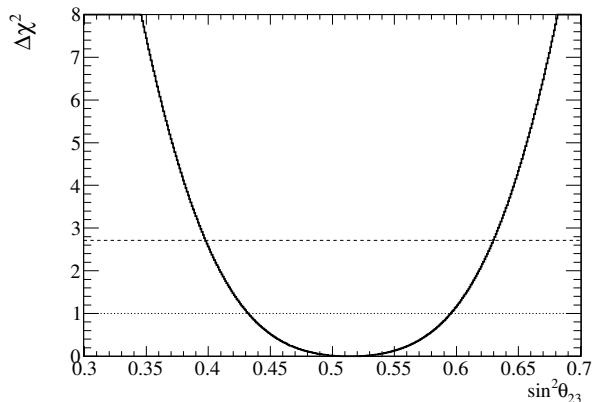


Figure 67: $\Delta\chi^2$ as a function of $\sin^2 \theta_{23}$ for the ‘1+N’ fit to the Run 1+2+3 dataset. The 68% and 90% constant- $\Delta\chi^2$ critical values are shown as dotted and dashed lines respectively.

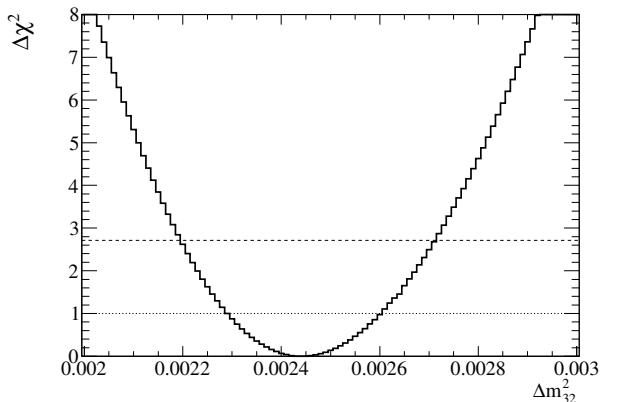


Figure 68: $\Delta\chi^2$ as a function of $|\Delta m_{32}^2|$ for the ‘1+N’ fit to the Run 1+2+3 dataset. The 68% and 90% constant- $\Delta\chi^2$ critical values are shown as dotted and dashed lines respectively.

¹²The procedure is equivalent for the limits with $\sin^2 \theta_{23}$, just with a different fit parameter.

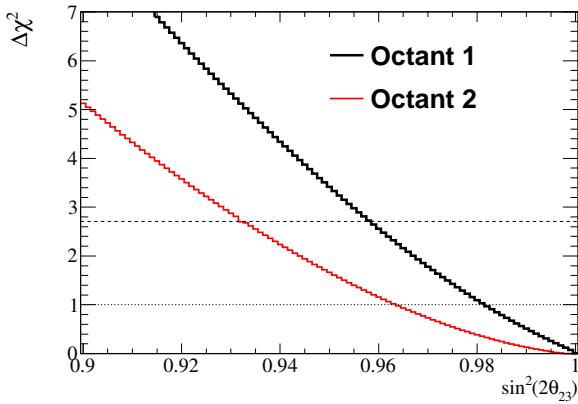


Figure 69: $\Delta\chi^2$ as a function of $\sin^2 2\theta_{23}$ for the '1+N' fit to the Run 1+2+3 dataset. Results are shown for θ_{23} in for both octants. The 68% and 90% constant- $\Delta\chi^2$ critical values are shown as dotted and dashed lines respectively.

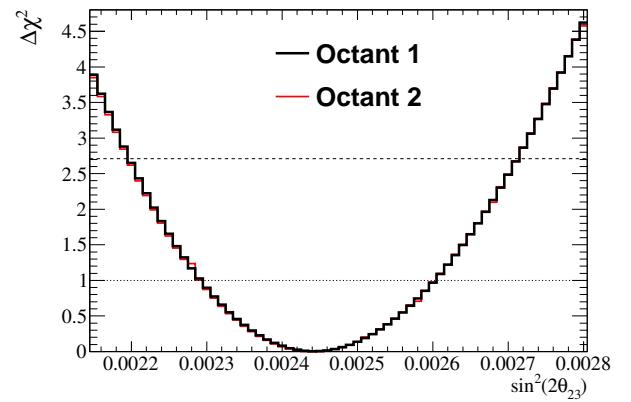


Figure 70: $\Delta\chi^2$ as a function of $|\Delta m_{32}^2|$ for the '1+N' fit to the Run 1+2+3 dataset. Results are shown for θ_{23} in both octants. The 68% and 90% constant- $\Delta\chi^2$ critical values are shown as dotted and dashed lines respectively.

910 5.5. Confidence regions

911 The first step in constructing confidence contours in the oscillation parameters $\sin^2 2\theta_{23}$ and $|\Delta m_{32}^2|$ is to calculate
 912 the values of $\Delta\chi^2$ for each point in a 2-dimensional grid in the oscillation parameter space. This is done as described
 913 in Sec. 4.5.1 for the constant- $\Delta\chi^2$ method and in Sec. 4.5.2 for the Feldman-Cousins method.

914 The $\Delta\chi^2$ surface for the the ‘2+N’ fit for $\sin^2 \theta_{23}$ to the Run 1+2+3 dataset is shown in Fig. 71, as a function of
 915 $\sin^2 \theta_{23}$ and $|\Delta m_{32}^2|$.

916 The $\Delta\chi^2$ surface for the the ‘2+N’ fit to the Run 1+2+3 dataset is shown in Figs. 72 and 73 for θ_{23} in the first and
 917 second octants respectively, as a function of $\sin^2 2\theta_{23}$ and $|\Delta m_{32}^2|$. For comparison, the corresponding $\Delta\chi^2$ surfaces
 918 for the ‘2+N’ fits to the Run 1+2 and Run 3 datasets are shown in Figs. 74 and 75 respectively. The same $\Delta\chi^2$ range
 919 is used in all colour plots to allow comparison. Marginalized $\Delta\chi^2$ distributions are also shown as a function of either
 920 $\sin^2 2\theta_{23}$ or $|\Delta m_{32}^2|$ for the ‘2+N’ fits to the Run 1+2+3, Run 1+2 and Run 3 datasets in Figs. 76 and 77 respectively.

921 The corresponding plots for the ‘2+8’ fits are shown in Fig. 78 for the Run 1+2+3 datset, Fig. 79 for the Run 1+2
 922 dataset and Fig. 80 for the Run 3 dataset. Meanwhile the marginalized $\Delta\chi^2$ distributions are shown for all the datasets
 923 as a function of $\sin^2 2\theta_{23}$ in Fig. 82 and as a function of $|\Delta m_{32}^2|$ in Fig. 81.

924 Comparisons were made between the ‘2+N’ $\Delta\chi^2$ distributions for θ_{23} in the first and second octants. The fractional
 925 difference between the $\Delta\chi^2$ surfaces obtained from the ‘2+N’ fits, assuming the first and second octant, to the Run
 926 1+2+3 dataset is shown in Fig. 83.

927 Comparisons were made between the ‘2+N’ and ‘2+8’ $\Delta\chi^2$ distributions. The fractional difference between the
 928 $\Delta\chi^2$ surfaces obtained from the ‘2+N’ and ‘2+8’ fits to the Run 1+2+3 dataset is shown in Fig. 84. The marginalized
 929 $\Delta\chi^2$ distributions for the ‘2+N’ and ‘2+8’ fits to the Run 1+2+3 dataset are compared as a function of $|\Delta m_{32}^2|$ in
 930 Fig. 86 and as a function of $\sin^2 2\theta_{23}$ in Fig. 87. As shown in these figures, the ‘2+N’ and ‘2+8’ marginalized $\Delta\chi^2$
 931 distributions are almost identical, even in areas of the parameter space that exceed the 99% CL region ($\Delta\chi^2 < 6.63$
 932 for a single parameter).

933 Confidence regions were constructed using both the constant- $\Delta\chi^2$ method described in Sec. 4.5.1 and the Feldman-
 934 Cousins method described in Sec. 4.5.2 for both the ‘2+N’ and the ‘2+8’ fits. Confidence contours were drawn using the
 935 constant- $\Delta\chi^2$ method for each of the Run 1+2+3, Run 1+2 and Run 3 datasets. Using the Feldman-Cousins method,
 936 however, they were drawn only for the Run 1+2+3 dataset due to the large amount of CPU time needed. All confidence
 937 regions presented below include the effect of systematic uncertainties.

938 The 68% and 90% CL regions for the ‘2+N’ $\sin^2 \theta_{23}$ fit to the Run 1+2+3 dataset are shown using the constant-
 939 $\Delta\chi^2$ method in Fig. 88. The corresponding constant- $\Delta\chi^2$ contours for the Run 1+2+3 dataset (assuming θ_{23} is in the
 940 first octant), the Run 1+2+3 dataset (assuming θ_{23} is in the second octant), and the Run 1+2 and Run 3 datasets are
 941 shown in Figs. 89, 90, 91 and 92 respectively. The constant- $\Delta\chi^2$ contours for the ‘2+8’ fits are shown in Fig. 93 for
 942 Run 1+2+3, in Fig. 94 for Run 1+2 and in Fig. 95 for Run 3.

943 The Feldman-Cousins 68% and 90% CL regions for the fits to the Run 1+2+3 dataset are shown in Fig. 96 for the
 944 ‘2+N’ fit (assuming θ_{23} is in the first octant), in Fig. 97 for the ‘2+N’ fit (assuming θ_{23} is in the second octant), and in
 945 Fig. 98 for the ‘2+8’ fit. The boundary of the 68% ‘2+N’ contour assuming θ_{23} is in the first octant includes the points
 946 $(\sin^2(2\theta_{23}), |\Delta m_{32}^2|) = (1.000, 2.64 \times 10^{-3} \text{ eV}^2/\text{c}^4), (0.964, 2.50 \times 10^{-3} \text{ eV}^2/\text{c}^4)$ and $(1.000, 2.26 \times 10^{-3} \text{ eV}^2/\text{c}^4)$.

947 We have accomplished our goal, which was to present the confidence regions constructed using various methods,
 948 and for different fits and datasets. In the next section, detailed comparisons are presented of the confidence regions
 949 obtained using different construction methods for the same fit, and using different fitting methods for the same con-
 950 struction method. The contours from different running periods are compared, and we also compare our contours from
 951 the fits to the combined Run 1+2+3 dataset with recent measurements from MINOS and SuperK and T2K 3.010×10^{20} -
 952 POT sensitivity contours. Finally, a more critical view of the 5 different results obtained by this analysis is presented
 953 in Sec. 5.7.

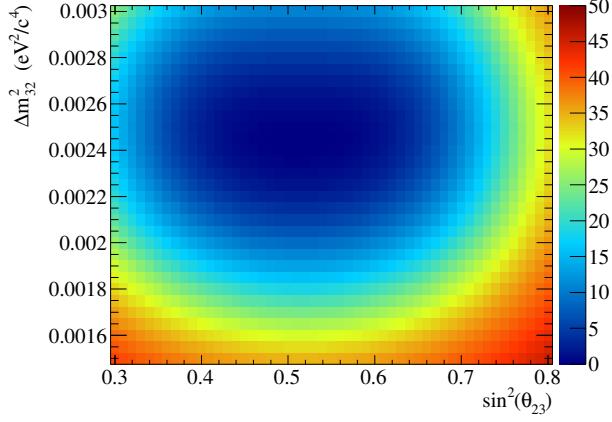


Figure 71: $\Delta\chi^2$ surface for the ‘2+N’ $\sin^2 \theta_{23}$ fit to the Run 1+2+3 dataset.

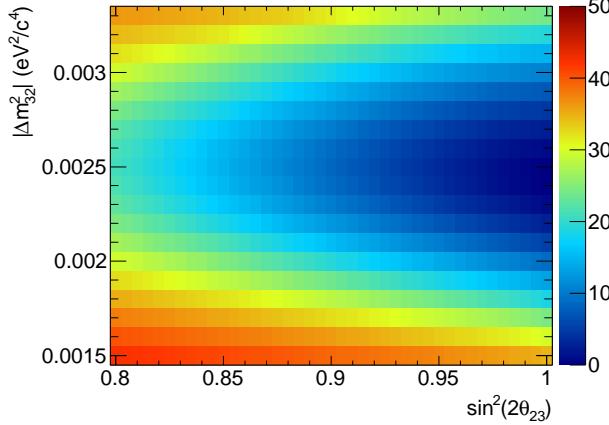


Figure 72: $\Delta\chi^2$ surface for the ‘2+N’ fit to the Run 1+2+3 dataset, assuming θ_{23} is in the first octant.

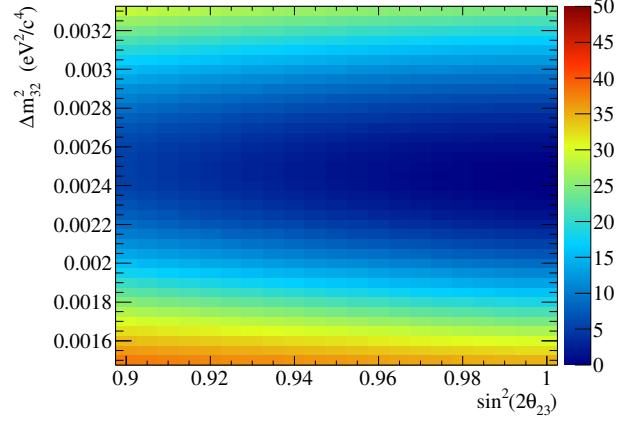


Figure 73: $\Delta\chi^2$ surface for the ‘2+N’ fit to the Run 1+2+3 dataset, assuming θ_{23} is in the second octant.

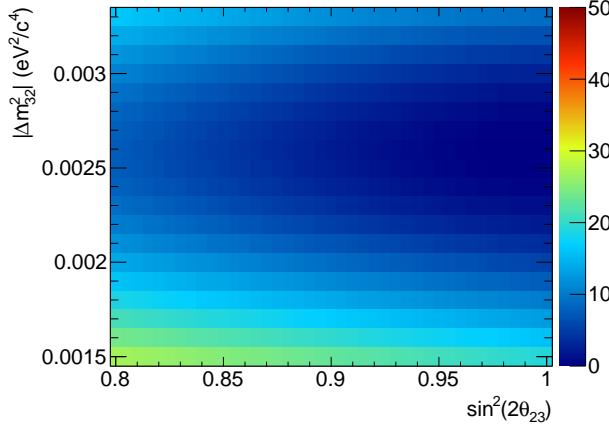


Figure 74: $\Delta\chi^2$ surface for the ‘2+N’ fit to the Run 1+2 dataset.

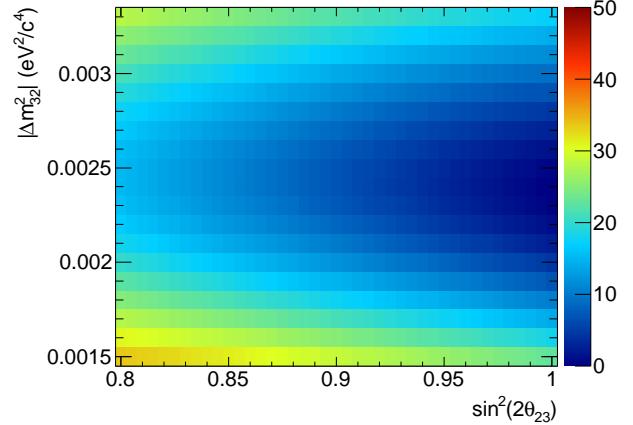


Figure 75: $\Delta\chi^2$ surface for the ‘2+N’ fit to the Run 3 dataset.

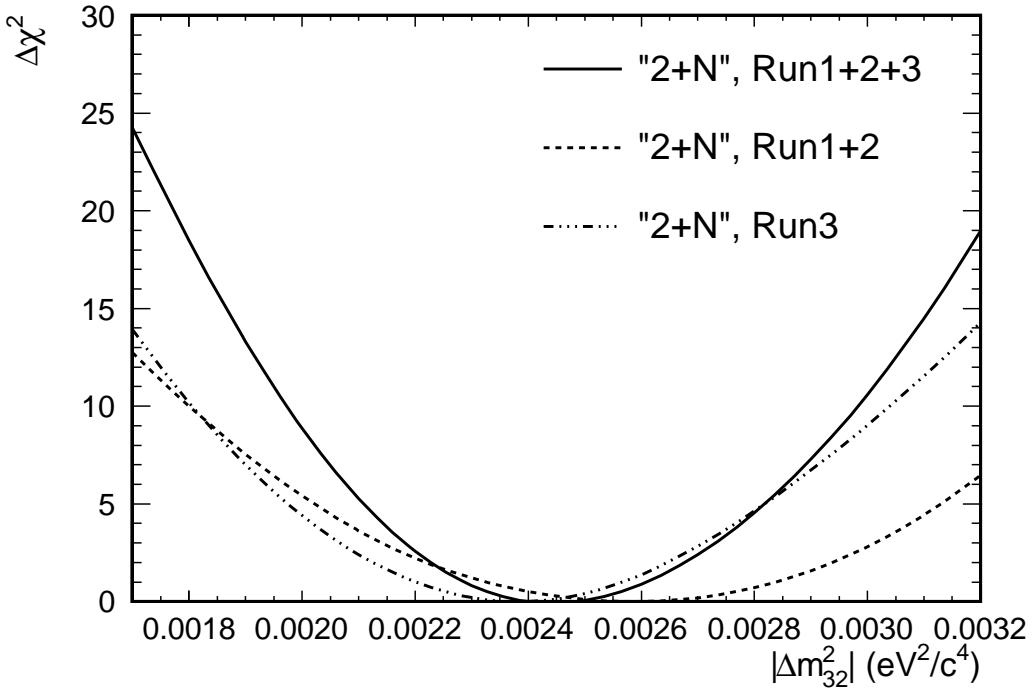


Figure 76: Marginalized $\Delta\chi^2$, as a function of $|\Delta m_{32}^2|$, for the four '2+N' fits to the Run 1+2+3, Run 1+2 and Run 3 datasets.

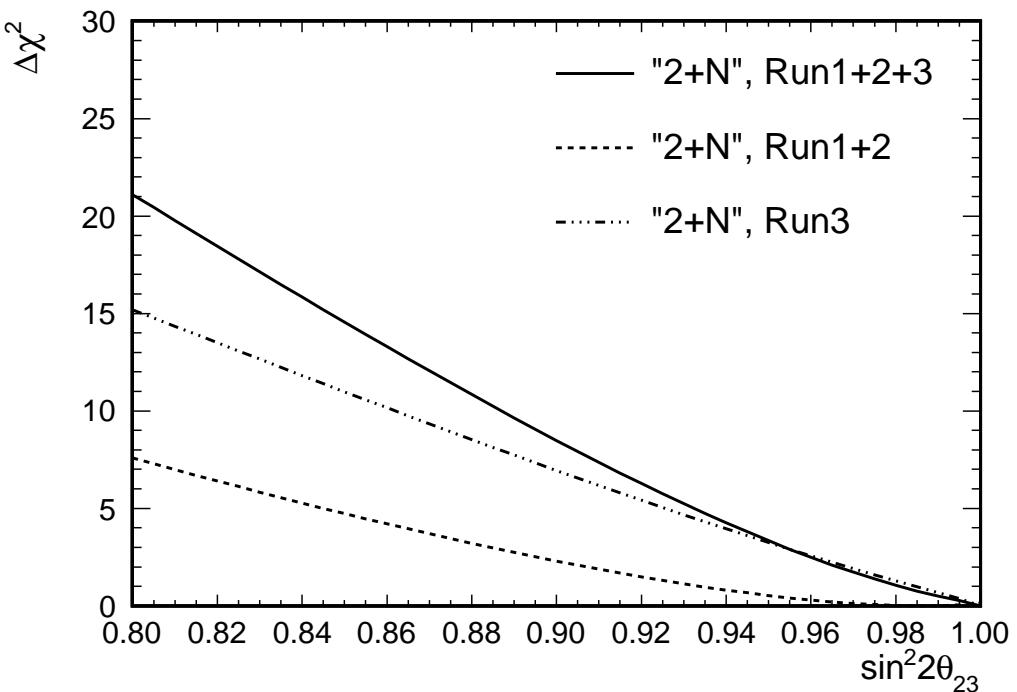


Figure 77: Marginalized $\Delta\chi^2$, as a function of $\sin^2 2\theta_{23}$, for the three '2+N' fits to the Run 1+2+3, Run 1+2 and Run 3 datasets.

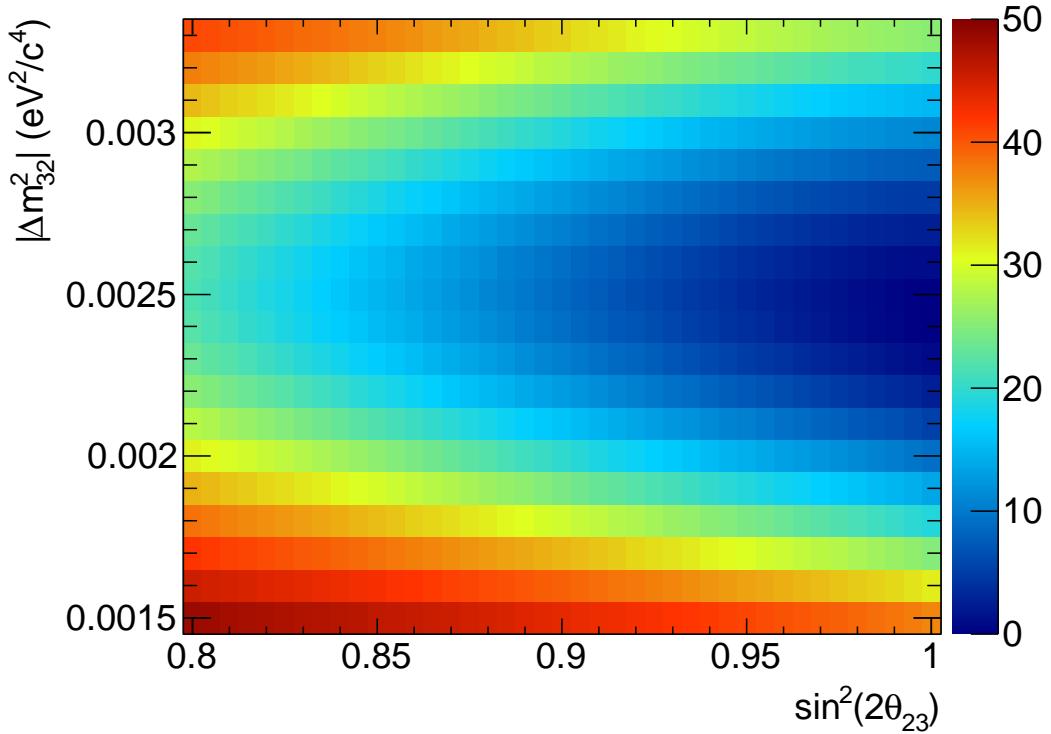


Figure 78: $\Delta\chi^2$ surface for the ‘2+8’ fit to the Run 1+2+3 dataset.

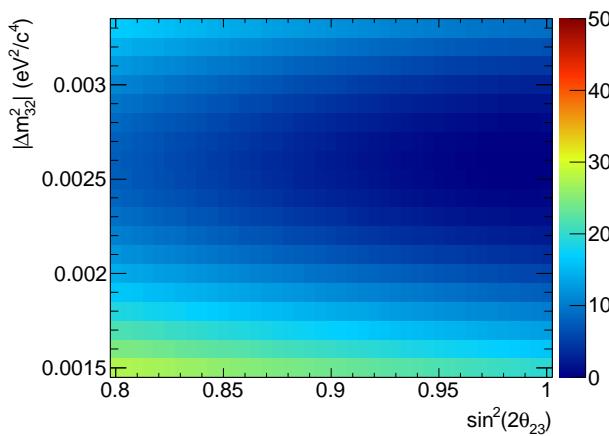


Figure 79: $\Delta\chi^2$ surface for the ‘2+8’ fit to the Run 1+2 dataset.

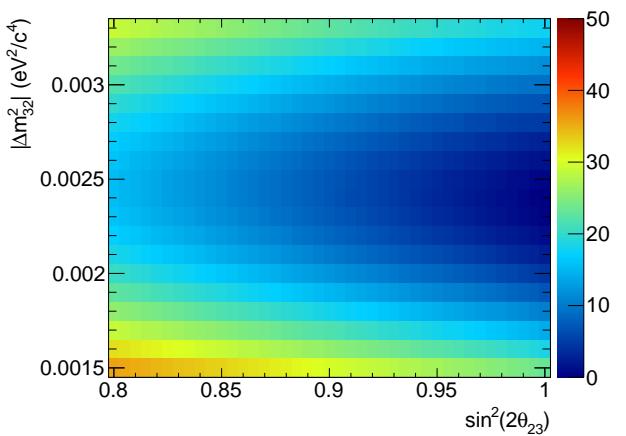


Figure 80: $\Delta\chi^2$ surface for the ‘2+8’ fit to the Run 3 dataset.

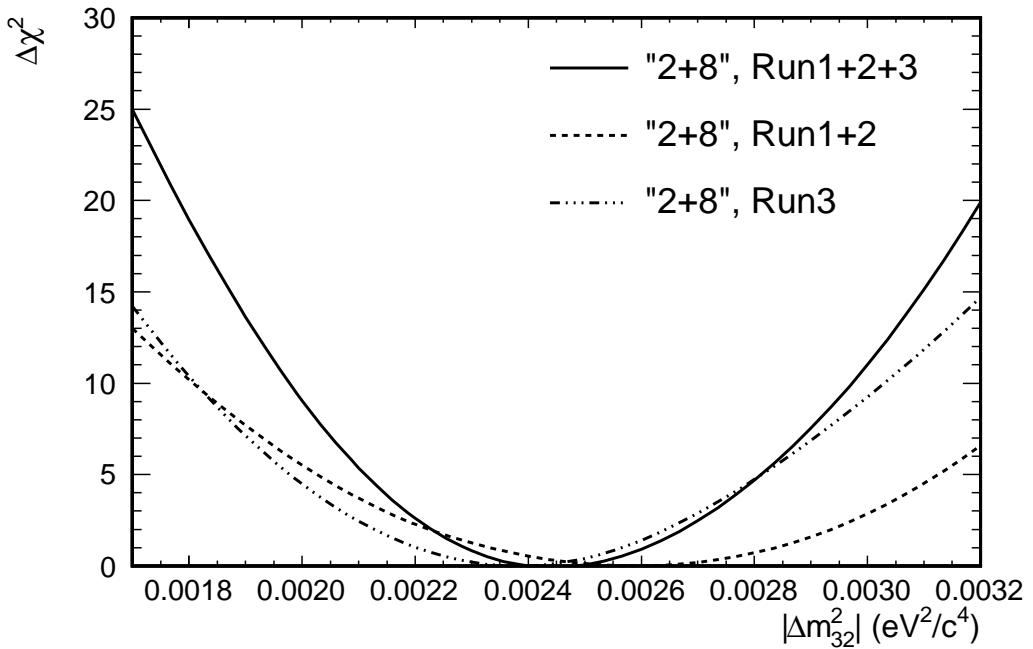


Figure 81: Marginalized $\Delta\chi^2$, as a function of $|\Delta m_{32}^2|$, for the three '2+8' fits to the Run 1+2+3, Run 1+2 and Run 3 datasets.

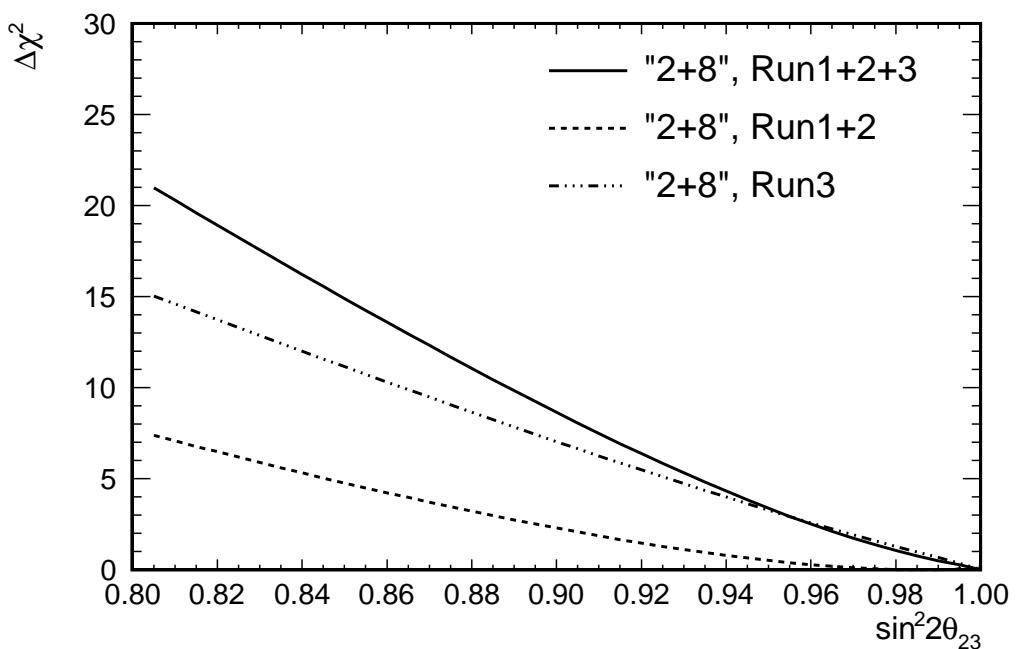


Figure 82: Marginalized $\Delta\chi^2$, as a function of $\sin^2 2\theta_{23}$, for the three '2+8' fits to the Run 1+2+3, Run 1+2 and Run 3 datasets.

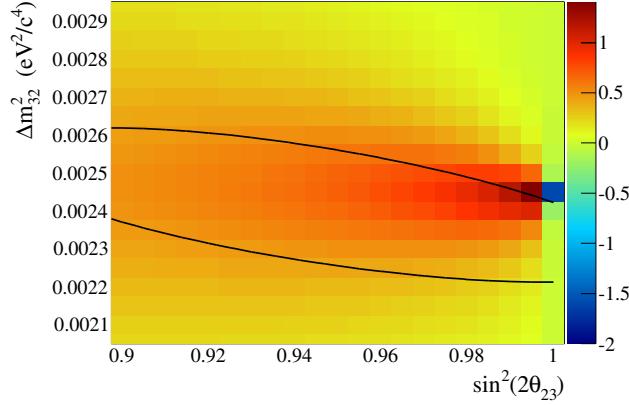


Figure 83: Fractional difference between the $\Delta\chi^2$ surfaces obtained from the ‘2+N’ fits to the Run 1+2+3 dataset assuming θ_{23} is in the first and second octants and shown in Figs. 72 and 73. The fractional difference is calculated as $2 \times (\Delta\chi^2(\text{octant 1}) - \Delta\chi^2(\text{octant 2})) / \Delta\chi^2(\text{octant 1}) + \Delta\chi^2(\text{octant 2})$. The 2012 MINOS 90% CL region is shown for reference. The large difference at the minimum of the $\Delta\chi^2$ maps is due to the best fit point in the second octant case being further away from a bin center.

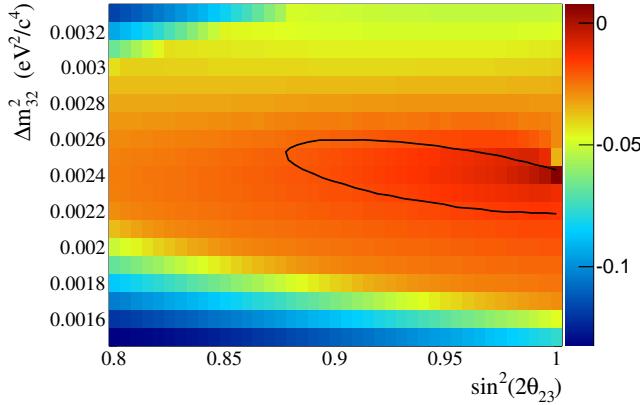


Figure 84: Fractional difference between the $\Delta\chi^2$ surfaces obtained from the ‘2+N’ and ‘2+8’ fits to the Run 1+2+3 dataset and shown in Figs. 72 and 78. The fractional difference is calculated as $2 \times (\Delta\chi^2(\text{'2+N'}) - \Delta\chi^2(\text{'2+8'})) / \Delta\chi^2(\text{'2+N'}) + \Delta\chi^2(\text{'2+8'})$. The 2012 MINOS 90% CL region is shown for reference.

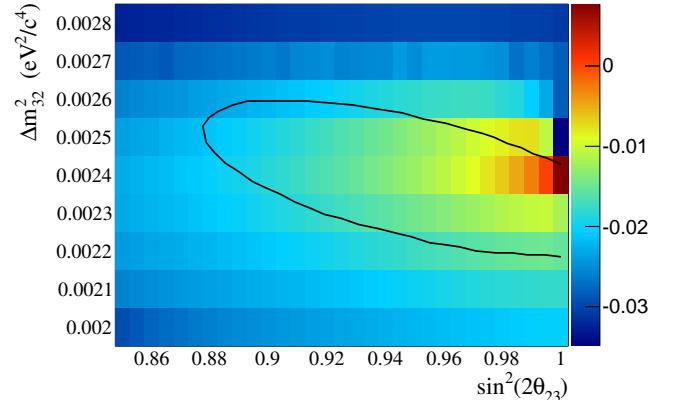


Figure 85: As on the left but zoomed into the area of the 2012 MINOS 90% CL region.

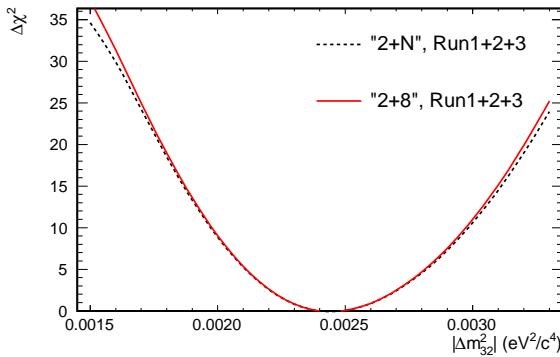


Figure 86: Comparison of marginalized $\Delta\chi^2$ as a function of $|\Delta m_{32}^2|$, for the ‘2+N’ and ‘2+8’ fits to the Run 1+2+3 dataset.

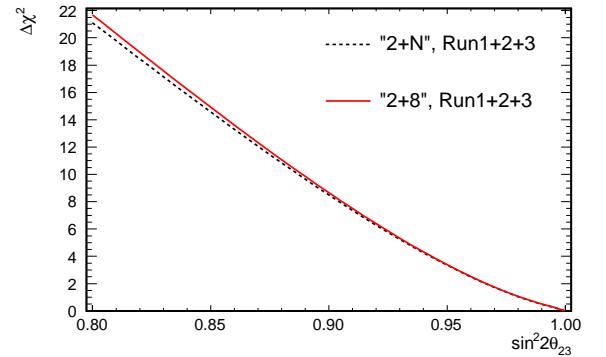


Figure 87: Comparison of marginalized $\Delta\chi^2$ as a function of $\sin^2 2\theta_{23}$, for the ‘2+N’ and ‘2+8’ fits to the Run 1+2+3 dataset.

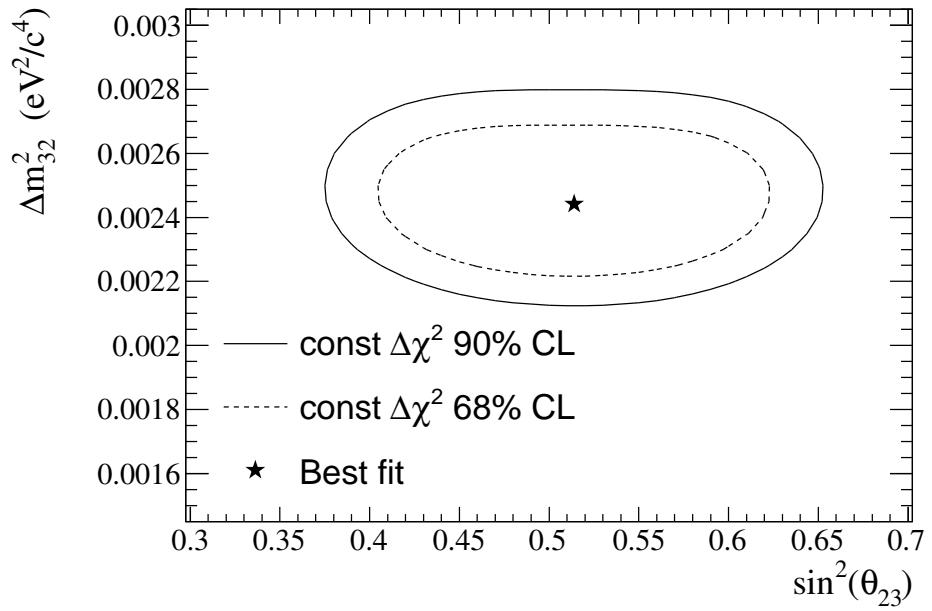


Figure 88: 68% CL and 90% CL allowed region (including systematics), constructed with the constant- $\Delta\chi^2$ method, for the ‘2+N’ $\sin^2\theta_{23}$ fit to the Run 1+2+3 dataset. The ‘2+N’ best-fit point is also shown.

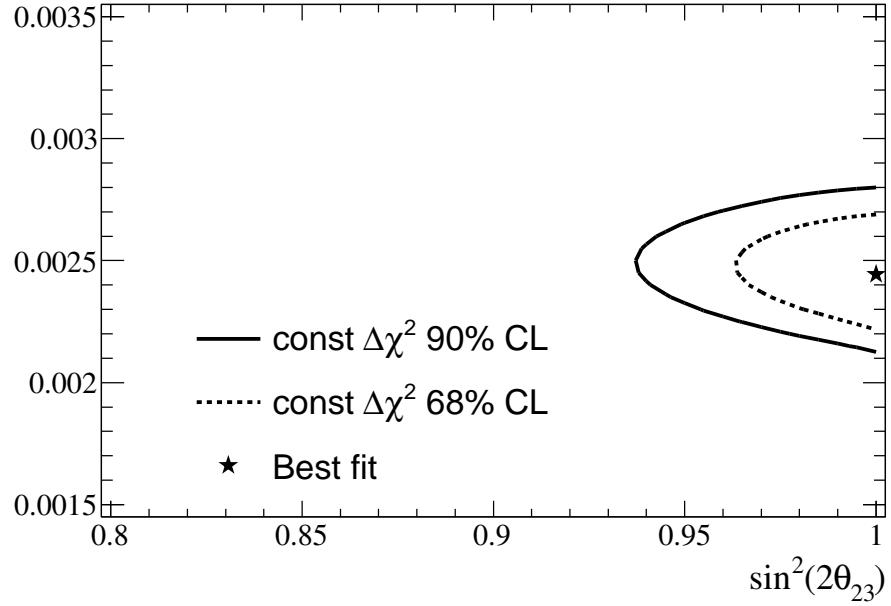


Figure 89: 68% CL and 90% CL allowed region (including systematics), constructed with the constant- $\Delta\chi^2$ method, for the ‘2+N’ fit to the Run 1+2+3 dataset assuming θ_{23} is in the first octant. The ‘2+N’ best-fit point is also shown.

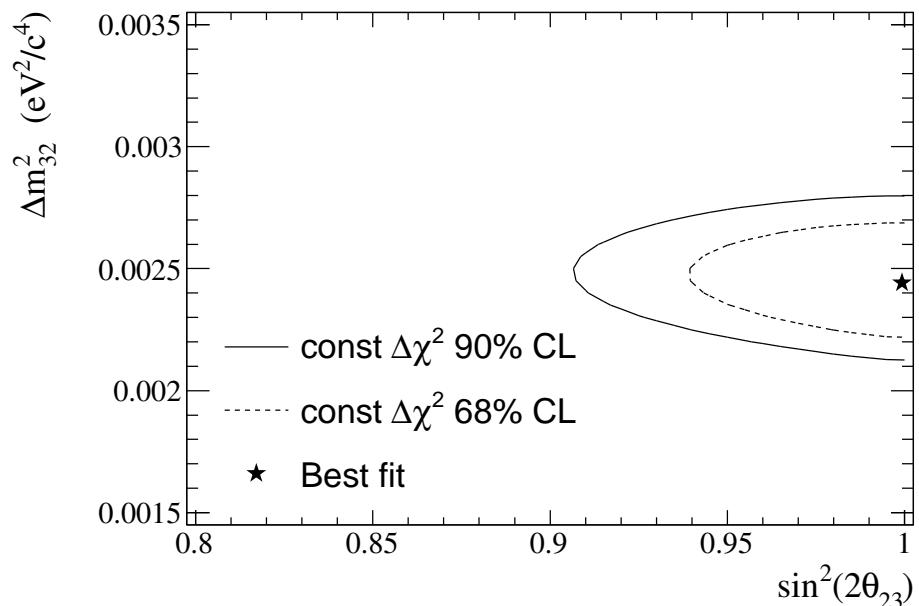


Figure 90: 68% CL and 90% CL allowed region (including systematics), constructed with the constant- $\Delta\chi^2$ method, for the ‘2+N’ fit to the Run 1+2+3 dataset assuming θ_{23} is in the second octant. The ‘2+N’ best-fit point is also shown.

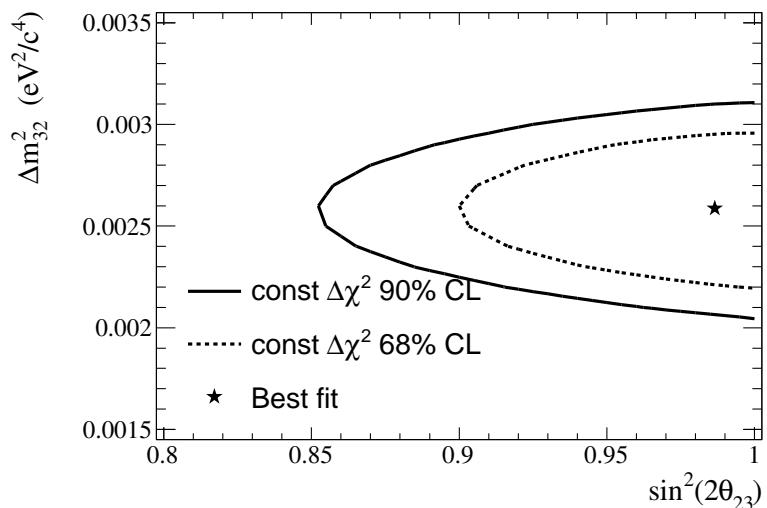


Figure 91: As in Fig. 89, but for the Run 1+2 dataset only.

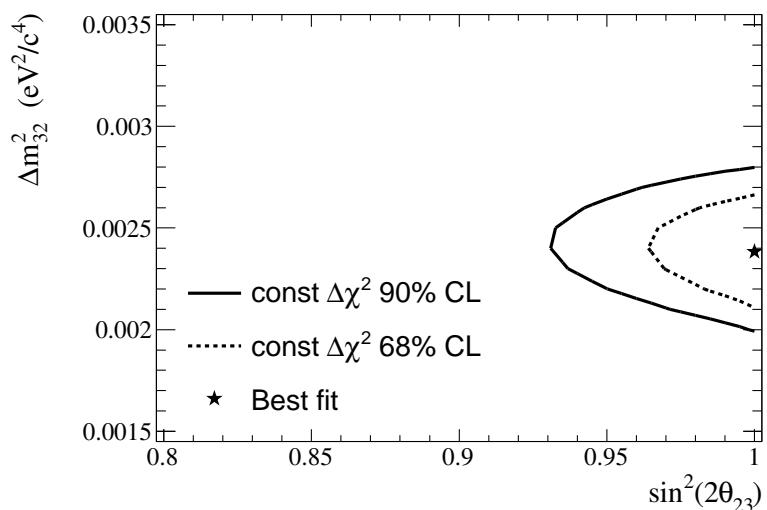
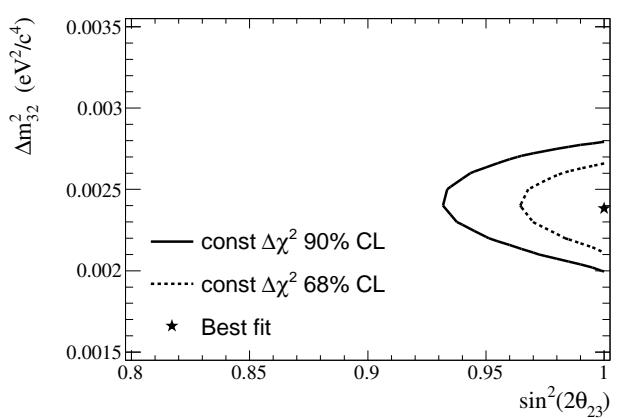
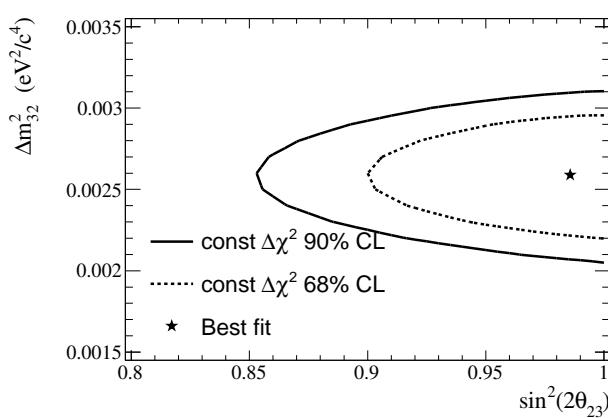
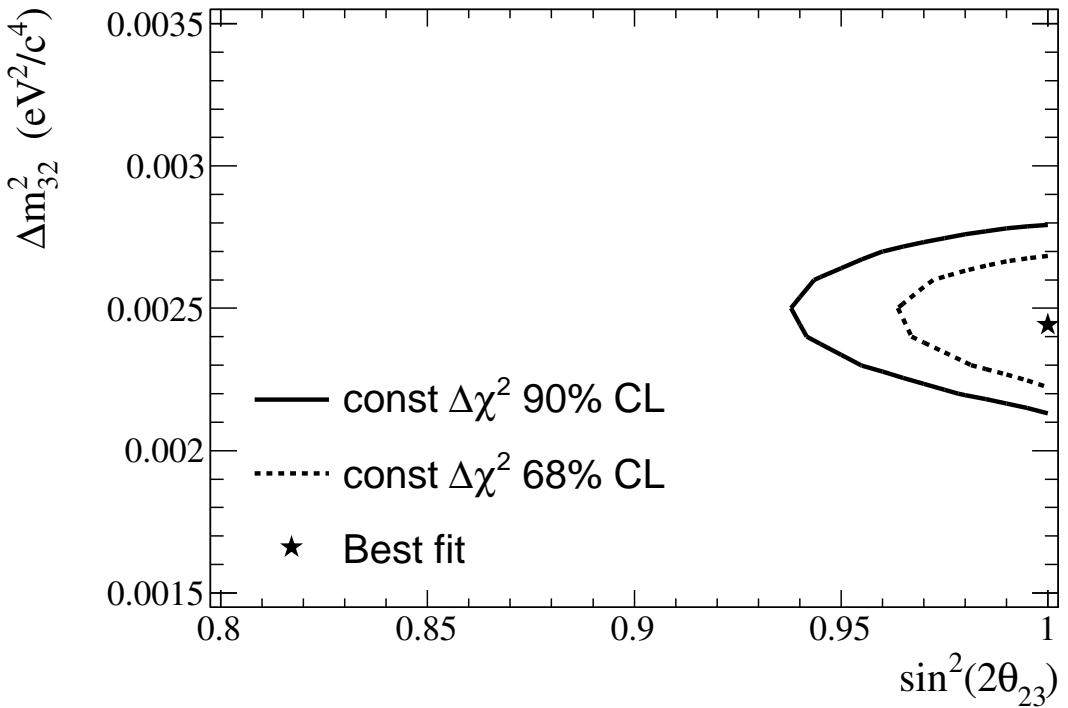


Figure 92: As in Fig. 89, but for the Run 3 dataset only.



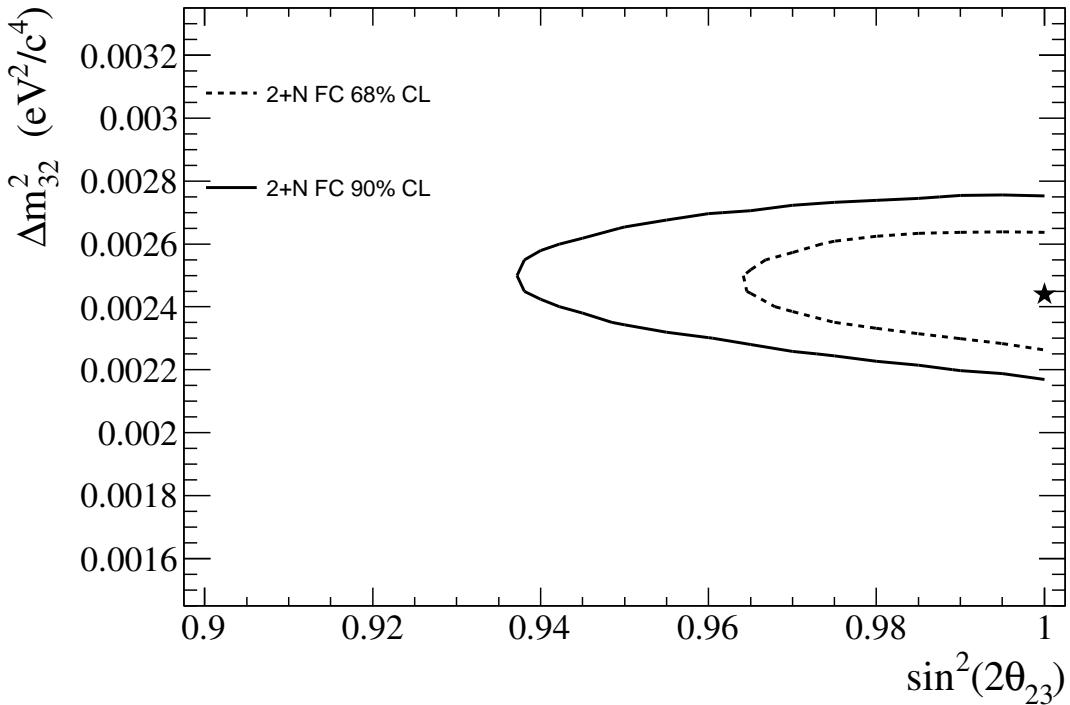


Figure 96: 68% CL and 90% CL allowed region (including systematics), constructed with the method of Feldman and Cousins, for the ‘2+N’ fit to the Run 1+2+3 dataset assuming θ_{23} is in the first octant. The ‘2+N’ best-fit point is also shown.

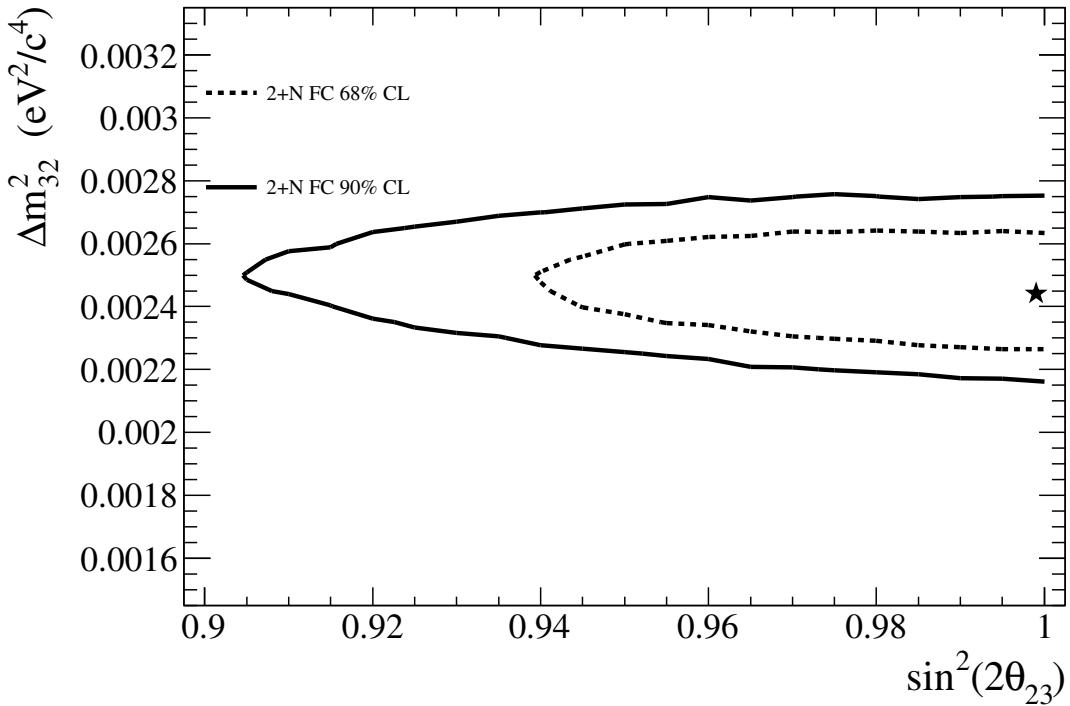


Figure 97: 68% CL and 90% CL allowed region (including systematics), constructed with the method of Feldman and Cousins, for the ‘2+N’ fit to the Run 1+2+3 dataset assuming θ_{23} is in the second octant. The ‘2+N’ best-fit point is also shown.

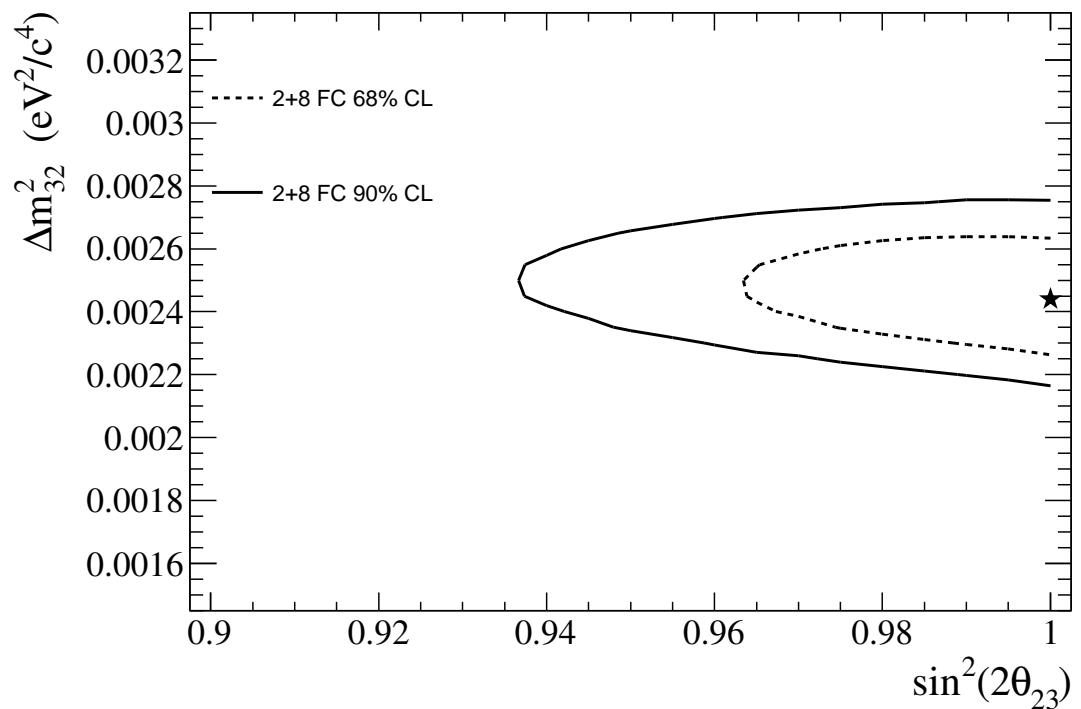


Figure 98: 68% CL and 90% CL allowed region (including systematics), constructed with the method of Feldman and Cousins, for the ‘2+8’ fit to the Run 1+2+3 dataset. The ‘2+8’ best-fit point is also shown.

954 5.6. Confidence region comparisons

955 5.6.1. Comparisons between the ‘2+N’ contours assuming θ_{23} is in the first and second octants

956 Comparisons were made between the allowed regions obtained using the different fits to the Run 1+2+3 dataset,
 957 A comparison between θ_{23} octant assumptions for the ‘2+N’ regions constructed using the constant- $\Delta\chi^2$ method is
 958 shown in Fig. 99. A comparison between θ_{23} octant assumptions for the ‘2+N’ regions constructed using the method
 959 of Feldman and Cousins is shown in Fig. 100. The contours are visibly different; this is due to the next-to-leading order
 960 term in Eq. 3.

961 Constant $\Delta\chi^2$ contours for both θ_{23} octant assumptions are converted into $\sin^2 \theta_{23}$ - $|\Delta m_{32}^2|$ space in Fig. 101. They
 962 are compared with the fit to $\sin^2 \theta_{23}$. The contours are identical, showing that the difference between contours from
 963 different θ_{23} octant assumptions shown in Fig. 99 is what is expected. The best-fit values in $\sin^2 \theta_{23}$ of the 3 fits are
 964 given in Tab. 13.

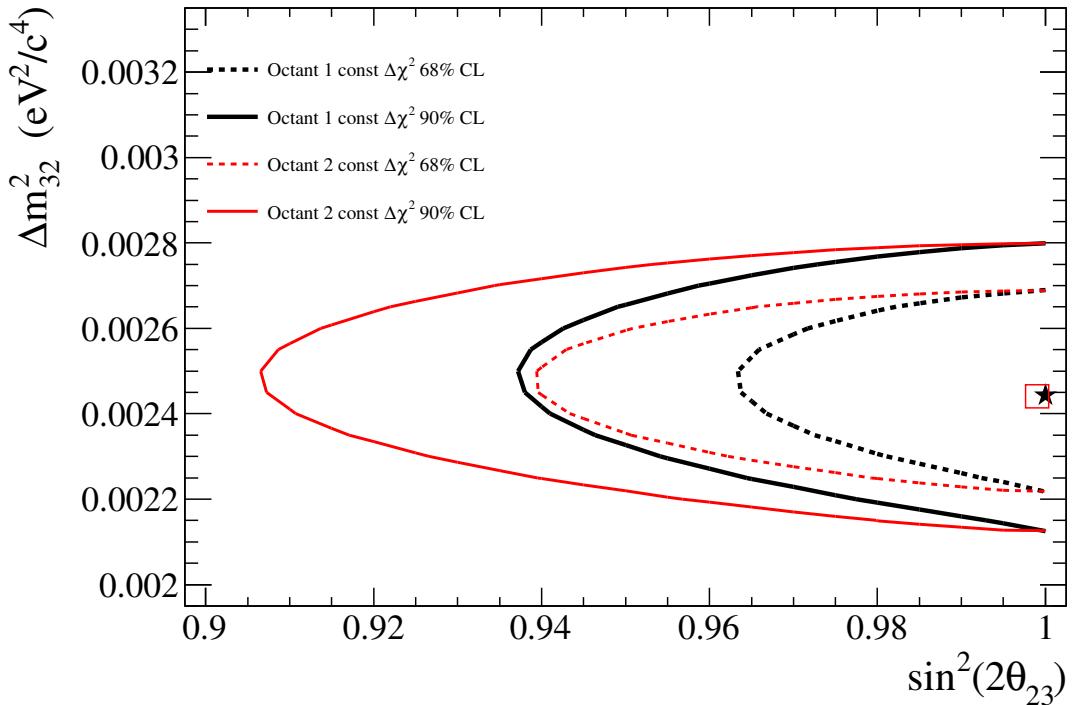


Figure 99: Comparison between the ‘2+N’ 68% CL and 90% CL allowed regions for θ_{23} in the first and second octants obtained using the constant- $\Delta\chi^2$ method. The comparison is shown for the fits to the Run 1+2+3 dataset.

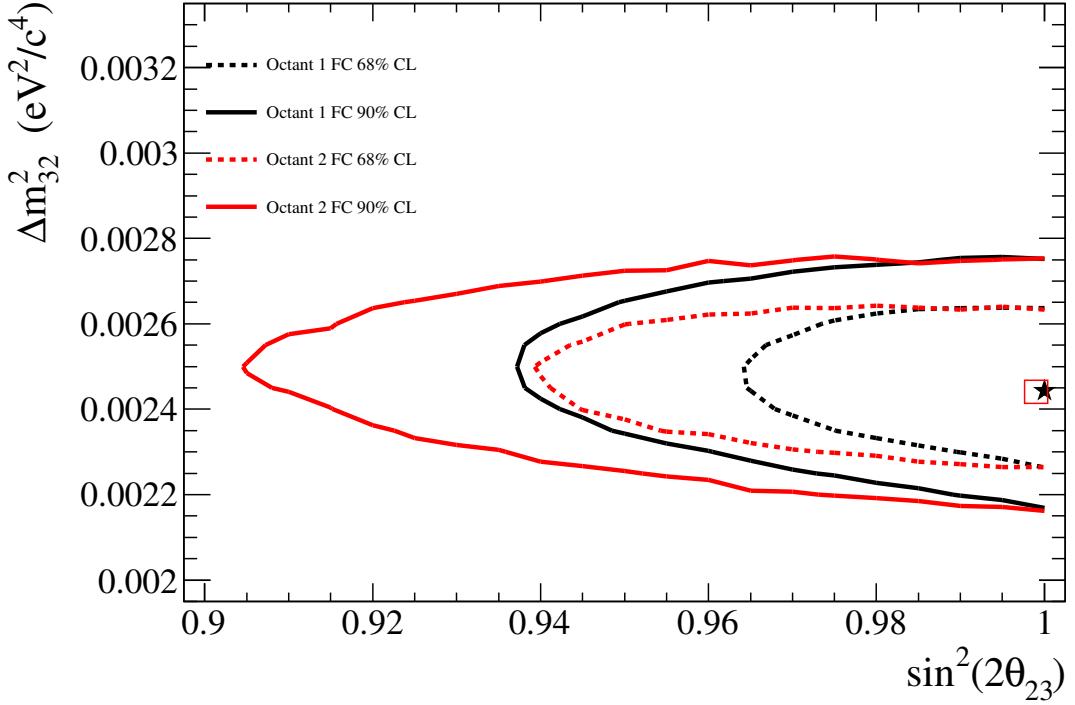


Figure 100: Comparison between the ‘2+N’ 68% CL and 90% CL allowed regions for θ_{23} in the first and second octants obtained using the method of Feldman and Cousins. The comparison is shown for the fits to the Run 1+2+3 dataset.

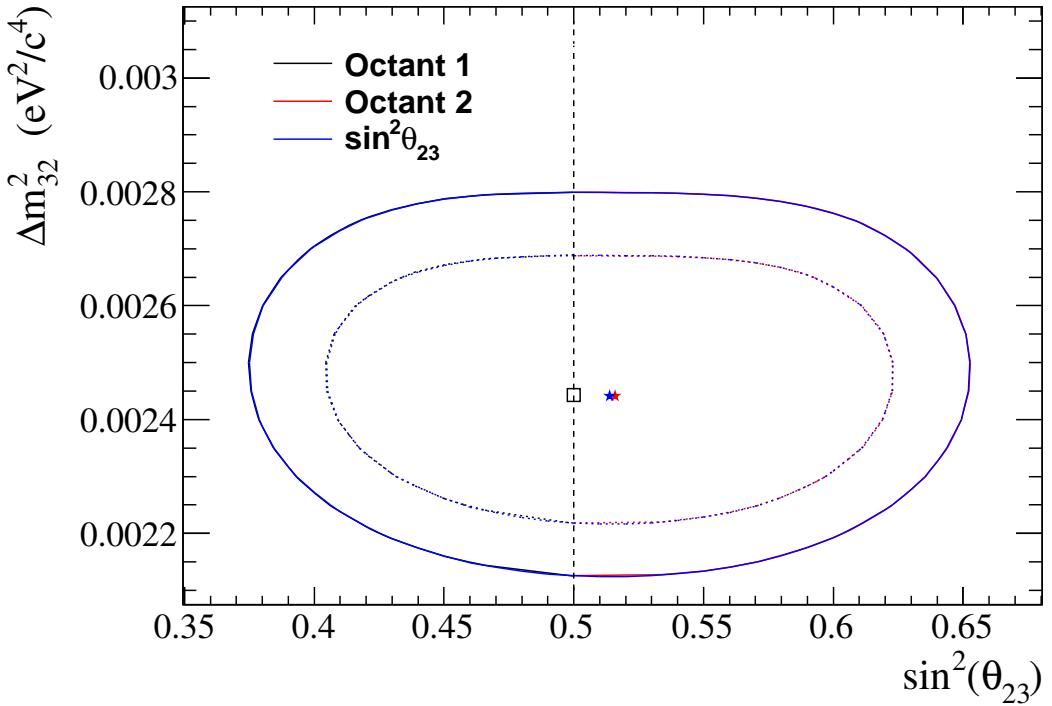


Figure 101: Comparison between the ‘2+N’ 68% CL and 90% CL allowed regions for θ_{23} in the first and second octants obtained using the constant- $\Delta\chi^2$ method, and with the x-axis converted from $\sin^2 2\theta_{23}$ to $\sin^2 \theta_{23}$ after the fit. A ‘2+N’ fit using $\sin^2 \theta_{23}$ directly is also shown. The vertical line is the boundary between the octants to help guide the reader’s eye. The comparison is shown for the fits to the Run 1+2+3 dataset.

965 5.6.2. Comparisons between the ‘2+N’ and ‘2+8’ contours

966 Comparisons were made between the allowed regions obtained using the different fits to the Run 1+2+3 dataset, A
 967 comparison between the ‘2+N’ and ‘2+8’ regions constructed using the constant- $\Delta\chi^2$ method is shown in Fig. 102. A
 968 comparison between the ‘2+N’ and ‘2+8’ regions constructed using the method of Feldman and Cousins is shown in
 969 Fig. 103. For a given contour construction method, the ‘2+N’ and ‘2+8’ contours are almost identical.

970 Fig. 104 shows a comparison between the ‘2+N’ and ‘2+8’ regions, constructed using the constant- $\Delta\chi^2$ method,
 971 with the corresponding results for ‘2+0’. The ‘2+0’ fit results in smaller contours. The plot illustrates that, while with
 972 the present statistics fitting for systematics is warranted (‘2+0’ contours smaller than ‘2+8’ and ‘2+N’), the full effect
 973 of the systematics on the contour is encapsulated by allowing only the the 8 dominant to float in the fit.

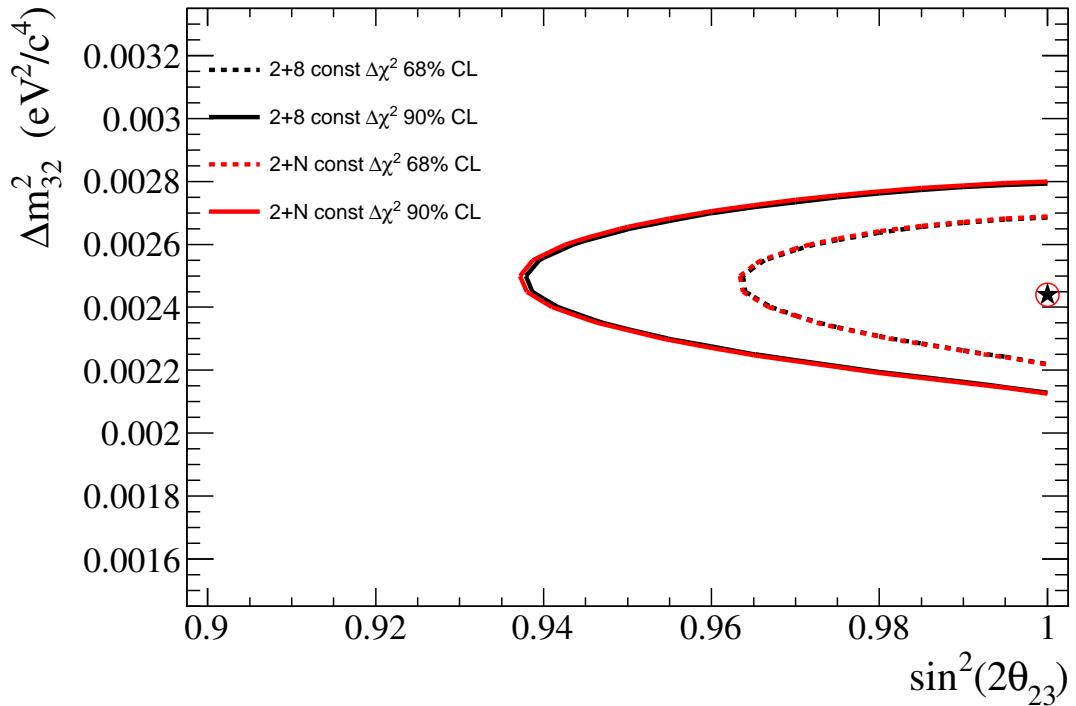


Figure 102: Comparison between the ‘2+N’ and ‘2+8’ 68% CL and 90% CL allowed regions obtained using the constant- $\Delta\chi^2$ method. The comparison is shown for the fits to the Run 1+2+3 dataset. The ‘2+N’ and ‘2+8’ confidence regions are identical.

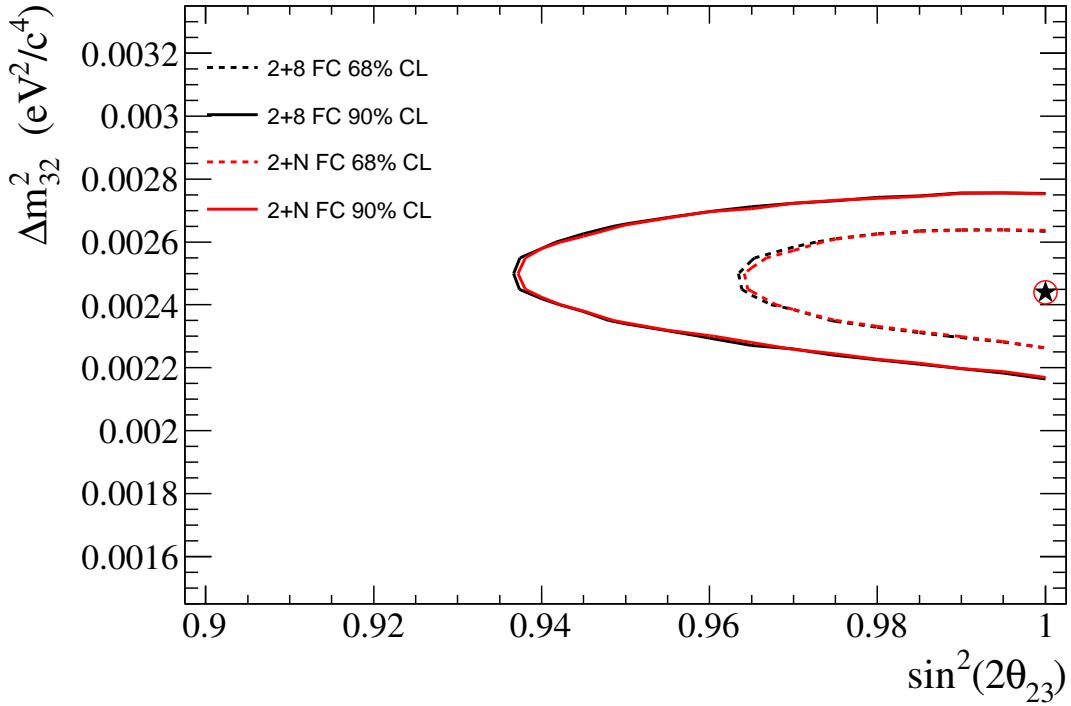


Figure 103: Comparison between the ‘2+N’ and ‘2+8’ 68% CL and 90% CL allowed regions obtained using the method of Feldman and Cousins. The comparison is shown for the fits to the Run 1+2+3 dataset.

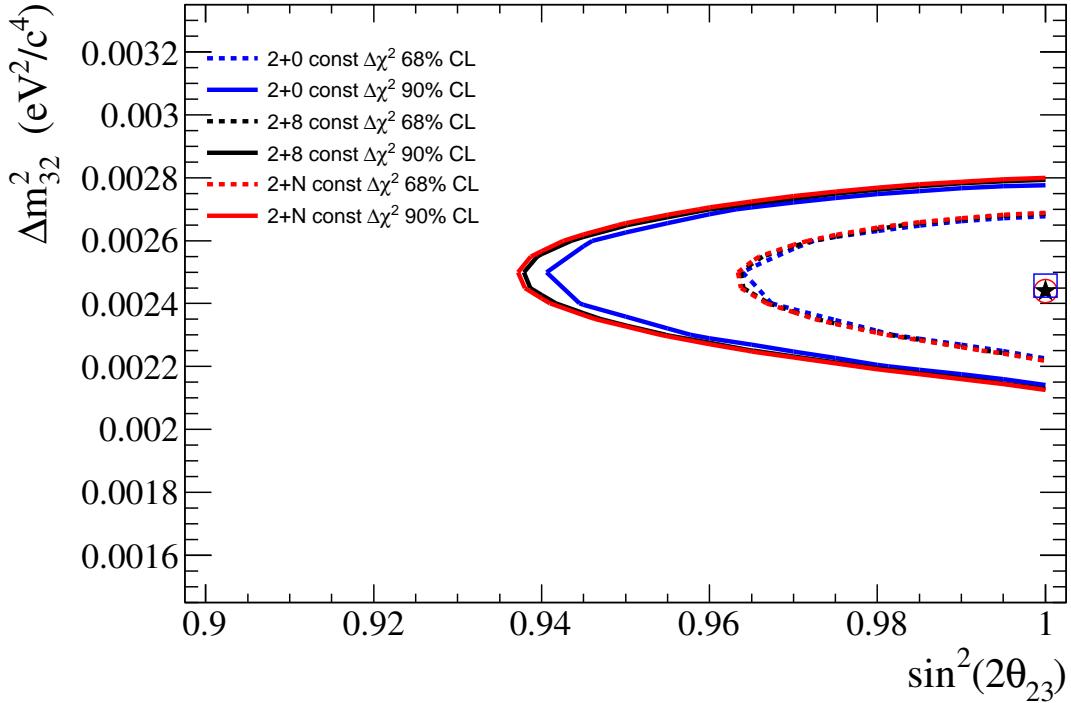


Figure 104: Comparison between the ‘2+N’, ‘2+8’ and ‘2+0’ 68% CL and 90% CL allowed regions obtained using the constant- $\Delta\chi^2$ method. The comparison is shown for the fits to the Run 1+2+3 dataset.

974 5.6.3. Comparisons between the constant- $\Delta\chi^2$ and Feldman-Cousins contours

975 The confidence regions obtained using the same fit variant but different contour construction methods were also
 976 compared. In Fig. 105, a comparison between the contours obtained using the constant- $\Delta\chi^2$ and Feldman-Cousins
 977 methods is shown for the ‘2+N’ fit to the Run 1+2+3 dataset. In Fig. 106, the same comparison is shown for the ‘2+N’
 978 fit assuming θ_{23} is in the second octant. In Fig. 107, the same comparison is shown for the ‘2+8’ fit.

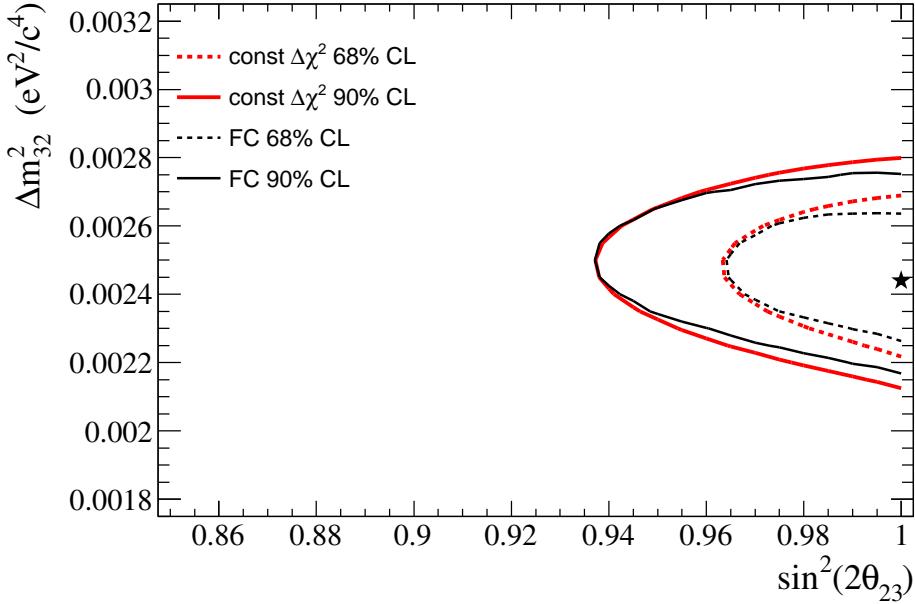


Figure 105: Comparison between the 68% CL and 90% CL allowed regions obtained using the constant- $\Delta\chi^2$ and Feldman-Cousins methods for the ‘2+N’ fit to the Run 1+2+3 dataset assuming θ_{23} is in the first octant.

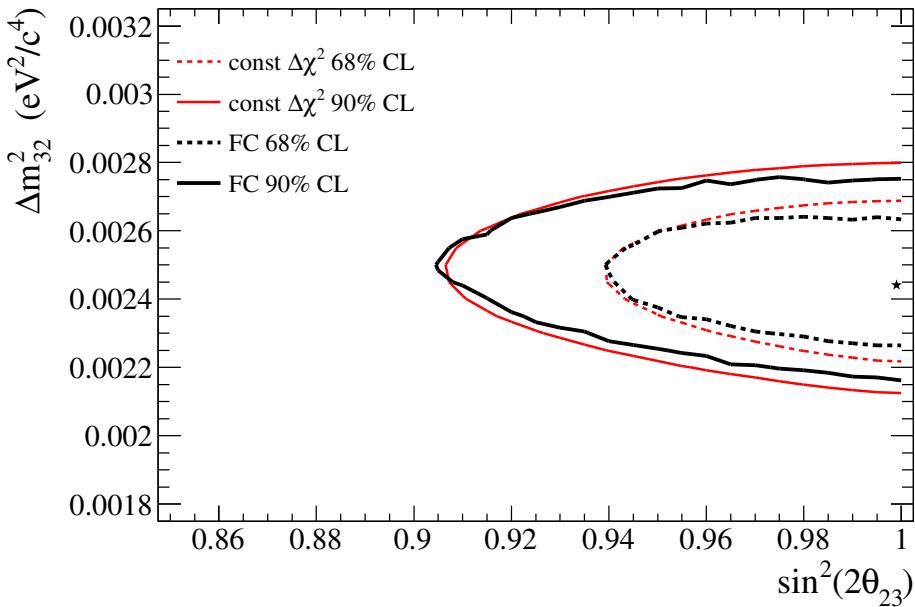


Figure 106: Comparison between the 68% CL and 90% CL allowed regions obtained using the constant- $\Delta\chi^2$ and Feldman-Cousins methods for the ‘2+N’ fit to the Run 1+2+3 dataset assuming θ_{23} is in the second octant.

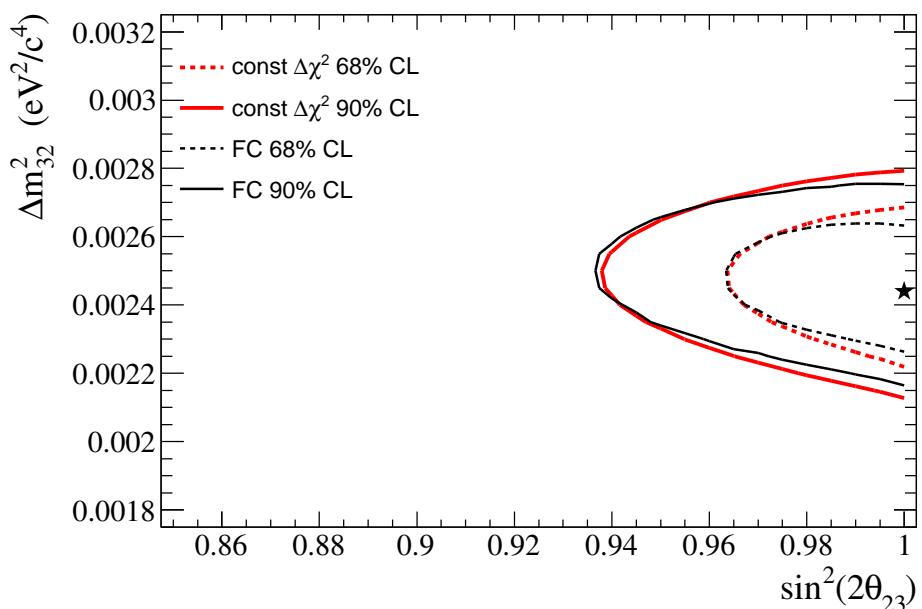


Figure 107: Comparison between the 68% CL and 90% CL allowed regions obtained using the constant- $\Delta\chi^2$ and Feldman-Cousins methods for the ‘2+8’ fit to the Run 1+2+3 dataset.

979 5.6.4. Comparisons with recent measurements from MINOS and SuperK

980 Comparisons were produced between our Run 1+2+3 results and the updated results from MINOS 2013 (3-flavour
 981 analysis) [32] and SuperK 2012 atmospheric (3-flavour zenith-angle analysis) [33]. The comparison is shown in Fig.
 982 108 for the ‘2+N’ fit for $\sin^2 \theta_{23}$.

983 Comparisons were produced between our Run 1+2+3 results and the updated (2012) results from MINOS [31] and
 984 SuperK atmospheric (both the 2-flavour L/E and 3-flavour zenith-angle analyses) [33]. The comparison is shown in
 985 Fig. 109 for the ‘2+N’ fit assuming θ_{23} is in the first octant, in Fig. 110 for the ‘2+N’ fit assuming it is in the second
 986 octant, and in Fig. 111 for the ‘2+8’ fit. A comparison of ‘2+N’ FC contours with the external data is shown in Fig.
 987 112 for both octant assumptions.

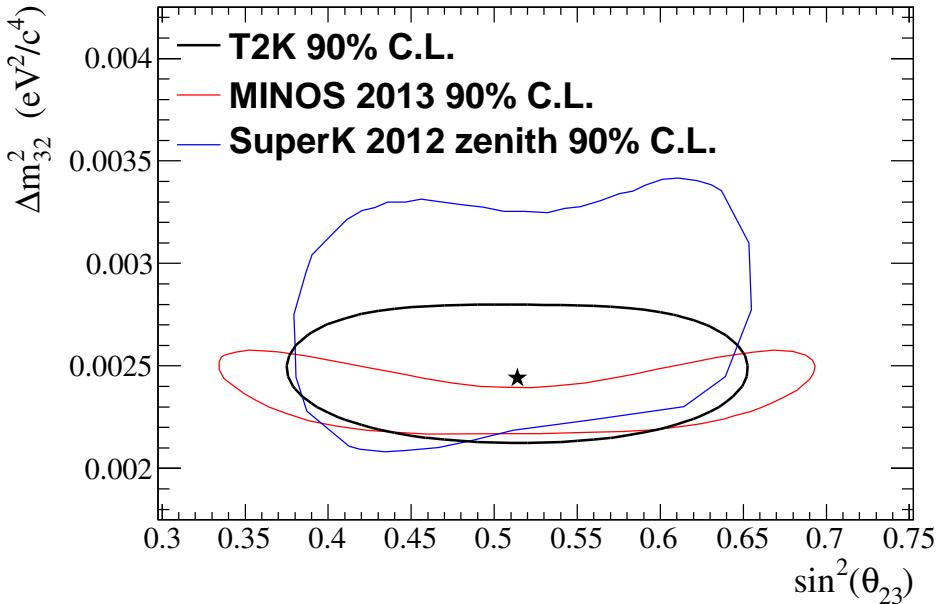


Figure 108: Comparison between 90% CL allowed regions from MINOS [32] and SuperK atmospheric [33], and the 90% CL region obtained from the VaLOR ‘2+N’ $\sin^2 \theta_{23}$ fit to the Run 1+2+3 dataset, using the constant- $\Delta\chi^2$ method.

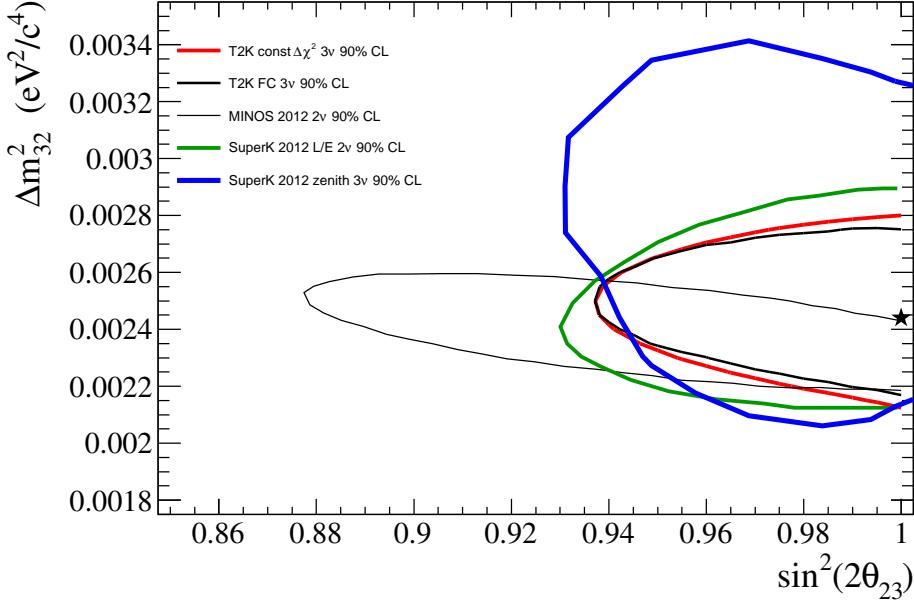


Figure 109: Comparison between 90% CL allowed regions from MINOS [31] and SuperK atmospherics [33], and the 90% CL regions obtained from the VaLOR ‘2+N’ fit to the Run 1+2+3 dataset. Contours obtained using both the constant- $\Delta\chi^2$ and Feldman-Cousins methods are shown.

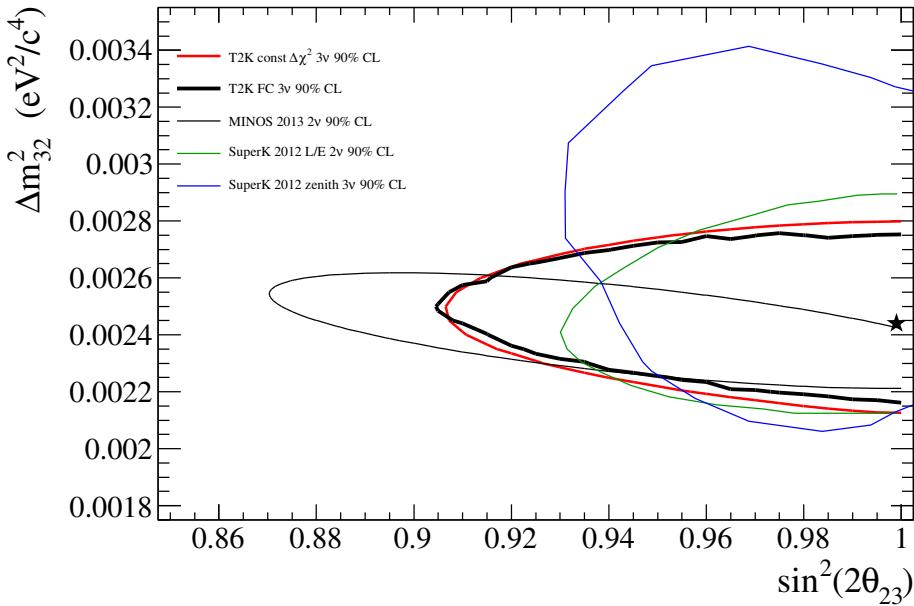


Figure 110: As in Fig. 109, but for the ‘2+N’ fit assuming θ_{23} is in the second octant.

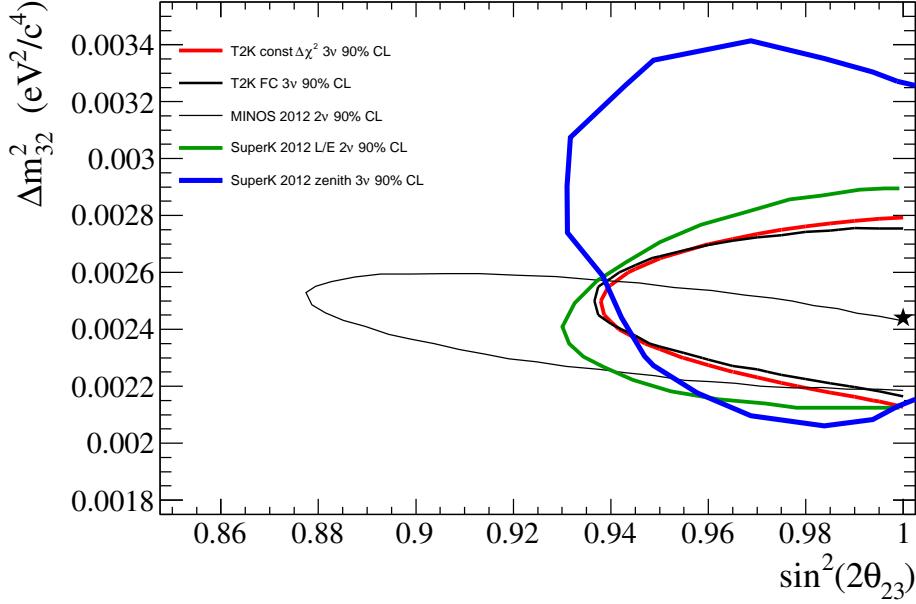
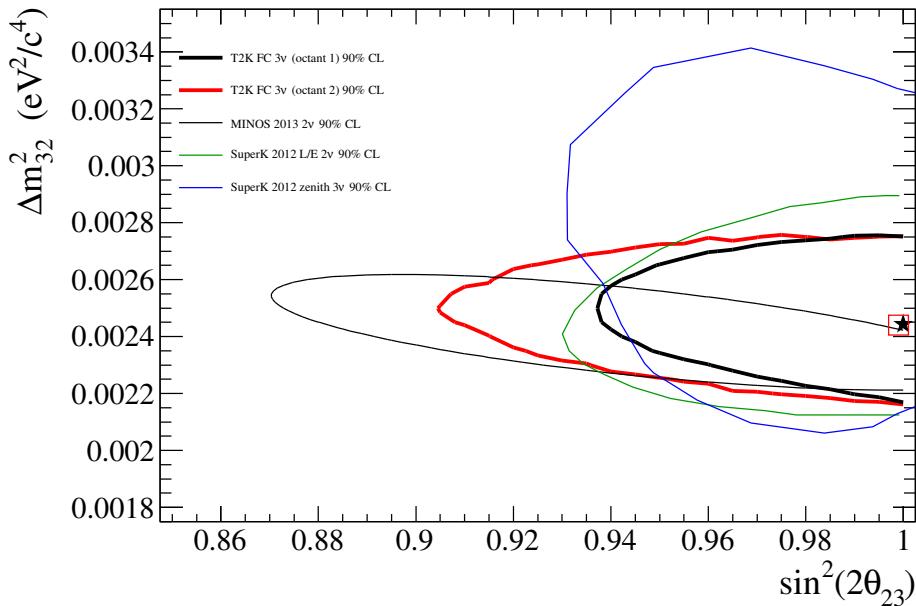


Figure 111: As in Fig. 109, but for the ‘2+8’ fit.

Figure 112: Comparison between 90% CL allowed regions from MINOS [31] and SuperK atmospherics [33], and the 90% CL regions obtained from the VaLOR ‘2+N’ fit to the Run 1+2+3 dataset. Contours obtained using both θ_{23} octant assumptions are shown.

988 5.6.5. Comparisons with sensitivity

989 In Fig. 113, a comparison is shown between the Run 1+2+3 allowed regions obtained using the ‘2+8’ fit and the
 990 constant- $\Delta\chi^2$ method, and the T2K 3.010×10^{20} POT sensitivity contours produced at the ‘2+8’ best-fit point for the
 991 Run 1+2+3 dataset. The sensitivity contours were computed by averaging the contours of 1k toy-MC experiments
 992 generated with statistical fluctuations and all systematic parameters randomized. The plot indicates that the Run 1+2+3
 993 dataset, is a “favourable” fluctuation allowing us to quote confidence regions which are more restrictive than those that
 994 would be expected given our sensitivity. This favourable fluctuation is not unlikely as shown in Fig. 114.

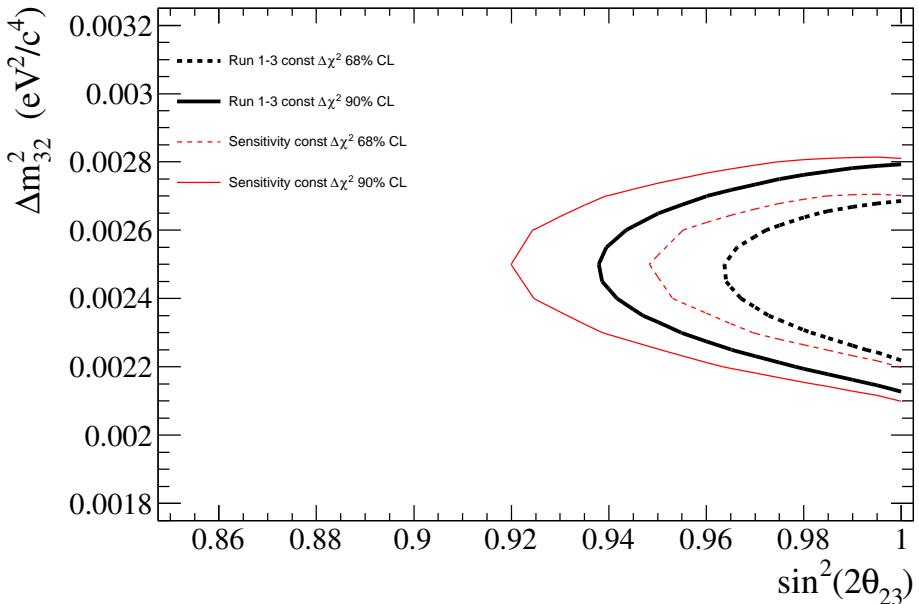


Figure 113: Comparison between the 68% CL and 90% CL allowed regions using the constant- $\Delta\chi^2$ method for the ‘2+8’ fit to the Run 1+2+3 dataset and the result of a sensitivity study at the ‘2+8’ best-fit point for Run 1+2+3.

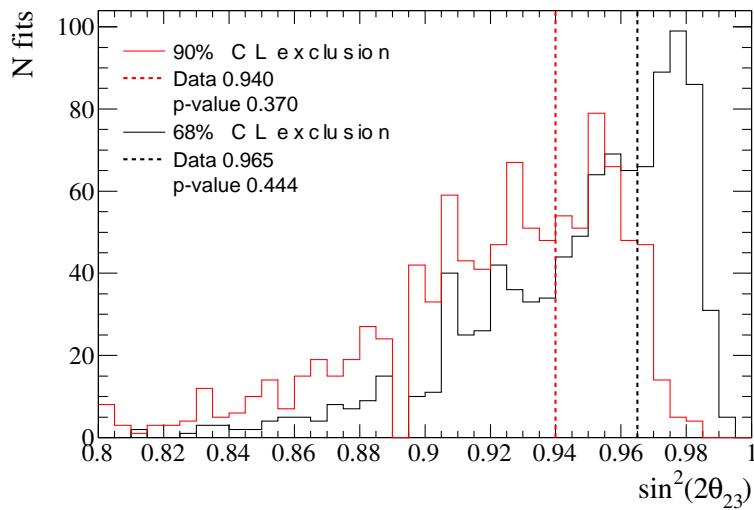


Figure 114: Distribution of minimum excluded value of $\sin^2 2\theta_{23}$, for both 68% CL and 90% CL. The dashed lines show the minimum excluded value for the ‘2+8’ fit to the Run 1+2+3 dataset, using the constant- $\Delta\chi^2$ method (68% CL in black and 90% CL in red).

995 5.6.6. Comparisons of individual run periods

996 A comparison between the confidence regions obtained by three separate ‘2+N’ analyses of the Run 1+2+3, Run
 997 1+2 and Run 3 datasets is shown in Fig. 115. The corresponding plot for the ‘2+8’ fit is shown in Fig. 116. The
 998 contours from the different running periods are consistent.

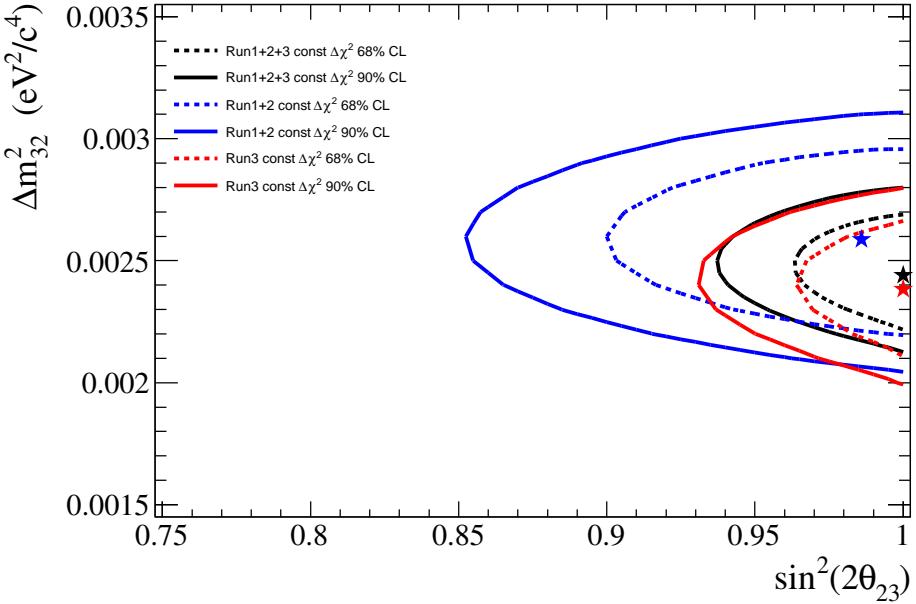


Figure 115: Comparison between the 68% CL and 90% CL allowed regions obtained from separate ‘2+N’ analyses of the Run 1+2+3, Run 1+2 and Run 3 datasets. All contours shown were calculated with the constant- $\Delta\chi^2$ method.

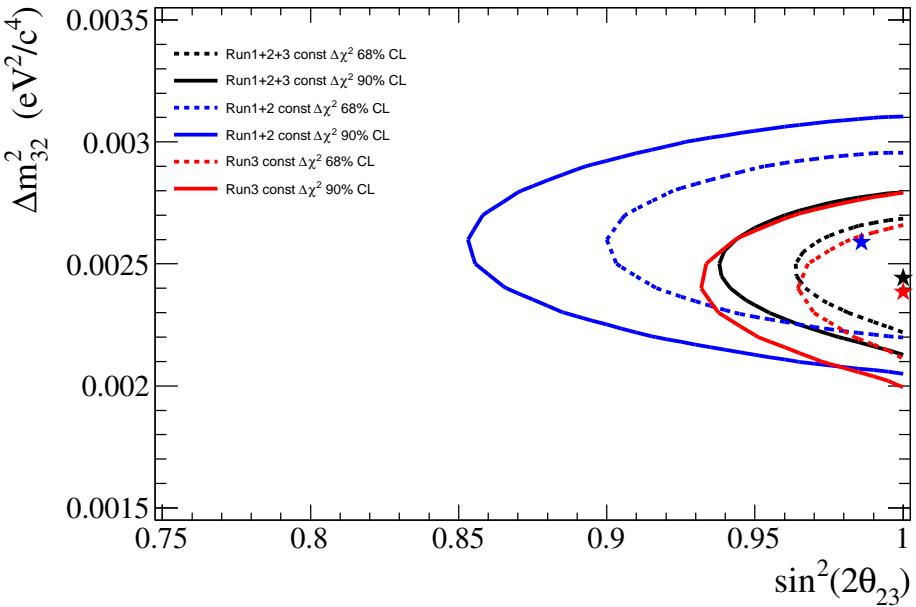


Figure 116: Comparison between the 68% CL and 90% CL allowed regions obtained from separate ‘2+8’ analyses of the Run 1+2+3, Run 1+2 and Run 3 datasets. All contours shown were calculated with the constant- $\Delta\chi^2$ method.

999 5.7. The *VaLOR* group perspective on the choice of primary result

1000 Four separate ν_μ -disappearance results have been produced by this analysis for the Run 1+2+3 dataset; this is
1001 because we have used two fitting methods ('2+N' and '2+8') and two methods for constructing confidence regions
1002 (constant- $\Delta\chi^2$ and Feldman-Cousins).

1003 This analysis used contours produced with the constant- $\Delta\chi^2$ method quite extensively, especially during its devel-
1004 opment and for the sensitivity studies. We considered that producing Feldman-Cousins contours at an early stage would
1005 not be the best use of our time or of the CPU resources available to us. In that respect, the constant- $\Delta\chi^2$ contours were
1006 invaluable as a tool for developing the analysis. The constant- $\Delta\chi^2$ contours meet some, but not all of the requirements
1007 set by the muon-neutrino contour committee: they should have correct coverage, they should be standard in the field
1008 and easy to explain, they should avoid paradoxical results and should be computationally feasible [30]. However our
1009 group has been a strong advocate of the use of the Feldman-Cousins method from the time of the Run 1 analysis. Since
1010 the best-fit value of $\sin^2 2\theta_{23}$ is at the physical boundary, the constant- $\Delta\chi^2$ contours do not have correct coverage with
1011 present statistics and we do not consider them as contenders for our primary result.

1012 This leaves only two options to consider: The '2+N' and the '2+8' Feldman-Cousins contours. As shown in this
1013 paper, no real difference exists between the '2+N' and the '2+8' results:

- 1014 • The best-fit points are identical for the combined Run 1+2+3 dataset (and nearly identical for the separate fits to
1015 the Run 1+2 and Run 3 datasets), as shown in Tab. 14.
- 1016 • The p-values for the fits to the combined Run 1+2+3 dataset are identical, as shown in Tab. 14.
- 1017 • Although all 48 systematic parameters are allowed to float in the '2+N' fit, only 6 parameters have best-fit values
1018 which are more than $\pm 0.1\sigma$ away from their corresponding nominal values, as shown in Fig. 34. Thus the vast
1019 majority of the systematic parameters included in the '2+N' fit have, in fact, a negligible effect on the fit.
- 1020 • The best-fit spectra are indistinguishable when superimposed on the same plot, as shown in Fig. 65. The best-fit
1021 spectra (binned using the same scheme used in the fit) never differ by more than 1.5% in the area below 3 GeV,
1022 and they are nearly identical in the area of the first oscillation maximum.
- 1023 • The 68% and 90% CL regions for the two fits are identical, as shown in Figs. 102 and 103. Indeed, the '2+N'
1024 and '2+8' marginalized $\Delta\chi^2$ distributions for are identical for both $\sin^2 2\theta_{23}$ and $|\Delta m_{32}^2|$, even in areas of the
1025 oscillation parameter space outside the 99% CL region (this is defined by $\Delta\chi^2 < 6.63$ for a single parameter).
1026 This is shown in Figs. 86 and 87.

1027 Given the marked similarity of the results of the '2+8' and '2+N' fits, it is difficult to make a choice between them.
1028 However the *VaLOR* group prefers the simpler '2+8' fit since it has fewer floating parameters. The choice of the 8
1029 floating parameters in this fit was made with an extremely careful study which is presented in Sec. 4.4.

1030 Ockham's razor states that "Pluralitas non est ponenda sine neccesitate" or "Plurality should not be posited without
1031 necessity" [39]. The plurality of the additional floating parameters in the '2+N' fit is unnecessary since it does not
1032 change the values of the oscillation parameters we seek to measure. Furthermore, the simpler fit is easier to explain to
1033 a wider audience. For these reasons, we feel strongly that the '2+8' result should be the one presented as the official
1034 result outside the T2K collaboration.

1035 **6. Summary**

1036 In this technical note, we have presented the results of a 3-flavour ν_μ -disappearance analysis, performed by the
1037 Valencia-Lancaster-Oxford-Rutherford (VaLOR) group, on the combined Run1+2+3 (3.010×10^{20} POT) dataset. This
1038 analysis is an update of the work presented in Refs. [1], [2] and [3] with improved methods and an enlarged dataset.

1039 This analysis predicts 204.75 ± 16.75 (syst) 1 μ -like ring events in SuperK in the absence of any oscillation, but
1040 only 58 were observed. The observed deficit has a strong energy dependence; the ratio of observed to expected, under
1041 the no oscillation hypothesis, is $\sim 30\% < 0.5 \text{ GeV}, \sim 10\% \text{ between } 0.5 \text{ and } 1 \text{ GeV} \text{ and } \sim 75\% > 1 \text{ GeV}$.

1042 A ν_μ -disappearance analysis was performed in a framework of 3-flavour oscillations including matter effects in
1043 constant-density matter. A total of 48 efficiency, energy scale, neutrino flux, neutrino cross-section, initial-state nuclear
1044 environment and final-state rescattering systematics was taken into account. The effect of these systematic uncertainties
1045 on the expected number of 1 μ -like ring events, on their reconstructed energy spectrum and on our oscillation
1046 measurement were presented in great detail.

1047 Two versions of the oscillation fit were performed: the ‘2+N’ fit allowed all 48 systematics considered in this
1048 analysis to float, whereas the ‘2+8’ fit allowed only the 8 most dominant systematics to float. The dominant systematics
1049 are those identified as having an effect on the measured oscillation parameters that is greater than 25% of the expected
1050 statistical error, for at least one set of true oscillation parameters in the area of interest. The ‘2+N’ 3-flavour ν_μ -
1051 disappearance fit to the observed reconstructed energy spectrum of 1 μ -like ring events of the combined Run1+2+3
1052 dataset, for $\sin^2 \theta_{23}$ yield $|\Delta m_{32}^2| = 2.441 \times 10^{-3} \text{ eV}^2/\text{c}^4$ and $\sin^2 \theta_{23} = 0.514$ as the best-fit values (p-value = 0.80).
1053 For the ‘2+N’ fit assuming the first octant ($\sin^2 2\theta_{23} \geq 0.5$), with $\sin^2 2\theta_{23}$ constrained to the physical region, the best-
1054 fit values are almost identical at $|\Delta m_{32}^2| = 2.443 \times 10^{-3} \text{ eV}^2/\text{c}^4$ and $\sin^2 2\theta_{23} = 1.000$ (p-value = 0.83). For the ‘2+N’
1055 fit assuming the second octant ($\sin^2 2\theta_{23} \geq 0.5$), the best-fit values are almost identical at $|\Delta m_{32}^2| = 2.441 \times 10^{-3}$
1056 eV^2/c^4 and $\sin^2 2\theta_{23} = 0.999$ (p-value = 0.82). For the ‘2+8’ fit, the best-fit values are almost identical. All fits used
1057 the 2012 PDG values for $\sin^2 2\theta_{13}$, $\sin^2 2\theta_{12}$ and Δm_{21}^2 [21], and assumed $\delta_{CP}=0$ and the normal mass hierarchy.

1058 Confidence regions obtained using both the constant- $\Delta\chi^2$ method and the method of Feldman and Cousins were
1059 presented for both the ‘2+N’ and ‘2+8’ fits. Using the results of the ‘1+N’ fits, and the constant- $\Delta\chi^2$ method, the 90%
1060 CL allowed region, for the ‘2+N’ fit for $\sin^2 \theta_{23}$, can be summarized as $2.19 \times 10^{-3} \text{ eV}^2/\text{c}^4 < |\Delta m_{32}^2| < 2.72 \times 10^{-3}$
1061 eV^2/c^4 and $0.397 < \sin^2 \theta_{23} < 0.630$. The corresponding limits for the ‘2+N’ fit assuming the first octant, can be
1062 summarized as $2.19 \times 10^{-3} \text{ eV}^2/\text{c}^4 < |\Delta m_{32}^2| < 2.72 \times 10^{-3} \text{ eV}^2/\text{c}^4$ and $\sin^2 2\theta_{23} > 0.958$. The corresponding limits
1063 for the ‘2+N’ fit assuming the second octant, can be summarized as $2.19 \times 10^{-3} \text{ eV}^2/\text{c}^4 < |\Delta m_{32}^2| < 2.72 \times 10^{-3}$
1064 eV^2/c^4 and $\sin^2 2\theta_{23} > 0.931$.

1065 Numerous comparisons were made of the best-fit values and spectra, of the systematic parameter pulls, and of the
1066 χ^2 surfaces obtained by the different fit methods and for different running periods. Detailed comparisons were pre-
1067 sented of the confidence regions obtained by using different construction methods, for the same fit, and by using dif-
1068 ferent fitting methods, for the same construction method. The contours from different running periods were compared.
1069 Comparisons of our contours with recent measurements from MINOS and SuperK and the T2K 3.010×10^{20} -POT sen-
1070 sitivity were also made. Finally, a more critical view of the 4 different results obtained by this analysis was presented
1071 in Sec. 5.7.

1072 **References**

- 1073 [1] C.Andreopoulos, T.Dealtry, J.Dobson, N.Grant, M.Haigh, J.Ilic, G.Pearce and A.Weber, T2K 3.23×10^{19} -POT
1074 Muon-Neutrino Disappearance Analysis, T2K-TN-036(v4),
1075 <http://www.t2k.org/docs/technotes/036>
- 1076 [2] C.Andreopoulos, T.Dealtry, J.Dobson, N.Grant, M.Haigh, J.Ilic, G.Pearce and A.Weber, T2K 1.431×10^{20} -POT
1077 Muon-Neutrino Disappearance Analysis T2K-TN-064(v3),
1078 <http://www.t2k.org/docs/technotes/064>
- 1079 [3] C.Andreopoulos, T.Dealtry, L.Escudero and N.Grant, T2K 1.431×10^{20} -POT 3-Flavour Muon-Neutrino Disap-
1080 pearance Analysis T2K-TN-087(v1),
1081 <http://www.t2k.org/docs/technotes/087>
- 1082 [4] C.Andreopoulos, A.Cervera, T.Dealtry, L.Escudero, N.Grant, M.Sorel and P.Stamoulis, T2K 1.431×10^{20} -POT
1083 Joint 3-Flavour Oscillation Analysis T2K-TN-133(v1),
1084 <http://www.t2k.org/docs/technotes/133>

- 1085 [5] C.Andreopoulos, A.Cervera, T.Dealtry, L.Escudero, N.Grant, M.Sorel and P.Stamoulis, T2K 3.010×10^{20} -POT
 1086 Joint 3-Flavour Oscillation Analysis T2K-TN-154(v2),
 1087 <http://www.t2k.org/docs/technotes/154>
- 1088 [6] C.Andreopoulos, T.Dealtry, L.Escudero, N.Grant and A.Weber, T2K 6.3933×10^{20} -POT 3-Flavour Muon-Neutrino
 1089 Disappearance Analysis T2K-TN-154(v2),
 1090 <http://www.t2k.org/docs/technotes/155>
- 1091 [7] T2K Collaboration (K.Abe et al.), First Muon-Neutirno Disappearance Study with an Off-Axis Beam,
 1092 Phys.Rev.D85:031103, 2012; arXiv:1201.1386
- 1093 [8] Y.Hayato, A neutrino interaction simulation program library NEUT, Acta Phys.Polon.B40:2477-2489,2009.
- 1094 [9] Beam WG, Flux tuning (11b v3.2), <http://www.t2k.org/beam/NuFlux/FluxRelease/11brelease/11btuned-v3.2>
- 1095 [10] M.Otani and J.Kameda, Super-K events and Updated systematic errors for ν_μ disappearance analysis with T2K
 1096 1.431×10^{20} POT T2K-TN-065(v6), <http://www.t2k.org/docs/technotes/065>
- 1097 [11] P. de Perio et al., NEUT nuclear effects (FSI) T2K-TN-033(v2.0), <http://www.t2k.org/docs/technotes/033>
- 1098 [12] P. de Perio et al., Cross section parameters for the 2012a oscillation analysis T2K-TN-108(v1.3),
 1099 <http://www.t2k.org/docs/technotes/108>
- 1100 [13] P. de Perio et al., Implementation of the NIWG cross-section parametrization, T2K-TN-113(v1.2)
- 1101 [14] P. de Perio et al., Constraining the Flux and Cross Section Models with Data from the ND280 Detector for the
 1102 2012a Oscillation Analysis, T2K-TN-106(v8.0) <http://www.t2k.org/docs/technotes/106>
- 1103 [15] P. de Perio et al., Pion Hadronic Secondary Interactions in Super-Kamiokande, T2K-TN-105(v1.1)
 1104 <http://www.t2k.org/docs/technotes/105>
- 1105 [16] Y. Ashie et al., Phys. Rev. Lett. 93, 101801 (2004); Y. Ashie et al., Phys. Rev. D71, 112005 (2005); J. Hosaka et
 1106 al., Phys. Rev. D 74, 032002 (2006).
- 1107 [17] T2KSK, http://www.t2k.org/t2ksk/code/sk11c_mc/sampleinfo.
- 1108 [18] Beam group, <http://www.t2k.org/beam/NuFlux/FluxRelease/11arelease/11atuned-v2.3>.
- 1109 [19] M. Hartz, BANFF Fit Update for the 2012 Disappearance Analyses,
 1110 <http://www.t2k.org/asg/meeting/20121015/banffinputsdisapp/view>.
- 1111 [20] N Abgrall et al. Measurements of Cross Sections and Charged Pion Spectra in Proton-Carbon Interactions at
 1112 31 GeV/c. Phys.Rev., C84:034604, 2011; N. Abgrall et al. Measurement of production properties of positively
 1113 charged kaons in proton-carbon interactions at 31 GeV/c. arXiv:hep-ex/1112.0150, 2011.
- 1114 [21] J. Beringer et al. (Particle Data Group), Phys. Rev. D86, 010001 (2012)
- 1115 [22] Lorena Escudero Sanchez for the VaLOR group, <http://www.t2k.org/asg/oagroup/meeting/20121219/VaLOR>
- 1116 [23] Tom Dealtry for the VaLOR group, <http://www.t2k.org/asg/meeting/2012/20121015/valornumudisapp/view>
- 1117 [24] G. Cowan (1998) Statistical data analysis, Oxford University Press, ISBN 0-19-850155-2.
- 1118 [25] F.James, M.Roos, Minuit: A System for Function Minimization and Analysis of the Parameter Errors and Corre-
 1119 lations, Comput.Phys.Commun. 10:343 (1975)
- 1120 [26] G.J. Feldman and R.D. Cousins, A Unified approach to the classical statistical analysis of small signals,
 1121 Phys.Rev.D57:3873-3889,1998; physics/9711021
- 1122 [27] R.D. Cousins and V.L.Highland, Nucl.Instr. and Meth. A320:331035, 1992.
- 1123 [28] N.Grant for the VaLOR group, <http://www.t2k.org/asg/meeting/2011/20111124/pvalues/view>

- 1124 [29] D.Karlen, p-values, distributions and low statistics, <http://www.t2k.org/asg/oagroup/meeting/20120416/lowstat/view>
 1125 [30] K. McFarland for the T2K ν_μ -disappearance contour committee (C.Andreopoulos, N.Grant, J.Kameda,
 1126 D.Karlen, E.Kearns, K.McFarland, M.Otani, M.Zito) Report to ASG conveners meeting, 17 May 2011,
 1127 <http://www.t2k.org/asg/contour/ASG-Conveners-Report/view>
- 1128 [31] R.Nichol, Talk at Neutrino 2012
 1129 [32] A. Radovic, Talk at DPF 2013
 1130 [33] Y.Itow, Talk at Neutrino 2012
 1131 [34] S. Abe et al., Precision measurements of neutrino oscillation parameters with KamLAND
 1132 Phys.Rev.Lett.100:221803,2008
 1133 [35] F.P. An et al., Observation of electron-antineutrino disappearance at Daya Bay Phys.Rev.Lett.108:171803,2012
 1134 [36] J.K. Ahn et al., Observation of reactor electron antineutrinos disappearance in the Reno experiment
 1135 Phys.Rev.Lett.108:191802,2012
 1136 [37] G.L.Fogli, E.Lisi et al., Evidence of $\theta_{13} > 0$ from global neutrino data analysis, arXiv:1106.6028 [hep-ph]
 1137 [38] M.C.Gonzalez-Garcia, M.Maltoni, J.Salvado and T.Schwetz, Global fit to three neutrino mixing: critical look at
 1138 present precision, arXiv:1209.3023 [hep-ph]
 1139 [39] "Ockham's razor", Encyclopedia Britannica <http://www.britannica.com/EBchecked/topic/424706/Ockhams-razor>
 1140
 1141 [40] B. Kayser (2005), Neutrino physics, hep-ph 0506165
 1142 [41] C Giunti and C.W. Kim (2007) Fundamentals of neutrino physics and astrophysics, Oxford Uninversity Press
 1143 [42] J. Kopp (2006), Efficient numerical diagonalisation of Hermitian 3x3 matrices, arXiv:physics/0610206
 1144 [43] T. Sloan, private communication (June-July 2011)
 1145 [44] Prob3++ 3-flavour oscillation probability software, <http://www.phy.duke.edu/raw22/public/Prob3++/>

1146 **A. VaLOR 3-flavour oscillation probability calculations**

1147 In this analysis, 3-flavour neutrino oscillation probabilities in constant density matter are used. Vacuum 3-flavour
 1148 oscillation probabilities are also calculated, but these are used only to estimate the accuracy of the 3-flavour probabilities
 1149 in matter (see section A.6). The method of calculation of the vacuum probabilities is given in section A.1, while the
 1150 calculation of the probabilities in constant density matter is described in section A.2. The code that makes these
 1151 calculations has been integrated into the VaLOR oscillation analysis package. In section A.4, comparisons are given
 1152 between 2-flavour and 3-flavour (in matter) oscillation probabilities, and between 3-flavour oscillation probabilities
 1153 in vacuum and matter. Validation of the code is described in section A.5: the vacuum probabilities were validated
 1154 by comparing their values with those obtained from an alternative formulation in the PDG review. Several validation
 1155 checks of the probabilities in constant density matter are made as they are calculated, and the values of the probabilities
 1156 were checked by comparing them with those given by an independently-written program. Finally, an estimate of the
 1157 accuracy of the oscillation probabilities in matter is given in section A.6.

1158 *A.1. 3-flavour neutrino oscillation probabilities in vacuum*

1159 The 3-flavour neutrino oscillation probabilities in vacuum are calculated from equation 11 in [40]:

$$P(\nu_\alpha \rightarrow \nu_\beta) = \delta_{\alpha\beta} - 4 \sum_{i>j} \text{Re}(U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*) \sin^2 \left(\frac{\Delta m_{ij}^2 L}{4E} \right) + 2 \sum_{i>j} \text{Im}(U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*) \sin \left(\frac{\Delta m_{ij}^2 L}{2E} \right) \quad (10)$$

1160 In equation 10, $\Delta m_{ij}^2 = m_j^2 - m_i^2$, L is the distance from the neutrino target in Tokai to Super-K (295 km), E is the
 1161 neutrino energy, and U is the PMNS matrix in vacuum:

$$U = \begin{pmatrix} c_{12}c_{13} & c_{13}s_{12} & s_{13}e^{-i\delta} \\ -c_{23}s_{12} - s_{13}s_{23}c_{12}e^{i\delta} & c_{12}c_{23} - s_{12}s_{13}s_{23}e^{i\delta} & c_{13}s_{23} \\ s_{12}s_{23} - s_{13}c_{12}c_{23}e^{i\delta} & -s_{23}c_{12} - s_{12}c_{23}s_{13}e^{i\delta} & c_{13}c_{23} \end{pmatrix} \quad (11)$$

1162 with $s_{12} = \sin(\theta_{12})$, $c_{12} = \cos(\theta_{12})$, etc. $P(\bar{\nu}_\alpha \rightarrow \bar{\nu}_\beta)$ is calculated by changing the sign of the third term in equation
 1163 10 (this assumes that CPT is conserved).

1164 *A.2. 3-flavour neutrino oscillation probabilities in constant density matter*

1165 All three neutrino flavours undergo neutral-current interactions with protons, neutrons and electrons in matter.
 1166 These neutral-current interactions have identical amplitudes for all three flavours, and they produce no observable
 1167 effects on the probabilities of oscillation between one flavour and another. However the oscillation probabilities are
 1168 changed by coherent forward scattering of electron neutrinos in charged-current interactions with electrons in matter
 1169 [40].

1170 Using natural units with $\hbar = c = 1$, the time evolution of neutrino flavour states in vacuum is described by the
 1171 Schrödinger equation:

$$i \frac{\partial \psi}{\partial t} = H_F \psi \quad (12)$$

1172 where

$$\psi = \begin{pmatrix} \psi_e \\ \psi_\mu \\ \psi_\tau \end{pmatrix} \quad (13)$$

1173 and H_F is the effective Hamiltonian in the flavour-state basis

$$H_F = \frac{1}{2E} U M U^\dagger \quad (14)$$

1174 with M defined by

$$M = \begin{pmatrix} 0 & 0 & 0 \\ 0 & \Delta m_{21}^2 & 0 \\ 0 & 0 & \Delta m_{31}^2 \end{pmatrix} \quad (15)$$

1175 The calculation of oscillation probabilities requires neutrino flight time to be converted to distance travelled, and this
 1176 conversion assumes that neutrinos are highly relativistic. In this calculation, UMU^\dagger is used for neutrinos, but its
 1177 complex conjugate is used for antineutrinos. For neutrinos, the effects of the charged-current interactions between
 1178 electron neutrinos and electrons are taken into account by adding the potential $2E\sqrt{2}G_F N_e$ to the real part of the first
 1179 diagonal element of UMU^\dagger , where E is the neutrino energy, G_F is the Fermi coupling constant, and N_e is the number
 1180 density of electrons in matter. For antineutrinos, this potential is subtracted from the real part of the first diagonal
 1181 element of the complex conjugate of UMU^\dagger (for further details see section 9.2 in [41]).

1182 After the addition or subtraction of this potential, UMU^\dagger (or its complex conjugate) is diagonalised. The eigen-
 1183 values of a Hermitian matrix are always real; they are calculated by solving the (cubic) characteristic equation using
 1184 the method of del Ferro, Tartaglia and Cardano as described in [42]. The differences between the eigenvalues are the
 1185 effective mass-squared differences in matter. The eigenvectors are calculated using an algebraic method: one of the
 1186 components is set to be 1.0 (real), and the other two components are calculated using two of the three simultaneous
 1187 equations in $UMU^\dagger - \lambda I = 0$, where the λ are the eigenvalues. After being normalised, the three eigenvectors become
 1188 the columns of the effective mixing matrix in matter.

1189 The initial flavour state of the neutrino is represented by a 1×3 column vector whose entries are complex; if, for
 1190 example, the initial flavour state is a muon neutrino, this column vector is

$$\begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix}$$

1191 The vector representing the initial flavour state is then multiplied by the Hermitian conjugate of the matter mixing
 1192 matrix to convert it to another 1×3 complex column vector representing the initial mass states. These mass states are
 1193 propagated to Super-K by multiplying the j th initial mass state by $\exp\left(\frac{-i\Delta m_{j1}^2 L}{2E}\right)$, where the Δm_{j1}^2 are the mass-
 1194 squared differences in matter, i.e. the differences between the eigenvalues of UMU^\dagger . This gives a new 1×3 complex
 1195 column vector representing the final mass states, and these are converted to the final flavour states by multiplying by the
 1196 matter mixing matrix. The entries of the resulting 1×3 complex column vector represent the amplitudes of each flavour
 1197 at Super-K, and the corresponding oscillation probabilities are calculated as the moduli squared of these amplitudes.

1198 A.3. Inputs to the 3-flavour neutrino oscillation probability calculations

1199 When calculating the 3-flavour oscillation probabilities, the mixing angles can be input either in the form $\sin^2(2\theta_{ij})$
 1200 or as $\sin^2(\theta_{ij})$. $\sin(\theta_{ij})$ and $\cos(\theta_{ij})$ are calculated from the input values, and these are used in turn to calculate the
 1201 elements of U . The “solar” mass-squared difference is input as Δm_{21}^2 , and this is > 0 for both mass hierarchies. The
 1202 “atmospheric” mass-squared difference is input either as $|\Delta m_{32}^2|$ or using a definition introduced by G. Fogli, E. Lisi
 1203 et al. in [?]:

$$\Delta m_{FL}^2 = m_3^2 - \frac{m_2^2 + m_1^2}{2} \quad (16)$$

1204 The quantity denoted Δm_{FL}^2 is useful since its absolute value is the same for both mass hierarchies, and only its sign
 1205 changes. If the atmospheric mass-squared difference is input as Δm_{32}^2 , the mass hierarchy is set using the sign of
 1206 Δm_{32}^2 ; this is positive for the normal mass hierarchy (NH) and negative for the inverted mass hierarchy (IH). In this
 1207 case, Δm_{31}^2 is not input but is calculated as $\Delta m_{31}^2 = \Delta m_{21}^2 + \Delta m_{32}^2$ for both hierarchies. If the atmospheric mass-
 1208 squared difference is input as Δm_{FL}^2 , the mass hierarchy is set using the sign of Δm_{FL}^2 . Then Δm_{32}^2 and Δm_{31}^2 are
 1209 calculated from the input values of Δm_{FL}^2 and Δm_{21}^2 .

1210 A.4. Results of the 3-flavour neutrino oscillation probability calculations

1211 A comparison of 2-flavour and 3-flavour (in matter) ν_μ -survival probabilities is given in figure 117. In this figure,
 1212 the nominal probabilities are calculated with $\sin^2(2\theta_{12}) = 0.87$, $\sin^2(2\theta_{13}) = 0.1$, $\sin^2(2\theta_{23}) = 1.0$, $\Delta m_{21}^2 = 7.6$
 1213 $\times 10^{-5}$ eV 2 /c 4 , $|\Delta m_{32}^2| = 2.32 \times 10^{-3}$ eV 2 /c 4 , $\delta_{CP} = 0$ and Earth crust density = 2.6 g/cm 3 . The bands represent
 1214 the maximum and minimum 3-flavour probabilities from 4000 random variations of the non-23 oscillation parameters
 1215 within their uncertainties at each energy with the same values of $\sin^2(2\theta_{23})$ and $|\Delta m_{32}^2|$ being used. The uncertainties
 1216 in $\sin^2(2\theta_{12})$ and Δm_{21}^2 are taken from KamLAND combined with solar experiments [34], while those in $\sin^2(2\theta_{13})$
 1217 are computed as a weighted average of measurements from Daya Bay [35] and Reno [36].

1218 The effect of $\sin^2(2\theta_{13})$ on the 3-flavour ν_μ -survival probability in matter is shown in figure 118: there is a small
 1219 increase in $P(\nu_\mu \rightarrow \nu_\mu)$ at all energies as $\sin^2(2\theta_{13})$ increases. Also shown in figure 119 is the effect of δ_{CP} on the

Energy (GeV)	$P(\nu_\mu \rightarrow \nu_\mu)$ for $\sin^2(2\theta_{12})$ $= 0.870,$ $\Delta m_{21}^2 =$ $7.6 \times 10^{-5} \text{ eV}^2/\text{c}^4$	$P(\nu_\mu \rightarrow \nu_\mu)$ for $\sin^2(2\theta_{12})$ $= 0.906,$ $\Delta m_{21}^2 =$ $7.6 \times 10^{-5} \text{ eV}^2/\text{c}^4$	$P(\nu_\mu \rightarrow \nu_\mu)$ for $\sin^2(2\theta_{12})$ $= 0.833,$ $\Delta m_{21}^2 =$ $7.6 \times 10^{-5} \text{ eV}^2/\text{c}^4$	$P(\nu_\mu \rightarrow \nu_\mu)$ for $\sin^2(2\theta_{12})$ $= 0.870,$ $\Delta m_{21}^2 =$ $7.8 \times 10^{-5} \text{ eV}^2/\text{c}^4$	$P(\nu_\mu \rightarrow \nu_\mu)$ for $\sin^2(2\theta_{12})$ $= 0.870,$ $\Delta m_{21}^2 =$ $7.4 \times 10^{-5} \text{ eV}^2/\text{c}^4$
0.3	0.95703	0.95809	0.95608	0.95733	0.95674
0.4	0.35053	0.35247	0.34877	0.35135	0.34971
0.5	0.037395	0.038009	0.036842	0.037663	0.037129
0.6	0.010963	0.010692	0.011212	0.010841	0.011086
0.7	0.094387	0.093711	0.095004	0.094083	0.094691
0.8	0.20453	0.20371	0.20528	0.20416	0.20490
0.9	0.31099	0.31015	0.31175	0.31061	0.31137
1.0	0.40463	0.40383	0.40535	0.40427	0.40499
1.1	0.48414	0.48340	0.48481	0.48380	0.48447
1.2	0.55080	0.55013	0.55141	0.55050	0.55111
1.3	0.60656	0.60594	0.60711	0.60628	0.60683
1.4	0.65329	0.65274	0.65380	0.65304	0.65354
1.5	0.69265	0.69215	0.69311	0.69243	0.69288
1.6	0.72599	0.72554	0.72640	0.72579	0.72620
1.7	0.75440	0.75399	0.75478	0.75421	0.75459
1.8	0.77876	0.77839	0.77910	0.77859	0.77893
1.9	0.79978	0.79943	0.80009	0.79962	0.79993
2.0	0.81801	0.81770	0.81830	0.81787	0.81815

Table 15: Effects of uncertainties in $\sin^2(2\theta_{12})$ and Δm_{21}^2 on the 3-flavour $P(\nu_\mu \rightarrow \nu_\mu)$ in matter; this is for the normal mass hierarchy, $\sin^2(2\theta_{23}) = 1.0$, $|\Delta m_{32}^2| = 2.32 \times 10^{-3} \text{ eV}^2/\text{c}^4$, $\sin^2(2\theta_{13}) = 0.1$ and $\delta_{CP} = 0$.

1220 3-flavour ν_μ -survival probability in matter: as δ_{CP} increases from 0 to π , $P(\nu_\mu \rightarrow \nu_\mu)$ increases above the oscillation
1221 maximum and decreases below it for the NH, with these changes being reversed for the IH. The effects of uncertainties
1222 in $\sin^2(2\theta_{12})$ and Δm_{21}^2 on the 3-flavour $P(\nu_\mu \rightarrow \nu_\mu)$ in matter are shown for the NH in table 15. At 0.6 GeV,
1223 uncertainties in $\sin^2(2\theta_{12})$ change $P(\nu_\mu \rightarrow \nu_\mu)$ by ≈ 0.00025 and uncertainties in Δm_{21}^2 change it by ≈ 0.0001 .

1224 For the NH, the 3-flavour $P(\nu_\mu \rightarrow \nu_\mu)$ is increased below the oscillation maximum and decreased above it compared
1225 with the 2-flavour probability, while for the IH these changes are reversed. The oscillation maximum is at lower energy
1226 for the IH than for the NH, and this can be understood more easily by considering the vacuum probabilities. In
1227 equation 10, the imaginary terms are zero if $\alpha = \beta$, and only the 3 real terms contribute to the vacuum $P(\nu_\mu \rightarrow \nu_\mu)$.
1228 If the atmospheric mass-squared difference is input as Δm_{32}^2 , the terms $|U_{\mu 1}|^2$, $|U_{\mu 2}|^2$, $|U_{\mu 3}|^2$, $\sin^2\left(\frac{\Delta m_{21}^2 L}{4E}\right)$ and
1229 $\sin^2\left(\frac{\Delta m_{32}^2 L}{4E}\right)$ are identical for the two hierarchies, and the only term that changes between them is $\sin^2\left(\frac{\Delta m_{31}^2 L}{4E}\right)$.
1230 Since Δm_{31}^2 is lower for the IH than for the NH, $\sin^2\left(\frac{\Delta m_{31}^2 L}{4E}\right)$ has its maximum at a lower energy for the IH than for
1231 the NH. The vacuum $P(\nu_\mu \rightarrow \nu_\mu)$ depends on $1 - 4 |U_{\mu 1}|^2 |U_{\mu 3}|^2 \sin^2\left(\frac{\Delta m_{31}^2 L}{4E}\right)$, which means that its minimum is at a
1232 lower energy for the IH than for the NH.

1233 Referring to the bands in figure 117, the highest ν_μ -survival probabilities for the NH are for low values of $\sin^2(2\theta_{12})$,
1234 high values of $\sin^2(2\theta_{13})$ and δ_{CP} near π above the oscillation maximum, while below the maximum they are for high
1235 values of $\sin^2(2\theta_{12})$ and $\sin^2(2\theta_{13})$ and δ_{CP} near 0. For the IH, the highest probabilities are for high values of
1236 $\sin^2(2\theta_{12})$ and $\sin^2(2\theta_{13})$ and δ_{CP} near 0 above the oscillation maximum, but for low values of $\sin^2(2\theta_{12})$, high
1237 values of $\sin^2(2\theta_{13})$ and δ_{CP} near π below it.

1238 Comparisons of ν_μ oscillation probabilities in vacuum and matter are given for the NH in table 16 and for the
1239 IH in table 17. At 0.6 GeV, $P(\nu_\mu \rightarrow \nu_e)$ is increased by ≈ 0.004 and $P(\nu_\mu \rightarrow \nu_\tau)$ is decreased by ≈ 0.004 in matter
1240 compared with vacuum for the NH, while for the IH the changes are once more reversed. The ν_μ -survival probability is
1241 relatively unaffected by the passage of ν_μ through matter, and is changed by only ≈ 0.0001 compared with the vacuum
1242 probability at 0.6 GeV.

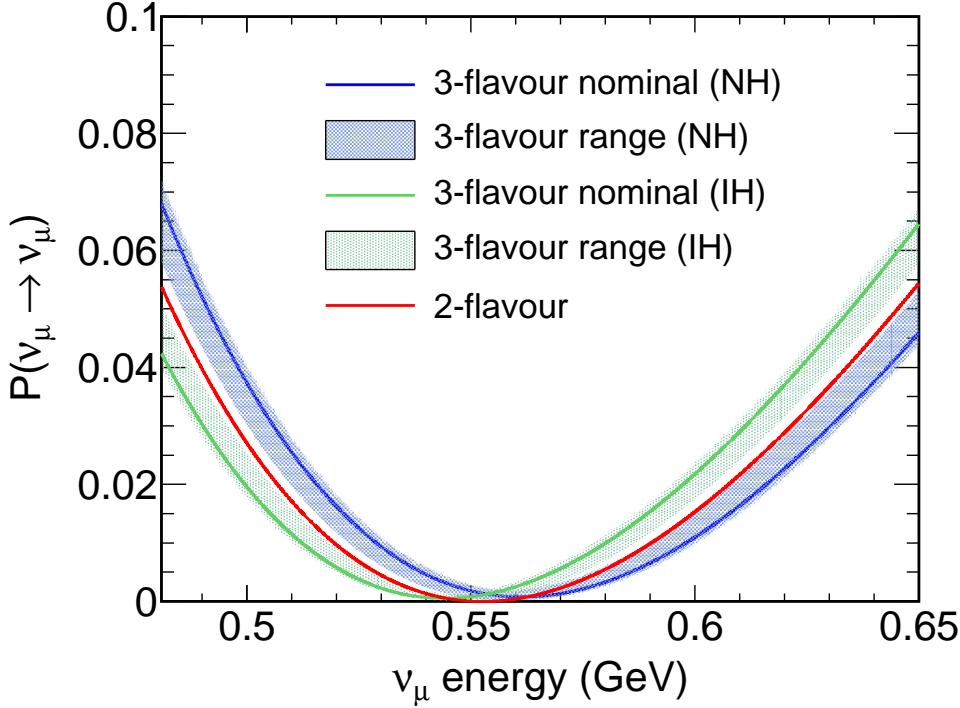


Figure 117: Comparison of $P(\nu_\mu \rightarrow \nu_\mu)$ for 2-flavour and 3-flavour (in matter) oscillations, NH = normal mass hierarchy, IH = inverted mass hierarchy. The nominal probabilities are calculated with $\sin^2(2\theta_{12}) = 0.87$, $\sin^2(2\theta_{13}) = 0.1$, $\sin^2(2\theta_{23}) = 1.0$, $\Delta m_{21}^2 = 7.6 \times 10^{-5} \text{ eV}^2/c^4$, $|\Delta m_{32}^2| = 2.32 \times 10^{-3} \text{ eV}^2/c^4$, $\delta_{CP} = 0$ and Earth crust density = 2.6 g/cm^3 . The bands represent the maximum and minimum 3-flavour probabilities from 4000 random variations of the non-23 oscillation parameters within their uncertainties at each energy with the same values of $\sin^2(2\theta_{23})$ and $|\Delta m_{32}^2|$ being used.

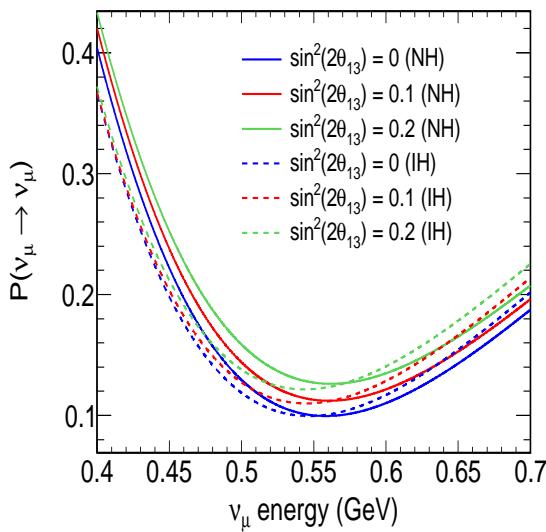


Figure 118: Effect of $\sin^2(2\theta_{13})$ on $P(\nu_\mu \rightarrow \nu_\mu)$ for 3-flavour oscillations in matter; NH = normal mass hierarchy, IH = inverted mass hierarchy, $\sin^2(2\theta_{12}) = 0.87$, $\sin^2(2\theta_{23}) = 1.0$, $\Delta m_{21}^2 = 7.6 \times 10^{-5} \text{ eV}^2/c^4$, $|\Delta m_{32}^2| = 2.32 \times 10^{-3} \text{ eV}^2/c^4$, $\delta_{CP} = 0$ and Earth crust density = 2.6 g/cm^3 .

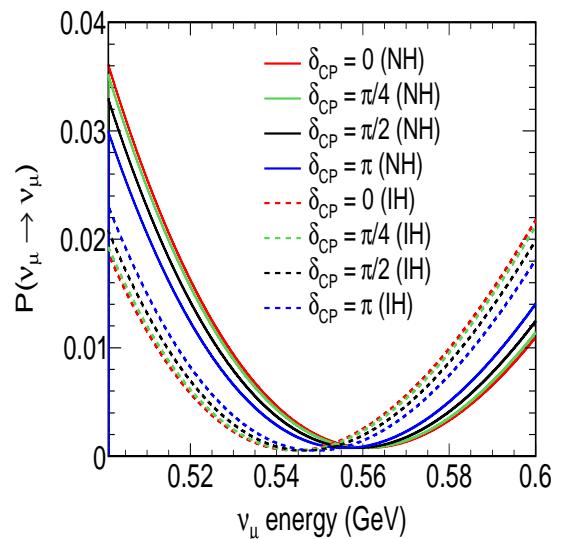


Figure 119: Effect of δ_{CP} on $P(\nu_\mu \rightarrow \nu_\mu)$ for 3-flavour oscillations in matter; NH = normal mass hierarchy, IH = inverted mass hierarchy, $\sin^2(2\theta_{12}) = 0.87$, $\sin^2(2\theta_{13}) = 0.1$, $\sin^2(2\theta_{23}) = 1.0$, $\Delta m_{21}^2 = 7.6 \times 10^{-5} \text{ eV}^2/c^4$, $|\Delta m_{32}^2| = 2.32 \times 10^{-3} \text{ eV}^2/c^4$ and Earth crust density = 2.6 g/cm^3 .

Energy (GeV)	P($\nu_\mu \rightarrow \nu_e$)		P($\nu_\mu \rightarrow \nu_\mu$)		P($\nu_\mu \rightarrow \nu_\tau$)	
	Vacuum	Matter	Vacuum	Matter	Vacuum	Matter
0.3	0.00054403	0.00016981	0.95496	0.95703	0.044501	0.042796
0.4	0.024253	0.029051	0.34954	0.35053	0.62621	0.62042
0.5	0.046291	0.051402	0.037071	0.037395	0.91664	0.91120
0.6	0.051975	0.056108	0.010883	0.010963	0.93714	0.93293
0.7	0.049739	0.052871	0.094385	0.094387	0.85588	0.85274
0.8	0.044830	0.047181	0.20455	0.20453	0.75062	0.74829
0.9	0.039478	0.041256	0.31101	0.31099	0.64951	0.64776
1.0	0.034502	0.035865	0.40464	0.40463	0.56085	0.55951
1.1	0.030139	0.031200	0.48415	0.48414	0.48571	0.48466
1.2	0.026403	0.027241	0.55081	0.55080	0.42279	0.42196
1.3	0.023233	0.023905	0.60656	0.60656	0.37021	0.36954
1.4	0.020548	0.021093	0.65329	0.65329	0.32616	0.32562
1.5	0.018268	0.018715	0.69266	0.69266	0.28908	0.28863
1.6	0.016325	0.016696	0.72599	0.72599	0.25769	0.25731
1.7	0.014661	0.014971	0.75440	0.75440	0.23094	0.23063
1.8	0.013228	0.013491	0.77876	0.77876	0.20801	0.20775
1.9	0.011988	0.012211	0.79977	0.79978	0.18824	0.18801
2.0	0.010908	0.011100	0.81801	0.81801	0.17108	0.17089

Table 16: Comparison of ν_μ oscillation probabilities in vacuum and matter for the normal mass hierarchy, Earth crust density = 2.6 g/cm³, $\sin^2(2\theta_{12}) = 0.87$, $\sin^2(2\theta_{13}) = 0.1$, $\sin^2(2\theta_{23}) = 1.0$, $\Delta m_{21}^2 = 7.6 \times 10^{-5}$ eV²/c⁴, $|\Delta m_{32}^2| = 2.32 \times 10^{-3}$ eV²/c⁴ and $\delta_{CP} = 0$.

Energy (GeV)	P($\nu_\mu \rightarrow \nu_e$)		P($\nu_\mu \rightarrow \nu_\mu$)		P($\nu_\mu \rightarrow \nu_\tau$)	
	Vacuum	Matter	Vacuum	Matter	Vacuum	Matter
0.3	0.016651	0.012718	0.91243	0.91427	0.070915	0.073016
0.4	0.047961	0.041880	0.28695	0.28747	0.66509	0.67065
0.5	0.052910	0.047892	0.019598	0.019587	0.92749	0.93252
0.6	0.047803	0.044104	0.021900	0.021756	0.93030	0.93414
0.7	0.040787	0.038101	0.11802	0.11787	0.84120	0.84403
0.8	0.034297	0.032325	0.23236	0.23222	0.73335	0.73545
0.9	0.028857	0.027381	0.33905	0.33895	0.63210	0.63367
1.0	0.024433	0.023306	0.43123	0.43115	0.54434	0.54555
1.1	0.020858	0.019980	0.50865	0.50859	0.47049	0.47143
1.2	0.017960	0.017265	0.57310	0.57305	0.40894	0.40969
1.3	0.015595	0.015037	0.62672	0.62669	0.35768	0.35828
1.4	0.013649	0.013194	0.67151	0.67148	0.31485	0.31533
1.5	0.012034	0.011657	0.70911	0.70909	0.27886	0.27926
1.6	0.010681	0.010366	0.74089	0.74087	0.24843	0.24876
1.7	0.0095379	0.0092726	0.76792	0.76791	0.22254	0.22282
1.8	0.0085654	0.0083395	0.79107	0.79105	0.20037	0.20061
1.9	0.0077316	0.0075376	0.81101	0.81010	0.18126	0.18146
2.0	0.0070119	0.0068441	0.82829	0.82829	0.16470	0.16487

Table 17: Comparison of ν_μ oscillation probabilities in vacuum and matter for the inverted mass hierarchy, Earth crust density = 2.6 g/cm³, $\sin^2(2\theta_{12}) = 0.87$, $\sin^2(2\theta_{13}) = 0.1$, $\sin^2(2\theta_{23}) = 1.0$, $\Delta m_{21}^2 = 7.6 \times 10^{-5}$ eV²/c⁴, $|\Delta m_{32}^2| = 2.32 \times 10^{-3}$ eV²/c⁴ and $\delta_{CP} = 0$.

1243 A.5. Validation of the 3-flavour oscillation probabilities

1244 The 3-flavour oscillation probabilities in vacuum were checked using an alternative formulation in equations 13.13
 1245 and 13.14 in the PDG review [21]:

$$P(\nu_\alpha \rightarrow \nu_\beta) = \sum_j |U_{\beta j}|^2 |U_{\alpha j}|^2 + 2 \sum_{j>k} |U_{\beta j} U_{\alpha j}^* U_{\alpha k} U_{\beta k}^*| \cos \left(\frac{\Delta m_{jk}^2 L}{2E} - \phi_{\beta\alpha;jk} \right) \quad (17)$$

1246 where $\phi_{\beta\alpha;jk} = \arg(U_{\beta j} U_{\alpha j}^* U_{\alpha k} U_{\beta k}^*)$. $P(\bar{\nu}_\alpha \rightarrow \bar{\nu}_\beta)$ is calculated by changing the sign of $\phi_{\beta\alpha;jk}$ in the argument of the
 1247 cosine. The probabilities calculated from equation 17 agreed with those calculated from equation 10 to 14 significant
 1248 figures.

1249 Several checks of the oscillation probabilities in constant density matter are written into the code that calculates
 1250 them:

- 1251 1. The eigenvalues of UMU^\dagger are checked by comparing their sum with the trace of the matrix.
- 1252 2. Each normalised eigenvector is multiplied in turn by each of the 3 matrices formed by subtracting the eigenvalues
 1253 from the real parts of the diagonal elements of UMU^\dagger , and a check is made of the differences between these
 1254 products and a zero vector.
- 1255 3. A check is made that the normalised eigenvectors of UMU^\dagger are orthogonal by calculating the scalar product
 1256 between them (the scalar product of two complex vectors is the product of the first vector with the complex
 1257 conjugate of the second vector).
- 1258 4. A check is also made that the Hermitian conjugate of the mixing matrix in matter is equal to the inverse of the
 1259 matrix. This is done by multiplying the mixing matrix in matter by its Hermitian conjugate, and checking the
 1260 differences between the product and an identity matrix.

1261 The values of the oscillation probabilities in constant density matter were checked by comparing them with equivalent
 1262 probabilities calculated by an independently-written Fortran program [43]. This Fortran program uses different
 1263 algorithms, and calculates numerically the eigenvalues and eigenvectors of UMU^\dagger . Nevertheless there was very good
 1264 agreement between the two calculations of the probabilities, with the fractional differences being $\approx 2 \times 10^{-6}$.

1265 The values of the matter oscillation probabilities were also compared with those given by Prob3++ [44], and the
 1266 fractional differences were $\approx 1.5 \times 10^{-4}$. The comparison plots can be seen in the next Appendix.

1267 A.6. Accuracy of the 3-flavour oscillation probabilities

1268 As stated in section A.5, the 3-flavour oscillation probabilities in vacuum agreed to 14 significant figures between
 1269 the two formulations.

1270 An estimate of the accuracy of the 3-flavour oscillation probabilities in constant density matter was made in three
 1271 separate ways:

- 1272 1. The matter probabilities for zero density were compared with the vacuum probabilities; there was good agree-
 1273 ment, with the fractional differences being $\approx 2.5 \times 10^{-6}$.
- 1274 2. The probabilities given when calculating the eigenvectors with simultaneous equations 1 and 2 in $UMU^\dagger - \lambda I =$
 1275 0 were compared with the probabilities given when calculating the eigenvectors with simultaneous equations 2
 1276 and 3. The fractional differences between these two calculations were again $\approx 2.5 \times 10^{-6}$.
- 1277 3. The sum of three matter probabilities, for example $P(\nu_\mu \rightarrow \nu_e) + P(\nu_\mu \rightarrow \nu_\mu) + P(\nu_\mu \rightarrow \nu_\tau)$, was compared
 1278 with 1.0; again there was good agreement, and the differences were $\approx 2 \times 10^{-6}$.

1279 This means that the matter oscillation probabilities should be considered to be accurate to 5 decimal places. The
 1280 accuracy of the matter probabilities is less than that of the vacuum probabilities due to the method of calculation of the
 1281 eigenvectors. This involves calculations of the form

$$\frac{(ab - cd)}{(ef - gh)}$$

1282 where a, b, c, etc. are elements of $UMU^\dagger - \lambda I$. Frequently ab is close in value to cd, which means that (ab - cd) is
 1283 much smaller than ab or cd, and the same applies to (ef - gh). However the advantage of the method of calculation
 1284 of the eigenvectors described in section A.2 is that it allows the worst of these cancellation errors to be avoided; this
 1285 can be done by calculating the eigenvectors using different pairs of simultaneous equations in $UMU^\dagger - \lambda I = 0$ for

₁₂₈₆ different combinations of the oscillation parameters. In practice, the eigenvectors are nearly always calculated using
₁₂₈₇ equations 1 and 2 in $UMU^\dagger - \lambda I = 0$, but equations 2 and 3 are used when $3.10 < \delta_{CP} < 3.18$ and $\sin^2(2\theta_{13}) >$
₁₂₈₈ 10^{-8} in order to avoid such cancellation errors.

B. Detailed comparison of VaLOR and Prob3++ oscillation probabilities

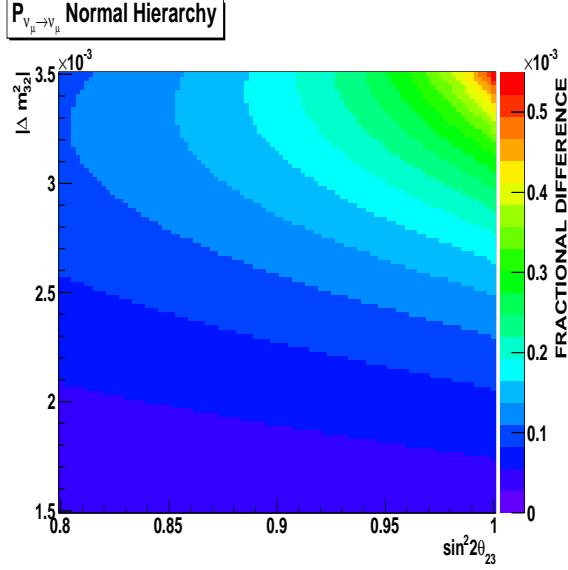


Figure 120: Comparison of the VaLOR $\nu_\mu \rightarrow \nu_\mu$ oscillation probabilities in matter with those obtained from Prob3++ as a function of $\sin^2 2\theta_{23}$ and $|\Delta m_{32}^2|$ for $E_\nu = 1$ GeV; normal mass hierarchy, $\sin^2 2\theta_{13} = 0.1$, $\sin^2 2\theta_{12} = 0.8704$, $\Delta m_{21}^2 = 7.6 \times 10^{-5}$ eV $^2/c^4$, $\delta_{CP} = 0$ and Earth crust density = 2.6 g/cm 3 .

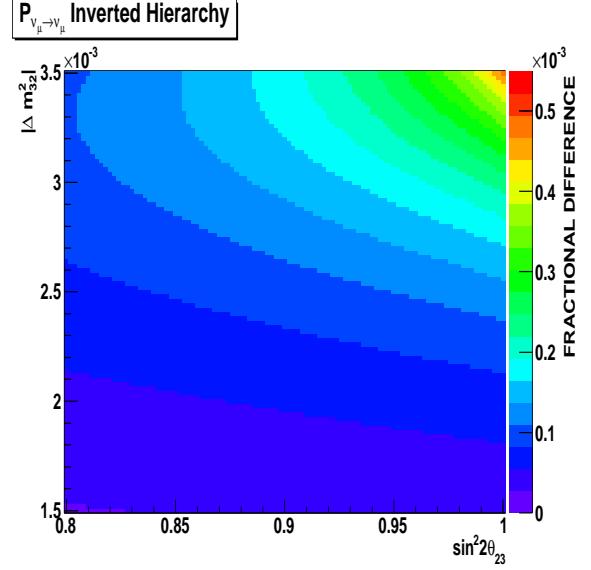


Figure 121: Comparison of the VaLOR $\nu_\mu \rightarrow \nu_\mu$ oscillation probabilities in matter with those obtained from Prob3++ as a function of $\sin^2 2\theta_{23}$ and $|\Delta m_{32}^2|$ for $E_\nu = 1$ GeV; inverted mass hierarchy, $\sin^2 2\theta_{13} = 0.1$, $\sin^2 2\theta_{12} = 0.8704$, $\Delta m_{21}^2 = 7.6 \times 10^{-5}$ eV $^2/c^4$, $\delta_{CP} = 0$ and Earth crust density = 2.6 g/cm 3 .

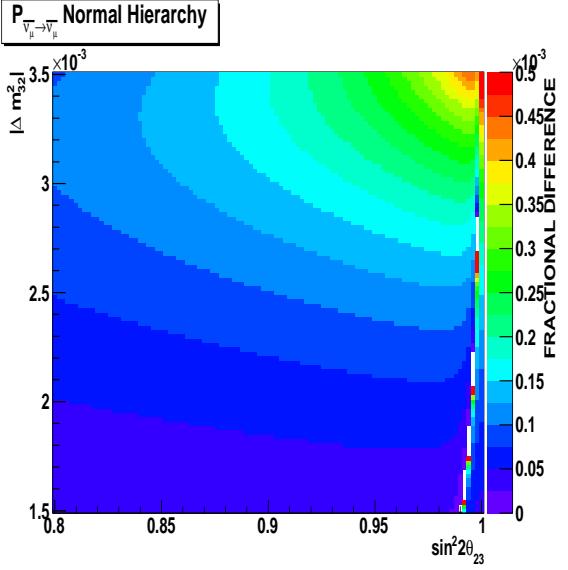


Figure 122: Comparison of the VaLOR $\bar{\nu}_\mu \rightarrow \bar{\nu}_\mu$ oscillation probabilities in matter with those obtained from Prob3++ as a function of $\sin^2 2\theta_{23}$ and $|\Delta m_{32}^2|$ for $E_\nu = 1$ GeV; normal mass hierarchy, $\sin^2 2\theta_{13} = 0.1$, $\sin^2 2\theta_{12} = 0.8704$, $\Delta m_{21}^2 = 7.6 \times 10^{-5}$ eV $^2/c^4$, $\delta_{CP} = 0$ and Earth crust density = 2.6 g/cm 3 .

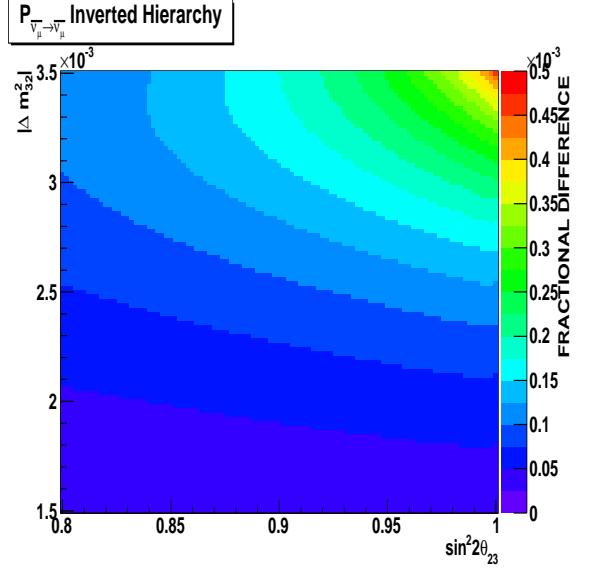


Figure 123: Comparison of the VaLOR $\bar{\nu}_\mu \rightarrow \bar{\nu}_\mu$ oscillation probabilities in matter with those obtained from Prob3++ as a function of $\sin^2 2\theta_{23}$ and $|\Delta m_{32}^2|$ for $E_\nu = 1$ GeV; inverted mass hierarchy, $\sin^2 2\theta_{13} = 0.1$, $\sin^2 2\theta_{12} = 0.8704$, $\Delta m_{21}^2 = 7.6 \times 10^{-5}$ eV $^2/c^4$, $\delta_{CP} = 0$ and Earth crust density = 2.6 g/cm 3 .

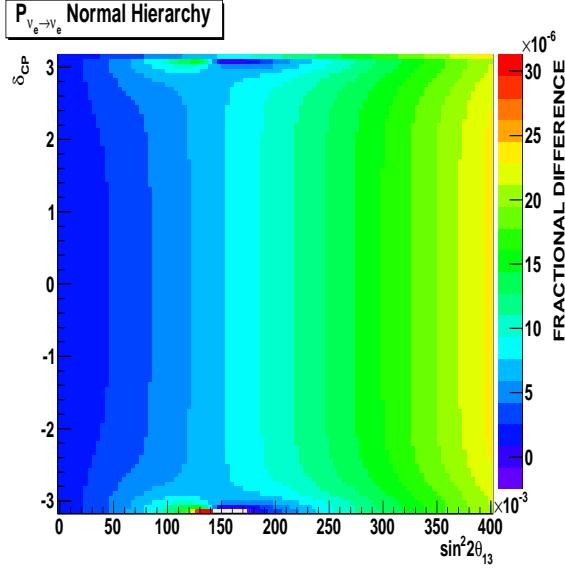


Figure 124: Comparison of the VaLOR $\nu_e \rightarrow \nu_e$ oscillation probabilities in matter with those obtained from Prob3++ as a function of $\sin^2 2\theta_{13}$ and δ_{CP} for $E_\nu = 1$ GeV; normal mass hierarchy, $\sin^2 2\theta_{23} = 1.0$, $|\Delta m_{32}^2| = 2.4 \times 10^{-3}$ eV $^2/c^4$, $\sin^2 2\theta_{12} = 0.8704$, $\Delta m_{21}^2 = 7.6 \times 10^{-5}$ eV $^2/c^4$ and Earth crust density = 2.6 g/cm 3 .

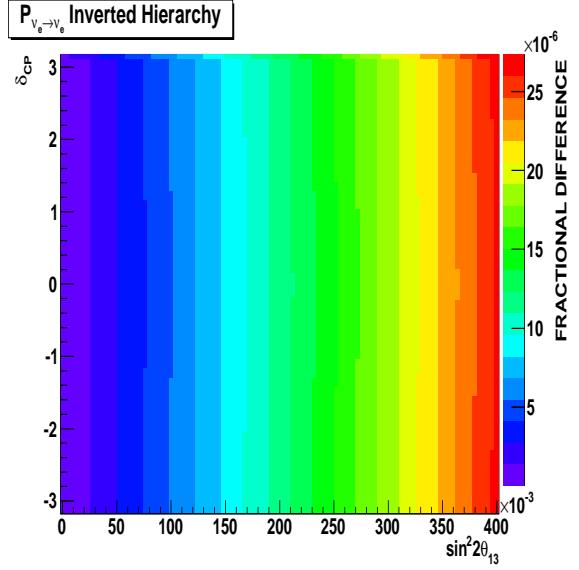


Figure 125: Comparison of the VaLOR $\nu_e \rightarrow \nu_e$ oscillation probabilities in matter with those obtained from Prob3++ as a function of $\sin^2 2\theta_{13}$ and δ_{CP} for $E_\nu = 1$ GeV; inverted mass hierarchy, $\sin^2 2\theta_{23} = 1.0$, $|\Delta m_{32}^2| = 2.4 \times 10^{-3}$ eV $^2/c^4$, $\sin^2 2\theta_{12} = 0.8704$, $\Delta m_{21}^2 = 7.6 \times 10^{-5}$ eV $^2/c^4$ and Earth crust density = 2.6 g/cm 3 .

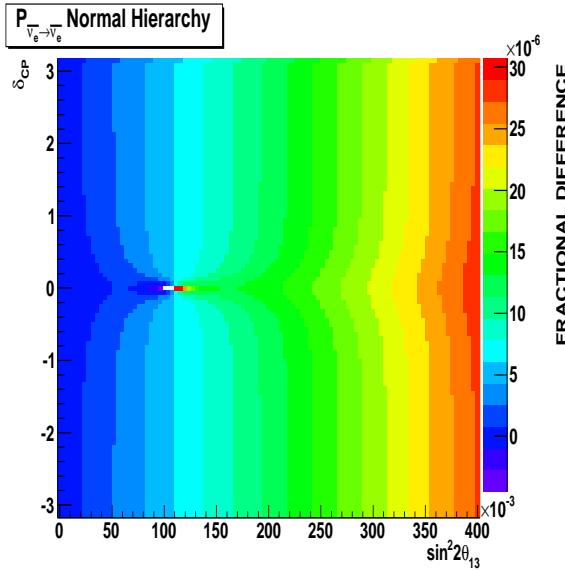


Figure 126: Comparison of the VaLOR $\bar{\nu}_e \rightarrow \bar{\nu}_e$ oscillation probabilities in matter with those obtained from Prob3++ as a function of $\sin^2 2\theta_{13}$ and δ_{CP} for $E_\nu = 1$ GeV; normal mass hierarchy, $\sin^2 2\theta_{23} = 1.0$, $|\Delta m_{32}^2| = 2.4 \times 10^{-3}$ eV $^2/c^4$, $\sin^2 2\theta_{12} = 0.8704$, $\Delta m_{21}^2 = 7.6 \times 10^{-5}$ eV $^2/c^4$ and Earth crust density = 2.6 g/cm 3 .

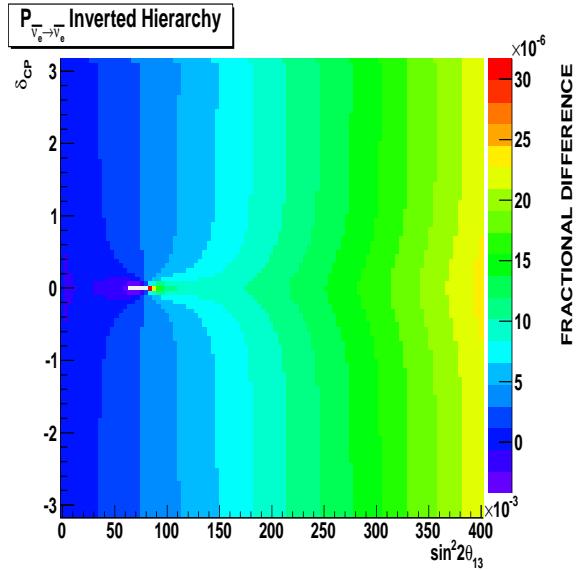


Figure 127: Comparison of the VaLOR $\bar{\nu}_e \rightarrow \bar{\nu}_e$ oscillation probabilities in matter with those obtained from Prob3++ as a function of $\sin^2 2\theta_{13}$ and δ_{CP} for $E_\nu = 1$ GeV; inverted mass hierarchy, $\sin^2 2\theta_{23} = 1.0$, $|\Delta m_{32}^2| = 2.4 \times 10^{-3}$ eV $^2/c^4$, $\sin^2 2\theta_{12} = 0.8704$, $\Delta m_{21}^2 = 7.6 \times 10^{-5}$ eV $^2/c^4$ and Earth crust density = 2.6 g/cm 3 .

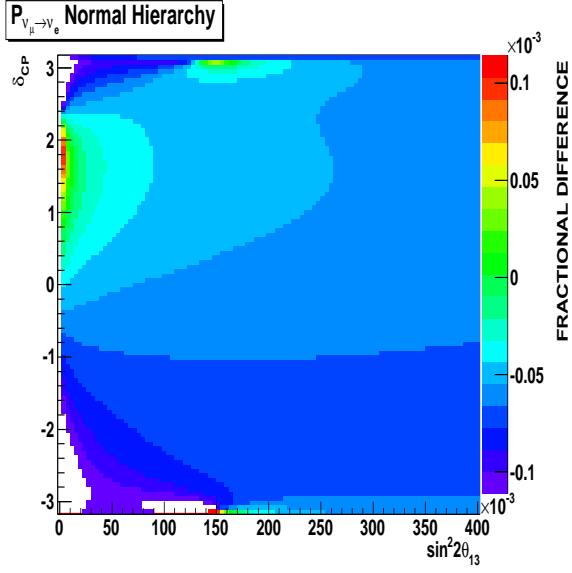


Figure 128: Comparison of the VaLOR $\nu_\mu \rightarrow \nu_e$ oscillation probabilities in matter with those obtained from Prob3++ as a function of $\sin^2 2\theta_{13}$ and δ_{CP} for $E_\nu = 1$ GeV; normal mass hierarchy, $\sin^2 2\theta_{23} = 1.0$, $|\Delta m_{32}^2| = 2.4 \times 10^{-3}$ eV $^2/c^4$, $\sin^2 2\theta_{12} = 0.8704$, $\Delta m_{21}^2 = 7.6 \times 10^{-5}$ eV $^2/c^4$ and Earth crust density = 2.6 g/cm 3 .

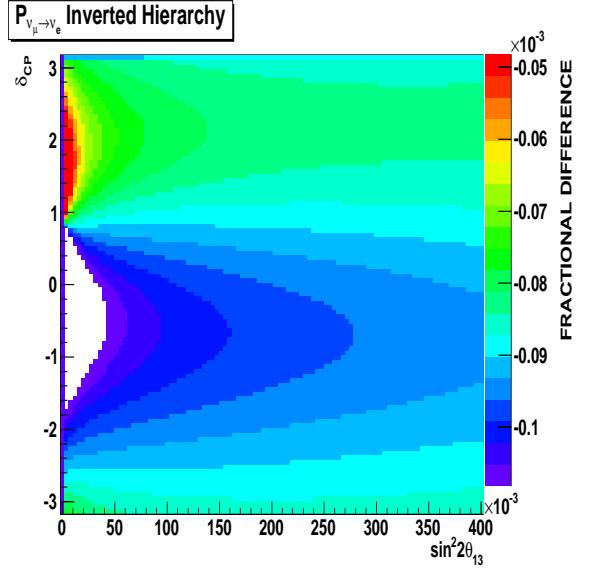


Figure 129: Comparison of the VaLOR $\nu_\mu \rightarrow \nu_e$ oscillation probabilities in matter with those obtained from Prob3++ as a function of $\sin^2 2\theta_{13}$ and δ_{CP} for $E_\nu = 1$ GeV; inverted mass hierarchy, $\sin^2 2\theta_{23} = 1.0$, $|\Delta m_{32}^2| = 2.4 \times 10^{-3}$ eV $^2/c^4$, $\sin^2 2\theta_{12} = 0.8704$, $\Delta m_{21}^2 = 7.6 \times 10^{-5}$ eV $^2/c^4$ and Earth crust density = 2.6 g/cm 3 .

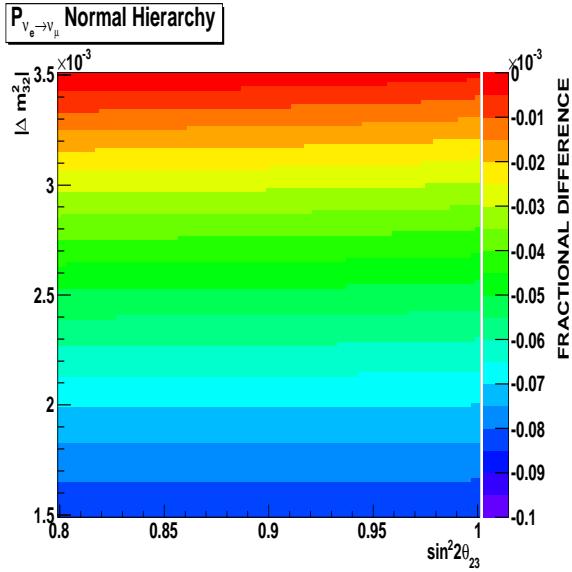


Figure 130: Comparison of the VaLOR $\nu_e \rightarrow \nu_\mu$ oscillation probabilities in matter with those obtained from Prob3++ as a function of $\sin^2 2\theta_{23}$ and $|\Delta m_{32}^2|$ for $E_\nu = 1$ GeV; normal mass hierarchy, $\sin^2 2\theta_{13} = 0.1$, $\sin^2 2\theta_{12} = 0.8704$, $\Delta m_{21}^2 = 7.6 \times 10^{-5}$ eV $^2/c^4$, $\delta_{CP} = 0$ and Earth crust density = 2.6 g/cm 3 .

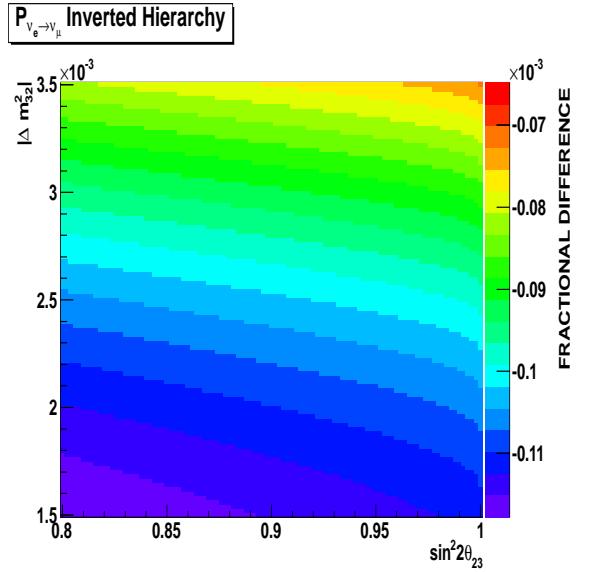


Figure 131: Comparison of the VaLOR $\nu_e \rightarrow \nu_\mu$ oscillation probabilities in matter with those obtained from Prob3++ as a function of $\sin^2 2\theta_{23}$ and $|\Delta m_{32}^2|$ for $E_\nu = 1$ GeV; inverted mass hierarchy, $\sin^2 2\theta_{13} = 0.1$, $\sin^2 2\theta_{12} = 0.8704$, $\Delta m_{21}^2 = 7.6 \times 10^{-5}$ eV $^2/c^4$, $\delta_{CP} = 0$ and Earth crust density = 2.6 g/cm 3 .

1290 **C. Sensitivity study for the 3.010×10^{20} POT ν_μ -disappearance analysis**

1291 A sensitivity study was performed at various points around the MINOS 2012 best-fit values [31]. These points are
 1292 shown in Fig. 132, and have the following values of $\sin^2 2\theta_{23}$:

- 1293 1. 1.0 (maximal)
 1294 2. 0.957 (2012 MINOS best-fit value)
 1295 3. 0.877 (smallest value in the 2012 MINOS 90% confidence region)

1296 The sensitivity study points have the following values of Δm_{32}^2 :

- 1297 1. $2.09 \times 10^{-3} \text{ eV}^2/c^4$ (2012 MINOS best-fit value - 3σ),
 1298 2. $2.29 \times 10^{-3} \text{ eV}^2/c^4$ (2012 MINOS best-fit value - 1σ),
 1299 3. $2.39 \times 10^{-3} \text{ eV}^2/c^4$ (2012 MINOS best-fit value),
 1300 4. $2.48 \times 10^{-3} \text{ eV}^2/c^4$ (2012 MINOS best-fit value + 1σ),
 1301 5. $2.66 \times 10^{-3} \text{ eV}^2/c^4$ (2012 MINOS best-fit value + 3σ).

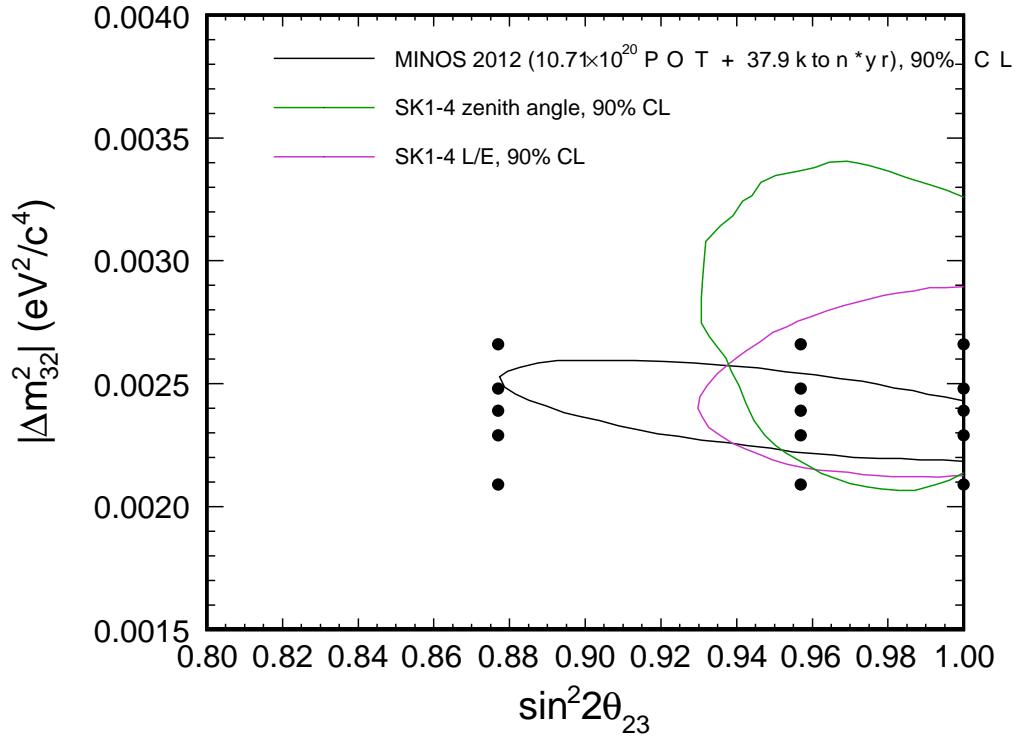


Figure 132: True oscillation parameters points considered in our T2K sensitivity study. The grid was constructed using the 2012 MINOS best-fit Δm_{32}^2 value and $\pm 1\sigma$, $\pm 3\sigma$ variations, and using $\sin^2 2\theta_{23}$ values of 1 (maximal), 0.957 (2012 MINOS best-fit value) and 0.877 (smallest value in the 2012 MINOS 90% confidence region).

1302 An average χ^2 surface was constructed as a function of $\sin^2 2\theta_{23}$ and Δm_{32}^2 by averaging the χ^2 surfaces obtained
 1303 by ‘2+8’ fits to 1K toy MC experiments. In each of these toy experiments, the systematic parameters were randomized
 1304 and statistical fluctuations were included. The confidence contours were then drawn using the constant- $\Delta\chi^2$ method
 1305 as described in Sec. 4.5.1.

1306 The results of the sensitivity study are shown in Figs. 133-137.

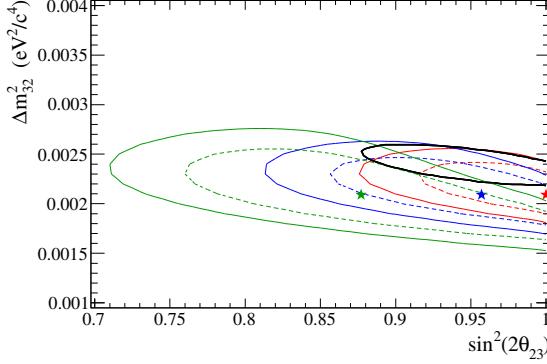


Figure 133: T2K 68% CL and 90% CL sensitivity contours, for 3.010×10^{20} POT, computed using the ‘2+8’ fit. The input ($\sin^2 2\theta_{23}$, Δm_{32}^2 (in eV^2/c^4)) points shown in red, blue and green are, respectively, (1.000, 0.00209), (0.957, 0.00209), (0.877, 0.00209). The 2012 MINOS 90% CL region is shown in black.

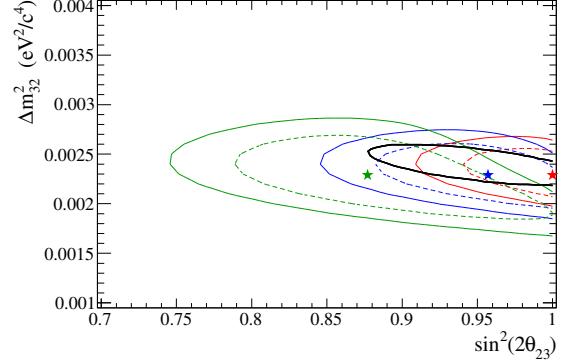


Figure 134: T2K 68% CL and 90% CL sensitivity contours, for 3.010×10^{20} POT, computed using the ‘2+8’ fit. The input ($\sin^2 2\theta_{23}$, Δm_{32}^2 (in eV^2/c^4)) points shown in red, blue and green are, respectively, (1.000, 0.00229), (0.957, 0.00229), (0.877, 0.00229). The 2012 MINOS 90% CL region is shown in black.

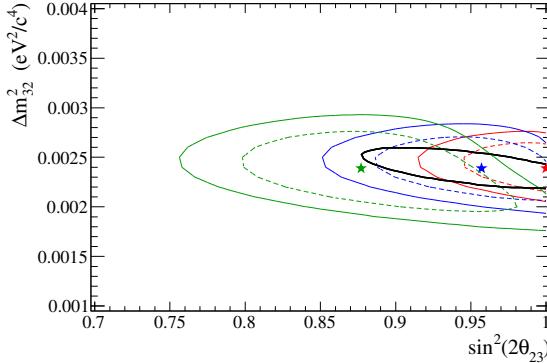


Figure 135: T2K 68% CL and 90% CL sensitivity contours, for 3.010×10^{20} POT, computed using the ‘2+8’ fit. The input ($\sin^2 2\theta_{23}$, Δm_{32}^2 (in eV^2/c^4)) points shown in red, blue and green are, respectively, (1.000, 0.00239), (0.957, 0.00239), (0.877, 0.00239). The 2012 MINOS 90% CL region is shown in black.

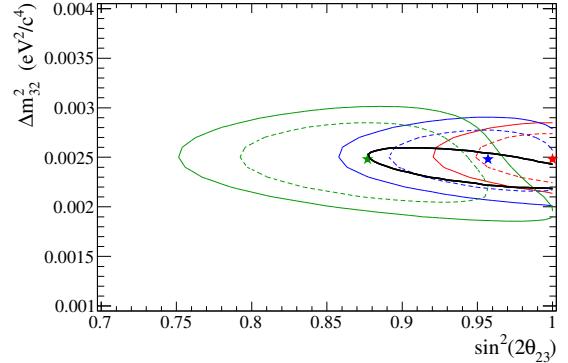


Figure 136: T2K 68% CL and 90% CL sensitivity contours, for 3.010×10^{20} POT, computed using the ‘2+8’ fit. The input ($\sin^2 2\theta_{23}$, Δm_{32}^2 (in eV^2/c^4)) points shown in red, blue and green are, respectively, (1.000, 0.00248), (0.957, 0.00248), (0.877, 0.00248). The 2012 MINOS 90% CL region is shown in black.

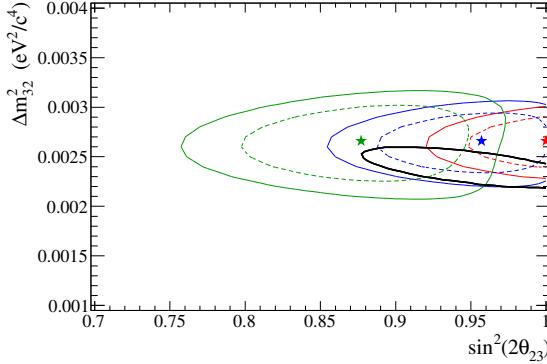


Figure 137: T2K 68% CL and 90% CL sensitivity contours, for 3.010×10^{20} POT, computed using the ‘2+8’ fit. The input ($\sin^2 2\theta_{23}$, Δm_{32}^2 (in eV^2/c^4)) points shown in red, blue and green are, respectively, (1.000, 0.00266), (0.957, 0.00266), (0.877, 0.00266). The 2012 MINOS 90% CL region is also shown in black.

1307 **D. Example toy MC fits**

1308 Six toy MC SuperK datasets were created with a POT corresponding to the Run 1+2+3 data; two datasets were
 1309 created by each of the KIT, VaLOR and MuSiC groups. Each dataset included random variations of all of the systematic
 1310 parameters, with these variations and the true oscillation parameters being unknown to the analysers in the groups that
 1311 did not create the datasets. Each dataset was fitted using both a 2+8 and a 2+N fit, and the value of chisq (from equation
 1312 5) was obtained at the best-fit point for each fit. All these fits were made with the coarse binning scheme discussed in
 1313 Sec. 4.2.

1314 Goodness-of-fit tests were carried out on these six toy datasets. The best-fit values of $\sin^2 2\theta_{23}$ and Δm_{32}^2 obtained
 1315 in the 5-bin fit to the first dataset were then used as input true oscillation parameters to create 1000 additional toy MC
 1316 datasets. Both statistical and systematic variations were included in these additional datasets. Each additional dataset
 1317 was fitted using a 5-bin 2+8 fit to find the value of chisq at the best-fit point. The p-value for the first of the original
 1318 datasets was then calculated as the ratio of the number of additional datasets whose best-fit chisq was greater than that
 1319 of the original dataset to the total number of additional datasets. This calculation of the p-value was then repeated for
 1320 each of the other 5 original datasets.

Fake data set	Analysis	$\sin^2 2\theta_{23}$	$ \Delta m_{32}^2 $ (eV $^2/c^4$)	N_{SK}	$\chi^2_{bestfit}/ndf$	Systematics
0	'2+N'	1.000	2.250×10^{-3}	63	-	Nominal
	'2+8'	1.000	2.130×10^{-3}	66.09	82.30/71	See Fig. 144
	'2+8'	1.000	2.133×10^{-3}	65.88	82.45/71	See Fig. 138
1	'2+N'	0.880	2.500×10^{-3}	95	-	$f_{NC}^{SK}: +100\%$
	'2+8'	0.943	2.243×10^{-3}	85.13	84.96/71	See Fig. 145
	'2+8'	0.938	2.241×10^{-3}	83.55	86.40/71	See Fig. 139
2	'2+N'	0.950	3.000×10^{-3}	65	-	$f_{pF}: +1\sigma, f_{16}^{banff}: 1.0$
	'2+8'	0.966	2.861×10^{-3}	64.27	73.00/71	See Fig. 146
	'2+8'	0.966	2.859×10^{-3}	64.60	73.22/71	See Fig. 140
3	'2+N'	1.000	2.200×10^{-3}	66	-	$f_E^{SK}: -1.0\sigma$
	'2+8'	1.000	2.228×10^{-3}	63.82	66.36/71	See Fig. 147
	'2+8'	1.000	2.226×10^{-3}	63.71	66.57/71	See Fig. 141
4	'2+N'	0.850	2.700×10^{-3}	82	-	$f_0^{banff} - f_3^{banff}: +5\%$
	'2+8'	0.837	2.600×10^{-3}	82.89	70.27/71	See Fig. 148
	'2+8'	0.838	2.600×10^{-3}	82.90	70.48/71	See Fig. 142
5	'2+N'	0.800	2.000×10^{-3}	77	-	Nominal
	'2+8'	0.828	2.176×10^{-3}	82.68	67.25/71	See Fig. 149
	'2+8'	0.826	2.201×10^{-3}	83.33	67.48/71	See Fig. 143

Table 18: True input (shown in bold) and VALOR '2+8' and '2+N' best-fit values for the test ensemble of 6 toy-MC experiments fit by all 3 disappearance analyses.

1321 D.1. Systematic parameter pulls

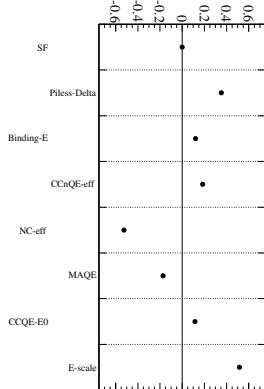


Figure 138: Systematic pulls for the 2+8 fit to fake data set 0.

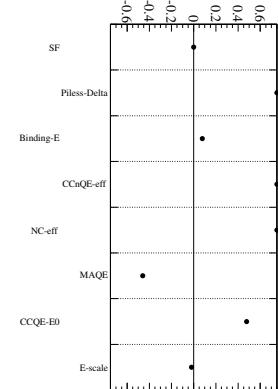


Figure 139: Systematic pulls for the 2+8 fit to fake data set 1.

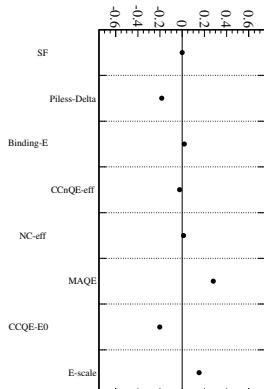


Figure 140: Systematic pulls for the 2+8 fit to fake data set 2.

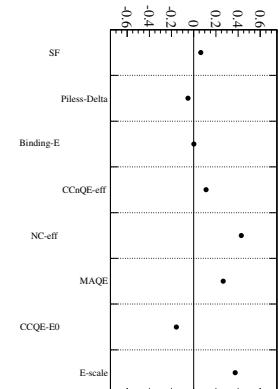


Figure 141: Systematic pulls for the 2+8 fit to fake data set 3.

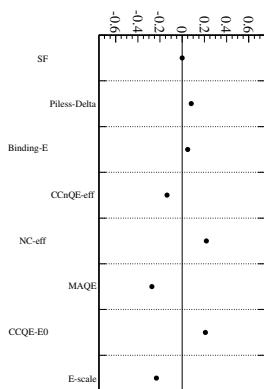


Figure 142: Systematic pulls for the 2+8 fit to fake data set 4.

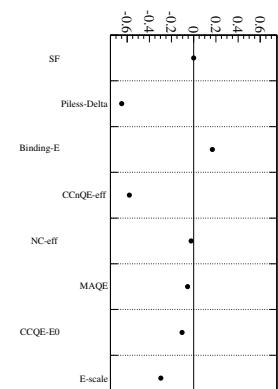


Figure 143: Systematic pulls for the 2+8 fit to fake data set 5.

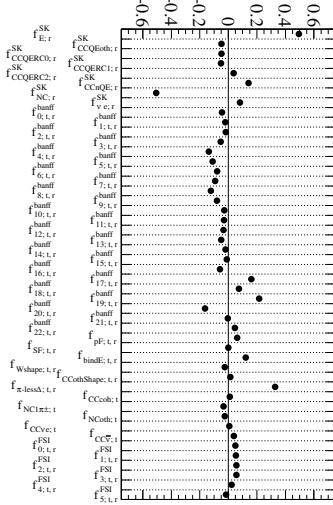


Figure 144: Systematic pulls for the 2+N fit to fake data set 0.

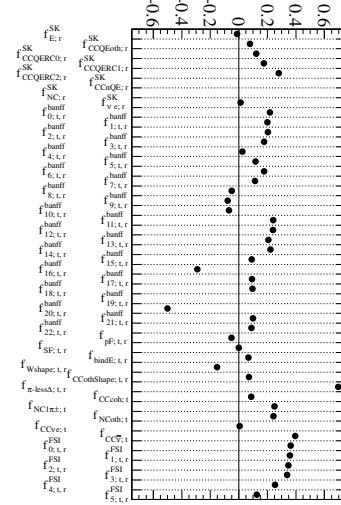


Figure 145: Systematic pulls for the 2+N fit to fake data set 1.

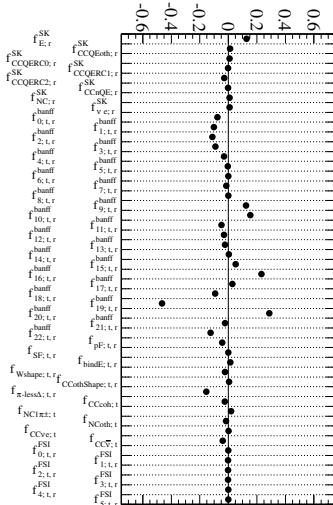


Figure 146: Systematic pulls for the 2+N fit to fake data set 2.

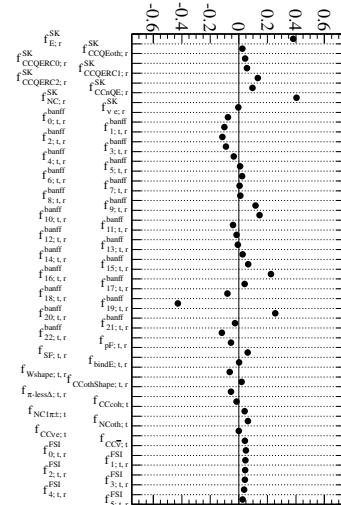


Figure 147: Systematic pulls for the 2+N fit to fake data set 3.

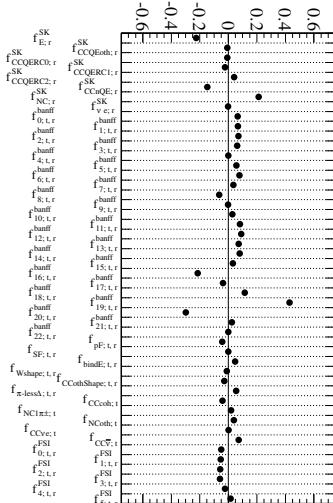


Figure 148: Systematic pulls for the 2+N fit to fake data set 4.

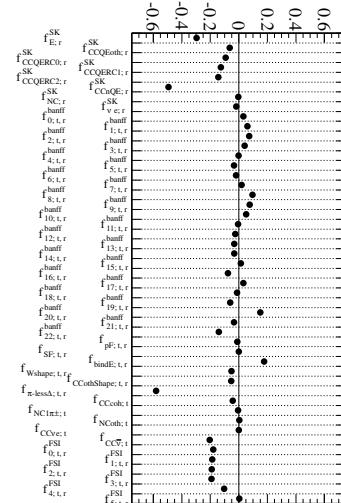


Figure 149: Systematic pulls for the 2+N fit to fake data set 5.

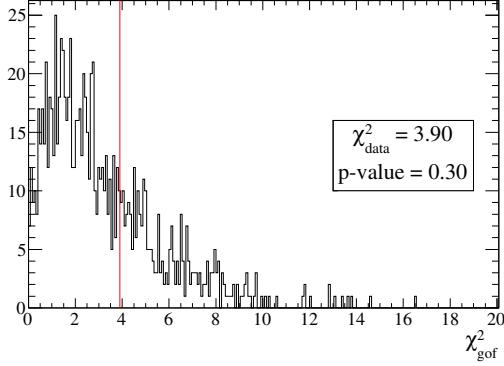


Figure 150: Distribution of χ^2_{gof} from 1000 toy MC datasets at the best-fit oscillation point for the 2+8 fit to fake data set 0. The χ^2_{gof} for data is highlighted.

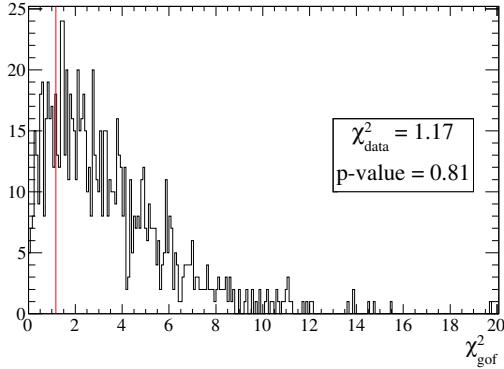


Figure 152: Distribution of χ^2_{gof} from 1000 toy MC datasets at the best-fit oscillation point for the 2+8 fit to fake data set 2. The χ^2_{gof} for data is highlighted.

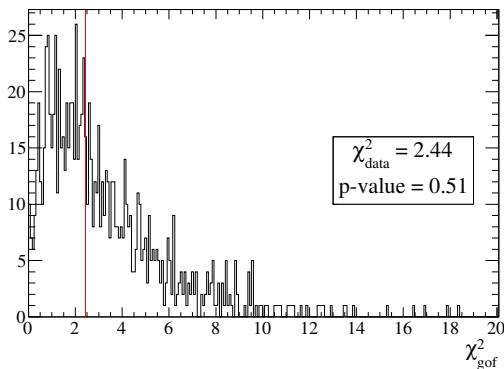


Figure 154: Distribution of χ^2_{gof} from 1000 toy MC datasets at the best-fit oscillation point for the 2+8 fit to fake data set 4. The χ^2_{gof} for data is highlighted.

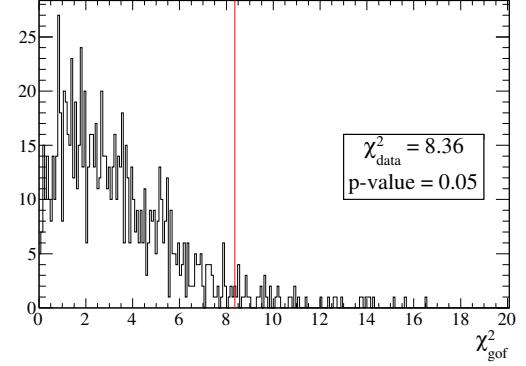


Figure 151: Distribution of χ^2_{gof} from 1000 toy MC datasets at the best-fit oscillation point for the 2+8 fit to fake data set 1. The χ^2_{gof} for data is highlighted.

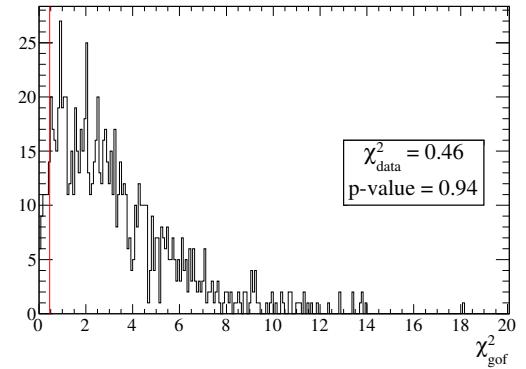


Figure 153: Distribution of χ^2_{gof} from 1000 toy MC datasets at the best-fit oscillation point for the 2+8 fit to fake data set 3. The χ^2_{gof} for data is highlighted.

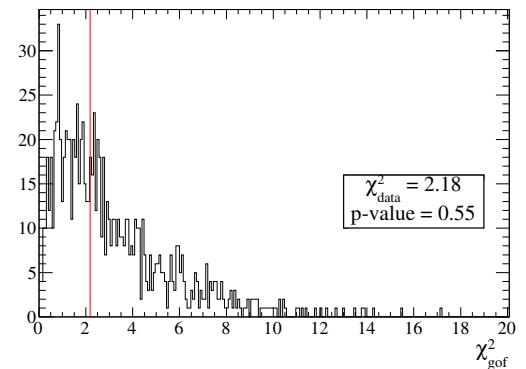


Figure 155: Distribution of χ^2_{gof} from 1000 toy MC datasets at the best-fit oscillation point for the 2+8 fit to fake data set 5. The χ^2_{gof} for data is highlighted.

1323 D.3. Best-fit spectra

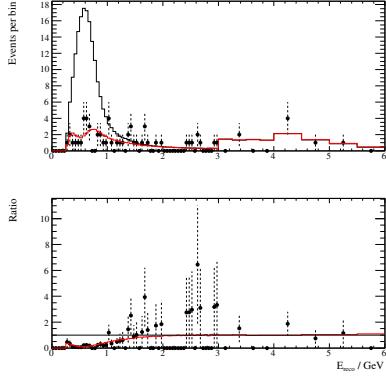


Figure 156: Best-fit spectrum (top) and ratios of data and best-fit spectrum to predicted spectrum for no oscillations (bottom) for the 2+N fit to fake data set 0

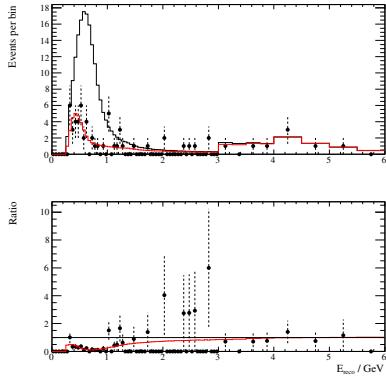


Figure 158: Best-fit spectrum (top) and ratios of data and best-fit spectrum to predicted spectrum for no oscillations (bottom) for the 2+N fit to fake data set 2

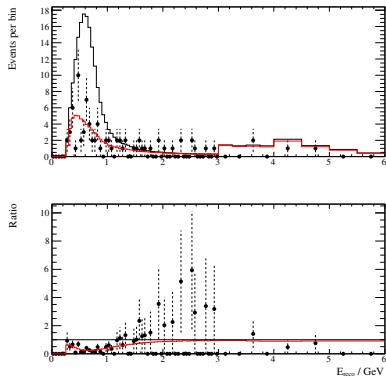


Figure 160: Best-fit spectrum (top) and ratios of data and best-fit spectrum to predicted spectrum for no oscillations (bottom) for the 2+N fit to fake data set 4

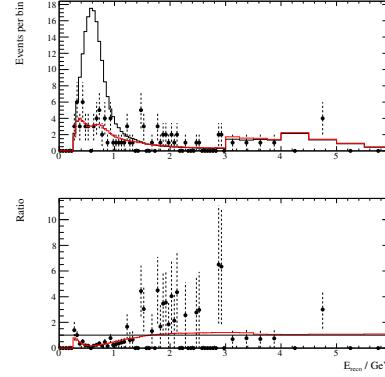


Figure 157: Best-fit spectrum (top) and ratios of data and best-fit spectrum to predicted spectrum for no oscillations (bottom) for the 2+N fit to fake data set 1

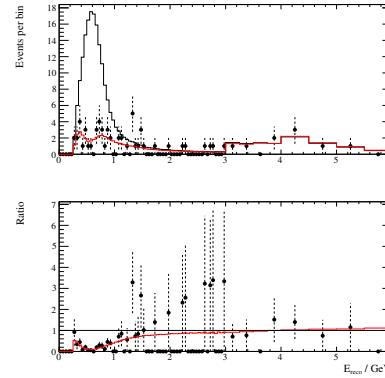


Figure 159: Best-fit spectrum (top) and ratios of data and best-fit spectrum to predicted spectrum for no oscillations (bottom) for the 2+N fit to fake data set 3

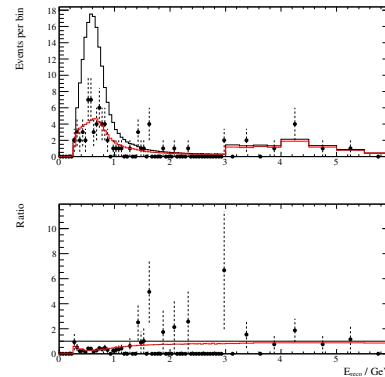


Figure 161: Best-fit spectrum (top) and ratios of data and best-fit spectrum to predicted spectrum for no oscillations (bottom) for the 2+N fit to fake data set 5

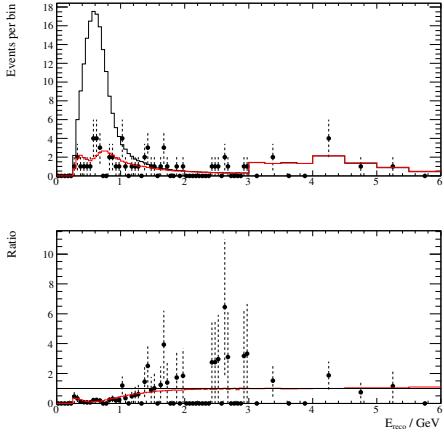


Figure 162: Best-fit spectrum (top) and ratios of data and best-fit spectrum to predicted spectrum for no oscillations (bottom) for the 2+8 fit to fake data set 0

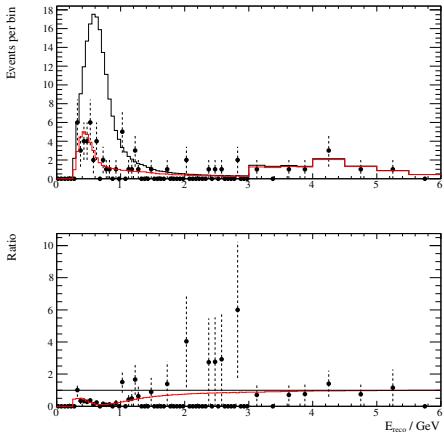


Figure 164: Best-fit spectrum (top) and ratios of data and best-fit spectrum to predicted spectrum for no oscillations (bottom) for the 2+8 fit to fake data set 2

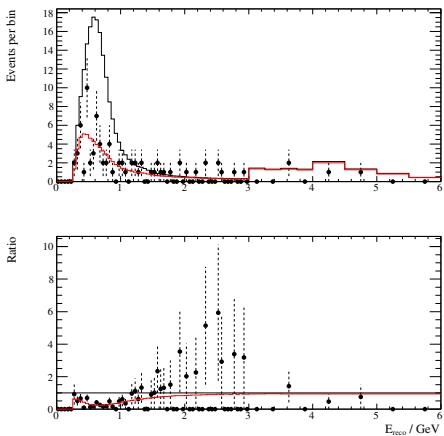


Figure 166: Best-fit spectrum (top) and ratios of data and best-fit spectrum to predicted spectrum for no oscillations (bottom) for the 2+8 fit to fake data set 4

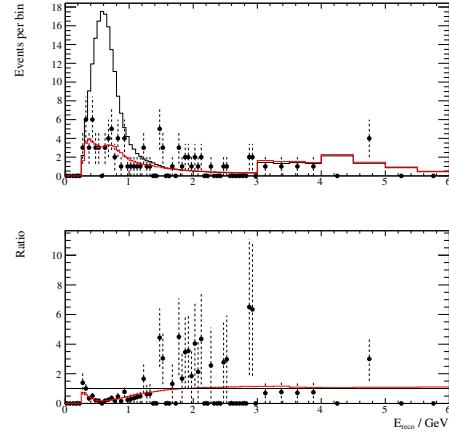


Figure 163: Best-fit spectrum (top) and ratios of data and best-fit spectrum to predicted spectrum for no oscillations (bottom) for the 2+8 fit to fake data set 1

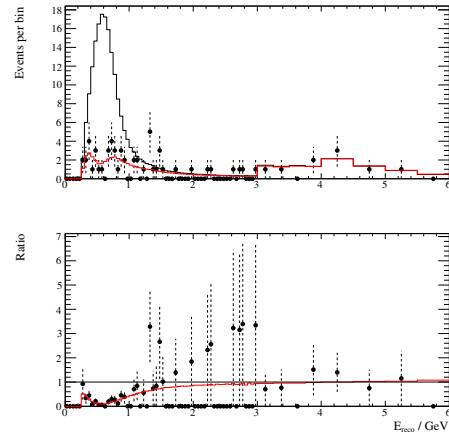


Figure 165: Best-fit spectrum (top) and ratios of data and best-fit spectrum to predicted spectrum for no oscillations (bottom) for the 2+8 fit to fake data set 3

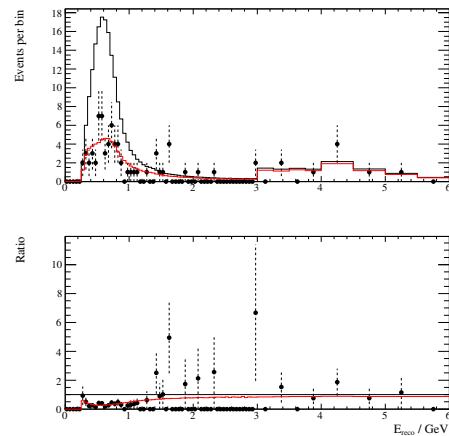


Figure 167: Best-fit spectrum (top) and ratios of data and best-fit spectrum to predicted spectrum for no oscillations (bottom) for the 2+8 fit to fake data set 5

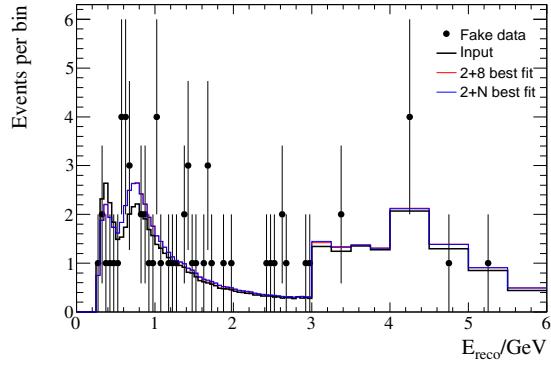


Figure 168: Comparisons of the 2+8 and 2+N best-fit spectra with the input distribution for fake data set 0

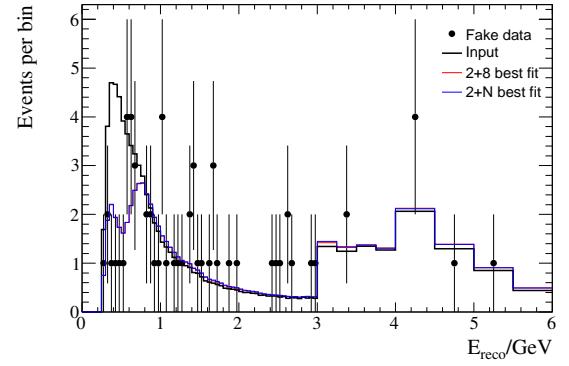


Figure 169: Comparisons of the 2+8 and 2+N best-fit spectra with the input distribution for fake data set 1

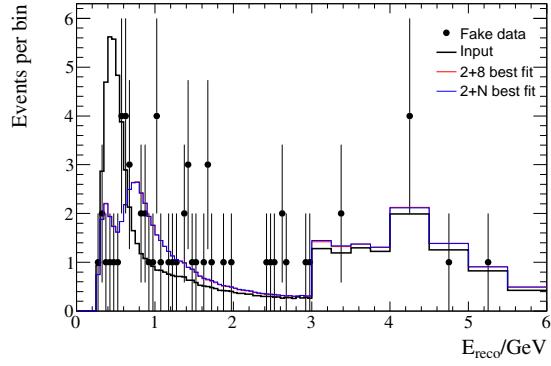


Figure 170: Comparisons of the 2+8 and 2+N best-fit spectra with the input distribution for fake data set 2

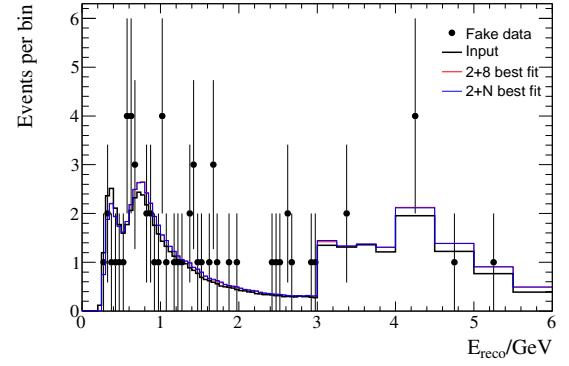


Figure 171: Comparisons of the 2+8 and 2+N best-fit spectra with the input distribution for fake data set 3

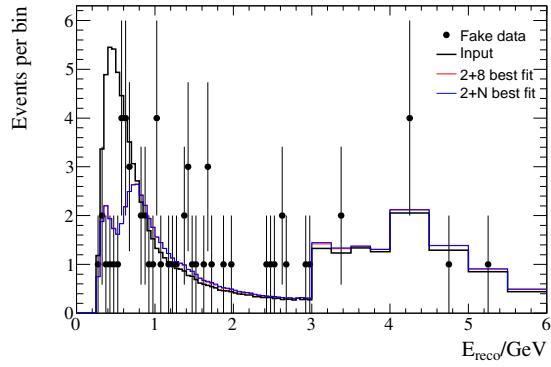


Figure 172: Comparisons of the 2+8 and 2+N best-fit spectra with the input distribution for fake data set 4

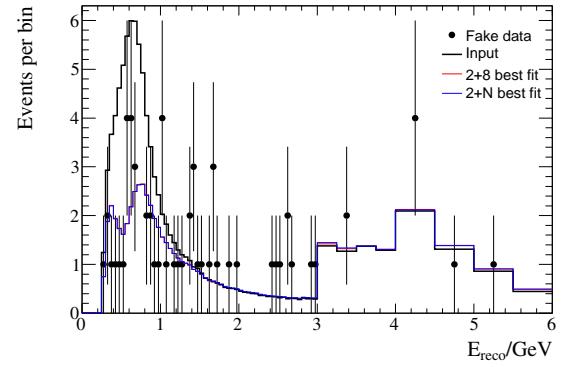


Figure 173: Comparisons of the 2+8 and 2+N best-fit spectra with the input distribution for fake data set 5

¹³²⁴ D.4. $\Delta\chi^2$ surfaces

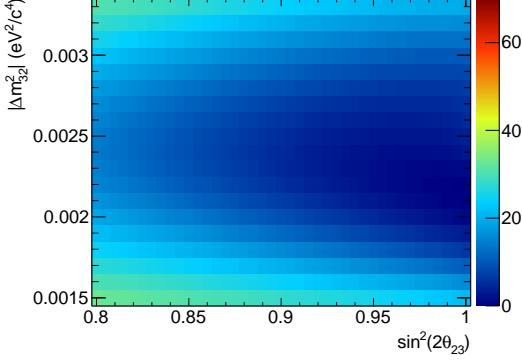


Figure 174: $\Delta\chi^2$ surface for the 2+N fit to fake data set 0

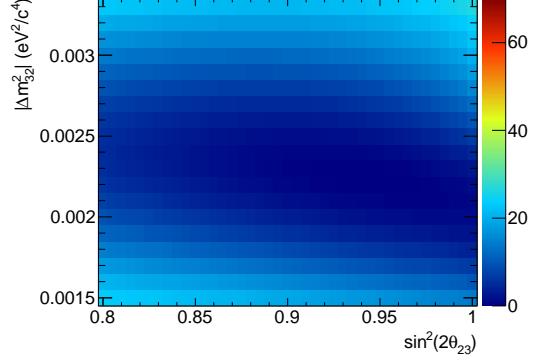


Figure 175: $\Delta\chi^2$ surface for the 2+N fit to fake data set 1

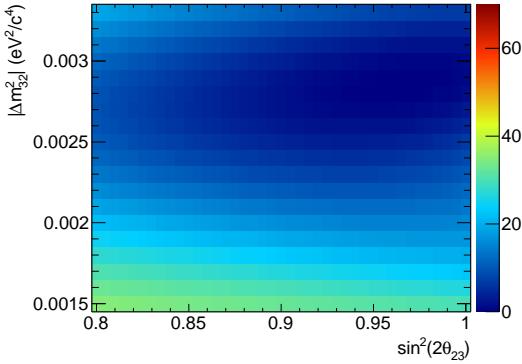


Figure 176: $\Delta\chi^2$ surface for the 2+N fit to fake data set 2

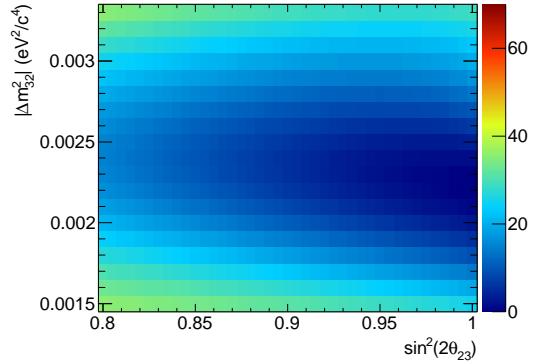


Figure 177: $\Delta\chi^2$ surface for the 2+N fit to fake data set 3

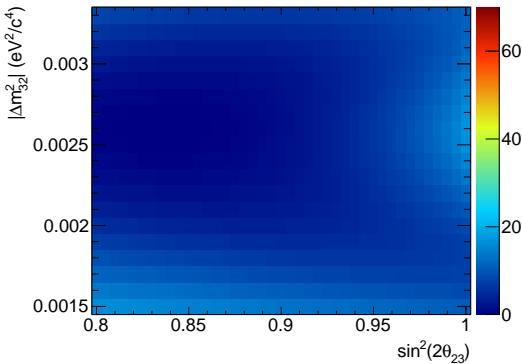


Figure 178: $\Delta\chi^2$ surface for the 2+N fit to fake data set 4

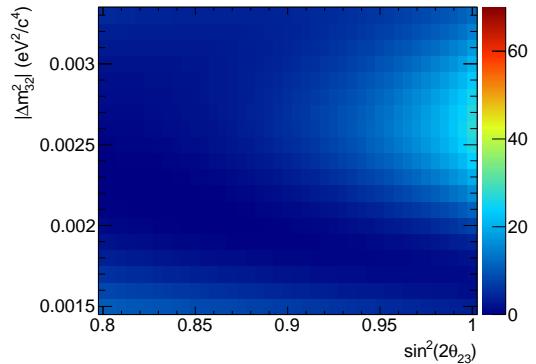
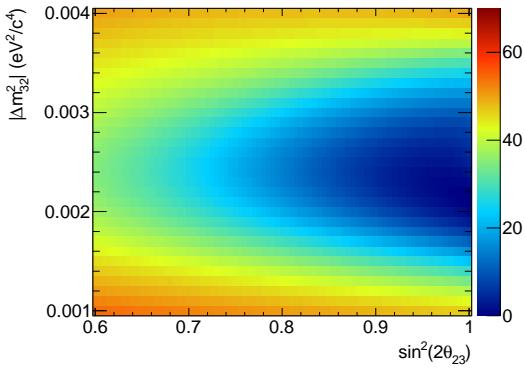
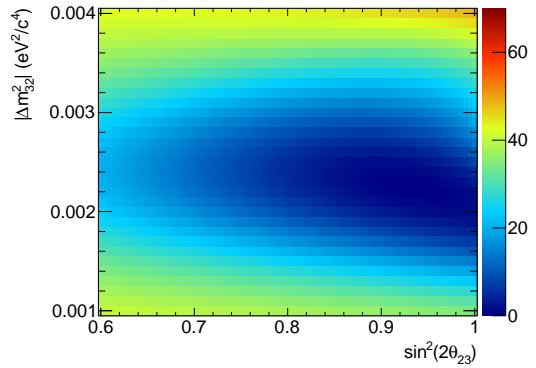
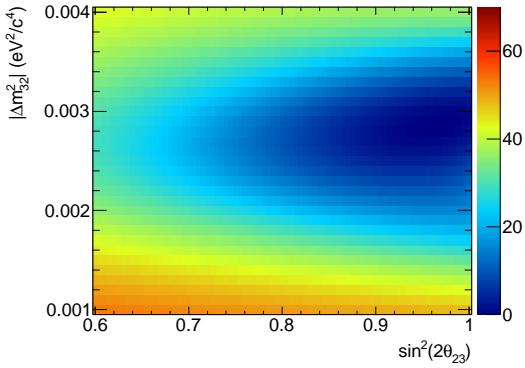
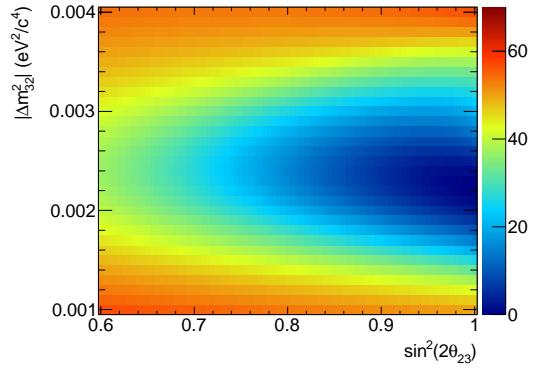
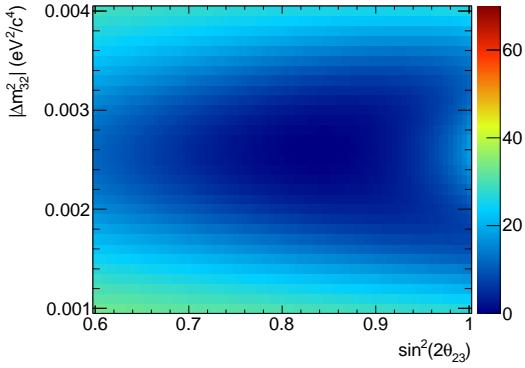
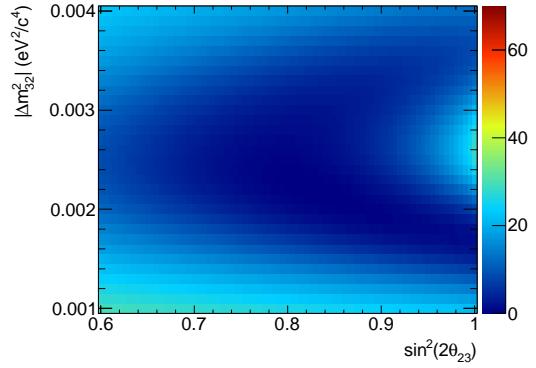


Figure 179: $\Delta\chi^2$ surface for the 2+N fit to fake data set 5

Figure 180: $\Delta\chi^2$ surface for the 2+8 fit to fake data set 0Figure 181: $\Delta\chi^2$ surface for the 2+8 fit to fake data set 1Figure 182: $\Delta\chi^2$ surface for the 2+8 fit to fake data set 2Figure 183: $\Delta\chi^2$ surface for the 2+8 fit to fake data set 3Figure 184: $\Delta\chi^2$ surface, for the 2+8 fit to fake data set 4Figure 185: $\Delta\chi^2$ surface for the 2+8 fit to fake data set 5

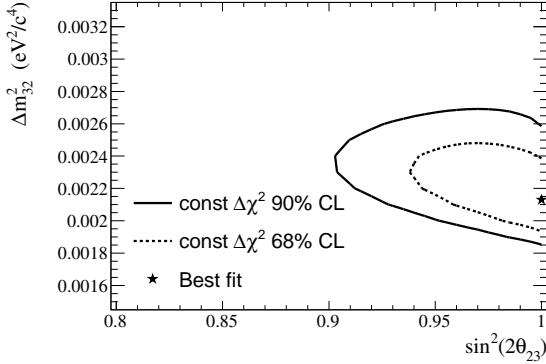


Figure 186: 68% and 90% confidence regions for the 2+N fit to fake data set 0

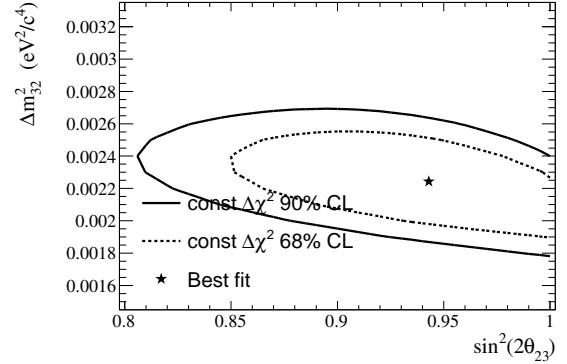


Figure 187: 68% and 90% confidence regions for the 2+N fit to fake data set 1

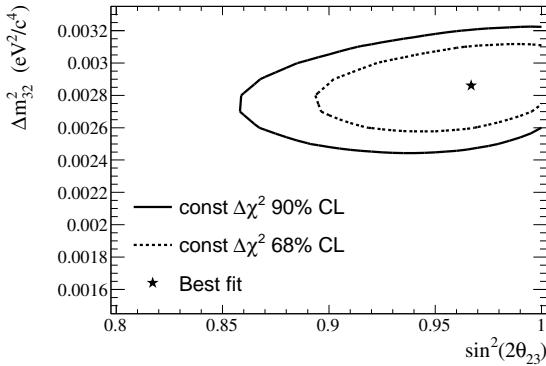


Figure 188: 68% and 90% confidence regions for the 2+N fit to fake data set 2

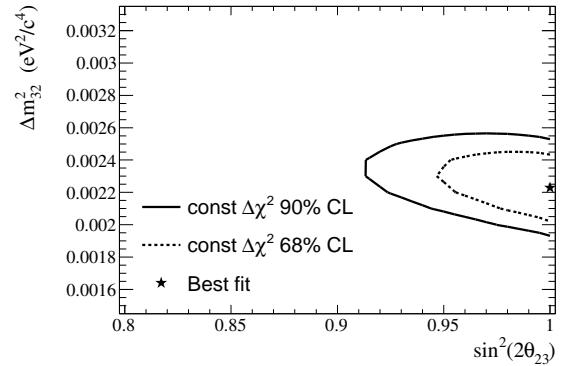


Figure 189: 68% and 90% confidence regions for the 2+N fit to fake data set 3

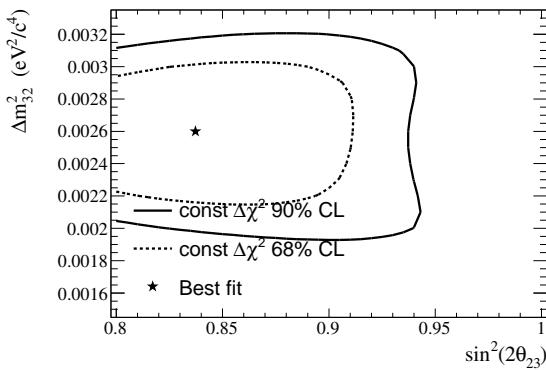


Figure 190: 68% and 90% confidence regions for the 2+N fit to fake data set 4

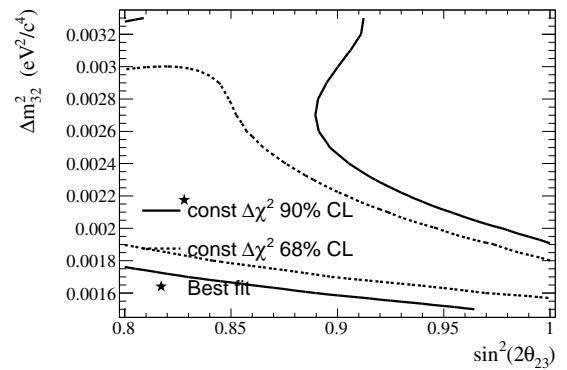


Figure 191: 68% and 90% confidence regions for the 2+N fit to fake data set 5

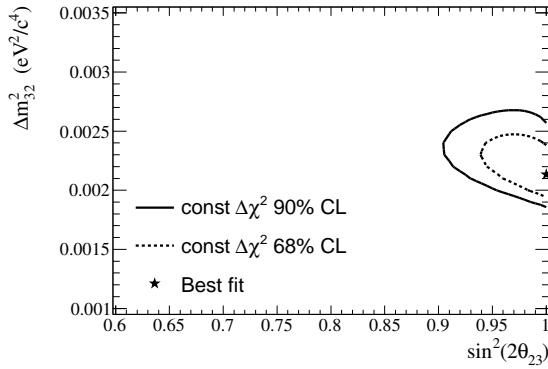


Figure 192: 68% and 90% confidence regions for the 2+8 fit to fake data set 0

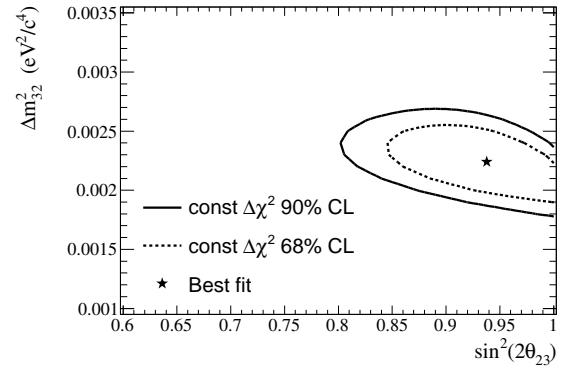


Figure 193: 68% and 90% confidence regions for the 2+8 fit to fake data set 1

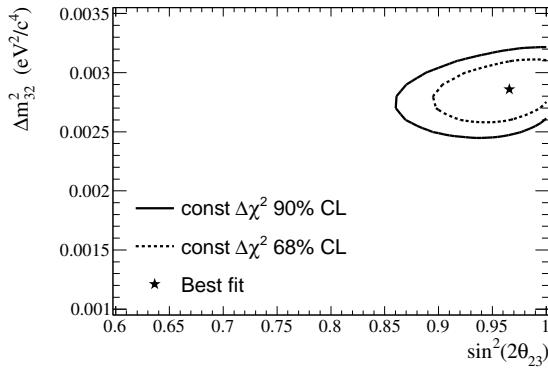


Figure 194: 68% and 90% confidence regions for the 2+8 fit to fake data set 2

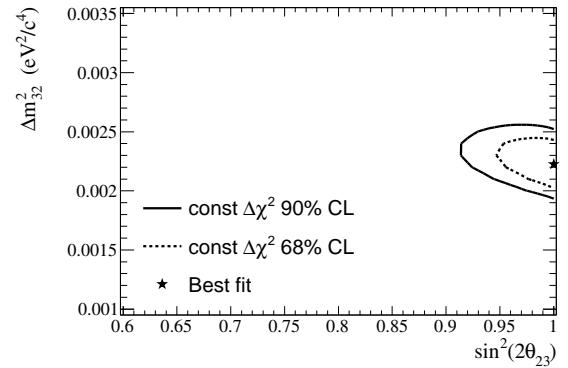


Figure 195: 68% and 90% confidence regions for the 2+8 fit to fake data set 3

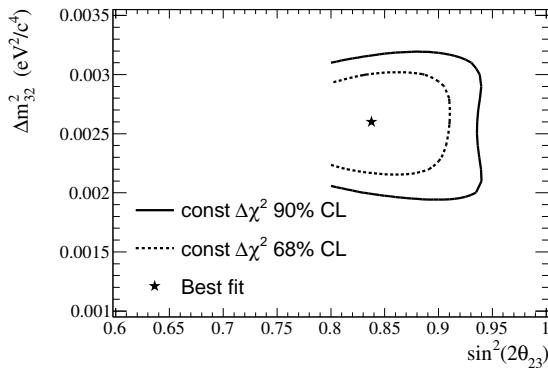


Figure 196: 68% and 90% confidence regions for the 2+8 fit to fake data set 4

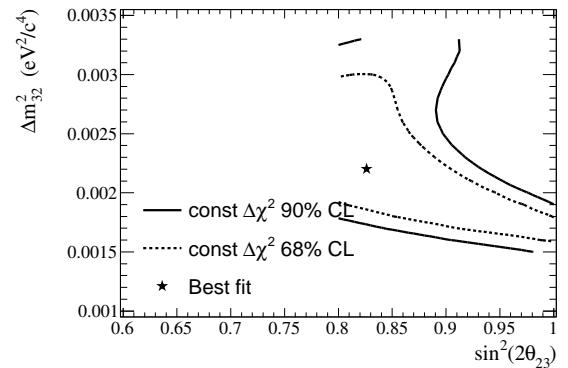


Figure 197: 68% and 90% confidence regions for the 2+8 fit to fake data set 5

1326 **E. Detailed study of the effect of systematics on the predicted number of 1 μ -like ring events**

1327 In this section, the effect of systematics on the predicted number of events in SuperK is presented in a number of
 1328 tables. Each table shows the pre- and post-BANFF tuning nominal N_{SK} for every SuperK MC mode considered in the
 1329 analysis, and the BANFF-tuned N_{SK} for $\pm 1\sigma$ deviations of a single systematic parameter. For correlated systematic
 1330 parameters, σ is defined as the square root of the corresponding diagonal entry in the covariance matrix. For certain
 1331 systematics, the modes are broken into E_{reco} or E_{true} bins, to show the energy dependence of that systematic (where
 1332 relevant). Tabs. 20-67 show the effect of systematics on the unoscillated N_{SK} . Tabs. 68-115 show the effect of
 1333 systematics on the N_{SK} with 3-flavour oscillations in matter, using the following values of the oscillation parameters:

- 1334 • $\sin^2 2\theta_{12} = 0.857$
 1335 • $\sin^2 2\theta_{13} = 0.098$
 1336 • $\sin^2 2\theta_{23} = 1.0$
 1337 • $\delta_{CP} = 0$
 1338 • $\Delta m_{21}^2 = 7.5 \times 10^{-5} \text{ eV}^2/\text{c}^4$
 1339 • $|\Delta m_{32}^2| = 2.4 \times 10^{-3} \text{ eV}^2/\text{c}^4$

1340 The percentage uncertainties in the systematic parameters are summarised in Tab. 19 (parameters whose effects are
 1341 evaluated using splines are not included in this table).

Systematic	Expected change
$f_{E:r}^{SK}$	0 % (movement in Ereco)
$f_{CCQE oth;r}^{SK}$	1.8 %
$f_{CCQERC0;r}^{SK}$	1.7 %
$f_{CCQERC1;r}^{SK}$	3.5 %
$f_{CCQERC2;r}^{SK}$	9.3 %
$f_{CCnQE;r}^{SK}$	20 %
$f_{NC;r}^{SK}$	111 %
$f_{\nu e;r}^{SK}$	100 %
$f_{banff}^{0:t,r}$	9.283 %
$f_{banff}^{1:t,r}$	9.757 %
$f_{banff}^{2:t,r}$	8.974 %
$f_{banff}^{3:t,r}$	8.457 %
$f_{banff}^{4:t,r}$	10.5 %
$f_{banff}^{5:t,r}$	9.26 %
$f_{banff}^{6:t,r}$	8.113 %
$f_{banff}^{7:t,r}$	7.279 %
$f_{banff}^{8:t,r}$	8.362 %
$f_{banff}^{9:t,r}$	10.77 %
$f_{banff}^{10:t,r}$	14.12 %
$f_{banff}^{11:t,r}$	11.03 %
$f_{banff}^{12:t,r}$	9.867 %
$f_{banff}^{13:t,r}$	10.33 %
$f_{banff}^{14:t,r}$	11.08 %
$f_{banff}^{15:t,r}$	10.91 %
$f_{banff}^{18:t,r}$	9.012 %
$f_{banff}^{19:t,r}$	29.57 %
$f_{banff}^{20:t,r}$	16.7 %
$f_{banff}^{21:t,r}$	14.9 %
$f_{banff}^{22:t,r}$	27.74 %
$f_{CCcoh;t}$	100 %
$f_{NC1\pi^\pm;t}$	30 %
$f_{NCoth;t}$	30 %
$f_{CC\nu_e;t}$	3 %
$f_{CC\bar{\nu};t}$	40 %
$f_{FSI}^{23:t,r}$	0.00363 %

Table 19: Summary table showing the magnitude of errors in the systematic parameters. The numbers should be compared with the changes in N_{SK} in the other tables in this appendix. Systematics with complicated energy dependence are treated with response functions, and are not shown.

Component	Nominal	BANFF tuned	BANFF tuned +1σ		BANFF tuned -1σ	
NS_K (1 μ -like ring)	210.5	204.7	204.7	-5.553e-14 %	204.7	-6.941e-14 %
NS_K (1 μ -like ring): ν_μ CCQE ($E_r < 0.4$ GeV)	7.784	7.518	7.518	0 %	7.518	0 %
NS_K (1 μ -like ring): ν_μ CCQE ($0.4 \leq E_r < 1.1$ GeV)	136.8	128.3	128.3	0 %	128.3	0 %
NS_K (1 μ -like ring): ν_μ CCQE ($E_r \geq 1.1$ GeV)	21.78	19.2	19.2	0 %	19.2	0 %
NS_K (1 μ -like ring): ν_μ CCQE	166.4	155	155	0 %	155	0 %
NS_K (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	34.95	0 %	34.95	0 %
NS_K (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.9503	0 %	0.9503	0 %
NS_K (1 μ -like ring): ν_μ CC other (ν_μ disp)	4.315	4.199	4.199	0 %	4.199	0 %
NS_K (1 μ -like ring): ν_μ CC all	200.6	195.1	195.1	0 %	195.1	0 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625	0 %	1.625	0 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466	0 %	1.466	0 %
NS_K (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092	0 %	3.092	0 %
NS_K (1 μ -like ring): ν_μ CCQE ($E_r < 0.4$ GeV)	0.1497	0.1414	0.1414	0 %	0.1414	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($0.4 \leq E_r < 1.1$ GeV)	1.979	1.873	1.873	0 %	1.873	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($E_r \geq 1.1$ GeV)	2.331	1.967	1.967	0 %	1.967	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	4.46	3.981	3.981	0 %	3.981	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	1.762	0 %	1.762	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.2111	0.2028	0.2028	0 %	0.2028	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2539	0.2478	0.2478	0 %	0.2478	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.194	0 %	6.194	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %	0.09042	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %	0.07761	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %	0.168	0 %
NS_K (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01626	0 %	0.01626	0 %
NS_K (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.01313	0 %	0.01313	0 %
NS_K (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004335	0 %	0.0004335	0 %
NS_K (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003048	0.003051	0.003051	0 %	0.003051	0 %
NS_K (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03287	0 %	0.03287	0 %
NS_K (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %	0.04942	0 %
NS_K (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %	0.05768	0 %
NS_K (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %	0.1071	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0007905	0 %	0.0007905	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.0007453	0 %	0.0007453	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.333e-05	7.333e-05	7.333e-05	0 %	7.333e-05	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002189	0.000219	0.000219	0 %	0.000219	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001828	0 %	0.001828	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %	0.005916	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %	0.005954	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %	0.01187	0 %
NS_K (1 μ -like ring): oscillation ν_e CCQE	0	0	0	0 %	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0	0 %	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC coherent	0	0	0	0 %	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0	0 %	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC all	0	0	0	0 %	0	0 %

Table 20: Effect of $f_{E;r}^{SK}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NSK (1 μ -like ring)	210.5	204.7	207.6	1.398 %
NSK (1 μ -like ring): ν_μ CCQE	166.4	155	157.8	1.8 %
NSK (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	34.95	0 %
NSK (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.9503	0 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	4.315	4.199	4.199	0 %
NSK (1 μ -like ring): ν_μ CC all	200.6	195.1	197.9	1.43 %
NSK (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625	0 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466	0 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092	0 %
NSK (1 μ -like ring): ν_e CCQE	4.46	3.981	4.053	1.8 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	1.762	0 %
NSK (1 μ -like ring): ν_e CC coherent	0.2111	0.2028	0.2028	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2539	0.2478	0.2478	0 %
NSK (1 μ -like ring): ν_e CC all	6.37	6.194	6.266	1.157 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %
NSK (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01626	0 %
NSK (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.01313	0 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004335	0 %
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003048	0.003051	0.003051	0 %
NSK (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03287	0 %
NSK (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0007905	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.0007453	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.333e-05	7.333e-05	7.333e-05	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002189	0.000219	0.000219	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001828	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC all	0	0	0	0 %

Table 21: Effect of $f_{CCQEoth;r}^{SK}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NS_K (1 μ -like ring)	210.5	204.7	204.9 0.0636 %	204.6 -0.0636 %
NS_K (1 μ -like ring): ν_μ CCQE ($E_r < 0.4$ GeV)	7.784	7.518	7.646 1.7 %	7.39 -1.7 %
NS_K (1 μ -like ring): ν_μ CCQE ($0.4 \leq E_r < 1.1$ GeV)	136.8	128.3	128.3 0 %	128.3 0 %
NS_K (1 μ -like ring): ν_μ CCQE ($E_r \geq 1.1$ GeV)	21.78	19.2	19.2 0 %	19.2 0 %
NS_K (1 μ -like ring): ν_μ CCQE	166.4	155	155.2 0.08243 %	154.9 -0.08243 %
NS_K (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	34.95 0 %	34.95 0 %
NS_K (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.9503 0 %	0.9503 0 %
NS_K (1 μ -like ring): ν_μ CC other (ν_μ disp)	4.315	4.199	4.199 0 %	4.199 0 %
NS_K (1 μ -like ring): ν_μ CC all	200.6	195.1	195.3 0.06549 %	195 -0.06549 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625 0 %	1.625 0 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466 0 %	1.466 0 %
NS_K (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092 0 %	3.092 0 %
NS_K (1 μ -like ring): ν_μ CCQE ($E_r < 0.4$ GeV)	0.1497	0.1414	0.1438 1.7 %	0.139 -1.7 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($0.4 \leq E_r < 1.1$ GeV)	1.979	1.873	1.873 0 %	1.873 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($E_r \geq 1.1$ GeV)	2.331	1.967	1.967 0 %	1.967 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	4.46	3.981	3.984 0.06039 %	3.979 -0.06039 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	1.762 0 %	1.762 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.2111	0.2028	0.2028 0 %	0.2028 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2539	0.2478	0.2478 0 %	0.2478 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.197 0.03881 %	6.192 -0.03881 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042 0 %	0.09042 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761 0 %	0.07761 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168 0 %	0.168 0 %
NS_K (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01626 0 %	0.01626 0 %
NS_K (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.01313 0 %	0.01313 0 %
NS_K (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004335 0 %	0.0004335 0 %
NS_K (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003048	0.003051	0.003051 0 %	0.003051 0 %
NS_K (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03287 0 %	0.03287 0 %
NS_K (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942 0 %	0.04942 0 %
NS_K (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768 0 %	0.05768 0 %
NS_K (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071 0 %	0.1071 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0007905 0 %	0.0007905 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.0007453 0 %	0.0007453 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.333e-05	7.333e-05	7.333e-05 0 %	7.333e-05 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002189	0.000219	0.000219 0 %	0.000219 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001828 0 %	0.001828 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916 0 %	0.005916 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954 0 %	0.005954 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187 0 %	0.01187 0 %
NS_K (1 μ -like ring): oscillation ν_e CCQE	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e CC coherent	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e CC all	0	0	0 0 %	0 0 %

Table 22: Effect of $f_{CCQERC0;r}^{SK}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1σ		BANFF tuned -1σ	
NS_K (1 μ -like ring)	210.5	204.7	209.3	2.226 %	200.2	-2.226 %
NS_K (1 μ -like ring): ν_μ CCQE ($E_r < 0.4$ GeV)	7.784	7.518	7.518	0 %	7.518	0 %
NS_K (1 μ -like ring): ν_μ CCQE ($0.4 \leq E_r < 1.1$ GeV)	136.8	128.3	132.8	3.5 %	123.8	-3.5 %
NS_K (1 μ -like ring): ν_μ CCQE ($E_r \geq 1.1$ GeV)	21.78	19.2	19.2	0 %	19.2	0 %
NS_K (1 μ -like ring): ν_μ CCQE	166.4	155	159.5	2.897 %	150.6	-2.897 %
NS_K (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	34.95	0 %	34.95	0 %
NS_K (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.9503	0 %	0.9503	0 %
NS_K (1 μ -like ring): ν_μ CC other (ν_μ disp)	4.315	4.199	4.199	0 %	4.199	0 %
NS_K (1 μ -like ring): ν_μ CC all	200.6	195.1	199.6	2.302 %	190.6	-2.302 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625	0 %	1.625	0 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466	0 %	1.466	0 %
NS_K (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092	0 %	3.092	0 %
NS_K (1 μ -like ring): ν_μ CCQE ($E_r < 0.4$ GeV)	0.1497	0.1414	0.1414	0 %	0.1414	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($0.4 \leq E_r < 1.1$ GeV)	1.979	1.873	1.939	3.5 %	1.808	-3.5 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($E_r \geq 1.1$ GeV)	2.331	1.967	1.967	0 %	1.967	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	4.46	3.981	4.047	1.647 %	3.916	-1.647 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	1.762	0 %	1.762	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.2111	0.2028	0.2028	0 %	0.2028	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2539	0.2478	0.2478	0 %	0.2478	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.26	1.058 %	6.129	-1.058 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %	0.09042	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %	0.07761	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %	0.168	0 %
NS_K (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01626	0 %	0.01626	0 %
NS_K (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.01313	0 %	0.01313	0 %
NS_K (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004335	0 %	0.0004335	0 %
NS_K (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003048	0.003051	0.003051	0 %	0.003051	0 %
NS_K (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03287	0 %	0.03287	0 %
NS_K (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %	0.04942	0 %
NS_K (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %	0.05768	0 %
NS_K (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %	0.1071	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0007905	0 %	0.0007905	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.0007453	0 %	0.0007453	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.333e-05	7.333e-05	7.333e-05	0 %	7.333e-05	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002189	0.000219	0.000219	0 %	0.000219	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001828	0 %	0.001828	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %	0.005916	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %	0.005954	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %	0.01187	0 %
NS_K (1 μ -like ring): oscillation ν_e CCQE	0	0	0	0 %	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0	0 %	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC coherent	0	0	0	0 %	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0	0 %	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC all	0	0	0	0 %	0	0 %

Table 23: Effect of $f_{CCQERC1;r}^{SK}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NS_K (1 μ -like ring)	210.5	204.7	206.7 0.9614 %	202.8 -0.9614 %
NS_K (1 μ -like ring): ν_μ CCQE ($E_r < 0.4$ GeV)	7.784	7.518	7.518 0 %	7.518 0 %
NS_K (1 μ -like ring): ν_μ CCQE ($0.4 \leq E_r < 1.1$ GeV)	136.8	128.3	128.3 0 %	128.3 0 %
NS_K (1 μ -like ring): ν_μ CCQE ($E_r \geq 1.1$ GeV)	21.78	19.2	20.98 9.3 %	17.41 -9.3 %
NS_K (1 μ -like ring): ν_μ CCQE	166.4	155	156.8 1.152 %	153.3 -1.152 %
NS_K (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	34.95 0 %	34.95 0 %
NS_K (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.9503 0 %	0.9503 0 %
NS_K (1 μ -like ring): ν_μ CC other (ν_μ disp)	4.315	4.199	4.199 0 %	4.199 0 %
NS_K (1 μ -like ring): ν_μ CC all	200.6	195.1	196.9 0.915 %	193.4 -0.915 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625 0 %	1.625 0 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466 0 %	1.466 0 %
NS_K (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092 0 %	3.092 0 %
NS_K (1 μ -like ring): ν_μ CCQE ($E_r < 0.4$ GeV)	0.1497	0.1414	0.1414 0 %	0.1414 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($0.4 \leq E_r < 1.1$ GeV)	1.979	1.873	1.873 0 %	1.873 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($E_r \geq 1.1$ GeV)	2.331	1.967	2.15 9.3 %	1.784 -9.3 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	4.46	3.981	4.164 4.594 %	3.799 -4.594 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	1.762 0 %	1.762 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.2111	0.2028	0.2028 0 %	0.2028 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2539	0.2478	0.2478 0 %	0.2478 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.377 2.953 %	6.012 -2.953 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042 0 %	0.09042 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761 0 %	0.07761 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168 0 %	0.168 0 %
NS_K (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01626 0 %	0.01626 0 %
NS_K (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.01313 0 %	0.01313 0 %
NS_K (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004335 0 %	0.0004335 0 %
NS_K (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003048	0.003051	0.003051 0 %	0.003051 0 %
NS_K (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03287 0 %	0.03287 0 %
NS_K (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942 0 %	0.04942 0 %
NS_K (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768 0 %	0.05768 0 %
NS_K (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071 0 %	0.1071 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0007905 0 %	0.0007905 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.0007453 0 %	0.0007453 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.333e-05	7.333e-05	7.333e-05 0 %	7.333e-05 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002189	0.000219	0.000219 0 %	0.000219 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001828 0 %	0.001828 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916 0 %	0.005916 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954 0 %	0.005954 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187 0 %	0.01187 0 %
NS_K (1 μ -like ring): oscillation ν_e CCQE	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e CC coherent	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e CC all	0	0	0 0 %	0 0 %

Table 24: Effect of $f_{CCERC2;r}^{SK}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NSK (1 μ -like ring)	210.5	204.7	213.2	4.133 %
NSK (1 μ -like ring): ν_μ CCQE	166.4	155	155	0 %
NSK (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	41.93	20 %
NSK (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	1.14	20 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	4.315	4.199	5.038	20 %
NSK (1 μ -like ring): ν_μ CC all	200.6	195.1	203.2	4.109 %
NSK (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625	0 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466	0 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092	0 %
NSK (1 μ -like ring): ν_e CCQE	4.46	3.981	3.981	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	2.115	20 %
NSK (1 μ -like ring): ν_e CC coherent	0.2111	0.2028	0.2434	20 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2539	0.2478	0.2974	20 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.637	7.145 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %
NSK (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01626	0 %
NSK (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.01313	0 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004335	0 %
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003048	0.003051	0.003051	0 %
NSK (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03287	0 %
NSK (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0007905	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.0007453	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.333e-05	7.333e-05	7.333e-05	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002189	0.000219	0.000219	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001828	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC all	0	0	0	0 %

Table 25: Effect of $f_{CCnQE;r}^{SK}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NSK (1 μ -like ring)	210.5	204.7	208.5	1.832 %
NSK (1 μ -like ring): ν_μ CCQE	166.4	155	155	0 %
NSK (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	34.95	0 %
NSK (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.9503	0 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	4.315	4.199	4.199	0 %
NSK (1 μ -like ring): ν_μ CC all	200.6	195.1	195.1	0 %
NSK (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	3.43	111 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	3.094	111 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	6.524	111 %
NSK (1 μ -like ring): ν_μ CCQE	4.46	3.981	3.981	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	1.762	0 %
NSK (1 μ -like ring): ν_μ CC coherent	0.2111	0.2028	0.2028	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2539	0.2478	0.2478	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.194	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.1908	111 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.1638	111 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.3546	111 %
NSK (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01626	0 %
NSK (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.01313	0 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004335	0 %
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003048	0.003051	0.003051	0 %
NSK (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03287	0 %
NSK (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.1043	111 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.1217	111 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.226	111 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0007905	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.0007453	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.333e-05	7.333e-05	7.333e-05	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002189	0.000219	0.000219	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001828	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.01248	111 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.01256	111 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.02505	111 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC all	0	0	0	0 %

Table 26: Effect of $f_{NC;r}^{SK}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1 σ		BANFF tuned -1 σ	
NS_K (1 μ -like ring)	210.5	204.7	204.8	0.01695 %	204.7	-0.01695 %
NS_K (1 μ -like ring): ν_μ CCQE	166.4	155	155	0 %	155	0 %
NS_K (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	34.95	0 %	34.95	0 %
NS_K (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.9503	0 %	0.9503	0 %
NS_K (1 μ -like ring) ν_μ CC other (ν_μ disp)	4.315	4.199	4.199	0 %	4.199	0 %
NS_K (1 μ -like ring): ν_μ CC all	200.6	195.1	195.1	0 %	195.1	0 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625	0 %	1.625	0 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466	0 %	1.466	0 %
NS_K (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092	0 %	3.092	0 %
NS_K (1 μ -like ring): ν_e CCQE	4.46	3.981	3.981	0 %	3.981	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	1.762	0 %	1.762	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.2111	0.2028	0.2028	0 %	0.2028	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2539	0.2478	0.2478	0 %	0.2478	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.194	0 %	6.194	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %	0.09042	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %	0.07761	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %	0.168	0 %
NS_K (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.03252	100 %	0	-100 %
NS_K (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.02625	100 %	0	-100 %
NS_K (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.000867	100 %	0	-100 %
NS_K (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003048	0.003051	0.006101	100 %	0	-100 %
NS_K (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.06574	100 %	0	-100 %
NS_K (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %	0.04942	0 %
NS_K (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %	0.05768	0 %
NS_K (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %	0.1071	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.001581	100 %	0	-100 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.001491	100 %	0	-100 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.333e-05	7.333e-05	0.0001467	100 %	0	-100 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002189	0.000219	0.000438	100 %	0	-100 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.003656	100 %	0	-100 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %	0.005916	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %	0.005954	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %	0.01187	0 %
NS_K (1 μ -like ring): oscillation ν_e CCQE	0	0	0	0 %	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0	0 %	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC coherent	0	0	0	0 %	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0	0 %	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC all	0	0	0	0 %	0	0 %

Table 27: Effect of $f_{\nu_e; \tau}^{SK}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NS_K (1 μ -like ring)	210.5	204.7	205.3	204.2
NS_K (1 μ -like ring): ν_μ CCQE	166.4	155	155.6	154.5
NS_K (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	34.95	34.95
NS_K (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.9504	0.9501
NS_K (1 μ -like ring): ν_μ CC other (ν_μ disp)	4.315	4.199	4.199	4.199
NS_K (1 μ -like ring): ν_μ CC all	200.6	195.1	195.7	194.6
NS_K (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625	1.625
NS_K (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466	1.466
NS_K (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092	3.092
NS_K (1 μ -like ring): ν_μ all ($0 \leq E_t < 0.4\text{GeV}$)	6.443	6.2	6.775	5.624
NS_K (1 μ -like ring): ν_μ all ($0.4 \leq E_t < 0.5\text{GeV}$)	17.43	17.1	17.1	17.1
NS_K (1 μ -like ring): ν_μ all ($0.5 \leq E_t < 0.6\text{GeV}$)	34.52	34.1	34.1	34.1
NS_K (1 μ -like ring): ν_μ all ($0.6 \leq E_t < 0.7\text{GeV}$)	42.48	41.33	41.33	41.33
NS_K (1 μ -like ring): ν_μ all ($0.7 \leq E_t < 1\text{GeV}$)	55.91	52.77	52.77	52.77
NS_K (1 μ -like ring): ν_μ all ($1 \leq E_t < 1.5\text{GeV}$)	17.65	17.75	17.75	17.75
NS_K (1 μ -like ring): ν_μ all ($1.5 \leq E_t < 2.5\text{GeV}$)	12.43	11.77	11.77	11.77
NS_K (1 μ -like ring): ν_μ all ($2.5 \leq E_t < 3.5\text{GeV}$)	6.888	6.106	6.106	6.106
NS_K (1 μ -like ring): ν_μ all ($3.5 \leq E_t < 5\text{GeV}$)	7.037	7.906	7.906	7.906
NS_K (1 μ -like ring): ν_μ all ($5 \leq E_t < 7\text{GeV}$)	2.459	2.675	2.675	2.675
NS_K (1 μ -like ring): ν_μ all ($7 \leq E_t < 30\text{GeV}$)	0.5239	0.5428	0.5428	0.5428
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	4.46	3.981	3.981	3.981
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	1.762	1.762
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.2111	0.2028	0.2028	0.2028
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2539	0.2478	0.2478	0.2478
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.194	6.194
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0.09042
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0.07761
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC all	0.1716	0.168	0.168	0.168
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($0 \leq E_t < 0.4\text{GeV}$)	0.147	0.139	0.139	0.139
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.2075	0.1984	0.1984	0.1984
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.2899	0.281	0.281	0.281
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.3624	0.3572	0.3572	0.3572
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($0.7 \leq E_t < 1\text{GeV}$)	1.118	1.107	1.107	1.107
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($1 \leq E_t < 1.5\text{GeV}$)	1.492	1.51	1.51	1.51
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($1.5 \leq E_t < 2.5\text{GeV}$)	1.635	1.495	1.495	1.495
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.71	0.6208	0.6208	0.6208
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($3.5 \leq E_t < 5\text{GeV}$)	0.4132	0.4731	0.4731	0.4731
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($5 \leq E_t < 7\text{GeV}$)	0.1389	0.1523	0.1523	0.1523
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($7 \leq E_t < 30\text{GeV}$)	0.02833	0.02887	0.02887	0.02887
NS_K (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01626	0.01626
NS_K (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.01313	0.01313
NS_K (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004335	0.0004335
NS_K (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003048	0.003051	0.003051	0.003051
NS_K (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03287	0.03287
NS_K (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0.04942
NS_K (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0.05768
NS_K (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0.1071
NS_K (1 μ -like ring): ν_e all ($0 \leq E_t < 0.5\text{GeV}$)	0.004443	0.004347	0.004347	0.004347
NS_K (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.7\text{GeV}$)	0.007368	0.007722	0.007722	0.007722
NS_K (1 μ -like ring): ν_e all ($0.7 \leq E_t < 0.8\text{GeV}$)	0.003958	0.004275	0.004275	0.004275
NS_K (1 μ -like ring): ν_e all ($0.8 \leq E_t < 1.5\text{GeV}$)	0.02699	0.02869	0.02869	0.02869
NS_K (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.03865	0.03927	0.03927	0.03927
NS_K (1 μ -like ring): ν_e all ($2.5 \leq E_t < 4\text{GeV}$)	0.03615	0.03646	0.03646	0.03646
NS_K (1 μ -like ring): ν_e all ($4 \leq E_t < 30\text{GeV}$)	0.01889	0.01921	0.01921	0.01921
NS_K (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0007905	0.0007905
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.0007453	0.0007453
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.33e-05	7.33e-05	7.33e-05	7.33e-05
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002189	0.000219	0.000219	0.000219
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001828	0.001828
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0.005916
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0.005954
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0.01187
NS_K (1 μ -like ring): $\bar{\nu}_e$ all ($0 \leq E_t < 2.5\text{GeV}$)	0.005279	0.005397	0.005397	0.005397
NS_K (1 μ -like ring): $\bar{\nu}_e$ all ($2.5 \leq E_t < 30\text{GeV}$)	0.008164	0.008302	0.008302	0.008302
NS_K (1 μ -like ring): oscillation ν_e CCQE	0	0	0	0
NS_K (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0	0
NS_K (1 μ -like ring): oscillation ν_e CC coherent	0	0	0	0
NS_K (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0	0
NS_K (1 μ -like ring): oscillation ν_e CC all	0	0	0	0
NS_K (1 μ -like ring): oscillation ν_e all ($0 \leq E_t < 0.4\text{GeV}$)	0	0	0	0
NS_K (1 μ -like ring): oscillation ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0	0	0	0
NS_K (1 μ -like ring): oscillation ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0	0	0	0
NS_K (1 μ -like ring): oscillation ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0	0	0	0
NS_K (1 μ -like ring): oscillation ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	0	0	0	0
NS_K (1 μ -like ring): oscillation ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	0	0	0	0
NS_K (1 μ -like ring): oscillation ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0	0	0	0
NS_K (1 μ -like ring): oscillation ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0	0	0	0
NS_K (1 μ -like ring): oscillation ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	0	0	0	0
NS_K (1 μ -like ring): oscillation ν_e all ($5 \leq E_t < 7\text{GeV}$)	0	0	0	0
NS_K (1 μ -like ring): oscillation ν_e all ($7 \leq E_t < 30\text{GeV}$)	0	0	0	0

Table 28: Effect of $f_{0;t,r}^{banff}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NS_K (1 μ -like ring)	210.5	204.7	206.4	8147 %
NS_K (1 μ -like ring): ν_μ CCQE	166.4	155	156.7	1.07 %
NS_K (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	34.95	0.01178 %
NS_K (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.9529	0.2779 %
NS_K (1 μ -like ring): ν_μ CC other (ν_μ disp)	4.315	4.199	4.199	0 %
NS_K (1 μ -like ring): ν_μ CC all	200.6	195.1	196.8	0.8535 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.628	0.1273 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.467	0.02926 %
NS_K (1 μ -like ring): ν_μ NC all	3.218	3.092	3.094	0.0808 %
NS_K (1 μ -like ring): ν_μ all ($0 \leq E_t < 0.4\text{GeV}$)	6.443	6.2	6.2	0 %
NS_K (1 μ -like ring): ν_μ all ($0.4 \leq E_t < 0.5\text{GeV}$)	17.43	17.1	18.76	9.757 %
NS_K (1 μ -like ring): ν_μ all ($0.5 \leq E_t < 0.6\text{GeV}$)	34.52	34.1	34.1	0 %
NS_K (1 μ -like ring): ν_μ all ($0.6 \leq E_t < 0.7\text{GeV}$)	42.48	41.33	41.33	0 %
NS_K (1 μ -like ring): ν_μ all ($0.7 \leq E_t < 1\text{GeV}$)	55.91	52.77	52.77	0 %
NS_K (1 μ -like ring): ν_μ all ($1 \leq E_t < 1.5\text{GeV}$)	17.65	17.75	17.75	0 %
NS_K (1 μ -like ring): ν_μ all ($1.5 \leq E_t < 2.5\text{GeV}$)	12.43	11.77	11.77	0 %
NS_K (1 μ -like ring): ν_μ all ($2.5 \leq E_t < 3.5\text{GeV}$)	6.888	6.106	6.106	0 %
NS_K (1 μ -like ring): ν_μ all ($3.5 \leq E_t < 5\text{GeV}$)	7.037	7.906	7.906	0 %
NS_K (1 μ -like ring): ν_μ all ($5 \leq E_t < 7\text{GeV}$)	2.459	2.675	2.675	0 %
NS_K (1 μ -like ring): ν_μ all ($7 \leq E_t < 30\text{GeV}$)	0.5239	0.5428	0.5428	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	4.46	3.981	3.981	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	1.762	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.2111	0.2028	0.2028	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2539	0.2478	0.2478	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.194	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC all	0.1716	0.168	0.168	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($0 \leq E_t < 0.4\text{GeV}$)	0.147	0.139	0.139	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.2075	0.1984	0.1984	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.2899	0.281	0.281	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.3624	0.3572	0.3572	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($0.7 \leq E_t < 1\text{GeV}$)	1.118	1.107	1.107	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($1 \leq E_t < 1.5\text{GeV}$)	1.492	1.51	1.51	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($1.5 \leq E_t < 2.5\text{GeV}$)	1.635	1.495	1.495	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.71	0.6208	0.6208	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($3.5 \leq E_t < 5\text{GeV}$)	0.4132	0.4731	0.4731	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($5 \leq E_t < 7\text{GeV}$)	0.1389	0.1523	0.1523	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($7 \leq E_t < 30\text{GeV}$)	0.02833	0.02887	0.02887	0 %
NS_K (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01626	0 %
NS_K (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.01313	0 %
NS_K (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004335	0 %
NS_K (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003048	0.003051	0.003051	0 %
NS_K (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03287	0 %
NS_K (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %
NS_K (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %
NS_K (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %
NS_K (1 μ -like ring): ν_e all ($0 \leq E_t < 0.5\text{GeV}$)	0.004443	0.004347	0.004347	0 %
NS_K (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.7\text{GeV}$)	0.007368	0.007722	0.007722	0 %
NS_K (1 μ -like ring): ν_e all ($0.7 \leq E_t < 0.8\text{GeV}$)	0.003958	0.004275	0.004275	0 %
NS_K (1 μ -like ring): ν_e all ($0.8 \leq E_t < 1.5\text{GeV}$)	0.02699	0.02869	0.02869	0 %
NS_K (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.03865	0.03927	0.03927	0 %
NS_K (1 μ -like ring): ν_e all ($2.5 \leq E_t < 4\text{GeV}$)	0.03615	0.03646	0.03646	0 %
NS_K (1 μ -like ring): ν_e all ($4 \leq E_t < 30\text{GeV}$)	0.01889	0.01921	0.01921	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0007905	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.0007453	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.33e-05	7.33e-05	7.33e-05	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002189	0.000219	0.000219	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001828	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ all ($0 \leq E_t < 2.5\text{GeV}$)	0.005279	0.005397	0.005397	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ all ($2.5 \leq E_t < 30\text{GeV}$)	0.008164	0.008302	0.008302	0 %
NS_K (1 μ -like ring): oscillation ν_e CCQE	0	0	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC coherent	0	0	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC all	0	0	0	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0 \leq E_t < 0.4\text{GeV}$)	0	0	0	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0	0	0	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0	0	0	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0	0	0	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	0	0	0	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	0	0	0	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0	0	0	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0	0	0	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	0	0	0	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($5 \leq E_t < 7\text{GeV}$)	0	0	0	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($7 \leq E_t < 30\text{GeV}$)	0	0	0	0 %

Table 29: Effect of $f_{1:t,r}^{banff}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NSK (1 μ -like ring)	210.5	204.7	207.8	1.495 %
NSK (1 μ -like ring): ν_μ CCQE	166.4	155	158	1.911 %
NSK (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	35.02	0.2235 %
NSK (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.9594	0.9618 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	4.315	4.199	4.199	0 %
NSK (1 μ -like ring): ν_μ CC all	200.6	195.1	198.2	1.563 %
NSK (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.634	0.5066 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.468	0.09125 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	3.102	0.3096 %
NSK (1 μ -like ring): ν_μ all ($0 \leq E_t < 0.4\text{GeV}$)	6.443	6.2	6.2	0 %
NSK (1 μ -like ring): ν_μ all ($0.4 \leq E_t < 0.5\text{GeV}$)	17.43	17.1	17.1	0 %
NSK (1 μ -like ring): ν_μ all ($0.5 \leq E_t < 0.6\text{GeV}$)	34.52	34.1	37.16	8.974 %
NSK (1 μ -like ring): ν_μ all ($0.6 \leq E_t < 0.7\text{GeV}$)	42.48	41.33	41.33	0 %
NSK (1 μ -like ring): ν_μ all ($0.7 \leq E_t < 1\text{GeV}$)	55.91	52.77	52.77	0 %
NSK (1 μ -like ring): ν_μ all ($1 \leq E_t < 1.5\text{GeV}$)	17.65	17.75	17.75	0 %
NSK (1 μ -like ring): ν_μ all ($1.5 \leq E_t < 2.5\text{GeV}$)	12.43	11.77	11.77	0 %
NSK (1 μ -like ring): ν_μ all ($2.5 \leq E_t < 3.5\text{GeV}$)	6.888	6.106	6.106	0 %
NSK (1 μ -like ring): ν_μ all ($3.5 \leq E_t < 5\text{GeV}$)	7.037	7.906	7.906	0 %
NSK (1 μ -like ring): ν_μ all ($5 \leq E_t < 7\text{GeV}$)	2.459	2.675	2.675	0 %
NSK (1 μ -like ring): ν_μ all ($7 \leq E_t < 30\text{GeV}$)	0.5239	0.5428	0.5428	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	4.46	3.981	3.981	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	1.762	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.2111	0.2028	0.2028	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2539	0.2478	0.2478	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.194	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC all	0.1716	0.168	0.168	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($0 \leq E_t < 0.4\text{GeV}$)	0.147	0.139	0.139	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.2075	0.1984	0.1984	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.2899	0.281	0.281	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.3624	0.3572	0.3572	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($0.7 \leq E_t < 1\text{GeV}$)	1.118	1.107	1.107	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($1 \leq E_t < 1.5\text{GeV}$)	1.492	1.51	1.51	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($1.5 \leq E_t < 2.5\text{GeV}$)	1.635	1.495	1.495	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.71	0.6208	0.6208	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($3.5 \leq E_t < 5\text{GeV}$)	0.4132	0.4731	0.4731	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($5 \leq E_t < 7\text{GeV}$)	0.1389	0.1523	0.1523	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($7 \leq E_t < 30\text{GeV}$)	0.02833	0.02887	0.02887	0 %
NSK (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01626	0 %
NSK (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.01313	0 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004335	0 %
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003048	0.003051	0.003051	0 %
NSK (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03287	0 %
NSK (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %
NSK (1 μ -like ring): ν_e all ($0 \leq E_t < 0.5\text{GeV}$)	0.004443	0.004347	0.004347	0 %
NSK (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.7\text{GeV}$)	0.007368	0.007722	0.007722	0 %
NSK (1 μ -like ring): ν_e all ($0.7 \leq E_t < 0.8\text{GeV}$)	0.003958	0.004275	0.004275	0 %
NSK (1 μ -like ring): ν_e all ($0.8 \leq E_t < 1.5\text{GeV}$)	0.02699	0.02869	0.02869	0 %
NSK (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.03865	0.03927	0.03927	0 %
NSK (1 μ -like ring): ν_e all ($2.5 \leq E_t < 4\text{GeV}$)	0.03615	0.03646	0.03646	0 %
NSK (1 μ -like ring): ν_e all ($4 \leq E_t < 30\text{GeV}$)	0.01889	0.01921	0.01921	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0007905	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.0007453	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.33e-05	7.33e-05	7.33e-05	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002189	0.000219	0.000219	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001828	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ all ($0 \leq E_t < 2.5\text{GeV}$)	0.005279	0.005397	0.005397	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ all ($2.5 \leq E_t < 30\text{GeV}$)	0.008164	0.008302	0.008302	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC all	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0 \leq E_t < 0.4\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($5 \leq E_t < 7\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($7 \leq E_t < 30\text{GeV}$)	0	0	0	0 %

Table 30: Effect of $f_{2;t,r}^{banff}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NSK (1 μ -like ring)	210.5	204.7	208.2	1.707 %
NSK (1 μ -like ring): ν_μ CCQE	166.4	155	158.2	2.02 %
NSK (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	35.28	0.9572 %
NSK (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.962	1.235 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	4.315	4.199	4.199	0.001422 %
NSK (1 μ -like ring): ν_μ CC all	200.6	195.1	198.6	1.782 %
NSK (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.64	0.9105 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.469	0.1885 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	3.11	0.568 %
NSK (1 μ -like ring): ν_μ all ($0 \leq E_t < 0.4\text{GeV}$)	6.443	6.2	6.2	0 %
NSK (1 μ -like ring): ν_μ all ($0.4 \leq E_t < 0.5\text{GeV}$)	17.43	17.1	17.1	0 %
NSK (1 μ -like ring): ν_μ all ($0.5 \leq E_t < 0.6\text{GeV}$)	34.52	34.1	34.1	0 %
NSK (1 μ -like ring): ν_μ all ($0.6 \leq E_t < 0.7\text{GeV}$)	42.48	41.33	44.82	8.457 %
NSK (1 μ -like ring): ν_μ all ($0.7 \leq E_t < 1\text{GeV}$)	55.91	52.77	52.77	0 %
NSK (1 μ -like ring): ν_μ all ($1 \leq E_t < 1.5\text{GeV}$)	17.65	17.75	17.75	0 %
NSK (1 μ -like ring): ν_μ all ($1.5 \leq E_t < 2.5\text{GeV}$)	12.43	11.77	11.77	0 %
NSK (1 μ -like ring): ν_μ all ($2.5 \leq E_t < 3.5\text{GeV}$)	6.888	6.106	6.106	0 %
NSK (1 μ -like ring): ν_μ all ($3.5 \leq E_t < 5\text{GeV}$)	7.037	7.906	7.906	0 %
NSK (1 μ -like ring): ν_μ all ($5 \leq E_t < 7\text{GeV}$)	2.459	2.675	2.675	0 %
NSK (1 μ -like ring): ν_μ all ($7 \leq E_t < 30\text{GeV}$)	0.5239	0.5428	0.5428	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	4.46	3.981	3.981	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	1.762	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.2111	0.2028	0.2028	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2539	0.2478	0.2478	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.194	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0 \leq E_t < 0.4\text{GeV}$)	0.147	0.139	0.139	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.2075	0.1984	0.1984	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.2899	0.281	0.281	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.3624	0.3572	0.3572	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.7 \leq E_t < 1\text{GeV}$)	1.118	1.107	1.107	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($1 \leq E_t < 1.5\text{GeV}$)	1.492	1.51	1.51	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($1.5 \leq E_t < 2.5\text{GeV}$)	1.635	1.495	1.495	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.71	0.6208	0.6208	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($3.5 \leq E_t < 5\text{GeV}$)	0.4132	0.4731	0.4731	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($5 \leq E_t < 7\text{GeV}$)	0.1389	0.1523	0.1523	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($7 \leq E_t < 30\text{GeV}$)	0.02833	0.02887	0.02887	0 %
NSK (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01626	0 %
NSK (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.01313	0 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004335	0 %
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003048	0.003051	0.003051	0 %
NSK (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03287	0 %
NSK (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %
NSK (1 μ -like ring): ν_e all ($0 \leq E_t < 0.5\text{GeV}$)	0.004443	0.004347	0.004347	0 %
NSK (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.7\text{GeV}$)	0.007368	0.007722	0.007722	0 %
NSK (1 μ -like ring): ν_e all ($0.7 \leq E_t < 0.8\text{GeV}$)	0.003958	0.004275	0.004275	0 %
NSK (1 μ -like ring): ν_e all ($0.8 \leq E_t < 1.5\text{GeV}$)	0.02699	0.02869	0.02869	0 %
NSK (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.03865	0.03927	0.03927	0 %
NSK (1 μ -like ring): ν_e all ($2.5 \leq E_t < 4\text{GeV}$)	0.03615	0.03646	0.03646	0 %
NSK (1 μ -like ring): ν_e all ($4 \leq E_t < 30\text{GeV}$)	0.01889	0.01921	0.01921	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0007905	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.0007453	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.33e-05	7.33e-05	7.33e-05	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002189	0.000219	0.000219	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001828	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ all ($0 \leq E_t < 2.5\text{GeV}$)	0.005279	0.005397	0.005397	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ all ($2.5 \leq E_t < 30\text{GeV}$)	0.008164	0.008302	0.008302	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC all	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0 \leq E_t < 0.4\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($5 \leq E_t < 7\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($7 \leq E_t < 30\text{GeV}$)	0	0	0	0 %

Table 31: Effect of $f_{3;t,r}^{banff}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NS_K (1 μ -like ring)	210.5	204.7	210.3	2.706 %
NS_K (1 μ -like ring): ν_μ CCQE	166.4	155	159.4	2.8 %
NS_K (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	36.07	3.211 %
NS_K (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.9765	2.763 %
NS_K (1 μ -like ring): ν_μ CC other (ν_μ disp)	4.315	4.199	4.201	0.06811 %
NS_K (1 μ -like ring): ν_μ CC all	200.6	195.1	200.6	2.815 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.663	2.336 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.476	0.6316 %
NS_K (1 μ -like ring): ν_μ NC all	3.218	3.092	3.139	1.528 %
NS_K (1 μ -like ring): ν_μ all ($0 \leq E_t < 0.4\text{GeV}$)	6.443	6.2	6.2	0 %
NS_K (1 μ -like ring): ν_μ all ($0.4 \leq E_t < 0.5\text{GeV}$)	17.43	17.1	17.1	0 %
NS_K (1 μ -like ring): ν_μ all ($0.5 \leq E_t < 0.6\text{GeV}$)	34.52	34.1	34.1	0 %
NS_K (1 μ -like ring): ν_μ all ($0.6 \leq E_t < 0.7\text{GeV}$)	42.48	41.33	41.33	0 %
NS_K (1 μ -like ring): ν_μ all ($0.7 \leq E_t < 1\text{GeV}$)	55.91	52.77	58.31	10.5 %
NS_K (1 μ -like ring): ν_μ all ($1 \leq E_t < 1.5\text{GeV}$)	17.65	17.75	17.75	0 %
NS_K (1 μ -like ring): ν_μ all ($1.5 \leq E_t < 2.5\text{GeV}$)	12.43	11.77	11.77	0 %
NS_K (1 μ -like ring): ν_μ all ($2.5 \leq E_t < 3.5\text{GeV}$)	6.888	6.106	6.106	0 %
NS_K (1 μ -like ring): ν_μ all ($3.5 \leq E_t < 5\text{GeV}$)	7.037	7.906	7.906	0 %
NS_K (1 μ -like ring): ν_μ all ($5 \leq E_t < 7\text{GeV}$)	2.459	2.675	2.675	0 %
NS_K (1 μ -like ring): ν_μ all ($7 \leq E_t < 30\text{GeV}$)	0.5239	0.5428	0.5428	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	4.46	3.981	3.981	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	1.762	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.2111	0.2028	0.2028	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2539	0.2478	0.2478	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.194	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC all	0.1716	0.168	0.168	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($0 \leq E_t < 0.4\text{GeV}$)	0.147	0.139	0.139	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.2075	0.1984	0.1984	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.2899	0.281	0.281	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.3624	0.3572	0.3572	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($0.7 \leq E_t < 1\text{GeV}$)	1.118	1.107	1.107	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($1 \leq E_t < 1.5\text{GeV}$)	1.492	1.51	1.51	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($1.5 \leq E_t < 2.5\text{GeV}$)	1.635	1.495	1.495	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.71	0.6208	0.6208	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($3.5 \leq E_t < 5\text{GeV}$)	0.4132	0.4731	0.4731	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($5 \leq E_t < 7\text{GeV}$)	0.1389	0.1523	0.1523	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($7 \leq E_t < 30\text{GeV}$)	0.02833	0.02887	0.02887	0 %
NS_K (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01626	0 %
NS_K (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.01313	0 %
NS_K (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004335	0 %
NS_K (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003048	0.003051	0.003051	0 %
NS_K (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03287	0 %
NS_K (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %
NS_K (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %
NS_K (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %
NS_K (1 μ -like ring): ν_e all ($0 \leq E_t < 0.5\text{GeV}$)	0.004443	0.004347	0.004347	0 %
NS_K (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.7\text{GeV}$)	0.007368	0.007722	0.007722	0 %
NS_K (1 μ -like ring): ν_e all ($0.7 \leq E_t < 0.8\text{GeV}$)	0.003958	0.004275	0.004275	0 %
NS_K (1 μ -like ring): ν_e all ($0.8 \leq E_t < 1.5\text{GeV}$)	0.02699	0.02869	0.02869	0 %
NS_K (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.03865	0.03927	0.03927	0 %
NS_K (1 μ -like ring): ν_e all ($2.5 \leq E_t < 4\text{GeV}$)	0.03615	0.03646	0.03646	0 %
NS_K (1 μ -like ring): ν_e all ($4 \leq E_t < 30\text{GeV}$)	0.01889	0.01921	0.01921	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0007905	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.0007453	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.33e-05	7.33e-05	7.33e-05	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002189	0.000219	0.000219	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001828	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ all ($0 \leq E_t < 2.5\text{GeV}$)	0.005279	0.005397	0.005397	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ all ($2.5 \leq E_t < 30\text{GeV}$)	0.008164	0.008302	0.008302	0 %
NS_K (1 μ -like ring): oscillation ν_e CCQE	0	0	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC coherent	0	0	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC all	0	0	0	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0 \leq E_t < 0.4\text{GeV}$)	0	0	0	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0	0	0	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0	0	0	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0	0	0	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	0	0	0	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	0	0	0	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0	0	0	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0	0	0	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	0	0	0	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($5 \leq E_t < 7\text{GeV}$)	0	0	0	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($7 \leq E_t < 30\text{GeV}$)	0	0	0	0 %

Table 32: Effect of $f_{4;t,r}^{banff}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NSK (1 μ -like ring)	210.5	204.7	206.4	0.8026 %
NSK (1 μ -like ring): ν_μ CCQE	166.4	155	156	0.6332 %
NSK (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	35.54	1.693 %
NSK (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.96	1.024 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	4.315	4.199	4.222	0.5606 %
NSK (1 μ -like ring): ν_μ CC all	200.6	195.1	196.7	0.8233 %
NSK (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.646	1.242 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.483	1.129 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	3.129	1.189 %
NSK (1 μ -like ring): ν_μ all ($0 \leq E_t < 0.4\text{GeV}$)	6.443	6.2	6.2	0 %
NSK (1 μ -like ring): ν_μ all ($0.4 \leq E_t < 0.5\text{GeV}$)	17.43	17.1	17.1	0 %
NSK (1 μ -like ring): ν_μ all ($0.5 \leq E_t < 0.6\text{GeV}$)	34.52	34.1	34.1	0 %
NSK (1 μ -like ring): ν_μ all ($0.6 \leq E_t < 0.7\text{GeV}$)	42.48	41.33	41.33	0 %
NSK (1 μ -like ring): ν_μ all ($0.7 \leq E_t < 1\text{GeV}$)	55.91	52.77	52.77	0 %
NSK (1 μ -like ring): ν_μ all ($1 \leq E_t < 1.5\text{GeV}$)	17.65	17.75	19.39	9.26 %
NSK (1 μ -like ring): ν_μ all ($1.5 \leq E_t < 2.5\text{GeV}$)	12.43	11.77	11.77	0 %
NSK (1 μ -like ring): ν_μ all ($2.5 \leq E_t < 3.5\text{GeV}$)	6.888	6.106	6.106	0 %
NSK (1 μ -like ring): ν_μ all ($3.5 \leq E_t < 5\text{GeV}$)	7.037	7.906	7.906	0 %
NSK (1 μ -like ring): ν_μ all ($5 \leq E_t < 7\text{GeV}$)	2.459	2.675	2.675	0 %
NSK (1 μ -like ring): ν_μ all ($7 \leq E_t < 30\text{GeV}$)	0.5239	0.5428	0.5428	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	4.46	3.981	3.981	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	1.762	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.2111	0.2028	0.2028	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2539	0.2478	0.2478	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.194	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0 \leq E_t < 0.4\text{GeV}$)	0.147	0.139	0.139	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.2075	0.1984	0.1984	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.2899	0.281	0.281	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.3624	0.3572	0.3572	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.7 \leq E_t < 1\text{GeV}$)	1.118	1.107	1.107	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($1 \leq E_t < 1.5\text{GeV}$)	1.492	1.51	1.51	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($1.5 \leq E_t < 2.5\text{GeV}$)	1.635	1.495	1.495	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.71	0.6208	0.6208	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($3.5 \leq E_t < 5\text{GeV}$)	0.4132	0.4731	0.4731	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($5 \leq E_t < 7\text{GeV}$)	0.1389	0.1523	0.1523	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($7 \leq E_t < 30\text{GeV}$)	0.02833	0.02887	0.02887	0 %
NSK (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01626	0 %
NSK (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.01313	0 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004335	0 %
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003048	0.003051	0.003051	0 %
NSK (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03287	0 %
NSK (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %
NSK (1 μ -like ring): ν_e all ($0 \leq E_t < 0.5\text{GeV}$)	0.004443	0.004347	0.004347	0 %
NSK (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.7\text{GeV}$)	0.007368	0.007722	0.007722	0 %
NSK (1 μ -like ring): ν_e all ($0.7 \leq E_t < 0.8\text{GeV}$)	0.003958	0.004275	0.004275	0 %
NSK (1 μ -like ring): ν_e all ($0.8 \leq E_t < 1.5\text{GeV}$)	0.02699	0.02869	0.02869	0 %
NSK (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.03865	0.03927	0.03927	0 %
NSK (1 μ -like ring): ν_e all ($2.5 \leq E_t < 4\text{GeV}$)	0.03615	0.03646	0.03646	0 %
NSK (1 μ -like ring): ν_e all ($4 \leq E_t < 30\text{GeV}$)	0.01889	0.01921	0.01921	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0007905	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.0007453	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.33e-05	7.33e-05	7.33e-05	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002189	0.000219	0.000219	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001828	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ all ($0 \leq E_t < 2.5\text{GeV}$)	0.005279	0.005397	0.005397	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ all ($2.5 \leq E_t < 30\text{GeV}$)	0.008164	0.008302	0.008302	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC all	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0 \leq E_t < 0.4\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($5 \leq E_t < 7\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($7 \leq E_t < 30\text{GeV}$)	0	0	0	0 %

Table 33: Effect of $f_{5;t,r}^{banff}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NSK (1 μ -like ring)	210.5	204.7	205.7	0.4662 %
NSK (1 μ -like ring): ν_μ CCQE	166.4	155	155.4	0.2321 %
NSK (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	35.43	1.386 %
NSK (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.9602	1.049 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	4.315	4.199	4.254	1.317 %
NSK (1 μ -like ring): ν_μ CC all	200.6	195.1	196	0.4662 %
NSK (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.646	1.255 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.491	1.672 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	3.137	1.453 %
NSK (1 μ -like ring): ν_μ all ($0 \leq E_t < 0.4\text{GeV}$)	6.443	6.2	6.2	0 %
NSK (1 μ -like ring): ν_μ all ($0.4 \leq E_t < 0.5\text{GeV}$)	17.43	17.1	17.1	0 %
NSK (1 μ -like ring): ν_μ all ($0.5 \leq E_t < 0.6\text{GeV}$)	34.52	34.1	34.1	0 %
NSK (1 μ -like ring): ν_μ all ($0.6 \leq E_t < 0.7\text{GeV}$)	42.48	41.33	41.33	0 %
NSK (1 μ -like ring): ν_μ all ($0.7 \leq E_t < 1\text{GeV}$)	55.91	52.77	52.77	0 %
NSK (1 μ -like ring): ν_μ all ($1 \leq E_t < 1.5\text{GeV}$)	17.65	17.75	17.75	0 %
NSK (1 μ -like ring): ν_μ all ($1.5 \leq E_t < 2.5\text{GeV}$)	12.43	11.77	12.72	8.113 %
NSK (1 μ -like ring): ν_μ all ($2.5 \leq E_t < 3.5\text{GeV}$)	6.888	6.106	6.106	0 %
NSK (1 μ -like ring): ν_μ all ($3.5 \leq E_t < 5\text{GeV}$)	7.037	7.906	7.906	0 %
NSK (1 μ -like ring): ν_μ all ($5 \leq E_t < 7\text{GeV}$)	2.459	2.675	2.675	0 %
NSK (1 μ -like ring): ν_μ all ($7 \leq E_t < 30\text{GeV}$)	0.5239	0.5428	0.5428	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	4.46	3.981	3.981	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	1.762	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.2111	0.2028	0.2028	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2539	0.2478	0.2478	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.194	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %
NSK (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01626	0 %
NSK (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.01313	0 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004335	0 %
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003048	0.003051	0.003051	0 %
NSK (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03287	0 %
NSK (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %
NSK (1 μ -like ring): ν_e all ($0 \leq E_t < 0.5\text{GeV}$)	0.004443	0.004347	0.004347	0 %
NSK (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.7\text{GeV}$)	0.007368	0.007722	0.007722	0 %
NSK (1 μ -like ring): ν_e all ($0.7 \leq E_t < 0.8\text{GeV}$)	0.003958	0.004275	0.004275	0 %
NSK (1 μ -like ring): ν_e all ($0.8 \leq E_t < 1.5\text{GeV}$)	0.02699	0.02869	0.02869	0 %
NSK (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.03865	0.03927	0.03927	0 %
NSK (1 μ -like ring): ν_e all ($2.5 \leq E_t < 4\text{GeV}$)	0.03615	0.03646	0.03646	0 %
NSK (1 μ -like ring): ν_e all ($4 \leq E_t < 30\text{GeV}$)	0.01889	0.01921	0.01921	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0007905	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.0007453	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.33e-05	7.33e-05	7.33e-05	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002189	0.000219	0.000219	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001828	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ all ($0 \leq E_t < 2.5\text{GeV}$)	0.005279	0.005397	0.005397	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ all ($2.5 \leq E_t < 30\text{GeV}$)	0.008164	0.008302	0.008302	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC all	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0 \leq E_t < 0.4\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($5 \leq E_t < 7\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($7 \leq E_t < 30\text{GeV}$)	0	0	0	0 %

Table 34: Effect of $f_{6;t,r}^{banff}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NS_K (1 μ -like ring)	210.5	204.7	205.2	204.3
NS_K (1 μ -like ring): ν_μ CCQE	166.4	155	155.2	154.9
NS_K (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	35.16	34.73
NS_K (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.956	0.9446
NS_K (1 μ -like ring): ν_μ CC other (ν_μ disp)	4.315	4.199	4.259	4.138
NS_K (1 μ -like ring): ν_μ CC all	200.6	195.1	195.6	194.7
NS_K (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.636	1.615
NS_K (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.485	1.448
NS_K (1 μ -like ring): ν_μ NC all	3.218	3.092	3.121	3.063
NS_K (1 μ -like ring): ν_μ all ($0 \leq E_t < 0.4\text{GeV}$)	6.443	6.2	6.2	6.2
NS_K (1 μ -like ring): ν_μ all ($0.4 \leq E_t < 0.5\text{GeV}$)	17.43	17.1	17.1	17.1
NS_K (1 μ -like ring): ν_μ all ($0.5 \leq E_t < 0.6\text{GeV}$)	34.52	34.1	34.1	34.1
NS_K (1 μ -like ring): ν_μ all ($0.6 \leq E_t < 0.7\text{GeV}$)	42.48	41.33	41.33	41.33
NS_K (1 μ -like ring): ν_μ all ($0.7 \leq E_t < 1\text{GeV}$)	55.91	52.77	52.77	52.77
NS_K (1 μ -like ring): ν_μ all ($1 \leq E_t < 1.5\text{GeV}$)	17.65	17.75	17.75	17.75
NS_K (1 μ -like ring): ν_μ all ($1.5 \leq E_t < 2.5\text{GeV}$)	12.43	11.77	11.77	11.77
NS_K (1 μ -like ring): ν_μ all ($2.5 \leq E_t < 3.5\text{GeV}$)	6.888	6.106	6.55	5.661
NS_K (1 μ -like ring): ν_μ all ($3.5 \leq E_t < 5\text{GeV}$)	7.037	7.906	0 %	7.906
NS_K (1 μ -like ring): ν_μ all ($5 \leq E_t < 7\text{GeV}$)	2.459	2.675	0 %	2.675
NS_K (1 μ -like ring): ν_μ all ($7 \leq E_t < 30\text{GeV}$)	0.5239	0.5428	0 %	0.5428
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	4.46	3.981	3.981	3.981
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	1.762	1.762
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.2111	0.2028	0.2028	0.2028
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2539	0.2478	0.2478	0.2478
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.194	6.194
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0.09042
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0.07761
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC all	0.1716	0.168	0.168	0.168
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($0 \leq E_t < 0.4\text{GeV}$)	0.147	0.139	0.139	0.139
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.2075	0.1984	0.1984	0.1984
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.2899	0.281	0.281	0.281
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.3624	0.3572	0.3572	0.3572
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($0.7 \leq E_t < 1\text{GeV}$)	1.118	1.107	1.107	1.107
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($1 \leq E_t < 1.5\text{GeV}$)	1.492	1.51	1.51	1.51
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($1.5 \leq E_t < 2.5\text{GeV}$)	1.635	1.495	1.495	1.495
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.71	0.6208	0.6208	0.6208
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($3.5 \leq E_t < 5\text{GeV}$)	0.4132	0.4731	0.4731	0.4731
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($5 \leq E_t < 7\text{GeV}$)	0.1389	0.1523	0.1523	0.1523
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($7 \leq E_t < 30\text{GeV}$)	0.02833	0.02887	0 %	0.02887
NS_K (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01626	0.01626
NS_K (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.01313	0.01313
NS_K (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004335	0.0004335
NS_K (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003048	0.003051	0.003051	0.003051
NS_K (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03287	0.03287
NS_K (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0.04942
NS_K (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0.05768
NS_K (1 μ -like ring): ν_e NC all	0.1061	0.1071	0 %	0.1071
NS_K (1 μ -like ring): ν_e all ($0 \leq E_t < 0.5\text{GeV}$)	0.004443	0.004347	0.004347	0.004347
NS_K (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.7\text{GeV}$)	0.007368	0.007722	0.007722	0.007722
NS_K (1 μ -like ring): ν_e all ($0.7 \leq E_t < 0.8\text{GeV}$)	0.003958	0.004275	0.004275	0.004275
NS_K (1 μ -like ring): ν_e all ($0.8 \leq E_t < 1.5\text{GeV}$)	0.02699	0.02869	0.02869	0.02869
NS_K (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.03865	0.03927	0.03927	0.03927
NS_K (1 μ -like ring): ν_e all ($2.5 \leq E_t < 4\text{GeV}$)	0.03615	0.03646	0.03646	0.03646
NS_K (1 μ -like ring): ν_e all ($4 \leq E_t < 30\text{GeV}$)	0.01889	0.01921	0.01921	0.01921
NS_K (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0007905	0.0007905
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.0007453	0.0007453
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.33e-05	7.33e-05	7.33e-05	7.33e-05
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002189	0.000219	0.000219	0.000219
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001828	0.001828
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0.005916
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0.005954
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0 %	0.01187
NS_K (1 μ -like ring): $\bar{\nu}_e$ all ($0 \leq E_t < 2.5\text{GeV}$)	0.005279	0.005397	0.005397	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ all ($2.5 \leq E_t < 30\text{GeV}$)	0.008164	0.008302	0 %	0.008302
NS_K (1 μ -like ring): oscillation ν_e CCQE	0	0	0 %	0 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0 %	0 %
NS_K (1 μ -like ring): oscillation ν_e CC coherent	0	0	0 %	0 %
NS_K (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0 %	0 %
NS_K (1 μ -like ring): oscillation ν_e CC all	0	0	0 %	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0 \leq E_t < 0.4\text{GeV}$)	0	0	0 %	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0	0	0 %	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0	0	0 %	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0	0	0 %	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	0	0	0 %	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	0	0	0 %	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0	0	0 %	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0	0	0 %	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	0	0	0 %	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($5 \leq E_t < 7\text{GeV}$)	0	0	0 %	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($7 \leq E_t < 30\text{GeV}$)	0	0	0 %	0 %

Table 35: Effect of $f_{7;t,r}^{banff}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NSK (1 μ -like ring)	210.5	204.7	205.4	0.3229 %
NSK (1 μ -like ring): ν_μ CCQE	166.4	155	155.3	0.1541 %
NSK (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	35.2	0.7295 %
NSK (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.9579	0.8063 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	4.315	4.199	4.313	2.726 %
NSK (1 μ -like ring): ν_μ CC all	200.6	195.1	195.8	0.3157 %
NSK (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.644	1.11 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.494	1.848 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	3.137	1.46 %
NSK (1 μ -like ring): ν_μ all ($0 \leq E_t < 0.4\text{GeV}$)	6.443	6.2	6.2	0 %
NSK (1 μ -like ring): ν_μ all ($0.4 \leq E_t < 0.5\text{GeV}$)	17.43	17.1	17.1	0 %
NSK (1 μ -like ring): ν_μ all ($0.5 \leq E_t < 0.6\text{GeV}$)	34.52	34.1	34.1	0 %
NSK (1 μ -like ring): ν_μ all ($0.6 \leq E_t < 0.7\text{GeV}$)	42.48	41.33	41.33	0 %
NSK (1 μ -like ring): ν_μ all ($0.7 \leq E_t < 1\text{GeV}$)	55.91	52.77	52.77	0 %
NSK (1 μ -like ring): ν_μ all ($1 \leq E_t < 1.5\text{GeV}$)	17.65	17.75	17.75	0 %
NSK (1 μ -like ring): ν_μ all ($1.5 \leq E_t < 2.5\text{GeV}$)	12.43	11.77	11.77	0 %
NSK (1 μ -like ring): ν_μ all ($2.5 \leq E_t < 3.5\text{GeV}$)	6.888	6.106	6.106	0 %
NSK (1 μ -like ring): ν_μ all ($3.5 \leq E_t < 5\text{GeV}$)	7.037	7.906	8.567	8.362 %
NSK (1 μ -like ring): ν_μ all ($5 \leq E_t < 7\text{GeV}$)	2.459	2.675	2.675	0 %
NSK (1 μ -like ring): ν_μ all ($7 \leq E_t < 30\text{GeV}$)	0.5239	0.5428	0.5428	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	4.46	3.981	3.981	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	1.762	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.2111	0.2028	0.2028	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2539	0.2478	0.2478	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.194	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0 \leq E_t < 0.4\text{GeV}$)	0.147	0.139	0.139	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.2075	0.1984	0.1984	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.2899	0.281	0.281	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.3624	0.3572	0.3572	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.7 \leq E_t < 1\text{GeV}$)	1.118	1.107	1.107	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($1 \leq E_t < 1.5\text{GeV}$)	1.492	1.51	1.51	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($1.5 \leq E_t < 2.5\text{GeV}$)	1.635	1.495	1.495	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.71	0.6208	0.6208	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($3.5 \leq E_t < 5\text{GeV}$)	0.4132	0.4731	0.4731	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($5 \leq E_t < 7\text{GeV}$)	0.1389	0.1523	0.1523	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($7 \leq E_t < 30\text{GeV}$)	0.02833	0.02887	0.02887	0 %
NSK (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01626	0 %
NSK (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.01313	0 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004335	0 %
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003048	0.003051	0.003051	0 %
NSK (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03287	0 %
NSK (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %
NSK (1 μ -like ring): ν_e all ($0 \leq E_t < 0.5\text{GeV}$)	0.004443	0.004347	0.004347	0 %
NSK (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.7\text{GeV}$)	0.007368	0.007722	0.007722	0 %
NSK (1 μ -like ring): ν_e all ($0.7 \leq E_t < 0.8\text{GeV}$)	0.003958	0.004275	0.004275	0 %
NSK (1 μ -like ring): ν_e all ($0.8 \leq E_t < 1.5\text{GeV}$)	0.02699	0.02869	0.02869	0 %
NSK (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.03865	0.03927	0.03927	0 %
NSK (1 μ -like ring): ν_e all ($2.5 \leq E_t < 4\text{GeV}$)	0.03615	0.03646	0.03646	0 %
NSK (1 μ -like ring): ν_e all ($4 \leq E_t < 30\text{GeV}$)	0.01889	0.01921	0.01921	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0007905	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.0007453	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.33e-05	7.33e-05	7.33e-05	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002189	0.000219	0.000219	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001828	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ all ($0 \leq E_t < 2.5\text{GeV}$)	0.005279	0.005397	0.005397	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ all ($2.5 \leq E_t < 30\text{GeV}$)	0.008164	0.008302	0.008302	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC all	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0 \leq E_t < 0.4\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($5 \leq E_t < 7\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($7 \leq E_t < 30\text{GeV}$)	0	0	0	0 %

Table 36: Effect of $f_{8;t,r}^{banff}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NSK (1 μ -like ring)	210.5	204.7	205	0.1407 %
NSK (1 μ -like ring): ν_μ CCQE	166.4	155	155.1	0.04339 %
NSK (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	35.05	0.2995 %
NSK (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.9535	0.3444 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	4.315	4.199	4.283	2.018 %
NSK (1 μ -like ring): ν_μ CC all	200.6	195.1	195.4	0.1332 %
NSK (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.635	0.6108 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.485	1.237 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	3.12	0.908 %
NSK (1 μ -like ring): ν_μ all ($0 \leq E_t < 0.4\text{GeV}$)	6.443	6.2	6.2	0 %
NSK (1 μ -like ring): ν_μ all ($0.4 \leq E_t < 0.5\text{GeV}$)	17.43	17.1	17.1	0 %
NSK (1 μ -like ring): ν_μ all ($0.5 \leq E_t < 0.6\text{GeV}$)	34.52	34.1	34.1	0 %
NSK (1 μ -like ring): ν_μ all ($0.6 \leq E_t < 0.7\text{GeV}$)	42.48	41.33	41.33	0 %
NSK (1 μ -like ring): ν_μ all ($0.7 \leq E_t < 1\text{GeV}$)	55.91	52.77	52.77	0 %
NSK (1 μ -like ring): ν_μ all ($1 \leq E_t < 1.5\text{GeV}$)	17.65	17.75	17.75	0 %
NSK (1 μ -like ring): ν_μ all ($1.5 \leq E_t < 2.5\text{GeV}$)	12.43	11.77	11.77	0 %
NSK (1 μ -like ring): ν_μ all ($2.5 \leq E_t < 3.5\text{GeV}$)	6.888	6.106	6.106	0 %
NSK (1 μ -like ring): ν_μ all ($3.5 \leq E_t < 5\text{GeV}$)	7.037	7.906	7.906	0 %
NSK (1 μ -like ring): ν_μ all ($5 \leq E_t < 7\text{GeV}$)	2.459	2.675	2.963	10.77 %
NSK (1 μ -like ring): ν_μ all ($7 \leq E_t < 30\text{GeV}$)	0.5239	0.5428	0.5428	-10.77 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	4.46	3.981	3.981	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	1.762	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.2111	0.2028	0.2028	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2539	0.2478	0.2478	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.194	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC all	0.1716	0.168	0.168	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($0 \leq E_t < 0.4\text{GeV}$)	0.147	0.139	0.139	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.2075	0.1984	0.1984	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.2899	0.281	0.281	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.3624	0.3572	0.3572	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($0.7 \leq E_t < 1\text{GeV}$)	1.118	1.107	1.107	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($1 \leq E_t < 1.5\text{GeV}$)	1.492	1.51	1.51	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($1.5 \leq E_t < 2.5\text{GeV}$)	1.635	1.495	1.495	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.71	0.6208	0.6208	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($3.5 \leq E_t < 5\text{GeV}$)	0.4132	0.4731	0.4731	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($5 \leq E_t < 7\text{GeV}$)	0.1389	0.1523	0.1523	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($7 \leq E_t < 30\text{GeV}$)	0.02833	0.02887	0.02887	0 %
NSK (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01626	0 %
NSK (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.01313	0 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004335	0 %
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003048	0.003051	0.003051	0 %
NSK (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03287	0 %
NSK (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %
NSK (1 μ -like ring): ν_e all ($0 \leq E_t < 0.5\text{GeV}$)	0.004443	0.004347	0.004347	0 %
NSK (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.7\text{GeV}$)	0.007368	0.007722	0.007722	0 %
NSK (1 μ -like ring): ν_e all ($0.7 \leq E_t < 0.8\text{GeV}$)	0.003958	0.004275	0.004275	0 %
NSK (1 μ -like ring): ν_e all ($0.8 \leq E_t < 1.5\text{GeV}$)	0.02699	0.02869	0.02869	0 %
NSK (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.03865	0.03927	0.03927	0 %
NSK (1 μ -like ring): ν_e all ($2.5 \leq E_t < 4\text{GeV}$)	0.03615	0.03646	0.03646	0 %
NSK (1 μ -like ring): ν_e all ($4 \leq E_t < 30\text{GeV}$)	0.01889	0.01921	0.01921	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0007905	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.0007453	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.33e-05	7.33e-05	7.33e-05	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002189	0.000219	0.000219	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001828	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ all ($0 \leq E_t < 2.5\text{GeV}$)	0.005279	0.005397	0.005397	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ all ($2.5 \leq E_t < 30\text{GeV}$)	0.008164	0.008302	0.008302	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC all	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0 \leq E_t < 0.4\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($5 \leq E_t < 7\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($7 \leq E_t < 30\text{GeV}$)	0	0	0	0 %

Table 37: Effect of $f_{9;t,r}^{banff}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NSK (1 μ -like ring)	210.5	204.7	204.8	0.03743 %
NSK (1 μ -like ring): ν_μ CCQE	166.4	155	155	0.003211 %
NSK (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	34.96	0.04319 %
NSK (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.9507	0.04195 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	4.315	4.199	4.233	0.8297 %
NSK (1 μ -like ring): ν_μ CC all	200.6	195.1	195.2	0.02834 %
NSK (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.633	0.458 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.48	0.9469 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	3.113	0.6899 %
NSK (1 μ -like ring): ν_μ all ($0 \leq E_t < 0.4\text{GeV}$)	6.443	6.2	6.2	0 %
NSK (1 μ -like ring): ν_μ all ($0.4 \leq E_t < 0.5\text{GeV}$)	17.43	17.1	17.1	0 %
NSK (1 μ -like ring): ν_μ all ($0.5 \leq E_t < 0.6\text{GeV}$)	34.52	34.1	34.1	0 %
NSK (1 μ -like ring): ν_μ all ($0.6 \leq E_t < 0.7\text{GeV}$)	42.48	41.33	41.33	0 %
NSK (1 μ -like ring): ν_μ all ($0.7 \leq E_t < 1\text{GeV}$)	55.91	52.77	52.77	0 %
NSK (1 μ -like ring): ν_μ all ($1 \leq E_t < 1.5\text{GeV}$)	17.65	17.75	17.75	0 %
NSK (1 μ -like ring): ν_μ all ($1.5 \leq E_t < 2.5\text{GeV}$)	12.43	11.77	11.77	0 %
NSK (1 μ -like ring): ν_μ all ($2.5 \leq E_t < 3.5\text{GeV}$)	6.888	6.106	6.106	0 %
NSK (1 μ -like ring): ν_μ all ($3.5 \leq E_t < 5\text{GeV}$)	7.037	7.906	7.906	0 %
NSK (1 μ -like ring): ν_μ all ($5 \leq E_t < 7\text{GeV}$)	2.459	2.675	2.675	0 %
NSK (1 μ -like ring): ν_μ all ($7 \leq E_t < 30\text{GeV}$)	0.5239	0.5428	0.6195	14.12 %
				0.4662
				-14.12 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	4.46	3.981	3.981	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	1.762	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.2111	0.2028	0.2028	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2539	0.2478	0.2478	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.194	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0 \leq E_t < 0.4\text{GeV}$)	0.147	0.139	0.139	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.2075	0.1984	0.1984	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.2899	0.281	0.281	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.3624	0.3572	0.3572	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.7 \leq E_t < 1\text{GeV}$)	1.118	1.107	1.107	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($1 \leq E_t < 1.5\text{GeV}$)	1.492	1.51	1.51	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($1.5 \leq E_t < 2.5\text{GeV}$)	1.635	1.495	1.495	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.71	0.6208	0.6208	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($3.5 \leq E_t < 5\text{GeV}$)	0.4132	0.4731	0.4731	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($5 \leq E_t < 7\text{GeV}$)	0.1389	0.1523	0.1523	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($7 \leq E_t < 30\text{GeV}$)	0.02833	0.02887	0.02887	0 %
NSK (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01626	0 %
NSK (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.01313	0 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004335	0 %
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003048	0.003051	0.003051	0 %
NSK (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03287	0 %
NSK (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %
NSK (1 μ -like ring): ν_e all ($0 \leq E_t < 0.5\text{GeV}$)	0.004443	0.004347	0.004347	0 %
NSK (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.7\text{GeV}$)	0.007368	0.007722	0.007722	0 %
NSK (1 μ -like ring): ν_e all ($0.7 \leq E_t < 0.8\text{GeV}$)	0.003958	0.004275	0.004275	0 %
NSK (1 μ -like ring): ν_e all ($0.8 \leq E_t < 1.5\text{GeV}$)	0.02699	0.02869	0.02869	0 %
NSK (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.03865	0.03927	0.03927	0 %
NSK (1 μ -like ring): ν_e all ($2.5 \leq E_t < 4\text{GeV}$)	0.03615	0.03646	0.03646	0 %
NSK (1 μ -like ring): ν_e all ($4 \leq E_t < 30\text{GeV}$)	0.01889	0.01921	0.01921	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0007905	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.0007453	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.33e-05	7.33e-05	7.33e-05	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002189	0.000219	0.000219	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001828	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ all ($0 \leq E_t < 2.5\text{GeV}$)	0.005279	0.005397	0.005397	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ all ($2.5 \leq E_t < 30\text{GeV}$)	0.008164	0.008302	0.008302	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC all	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0 \leq E_t < 0.4\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($5 \leq E_t < 7\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($7 \leq E_t < 30\text{GeV}$)	0	0	0	0 %

Table 38: Effect of $f_{10;t,r}^{banff}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NS_K (1 μ -like ring)	210.5	204.7	204.9 0.05254 %	204.6 -0.05254 %
NS_K (1 μ -like ring): ν_μ CCQE	166.4	155	155 0 %	155 0 %
NS_K (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	34.95 0 %	34.95 0 %
NS_K (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.9503 0 %	0.9503 0 %
NS_K (1 μ -like ring): ν_μ CC other (ν_μ disp)	4.315	4.199	4.199 0 %	4.199 0 %
NS_K (1 μ -like ring): ν_μ CC all	200.6	195.1	195.1 0 %	195.1 0 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625 0 %	1.625 0 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466 0 %	1.466 0 %
NS_K (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092 0 %	3.092 0 %
NS_K (1 μ -like ring): ν_μ all ($0 \leq E_t < 0.4\text{GeV}$)	6.443	6.2	6.2 0 %	6.2 0 %
NS_K (1 μ -like ring): ν_μ all ($0.4 \leq E_t < 0.5\text{GeV}$)	17.43	17.1	17.1 0 %	17.1 0 %
NS_K (1 μ -like ring): ν_μ all ($0.5 \leq E_t < 0.6\text{GeV}$)	34.52	34.1	34.1 0 %	34.1 0 %
NS_K (1 μ -like ring): ν_μ all ($0.6 \leq E_t < 0.7\text{GeV}$)	42.48	41.33	41.33 0 %	41.33 0 %
NS_K (1 μ -like ring): ν_μ all ($0.7 \leq E_t < 1\text{GeV}$)	55.91	52.77	52.77 0 %	52.77 0 %
NS_K (1 μ -like ring): ν_μ all ($1 \leq E_t < 1.5\text{GeV}$)	17.65	17.75	17.75 0 %	17.75 0 %
NS_K (1 μ -like ring): ν_μ all ($1.5 \leq E_t < 2.5\text{GeV}$)	12.43	11.77	11.77 0 %	11.77 0 %
NS_K (1 μ -like ring): ν_μ all ($2.5 \leq E_t < 3.5\text{GeV}$)	6.888	6.106	6.106 0 %	6.106 0 %
NS_K (1 μ -like ring): ν_μ all ($3.5 \leq E_t < 5\text{GeV}$)	7.037	7.906	7.906 0 %	7.906 0 %
NS_K (1 μ -like ring): ν_μ all ($5 \leq E_t < 7\text{GeV}$)	2.459	2.675	2.675 0 %	2.675 0 %
NS_K (1 μ -like ring): ν_μ all ($7 \leq E_t < 30\text{GeV}$)	0.5239	0.5428	0.5428 0 %	0.5428 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	4.46	3.981	4.082 2.517 %	3.881 -2.517 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	1.767 0.2412 %	1.758 -0.2412 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.2111	0.2028	0.2056 1.397 %	0.2 -1.397 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2539	0.2478	0.2478 0 %	0.2478 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.302 1.732 %	6.087 -1.732 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09066 0.265 %	0.09018 -0.265 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07766 0.06249 %	0.07757 -0.06249 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.1683 0.1715 %	0.1677 -0.1715 %
NS_K (1 μ -like ring): ν_e CCQE	0.147	0.139	0.1544 11.03 %	0.1237 -11.03 %
NS_K (1 μ -like ring): ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.2075	0.1984	0.2203 11.03 %	0.1765 -11.03 %
NS_K (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.2899	0.281	0.312 11.03 %	0.25 -11.03 %
NS_K (1 μ -like ring): ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.3624	0.3572	0.3966 11.03 %	0.3178 -11.03 %
NS_K (1 μ -like ring): ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	1.118	1.107	1.107 0 %	1.107 0 %
NS_K (1 μ -like ring): ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	1.492	1.51	1.51 0 %	1.51 0 %
NS_K (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	1.635	1.495	1.495 0 %	1.495 0 %
NS_K (1 μ -like ring): ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.71	0.6208	0.6208 0 %	0.6208 0 %
NS_K (1 μ -like ring): ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	0.4132	0.4731	0.4731 0 %	0.4731 0 %
NS_K (1 μ -like ring): ν_e all ($5 \leq E_t < 7\text{GeV}$)	0.1389	0.1523	0.1523 0 %	0.1523 0 %
NS_K (1 μ -like ring): ν_e all ($7 \leq E_t < 30\text{GeV}$)	0.02833	0.02887	0.02887 0 %	0.02887 0 %
NS_K (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01626 0 %	0.01626 0 %
NS_K (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.01313 0 %	0.01313 0 %
NS_K (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004335 0 %	0.0004335 0 %
NS_K (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003048	0.003051	0.003051 0 %	0.003051 0 %
NS_K (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03287 0 %	0.03287 0 %
NS_K (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942 0 %	0.04942 0 %
NS_K (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768 0 %	0.05768 0 %
NS_K (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071 0 %	0.1071 0 %
NS_K (1 μ -like ring): ν_e all ($0 \leq E_t < 0.5\text{GeV}$)	0.004443	0.004347	0.004347 0 %	0.004347 0 %
NS_K (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.7\text{GeV}$)	0.007368	0.007722	0.007722 0 %	0.007722 0 %
NS_K (1 μ -like ring): ν_e all ($0.7 \leq E_t < 0.8\text{GeV}$)	0.003958	0.004275	0.004275 0 %	0.004275 0 %
NS_K (1 μ -like ring): ν_e all ($0.8 \leq E_t < 1.5\text{GeV}$)	0.02699	0.02869	0.02869 0 %	0.02869 0 %
NS_K (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.03865	0.03927	0.03927 0 %	0.03927 0 %
NS_K (1 μ -like ring): ν_e all ($2.5 \leq E_t < 4\text{GeV}$)	0.03615	0.03646	0.03646 0 %	0.03646 0 %
NS_K (1 μ -like ring): ν_e all ($4 \leq E_t < 30\text{GeV}$)	0.01889	0.01921	0.01921 0 %	0.01921 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0007905 0 %	0.0007905 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.0007453 0 %	0.0007453 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.33e-05	7.33e-05	7.33e-05 0 %	7.33e-05 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002189	0.000219	0.000219 0 %	0.000219 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001828 0 %	0.001828 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916 0 %	0.005916 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954 0 %	0.005954 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187 0 %	0.01187 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ all ($0 \leq E_t < 2.5\text{GeV}$)	0.005279	0.005397	0.005397 0 %	0.005397 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ all ($2.5 \leq E_t < 30\text{GeV}$)	0.008164	0.008302	0.008302 0 %	0.008302 0 %
NS_K (1 μ -like ring): oscillation ν_e CCQE	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e CC coherent	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e CC all	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0 \leq E_t < 0.4\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($5 \leq E_t < 7\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($7 \leq E_t < 30\text{GeV}$)	0	0	0 0 %	0 0 %

Table 39: Effect of $f_{11;t,r}^{banff}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NS_K (1 μ -like ring)	210.5	204.7	204.9 0.05333 %	204.6 -0.05333 %
NS_K (1 μ -like ring): ν_μ CCQE	166.4	155	155 0 %	155 0 %
NS_K (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	34.95 0 %	34.95 0 %
NS_K (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.9503 0 %	0.9503 0 %
NS_K (1 μ -like ring): ν_μ CC other (ν_μ disp)	4.315	4.199	4.199 0 %	4.199 0 %
NS_K (1 μ -like ring): ν_μ CC all	200.6	195.1	195.1 0 %	195.1 0 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625 0 %	1.625 0 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466 0 %	1.466 0 %
NS_K (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092 0 %	3.092 0 %
NS_K (1 μ -like ring): ν_μ all ($0 \leq E_t < 0.4\text{GeV}$)	6.443	6.2	6.2 0 %	6.2 0 %
NS_K (1 μ -like ring): ν_μ all ($0.4 \leq E_t < 0.5\text{GeV}$)	17.43	17.1	17.1 0 %	17.1 0 %
NS_K (1 μ -like ring): ν_μ all ($0.5 \leq E_t < 0.6\text{GeV}$)	34.52	34.1	34.1 0 %	34.1 0 %
NS_K (1 μ -like ring): ν_μ all ($0.6 \leq E_t < 0.7\text{GeV}$)	42.48	41.33	41.33 0 %	41.33 0 %
NS_K (1 μ -like ring): ν_μ all ($0.7 \leq E_t < 1\text{GeV}$)	55.91	52.77	52.77 0 %	52.77 0 %
NS_K (1 μ -like ring): ν_μ all ($1 \leq E_t < 1.5\text{GeV}$)	17.65	17.75	17.75 0 %	17.75 0 %
NS_K (1 μ -like ring): ν_μ all ($1.5 \leq E_t < 2.5\text{GeV}$)	12.43	11.77	11.77 0 %	11.77 0 %
NS_K (1 μ -like ring): ν_μ all ($2.5 \leq E_t < 3.5\text{GeV}$)	6.888	6.106	6.106 0 %	6.106 0 %
NS_K (1 μ -like ring): ν_μ all ($3.5 \leq E_t < 5\text{GeV}$)	7.037	7.906	7.906 0 %	7.906 0 %
NS_K (1 μ -like ring): ν_μ all ($5 \leq E_t < 7\text{GeV}$)	2.459	2.675	2.675 0 %	2.675 0 %
NS_K (1 μ -like ring): ν_μ all ($7 \leq E_t < 30\text{GeV}$)	0.5239	0.5428	0.5428 0 %	0.5428 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	4.46	3.981	4.067 2.154 %	3.896 -2.154 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	1.781 1.047 %	1.744 -1.047 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.2111	0.2028	0.2067 1.947 %	0.1988 -1.947 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2539	0.2478	0.2479 0.05166 %	0.2477 -0.05166 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.303 1.748 %	6.086 -1.748 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09112 0.7694 %	0.08973 -0.7694 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07781 0.2482 %	0.07742 -0.2482 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.1689 0.5287 %	0.1671 -0.5287 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0 \leq E_t < 0.4\text{GeV}$)	0.147	0.139	0.139 0 %	0.139 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.2075	0.1984	0.1984 0 %	0.1984 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.2899	0.281	0.281 0 %	0.281 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.3624	0.3572	0.3572 0 %	0.3572 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.7 \leq E_t < 1\text{GeV}$)	1.118	1.107	1.216 9.867 %	0.9974 -9.867 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($1 \leq E_t < 1.5\text{GeV}$)	1.492	1.51	1.51 0 %	1.51 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($1.5 \leq E_t < 2.5\text{GeV}$)	1.635	1.495	1.495 0 %	1.495 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.71	0.6208	0.6208 0 %	0.6208 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($3.5 \leq E_t < 5\text{GeV}$)	0.4132	0.4731	0.4731 0 %	0.4731 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($5 \leq E_t < 7\text{GeV}$)	0.1389	0.1523	0.1523 0 %	0.1523 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($7 \leq E_t < 30\text{GeV}$)	0.02833	0.02887	0.02887 0 %	0.02887 0 %
NS_K (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01626 0 %	0.01626 0 %
NS_K (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.01313 0 %	0.01313 0 %
NS_K (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004335 0 %	0.0004335 0 %
NS_K (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003048	0.003051	0.003051 0 %	0.003051 0 %
NS_K (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03287 0 %	0.03287 0 %
NS_K (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942 0 %	0.04942 0 %
NS_K (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768 0 %	0.05768 0 %
NS_K (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071 0 %	0.1071 0 %
NS_K (1 μ -like ring): ν_e all ($0 \leq E_t < 0.5\text{GeV}$)	0.004443	0.004347	0.004347 0 %	0.004347 0 %
NS_K (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.7\text{GeV}$)	0.007368	0.007722	0.007722 0 %	0.007722 0 %
NS_K (1 μ -like ring): ν_e all ($0.7 \leq E_t < 0.8\text{GeV}$)	0.003958	0.004275	0.004275 0 %	0.004275 0 %
NS_K (1 μ -like ring): ν_e all ($0.8 \leq E_t < 1.5\text{GeV}$)	0.02699	0.02869	0.02869 0 %	0.02869 0 %
NS_K (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.03865	0.03927	0.03927 0 %	0.03927 0 %
NS_K (1 μ -like ring): ν_e all ($2.5 \leq E_t < 4\text{GeV}$)	0.03615	0.03646	0.03646 0 %	0.03646 0 %
NS_K (1 μ -like ring): ν_e all ($4 \leq E_t < 30\text{GeV}$)	0.01889	0.01921	0.01921 0 %	0.01921 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0007905 0 %	0.0007905 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.0007453 0 %	0.0007453 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.33e-05	7.33e-05	7.33e-05 0 %	7.33e-05 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002189	0.000219	0.000219 0 %	0.000219 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001828 0 %	0.001828 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916 0 %	0.005916 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954 0 %	0.005954 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187 0 %	0.01187 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ all ($0 \leq E_t < 2.5\text{GeV}$)	0.005279	0.005397	0.005397 0 %	0.005397 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ all ($2.5 \leq E_t < 30\text{GeV}$)	0.008164	0.008302	0.008302 0 %	0.008302 0 %
NS_K (1 μ -like ring): oscillation ν_e CCQE	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e CC coherent	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e CC all	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0 \leq E_t < 0.4\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($5 \leq E_t < 7\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($7 \leq E_t < 30\text{GeV}$)	0	0	0 0 %	0 0 %

Table 40: Effect of $f_{12;t,r}^{banff}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NS_K (1 μ -like ring)	210.5	204.7	204.9 0.07621 %	204.6 -0.07621 %
NS_K (1 μ -like ring): ν_μ CCQE	166.4	155	155 0 %	155 0 %
NS_K (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	34.95 0 %	34.95 0 %
NS_K (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.9503 0 %	0.9503 0 %
NS_K (1 μ -like ring): ν_μ CC other (ν_μ disp)	4.315	4.199	4.199 0 %	4.199 0 %
NS_K (1 μ -like ring): ν_μ CC all	200.6	195.1	195.1 0 %	195.1 0 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625 0 %	1.625 0 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466 0 %	1.466 0 %
NS_K (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092 0 %	3.092 0 %
NS_K (1 μ -like ring): ν_μ all ($0 \leq E_t < 0.4\text{GeV}$)	6.443	6.2	6.2 0 %	6.2 0 %
NS_K (1 μ -like ring): ν_μ all ($0.4 \leq E_t < 0.5\text{GeV}$)	17.43	17.1	17.1 0 %	17.1 0 %
NS_K (1 μ -like ring): ν_μ all ($0.5 \leq E_t < 0.6\text{GeV}$)	34.52	34.1	34.1 0 %	34.1 0 %
NS_K (1 μ -like ring): ν_μ all ($0.6 \leq E_t < 0.7\text{GeV}$)	42.48	41.33	41.33 0 %	41.33 0 %
NS_K (1 μ -like ring): ν_μ all ($0.7 \leq E_t < 1\text{GeV}$)	55.91	52.77	52.77 0 %	52.77 0 %
NS_K (1 μ -like ring): ν_μ all ($1 \leq E_t < 1.5\text{GeV}$)	17.65	17.75	17.75 0 %	17.75 0 %
NS_K (1 μ -like ring): ν_μ all ($1.5 \leq E_t < 2.5\text{GeV}$)	12.43	11.77	11.77 0 %	11.77 0 %
NS_K (1 μ -like ring): ν_μ all ($2.5 \leq E_t < 3.5\text{GeV}$)	6.888	6.106	6.106 0 %	6.106 0 %
NS_K (1 μ -like ring): ν_μ all ($3.5 \leq E_t < 5\text{GeV}$)	7.037	7.906	7.906 0 %	7.906 0 %
NS_K (1 μ -like ring): ν_μ all ($5 \leq E_t < 7\text{GeV}$)	2.459	2.675	2.675 0 %	2.675 0 %
NS_K (1 μ -like ring): ν_μ all ($7 \leq E_t < 30\text{GeV}$)	0.5239	0.5428	0.5428 0 %	0.5428 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	4.46	3.981	4.086 2.628 %	3.877 -2.628 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	1.804 2.377 %	1.721 -2.377 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.2111	0.2028	0.2083 2.736 %	0.1973 -2.736 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2539	0.2478	0.2492 0.5542 %	0.2464 -0.5542 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.348 2.477 %	6.041 -2.477 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09208 1.833 %	0.08876 -1.833 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07855 1.211 %	0.07667 -1.211 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.1706 1.546 %	0.1654 -1.546 %
NS_K (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01626 0 %	0.01626 0 %
NS_K (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.01313 0 %	0.01313 0 %
NS_K (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004335 0 %	0.0004335 0 %
NS_K (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003048	0.003051	0.003051 0 %	0.003051 0 %
NS_K (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03287 0 %	0.03287 0 %
NS_K (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942 0 %	0.04942 0 %
NS_K (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768 0 %	0.05768 0 %
NS_K (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071 0 %	0.1071 0 %
NS_K (1 μ -like ring): ν_e all ($0 \leq E_t < 0.5\text{GeV}$)	0.004443	0.004347	0.004347 0 %	0.004347 0 %
NS_K (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.7\text{GeV}$)	0.007368	0.007722	0.007722 0 %	0.007722 0 %
NS_K (1 μ -like ring): ν_e all ($0.7 \leq E_t < 0.8\text{GeV}$)	0.003958	0.004275	0.004275 0 %	0.004275 0 %
NS_K (1 μ -like ring): ν_e all ($0.8 \leq E_t < 1.5\text{GeV}$)	0.02699	0.02869	0.02869 0 %	0.02869 0 %
NS_K (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.03865	0.03927	0.03927 0 %	0.03927 0 %
NS_K (1 μ -like ring): ν_e all ($2.5 \leq E_t < 4\text{GeV}$)	0.03615	0.03646	0.03646 0 %	0.03646 0 %
NS_K (1 μ -like ring): ν_e all ($4 \leq E_t < 30\text{GeV}$)	0.01889	0.01921	0.01921 0 %	0.01921 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0007905 0 %	0.0007905 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.0007453 0 %	0.0007453 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.33e-05	7.33e-05	7.33e-05 0 %	7.33e-05 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002189	0.000219	0.000219 0 %	0.000219 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001828 0 %	0.001828 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916 0 %	0.005916 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954 0 %	0.005954 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187 0 %	0.01187 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ all ($0 \leq E_t < 2.5\text{GeV}$)	0.005279	0.005397	0.005397 0 %	0.005397 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ all ($2.5 \leq E_t < 30\text{GeV}$)	0.008164	0.008302	0.008302 0 %	0.008302 0 %
NS_K (1 μ -like ring): oscillation ν_e CCQE	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e CC coherent	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e CC all	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0 \leq E_t < 0.4\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($5 \leq E_t < 7\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($7 \leq E_t < 30\text{GeV}$)	0	0	0 0 %	0 0 %

Table 41: Effect of $f_{13;t,r}^{banff}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NS_K (1 μ -like ring)	210.5	204.7	204.9 0.08094 %	204.6 -0.08094 %
NS_K (1 μ -like ring): ν_μ CCQE	166.4	155	155 0 %	155 0 %
NS_K (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	34.95 0 %	34.95 0 %
NS_K (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.9503 0 %	0.9503 0 %
NS_K (1 μ -like ring): ν_μ CC other (ν_μ disp)	4.315	4.199	4.199 0 %	4.199 0 %
NS_K (1 μ -like ring): ν_μ CC all	200.6	195.1	195.1 0 %	195.1 0 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625 0 %	1.625 0 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466 0 %	1.466 0 %
NS_K (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092 0 %	3.092 0 %
NS_K (1 μ -like ring): ν_μ all ($0 \leq E_t < 0.4\text{GeV}$)	6.443	6.2	6.2 0 %	6.2 0 %
NS_K (1 μ -like ring): ν_μ all ($0.4 \leq E_t < 0.5\text{GeV}$)	17.43	17.1	17.1 0 %	17.1 0 %
NS_K (1 μ -like ring): ν_μ all ($0.5 \leq E_t < 0.6\text{GeV}$)	34.52	34.1	34.1 0 %	34.1 0 %
NS_K (1 μ -like ring): ν_μ all ($0.6 \leq E_t < 0.7\text{GeV}$)	42.48	41.33	41.33 0 %	41.33 0 %
NS_K (1 μ -like ring): ν_μ all ($0.7 \leq E_t < 1\text{GeV}$)	55.91	52.77	52.77 0 %	52.77 0 %
NS_K (1 μ -like ring): ν_μ all ($1 \leq E_t < 1.5\text{GeV}$)	17.65	17.75	17.75 0 %	17.75 0 %
NS_K (1 μ -like ring): ν_μ all ($1.5 \leq E_t < 2.5\text{GeV}$)	12.43	11.77	11.77 0 %	11.77 0 %
NS_K (1 μ -like ring): ν_μ all ($2.5 \leq E_t < 3.5\text{GeV}$)	6.888	6.106	6.106 0 %	6.106 0 %
NS_K (1 μ -like ring): ν_μ all ($3.5 \leq E_t < 5\text{GeV}$)	7.037	7.906	7.906 0 %	7.906 0 %
NS_K (1 μ -like ring): ν_μ all ($5 \leq E_t < 7\text{GeV}$)	2.459	2.675	2.675 0 %	2.675 0 %
NS_K (1 μ -like ring): ν_μ all ($7 \leq E_t < 30\text{GeV}$)	0.5239	0.5428	0.5428 0 %	0.5428 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	4.46	3.981	4.058 1.914 %	3.905 -1.914 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	1.834 4.085 %	1.69 -4.085 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.2111	0.2028	0.2084 2.775 %	0.1972 -2.775 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2539	0.2478	0.2543 2.63 %	0.2413 -2.63 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.355 2.588 %	6.034 -2.588 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09337 3.26 %	0.08747 -3.26 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.08005 3.141 %	0.07518 -3.141 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.1734 3.205 %	0.1627 -3.205 %
NS_K (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01626 0 %	0.01626 0 %
NS_K (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.01313 0 %	0.01313 0 %
NS_K (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004335 0 %	0.0004335 0 %
NS_K (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003048	0.003051	0.003051 0 %	0.003051 0 %
NS_K (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03287 0 %	0.03287 0 %
NS_K (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942 0 %	0.04942 0 %
NS_K (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768 0 %	0.05768 0 %
NS_K (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071 0 %	0.1071 0 %
NS_K (1 μ -like ring): ν_e all ($0 \leq E_t < 0.5\text{GeV}$)	0.004443	0.004347	0.004347 0 %	0.004347 0 %
NS_K (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.7\text{GeV}$)	0.007368	0.007722	0.007722 0 %	0.007722 0 %
NS_K (1 μ -like ring): ν_e all ($0.7 \leq E_t < 0.8\text{GeV}$)	0.003958	0.004275	0.004275 0 %	0.004275 0 %
NS_K (1 μ -like ring): ν_e all ($0.8 \leq E_t < 1.5\text{GeV}$)	0.02699	0.02869	0.02869 0 %	0.02869 0 %
NS_K (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.03865	0.03927	0.03927 0 %	0.03927 0 %
NS_K (1 μ -like ring): ν_e all ($2.5 \leq E_t < 4\text{GeV}$)	0.03615	0.03646	0.03646 0 %	0.03646 0 %
NS_K (1 μ -like ring): ν_e all ($4 \leq E_t < 30\text{GeV}$)	0.01889	0.01921	0.01921 0 %	0.01921 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0007905 0 %	0.0007905 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.0007453 0 %	0.0007453 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.33e-05	7.33e-05	7.33e-05 0 %	7.33e-05 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002189	0.000219	0.000219 0 %	0.000219 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001828 0 %	0.001828 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916 0 %	0.005916 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954 0 %	0.005954 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187 0 %	0.01187 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ all ($0 \leq E_t < 2.5\text{GeV}$)	0.005279	0.005397	0.005397 0 %	0.005397 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ all ($2.5 \leq E_t < 30\text{GeV}$)	0.008164	0.008302	0.008302 0 %	0.008302 0 %
NS_K (1 μ -like ring): oscillation ν_e CCQE	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e CC coherent	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e CC all	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0 \leq E_t < 0.4\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($5 \leq E_t < 7\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($7 \leq E_t < 30\text{GeV}$)	0	0	0 0 %	0 0 %

Table 42: Effect of $f_{14;t,r}^{banff}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NS_K (1 μ -like ring)	210.5	204.7	204.9 0.06796 %	204.6 -0.06796 %
NS_K (1 μ -like ring): ν_μ CCQE	166.4	155	155 0 %	155 0 %
NS_K (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	34.95 0 %	34.95 0 %
NS_K (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.9503 0 %	0.9503 0 %
NS_K (1 μ -like ring): ν_μ CC other (ν_μ disp)	4.315	4.199	4.199 0 %	4.199 0 %
NS_K (1 μ -like ring): ν_μ CC all	200.6	195.1	195.1 0 %	195.1 0 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625 0 %	1.625 0 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466 0 %	1.466 0 %
NS_K (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092 0 %	3.092 0 %
NS_K (1 μ -like ring): ν_μ all ($0 \leq E_t < 0.4\text{GeV}$)	6.443	6.2	6.2 0 %	6.2 0 %
NS_K (1 μ -like ring): ν_μ all ($0.4 \leq E_t < 0.5\text{GeV}$)	17.43	17.1	17.1 0 %	17.1 0 %
NS_K (1 μ -like ring): ν_μ all ($0.5 \leq E_t < 0.6\text{GeV}$)	34.52	34.1	34.1 0 %	34.1 0 %
NS_K (1 μ -like ring): ν_μ all ($0.6 \leq E_t < 0.7\text{GeV}$)	42.48	41.33	41.33 0 %	41.33 0 %
NS_K (1 μ -like ring): ν_μ all ($0.7 \leq E_t < 1\text{GeV}$)	55.91	52.77	52.77 0 %	52.77 0 %
NS_K (1 μ -like ring): ν_μ all ($1 \leq E_t < 1.5\text{GeV}$)	17.65	17.75	17.75 0 %	17.75 0 %
NS_K (1 μ -like ring): ν_μ all ($1.5 \leq E_t < 2.5\text{GeV}$)	12.43	11.77	11.77 0 %	11.77 0 %
NS_K (1 μ -like ring): ν_μ all ($2.5 \leq E_t < 3.5\text{GeV}$)	6.888	6.106	6.106 0 %	6.106 0 %
NS_K (1 μ -like ring): ν_μ all ($3.5 \leq E_t < 5\text{GeV}$)	7.037	7.906	7.906 0 %	7.906 0 %
NS_K (1 μ -like ring): ν_μ all ($5 \leq E_t < 7\text{GeV}$)	2.459	2.675	2.675 0 %	2.675 0 %
NS_K (1 μ -like ring): ν_μ all ($7 \leq E_t < 30\text{GeV}$)	0.5239	0.5428	0.5428 0 %	0.5428 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	4.46	3.981	4.036 1.38 %	3.927 -1.38 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	1.815 2.984 %	1.71 -2.984 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.2111	0.2028	0.2064 1.755 %	0.1992 -1.755 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2539	0.2478	0.2668 7.68 %	0.2288 -7.68 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.325 2.101 %	6.064 -2.101 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09463 4.654 %	0.08621 -4.654 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.08243 6.204 %	0.0728 -6.204 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.1771 5.37 %	0.159 -5.37 %
NS_K (1 μ -like ring): ν_e CCQE	0.147	0.139	0.139 0 %	0.139 0 %
NS_K (1 μ -like ring): ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.2075	0.1984	0.1984 0 %	0.1984 0 %
NS_K (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.2899	0.281	0.281 0 %	0.281 0 %
NS_K (1 μ -like ring): ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.3624	0.3572	0.3572 0 %	0.3572 0 %
NS_K (1 μ -like ring): ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	1.118	1.107	1.107 0 %	1.107 0 %
NS_K (1 μ -like ring): ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	1.492	1.51	1.51 0 %	1.51 0 %
NS_K (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	1.635	1.495	1.495 0 %	1.495 0 %
NS_K (1 μ -like ring): ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.71	0.6208	0.6886 10.91 %	0.5531 -10.91 %
NS_K (1 μ -like ring): ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	0.4132	0.4731	0.5247 10.91 %	0.4215 -10.91 %
NS_K (1 μ -like ring): ν_e all ($5 \leq E_t < 7\text{GeV}$)	0.1389	0.1523	0.1689 10.91 %	0.1357 -10.91 %
NS_K (1 μ -like ring): ν_e all ($7 \leq E_t < 30\text{GeV}$)	0.02833	0.02887	0.03202 10.91 %	0.02572 -10.91 %
NS_K (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01626 0 %	0.01626 0 %
NS_K (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.01313 0 %	0.01313 0 %
NS_K (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004335 0 %	0.0004335 0 %
NS_K (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003048	0.003051	0.003051 0 %	0.003051 0 %
NS_K (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03287 0 %	0.03287 0 %
NS_K (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942 0 %	0.04942 0 %
NS_K (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768 0 %	0.05768 0 %
NS_K (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071 0 %	0.1071 0 %
NS_K (1 μ -like ring): ν_e all ($0 \leq E_t < 0.5\text{GeV}$)	0.004443	0.004347	0.004347 0 %	0.004347 0 %
NS_K (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.7\text{GeV}$)	0.007368	0.007722	0.007722 0 %	0.007722 0 %
NS_K (1 μ -like ring): ν_e all ($0.7 \leq E_t < 0.8\text{GeV}$)	0.003958	0.004275	0.004275 0 %	0.004275 0 %
NS_K (1 μ -like ring): ν_e all ($0.8 \leq E_t < 1.5\text{GeV}$)	0.02699	0.02869	0.02869 0 %	0.02869 0 %
NS_K (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.03865	0.03927	0.03927 0 %	0.03927 0 %
NS_K (1 μ -like ring): ν_e all ($2.5 \leq E_t < 4\text{GeV}$)	0.03615	0.03646	0.03646 0 %	0.03646 0 %
NS_K (1 μ -like ring): ν_e all ($4 \leq E_t < 30\text{GeV}$)	0.01889	0.01921	0.01921 0 %	0.01921 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0007905 0 %	0.0007905 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.0007453 0 %	0.0007453 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.33e-05	7.33e-05	7.33e-05 0 %	7.33e-05 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002189	0.000219	0.000219 0 %	0.000219 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001828 0 %	0.001828 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916 0 %	0.005916 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954 0 %	0.005954 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187 0 %	0.01187 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ all ($0 \leq E_t < 2.5\text{GeV}$)	0.005279	0.005397	0.005397 0 %	0.005397 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ all ($2.5 \leq E_t < 30\text{GeV}$)	0.008164	0.008302	0.008302 0 %	0.008302 0 %
NS_K (1 μ -like ring): oscillation ν_e CCQE	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e CC coherent	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e CC all	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0 \leq E_t < 0.4\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($5 \leq E_t < 7\text{GeV}$)	0	0	0 0 %	0 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($7 \leq E_t < 30\text{GeV}$)	0	0	0 0 %	0 0 %

Table 43: Effect of $f_{15;t,r}^{banff}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ	
NSK (1 μ -like ring)	210.5	204.7	220.2	7.536 %	186.4 -8.968 %
NSK (1 μ -like ring): ν_μ CCQE	166.4	155	170	9.648 %	137.1 -11.56 %
NSK (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	34.95	0 %	34.95 0 %
NSK (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.9503	0 %	0.9503 0 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	4.315	4.199	4.199	0 %	4.199 0 %
NSK (1 μ -like ring): ν_μ CC all	200.6	195.1	210.1	7.666 %	177.2 -9.186 %
NSK (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625	0 %	1.625 0 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466	0 %	1.466 0 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092	0 %	3.092 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	4.46	3.981	4.449	11.75 %	3.546 -10.93 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	1.762	0 %	1.762 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.2111	0.2028	0.2028	0 %	0.2028 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2539	0.2478	0.2478	0 %	0.2478 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.662	7.554 %	5.759 -7.024 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %	0.09042 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %	0.07761 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %	0.168 0 %
NSK (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.0181	11.31 %	0.01416 -12.91 %
NSK (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.01313	0 %	0.01313 0 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004335	0 %	0.0004335 0 %
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003048	0.003051	0.003051	0 %	0.003051 0 %
NSK (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03471	5.596 %	0.03077 -6.386 %
NSK (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %	0.04942 0 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %	0.05768 0 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %	0.1071 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0008931	12.99 %	0.0006939 -12.21 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.0007453	0 %	0.0007453 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.333e-05	7.333e-05	7.333e-05	0 %	7.333e-05 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002189	0.000219	0.000219	0 %	0.000219 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001931	5.616 %	0.001732 -5.281 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %	0.005916 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %	0.005954 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %	0.01187 0 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0	0	0	0 %	0 0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0	0 %	0 0 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0	0	0	0 %	0 0 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0	0 %	0 0 %
NSK (1 μ -like ring): oscillation ν_e CC all	0	0	0	0 %	0 0 %

Table 44: Effect of $f_{16;t,r}^{banff}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NSK (1 μ -like ring)	210.5	204.7	208.5	1.839 %
NSK (1 μ -like ring): ν_μ CCQE	166.4	155	155	0 %
NSK (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	38.15	9.179 %
NSK (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.9503	0 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	4.315	4.199	4.235	0.8785 %
NSK (1 μ -like ring): ν_μ CC all	200.6	195.1	198.4	1.663 %
NSK (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.827	12.39 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.534	4.608 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	3.361	8.699 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	4.46	3.981	3.981	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	1.978	12.21 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.2111	0.2028	0.2028	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2539	0.2478	0.2508	1.204 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.413	3.523 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.1061	17.33 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.08173	5.309 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.1878	11.78 %
NSK (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01626	0 %
NSK (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.0143	8.924 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004335	0 %
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003048	0.003051	0.003074	0.7756 %
NSK (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03406	3.635 %
NSK (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.05699	15.32 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.06045	4.798 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1174	9.652 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0007905	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.0008425	13.04 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.333e-05	7.333e-05	7.333e-05	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002189	0.000219	0.0002201	0.4931 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001926	5.376 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.007048	19.13 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.006334	6.376 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01338	12.73 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC all	0	0	0	0 %

Table 45: Effect of $f_{17;t,r}^{banff}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1 σ		BANFF tuned -1 σ	
NSK (1 μ -like ring)	210.5	204.7	218.1	6.514 %	191.4	-6.514 %
NSK (1 μ -like ring): ν_μ CCQE ($E_t < 1.5$ GeV)	154.8	145.2	158.3	9.012 %	132.1	-9.012 %
NSK (1 μ -like ring): ν_μ CCQE ($1.5 \leq E_t < 3.5$ GeV)	9.007	6.329	6.329	0 %	6.329	0 %
NSK (1 μ -like ring): ν_μ CCQE ($E_t \geq 3.5$ GeV)	2.498	3.518	3.518	0 %	3.518	0 %
NSK (1 μ -like ring): ν_μ CCQE	166.4	155	168.1	8.439 %	142	-8.439 %
NSK (1 μ -like ring): ν_μ CC 1 π ($E_t < 2.5$ GeV)	21.94	27.92	27.92	0 %	27.92	0 %
NSK (1 μ -like ring): ν_μ CC 1 π ($E_t \geq 2.5$ GeV)	6.942	7.03	7.03	0 %	7.03	0 %
NSK (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	34.95	0 %	34.95	0 %
NSK (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.9503	0 %	0.9503	0 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	4.315	4.199	4.199	0 %	4.199	0 %
NSK (1 μ -like ring): ν_μ CC all	200.6	195.1	208.2	6.705 %	182.1	-6.705 %
NSK (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625	0 %	1.625	0 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466	0 %	1.466	0 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092	0 %	3.092	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($E_t < 1.5$ GeV)	2.959	2.791	3.042	9.012 %	2.539	-9.012 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($1.5 \leq E_t < 3.5$ GeV)	1.317	0.9346	0.9346	0 %	0.9346	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($E_t \geq 3.5$ GeV)	0.184	0.2562	0.2562	0 %	0.2562	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	4.46	3.981	4.233	6.316 %	3.73	-6.316 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π ($E_t < 2.5$ GeV)	0.9707	1.28	1.28	0 %	1.28	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π ($E_t \geq 2.5$ GeV)	0.4747	0.482	0.482	0 %	0.482	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	1.762	0 %	1.762	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.2111	0.2028	0.2028	0 %	0.2028	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2539	0.2478	0.2478	0 %	0.2478	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.446	4.06 %	5.943	-4.06 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %	0.09042	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %	0.07761	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %	0.168	0 %
NSK (1 μ -like ring): ν_e CCQE ($E_t < 1.5$ GeV)	0.01415	0.01394	0.0152	9.012 %	0.01269	-9.012 %
NSK (1 μ -like ring): ν_e CCQE ($1.5 \leq E_t < 3.5$ GeV)	0.002513	0.001883	0.001883	0 %	0.001883	0 %
NSK (1 μ -like ring): ν_e CCQE ($E_t \geq 3.5$ GeV)	0.0003079	0.0004323	0.0004323	0 %	0.0004323	0 %
NSK (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01752	7.728 %	0.015	-7.728 %
NSK (1 μ -like ring): ν_e CC 1 π ($E_t < 2.5$ GeV)	0.008235	0.01137	0.01137	0 %	0.01137	0 %
NSK (1 μ -like ring): ν_e CC 1 π ($E_t \geq 2.5$ GeV)	0.001697	0.001754	0.001754	0 %	0.001754	0 %
NSK (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.01313	0 %	0.01313	0 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004335	0 %	0.0004335	0 %
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003048	0.003051	0.003051	0 %	0.003051	0 %
NSK (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03413	3.823 %	0.03161	-3.823 %
NSK (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %	0.04942	0 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %	0.05768	0 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %	0.1071	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE ($E_t < 1.5$ GeV)	0.0004675	0.0004589	0.0005003	9.012 %	0.0004176	-9.012 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE ($1.5 \leq E_t < 3.5$ GeV)	0.0002641	0.000197	0.000197	0 %	0.000197	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE ($E_t \geq 3.5$ GeV)	9.541e-05	0.0001345	0.0001345	0 %	0.0001345	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0008318	5.232 %	0.0007491	-5.232 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π ($E_t < 2.5$ GeV)	0.0003538	0.0004898	0.0004898	0 %	0.0004898	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π ($E_t \geq 2.5$ GeV)	0.0002475	0.0002555	0.0002555	0 %	0.0002555	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.0007453	0 %	0.0007453	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.333e-05	7.333e-05	7.333e-05	0 %	7.333e-05	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002189	0.000219	0.000219	0 %	0.000219	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001869	2.262 %	0.001787	-2.262 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %	0.005916	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %	0.005954	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %	0.01187	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE ($E_t < 1.5$ GeV)	0	0	0	0 %	0	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE ($1.5 \leq E_t < 3.5$ GeV)	0	0	0	0 %	0	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE ($E_t \geq 3.5$ GeV)	0	0	0	0 %	0	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0	0	0	0 %	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π ($E_t < 2.5$ GeV)	0	0	0	0 %	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π ($E_t \geq 2.5$ GeV)	0	0	0	0 %	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0	0 %	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0	0	0	0 %	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0	0 %	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC all	0	0	0	0 %	0	0 %

Table 46: Effect of $f_{18;t,r}^{bannf}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NSK (1 μ -like ring)	210.5	204.7	206.9	1.049 %
NSK (1 μ -like ring): ν_μ CCQE ($E_t < 1.5$ GeV)	154.8	145.2	145.2	0 %
NSK (1 μ -like ring): ν_μ CCQE ($1.5 \leq E_t < 3.5$ GeV)	9.007	6.329	8.201	29.57 %
NSK (1 μ -like ring): ν_μ CCQE ($E_t \geq 3.5$ GeV)	2.498	3.518	3.518	0 %
NSK (1 μ -like ring): ν_μ CCQE	166.4	155	156.9	1.207 %
NSK (1 μ -like ring): ν_μ CC 1 π ($E_t < 2.5$ GeV)	21.94	27.92	27.92	0 %
NSK (1 μ -like ring): ν_μ CC 1 π ($E_t \geq 2.5$ GeV)	6.942	7.03	7.03	0 %
NSK (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	34.95	0 %
NSK (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.9503	0 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	4.315	4.199	4.199	0 %
NSK (1 μ -like ring): ν_μ CC all	200.6	195.1	197	0.9591 %
NSK (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625	0 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466	0 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($E_t < 1.5$ GeV)	2.959	2.791	2.791	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($1.5 \leq E_t < 3.5$ GeV)	1.317	0.9346	1.211	29.57 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($E_t \geq 3.5$ GeV)	0.184	0.2562	0.2562	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	4.46	3.981	4.258	6.942 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π ($E_t < 2.5$ GeV)	0.9707	1.28	1.28	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π ($E_t \geq 2.5$ GeV)	0.4747	0.482	0.482	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	1.762	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.2111	0.2028	0.2028	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2539	0.2478	0.2478	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.471	4.462 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %
NSK (1 μ -like ring): ν_e CCQE ($E_t < 1.5$ GeV)	0.01415	0.01394	0.01394	0 %
NSK (1 μ -like ring): ν_e CCQE ($1.5 \leq E_t < 3.5$ GeV)	0.002513	0.001883	0.00244	29.57 %
NSK (1 μ -like ring): ν_e CCQE ($E_t \geq 3.5$ GeV)	0.0003079	0.0004323	0.0004323	0 %
NSK (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01682	3.424 %
NSK (1 μ -like ring): ν_e CC 1 π ($E_t < 2.5$ GeV)	0.008235	0.01137	0.01137	0 %
NSK (1 μ -like ring): ν_e CC 1 π ($E_t \geq 2.5$ GeV)	0.001697	0.001754	0.001754	0 %
NSK (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.01313	0 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004335	0 %
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003048	0.003051	0.003051	0 %
NSK (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03343	1.694 %
NSK (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE ($E_t < 1.5$ GeV)	0.0004675	0.0004589	0.0004589	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE ($1.5 \leq E_t < 3.5$ GeV)	0.0002641	0.000197	0.0002553	29.57 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE ($E_t \geq 3.5$ GeV)	9.541e-05	0.0001345	0.0001345	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0008487	7.37 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π ($E_t < 2.5$ GeV)	0.0003538	0.0004898	0.0004898	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π ($E_t \geq 2.5$ GeV)	0.0002475	0.0002555	0.0002555	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.0007453	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.333e-05	7.333e-05	7.333e-05	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002189	0.000219	0.000219	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001886	3.187 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE ($E_t < 1.5$ GeV)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE ($1.5 \leq E_t < 3.5$ GeV)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE ($E_t \geq 3.5$ GeV)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π ($E_t < 2.5$ GeV)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π ($E_t \geq 2.5$ GeV)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC all	0	0	0	0 %

Table 47: Effect of $f_{19;t,r}^{bannf}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1 σ		BANFF tuned -1 σ	
NSK (1 μ -like ring)	210.5	204.7	205.4	0.3079 %	204.1	-0.3079 %
NSK (1 μ -like ring): ν_μ CCQE ($E_t < 1.5$ GeV)	154.8	145.2	145.2	0 %	145.2	0 %
NSK (1 μ -like ring): ν_μ CCQE ($1.5 \leq E_t < 3.5$ GeV)	9.007	6.329	6.329	0 %	6.329	0 %
NSK (1 μ -like ring): ν_μ CCQE ($E_t \geq 3.5$ GeV)	2.498	3.518	4.105	16.7 %	2.93	-16.7 %
NSK (1 μ -like ring): ν_μ CCQE	166.4	155	155.6	0.3789 %	154.5	-0.3789 %
NSK (1 μ -like ring): ν_μ CC 1 π ($E_t < 2.5$ GeV)	21.94	27.92	27.92	0 %	27.92	0 %
NSK (1 μ -like ring): ν_μ CC 1 π ($E_t \geq 2.5$ GeV)	6.942	7.03	7.03	0 %	7.03	0 %
NSK (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	34.95	0 %	34.95	0 %
NSK (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.9503	0 %	0.9503	0 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	4.315	4.199	4.199	0 %	4.199	0 %
NSK (1 μ -like ring): ν_μ CC all	200.6	195.1	195.7	0.3011 %	194.6	-0.3011 %
NSK (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625	0 %	1.625	0 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466	0 %	1.466	0 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092	0 %	3.092	0 %
NSK (1 μ -like ring): ν_μ CCQE ($E_t < 1.5$ GeV)	2.959	2.791	2.791	0 %	2.791	0 %
NSK (1 μ -like ring): ν_μ CCQE ($1.5 \leq E_t < 3.5$ GeV)	1.317	0.9346	0.9346	0 %	0.9346	0 %
NSK (1 μ -like ring): ν_μ CCQE ($E_t \geq 3.5$ GeV)	0.184	0.2562	0.299	16.7 %	0.2134	-16.7 %
NSK (1 μ -like ring): ν_μ CCQE	4.46	3.981	4.024	1.075 %	3.939	-1.075 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π ($E_t < 2.5$ GeV)	0.9707	1.28	1.28	0 %	1.28	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π ($E_t \geq 2.5$ GeV)	0.4747	0.482	0.482	0 %	0.482	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	1.762	0 %	1.762	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.2111	0.2028	0.2028	0 %	0.2028	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2539	0.2478	0.2478	0 %	0.2478	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.237	0.6909 %	6.152	-0.6909 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %	0.09042	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %	0.07761	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %	0.168	0 %
NSK (1 μ -like ring): ν_e CCQE ($E_t < 1.5$ GeV)	0.01415	0.01394	0.01394	0 %	0.01394	0 %
NSK (1 μ -like ring): ν_e CCQE ($1.5 \leq E_t < 3.5$ GeV)	0.002513	0.001883	0.001883	0 %	0.001883	0 %
NSK (1 μ -like ring): ν_e CCQE ($E_t \geq 3.5$ GeV)	0.0003079	0.0004323	0.0005045	16.7 %	0.0003601	-16.7 %
NSK (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01633	0.4441 %	0.01619	-0.4441 %
NSK (1 μ -like ring): ν_e CC 1 π ($E_t < 2.5$ GeV)	0.008235	0.01137	0.01137	0 %	0.01137	0 %
NSK (1 μ -like ring): ν_e CC 1 π ($E_t \geq 2.5$ GeV)	0.001697	0.001754	0.001754	0 %	0.001754	0 %
NSK (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.01313	0 %	0.01313	0 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004335	0 %	0.0004335	0 %
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003048	0.003051	0.003051	0 %	0.003051	0 %
NSK (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03294	0.2197 %	0.0328	-0.2197 %
NSK (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %	0.04942	0 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %	0.05768	0 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %	0.1071	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE ($E_t < 1.5$ GeV)	0.0004675	0.0004589	0.0004589	0 %	0.0004589	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE ($1.5 \leq E_t < 3.5$ GeV)	0.0002641	0.000197	0.000197	0 %	0.000197	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE ($E_t \geq 3.5$ GeV)	9.541e-05	0.0001345	0.0001569	16.7 %	0.000112	-16.7 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0008129	2.842 %	0.000768	-2.842 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π ($E_t < 2.5$ GeV)	0.0003538	0.0004898	0.0004898	0 %	0.0004898	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π ($E_t \geq 2.5$ GeV)	0.0002475	0.0002555	0.0002555	0 %	0.0002555	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.0007453	0 %	0.0007453	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.333e-05	7.333e-05	7.333e-05	0 %	7.333e-05	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002189	0.000219	0.000219	0 %	0.000219	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001851	1.229 %	0.001806	-1.229 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %	0.005916	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %	0.005954	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %	0.01187	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE ($E_t < 1.5$ GeV)	0	0	0	0 %	0	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE ($1.5 \leq E_t < 3.5$ GeV)	0	0	0	0 %	0	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE ($E_t \geq 3.5$ GeV)	0	0	0	0 %	0	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0	0	0	0 %	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π ($E_t < 2.5$ GeV)	0	0	0	0 %	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π ($E_t \geq 2.5$ GeV)	0	0	0	0 %	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0	0 %	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0	0	0	0 %	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0	0 %	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC all	0	0	0	0 %	0	0 %

Table 48: Effect of $f_{20;t,r}^{bannf}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1 σ		BANFF tuned -1 σ	
NS_K (1 μ -like ring)	210.5	204.7	209.1	2.125 %	200.4	-2.125 %
NS_K (1 μ -like ring): ν_μ CCQE ($E_t < 1.5$ GeV)	154.8	145.2	145.2	0 %	145.2	0 %
NS_K (1 μ -like ring): ν_μ CCQE ($1.5 \leq E_t < 3.5$ GeV)	9.007	6.329	6.329	0 %	6.329	0 %
NS_K (1 μ -like ring): ν_μ CCQE ($E_t \geq 3.5$ GeV)	2.498	3.518	3.518	0 %	3.518	0 %
NS_K (1 μ -like ring): ν_μ CCQE	166.4	155	155	0 %	155	0 %
NS_K (1 μ -like ring): ν_μ CC 1 π ($E_t < 2.5$ GeV)	21.94	27.92	32.07	14.9 %	23.76	-14.9 %
NS_K (1 μ -like ring): ν_μ CC 1 π ($E_t \geq 2.5$ GeV)	6.942	7.03	7.03	0 %	7.03	0 %
NS_K (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	39.1	11.9 %	30.79	-11.9 %
NS_K (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.9503	0 %	0.9503	0 %
NS_K (1 μ -like ring): ν_μ CC other (ν_μ disp)	4.315	4.199	4.199	0 %	4.199	0 %
NS_K (1 μ -like ring): ν_μ CC all	200.6	195.1	199.3	2.131 %	191	-2.131 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625	0 %	1.625	0 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466	0 %	1.466	0 %
NS_K (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092	0 %	3.092	0 %
NS_K (1 μ -like ring): ν_μ CCQE ($E_t < 1.5$ GeV)	2.959	2.791	2.791	0 %	2.791	0 %
NS_K (1 μ -like ring): ν_μ CCQE ($1.5 \leq E_t < 3.5$ GeV)	1.317	0.9346	0.9346	0 %	0.9346	0 %
NS_K (1 μ -like ring): ν_μ CCQE ($E_t \geq 3.5$ GeV)	0.184	0.2562	0.2562	0 %	0.2562	0 %
NS_K (1 μ -like ring): ν_μ CCQE	4.46	3.981	3.981	0 %	3.981	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π ($E_t < 2.5$ GeV)	0.9707	1.28	1.471	14.9 %	1.09	-14.9 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π ($E_t \geq 2.5$ GeV)	0.4747	0.482	0.482	0 %	0.482	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	1.953	10.82 %	1.572	-10.82 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.2111	0.2028	0.2028	0 %	0.2028	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2539	0.2478	0.2478	0 %	0.2478	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.385	3.079 %	6.004	-3.079 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %	0.09042	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %	0.07761	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %	0.168	0 %
NS_K (1 μ -like ring): ν_e CCQE ($E_t < 1.5$ GeV)	0.01415	0.01394	0.01394	0 %	0.01394	0 %
NS_K (1 μ -like ring): ν_e CCQE ($1.5 \leq E_t < 3.5$ GeV)	0.002513	0.001883	0.001883	0 %	0.001883	0 %
NS_K (1 μ -like ring): ν_e CCQE ($E_t \geq 3.5$ GeV)	0.0003079	0.0004323	0.0004323	0 %	0.0004323	0 %
NS_K (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01626	0 %	0.01626	0 %
NS_K (1 μ -like ring): ν_e CC 1 π ($E_t < 2.5$ GeV)	0.008235	0.01137	0.01307	14.9 %	0.009677	-14.9 %
NS_K (1 μ -like ring): ν_e CC 1 π ($E_t \geq 2.5$ GeV)	0.001697	0.001754	0.001754	0 %	0.001754	0 %
NS_K (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.01482	12.91 %	0.01143	-12.91 %
NS_K (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004335	0 %	0.0004335	0 %
NS_K (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003048	0.003051	0.003051	0 %	0.003051	0 %
NS_K (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03456	5.154 %	0.03118	-5.154 %
NS_K (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %	0.04942	0 %
NS_K (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %	0.05768	0 %
NS_K (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %	0.1071	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CCQE ($E_t < 1.5$ GeV)	0.0004675	0.0004589	0.0004589	0 %	0.0004589	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CCQE ($1.5 \leq E_t < 3.5$ GeV)	0.0002641	0.000197	0.000197	0 %	0.000197	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CCQE ($E_t \geq 3.5$ GeV)	9.541e-05	0.0001345	0.0001345	0 %	0.0001345	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0007905	0 %	0.0007905	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC 1 π ($E_t < 2.5$ GeV)	0.0003538	0.0004898	0.0005628	14.9 %	0.0004168	-14.9 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC 1 π ($E_t \geq 2.5$ GeV)	0.0002475	0.0002555	0.0002555	0 %	0.0002555	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.0008183	9.79 %	0.0006723	-9.79 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.333e-05	7.333e-05	7.333e-05	0 %	7.333e-05	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002189	0.000219	0.000219	0 %	0.000219	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001901	3.992 %	0.001755	-3.992 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %	0.005916	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %	0.005954	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %	0.01187	0 %
NS_K (1 μ -like ring): oscillation ν_e CCQE ($E_t < 1.5$ GeV)	0	0	0	0 %	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CCQE ($1.5 \leq E_t < 3.5$ GeV)	0	0	0	0 %	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CCQE ($E_t \geq 3.5$ GeV)	0	0	0	0 %	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CCQE	0	0	0	0 %	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π ($E_t < 2.5$ GeV)	0	0	0	0 %	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π ($E_t \geq 2.5$ GeV)	0	0	0	0 %	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0	0 %	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC coherent	0	0	0	0 %	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0	0 %	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC all	0	0	0	0 %	0	0 %

Table 49: Effect of $f_{21;t,r}^{bannf}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NSK (1 μ -like ring)	210.5	204.7	206.8	1.018 %
NSK (1 μ -like ring): ν_μ CCQE ($E_t < 1.5$ GeV)	154.8	145.2	145.2	0 %
NSK (1 μ -like ring): ν_μ CCQE ($1.5 \leq E_t < 3.5$ GeV)	9.007	6.329	6.329	0 %
NSK (1 μ -like ring): ν_μ CCQE ($E_t \geq 3.5$ GeV)	2.498	3.518	3.518	0 %
NSK (1 μ -like ring): ν_μ CCQE	166.4	155	155	0 %
NSK (1 μ -like ring): ν_μ CC 1 π ($E_t < 2.5$ GeV)	21.94	27.92	27.92	0 %
NSK (1 μ -like ring): ν_μ CC 1 π ($E_t \geq 2.5$ GeV)	6.942	7.03	8.98	27.74 %
NSK (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	36.9	5.58 %
NSK (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.9503	0 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	4.315	4.199	4.199	0 %
NSK (1 μ -like ring): ν_μ CC all	200.6	195.1	197.1	0.9993 %
NSK (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625	0 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466	0 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($E_t < 1.5$ GeV)	2.959	2.791	2.791	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($1.5 \leq E_t < 3.5$ GeV)	1.317	0.9346	0.9346	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($E_t \geq 3.5$ GeV)	0.184	0.2562	0.2562	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	4.46	3.981	3.981	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π ($E_t < 2.5$ GeV)	0.9707	1.28	1.28	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π ($E_t \geq 2.5$ GeV)	0.4747	0.482	0.6158	27.74 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	1.896	7.587 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.2111	0.2028	0.2028	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2539	0.2478	0.2478	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.328	2.159 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %
NSK (1 μ -like ring): ν_e CCQE ($E_t < 1.5$ GeV)	0.01415	0.01394	0.01394	0 %
NSK (1 μ -like ring): ν_e CCQE ($1.5 \leq E_t < 3.5$ GeV)	0.002513	0.001883	0.001883	0 %
NSK (1 μ -like ring): ν_e CCQE ($E_t \geq 3.5$ GeV)	0.0003079	0.0004323	0.0004323	0 %
NSK (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01626	0 %
NSK (1 μ -like ring): ν_e CC 1 π ($E_t < 2.5$ GeV)	0.008235	0.01137	0.01137	0 %
NSK (1 μ -like ring): ν_e CC 1 π ($E_t \geq 2.5$ GeV)	0.001697	0.001754	0.00224	27.74 %
NSK (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.01361	3.707 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004335	0 %
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003048	0.003051	0.003051	0 %
NSK (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03336	1.48 %
NSK (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE ($E_t < 1.5$ GeV)	0.0004675	0.0004589	0.0004589	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE ($1.5 \leq E_t < 3.5$ GeV)	0.0002641	0.000197	0.000197	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE ($E_t \geq 3.5$ GeV)	9.541e-05	0.0001345	0.0001345	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0007905	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π ($E_t < 2.5$ GeV)	0.0003538	0.0004898	0.0004898	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π ($E_t \geq 2.5$ GeV)	0.0002475	0.0002555	0.0003264	27.74 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.0008162	9.51 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.333e-05	7.333e-05	7.333e-05	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002189	0.000219	0.000219	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001899	3.877 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE ($E_t < 1.5$ GeV)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE ($1.5 \leq E_t < 3.5$ GeV)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE ($E_t \geq 3.5$ GeV)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π ($E_t < 2.5$ GeV)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π ($E_t \geq 2.5$ GeV)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC all	0	0	0	0 %

Table 50: Effect of $f_{22;t,r}^{bannf}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NSK (1 μ -like ring)	210.5	204.7	204.9 0.06749 %	204.7 -0.04195 %
NSK (1 μ -like ring): ν_μ CCQE	166.4	155	155.2 0.08902 %	155 -0.05531 %
NSK (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	34.95 0 %	34.95 0 %
NSK (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.9503 0 %	0.9503 0 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	4.315	4.199	4.199 0 %	4.199 0 %
NSK (1 μ -like ring): ν_μ CC all	200.6	195.1	195.3 0.07073 %	195.1 -0.04395 %
NSK (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625 0 %	1.625 0 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466 0 %	1.466 0 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092 0 %	3.092 0 %
NSK (1 μ -like ring): ν_μ all ($0 \leq E_t < 0.4\text{GeV}$)	6.443	6.2	5.952 -3.992 %	6.412 3.419 %
NSK (1 μ -like ring): ν_μ all ($0.4 \leq E_t < 0.5\text{GeV}$)	17.43	17.1	16.91 -1.081 %	17.21 0.6798 %
NSK (1 μ -like ring): ν_μ all ($0.5 \leq E_t < 0.6\text{GeV}$)	34.52	34.1	34.14 0.1264 %	34.02 -0.2378 %
NSK (1 μ -like ring): ν_μ all ($0.6 \leq E_t < 0.7\text{GeV}$)	42.48	41.33	41.36 0.08597 %	41.26 -0.1577 %
NSK (1 μ -like ring): ν_μ all ($0.7 \leq E_t < 1\text{GeV}$)	55.91	52.77	52.87 0.1938 %	52.75 -0.0275 %
NSK (1 μ -like ring): ν_μ all ($1 \leq E_t < 1.5\text{GeV}$)	17.65	17.75	17.9 0.8537 %	17.67 -0.4186 %
NSK (1 μ -like ring): ν_μ all ($1.5 \leq E_t < 2.5\text{GeV}$)	12.43	11.77	11.87 0.858 %	11.69 -0.6746 %
NSK (1 μ -like ring): ν_μ all ($2.5 \leq E_t < 3.5\text{GeV}$)	6.888	6.106	6.156 0.818 %	6.072 -0.5442 %
NSK (1 μ -like ring): ν_μ all ($3.5 \leq E_t < 5\text{GeV}$)	7.037	7.906	7.986 1.015 %	7.845 -0.7706 %
NSK (1 μ -like ring): ν_μ all ($5 \leq E_t < 7\text{GeV}$)	2.459	2.675	2.682 0.2585 %	2.67 -0.2 %
NSK (1 μ -like ring): ν_μ all ($7 \leq E_t < 30\text{GeV}$)	0.5239	0.5428	0.5428 0 %	0.5428 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	4.46	3.981	3.981 0 %	3.981 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	1.762 0 %	1.762 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.2111	0.2028	0.2028 0 %	0.2028 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2539	0.2478	0.2478 0 %	0.2478 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.194 0 %	6.194 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042 0 %	0.09042 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761 0 %	0.07761 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168 0 %	0.168 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0 \leq E_t < 0.4\text{GeV}$)	0.147	0.139	0.139 0 %	0.139 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.2075	0.1984	0.1984 0 %	0.1984 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.2899	0.281	0.281 0 %	0.281 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.3624	0.3572	0.3572 0 %	0.3572 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.7 \leq E_t < 1\text{GeV}$)	1.118	1.107	1.107 0 %	1.107 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($1 \leq E_t < 1.5\text{GeV}$)	1.492	1.51	1.51 0 %	1.51 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($1.5 \leq E_t < 2.5\text{GeV}$)	1.635	1.495	1.495 0 %	1.495 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.71	0.6208	0.6208 0 %	0.6208 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($3.5 \leq E_t < 5\text{GeV}$)	0.4132	0.4731	0.4731 0 %	0.4731 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($5 \leq E_t < 7\text{GeV}$)	0.1389	0.1523	0.1523 0 %	0.1523 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($7 \leq E_t < 30\text{GeV}$)	0.02833	0.02887	0.02887 0 %	0.02887 0 %
NSK (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01642 0.9615 %	0.01613 -0.7929 %
NSK (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.01313 0 %	0.01313 0 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004335 0 %	0.0004335 0 %
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003048	0.003051	0.003051 0 %	0.003051 0 %
NSK (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03303 0.4756 %	0.03274 -0.3922 %
NSK (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942 0 %	0.04942 0 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768 0 %	0.05768 0 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071 0 %	0.1071 0 %
NSK (1 μ -like ring): ν_e all ($0 \leq E_t < 0.5\text{GeV}$)	0.004443	0.004347	0.004286 -1.395 %	0.004382 0.8008 %
NSK (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.7\text{GeV}$)	0.007368	0.007722	0.007776 0.7016 %	0.00767 -0.6719 %
NSK (1 μ -like ring): ν_e all ($0.7 \leq E_t < 0.8\text{GeV}$)	0.003958	0.004275	0.004294 0.453 %	0.004263 -0.2681 %
NSK (1 μ -like ring): ν_e all ($0.8 \leq E_t < 1.5\text{GeV}$)	0.02699	0.02869	0.02877 0.302 %	0.02863 -0.2155 %
NSK (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.03865	0.03927	0.03931 0.0953 %	0.03924 -0.08852 %
NSK (1 μ -like ring): ν_e all ($2.5 \leq E_t < 4\text{GeV}$)	0.03615	0.03646	0.03648 0.0411 %	0.03645 -0.02834 %
NSK (1 μ -like ring): ν_e all ($4 \leq E_t < 30\text{GeV}$)	0.01889	0.01921	0.01921 0.02287 %	0.01922 0.03394 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0007905 0 %	0.0007905 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.0007453 0 %	0.0007453 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.33e-05	7.33e-05	7.33e-05 0 %	7.33e-05 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002189	0.000219	0.000219 0 %	0.000219 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001828 0 %	0.001828 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916 0 %	0.005916 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954 0 %	0.005954 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187 0 %	0.01187 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ all ($0 \leq E_t < 2.5\text{GeV}$)	0.005279	0.005397	0.005397 0 %	0.005397 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ all ($2.5 \leq E_t < 30\text{GeV}$)	0.008164	0.008302	0.008302 0 %	0.008302 0 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0	0	0 0 %	0 0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0 0 %	0 0 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0	0	0 0 %	0 0 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0 0 %	0 0 %
NSK (1 μ -like ring): oscillation ν_e CC all	0	0	0 0 %	0 0 %
NSK (1 μ -like ring): oscillation ν_e all ($0 \leq E_t < 0.4\text{GeV}$)	0	0	0 0 %	0 0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0	0	0 0 %	0 0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0	0	0 0 %	0 0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0	0	0 0 %	0 0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	0	0	0 0 %	0 0 %
NSK (1 μ -like ring): oscillation ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	0	0	0 0 %	0 0 %
NSK (1 μ -like ring): oscillation ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0	0	0 0 %	0 0 %
NSK (1 μ -like ring): oscillation ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0	0	0 0 %	0 0 %
NSK (1 μ -like ring): oscillation ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	0	0	0 0 %	0 0 %
NSK (1 μ -like ring): oscillation ν_e all ($5 \leq E_t < 7\text{GeV}$)	0	0	0 0 %	0 0 %
NSK (1 μ -like ring): oscillation ν_e all ($7 \leq E_t < 30\text{GeV}$)	0	0	0 0 %	0 0 %

Table 51: Effect of $f_{pF;t,r}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NSK (1 μ -like ring)	210.5	204.7	199.7	-2.466 %
NSK (1 μ -like ring): ν_μ CCQE	166.4	155	150	-3.255 %
NSK (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	34.95	0 %
NSK (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.9503	0 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	4.315	4.199	4.199	0 %
NSK (1 μ -like ring): ν_μ CC all	200.6	195.1	190.1	-2.587 %
NSK (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625	0 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466	0 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092	0 %
NSK (1 μ -like ring): ν_μ all ($0 \leq E_t < 0.4\text{GeV}$)	6.443	6.2	6.615	6.69 %
NSK (1 μ -like ring): ν_μ all ($0.4 \leq E_t < 0.5\text{GeV}$)	17.43	17.1	16.59	-2.954 %
NSK (1 μ -like ring): ν_μ all ($0.5 \leq E_t < 0.6\text{GeV}$)	34.52	34.1	33.94	-0.4548 %
NSK (1 μ -like ring): ν_μ all ($0.6 \leq E_t < 0.7\text{GeV}$)	42.48	41.33	38.88	-5.915 %
NSK (1 μ -like ring): ν_μ all ($0.7 \leq E_t < 1\text{GeV}$)	55.91	52.77	50.41	-4.468 %
NSK (1 μ -like ring): ν_μ all ($1 \leq E_t < 1.5\text{GeV}$)	17.65	17.75	17.75	0 %
NSK (1 μ -like ring): ν_μ all ($1.5 \leq E_t < 2.5\text{GeV}$)	12.43	11.77	11.77	0 %
NSK (1 μ -like ring): ν_μ all ($2.5 \leq E_t < 3.5\text{GeV}$)	6.888	6.106	6.106	0 %
NSK (1 μ -like ring): ν_μ all ($3.5 \leq E_t < 5\text{GeV}$)	7.037	7.906	7.906	0 %
NSK (1 μ -like ring): ν_μ all ($5 \leq E_t < 7\text{GeV}$)	2.459	2.675	2.675	0 %
NSK (1 μ -like ring): ν_μ all ($7 \leq E_t < 30\text{GeV}$)	0.5239	0.5428	0.5428	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	4.46	3.981	3.981	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	1.762	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.2111	0.2028	0.2028	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2539	0.2478	0.2478	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.194	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0 \leq E_t < 0.4\text{GeV}$)	0.147	0.139	0.139	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.2075	0.1984	0.1984	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.2899	0.281	0.281	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.3624	0.3572	0.3572	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.7 \leq E_t < 1\text{GeV}$)	1.118	1.107	1.107	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($1 \leq E_t < 1.5\text{GeV}$)	1.492	1.51	1.51	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($1.5 \leq E_t < 2.5\text{GeV}$)	1.635	1.495	1.495	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.71	0.6208	0.6208	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($3.5 \leq E_t < 5\text{GeV}$)	0.4132	0.4731	0.4731	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($5 \leq E_t < 7\text{GeV}$)	0.1389	0.1523	0.1523	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($7 \leq E_t < 30\text{GeV}$)	0.02833	0.02887	0.02887	0 %
NSK (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01531	-5.827 %
NSK (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.01313	0 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004335	0 %
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003048	0.003051	0.003051	0 %
NSK (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03192	-2.883 %
NSK (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %
NSK (1 μ -like ring): ν_e all ($0 \leq E_t < 0.5\text{GeV}$)	0.004443	0.004347	0.004135	-4.863 %
NSK (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.7\text{GeV}$)	0.007368	0.007722	0.007157	-7.31 %
NSK (1 μ -like ring): ν_e all ($0.7 \leq E_t < 0.8\text{GeV}$)	0.003958	0.004275	0.004164	-2.585 %
NSK (1 μ -like ring): ν_e all ($0.8 \leq E_t < 1.5\text{GeV}$)	0.02699	0.02869	0.02863	-0.2129 %
NSK (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.03865	0.03927	0.03927	0 %
NSK (1 μ -like ring): ν_e all ($2.5 \leq E_t < 4\text{GeV}$)	0.03615	0.03646	0.03646	0 %
NSK (1 μ -like ring): ν_e all ($4 \leq E_t < 30\text{GeV}$)	0.01889	0.01921	0.01921	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0007905	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.0007453	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.333e-05	7.333e-05	7.333e-05	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002189	0.000219	0.000219	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001828	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ all ($0 \leq E_t < 2.5\text{GeV}$)	0.005279	0.005397	0.005397	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ all ($2.5 \leq E_t < 30\text{GeV}$)	0.008164	0.008302	0.008302	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC all	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0 \leq E_t < 0.4\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($5 \leq E_t < 7\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($7 \leq E_t < 30\text{GeV}$)	0	0	0	0 %

Table 52: Effect of $f_{SF;t,r}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NSK (1 μ -like ring)	210.5	204.7	205	0.1026 %
NSK (1 μ -like ring): ν_μ CCQE	166.4	155	155	0 %
NSK (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	34.95	0 %
NSK (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.9503	0 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	4.315	4.199	4.199	0 %
NSK (1 μ -like ring): ν_μ CC all	200.6	195.1	195.1	0 %
NSK (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.753	7.821 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.522	3.763 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	3.274	5.896 %
NSK (1 μ -like ring): ν_μ all ($0 \leq E_t < 0.4\text{GeV}$)	6.443	6.2	6.2	0 %
NSK (1 μ -like ring): ν_μ all ($0.4 \leq E_t < 0.5\text{GeV}$)	17.43	17.1	17.09	-0.03214 %
NSK (1 μ -like ring): ν_μ all ($0.5 \leq E_t < 0.6\text{GeV}$)	34.52	34.1	34.08	-0.05275 %
NSK (1 μ -like ring): ν_μ all ($0.6 \leq E_t < 0.7\text{GeV}$)	42.48	41.33	41.3	-0.06448 %
NSK (1 μ -like ring): ν_μ all ($0.7 \leq E_t < 1\text{GeV}$)	55.91	52.77	52.76	-0.01004 %
NSK (1 μ -like ring): ν_μ all ($1 \leq E_t < 1.5\text{GeV}$)	17.65	17.75	17.78	0.1911 %
NSK (1 μ -like ring): ν_μ all ($1.5 \leq E_t < 2.5\text{GeV}$)	12.43	11.77	11.83	0.5512 %
NSK (1 μ -like ring): ν_μ all ($2.5 \leq E_t < 3.5\text{GeV}$)	6.888	6.106	6.149	0.7171 %
NSK (1 μ -like ring): ν_μ all ($3.5 \leq E_t < 5\text{GeV}$)	7.037	7.906	7.96	0.6778 %
NSK (1 μ -like ring): ν_μ all ($5 \leq E_t < 7\text{GeV}$)	2.459	2.675	2.703	1.037 %
NSK (1 μ -like ring): ν_μ all ($7 \leq E_t < 30\text{GeV}$)	0.5239	0.5428	0.5567	2.551 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	4.46	3.981	3.981	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	1.762	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.2111	0.2028	0.2028	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2539	0.2478	0.2478	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.194	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.1036	14.54 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.08124	4.668 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.1848	9.981 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0 \leq E_t < 0.4\text{GeV}$)	0.147	0.139	0.139	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.2075	0.1984	0.1983	-0.02255 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.2899	0.281	0.2808	-0.06753 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.3624	0.3572	0.3571	-0.01382 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.7 \leq E_t < 1\text{GeV}$)	1.118	1.107	1.106	-0.012 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($1 \leq E_t < 1.5\text{GeV}$)	1.492	1.51	1.513	0.1804 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($1.5 \leq E_t < 2.5\text{GeV}$)	1.635	1.495	1.501	0.3731 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.71	0.6208	0.6247	0.6242 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($3.5 \leq E_t < 5\text{GeV}$)	0.4132	0.4731	0.4763	0.673 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($5 \leq E_t < 7\text{GeV}$)	0.1389	0.1523	0.1535	0.791 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($7 \leq E_t < 30\text{GeV}$)	0.02833	0.02887	0.02949	2.151 %
NSK (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01626	0 %
NSK (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.01313	0 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004335	0 %
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003048	0.003051	0.003051	0 %
NSK (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03287	0 %
NSK (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.05687	15.07 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05983	3.724 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1167	8.961 %
NSK (1 μ -like ring): ν_e all ($0 \leq E_t < 0.5\text{GeV}$)	0.004443	0.004347	0.004323	-0.5563 %
NSK (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.7\text{GeV}$)	0.007368	0.007722	0.007502	-2.844 %
NSK (1 μ -like ring): ν_e all ($0.7 \leq E_t < 0.8\text{GeV}$)	0.003958	0.004275	0.004193	-1.915 %
NSK (1 μ -like ring): ν_e all ($0.8 \leq E_t < 1.5\text{GeV}$)	0.02699	0.02869	0.02978	3.826 %
NSK (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.03865	0.03927	0.043	9.486 %
NSK (1 μ -like ring): ν_e all ($2.5 \leq E_t < 4\text{GeV}$)	0.03615	0.03646	0.0399	9.42 %
NSK (1 μ -like ring): ν_e all ($4 \leq E_t < 30\text{GeV}$)	0.01889	0.01921	0.02087	8.669 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0007905	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.0007453	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.33e-05	7.33e-05	7.33e-05	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002189	0.000219	0.000219	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001828	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.007015	18.57 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.006256	5.079 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01327	11.81 %
NSK (1 μ -like ring): $\bar{\nu}_e$ all ($0 \leq E_t < 2.5\text{GeV}$)	0.005279	0.005397	0.00586	8.593 %
NSK (1 μ -like ring): $\bar{\nu}_e$ all ($2.5 \leq E_t < 30\text{GeV}$)	0.008164	0.008302	0.009239	11.29 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC all	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0 \leq E_t < 0.4\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($5 \leq E_t < 7\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($7 \leq E_t < 30\text{GeV}$)	0	0	0	0 %

Table 53: Effect of $f_{Wshape;t,r}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NSK (1 μ -like ring)	210.5	204.7	205.3	0.2799 %
NSK (1 μ -like ring): ν_μ CCQE	166.4	155	155	0 %
NSK (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	34.95	0 %
NSK (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.9503	0 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	4.315	4.199	4.737	12.83 %
NSK (1 μ -like ring): ν_μ CC all	200.6	195.1	195.7	0.276 %
NSK (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625	0 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466	0 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092	0 %
NSK (1 μ -like ring): ν_μ all ($0 \leq E_t < 0.4\text{GeV}$)	6.443	6.2	6.2	0 %
NSK (1 μ -like ring): ν_μ all ($0.4 \leq E_t < 0.5\text{GeV}$)	17.43	17.1	17.1	0 %
NSK (1 μ -like ring): ν_μ all ($0.5 \leq E_t < 0.6\text{GeV}$)	34.52	34.1	34.1	0 %
NSK (1 μ -like ring): ν_μ all ($0.6 \leq E_t < 0.7\text{GeV}$)	42.48	41.33	41.33	0.0009852 %
NSK (1 μ -like ring): ν_μ all ($0.7 \leq E_t < 1\text{GeV}$)	55.91	52.77	52.78	0.0228 %
NSK (1 μ -like ring): ν_μ all ($1 \leq E_t < 1.5\text{GeV}$)	17.65	17.75	17.83	0.4463 %
NSK (1 μ -like ring): ν_μ all ($1.5 \leq E_t < 2.5\text{GeV}$)	12.43	11.77	11.9	1.168 %
NSK (1 μ -like ring): ν_μ all ($2.5 \leq E_t < 3.5\text{GeV}$)	6.888	6.106	6.217	1.826 %
NSK (1 μ -like ring): ν_μ all ($3.5 \leq E_t < 5\text{GeV}$)	7.037	7.906	8.037	1.657 %
NSK (1 μ -like ring): ν_μ all ($5 \leq E_t < 7\text{GeV}$)	2.459	2.675	2.73	2.038 %
NSK (1 μ -like ring): ν_μ all ($7 \leq E_t < 30\text{GeV}$)	0.5239	0.5428	0.5553	2.291 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	4.46	3.981	3.981	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	1.762	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.2111	0.2028	0.2028	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2539	0.2478	0.2818	13.72 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.228	0.549 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0 \leq E_t < 0.4\text{GeV}$)	0.147	0.139	0.139	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.2075	0.1984	0.1984	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.2899	0.281	0.281	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.3624	0.3572	0.3572	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.7 \leq E_t < 1\text{GeV}$)	1.118	1.107	1.107	0.05007 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($1 \leq E_t < 1.5\text{GeV}$)	1.492	1.51	1.514	0.2717 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($1.5 \leq E_t < 2.5\text{GeV}$)	1.635	1.495	1.507	0.7845 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.71	0.6208	0.629	1.311 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($3.5 \leq E_t < 5\text{GeV}$)	0.4132	0.4731	0.4794	1.327 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($5 \leq E_t < 7\text{GeV}$)	0.1389	0.1523	0.1549	1.705 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($7 \leq E_t < 30\text{GeV}$)	0.02833	0.02887	0.02947	2.093 %
NSK (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01626	0 %
NSK (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.01313	0 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004335	0 %
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003048	0.003051	0.003523	15.47 %
NSK (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03334	1.436 %
NSK (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %
NSK (1 μ -like ring): ν_e all ($0 \leq E_t < 0.5\text{GeV}$)	0.004443	0.004347	0.004347	0 %
NSK (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.7\text{GeV}$)	0.007368	0.007722	0.007722	0 %
NSK (1 μ -like ring): ν_e all ($0.7 \leq E_t < 0.8\text{GeV}$)	0.003958	0.004275	0.004281	0.1605 %
NSK (1 μ -like ring): ν_e all ($0.8 \leq E_t < 1.5\text{GeV}$)	0.02699	0.02869	0.02879	0.3448 %
NSK (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.03865	0.03927	0.03943	0.4084 %
NSK (1 μ -like ring): ν_e all ($2.5 \leq E_t < 4\text{GeV}$)	0.03615	0.03646	0.03661	0.3997 %
NSK (1 μ -like ring): ν_e all ($4 \leq E_t < 30\text{GeV}$)	0.01889	0.01921	0.01927	0.3127 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0007905	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.0007453	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.33e-05	7.33e-05	7.33e-05	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002189	0.000219	0.0002482	13.31 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001857	1.595 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ all ($0 \leq E_t < 2.5\text{GeV}$)	0.005279	0.005397	0.00541	0.2464 %
NSK (1 μ -like ring): $\bar{\nu}_e$ all ($2.5 \leq E_t < 30\text{GeV}$)	0.008164	0.008302	0.008317	0.191 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC all	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0 \leq E_t < 0.4\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($5 \leq E_t < 7\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($7 \leq E_t < 30\text{GeV}$)	0	0	0	0 %

Table 54: Effect of $f_{CCothShape;t,r}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NSK (1 μ -like ring)	210.5	204.7	212	3.553 %
NSK (1 μ -like ring): ν_μ CCQE	166.4	155	155	0 %
NSK (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	42.44	21.46 %
NSK (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.9503	0 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	4.315	4.199	4.199	0 %
NSK (1 μ -like ring): ν_μ CC all	200.6	195.1	202.6	3.843 %
NSK (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.317	-18.97 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.379	-5.958 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	2.696	-12.8 %
NSK (1 μ -like ring): ν_μ all ($0 \leq E_t < 0.4\text{GeV}$)	6.443	6.2	6.2	0 %
NSK (1 μ -like ring): ν_μ all ($0.4 \leq E_t < 0.5\text{GeV}$)	17.43	17.1	17.09	-0.01126 %
NSK (1 μ -like ring): ν_μ all ($0.5 \leq E_t < 0.6\text{GeV}$)	34.52	34.1	34.19	0.2545 %
NSK (1 μ -like ring): ν_μ all ($0.6 \leq E_t < 0.7\text{GeV}$)	42.48	41.33	41.98	1.586 %
NSK (1 μ -like ring): ν_μ all ($0.7 \leq E_t < 1\text{GeV}$)	55.91	52.77	54.75	3.757 %
NSK (1 μ -like ring): ν_μ all ($1 \leq E_t < 1.5\text{GeV}$)	17.65	17.75	19.19	8.149 %
NSK (1 μ -like ring): ν_μ all ($1.5 \leq E_t < 2.5\text{GeV}$)	12.43	11.77	13.18	12.05 %
NSK (1 μ -like ring): ν_μ all ($2.5 \leq E_t < 3.5\text{GeV}$)	6.888	6.106	6.834	11.92 %
NSK (1 μ -like ring): ν_μ all ($3.5 \leq E_t < 5\text{GeV}$)	7.037	7.906	8.521	7.777 %
NSK (1 μ -like ring): ν_μ all ($5 \leq E_t < 7\text{GeV}$)	2.459	2.675	2.829	5.744 %
NSK (1 μ -like ring): ν_μ all ($7 \leq E_t < 30\text{GeV}$)	0.5239	0.5428	0.5632	3.745 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	4.46	3.981	3.981	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	1.969	11.72 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.2111	0.2028	0.2028	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2539	0.2478	0.2478	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.401	3.336 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.07284	-19.45 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07297	-5.987 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.1458	-13.23 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0 \leq E_t < 0.4\text{GeV}$)	0.147	0.139	0.139	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.2075	0.1984	0.1984	0.008401 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.2899	0.281	0.282	0.3366 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.3624	0.3572	0.3585	0.3668 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.7 \leq E_t < 1\text{GeV}$)	1.118	1.107	1.124	1.539 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($1 \leq E_t < 1.5\text{GeV}$)	1.492	1.51	1.546	2.364 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($1.5 \leq E_t < 2.5\text{GeV}$)	1.635	1.495	1.574	5.265 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.71	0.6208	0.6514	4.931 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($3.5 \leq E_t < 5\text{GeV}$)	0.4132	0.4731	0.4892	3.389 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($5 \leq E_t < 7\text{GeV}$)	0.1389	0.1523	0.1559	2.38 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($7 \leq E_t < 30\text{GeV}$)	0.02833	0.02887	0.02927	1.403 %
NSK (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01626	0 %
NSK (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.01394	6.182 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004335	0 %
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003048	0.003051	0.003051	0 %
NSK (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03368	2.468 %
NSK (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.0398	-19.46 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.0548	-4.999 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.0946	-11.67 %
NSK (1 μ -like ring): ν_e all ($0 \leq E_t < 0.5\text{GeV}$)	0.004443	0.004347	0.004321	-0.6039 %
NSK (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.7\text{GeV}$)	0.007368	0.007722	0.007632	-1.158 %
NSK (1 μ -like ring): ν_e all ($0.7 \leq E_t < 0.8\text{GeV}$)	0.003958	0.004275	0.004103	-4.003 %
NSK (1 μ -like ring): ν_e all ($0.8 \leq E_t < 1.5\text{GeV}$)	0.02699	0.02869	0.02612	-8.948 %
NSK (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.03865	0.03927	0.03543	-9.787 %
NSK (1 μ -like ring): ν_e all ($2.5 \leq E_t < 4\text{GeV}$)	0.03615	0.03646	0.03311	-9.196 %
NSK (1 μ -like ring): ν_e all ($4 \leq E_t < 30\text{GeV}$)	0.01889	0.01921	0.01757	-8.537 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0007905	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.0007734	3.767 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.33e-05	7.33e-05	7.33e-05	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002189	0.000219	0.000219	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001856	1.536 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.004761	-19.52 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005621	-5.585 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01038	-12.53 %
NSK (1 μ -like ring): $\bar{\nu}_e$ all ($0 \leq E_t < 2.5\text{GeV}$)	0.005279	0.005397	0.004841	-10.3 %
NSK (1 μ -like ring): $\bar{\nu}_e$ all ($2.5 \leq E_t < 30\text{GeV}$)	0.008164	0.008302	0.007398	-10.88 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC all	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0 \leq E_t < 0.4\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($5 \leq E_t < 7\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($7 \leq E_t < 30\text{GeV}$)	0	0	0	0 %

Table 55: Effect of $f_{\pi-less\Delta;t,r}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NSK (1 μ -like ring)	210.5	204.7	203.9	-0.418 %
NSK (1 μ -like ring): ν_μ CCQE	166.4	155	154.2	-0.5519 %
NSK (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	34.95	0 %
NSK (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.9503	0 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	4.315	4.199	4.199	0 %
NSK (1 μ -like ring): ν_μ CC all	200.6	195.1	194.3	-0.4385 %
NSK (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625	0 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466	0 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092	0 %
NSK (1 μ -like ring): ν_μ all ($0 \leq E_t < 0.4\text{GeV}$)	6.443	6.2	6.919	11.59 %
NSK (1 μ -like ring): ν_μ all ($0.4 \leq E_t < 0.5\text{GeV}$)	17.43	17.1	18.3	7.015 %
NSK (1 μ -like ring): ν_μ all ($0.5 \leq E_t < 0.6\text{GeV}$)	34.52	34.1	34.97	2.548 %
NSK (1 μ -like ring): ν_μ all ($0.6 \leq E_t < 0.7\text{GeV}$)	42.48	41.33	40.64	-1.656 %
NSK (1 μ -like ring): ν_μ all ($0.7 \leq E_t < 1\text{GeV}$)	55.91	52.77	50.37	-4.542 %
NSK (1 μ -like ring): ν_μ all ($1 \leq E_t < 1.5\text{GeV}$)	17.65	17.75	17.29	-2.59 %
NSK (1 μ -like ring): ν_μ all ($1.5 \leq E_t < 2.5\text{GeV}$)	12.43	11.77	11.69	-0.6316 %
NSK (1 μ -like ring): ν_μ all ($2.5 \leq E_t < 3.5\text{GeV}$)	6.888	6.106	6.098	-0.1303 %
NSK (1 μ -like ring): ν_μ all ($3.5 \leq E_t < 5\text{GeV}$)	7.037	7.906	7.889	-0.2169 %
NSK (1 μ -like ring): ν_μ all ($5 \leq E_t < 7\text{GeV}$)	2.459	2.675	2.672	-0.0984 %
NSK (1 μ -like ring): ν_μ all ($7 \leq E_t < 30\text{GeV}$)	0.5239	0.5428	0.5428	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	4.46	3.981	3.981	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	1.762	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.2111	0.2028	0.2028	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2539	0.2478	0.2478	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.194	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0 \leq E_t < 0.4\text{GeV}$)	0.147	0.139	0.139	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.2075	0.1984	0.1984	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.2899	0.281	0.281	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.3624	0.3572	0.3572	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.7 \leq E_t < 1\text{GeV}$)	1.118	1.107	1.107	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($1 \leq E_t < 1.5\text{GeV}$)	1.492	1.51	1.51	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($1.5 \leq E_t < 2.5\text{GeV}$)	1.635	1.495	1.495	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.71	0.6208	0.6208	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($3.5 \leq E_t < 5\text{GeV}$)	0.4132	0.4731	0.4731	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($5 \leq E_t < 7\text{GeV}$)	0.1389	0.1523	0.1523	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ all ($7 \leq E_t < 30\text{GeV}$)	0.02833	0.02887	0.02887	0 %
NSK (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.0162	-0.388 %
NSK (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.01313	0 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004335	0 %
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003048	0.003051	0.003051	0 %
NSK (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03281	-0.1919 %
NSK (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %
NSK (1 μ -like ring): ν_e all ($0 \leq E_t < 0.5\text{GeV}$)	0.004443	0.004347	0.004701	8.153 %
NSK (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.7\text{GeV}$)	0.007368	0.007722	0.00769	-0.4125 %
NSK (1 μ -like ring): ν_e all ($0.7 \leq E_t < 0.8\text{GeV}$)	0.003958	0.004275	0.004176	-2.312 %
NSK (1 μ -like ring): ν_e all ($0.8 \leq E_t < 1.5\text{GeV}$)	0.02699	0.02869	0.02844	-0.8739 %
NSK (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.03865	0.03927	0.03924	-0.06955 %
NSK (1 μ -like ring): ν_e all ($2.5 \leq E_t < 4\text{GeV}$)	0.03615	0.03646	0.03646	-0.01529 %
NSK (1 μ -like ring): ν_e all ($4 \leq E_t < 30\text{GeV}$)	0.01889	0.01921	0.01921	-0.01682 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0007905	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.0007453	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.33e-05	7.33e-05	7.33e-05	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002189	0.000219	0.000219	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001828	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ all ($0 \leq E_t < 2.5\text{GeV}$)	0.005279	0.005397	0.005397	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ all ($2.5 \leq E_t < 30\text{GeV}$)	0.008164	0.008302	0.008302	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC all	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0 \leq E_t < 0.4\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($5 \leq E_t < 7\text{GeV}$)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e all ($7 \leq E_t < 30\text{GeV}$)	0	0	0	0 %

Table 56: Effect of $f_{bindE;t,r}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1σ		BANFF tuned -1σ	
NS_K (1 μ -like ring)	210.5	204.7	205.9	0.5634 %	203.6	-0.5634 %
NS_K (1 μ -like ring): ν_μ CCQE	166.4	155	155	0 %	155	0 %
NS_K (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	34.95	0 %	34.95	0 %
NS_K (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	1.901	100 %	0	-100 %
NS_K (1 μ -like ring): ν_μ CC other (ν_μ disap)	4.315	4.199	4.199	0 %	4.199	0 %
NS_K (1 μ -like ring): ν_μ CC all	200.6	195.1	196.1	0.487 %	194.2	-0.487 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625	0 %	1.625	0 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466	0 %	1.466	0 %
NS_K (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092	0 %	3.092	0 %
NS_K (1 μ -like ring): ν_μ CCQE	4.46	3.981	3.981	0 %	3.981	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	1.762	0 %	1.762	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.2111	0.2028	0.4056	100 %	0	-100 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disap)	0.2539	0.2478	0.2478	0 %	0.2478	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.397	3.274 %	5.992	-3.274 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %	0.09042	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %	0.07761	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %	0.168	0 %
NS_K (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01626	0 %	0.01626	0 %
NS_K (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.01313	0 %	0.01313	0 %
NS_K (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.000867	100 %	0	-100 %
NS_K (1 μ -like ring): ν_e CC other (ν_μ disap)	0.003048	0.003051	0.003051	0 %	0.003051	0 %
NS_K (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.0333	1.319 %	0.03244	-1.319 %
NS_K (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %	0.04942	0 %
NS_K (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %	0.05768	0 %
NS_K (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %	0.1071	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0007905	0 %	0.0007905	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.0007453	0 %	0.0007453	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.333e-05	7.333e-05	0.0001467	100 %	0	-100 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disap)	0.0002189	0.000219	0.000219	0 %	0.000219	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001901	4.011 %	0.001755	-4.011 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %	0.005916	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %	0.005954	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %	0.01187	0 %
NS_K (1 μ -like ring): oscillation ν_e CCQE	0	0	0	0 %	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0	0 %	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC coherent	0	0	0	0 %	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0	0 %	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC all	0	0	0	0 %	0	0 %

Table 57: Effect of $f_{CCcoh;t}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1 σ		BANFF tuned -1 σ	
NS_K (1 μ -like ring)	210.5	204.7	205.3	0.2595 %	204.2	-0.2595 %
NS_K (1 μ -like ring): ν_μ CCQE	166.4	155	155	0 %	155	0 %
NS_K (1 μ -like ring): ν_μ CC 1π	28.88	34.95	34.95	0 %	34.95	0 %
NS_K (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.9503	0 %	0.9503	0 %
NS_K (1 μ -like ring): ν_μ CC other (ν_μ disap)	4.315	4.199	4.199	0 %	4.199	0 %
NS_K (1 μ -like ring): ν_μ CC all	200.6	195.1	195.1	0 %	195.1	0 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC $1\pi^{+/-}$	1.697	1.625	2.113	30 %	1.138	-30 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466	0 %	1.466	0 %
NS_K (1 μ -like ring): ν_μ NC all	3.218	3.092	3.58	15.77 %	2.604	-15.77 %
NS_K (1 μ -like ring): ν_μ CCQE	4.46	3.981	3.981	0 %	3.981	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC 1π	1.445	1.762	1.762	0 %	1.762	0 %
NS_K (1 μ -like ring): ν_μ CC coherent	0.2111	0.2028	0.2028	0 %	0.2028	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disap)	0.2539	0.2478	0.2478	0 %	0.2478	0 %
NS_K (1 μ -like ring): ν_μ CC all	6.37	6.194	6.194	0 %	6.194	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC $1\pi^{+/-}$	0.09198	0.09042	0.1175	30 %	0.0633	-30 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %	0.07761	0 %
NS_K (1 μ -like ring): ν_μ NC all	0.1716	0.168	0.1952	16.14 %	0.1409	-16.14 %
NS_K (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01626	0 %	0.01626	0 %
NS_K (1 μ -like ring): ν_e CC 1π	0.009932	0.01313	0.01313	0 %	0.01313	0 %
NS_K (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004335	0 %	0.0004335	0 %
NS_K (1 μ -like ring): ν_e CC other (ν_μ disap)	0.003048	0.003051	0.003051	0 %	0.003051	0 %
NS_K (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03287	0 %	0.03287	0 %
NS_K (1 μ -like ring): ν_e NC $1\pi^{+/-}$	0.04865	0.04942	0.06425	30 %	0.03459	-30 %
NS_K (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %	0.05768	0 %
NS_K (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1219	13.84 %	0.09228	-13.84 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0007905	0 %	0.0007905	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC 1π	0.0006013	0.0007453	0.0007453	0 %	0.0007453	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.333e-05	7.333e-05	7.333e-05	0 %	7.333e-05	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disap)	0.0002189	0.000219	0.000219	0 %	0.000219	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001828	0 %	0.001828	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC $1\pi^{+/-}$	0.005805	0.005916	0.007691	30 %	0.004141	-30 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %	0.005954	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01365	14.95 %	0.0101	-14.95 %
NS_K (1 μ -like ring): oscillation ν_e CCQE	0	0	0	0 %	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC 1π	0	0	0	0 %	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC coherent	0	0	0	0 %	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0	0 %	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC all	0	0	0	0 %	0	0 %

Table 58: Effect of $f_{NC1\pi^\pm;t}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1 σ		BANFF tuned -1 σ	
NS_K (1 μ -like ring)	210.5	204.7	205.2	0.2356 %	204.3	-0.2356 %
NS_K (1 μ -like ring): ν_μ CCQE	166.4	155	155	0 %	155	0 %
NS_K (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	34.95	0 %	34.95	0 %
NS_K (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.9503	0 %	0.9503	0 %
NS_K (1 μ -like ring): ν_μ CC other (ν_μ disap)	4.315	4.199	4.199	0 %	4.199	0 %
NS_K (1 μ -like ring): ν_μ CC all	200.6	195.1	195.1	0 %	195.1	0 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625	0 %	1.625	0 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.906	30 %	1.027	-30 %
NS_K (1 μ -like ring): ν_μ NC all	3.218	3.092	3.532	14.23 %	2.652	-14.23 %
NS_K (1 μ -like ring): ν_μ CCQE	4.46	3.981	3.981	0 %	3.981	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	1.762	0 %	1.762	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.2111	0.2028	0.2028	0 %	0.2028	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disap)	0.2539	0.2478	0.2478	0 %	0.2478	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.194	0 %	6.194	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %	0.09042	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.1009	30 %	0.05433	-30 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.1913	13.86 %	0.1448	-13.86 %
NS_K (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01626	0 %	0.01626	0 %
NS_K (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.01313	0 %	0.01313	0 %
NS_K (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004335	0 %	0.0004335	0 %
NS_K (1 μ -like ring): ν_e CC other (ν_μ disap)	0.003048	0.003051	0.003051	0 %	0.003051	0 %
NS_K (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03287	0 %	0.03287	0 %
NS_K (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %	0.04942	0 %
NS_K (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.07499	30 %	0.04038	-30 %
NS_K (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1244	16.16 %	0.0898	-16.16 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0007905	0 %	0.0007905	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.0007453	0 %	0.0007453	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.333e-05	7.333e-05	7.333e-05	0 %	7.333e-05	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disap)	0.0002189	0.000219	0.000219	0 %	0.000219	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001828	0 %	0.001828	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %	0.005916	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.00774	30 %	0.004168	-30 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01366	15.05 %	0.01008	-15.05 %
NS_K (1 μ -like ring): oscillation ν_e CCQE	0	0	0	0 %	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0	0 %	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC coherent	0	0	0	0 %	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0	0 %	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC all	0	0	0	0 %	0	0 %

Table 59: Effect of $f_{NCoth;t}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1 σ		BANFF tuned -1 σ	
NS_K (1 μ -like ring)	210.5	204.7	204.7	0.0005084 %	204.7	-0.0005084 %
NS_K (1 μ -like ring): ν_μ CCQE	166.4	155	155	0 %	155	0 %
NS_K (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	34.95	0 %	34.95	0 %
NS_K (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.9503	0 %	0.9503	0 %
NS_K (1 μ -like ring): ν_μ CC other (ν_μ disap)	4.315	4.199	4.199	0 %	4.199	0 %
NS_K (1 μ -like ring): ν_μ CC all	200.6	195.1	195.1	0 %	195.1	0 %
NS_K (1 μ -like ring): $\nu_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	1.697	1.625	1.625	0 %	1.625	0 %
NS_K (1 μ -like ring): $\nu_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	1.522	1.466	1.466	0 %	1.466	0 %
NS_K (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092	0 %	3.092	0 %
NS_K (1 μ -like ring): ν_μ CCQE	4.46	3.981	3.981	0 %	3.981	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	1.762	0 %	1.762	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.2111	0.2028	0.2028	0 %	0.2028	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disap)	0.2539	0.2478	0.2478	0 %	0.2478	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.194	0 %	6.194	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\nu_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %	0.09042	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\nu_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %	0.07761	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %	0.168	0 %
NS_K (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01675	3 %	0.01577	-3 %
NS_K (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.01352	3 %	0.01273	-3 %
NS_K (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004465	3 %	0.0004205	-3 %
NS_K (1 μ -like ring): ν_e CC other (ν_μ disap)	0.003048	0.003051	0.003142	3 %	0.002959	-3 %
NS_K (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03386	3 %	0.03188	-3 %
NS_K (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %	0.04942	0 %
NS_K (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %	0.05768	0 %
NS_K (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %	0.1071	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0008142	3 %	0.0007667	-3 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.0007677	3 %	0.000723	-3 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.333e-05	7.333e-05	7.553e-05	3 %	7.113e-05	-3 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disap)	0.0002189	0.000219	0.0002256	3 %	0.0002125	-3 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001883	3 %	0.001773	-3 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %	0.005916	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %	0.005954	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %	0.01187	0 %
NS_K (1 μ -like ring): oscillation ν_e CCQE	0	0	0	0 %	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0	0 %	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC coherent	0	0	0	0 %	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0	0 %	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC all	0	0	0	0 %	0	0 %

Table 60: Effect of $f_{CC\nu_e;t}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NS_K (1 μ -like ring)	210.5	204.7	207.2	1.211 %
NS_K (1 μ -like ring): ν_μ CCQE	166.4	155	155	0 %
NS_K (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	34.95	0 %
NS_K (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.9503	0 %
NS_K (1 μ -like ring): ν_μ CC other (ν_μ disap)	4.315	4.199	4.199	0 %
NS_K (1 μ -like ring): ν_μ CC all	200.6	195.1	195.1	0 %
NS_K (1 μ -like ring): $\nu_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	1.697	1.625	1.625	0 %
NS_K (1 μ -like ring): $\nu_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	1.522	1.466	1.466	0 %
NS_K (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092	0 %
NS_K (1 μ -like ring): ν_μ CCQE	4.46	3.981	5.574	40 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	2.467	40 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.2111	0.2028	0.2839	40 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disap)	0.2539	0.2478	0.3469	40 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	8.672	40 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %
NS_K (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01626	0 %
NS_K (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.01313	0 %
NS_K (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004335	0 %
NS_K (1 μ -like ring): ν_e CC other (ν_μ disap)	0.003048	0.003051	0.003051	0 %
NS_K (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03287	0 %
NS_K (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %
NS_K (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %
NS_K (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.001107	40 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.001043	40 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.333e-05	7.333e-05	0.0001027	40 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disap)	0.0002189	0.000219	0.0003066	40 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.002559	40 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %
NS_K (1 μ -like ring): oscillation ν_e CCQE	0	0	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC coherent	0	0	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0	0 %
NS_K (1 μ -like ring): oscillation ν_e CC all	0	0	0	0 %

Table 61: Effect of $f_{CC\bar{\nu};t}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned $+1\sigma$		BANFF tuned -1σ	
NSK (1 μ -like ring)	210.5	204.7	204.7	0.0001358 %	204.7	-0.0001358 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r < 0.4$ GeV)	7.784	7.518	7.518	0.00363 %	7.518	-0.00363 %
NSK (1 μ -like ring): ν_μ CCQE ($0.4 \leq E_r < 1.1$ GeV)	136.8	128.3	128.3	0 %	128.3	0 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r \geq 1.1$ GeV)	21.78	19.2	19.2	0 %	19.2	0 %
NSK (1 μ -like ring): ν_μ CCQE	166.4	155	155	0.000176 %	155	-0.000176 %
NSK (1 μ -like ring): ν_μ CC 1π	28.88	34.95	34.95	0 %	34.95	0 %
NSK (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.9503	0 %	0.9503	0 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	4.315	4.199	4.199	0 %	4.199	0 %
NSK (1 μ -like ring): ν_μ CC all	200.6	195.1	195.1	0.0001399 %	195.1	-0.0001399 %
NSK (1 μ -like ring): ν_μ/ν_τ NC $1\pi^{+/-}$	1.697	1.625	1.625	0 %	1.625	0 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466	0 %	1.466	0 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092	0 %	3.092	0 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r < 0.4$ GeV)	0.1497	0.1414	0.1414	0.00363 %	0.1414	-0.00363 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($0.4 \leq E_r < 1.1$ GeV)	1.979	1.873	1.873	0 %	1.873	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($E_r \geq 1.1$ GeV)	2.331	1.967	1.967	0 %	1.967	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	4.46	3.981	3.981	0.000129 %	3.981	-0.000129 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1π	1.445	1.762	1.762	0 %	1.762	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.2111	0.2028	0.2028	0 %	0.2028	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2539	0.2478	0.2478	0 %	0.2478	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.194	8.289e-05 %	6.194	-8.289e-05 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC $1\pi^{+/-}$	0.09198	0.09042	0.09042	0 %	0.09042	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %	0.07761	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %	0.168	0 %
NSK (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01626	0 %	0.01626	0 %
NSK (1 μ -like ring): ν_e CC 1π	0.009932	0.01313	0.01313	0 %	0.01313	0 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004335	0 %	0.0004335	0 %
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003048	0.003051	0.003051	0 %	0.003051	0 %
NSK (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03287	0 %	0.03287	0 %
NSK (1 μ -like ring): ν_e NC $1\pi^{+/-}$	0.04865	0.04942	0.04942	0 %	0.04942	0 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %	0.05768	0 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %	0.1071	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0007905	0 %	0.0007905	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1π	0.0006013	0.0007453	0.0007453	0 %	0.0007453	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.333e-05	7.333e-05	7.333e-05	0 %	7.333e-05	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002189	0.000219	0.000219	0 %	0.000219	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001828	0 %	0.001828	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC $1\pi^{+/-}$	0.005805	0.005916	0.005916	0 %	0.005916	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %	0.005954	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %	0.01187	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0	0	0	0 %	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1π	0	0	0	0 %	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0	0	0	0 %	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0	0 %	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC all	0	0	0	0 %	0	0 %

Table 62: Effect of $f_{0;t,r}^{FSI}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NSK (1 μ -like ring)	210.5	204.7	204.8 0.04533 %	204.7 -0.04533 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r < 0.4$ GeV)	7.784	7.518	7.518 0 %	7.518 0 %
NSK (1 μ -like ring): ν_μ CCQE ($0.4 \leq E_r < 1.1$ GeV)	136.8	128.3	128.4 0.07128 %	128.2 -0.07128 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r \geq 1.1$ GeV)	21.78	19.2	19.2 0 %	19.2 0 %
NSK (1 μ -like ring): ν_μ CCQE	166.4	155	155.1 0.059 %	155 -0.059 %
NSK (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	34.95 0 %	34.95 0 %
NSK (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.9503 0 %	0.9503 0 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	4.315	4.199	4.199 0 %	4.199 0 %
NSK (1 μ -like ring): ν_μ CC all	200.6	195.1	195.2 0.04687 %	195 -0.04687 %
NSK (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625 0 %	1.625 0 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466 0 %	1.466 0 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092 0 %	3.092 0 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r < 0.4$ GeV)	0.1497	0.1414	0.1414 0 %	0.1414 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($0.4 \leq E_r < 1.1$ GeV)	1.979	1.873	1.874 0.07128 %	1.872 -0.07128 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($E_r \geq 1.1$ GeV)	2.331	1.967	1.967 0 %	1.967 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	4.46	3.981	3.983 0.03353 %	3.98 -0.03353 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	1.762 0 %	1.762 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.2111	0.2028	0.2028 0 %	0.2028 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2539	0.2478	0.2478 0 %	0.2478 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.196 0.02155 %	6.193 -0.02155 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042 0 %	0.09042 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761 0 %	0.07761 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168 0 %	0.168 0 %
NSK (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01626 0 %	0.01626 0 %
NSK (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.01313 0 %	0.01313 0 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004335 0 %	0.0004335 0 %
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003048	0.003051	0.003051 0 %	0.003051 0 %
NSK (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03287 0 %	0.03287 0 %
NSK (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942 0 %	0.04942 0 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768 0 %	0.05768 0 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071 0 %	0.1071 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0007905 0 %	0.0007905 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.0007453 0 %	0.0007453 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.333e-05	7.333e-05	7.333e-05 0 %	7.333e-05 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002189	0.000219	0.000219 0 %	0.000219 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001828 0 %	0.001828 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916 0 %	0.005916 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954 0 %	0.005954 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187 0 %	0.01187 0 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0	0	0 0 %	0 0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0 0 %	0 0 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0	0	0 0 %	0 0 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0 0 %	0 0 %
NSK (1 μ -like ring): oscillation ν_e CC all	0	0	0 0 %	0 0 %

Table 63: Effect of $f_{1;t,r}^{FSI}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NSK (1 μ -like ring)	210.5	204.7	204.8	0.02872 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r < 0.4$ GeV)	7.784	7.518	7.518	0 %
NSK (1 μ -like ring): ν_μ CCQE ($0.4 \leq E_r < 1.1$ GeV)	136.8	128.3	128.3	0 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r \geq 1.1$ GeV)	21.78	19.2	19.25	0.2778 %
NSK (1 μ -like ring): ν_μ CCQE	166.4	155	155.1	0.0344 %
NSK (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	34.95	0 %
NSK (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.9503	0 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	4.315	4.199	4.199	0 %
NSK (1 μ -like ring): ν_μ CC all	200.6	195.1	195.2	0.02733 %
NSK (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625	0 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466	0 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092	0 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r < 0.4$ GeV)	0.1497	0.1414	0.1414	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($0.4 \leq E_r < 1.1$ GeV)	1.979	1.873	1.873	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($E_r \geq 1.1$ GeV)	2.331	1.967	1.972	0.2778 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	4.46	3.981	3.987	0.1372 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	1.762	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.2111	0.2028	0.2028	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2539	0.2478	0.2478	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.2	0.08821 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %
NSK (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01626	0 %
NSK (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.01313	0 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004335	0 %
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003048	0.003051	0.003051	0 %
NSK (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03287	0 %
NSK (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0007905	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.0007453	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.333e-05	7.333e-05	7.333e-05	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002189	0.000219	0.000219	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001828	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC all	0	0	0	0 %

Table 64: Effect of $f_{2;t,r}^{FSI}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NSK (1 μ -like ring)	210.5	204.7	208.4	1.79 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r < 0.4$ GeV)	7.784	7.518	7.518	0 %
NSK (1 μ -like ring): ν_μ CCQE ($0.4 \leq E_r < 1.1$ GeV)	136.8	128.3	128.3	0 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r \geq 1.1$ GeV)	21.78	19.2	19.2	0 %
NSK (1 μ -like ring): ν_μ CCQE	166.4	155	155	0 %
NSK (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	37.97	8.66 %
NSK (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	1.033	8.66 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	4.315	4.199	4.562	8.66 %
NSK (1 μ -like ring): ν_μ CC all	200.6	195.1	198.6	1.779 %
NSK (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625	0 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466	0 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092	0 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r < 0.4$ GeV)	0.1497	0.1414	0.1414	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($0.4 \leq E_r < 1.1$ GeV)	1.979	1.873	1.873	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($E_r \geq 1.1$ GeV)	2.331	1.967	1.967	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	4.46	3.981	3.981	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	1.915	8.66 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.2111	0.2028	0.2204	8.66 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2539	0.2478	0.2693	8.66 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.386	3.094 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %
NSK (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01626	0 %
NSK (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.01313	0 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0 %	0.0004335
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003048	0.003051	0 %	0.003051
NSK (1 μ -like ring): ν_e CC all	0.03039	0.03287	0 %	0.03287
NSK (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0007905	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.0007453	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.333e-05	7.333e-05	0 %	7.333e-05
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002189	0.000219	0 %	0.000219
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001828	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC all	0	0	0	0 %

Table 65: Effect of $f_{3;t,r}^{FSI}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned $+1\sigma$		BANFF tuned -1σ	
NSK (1 μ -like ring)	210.5	204.7	204.7	0.0001911 %	204.7	-0.0001911 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r < 0.4$ GeV)	7.784	7.518	7.518	0 %	7.518	0 %
NSK (1 μ -like ring): ν_μ CCQE ($0.4 \leq E_r < 1.1$ GeV)	136.8	128.3	128.3	0 %	128.3	0 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r \geq 1.1$ GeV)	21.78	19.2	19.2	0 %	19.2	0 %
NSK (1 μ -like ring): ν_μ CCQE	166.4	155	155	0 %	155	0 %
NSK (1 μ -like ring): ν_μ CC 1π	28.88	34.95	34.95	0 %	34.95	0 %
NSK (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.9503	0 %	0.9503	0 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	4.315	4.199	4.199	0 %	4.199	0 %
NSK (1 μ -like ring): ν_μ CC all	200.6	195.1	195.1	0 %	195.1	0 %
NSK (1 μ -like ring): ν_μ/ν_τ NC $1\pi^{+/-}$	1.697	1.625	1.625	0 %	1.625	0 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466	0 %	1.466	0 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092	0 %	3.092	0 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r < 0.4$ GeV)	0.1497	0.1414	0.1414	0 %	0.1414	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($0.4 \leq E_r < 1.1$ GeV)	1.979	1.873	1.873	0 %	1.873	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($E_r \geq 1.1$ GeV)	2.331	1.967	1.967	0 %	1.967	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	4.46	3.981	3.981	0 %	3.981	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1π	1.445	1.762	1.762	0 %	1.762	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.2111	0.2028	0.2028	0 %	0.2028	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2539	0.2478	0.2478	0 %	0.2478	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.194	0 %	6.194	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC $1\pi^{+/-}$	0.09198	0.09042	0.09042	0 %	0.09042	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %	0.07761	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %	0.168	0 %
NSK (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01644	1.128 %	0.01608	-1.128 %
NSK (1 μ -like ring): ν_e CC 1π	0.009932	0.01313	0.01327	1.128 %	0.01298	-1.128 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004384	1.128 %	0.0004286	-1.128 %
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003048	0.003051	0.003085	1.128 %	0.003016	-1.128 %
NSK (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03324	1.128 %	0.0325	-1.128 %
NSK (1 μ -like ring): ν_e NC $1\pi^{+/-}$	0.04865	0.04942	0.04942	0 %	0.04942	0 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %	0.05768	0 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %	0.1071	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0007994	1.128 %	0.0007815	-1.128 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1π	0.0006013	0.0007453	0.0007537	1.128 %	0.0007369	-1.128 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.333e-05	7.333e-05	7.415e-05	1.128 %	7.25e-05	-1.128 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002189	0.000219	0.0002215	1.128 %	0.0002166	-1.128 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001849	1.128 %	0.001808	-1.128 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC $1\pi^{+/-}$	0.005805	0.005916	0.005916	0 %	0.005916	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %	0.005954	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %	0.01187	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0	0	0	0 %	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1π	0	0	0	0 %	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0	0	0	0 %	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0	0 %	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC all	0	0	0	0 %	0	0 %

Table 66: Effect of $f_{4;t,r}^{FSI}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned +1 σ		BANFF tuned -1 σ	
NSK (1 μ -like ring)	210.5	204.7	205	0.1277 %	204.5	-0.1277 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r < 0.4$ GeV)	7.784	7.518	7.518	0 %	7.518	0 %
NSK (1 μ -like ring): ν_μ CCQE ($0.4 \leq E_r < 1.1$ GeV)	136.8	128.3	128.3	0 %	128.3	0 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r \geq 1.1$ GeV)	21.78	19.2	19.2	0 %	19.2	0 %
NSK (1 μ -like ring): ν_μ CCQE	166.4	155	155	0 %	155	0 %
NSK (1 μ -like ring): ν_μ CC 1 π	28.88	34.95	34.95	0 %	34.95	0 %
NSK (1 μ -like ring): ν_μ CC coherent	1.006	0.9503	0.9503	0 %	0.9503	0 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	4.315	4.199	4.199	0 %	4.199	0 %
NSK (1 μ -like ring): ν_μ CC all	200.6	195.1	195.1	0 %	195.1	0 %
NSK (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.751	7.737 %	1.5	-7.737 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.58	7.737 %	1.353	-7.737 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	3.331	7.737 %	2.853	-7.737 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r < 0.4$ GeV)	0.1497	0.1414	0.1414	0 %	0.1414	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($0.4 \leq E_r < 1.1$ GeV)	1.979	1.873	1.873	0 %	1.873	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($E_r \geq 1.1$ GeV)	2.331	1.967	1.967	0 %	1.967	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	4.46	3.981	3.981	0 %	3.981	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.445	1.762	1.762	0 %	1.762	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.2111	0.2028	0.2028	0 %	0.2028	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2539	0.2478	0.2478	0 %	0.2478	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	6.37	6.194	6.194	0 %	6.194	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09742	7.737 %	0.08343	-7.737 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.08362	7.737 %	0.07161	-7.737 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.181	7.737 %	0.155	-7.737 %
NSK (1 μ -like ring): ν_e CCQE	0.01697	0.01626	0.01626	0 %	0.01626	0 %
NSK (1 μ -like ring): ν_e CC 1 π	0.009932	0.01313	0.01313	0 %	0.01313	0 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004335	0.0004335	0.0004335	0 %	0.0004335	0 %
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003048	0.003051	0.003051	0 %	0.003051	0 %
NSK (1 μ -like ring): ν_e CC all	0.03039	0.03287	0.03287	0 %	0.03287	0 %
NSK (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.05324	7.737 %	0.0456	-7.737 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.06215	7.737 %	0.05322	-7.737 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1154	7.737 %	0.09882	-7.737 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.000827	0.0007905	0.0007905	0 %	0.0007905	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0006013	0.0007453	0.0007453	0 %	0.0007453	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.333e-05	7.333e-05	7.333e-05	0 %	7.333e-05	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002189	0.000219	0.000219	0 %	0.000219	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001721	0.001828	0.001828	0 %	0.001828	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.006374	7.737 %	0.005458	-7.737 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.006415	7.737 %	0.005493	-7.737 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01279	7.737 %	0.01095	-7.737 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0	0	0	0 %	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π	0	0	0	0 %	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0	0	0	0 %	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0	0	0	0 %	0	0 %
NSK (1 μ -like ring): oscillation ν_e CC all	0	0	0	0 %	0	0 %

Table 67: Effect of $f_{5;t,r}^{FSI}$ for no oscillations (all mixing parameters set to 0)..

Component	Nominal	BANFF tuned	BANFF tuned $+1\sigma$		BANFF tuned -1σ	
NSK (1 μ -like ring)	59.41	58.37	58.37	-1.217e-14 %	58.37	-2.435e-14 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r < 0.4$ GeV)	3.802	3.653	3.653	0 %	3.653	0 %
NSK (1 μ -like ring): ν_μ CCQE ($0.4 \leq E_r < 1.1$ GeV)	14.98	13.78	13.78	0 %	13.78	0 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r > 1.1$ GeV)	14.5	12.85	12.85	0 %	12.85	0 %
NSK (1 μ -like ring): ν_μ CCQE	33.28	30.29	30.29	0 %	30.29	0 %
NSK (1 μ -like ring): ν_μ CC 1π	14.63	16.93	16.93	0 %	16.93	0 %
NSK (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.3997	0 %	0.3997	0 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	3.771	0 %	3.771	0 %
NSK (1 μ -like ring): ν_μ CC all	52.19	51.39	51.39	0 %	51.39	0 %
NSK (1 μ -like ring): ν_μ/ν_τ NC $1\pi^{+/-}$	1.697	1.625	1.625	0 %	1.625	0 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466	0 %	1.466	0 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092	0 %	3.092	0 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r < 0.4$ GeV)	0.09866	0.09305	0.09305	0 %	0.09305	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($0.4 \leq E_r < 1.1$ GeV)	0.3816	0.3585	0.3585	0 %	0.3585	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($E_r > 1.1$ GeV)	1.71	1.44	1.44	0 %	1.44	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	2.191	1.891	1.891	0 %	1.891	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1π	1.033	1.228	1.228	0 %	1.228	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1084	0 %	0.1084	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.22	0 %	0.22	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.448	0 %	3.448	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC $1\pi^{+/-}$	0.09198	0.09042	0.09042	0 %	0.09042	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %	0.07761	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %	0.168	0 %
NSK (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01507	0 %	0.01507	0 %
NSK (1 μ -like ring): ν_e CC 1π	0.009421	0.01243	0.01243	0 %	0.01243	0 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004036	0 %	0.0004036	0 %
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003007	0 %	0.003007	0 %
NSK (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.0309	0 %	0.0309	0 %
NSK (1 μ -like ring): ν_e NC $1\pi^{+/-}$	0.04865	0.04942	0.04942	0 %	0.04942	0 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %	0.05768	0 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %	0.1071	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.0007554	0 %	0.0007554	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1π	0.0005852	0.0007237	0.0007237	0 %	0.0007237	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	7.028e-05	0 %	7.028e-05	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0002168	0 %	0.0002168	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.001766	0 %	0.001766	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC $1\pi^{+/-}$	0.005805	0.005916	0.005916	0 %	0.005916	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %	0.005954	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %	0.01187	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.08288	0 %	0.08288	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1π	0.02732	0.03527	0.03527	0 %	0.03527	0 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.001949	0 %	0.001949	0 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006716	0 %	0.0006716	0 %
NSK (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.1208	0 %	0.1208	0 %

Table 68: Effect of $f_{E;r}^{SK}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5e-05$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NS_K (1 μ -like ring)	59.41	58.37	58.95 0.9923 %	57.79 -0.9923 %
NS_K (1 μ -like ring): ν_μ CCQE	33.28	30.29	30.83 1.8 %	29.74 -1.8 %
NS_K (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	16.93 0 %	16.93 0 %
NS_K (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.3997 0 %	0.3997 0 %
NS_K (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	3.771 0 %	3.771 0 %
NS_K (1 μ -like ring): ν_μ CC all	52.19	51.39	51.93 1.061 %	50.84 -1.061 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625 0 %	1.625 0 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466 0 %	1.466 0 %
NS_K (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092 0 %	3.092 0 %
NS_K (1 μ -like ring): ν_μ CCQE	2.191	1.891	1.925 1.8 %	1.857 -1.8 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.033	1.228	1.228 0 %	1.228 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1084 0 %	0.1084 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.22 0 %	0.22 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.482 0.9873 %	3.414 -0.9873 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042 0 %	0.09042 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761 0 %	0.07761 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168 0 %	0.168 0 %
NS_K (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01507 0 %	0.01507 0 %
NS_K (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.01243 0 %	0.01243 0 %
NS_K (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004036 0 %	0.0004036 0 %
NS_K (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003007 0 %	0.003007 0 %
NS_K (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.0309 0 %	0.0309 0 %
NS_K (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942 0 %	0.04942 0 %
NS_K (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768 0 %	0.05768 0 %
NS_K (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071 0 %	0.1071 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.0007554 0 %	0.0007554 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0005852	0.0007237	0.0007237 0 %	0.0007237 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	7.028e-05 0 %	7.028e-05 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0002168 0 %	0.0002168 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.001766 0 %	0.001766 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916 0 %	0.005916 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954 0 %	0.005954 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187 0 %	0.01187 0 %
NS_K (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.08288 0 %	0.08288 0 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.03527 0 %	0.03527 0 %
NS_K (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.001949 0 %	0.001949 0 %
NS_K (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006716 0 %	0.0006716 0 %
NS_K (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.1208 0 %	0.1208 0 %

Table 69: Effect of $f_{CCQEoth;r}^{SK}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned $+1\sigma$		BANFF tuned -1σ	
NSK (1 μ -like ring)	59.41	58.37	58.43	0.1091 %	58.3	-0.1091 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r < 0.4$ GeV)	3.802	3.653	3.715	1.7 %	3.591	-1.7 %
NSK (1 μ -like ring): ν_μ CCQE ($0.4 \leq E_r < 1.1$ GeV)	14.98	13.78	13.78	0 %	13.78	0 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r > 1.1$ GeV)	14.5	12.85	12.85	0 %	12.85	0 %
NSK (1 μ -like ring): ν_μ CCQE	33.28	30.29	30.35	0.2051 %	30.22	-0.2051 %
NSK (1 μ -like ring): ν_μ CC 1π	14.63	16.93	16.93	0 %	16.93	0 %
NSK (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.3997	0 %	0.3997	0 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	3.771	0 %	3.771	0 %
NSK (1 μ -like ring): ν_μ CC all	52.19	51.39	51.45	0.1209 %	51.33	-0.1209 %
NSK (1 μ -like ring): ν_μ/ν_τ NC $1\pi^{+/-}$	1.697	1.625	1.625	0 %	1.625	0 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466	0 %	1.466	0 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092	0 %	3.092	0 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r < 0.4$ GeV)	0.09866	0.09305	0.09464	1.7 %	0.09147	-1.7 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($0.4 \leq E_r < 1.1$ GeV)	0.3816	0.3585	0.3585	0 %	0.3585	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($E_r > 1.1$ GeV)	1.71	1.44	1.44	0 %	1.44	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	2.191	1.891	1.893	0.08365 %	1.89	-0.08365 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1π	1.033	1.228	1.228	0 %	1.228	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1084	0 %	0.1084	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.22	0 %	0.22	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.449	0.04589 %	3.446	-0.04589 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC $1\pi^{+/-}$	0.09198	0.09042	0.09042	0 %	0.09042	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %	0.07761	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %	0.168	0 %
NSK (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01507	0 %	0.01507	0 %
NSK (1 μ -like ring): ν_e CC 1π	0.009421	0.01243	0.01243	0 %	0.01243	0 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004036	0 %	0.0004036	0 %
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003007	0 %	0.003007	0 %
NSK (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.0309	0 %	0.0309	0 %
NSK (1 μ -like ring): ν_e NC $1\pi^{+/-}$	0.04865	0.04942	0.04942	0 %	0.04942	0 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %	0.05768	0 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %	0.1071	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.0007554	0 %	0.0007554	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1π	0.0005852	0.0007237	0.0007237	0 %	0.0007237	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	7.028e-05	0 %	7.028e-05	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0002168	0 %	0.0002168	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.001766	0 %	0.001766	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC $1\pi^{+/-}$	0.005805	0.005916	0.005916	0 %	0.005916	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %	0.005954	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %	0.01187	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.08288	0 %	0.08288	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1π	0.02732	0.03527	0.03527	0 %	0.03527	0 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.001949	0 %	0.001949	0 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006716	0 %	0.0006716	0 %
NSK (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.1208	0 %	0.1208	0 %

Table 70: Effect of $f_{CCQERC0;r}^{SK}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned $+1\sigma$		BANFF tuned -1σ	
NSK (1 μ -like ring)	59.41	58.37	58.86	0.8477 %	57.87	-0.8477 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r < 0.4$ GeV)	3.802	3.653	3.653	0 %	3.653	0 %
NSK (1 μ -like ring): ν_μ CCQE ($0.4 \leq E_r < 1.1$ GeV)	14.98	13.78	14.26	3.5 %	13.3	-3.5 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r > 1.1$ GeV)	14.5	12.85	12.85	0 %	12.85	0 %
NSK (1 μ -like ring): ν_μ CCQE	33.28	30.29	30.77	1.592 %	29.8	-1.592 %
NSK (1 μ -like ring): ν_μ CC 1π	14.63	16.93	16.93	0 %	16.93	0 %
NSK (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.3997	0 %	0.3997	0 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	3.771	0 %	3.771	0 %
NSK (1 μ -like ring): ν_μ CC all	52.19	51.39	51.87	0.9384 %	50.91	-0.9384 %
NSK (1 μ -like ring): ν_μ/ν_τ NC $1\pi^{+/-}$	1.697	1.625	1.625	0 %	1.625	0 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466	0 %	1.466	0 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092	0 %	3.092	0 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r < 0.4$ GeV)	0.09866	0.09305	0.09305	0 %	0.09305	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($0.4 \leq E_r < 1.1$ GeV)	0.3816	0.3585	0.371	3.5 %	0.3459	-3.5 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($E_r > 1.1$ GeV)	1.71	1.44	1.44	0 %	1.44	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	2.191	1.891	1.904	0.6634 %	1.879	-0.6634 %
NSK (1 μ -like ring): ν_μ CC 1π	1.033	1.228	1.228	0 %	1.228	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1084	0 %	0.1084	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.22	0 %	0.22	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.46	0.3639 %	3.435	-0.3639 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC $1\pi^{+/-}$	0.09198	0.09042	0.09042	0 %	0.09042	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %	0.07761	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %	0.168	0 %
NSK (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01507	0 %	0.01507	0 %
NSK (1 μ -like ring): ν_e CC 1π	0.009421	0.01243	0.01243	0 %	0.01243	0 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004036	0 %	0.0004036	0 %
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003007	0 %	0.003007	0 %
NSK (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.0309	0 %	0.0309	0 %
NSK (1 μ -like ring): ν_e NC $1\pi^{+/-}$	0.04865	0.04942	0.04942	0 %	0.04942	0 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %	0.05768	0 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %	0.1071	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.0007554	0 %	0.0007554	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1π	0.0005852	0.0007237	0.0007237	0 %	0.0007237	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	7.028e-05	0 %	7.028e-05	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0002168	0 %	0.0002168	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.001766	0 %	0.001766	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC $1\pi^{+/-}$	0.005805	0.005916	0.005916	0 %	0.005916	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %	0.005954	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %	0.01187	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.08288	0 %	0.08288	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1π	0.02732	0.03527	0.03527	0 %	0.03527	0 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.001949	0 %	0.001949	0 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006716	0 %	0.0006716	0 %
NSK (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.1208	0 %	0.1208	0 %

Table 71: Effect of $f_{CCQERC1;r}^{SK}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NSK (1 μ -like ring)	59.41	58.37	59.7 2.278 %	57.04 -2.278 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r < 0.4$ GeV)	3.802	3.653	3.653 0 %	3.653 0 %
NSK (1 μ -like ring): ν_μ CCQE ($0.4 \leq E_r < 1.1$ GeV)	14.98	13.78	13.78 0 %	13.78 0 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r > 1.1$ GeV)	14.5	12.85	14.05 9.3 %	11.66 -9.3 %
NSK (1 μ -like ring): ν_μ CCQE	33.28	30.29	31.48 3.947 %	29.09 -3.947 %
NSK (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	16.93 0 %	16.93 0 %
NSK (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.3997 0 %	0.3997 0 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	3.771 0 %	3.771 0 %
NSK (1 μ -like ring): ν_μ CC all	52.19	51.39	52.58 2.326 %	50.19 -2.326 %
NSK (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625 0 %	1.625 0 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466 0 %	1.466 0 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092 0 %	3.092 0 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r < 0.4$ GeV)	0.09866	0.09305	0.09305 0 %	0.09305 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($0.4 \leq E_r < 1.1$ GeV)	0.3816	0.3585	0.3585 0 %	0.3585 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($E_r > 1.1$ GeV)	1.71	1.44	1.573 9.3 %	1.306 -9.3 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	2.191	1.891	2.025 7.08 %	1.757 -7.08 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.033	1.228	1.228 0 %	1.228 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1084 0 %	0.1084 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.22 0 %	0.22 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.581 3.883 %	3.314 -3.883 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042 0 %	0.09042 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761 0 %	0.07761 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168 0 %	0.168 0 %
NSK (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01507 0 %	0.01507 0 %
NSK (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.01243 0 %	0.01243 0 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004036 0 %	0.0004036 0 %
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003007 0 %	0.003007 0 %
NSK (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.0309 0 %	0.0309 0 %
NSK (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942 0 %	0.04942 0 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768 0 %	0.05768 0 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071 0 %	0.1071 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.0007554 0 %	0.0007554 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0005852	0.0007237	0.0007237 0 %	0.0007237 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	7.028e-05 0 %	7.028e-05 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0002168 0 %	0.0002168 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.001766 0 %	0.001766 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916 0 %	0.005916 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954 0 %	0.005954 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187 0 %	0.01187 0 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.08288 0 %	0.08288 0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.03527 0 %	0.03527 0 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.001949 0 %	0.001949 0 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006716 0 %	0.0006716 0 %
NSK (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.1208 0 %	0.1208 0 %

Table 72: Effect of $f_{CCQERC2;r}^{SK}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NS_K (1 μ -like ring)	59.41	58.37	62.9 7.764 %	53.84 -7.764 %
NS_K (1 μ -like ring): ν_μ CCQE	33.28	30.29	30.29 0 %	30.29 0 %
NS_K (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	20.32 20 %	13.55 -20 %
NS_K (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.4797 20 %	0.3198 -20 %
NS_K (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	4.525 20 %	3.017 -20 %
NS_K (1 μ -like ring): ν_μ CC all	52.19	51.39	55.61 8.213 %	47.17 -8.213 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625 0 %	1.625 0 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466 0 %	1.466 0 %
NS_K (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092 0 %	3.092 0 %
NS_K (1 μ -like ring): ν_μ CCQE	2.191	1.891	1.891 0 %	1.891 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.033	1.228	1.474 20 %	0.9824 -20 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1301 20 %	0.08676 -20 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.2641 20 %	0.176 -20 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.759 9.029 %	3.136 -9.029 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042 0 %	0.09042 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761 0 %	0.07761 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168 0 %	0.168 0 %
NS_K (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01507 0 %	0.01507 0 %
NS_K (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.01243 0 %	0.01243 0 %
NS_K (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004036 0 %	0.0004036 0 %
NS_K (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003007 0 %	0.003007 0 %
NS_K (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.0309 0 %	0.0309 0 %
NS_K (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942 0 %	0.04942 0 %
NS_K (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768 0 %	0.05768 0 %
NS_K (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071 0 %	0.1071 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.0007554 0 %	0.0007554 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0005852	0.0007237	0.0007237 0 %	0.0007237 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	7.028e-05 0 %	7.028e-05 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0002168 0 %	0.0002168 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.001766 0 %	0.001766 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916 0 %	0.005916 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954 0 %	0.005954 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187 0 %	0.01187 0 %
NS_K (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.08288 0 %	0.08288 0 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.03527 0 %	0.03527 0 %
NS_K (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.001949 0 %	0.001949 0 %
NS_K (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006716 0 %	0.0006716 0 %
NS_K (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.1208 0 %	0.1208 0 %

Table 73: Effect of $f_{CCnQE;r}^{SK}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NS_K (1 μ -like ring)	59.41	58.37	62.12	6.426 %
NS_K (1 μ -like ring): ν_μ CCQE	33.28	30.29	30.29	0 %
NS_K (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	16.93	0 %
NS_K (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.3997	0 %
NS_K (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	3.771	0 %
NS_K (1 μ -like ring): ν_μ CC all	52.19	51.39	51.39	0 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	3.43	111 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	3.094	111 %
NS_K (1 μ -like ring): ν_μ NC all	3.218	3.092	6.524	111 %
NS_K (1 μ -like ring): ν_μ CCQE	2.191	1.891	1.891	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.033	1.228	1.228	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1084	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.22	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.448	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.1908	111 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.1638	111 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.3546	111 %
NS_K (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01507	0 %
NS_K (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.01243	0 %
NS_K (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004036	0 %
NS_K (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003007	0 %
NS_K (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.0309	0 %
NS_K (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.1043	111 %
NS_K (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.1217	111 %
NS_K (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.226	111 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.0007554	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0005852	0.0007237	0.0007237	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	7.028e-05	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0002168	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.001766	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.01248	111 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.01256	111 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.02505	111 %
NS_K (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.08288	0 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.03527	0 %
NS_K (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.001949	0 %
NS_K (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006716	0 %
NS_K (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.1208	0 %

Table 74: Effect of $f_{NC;r}^{SK}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ		BANFF tuned -1 σ	
NS_K (1 μ -like ring)	59.41	58.37	58.52	0.2629 %	58.21	-0.2629 %
NS_K (1 μ -like ring): ν_μ CCQE	33.28	30.29	30.29	0 %	30.29	0 %
NS_K (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	16.93	0 %	16.93	0 %
NS_K (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.3997	0 %	0.3997	0 %
NS_K (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	3.771	0 %	3.771	0 %
NS_K (1 μ -like ring): ν_μ CC all	52.19	51.39	51.39	0 %	51.39	0 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625	0 %	1.625	0 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466	0 %	1.466	0 %
NS_K (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092	0 %	3.092	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	2.191	1.891	1.891	0 %	1.891	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.033	1.228	1.228	0 %	1.228	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1084	0 %	0.1084	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.22	0 %	0.22	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.448	0 %	3.448	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %	0.09042	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %	0.07761	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %	0.168	0 %
NS_K (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.03014	100 %	0	-100 %
NS_K (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.02485	100 %	0	-100 %
NS_K (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0008072	100 %	0	-100 %
NS_K (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.006014	100 %	0	-100 %
NS_K (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.06181	100 %	0	-100 %
NS_K (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %	0.04942	0 %
NS_K (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %	0.05768	0 %
NS_K (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %	0.1071	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.001511	100 %	0	-100 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0005852	0.0007237	0.001447	100 %	0	-100 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	0.0001406	100 %	0	-100 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0004335	100 %	0	-100 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.003532	100 %	0	-100 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %	0.005916	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %	0.005954	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %	0.01187	0 %
NS_K (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.1658	100 %	0	-100 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.07054	100 %	0	-100 %
NS_K (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.003897	100 %	0	-100 %
NS_K (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.001343	100 %	0	-100 %
NS_K (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.2415	100 %	0	-100 %

Table 75: Effect of $f_{\nu_e:r}^{SK}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NS_K (1 μ -like ring)	59.41	58.37	58.76 0.6702 %	57.98 -0.6702 %
NS_K (1 μ -like ring): ν_μ CCQE	33.28	30.29	30.68 1.291 %	29.89 -1.291 %
NS_K (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	16.93 0 %	16.93 0 %
NS_K (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.3998 0.01628 %	0.3996 -0.01628 %
NS_K (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	3.771 0 %	3.771 0 %
NS_K (1 μ -like ring): ν_μ CC all	52.19	51.39	51.78 0.761 %	51 -0.761 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625 0 %	1.625 0 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466 0 %	1.466 0 %
NS_K (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092 0 %	3.092 0 %
NS_K (1 μ -like ring): ν_μ all ($0 \leq E_t < 0.4\text{GeV}$)	4.38	4.212	4.603 9.283 %	3.821 -9.283 %
NS_K (1 μ -like ring): ν_μ all ($0.4 \leq E_t < 0.5\text{GeV}$)	3.276	3.209	3.209 0 %	3.209 0 %
NS_K (1 μ -like ring): ν_μ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.5893	0.5811	0.5811 0 %	0.5811 0 %
NS_K (1 μ -like ring): ν_μ all ($0.6 \leq E_t < 0.7\text{GeV}$)	1.578	1.54	1.54 0 %	1.54 0 %
NS_K (1 μ -like ring): ν_μ all ($0.7 \leq E_t < 1\text{GeV}$)	10.46	9.917	9.917 0 %	9.917 0 %
NS_K (1 μ -like ring): ν_μ all ($1 \leq E_t < 1.5\text{GeV}$)	9.362	9.414	9.414 0 %	9.414 0 %
NS_K (1 μ -like ring): ν_μ all ($1.5 \leq E_t < 2.5\text{GeV}$)	9.824	9.316	9.316 0 %	9.316 0 %
NS_K (1 μ -like ring): ν_μ all ($2.5 \leq E_t < 3.5\text{GeV}$)	6.285	5.575	5.575 0 %	5.575 0 %
NS_K (1 μ -like ring): ν_μ all ($3.5 \leq E_t < 5\text{GeV}$)	6.729	7.556	7.556 0 %	7.556 0 %
NS_K (1 μ -like ring): ν_μ all ($5 \leq E_t < 7\text{GeV}$)	2.408	2.62	2.62 0 %	2.62 0 %
NS_K (1 μ -like ring): ν_μ all ($7 \leq E_t < 30\text{GeV}$)	0.5198	0.5386	0.5386 0 %	0.5386 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	2.191	1.891	1.891 0 %	1.891 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.033	1.228	1.228 0 %	1.228 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1084 0 %	0.1084 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.22 0 %	0.22 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.448 0 %	3.448 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042 0 %	0.09042 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761 0 %	0.07761 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC all	0.1716	0.168	0.168 0 %	0.168 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0 \leq E_t < 0.4\text{GeV}$)	0.1056	0.09981	0.09981 0 %	0.09981 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.04076	0.03888	0.03888 0 %	0.03888 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.005182	0.005009	0.005009 0 %	0.005009 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.01328	0.01312	0.01312 0 %	0.01312 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.7 \leq E_t < 1\text{GeV}$)	0.2604	0.2585	0.2585 0 %	0.2585 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($1 \leq E_t < 1.5\text{GeV}$)	0.8119	0.8223	0.8223 0 %	0.8223 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($1.5 \leq E_t < 2.5\text{GeV}$)	1.292	1.184	1.184 0 %	1.184 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.6451	0.5646	0.5646 0 %	0.5646 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($3.5 \leq E_t < 5\text{GeV}$)	0.3945	0.4515	0.4515 0 %	0.4515 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($5 \leq E_t < 7\text{GeV}$)	0.1361	0.1492	0.1492 0 %	0.1492 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($7 \leq E_t < 30\text{GeV}$)	0.02811	0.02864	0.02864 0 %	0.02864 0 %
NS_K (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01507 0 %	0.01507 0 %
NS_K (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.01243 0 %	0.01243 0 %
NS_K (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004036 0 %	0.0004036 0 %
NS_K (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003007 0 %	0.003007 0 %
NS_K (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.0309 0 %	0.0309 0 %
NS_K (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942 0 %	0.04942 0 %
NS_K (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768 0 %	0.05768 0 %
NS_K (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071 0 %	0.1071 0 %
NS_K (1 μ -like ring): ν_e all ($0 \leq E_t < 0.5\text{GeV}$)	0.004149	0.004058	0.004058 0 %	0.004058 0 %
NS_K (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.7\text{GeV}$)	0.006751	0.007069	0.007069 0 %	0.007069 0 %
NS_K (1 μ -like ring): ν_e all ($0.7 \leq E_t < 0.8\text{GeV}$)	0.003714	0.004002	0.004002 0 %	0.004002 0 %
NS_K (1 μ -like ring): ν_e all ($0.8 \leq E_t < 1.5\text{GeV}$)	0.02648	0.02808	0.02808 0 %	0.02808 0 %
NS_K (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.03854	0.03916	0.03916 0 %	0.03916 0 %
NS_K (1 μ -like ring): ν_e all ($2.5 \leq E_t < 4\text{GeV}$)	0.03613	0.03644	0.03644 0 %	0.03644 0 %
NS_K (1 μ -like ring): ν_e all ($4 \leq E_t < 30\text{GeV}$)	0.01889	0.0192	0.0192 0 %	0.0192 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.0007554 0 %	0.0007554 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0005852	0.0007237	0.0007237 0 %	0.0007237 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	7.028e-05 0 %	7.028e-05 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0002168 0 %	0.0002168 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.001766 0 %	0.001766 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916 0 %	0.005916 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954 0 %	0.005954 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187 0 %	0.01187 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ all ($0 \leq E_t < 2.5\text{GeV}$)	0.005225	0.005338	0.005338 0 %	0.005338 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ all ($2.5 \leq E_t < 30\text{GeV}$)	0.008161	0.008298	0.008298 0 %	0.008298 0 %
NS_K (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.08305 0.1982 %	0.08272 -0.1982 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.03528 0.01083 %	0.03527 -0.01083 %
NS_K (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.001949 0 %	0.001949 0 %
NS_K (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006716 0 %	0.0006716 0 %
NS_K (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.1209 0.1392 %	0.1206 -0.1392 %
NS_K (1 μ -like ring): oscillation ν_e all ($0 \leq E_t < 0.4\text{GeV}$)	0.001862	0.001811	0.001979 0.283 %	0.001642 -0.283 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.01178	0.01191	0.01191 0 %	0.01191 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.0301	0.03129	0.03129 0 %	0.03129 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.03551	0.03652	0.03652 0 %	0.03652 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	0.0326	0.03309	0.03309 0 %	0.03309 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	0.004319	0.004798	0.004798 0 %	0.004798 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.001024	0.001061	0.001061 0 %	0.001061 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.000191	0.0001771	0.0001771 0 %	0.0001771 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	7.323e-05	7.676e-05	7.676e-05 0 %	7.676e-05 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($5 \leq E_t < 7\text{GeV}$)	3.281e-05	3.708e-05	3.708e-05 0 %	3.708e-05 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($7 \leq E_t < 30\text{GeV}$)	5.487e-06	6.152e-06	6.152e-06 0 %	6.152e-06 0 %

Table 76: Effect of $f_{0,t,r}^{bandff}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
N_{SK} (1 μ -like ring)	59.41	58.37	58.68	58.05
N_{SK} (1 μ -like ring): ν_μ CCQE	33.28	30.29	30.6	29.98
N_{SK} (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	16.93	16.93
N_{SK} (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.4001	0.3993
N_{SK} (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	3.771	3.771
N_{SK} (1 μ -like ring): ν_μ CC all	52.19	51.39	51.7	51.08
N_{SK} (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.628	1.623
N_{SK} (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.467	1.466
N_{SK} (1 μ -like ring): ν_μ NC all	3.218	3.092	3.094	3.089
N_{SK} (1 μ -like ring): ν_μ all ($0 \leq E_t < 0.4\text{GeV}$)	4.38	4.212	4.212	4.212
N_{SK} (1 μ -like ring): ν_μ all ($0.4 \leq E_t < 0.5\text{GeV}$)	3.276	3.209	3.522	2.896
N_{SK} (1 μ -like ring): ν_μ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.5893	0.5811	0.5811	0.5811
N_{SK} (1 μ -like ring): ν_μ all ($0.6 \leq E_t < 0.7\text{GeV}$)	1.578	1.54	1.54	1.54
N_{SK} (1 μ -like ring): ν_μ all ($0.7 \leq E_t < 1\text{GeV}$)	10.46	9.917	9.917	9.917
N_{SK} (1 μ -like ring): ν_μ all ($1 \leq E_t < 1.5\text{GeV}$)	9.362	9.414	9.414	9.414
N_{SK} (1 μ -like ring): ν_μ all ($1.5 \leq E_t < 2.5\text{GeV}$)	9.824	9.316	9.316	9.316
N_{SK} (1 μ -like ring): ν_μ all ($2.5 \leq E_t < 3.5\text{GeV}$)	6.285	5.575	5.575	5.575
N_{SK} (1 μ -like ring): ν_μ all ($3.5 \leq E_t < 5\text{GeV}$)	6.729	7.556	7.556	7.556
N_{SK} (1 μ -like ring): ν_μ all ($5 \leq E_t < 7\text{GeV}$)	2.408	2.62	2.62	2.62
N_{SK} (1 μ -like ring): ν_μ all ($7 \leq E_t < 30\text{GeV}$)	0.5198	0.5386	0.5386	0.5386
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	2.191	1.891	1.891	1.891
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.033	1.228	1.228	1.228
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1084	0.1084
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.22	0.22
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.448	3.448
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0.09042
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0.07761
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0.168
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0 \leq E_t < 0.4\text{GeV}$)	0.1056	0.09981	0.09981	0.09981
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.04076	0.03888	0.03888	0.03888
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.005182	0.005009	0.005009	0.005009
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.01328	0.01312	0.01312	0.01312
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.7 \leq E_t < 1\text{GeV}$)	0.2604	0.2585	0.2585	0.2585
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($1 \leq E_t < 1.5\text{GeV}$)	0.8119	0.8223	0.8223	0.8223
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($1.5 \leq E_t < 2.5\text{GeV}$)	1.292	1.184	1.184	1.184
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.6451	0.5646	0.5646	0.5646
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($3.5 \leq E_t < 5\text{GeV}$)	0.3945	0.4515	0.4515	0.4515
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($5 \leq E_t < 7\text{GeV}$)	0.1361	0.1492	0.1492	0.1492
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($7 \leq E_t < 30\text{GeV}$)	0.02811	0.02864	0.02864	0.02864
N_{SK} (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01507	0.01507
N_{SK} (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.01243	0.01243
N_{SK} (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004036	0.0004036
N_{SK} (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003007	0.003007
N_{SK} (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.0309	0.0309
N_{SK} (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0.04942
N_{SK} (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0.05768
N_{SK} (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0.1071
N_{SK} (1 μ -like ring): ν_e all ($0 \leq E_t < 0.5\text{GeV}$)	0.004149	0.004058	0.004058	0.004058
N_{SK} (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.7\text{GeV}$)	0.006751	0.007069	0.007069	0.007069
N_{SK} (1 μ -like ring): ν_e all ($0.7 \leq E_t < 0.8\text{GeV}$)	0.003714	0.004002	0.004002	0.004002
N_{SK} (1 μ -like ring): ν_e all ($0.8 \leq E_t < 1.5\text{GeV}$)	0.02648	0.02808	0.02808	0.02808
N_{SK} (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.03854	0.03916	0.03916	0.03916
N_{SK} (1 μ -like ring): ν_e all ($2.5 \leq E_t < 4\text{GeV}$)	0.03613	0.03644	0.03644	0.03644
N_{SK} (1 μ -like ring): ν_e all ($4 \leq E_t < 30\text{GeV}$)	0.01889	0.0192	0.0192	0.0192
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.0007554	0.0007554
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0005852	0.0007237	0.0007237	0.0007237
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	7.028e-05	7.028e-05
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0002168	0.0002168
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.001766	0.001766
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0.005916
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0.005954
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0.01187
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ all ($0 \leq E_t < 2.5\text{GeV}$)	0.005225	0.005338	0.005338	0.005338
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ all ($2.5 \leq E_t < 30\text{GeV}$)	0.008161	0.008298	0.008298	0.008298
N_{SK} (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.08392	0.08185
N_{SK} (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.03539	0.03515
N_{SK} (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.00196	0.001937
N_{SK} (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006716	0.0006716
N_{SK} (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.1219	0.1196
N_{SK} (1 μ -like ring): oscillation ν_e all ($0 \leq E_t < 0.4\text{GeV}$)	0.001862	0.001811	0.001811	0.001811
N_{SK} (1 μ -like ring): oscillation ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.01178	0.01191	0.01307	9.757 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.0301	0.03129	0.03129	0.03129
N_{SK} (1 μ -like ring): oscillation ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.03551	0.03652	0.03652	0.03652
N_{SK} (1 μ -like ring): oscillation ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	0.0326	0.03309	0.03309	0.03309
N_{SK} (1 μ -like ring): oscillation ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	0.004319	0.004798	0.004798	0.004798
N_{SK} (1 μ -like ring): oscillation ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.001024	0.001061	0.001061	0.001061
N_{SK} (1 μ -like ring): oscillation ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.000191	0.0001771	0.0001771	0.0001771
N_{SK} (1 μ -like ring): oscillation ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	7.323e-05	7.676e-05	7.676e-05	7.676e-05
N_{SK} (1 μ -like ring): oscillation ν_e all ($5 \leq E_t < 7\text{GeV}$)	3.281e-05	3.708e-05	3.708e-05	3.708e-05
N_{SK} (1 μ -like ring): oscillation ν_e all ($7 \leq E_t < 30\text{GeV}$)	5.487e-06	6.152e-06	6.152e-06	6.152e-06

Table 77: Effect of $f_{1;t,r}^{banff}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
N_{SK} (1 μ -like ring)	59.41	58.37	58.42	0.09415 %
N_{SK} (1 μ -like ring): ν_μ CCQE	33.28	30.29	30.33	0.1385 %
N_{SK} (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	16.93	0.002884 %
N_{SK} (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.3998	0.03394 %
N_{SK} (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	3.771	0 %
N_{SK} (1 μ -like ring): ν_μ CC all	52.19	51.39	51.43	0.08285 %
N_{SK} (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.634	0.5066 %
N_{SK} (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.468	0.09125 %
N_{SK} (1 μ -like ring): ν_μ NC all	3.218	3.092	3.102	0.3096 %
N_{SK} (1 μ -like ring): ν_μ all ($0 \leq E_t < 0.4\text{GeV}$)	4.38	4.212	4.212	0 %
N_{SK} (1 μ -like ring): ν_μ all ($0.4 \leq E_t < 0.5\text{GeV}$)	3.276	3.209	3.209	0 %
N_{SK} (1 μ -like ring): ν_μ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.5893	0.5811	0.6332	8.974 %
N_{SK} (1 μ -like ring): ν_μ all ($0.6 \leq E_t < 0.7\text{GeV}$)	1.578	1.54	1.54	0 %
N_{SK} (1 μ -like ring): ν_μ all ($0.7 \leq E_t < 1\text{GeV}$)	10.46	9.917	9.917	0 %
N_{SK} (1 μ -like ring): ν_μ all ($1 \leq E_t < 1.5\text{GeV}$)	9.362	9.414	9.414	0 %
N_{SK} (1 μ -like ring): ν_μ all ($1.5 \leq E_t < 2.5\text{GeV}$)	9.824	9.316	9.316	0 %
N_{SK} (1 μ -like ring): ν_μ all ($2.5 \leq E_t < 3.5\text{GeV}$)	6.285	5.575	5.575	0 %
N_{SK} (1 μ -like ring): ν_μ all ($3.5 \leq E_t < 5\text{GeV}$)	6.729	7.556	7.556	0 %
N_{SK} (1 μ -like ring): ν_μ all ($5 \leq E_t < 7\text{GeV}$)	2.408	2.62	2.62	0 %
N_{SK} (1 μ -like ring): ν_μ all ($7 \leq E_t < 30\text{GeV}$)	0.5198	0.5386	0.5386	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	2.191	1.891	1.891	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.033	1.228	1.228	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1084	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.22	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.448	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0 \leq E_t < 0.4\text{GeV}$)	0.1056	0.09981	0.09981	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.04076	0.03888	0.03888	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.005182	0.005009	0.005009	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.01328	0.01312	0.01312	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.7 \leq E_t < 1\text{GeV}$)	0.2604	0.2585	0.2585	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($1 \leq E_t < 1.5\text{GeV}$)	0.8119	0.8223	0.8223	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($1.5 \leq E_t < 2.5\text{GeV}$)	1.292	1.184	1.184	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.6451	0.5646	0.5646	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($3.5 \leq E_t < 5\text{GeV}$)	0.3945	0.4515	0.4515	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($5 \leq E_t < 7\text{GeV}$)	0.1361	0.1492	0.1492	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($7 \leq E_t < 30\text{GeV}$)	0.02811	0.02864	0.02864	0 %
N_{SK} (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01507	0 %
N_{SK} (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.01243	0 %
N_{SK} (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004036	0 %
N_{SK} (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003007	0 %
N_{SK} (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.0309	0 %
N_{SK} (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %
N_{SK} (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %
N_{SK} (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %
N_{SK} (1 μ -like ring): ν_e all ($0 \leq E_t < 0.5\text{GeV}$)	0.004149	0.004058	0.004058	0 %
N_{SK} (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.7\text{GeV}$)	0.006751	0.007069	0.007069	0 %
N_{SK} (1 μ -like ring): ν_e all ($0.7 \leq E_t < 0.8\text{GeV}$)	0.003714	0.004002	0.004002	0 %
N_{SK} (1 μ -like ring): ν_e all ($0.8 \leq E_t < 1.5\text{GeV}$)	0.02648	0.02808	0.02808	0 %
N_{SK} (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.03854	0.03916	0.03916	0 %
N_{SK} (1 μ -like ring): ν_e all ($2.5 \leq E_t < 4\text{GeV}$)	0.03613	0.03644	0.03644	0 %
N_{SK} (1 μ -like ring): ν_e all ($4 \leq E_t < 30\text{GeV}$)	0.01889	0.0192	0.0192	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.0007554	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0005852	0.0007237	0.0007237	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	7.028e-05	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0002168	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.001766	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ all ($0 \leq E_t < 2.5\text{GeV}$)	0.005225	0.005338	0.005338	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ all ($2.5 \leq E_t < 30\text{GeV}$)	0.008161	0.008298	0.008298	0 %
N_{SK} (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.0851	2.676 %
N_{SK} (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.03581	1.529 %
N_{SK} (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.001999	2.597 %
N_{SK} (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006716	0 %
N_{SK} (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.1236	2.325 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($0 \leq E_t < 0.4\text{GeV}$)	0.001862	0.001811	0.001811	0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.01178	0.01191	0.01191	0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.0301	0.03129	0.0341	8.974 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.03551	0.03652	0.03652	0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	0.0326	0.03309	0.03309	0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	0.004319	0.004798	0.004798	0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.001024	0.001061	0.001061	0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.000191	0.0001771	0.0001771	0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	7.323e-05	7.676e-05	7.676e-05	0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($5 \leq E_t < 7\text{GeV}$)	3.281e-05	3.708e-05	3.708e-05	0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($7 \leq E_t < 30\text{GeV}$)	5.487e-06	6.152e-06	6.152e-06	0 %

Table 78: Effect of $f_{2;t,r}^{banff}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NS_K (1 μ -like ring)	59.41	58.37	58.5 0.2285 %	58.23 -0.2285 %
NS_K (1 μ -like ring): ν_μ CCQE	33.28	30.29	30.39 0.3297 %	30.19 -0.3297 %
NS_K (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	16.94 0.07373 %	16.92 -0.07373 %
NS_K (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.4001 0.09391 %	0.3993 -0.09391 %
NS_K (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	3.771 9.566e-05 %	3.771 -9.566e-05 %
NS_K (1 μ -like ring): ν_μ CC all	52.19	51.39	51.5 0.2193 %	51.28 -0.2193 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.64 0.9105 %	1.611 -0.9105 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.469 0.1885 %	1.464 -0.1885 %
NS_K (1 μ -like ring): ν_μ NC all	3.218	3.092	3.11 0.568 %	3.074 -0.568 %
NS_K (1 μ -like ring): ν_μ all ($0 \leq E_t < 0.4\text{GeV}$)	4.38	4.212	4.212 0 %	4.212 0 %
NS_K (1 μ -like ring): ν_μ all ($0.4 \leq E_t < 0.5\text{GeV}$)	3.276	3.209	3.209 0 %	3.209 0 %
NS_K (1 μ -like ring): ν_μ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.5893	0.5811	0.5811 0 %	0.5811 0 %
NS_K (1 μ -like ring): ν_μ all ($0.6 \leq E_t < 0.7\text{GeV}$)	1.578	1.54	1.671 8.457 %	1.41 -8.457 %
NS_K (1 μ -like ring): ν_μ all ($0.7 \leq E_t < 1\text{GeV}$)	10.46	9.917	9.917 0 %	9.917 0 %
NS_K (1 μ -like ring): ν_μ all ($1 \leq E_t < 1.5\text{GeV}$)	9.362	9.414	9.414 0 %	9.414 0 %
NS_K (1 μ -like ring): ν_μ all ($1.5 \leq E_t < 2.5\text{GeV}$)	9.824	9.316	9.316 0 %	9.316 0 %
NS_K (1 μ -like ring): ν_μ all ($2.5 \leq E_t < 3.5\text{GeV}$)	6.285	5.575	5.575 0 %	5.575 0 %
NS_K (1 μ -like ring): ν_μ all ($3.5 \leq E_t < 5\text{GeV}$)	6.729	7.556	7.556 0 %	7.556 0 %
NS_K (1 μ -like ring): ν_μ all ($5 \leq E_t < 7\text{GeV}$)	2.408	2.62	2.62 0 %	2.62 0 %
NS_K (1 μ -like ring): ν_μ all ($7 \leq E_t < 30\text{GeV}$)	0.5198	0.5386	0.5386 0 %	0.5386 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	2.191	1.891	1.891 0 %	1.891 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.033	1.228	1.228 0 %	1.228 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1084 0 %	0.1084 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.22 0 %	0.22 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.448 0 %	3.448 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042 0 %	0.09042 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761 0 %	0.07761 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168 0 %	0.168 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0 \leq E_t < 0.4\text{GeV}$)	0.1056	0.09981	0.09981 0 %	0.09981 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.04076	0.03888	0.03888 0 %	0.03888 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.005182	0.005009	0.005009 0 %	0.005009 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.01328	0.01312	0.01312 0 %	0.01312 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.7 \leq E_t < 1\text{GeV}$)	0.2604	0.2585	0.2585 0 %	0.2585 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($1 \leq E_t < 1.5\text{GeV}$)	0.8119	0.8223	0.8223 0 %	0.8223 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($1.5 \leq E_t < 2.5\text{GeV}$)	1.292	1.184	1.184 0 %	1.184 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.6451	0.5646	0.5646 0 %	0.5646 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($3.5 \leq E_t < 5\text{GeV}$)	0.3945	0.4515	0.4515 0 %	0.4515 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($5 \leq E_t < 7\text{GeV}$)	0.1361	0.1492	0.1492 0 %	0.1492 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($7 \leq E_t < 30\text{GeV}$)	0.02811	0.02864	0.02864 0 %	0.02864 0 %
NS_K (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01507 0 %	0.01507 0 %
NS_K (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.01243 0 %	0.01243 0 %
NS_K (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004036 0 %	0.0004036 0 %
NS_K (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003007 0 %	0.003007 0 %
NS_K (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.0309 0 %	0.0309 0 %
NS_K (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942 0 %	0.04942 0 %
NS_K (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768 0 %	0.05768 0 %
NS_K (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071 0 %	0.1071 0 %
NS_K (1 μ -like ring): ν_e all ($0 \leq E_t < 0.5\text{GeV}$)	0.004149	0.004058	0.004058 0 %	0.004058 0 %
NS_K (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.7\text{GeV}$)	0.006751	0.007069	0.007069 0 %	0.007069 0 %
NS_K (1 μ -like ring): ν_e all ($0.7 \leq E_t < 0.8\text{GeV}$)	0.003714	0.004002	0.004002 0 %	0.004002 0 %
NS_K (1 μ -like ring): ν_e all ($0.8 \leq E_t < 1.5\text{GeV}$)	0.02648	0.02808	0.02808 0 %	0.02808 0 %
NS_K (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.03854	0.03916	0.03916 0 %	0.03916 0 %
NS_K (1 μ -like ring): ν_e all ($2.5 \leq E_t < 4\text{GeV}$)	0.03613	0.03644	0.03644 0 %	0.03644 0 %
NS_K (1 μ -like ring): ν_e all ($4 \leq E_t < 30\text{GeV}$)	0.01889	0.0192	0.0192 0 %	0.0192 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.0007554 0 %	0.0007554 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0005852	0.0007237	0.0007237 0 %	0.0007237 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	7.028e-05 0 %	7.028e-05 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0002168 0 %	0.0002168 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.001766 0 %	0.001766 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916 0 %	0.005916 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954 0 %	0.005954 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187 0 %	0.01187 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ all ($0 \leq E_t < 2.5\text{GeV}$)	0.005225	0.005338	0.005338 0 %	0.005338 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ all ($2.5 \leq E_t < 30\text{GeV}$)	0.008161	0.008298	0.008298 0 %	0.008298 0 %
NS_K (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.08506 2.631 %	0.0807 -2.631 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.03613 2.421 %	0.03442 -2.421 %
NS_K (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.002003 2.773 %	0.001895 -2.773 %
NS_K (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006716 0 %	0.0006716 0 %
NS_K (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.1239 2.557 %	0.1177 -2.557 %
NS_K (1 μ -like ring): oscillation ν_e all ($0 \leq E_t < 0.4\text{GeV}$)	0.001862	0.001811	0.001811 0 %	0.001811 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.01178	0.01191	0.01191 0 %	0.01191 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.0301	0.03129	0.03129 0 %	0.03129 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.03551	0.03652	0.03961 8.457 %	0.03343 -8.457 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	0.0326	0.03309	0.03309 0 %	0.03309 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	0.004319	0.004798	0.004798 0 %	0.004798 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.001024	0.001061	0.001061 0 %	0.001061 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.000191	0.0001771	0.0001771 0 %	0.0001771 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	7.323e-05	7.676e-05	7.676e-05 0 %	7.676e-05 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($5 \leq E_t < 7\text{GeV}$)	3.281e-05	3.708e-05	3.708e-05 0 %	3.708e-05 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($7 \leq E_t < 30\text{GeV}$)	5.487e-06	6.152e-06	6.152e-06 0 %	6.152e-06 0 %

Table 79: Effect of $f_{3;t,r}^{banff}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NS_K (1 μ -like ring)	59.41	58.37	59.41	1.79 %
NS_K (1 μ -like ring): ν_μ CCQE	33.28	30.29	31.05	2.525 %
NS_K (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	17.16	1.322 %
NS_K (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.4046	1.222 %
NS_K (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	3.772	0.02109 %
NS_K (1 μ -like ring): ν_μ CC all	52.19	51.39	52.38	1.935 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.663	2.336 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.476	0.6316 %
NS_K (1 μ -like ring): ν_μ NC all	3.218	3.092	3.139	1.528 %
NS_K (1 μ -like ring): ν_μ all ($0 \leq E_t < 0.4\text{GeV}$)	4.38	4.212	4.212	0 %
NS_K (1 μ -like ring): ν_μ all ($0.4 \leq E_t < 0.5\text{GeV}$)	3.276	3.209	3.209	0 %
NS_K (1 μ -like ring): ν_μ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.5893	0.5811	0.5811	0 %
NS_K (1 μ -like ring): ν_μ all ($0.6 \leq E_t < 0.7\text{GeV}$)	1.578	1.54	1.54	0 %
NS_K (1 μ -like ring): ν_μ all ($0.7 \leq E_t < 1\text{GeV}$)	10.46	9.917	10.96	10.5 %
NS_K (1 μ -like ring): ν_μ all ($1 \leq E_t < 1.5\text{GeV}$)	9.362	9.414	9.414	0 %
NS_K (1 μ -like ring): ν_μ all ($1.5 \leq E_t < 2.5\text{GeV}$)	9.824	9.316	9.316	0 %
NS_K (1 μ -like ring): ν_μ all ($2.5 \leq E_t < 3.5\text{GeV}$)	6.285	5.575	5.575	0 %
NS_K (1 μ -like ring): ν_μ all ($3.5 \leq E_t < 5\text{GeV}$)	6.729	7.556	7.556	0 %
NS_K (1 μ -like ring): ν_μ all ($5 \leq E_t < 7\text{GeV}$)	2.408	2.62	2.62	0 %
NS_K (1 μ -like ring): ν_μ all ($7 \leq E_t < 30\text{GeV}$)	0.5198	0.5386	0.5386	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	2.191	1.891	1.891	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.033	1.228	1.228	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1084	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.22	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.448	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0 \leq E_t < 0.4\text{GeV}$)	0.1056	0.09981	0.09981	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.04076	0.03888	0.03888	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.005182	0.005009	0.005009	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.01328	0.01312	0.01312	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.7 \leq E_t < 1\text{GeV}$)	0.2604	0.2585	0.2585	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($1 \leq E_t < 1.5\text{GeV}$)	0.8119	0.8223	0.8223	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($1.5 \leq E_t < 2.5\text{GeV}$)	1.292	1.184	1.184	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.6451	0.5646	0.5646	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($3.5 \leq E_t < 5\text{GeV}$)	0.3945	0.4515	0.4515	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($5 \leq E_t < 7\text{GeV}$)	0.1361	0.1492	0.1492	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($7 \leq E_t < 30\text{GeV}$)	0.02811	0.02864	0.02864	0 %
NS_K (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01507	0 %
NS_K (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.01243	0 %
NS_K (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004036	0 %
NS_K (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003007	0 %
NS_K (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.0309	0 %
NS_K (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %
NS_K (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %
NS_K (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %
NS_K (1 μ -like ring): ν_e all ($0 \leq E_t < 0.5\text{GeV}$)	0.004149	0.004058	0.004058	0 %
NS_K (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.7\text{GeV}$)	0.006751	0.007069	0.007069	0 %
NS_K (1 μ -like ring): ν_e all ($0.7 \leq E_t < 0.8\text{GeV}$)	0.003714	0.004002	0.004002	0 %
NS_K (1 μ -like ring): ν_e all ($0.8 \leq E_t < 1.5\text{GeV}$)	0.02648	0.02808	0.02808	0 %
NS_K (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.03854	0.03916	0.03916	0 %
NS_K (1 μ -like ring): ν_e all ($2.5 \leq E_t < 4\text{GeV}$)	0.03613	0.03644	0.03644	0 %
NS_K (1 μ -like ring): ν_e all ($4 \leq E_t < 30\text{GeV}$)	0.01889	0.0192	0.0192	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.0007554	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0005852	0.0007237	0.0007237	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	7.028e-05	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0002168	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.001766	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ all ($0 \leq E_t < 2.5\text{GeV}$)	0.005225	0.005338	0.005338	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ all ($2.5 \leq E_t < 30\text{GeV}$)	0.008161	0.008298	0.008298	0 %
NS_K (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.0848	2.317 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.03675	4.199 %
NS_K (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.002003	2.792 %
NS_K (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006903	2.782 %
NS_K (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.1242	2.877 %
NS_K (1 μ -like ring): oscillation ν_e all ($0 \leq E_t < 0.4\text{GeV}$)	0.001862	0.001811	0.001811	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.01178	0.01191	0.01191	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.0301	0.03129	0.03129	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.03551	0.03652	0.03652	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	0.0326	0.03309	0.03656	10.5 %
NS_K (1 μ -like ring): oscillation ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	0.004319	0.004798	0.004798	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.001024	0.001061	0.001061	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.000191	0.0001771	0.0001771	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	7.323e-05	7.676e-05	7.676e-05	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($5 \leq E_t < 7\text{GeV}$)	3.281e-05	3.708e-05	3.708e-05	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($7 \leq E_t < 30\text{GeV}$)	5.487e-06	6.152e-06	6.152e-06	0 %

Table 80: Effect of $f_{4;t,r}^{banff}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
N_{SK} (1 μ -like ring)	59.41	58.37	59.24	1.494 %
N_{SK} (1 μ -like ring): ν_μ CCQE	33.28	30.29	30.79	1.666 %
N_{SK} (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	17.24	1.842 %
N_{SK} (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.4048	1.277 %
N_{SK} (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	3.784	0.3535 %
N_{SK} (1 μ -like ring): ν_μ CC all	52.19	51.39	52.22	1.625 %
N_{SK} (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.646	1.242 %
N_{SK} (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.483	1.129 %
N_{SK} (1 μ -like ring): ν_μ NC all	3.218	3.092	3.129	1.189 %
N_{SK} (1 μ -like ring): ν_μ all ($0 \leq E_t < 0.4\text{GeV}$)	4.38	4.212	4.212	0 %
N_{SK} (1 μ -like ring): ν_μ all ($0.4 \leq E_t < 0.5\text{GeV}$)	3.276	3.209	3.209	0 %
N_{SK} (1 μ -like ring): ν_μ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.5893	0.5811	0.5811	0 %
N_{SK} (1 μ -like ring): ν_μ all ($0.6 \leq E_t < 0.7\text{GeV}$)	1.578	1.54	1.54	0 %
N_{SK} (1 μ -like ring): ν_μ all ($0.7 \leq E_t < 1\text{GeV}$)	10.46	9.917	9.917	0 %
N_{SK} (1 μ -like ring): ν_μ all ($1 \leq E_t < 1.5\text{GeV}$)	9.362	9.414	10.29	9.26 %
N_{SK} (1 μ -like ring): ν_μ all ($1.5 \leq E_t < 2.5\text{GeV}$)	9.824	9.316	9.316	0 %
N_{SK} (1 μ -like ring): ν_μ all ($2.5 \leq E_t < 3.5\text{GeV}$)	6.285	5.575	5.575	0 %
N_{SK} (1 μ -like ring): ν_μ all ($3.5 \leq E_t < 5\text{GeV}$)	6.729	7.556	7.556	0 %
N_{SK} (1 μ -like ring): ν_μ all ($5 \leq E_t < 7\text{GeV}$)	2.408	2.62	2.62	0 %
N_{SK} (1 μ -like ring): ν_μ all ($7 \leq E_t < 30\text{GeV}$)	0.5198	0.5386	0.5386	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	2.191	1.891	1.891	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.033	1.228	1.228	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1084	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.22	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.448	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0 \leq E_t < 0.4\text{GeV}$)	0.1056	0.09981	0.09981	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.04076	0.03888	0.03888	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.005182	0.005009	0.005009	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.01328	0.01312	0.01312	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.7 \leq E_t < 1\text{GeV}$)	0.2604	0.2585	0.2585	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($1 \leq E_t < 1.5\text{GeV}$)	0.8119	0.8223	0.8223	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($1.5 \leq E_t < 2.5\text{GeV}$)	1.292	1.184	1.184	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.6451	0.5646	0.5646	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($3.5 \leq E_t < 5\text{GeV}$)	0.3945	0.4515	0.4515	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($5 \leq E_t < 7\text{GeV}$)	0.1361	0.1492	0.1492	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($7 \leq E_t < 30\text{GeV}$)	0.02811	0.02864	0.02864	0 %
N_{SK} (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01507	0 %
N_{SK} (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.01243	0 %
N_{SK} (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004036	0 %
N_{SK} (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003007	0 %
N_{SK} (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.0309	0 %
N_{SK} (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %
N_{SK} (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %
N_{SK} (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %
N_{SK} (1 μ -like ring): ν_e all ($0 \leq E_t < 0.5\text{GeV}$)	0.004149	0.004058	0.004058	0 %
N_{SK} (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.7\text{GeV}$)	0.006751	0.007069	0.007069	0 %
N_{SK} (1 μ -like ring): ν_e all ($0.7 \leq E_t < 0.8\text{GeV}$)	0.003714	0.004002	0.004002	0 %
N_{SK} (1 μ -like ring): ν_e all ($0.8 \leq E_t < 1.5\text{GeV}$)	0.02648	0.02808	0.02808	0 %
N_{SK} (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.03854	0.03916	0.03916	0 %
N_{SK} (1 μ -like ring): ν_e all ($2.5 \leq E_t < 4\text{GeV}$)	0.03613	0.03644	0.03644	0 %
N_{SK} (1 μ -like ring): ν_e all ($4 \leq E_t < 30\text{GeV}$)	0.01889	0.0192	0.0192	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.0007554	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0005852	0.0007237	0.0007237	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	7.028e-05	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0002168	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.001766	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ all ($0 \leq E_t < 2.5\text{GeV}$)	0.005225	0.005338	0.005338	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ all ($2.5 \leq E_t < 30\text{GeV}$)	0.008161	0.008298	0.008298	0 %
N_{SK} (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.08302	0.1619 %
N_{SK} (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.03556	0.8165 %
N_{SK} (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.001956	0.3875 %
N_{SK} (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006862	2.173 %
N_{SK} (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.1212	0.3679 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($0 \leq E_t < 0.4\text{GeV}$)	0.001862	0.001811	0.001811	0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.01178	0.01191	0.01191	0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.0301	0.03129	0.03129	0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.03551	0.03652	0.03652	0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	0.0326	0.03309	0.03309	0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	0.004319	0.004798	0.005243	9.26 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.001024	0.001061	0.001061	0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.000191	0.0001771	0.0001771	0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	7.323e-05	7.676e-05	7.676e-05	0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($5 \leq E_t < 7\text{GeV}$)	3.281e-05	3.708e-05	3.708e-05	0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($7 \leq E_t < 30\text{GeV}$)	5.487e-06	6.152e-06	6.152e-06	0 %

Table 81: Effect of $f_{5,t,r}^{banff}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NS_K (1 μ -like ring)	59.41	58.37	59.12	1.295 %
NS_K (1 μ -like ring): ν_μ CCQE	33.28	30.29	30.56	0.9214 %
NS_K (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	17.31	2.243 %
NS_K (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.4076	1.962 %
NS_K (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	3.815	1.172 %
NS_K (1 μ -like ring): ν_μ CC all	52.19	51.39	52.1	1.383 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.646	1.255 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.491	1.672 %
NS_K (1 μ -like ring): ν_μ NC all	3.218	3.092	3.137	1.453 %
NS_K (1 μ -like ring): ν_μ all ($0 \leq E_t < 0.4\text{GeV}$)	4.38	4.212	4.212	0 %
NS_K (1 μ -like ring): ν_μ all ($0.4 \leq E_t < 0.5\text{GeV}$)	3.276	3.209	3.209	0 %
NS_K (1 μ -like ring): ν_μ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.5893	0.5811	0.5811	0 %
NS_K (1 μ -like ring): ν_μ all ($0.6 \leq E_t < 0.7\text{GeV}$)	1.578	1.54	1.54	0 %
NS_K (1 μ -like ring): ν_μ all ($0.7 \leq E_t < 1\text{GeV}$)	10.46	9.917	9.917	0 %
NS_K (1 μ -like ring): ν_μ all ($1 \leq E_t < 1.5\text{GeV}$)	9.362	9.414	9.414	0 %
NS_K (1 μ -like ring): ν_μ all ($1.5 \leq E_t < 2.5\text{GeV}$)	9.824	9.316	10.07	8.113 %
NS_K (1 μ -like ring): ν_μ all ($2.5 \leq E_t < 3.5\text{GeV}$)	6.285	5.575	5.575	0 %
NS_K (1 μ -like ring): ν_μ all ($3.5 \leq E_t < 5\text{GeV}$)	6.729	7.556	7.556	0 %
NS_K (1 μ -like ring): ν_μ all ($5 \leq E_t < 7\text{GeV}$)	2.408	2.62	2.62	0 %
NS_K (1 μ -like ring): ν_μ all ($7 \leq E_t < 30\text{GeV}$)	0.5198	0.5386	0.5386	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	2.191	1.891	1.891	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.033	1.228	1.228	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1084	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.22	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.448	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC all	0.1716	0.168	0.168	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($0 \leq E_t < 0.4\text{GeV}$)	0.1056	0.09981	0.09981	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.04076	0.03888	0.03888	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.005182	0.005009	0.005009	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.01328	0.01312	0.01312	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($0.7 \leq E_t < 1\text{GeV}$)	0.2604	0.2585	0.2585	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($1 \leq E_t < 1.5\text{GeV}$)	0.8119	0.8223	0.8223	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($1.5 \leq E_t < 2.5\text{GeV}$)	1.292	1.184	1.184	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.6451	0.5646	0.5646	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($3.5 \leq E_t < 5\text{GeV}$)	0.3945	0.4515	0.4515	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($5 \leq E_t < 7\text{GeV}$)	0.1361	0.1492	0.1492	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($7 \leq E_t < 30\text{GeV}$)	0.02811	0.02864	0.02864	0 %
NS_K (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01507	0 %
NS_K (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.01243	0 %
NS_K (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004036	0 %
NS_K (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003007	0 %
NS_K (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.0309	0 %
NS_K (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %
NS_K (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %
NS_K (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %
NS_K (1 μ -like ring): ν_e all ($0 \leq E_t < 0.5\text{GeV}$)	0.004149	0.004058	0.004058	0 %
NS_K (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.7\text{GeV}$)	0.006751	0.007069	0.007069	0 %
NS_K (1 μ -like ring): ν_e all ($0.7 \leq E_t < 0.8\text{GeV}$)	0.003714	0.004002	0.004002	0 %
NS_K (1 μ -like ring): ν_e all ($0.8 \leq E_t < 1.5\text{GeV}$)	0.02648	0.02808	0.02808	0 %
NS_K (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.03854	0.03916	0.03916	0 %
NS_K (1 μ -like ring): ν_e all ($2.5 \leq E_t < 4\text{GeV}$)	0.03613	0.03644	0.03644	0 %
NS_K (1 μ -like ring): ν_e all ($4 \leq E_t < 30\text{GeV}$)	0.01889	0.0192	0.0192	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.0007554	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0005852	0.0007237	0.0007237	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	7.028e-05	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0002168	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.001766	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ all ($0 \leq E_t < 2.5\text{GeV}$)	0.005225	0.005338	0.005338	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ all ($2.5 \leq E_t < 30\text{GeV}$)	0.008161	0.008298	0.008298	0 %
NS_K (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.0829	0.02133 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.03532	0.1449 %
NS_K (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.00195	0.08788 %
NS_K (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006872	2.323 %
NS_K (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.1209	0.07129 %
NS_K (1 μ -like ring): oscillation ν_e all ($0 \leq E_t < 0.4\text{GeV}$)	0.001862	0.001811	0.001811	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.01178	0.01191	0.01191	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.0301	0.03129	0.03129	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.03551	0.03652	0.03652	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	0.0326	0.03309	0.03309	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	0.004319	0.004798	0.004798	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.001024	0.001061	0.001147	8.113 %
NS_K (1 μ -like ring): oscillation ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.000191	0.0001771	0.0001771	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	7.323e-05	7.676e-05	7.676e-05	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($5 \leq E_t < 7\text{GeV}$)	3.281e-05	3.708e-05	3.708e-05	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($7 \leq E_t < 30\text{GeV}$)	5.487e-06	6.152e-06	6.152e-06	0 %

Table 82: Effect of $f_{6;t,r}^{bandff}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NS_K (1 μ -like ring)	59.41	58.37	58.77 0.6953 %	57.96 -0.6953 %
NS_K (1 μ -like ring): ν_μ CCQE	33.28	30.29	30.41 0.4119 %	30.16 -0.4119 %
NS_K (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	17.12 1.132 %	16.74 -1.132 %
NS_K (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.4049 1.296 %	0.3945 -1.296 %
NS_K (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	3.826 1.461 %	3.716 -1.461 %
NS_K (1 μ -like ring): ν_μ CC all	52.19	51.39	51.76 0.733 %	51.01 -0.733 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.636 0.6523 %	1.615 -0.6523 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.485 1.262 %	1.448 -1.262 %
NS_K (1 μ -like ring): ν_μ NC all	3.218	3.092	3.121 0.9416 %	3.063 -0.9416 %
NS_K (1 μ -like ring): ν_μ all ($0 \leq E_t < 0.4\text{GeV}$)	4.38	4.212	4.212 0 %	4.212 0 %
NS_K (1 μ -like ring): ν_μ all ($0.4 \leq E_t < 0.5\text{GeV}$)	3.276	3.209	3.209 0 %	3.209 0 %
NS_K (1 μ -like ring): ν_μ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.5893	0.5811	0.5811 0 %	0.5811 0 %
NS_K (1 μ -like ring): ν_μ all ($0.6 \leq E_t < 0.7\text{GeV}$)	1.578	1.54	1.54 0 %	1.54 0 %
NS_K (1 μ -like ring): ν_μ all ($0.7 \leq E_t < 1\text{GeV}$)	10.46	9.917	9.917 0 %	9.917 0 %
NS_K (1 μ -like ring): ν_μ all ($1 \leq E_t < 1.5\text{GeV}$)	9.362	9.414	9.414 0 %	9.414 0 %
NS_K (1 μ -like ring): ν_μ all ($1.5 \leq E_t < 2.5\text{GeV}$)	9.824	9.316	9.316 0 %	9.316 0 %
NS_K (1 μ -like ring): ν_μ all ($2.5 \leq E_t < 3.5\text{GeV}$)	6.285	5.575	5.981 7.279 %	5.169 -7.279 %
NS_K (1 μ -like ring): ν_μ all ($3.5 \leq E_t < 5\text{GeV}$)	6.729	7.556	7.556 0 %	7.556 0 %
NS_K (1 μ -like ring): ν_μ all ($5 \leq E_t < 7\text{GeV}$)	2.408	2.62	2.62 0 %	2.62 0 %
NS_K (1 μ -like ring): ν_μ all ($7 \leq E_t < 30\text{GeV}$)	0.5198	0.5386	0.5386 0 %	0.5386 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	2.191	1.891	1.891 0 %	1.891 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.033	1.228	1.228 0 %	1.228 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1084 0 %	0.1084 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.22 0 %	0.22 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.448 0 %	3.448 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042 0 %	0.09042 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761 0 %	0.07761 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168 0 %	0.168 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0 \leq E_t < 0.4\text{GeV}$)	0.1056	0.09981	0.09981 0 %	0.09981 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.04076	0.03888	0.03888 0 %	0.03888 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.005182	0.005009	0.005009 0 %	0.005009 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.01328	0.01312	0.01312 0 %	0.01312 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.7 \leq E_t < 1\text{GeV}$)	0.2604	0.2585	0.2585 0 %	0.2585 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($1 \leq E_t < 1.5\text{GeV}$)	0.8119	0.8223	0.8223 0 %	0.8223 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($1.5 \leq E_t < 2.5\text{GeV}$)	1.292	1.184	1.184 0 %	1.184 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.6451	0.5646	0.5646 0 %	0.5646 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($3.5 \leq E_t < 5\text{GeV}$)	0.3945	0.4515	0.4515 0 %	0.4515 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($5 \leq E_t < 7\text{GeV}$)	0.1361	0.1492	0.1492 0 %	0.1492 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($7 \leq E_t < 30\text{GeV}$)	0.02811	0.02864	0.02864 0 %	0.02864 0 %
NS_K (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01507 0 %	0.01507 0 %
NS_K (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.01243 0 %	0.01243 0 %
NS_K (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004036 0 %	0.0004036 0 %
NS_K (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003007 0 %	0.003007 0 %
NS_K (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.0309 0 %	0.0309 0 %
NS_K (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942 0 %	0.04942 0 %
NS_K (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768 0 %	0.05768 0 %
NS_K (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071 0 %	0.1071 0 %
NS_K (1 μ -like ring): ν_e all ($0 \leq E_t < 0.5\text{GeV}$)	0.004149	0.004058	0.004058 0 %	0.004058 0 %
NS_K (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.7\text{GeV}$)	0.006751	0.007069	0.007069 0 %	0.007069 0 %
NS_K (1 μ -like ring): ν_e all ($0.7 \leq E_t < 0.8\text{GeV}$)	0.003714	0.004002	0.004002 0 %	0.004002 0 %
NS_K (1 μ -like ring): ν_e all ($0.8 \leq E_t < 1.5\text{GeV}$)	0.02648	0.02808	0.02808 0 %	0.02808 0 %
NS_K (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.03854	0.03916	0.03916 0 %	0.03916 0 %
NS_K (1 μ -like ring): ν_e all ($2.5 \leq E_t < 4\text{GeV}$)	0.03613	0.03644	0.03644 0 %	0.03644 0 %
NS_K (1 μ -like ring): ν_e all ($4 \leq E_t < 30\text{GeV}$)	0.01889	0.0192	0.0192 0 %	0.0192 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.0007554 0 %	0.0007554 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0005852	0.0007237	0.0007237 0 %	0.0007237 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	7.028e-05 0 %	7.028e-05 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0002168 0 %	0.0002168 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.001766 0 %	0.001766 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916 0 %	0.005916 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954 0 %	0.005954 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187 0 %	0.01187 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ all ($0 \leq E_t < 2.5\text{GeV}$)	0.005225	0.005338	0.005338 0 %	0.005338 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ all ($2.5 \leq E_t < 30\text{GeV}$)	0.008161	0.008298	0.008298 0 %	0.008298 0 %
NS_K (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.08288 0.002569 %	0.08288 -0.002569 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.03527 0.01036 %	0.03527 -0.01036 %
NS_K (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.001949 0.03316 %	0.001948 -0.03316 %
NS_K (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006781 0.9627 %	0.0006651 -0.9627 %
NS_K (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.1208 0.01068 %	0.1208 -0.01068 %
NS_K (1 μ -like ring): oscillation ν_e all ($0 \leq E_t < 0.4\text{GeV}$)	0.001862	0.001811	0.001811 0 %	0.001811 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.01178	0.01191	0.01191 0 %	0.01191 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.0301	0.03129	0.03129 0 %	0.03129 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.03551	0.03652	0.03652 0 %	0.03652 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	0.0326	0.03309	0.03309 0 %	0.03309 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	0.004319	0.004798	0.004798 0 %	0.004798 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.001024	0.001061	0.001061 0 %	0.001061 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.000191	0.0001771	0.0001771 7.279 %	0.0001642 -7.279 %
NS_K (1 μ -like ring): oscillation ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	7.323e-05	7.676e-05	7.676e-05 0 %	7.676e-05 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($5 \leq E_t < 7\text{GeV}$)	3.281e-05	3.708e-05	3.708e-05 0 %	3.708e-05 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($7 \leq E_t < 30\text{GeV}$)	5.487e-06	6.152e-06	6.152e-06 0 %	6.152e-06 0 %

Table 83: Effect of $f_{7;t,r}^{banff}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NS_K (1 μ -like ring)	59.41	58.37	59	1.082 %
NS_K (1 μ -like ring): ν_μ CCQE	33.28	30.29	30.51	0.7511 %
NS_K (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	17.17	1.434 %
NS_K (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.407	1.827 %
NS_K (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	3.88	2.893 %
NS_K (1 μ -like ring): ν_μ CC all	52.19	51.39	51.97	1.142 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.644	1.11 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.494	1.848 %
NS_K (1 μ -like ring): ν_μ NC all	3.218	3.092	3.137	1.46 %
NS_K (1 μ -like ring): ν_μ all ($0 \leq E_t < 0.4\text{GeV}$)	4.38	4.212	4.212	0 %
NS_K (1 μ -like ring): ν_μ all ($0.4 \leq E_t < 0.5\text{GeV}$)	3.276	3.209	3.209	0 %
NS_K (1 μ -like ring): ν_μ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.5893	0.5811	0.5811	0 %
NS_K (1 μ -like ring): ν_μ all ($0.6 \leq E_t < 0.7\text{GeV}$)	1.578	1.54	1.54	0 %
NS_K (1 μ -like ring): ν_μ all ($0.7 \leq E_t < 1\text{GeV}$)	10.46	9.917	9.917	0 %
NS_K (1 μ -like ring): ν_μ all ($1 \leq E_t < 1.5\text{GeV}$)	9.362	9.414	9.414	0 %
NS_K (1 μ -like ring): ν_μ all ($1.5 \leq E_t < 2.5\text{GeV}$)	9.824	9.316	9.316	0 %
NS_K (1 μ -like ring): ν_μ all ($2.5 \leq E_t < 3.5\text{GeV}$)	6.285	5.575	5.575	0 %
NS_K (1 μ -like ring): ν_μ all ($3.5 \leq E_t < 5\text{GeV}$)	6.729	7.556	8.188	8.362 %
NS_K (1 μ -like ring): ν_μ all ($5 \leq E_t < 7\text{GeV}$)	2.408	2.62	2.62	0 %
NS_K (1 μ -like ring): ν_μ all ($7 \leq E_t < 30\text{GeV}$)	0.5198	0.5386	0.5386	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	2.191	1.891	1.891	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.033	1.228	1.228	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1084	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.22	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.448	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0 \leq E_t < 0.4\text{GeV}$)	0.1056	0.09981	0.09981	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.04076	0.03888	0.03888	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.005182	0.005009	0.005009	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.01328	0.01312	0.01312	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.7 \leq E_t < 1\text{GeV}$)	0.2604	0.2585	0.2585	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($1 \leq E_t < 1.5\text{GeV}$)	0.8119	0.8223	0.8223	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($1.5 \leq E_t < 2.5\text{GeV}$)	1.292	1.184	1.184	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.6451	0.5646	0.5646	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($3.5 \leq E_t < 5\text{GeV}$)	0.3945	0.4515	0.4515	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($5 \leq E_t < 7\text{GeV}$)	0.1361	0.1492	0.1492	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($7 \leq E_t < 30\text{GeV}$)	0.02811	0.02864	0.02864	0 %
NS_K (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01507	0 %
NS_K (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.01243	0 %
NS_K (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004036	0 %
NS_K (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003007	0 %
NS_K (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.0309	0 %
NS_K (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %
NS_K (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %
NS_K (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %
NS_K (1 μ -like ring): ν_e all ($0 \leq E_t < 0.5\text{GeV}$)	0.004149	0.004058	0.004058	0 %
NS_K (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.7\text{GeV}$)	0.006751	0.007069	0.007069	0 %
NS_K (1 μ -like ring): ν_e all ($0.7 \leq E_t < 0.8\text{GeV}$)	0.003714	0.004002	0.004002	0 %
NS_K (1 μ -like ring): ν_e all ($0.8 \leq E_t < 1.5\text{GeV}$)	0.02648	0.02808	0.02808	0 %
NS_K (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.03854	0.03916	0.03916	0 %
NS_K (1 μ -like ring): ν_e all ($2.5 \leq E_t < 4\text{GeV}$)	0.03613	0.03644	0.03644	0 %
NS_K (1 μ -like ring): ν_e all ($4 \leq E_t < 30\text{GeV}$)	0.01889	0.0192	0.0192	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.0007554	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0005852	0.0007237	0.0007237	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	7.028e-05	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0002168	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.001766	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ all ($0 \leq E_t < 2.5\text{GeV}$)	0.005225	0.005338	0.005338	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ all ($2.5 \leq E_t < 30\text{GeV}$)	0.008161	0.008298	0.008298	0 %
NS_K (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.08288	0.001208 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.03527	0.006287 %
NS_K (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.001949	0 %
NS_K (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006748	0.4766 %
NS_K (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.1208	0.005135 %
NS_K (1 μ -like ring): oscillation ν_e all ($0 \leq E_t < 0.4\text{GeV}$)	0.001862	0.001811	0.001811	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.01178	0.01191	0.01191	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.0301	0.03129	0.03129	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.03551	0.03652	0.03652	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	0.0326	0.03309	0.03309	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	0.004319	0.004798	0.004798	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.001024	0.001061	0.001061	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.000191	0.0001771	0.0001771	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	7.323e-05	7.676e-05	8.318e-05	8.362 %
NS_K (1 μ -like ring): oscillation ν_e all ($5 \leq E_t < 7\text{GeV}$)	3.281e-05	3.708e-05	3.708e-05	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($7 \leq E_t < 30\text{GeV}$)	5.487e-06	6.152e-06	6.152e-06	0 %

Table 84: Effect of $f_{8;t,r}^{banff}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
N_{SK} (1 μ -like ring)	59.41	58.37	58.65	0.4833 %
N_{SK} (1 μ -like ring): ν_μ CCQE	33.28	30.29	30.35	0.2171 %
N_{SK} (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	17.03	0.604 %
N_{SK} (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.4029	0.8002 %
N_{SK} (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	3.854	2.196 %
N_{SK} (1 μ -like ring): ν_μ CC all	52.19	51.39	51.64	0.4943 %
N_{SK} (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.635	0.6108 %
N_{SK} (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.485	1.237 %
N_{SK} (1 μ -like ring): ν_μ NC all	3.218	3.092	3.12	0.908 %
N_{SK} (1 μ -like ring): ν_μ all ($0 \leq E_t < 0.4\text{GeV}$)	4.38	4.212	4.212	0 %
N_{SK} (1 μ -like ring): ν_μ all ($0.4 \leq E_t < 0.5\text{GeV}$)	3.276	3.209	3.209	0 %
N_{SK} (1 μ -like ring): ν_μ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.5893	0.5811	0.5811	0 %
N_{SK} (1 μ -like ring): ν_μ all ($0.6 \leq E_t < 0.7\text{GeV}$)	1.578	1.54	1.54	0 %
N_{SK} (1 μ -like ring): ν_μ all ($0.7 \leq E_t < 1\text{GeV}$)	10.46	9.917	9.917	0 %
N_{SK} (1 μ -like ring): ν_μ all ($1 \leq E_t < 1.5\text{GeV}$)	9.362	9.414	9.414	0 %
N_{SK} (1 μ -like ring): ν_μ all ($1.5 \leq E_t < 2.5\text{GeV}$)	9.824	9.316	9.316	0 %
N_{SK} (1 μ -like ring): ν_μ all ($2.5 \leq E_t < 3.5\text{GeV}$)	6.285	5.575	5.575	0 %
N_{SK} (1 μ -like ring): ν_μ all ($3.5 \leq E_t < 5\text{GeV}$)	6.729	7.556	7.556	0 %
N_{SK} (1 μ -like ring): ν_μ all ($5 \leq E_t < 7\text{GeV}$)	2.408	2.62	2.902	10.77 %
N_{SK} (1 μ -like ring): ν_μ all ($7 \leq E_t < 30\text{GeV}$)	0.5198	0.5386	0.5386	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	2.191	1.891	1.891	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.033	1.228	1.228	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1084	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.22	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.448	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0 \leq E_t < 0.4\text{GeV}$)	0.1056	0.09981	0.09981	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.04076	0.03888	0.03888	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.005182	0.005009	0.005009	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.01328	0.01312	0.01312	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.7 \leq E_t < 1\text{GeV}$)	0.2604	0.2585	0.2585	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($1 \leq E_t < 1.5\text{GeV}$)	0.8119	0.8223	0.8223	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($1.5 \leq E_t < 2.5\text{GeV}$)	1.292	1.184	1.184	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.6451	0.5646	0.5646	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($3.5 \leq E_t < 5\text{GeV}$)	0.3945	0.4515	0.4515	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($5 \leq E_t < 7\text{GeV}$)	0.1361	0.1492	0.1492	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($7 \leq E_t < 30\text{GeV}$)	0.02811	0.02864	0.02864	0 %
N_{SK} (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01507	0 %
N_{SK} (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.01243	0 %
N_{SK} (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004036	0 %
N_{SK} (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003007	0 %
N_{SK} (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.0309	0 %
N_{SK} (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %
N_{SK} (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %
N_{SK} (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %
N_{SK} (1 μ -like ring): ν_e all ($0 \leq E_t < 0.5\text{GeV}$)	0.004149	0.004058	0.004058	0 %
N_{SK} (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.7\text{GeV}$)	0.006751	0.007069	0.007069	0 %
N_{SK} (1 μ -like ring): ν_e all ($0.7 \leq E_t < 0.8\text{GeV}$)	0.003714	0.004002	0.004002	0 %
N_{SK} (1 μ -like ring): ν_e all ($0.8 \leq E_t < 1.5\text{GeV}$)	0.02648	0.02808	0.02808	0 %
N_{SK} (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.03854	0.03916	0.03916	0 %
N_{SK} (1 μ -like ring): ν_e all ($2.5 \leq E_t < 4\text{GeV}$)	0.03613	0.03644	0.03644	0 %
N_{SK} (1 μ -like ring): ν_e all ($4 \leq E_t < 30\text{GeV}$)	0.01889	0.0192	0.0192	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.0007554	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0005852	0.0007237	0.0007237	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	7.028e-05	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0002168	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.001766	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ all ($0 \leq E_t < 2.5\text{GeV}$)	0.005225	0.005338	0.005338	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ all ($2.5 \leq E_t < 30\text{GeV}$)	0.008161	0.008298	0.008298	0 %
N_{SK} (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.08288	0.001879 %
N_{SK} (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.03527	0.001583 %
N_{SK} (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.001949	0.001948 %
N_{SK} (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006732	0.2415 %
N_{SK} (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.1208	0.003306 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($0 \leq E_t < 0.4\text{GeV}$)	0.001862	0.001811	0.001811	0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.01178	0.01191	0.01191	0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.0301	0.03129	0.03129	0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.03551	0.03652	0.03652	0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	0.0326	0.03309	0.03309	0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	0.004319	0.004798	0.004798	0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.001024	0.001061	0.001061	0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.000191	0.0001771	0.0001771	0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	7.323e-05	7.676e-05	7.676e-05	0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($5 \leq E_t < 7\text{GeV}$)	3.281e-05	3.708e-05	4.108e-05	10.77 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($7 \leq E_t < 30\text{GeV}$)	5.487e-06	6.152e-06	6.152e-06	0 %

Table 85: Effect of $f_{9;t,r}^{banff}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NS_K (1 μ -like ring)	59.41	58.37	58.44	0.1303 %
NS_K (1 μ -like ring): ν_μ CCQE	33.28	30.29	30.29	0.01625 %
NS_K (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	16.95	0.08816 %
NS_K (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.4001	0.0986 %
NS_K (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	3.806	0.9139 %
NS_K (1 μ -like ring): ν_μ CC all	52.19	51.39	51.44	0.1065 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.633	0.458 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.48	0.9469 %
NS_K (1 μ -like ring): ν_μ NC all	3.218	3.092	3.113	0.6899 %
NS_K (1 μ -like ring): ν_μ all ($0 \leq E_t < 0.4\text{GeV}$)	4.38	4.212	4.212	0 %
NS_K (1 μ -like ring): ν_μ all ($0.4 \leq E_t < 0.5\text{GeV}$)	3.276	3.209	3.209	0 %
NS_K (1 μ -like ring): ν_μ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.5893	0.5811	0.5811	0 %
NS_K (1 μ -like ring): ν_μ all ($0.6 \leq E_t < 0.7\text{GeV}$)	1.578	1.54	1.54	0 %
NS_K (1 μ -like ring): ν_μ all ($0.7 \leq E_t < 1\text{GeV}$)	10.46	9.917	9.917	0 %
NS_K (1 μ -like ring): ν_μ all ($1 \leq E_t < 1.5\text{GeV}$)	9.362	9.414	9.414	0 %
NS_K (1 μ -like ring): ν_μ all ($1.5 \leq E_t < 2.5\text{GeV}$)	9.824	9.316	9.316	0 %
NS_K (1 μ -like ring): ν_μ all ($2.5 \leq E_t < 3.5\text{GeV}$)	6.285	5.575	5.575	0 %
NS_K (1 μ -like ring): ν_μ all ($3.5 \leq E_t < 5\text{GeV}$)	6.729	7.556	7.556	0 %
NS_K (1 μ -like ring): ν_μ all ($5 \leq E_t < 7\text{GeV}$)	2.408	2.62	2.62	0 %
NS_K (1 μ -like ring): ν_μ all ($7 \leq E_t < 30\text{GeV}$)	0.5198	0.5386	0.6146	14.12 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	2.191	1.891	1.891	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.033	1.228	1.228	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1084	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.22	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.448	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0 \leq E_t < 0.4\text{GeV}$)	0.1056	0.09981	0.09981	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.04076	0.03888	0.03888	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.005182	0.005009	0.005009	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.01328	0.01312	0.01312	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.7 \leq E_t < 1\text{GeV}$)	0.2604	0.2585	0.2585	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($1 \leq E_t < 1.5\text{GeV}$)	0.8119	0.8223	0.8223	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($1.5 \leq E_t < 2.5\text{GeV}$)	1.292	1.184	1.184	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.6451	0.5646	0.5646	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($3.5 \leq E_t < 5\text{GeV}$)	0.3945	0.4515	0.4515	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($5 \leq E_t < 7\text{GeV}$)	0.1361	0.1492	0.1492	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($7 \leq E_t < 30\text{GeV}$)	0.02811	0.02864	0.02864	0 %
NS_K (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01507	0 %
NS_K (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.01243	0 %
NS_K (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004036	0 %
NS_K (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003007	0 %
NS_K (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.0309	0 %
NS_K (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %
NS_K (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %
NS_K (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %
NS_K (1 μ -like ring): ν_e all ($0 \leq E_t < 0.5\text{GeV}$)	0.004149	0.004058	0.004058	0 %
NS_K (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.7\text{GeV}$)	0.006751	0.007069	0.007069	0 %
NS_K (1 μ -like ring): ν_e all ($0.7 \leq E_t < 0.8\text{GeV}$)	0.003714	0.004002	0.004002	0 %
NS_K (1 μ -like ring): ν_e all ($0.8 \leq E_t < 1.5\text{GeV}$)	0.02648	0.02808	0.02808	0 %
NS_K (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.03854	0.03916	0.03916	0 %
NS_K (1 μ -like ring): ν_e all ($2.5 \leq E_t < 4\text{GeV}$)	0.03613	0.03644	0.03644	0 %
NS_K (1 μ -like ring): ν_e all ($4 \leq E_t < 30\text{GeV}$)	0.01889	0.0192	0.0192	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.0007554	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0005852	0.0007237	0.0007237	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	7.028e-05	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0002168	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.001766	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ all ($0 \leq E_t < 2.5\text{GeV}$)	0.005225	0.005338	0.005338	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ all ($2.5 \leq E_t < 30\text{GeV}$)	0.008161	0.008298	0.008298	0 %
NS_K (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.08288	0.0003308 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.03527	0.001054 %
NS_K (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.001949	0 %
NS_K (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006716	-0.03317 %
NS_K (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.1208	0.0007191 %
NS_K (1 μ -like ring): oscillation ν_e all ($0 \leq E_t < 0.4\text{GeV}$)	0.001862	0.001811	0.001811	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.01178	0.01191	0.01191	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.0301	0.03129	0.03129	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.03551	0.03652	0.03652	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	0.0326	0.03309	0.03309	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	0.004319	0.004798	0.004798	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.001024	0.001061	0.001061	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.000191	0.0001771	0.0001771	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	7.323e-05	7.676e-05	7.676e-05	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($5 \leq E_t < 7\text{GeV}$)	3.281e-05	3.708e-05	3.708e-05	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($7 \leq E_t < 30\text{GeV}$)	5.487e-06	6.152e-06	7.02e-06	14.12 %
				5.283e-06
				-14.12 %

Table 86: Effect of $f_{10;t,r}^{banff}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
N_{SK} (1 μ -like ring)	59.41	58.37	58.39 0.02962 %	58.35 -0.02962 %
N_{SK} (1 μ -like ring): ν_μ CCQE	33.28	30.29	30.29 0 %	30.29 0 %
N_{SK} (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	16.93 0 %	16.93 0 %
N_{SK} (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.3997 0 %	0.3997 0 %
N_{SK} (1 μ -like ring): ν_μ CC other (ν_μ disap)	3.862	3.771	3.771 0 %	3.771 0 %
N_{SK} (1 μ -like ring): ν_μ CC all	52.19	51.39	51.39 0 %	51.39 0 %
N_{SK} (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625 0 %	1.625 0 %
N_{SK} (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466 0 %	1.466 0 %
N_{SK} (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092 0 %	3.092 0 %
N_{SK} (1 μ -like ring): ν_μ all ($0 \leq E_t < 0.4\text{GeV}$)	4.38	4.212	4.212 0 %	4.212 0 %
N_{SK} (1 μ -like ring): ν_μ all ($0.4 \leq E_t < 0.5\text{GeV}$)	3.276	3.209	3.209 0 %	3.209 0 %
N_{SK} (1 μ -like ring): ν_μ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.5893	0.5811	0.5811 0 %	0.5811 0 %
N_{SK} (1 μ -like ring): ν_μ all ($0.6 \leq E_t < 0.7\text{GeV}$)	1.578	1.54	1.54 0 %	1.54 0 %
N_{SK} (1 μ -like ring): ν_μ all ($0.7 \leq E_t < 1\text{GeV}$)	10.46	9.917	9.917 0 %	9.917 0 %
N_{SK} (1 μ -like ring): ν_μ all ($1 \leq E_t < 1.5\text{GeV}$)	9.362	9.414	9.414 0 %	9.414 0 %
N_{SK} (1 μ -like ring): ν_μ all ($1.5 \leq E_t < 2.5\text{GeV}$)	9.824	9.316	9.316 0 %	9.316 0 %
N_{SK} (1 μ -like ring): ν_μ all ($2.5 \leq E_t < 3.5\text{GeV}$)	6.285	5.575	5.575 0 %	5.575 0 %
N_{SK} (1 μ -like ring): ν_μ all ($3.5 \leq E_t < 5\text{GeV}$)	6.729	7.556	7.556 0 %	7.556 0 %
N_{SK} (1 μ -like ring): ν_μ all ($5 \leq E_t < 7\text{GeV}$)	2.408	2.62	2.62 0 %	2.62 0 %
N_{SK} (1 μ -like ring): ν_μ all ($7 \leq E_t < 30\text{GeV}$)	0.5198	0.5386	0.5386 0 %	0.5386 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	2.191	1.891	1.908 0.8853 %	1.874 -0.8853 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.033	1.228	1.228 0.01074 %	1.228 -0.01074 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1086 0.1181 %	0.1083 -0.1181 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disap)	0.2251	0.22	0.22 0 %	0.22 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.465 0.4932 %	3.431 -0.4932 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09066 0.265 %	0.09018 -0.265 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07766 0.06249 %	0.07757 -0.06249 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.1683 0.1715 %	0.1677 -0.1715 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0 \leq E_t < 0.4\text{GeV}$)	0.1056	0.09981	0.1108 11.03 %	0.08881 -11.03 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.04076	0.03888	0.04316 11.03 %	0.03459 -11.03 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.005182	0.005009	0.005562 11.03 %	0.004457 -11.03 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.01328	0.01312	0.01456 11.03 %	0.01167 -11.03 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.7 \leq E_t < 1\text{GeV}$)	0.2604	0.2585	0.2585 0 %	0.2585 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($1 \leq E_t < 1.5\text{GeV}$)	0.8119	0.8223	0.8223 0 %	0.8223 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($1.5 \leq E_t < 2.5\text{GeV}$)	1.292	1.184	1.184 0 %	1.184 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.6451	0.5646	0.5646 0 %	0.5646 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($3.5 \leq E_t < 5\text{GeV}$)	0.3945	0.4515	0.4515 0 %	0.4515 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($5 \leq E_t < 7\text{GeV}$)	0.1361	0.1492	0.1492 0 %	0.1492 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($7 \leq E_t < 30\text{GeV}$)	0.02811	0.02864	0.02864 0 %	0.02864 0 %
N_{SK} (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01507 0 %	0.01507 0 %
N_{SK} (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.01243 0 %	0.01243 0 %
N_{SK} (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004036 0 %	0.0004036 0 %
N_{SK} (1 μ -like ring): ν_e CC other (ν_μ disap)	0.003005	0.003007	0.003007 0 %	0.003007 0 %
N_{SK} (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.0309 0 %	0.0309 0 %
N_{SK} (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942 0 %	0.04942 0 %
N_{SK} (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768 0 %	0.05768 0 %
N_{SK} (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071 0 %	0.1071 0 %
N_{SK} (1 μ -like ring): ν_e all ($0 \leq E_t < 0.5\text{GeV}$)	0.004149	0.004058	0.004058 0 %	0.004058 0 %
N_{SK} (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.7\text{GeV}$)	0.006751	0.007069	0.007069 0 %	0.007069 0 %
N_{SK} (1 μ -like ring): ν_e all ($0.7 \leq E_t < 0.8\text{GeV}$)	0.003714	0.004002	0.004002 0 %	0.004002 0 %
N_{SK} (1 μ -like ring): ν_e all ($0.8 \leq E_t < 1.5\text{GeV}$)	0.02648	0.02808	0.02808 0 %	0.02808 0 %
N_{SK} (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.03854	0.03916	0.03916 0 %	0.03916 0 %
N_{SK} (1 μ -like ring): ν_e all ($2.5 \leq E_t < 4\text{GeV}$)	0.03613	0.03644	0.03644 0 %	0.03644 0 %
N_{SK} (1 μ -like ring): ν_e all ($4 \leq E_t < 30\text{GeV}$)	0.01889	0.0192	0.0192 0 %	0.0192 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.0007554 0 %	0.0007554 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0005852	0.0007237	0.0007237 0 %	0.0007237 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	7.028e-05 0 %	7.028e-05 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disap)	0.0002167	0.0002168	0.0002168 0 %	0.0002168 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.001766 0 %	0.001766 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916 0 %	0.005916 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954 0 %	0.005954 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187 0 %	0.01187 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ all ($0 \leq E_t < 2.5\text{GeV}$)	0.005225	0.005338	0.005338 0 %	0.005338 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ all ($2.5 \leq E_t < 30\text{GeV}$)	0.008161	0.008298	0.008298 0 %	0.008298 0 %
N_{SK} (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.08288 0 %	0.08288 0 %
N_{SK} (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.03527 0 %	0.03527 0 %
N_{SK} (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.001949 0 %	0.001949 0 %
N_{SK} (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006716 0 %	0.0006716 0 %
N_{SK} (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.1208 0 %	0.1208 0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($0 \leq E_t < 0.4\text{GeV}$)	0.001862	0.001811	0.001811 0 %	0.001811 0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.01178	0.01191	0.01191 0 %	0.01191 0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.0301	0.03129	0.03129 0 %	0.03129 0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.03551	0.03652	0.03652 0 %	0.03652 0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	0.0326	0.03309	0.03309 0 %	0.03309 0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	0.004319	0.004798	0.004798 0 %	0.004798 0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.001024	0.001061	0.001061 0 %	0.001061 0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.000191	0.0001771	0.0001771 0 %	0.0001771 0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	7.323e-05	7.676e-05	7.676e-05 0 %	7.676e-05 0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($5 \leq E_t < 7\text{GeV}$)	3.281e-05	3.708e-05	3.708e-05 0 %	3.708e-05 0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($7 \leq E_t < 30\text{GeV}$)	5.487e-06	6.152e-06	6.152e-06 0 %	6.152e-06 0 %

Table 87: Effect of $f_{11;t,r}^{banff}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
N_{SK} (1 μ -like ring)	59.41	58.37	58.39 0.0437 %	58.34 -0.0437 %
N_{SK} (1 μ -like ring): ν_μ CCQE	33.28	30.29	30.29 0 %	30.29 0 %
N_{SK} (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	16.93 0 %	16.93 0 %
N_{SK} (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.3997 0 %	0.3997 0 %
N_{SK} (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	3.771 0 %	3.771 0 %
N_{SK} (1 μ -like ring): ν_μ CC all	52.19	51.39	51.39 0 %	51.39 0 %
N_{SK} (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625 0 %	1.625 0 %
N_{SK} (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466 0 %	1.466 0 %
N_{SK} (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092 0 %	3.092 0 %
N_{SK} (1 μ -like ring): ν_μ all ($0 \leq E_t < 0.4\text{GeV}$)	4.38	4.212	4.212 0 %	4.212 0 %
N_{SK} (1 μ -like ring): ν_μ all ($0.4 \leq E_t < 0.5\text{GeV}$)	3.276	3.209	3.209 0 %	3.209 0 %
N_{SK} (1 μ -like ring): ν_μ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.5893	0.5811	0.5811 0 %	0.5811 0 %
N_{SK} (1 μ -like ring): ν_μ all ($0.6 \leq E_t < 0.7\text{GeV}$)	1.578	1.54	1.54 0 %	1.54 0 %
N_{SK} (1 μ -like ring): ν_μ all ($0.7 \leq E_t < 1\text{GeV}$)	10.46	9.917	9.917 0 %	9.917 0 %
N_{SK} (1 μ -like ring): ν_μ all ($1 \leq E_t < 1.5\text{GeV}$)	9.362	9.414	9.414 0 %	9.414 0 %
N_{SK} (1 μ -like ring): ν_μ all ($1.5 \leq E_t < 2.5\text{GeV}$)	9.824	9.316	9.316 0 %	9.316 0 %
N_{SK} (1 μ -like ring): ν_μ all ($2.5 \leq E_t < 3.5\text{GeV}$)	6.285	5.575	5.575 0 %	5.575 0 %
N_{SK} (1 μ -like ring): ν_μ all ($3.5 \leq E_t < 5\text{GeV}$)	6.729	7.556	7.556 0 %	7.556 0 %
N_{SK} (1 μ -like ring): ν_μ all ($5 \leq E_t < 7\text{GeV}$)	2.408	2.62	2.62 0 %	2.62 0 %
N_{SK} (1 μ -like ring): ν_μ all ($7 \leq E_t < 30\text{GeV}$)	0.5198	0.5386	0.5386 0 %	0.5386 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	2.191	1.891	1.91 1.015 %	1.872 -1.015 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.033	1.228	1.233 0.3667 %	1.223 -0.3667 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1093 0.8169 %	0.1076 -0.8169 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.2201 0.01781 %	0.22 -0.01781 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.472 0.714 %	3.423 -0.714 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09112 0.7694 %	0.08973 -0.7694 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07781 0.2482 %	0.07742 -0.2482 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.1689 0.5287 %	0.1671 -0.5287 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0 \leq E_t < 0.4\text{GeV}$)	0.1056	0.09981	0.09981 0 %	0.09981 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.04076	0.03888	0.03888 0 %	0.03888 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.005182	0.005009	0.005009 0 %	0.005009 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.01328	0.01312	0.01312 0 %	0.01312 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.7 \leq E_t < 1\text{GeV}$)	0.2604	0.2585	0.284 9.867 %	0.233 -9.867 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($1 \leq E_t < 1.5\text{GeV}$)	0.8119	0.8223	0.8223 0 %	0.8223 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($1.5 \leq E_t < 2.5\text{GeV}$)	1.292	1.184	1.184 0 %	1.184 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.6451	0.5646	0.5646 0 %	0.5646 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($3.5 \leq E_t < 5\text{GeV}$)	0.3945	0.4515	0.4515 0 %	0.4515 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($5 \leq E_t < 7\text{GeV}$)	0.1361	0.1492	0.1492 0 %	0.1492 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($7 \leq E_t < 30\text{GeV}$)	0.02811	0.02864	0.02864 0 %	0.02864 0 %
N_{SK} (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01507 0 %	0.01507 0 %
N_{SK} (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.01243 0 %	0.01243 0 %
N_{SK} (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004036 0 %	0.0004036 0 %
N_{SK} (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003007 0 %	0.003007 0 %
N_{SK} (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.0309 0 %	0.0309 0 %
N_{SK} (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942 0 %	0.04942 0 %
N_{SK} (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768 0 %	0.05768 0 %
N_{SK} (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071 0 %	0.1071 0 %
N_{SK} (1 μ -like ring): ν_e all ($0 \leq E_t < 0.5\text{GeV}$)	0.004149	0.004058	0.004058 0 %	0.004058 0 %
N_{SK} (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.7\text{GeV}$)	0.006751	0.007069	0.007069 0 %	0.007069 0 %
N_{SK} (1 μ -like ring): ν_e all ($0.7 \leq E_t < 0.8\text{GeV}$)	0.003714	0.004002	0.004002 0 %	0.004002 0 %
N_{SK} (1 μ -like ring): ν_e all ($0.8 \leq E_t < 1.5\text{GeV}$)	0.02648	0.02808	0.02808 0 %	0.02808 0 %
N_{SK} (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.03854	0.03916	0.03916 0 %	0.03916 0 %
N_{SK} (1 μ -like ring): ν_e all ($2.5 \leq E_t < 4\text{GeV}$)	0.03613	0.03644	0.03644 0 %	0.03644 0 %
N_{SK} (1 μ -like ring): ν_e all ($4 \leq E_t < 30\text{GeV}$)	0.01889	0.0192	0.0192 0 %	0.0192 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.0007554 0 %	0.0007554 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0005852	0.0007237	0.0007237 0 %	0.0007237 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	7.028e-05 0 %	7.028e-05 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0002168 0 %	0.0002168 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.001766 0 %	0.001766 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916 0 %	0.005916 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954 0 %	0.005954 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187 0 %	0.01187 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ all ($0 \leq E_t < 2.5\text{GeV}$)	0.005225	0.005338	0.005338 0 %	0.005338 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ all ($2.5 \leq E_t < 30\text{GeV}$)	0.008161	0.008298	0.008298 0 %	0.008298 0 %
N_{SK} (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.08288 0 %	0.08288 0 %
N_{SK} (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.03527 0 %	0.03527 0 %
N_{SK} (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.001949 0 %	0.001949 0 %
N_{SK} (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006716 0 %	0.0006716 0 %
N_{SK} (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.1208 0 %	0.1208 0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($0 \leq E_t < 0.4\text{GeV}$)	0.001862	0.001811	0.001811 0 %	0.001811 0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.01178	0.01191	0.01191 0 %	0.01191 0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.0301	0.03129	0.03129 0 %	0.03129 0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.03551	0.03652	0.03652 0 %	0.03652 0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	0.0326	0.03309	0.03309 0 %	0.03309 0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	0.004319	0.004798	0.004798 0 %	0.004798 0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.001024	0.001061	0.001061 0 %	0.001061 0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.000191	0.0001771	0.0001771 0 %	0.0001771 0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	7.323e-05	7.676e-05	7.676e-05 0 %	7.676e-05 0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($5 \leq E_t < 7\text{GeV}$)	3.281e-05	3.708e-05	3.708e-05 0 %	3.708e-05 0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($7 \leq E_t < 30\text{GeV}$)	5.487e-06	6.152e-06	6.152e-06 0 %	6.152e-06 0 %

Table 88: Effect of $f_{12;t,r}^{banff}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
N_{SK} (1 μ -like ring)	59.41	58.37	58.45	0.1456 %
N_{SK} (1 μ -like ring): ν_μ CCQE	33.28	30.29	30.29	0 %
N_{SK} (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	16.93	0 %
N_{SK} (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.3997	0 %
N_{SK} (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	3.771	0 %
N_{SK} (1 μ -like ring): ν_μ CC all	52.19	51.39	51.39	0 %
N_{SK} (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625	0 %
N_{SK} (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466	0 %
N_{SK} (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092	0 %
N_{SK} (1 μ -like ring): ν_μ all ($0 \leq E_t < 0.4\text{GeV}$)	4.38	4.212	4.212	0 %
N_{SK} (1 μ -like ring): ν_μ all ($0.4 \leq E_t < 0.5\text{GeV}$)	3.276	3.209	3.209	0 %
N_{SK} (1 μ -like ring): ν_μ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.5893	0.5811	0.5811	0 %
N_{SK} (1 μ -like ring): ν_μ all ($0.6 \leq E_t < 0.7\text{GeV}$)	1.578	1.54	1.54	0 %
N_{SK} (1 μ -like ring): ν_μ all ($0.7 \leq E_t < 1\text{GeV}$)	10.46	9.917	9.917	0 %
N_{SK} (1 μ -like ring): ν_μ all ($1 \leq E_t < 1.5\text{GeV}$)	9.362	9.414	9.414	0 %
N_{SK} (1 μ -like ring): ν_μ all ($1.5 \leq E_t < 2.5\text{GeV}$)	9.824	9.316	9.316	0 %
N_{SK} (1 μ -like ring): ν_μ all ($2.5 \leq E_t < 3.5\text{GeV}$)	6.285	5.575	5.575	0 %
N_{SK} (1 μ -like ring): ν_μ all ($3.5 \leq E_t < 5\text{GeV}$)	6.729	7.556	7.556	0 %
N_{SK} (1 μ -like ring): ν_μ all ($5 \leq E_t < 7\text{GeV}$)	2.408	2.62	2.62	0 %
N_{SK} (1 μ -like ring): ν_μ all ($7 \leq E_t < 30\text{GeV}$)	0.5198	0.5386	0.5386	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	2.191	1.891	1.947	2.951 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.033	1.228	1.251	1.859 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1114	2.717 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.2208	0.358 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.53	2.389 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09208	1.833 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07855	1.211 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.1706	1.546 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0 \leq E_t < 0.4\text{GeV}$)	0.1056	0.09981	0.09981	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.04076	0.03888	0.03888	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.005182	0.005009	0.005009	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.01328	0.01312	0.01312	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.7 \leq E_t < 1\text{GeV}$)	0.2604	0.2585	0.2585	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($1 \leq E_t < 1.5\text{GeV}$)	0.8119	0.8223	0.9073	10.33 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($1.5 \leq E_t < 2.5\text{GeV}$)	1.292	1.184	1.184	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.6451	0.5646	0.5646	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($3.5 \leq E_t < 5\text{GeV}$)	0.3945	0.4515	0.4515	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($5 \leq E_t < 7\text{GeV}$)	0.1361	0.1492	0.1492	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($7 \leq E_t < 30\text{GeV}$)	0.02811	0.02864	0.02864	0 %
N_{SK} (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01507	0 %
N_{SK} (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.01243	0 %
N_{SK} (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004036	0 %
N_{SK} (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003007	0 %
N_{SK} (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.0309	0 %
N_{SK} (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %
N_{SK} (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %
N_{SK} (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %
N_{SK} (1 μ -like ring): ν_e all ($0 \leq E_t < 0.5\text{GeV}$)	0.004149	0.004058	0.004058	0 %
N_{SK} (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.7\text{GeV}$)	0.006751	0.007069	0.007069	0 %
N_{SK} (1 μ -like ring): ν_e all ($0.7 \leq E_t < 0.8\text{GeV}$)	0.003714	0.004002	0.004002	0 %
N_{SK} (1 μ -like ring): ν_e all ($0.8 \leq E_t < 1.5\text{GeV}$)	0.02648	0.02808	0.02808	0 %
N_{SK} (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.03854	0.03916	0.03916	0 %
N_{SK} (1 μ -like ring): ν_e all ($2.5 \leq E_t < 4\text{GeV}$)	0.03613	0.03644	0.03644	0 %
N_{SK} (1 μ -like ring): ν_e all ($4 \leq E_t < 30\text{GeV}$)	0.01889	0.0192	0.0192	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.0007554	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0005852	0.0007237	0.0007237	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	7.028e-05	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0002168	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.001766	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ all ($0 \leq E_t < 2.5\text{GeV}$)	0.005225	0.005338	0.005338	0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ all ($2.5 \leq E_t < 30\text{GeV}$)	0.008161	0.008298	0.008298	0 %
N_{SK} (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.08288	0 %
N_{SK} (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.03527	0 %
N_{SK} (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.001949	0 %
N_{SK} (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006716	0 %
N_{SK} (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.1208	0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($0 \leq E_t < 0.4\text{GeV}$)	0.001862	0.001811	0.001811	0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.01178	0.01191	0.01191	0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.0301	0.03129	0.03129	0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.03551	0.03652	0.03652	0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	0.0326	0.03309	0.03309	0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	0.004319	0.004798	0.004798	0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.001024	0.001061	0.001061	0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.000191	0.0001771	0.0001771	0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	7.323e-05	7.676e-05	7.676e-05	0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($5 \leq E_t < 7\text{GeV}$)	3.281e-05	3.708e-05	3.708e-05	0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($7 \leq E_t < 30\text{GeV}$)	5.487e-06	6.152e-06	6.152e-06	0 %

Table 89: Effect of $f_{13;t,r}^{banff}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NS_K (1 μ -like ring)	59.41	58.37	58.5 0.2249 %	58.24 -0.2249 %
NS_K (1 μ -like ring): ν_μ CCQE	33.28	30.29	30.29 0 %	30.29 0 %
NS_K (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	16.93 0 %	16.93 0 %
NS_K (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.3997 0 %	0.3997 0 %
NS_K (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	3.771 0 %	3.771 0 %
NS_K (1 μ -like ring): ν_μ CC all	52.19	51.39	51.39 0 %	51.39 0 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625 0 %	1.625 0 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466 0 %	1.466 0 %
NS_K (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092 0 %	3.092 0 %
NS_K (1 μ -like ring): ν_μ all ($0 \leq E_t < 0.4\text{GeV}$)	4.38	4.212	4.212 0 %	4.212 0 %
NS_K (1 μ -like ring): ν_μ all ($0.4 \leq E_t < 0.5\text{GeV}$)	3.276	3.209	3.209 0 %	3.209 0 %
NS_K (1 μ -like ring): ν_μ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.5893	0.5811	0.5811 0 %	0.5811 0 %
NS_K (1 μ -like ring): ν_μ all ($0.6 \leq E_t < 0.7\text{GeV}$)	1.578	1.54	1.54 0 %	1.54 0 %
NS_K (1 μ -like ring): ν_μ all ($0.7 \leq E_t < 1\text{GeV}$)	10.46	9.917	9.917 0 %	9.917 0 %
NS_K (1 μ -like ring): ν_μ all ($1 \leq E_t < 1.5\text{GeV}$)	9.362	9.414	9.414 0 %	9.414 0 %
NS_K (1 μ -like ring): ν_μ all ($1.5 \leq E_t < 2.5\text{GeV}$)	9.824	9.316	9.316 0 %	9.316 0 %
NS_K (1 μ -like ring): ν_μ all ($2.5 \leq E_t < 3.5\text{GeV}$)	6.285	5.575	5.575 0 %	5.575 0 %
NS_K (1 μ -like ring): ν_μ all ($3.5 \leq E_t < 5\text{GeV}$)	6.729	7.556	7.556 0 %	7.556 0 %
NS_K (1 μ -like ring): ν_μ all ($5 \leq E_t < 7\text{GeV}$)	2.408	2.62	2.62 0 %	2.62 0 %
NS_K (1 μ -like ring): ν_μ all ($7 \leq E_t < 30\text{GeV}$)	0.5198	0.5386	0.5386 0 %	0.5386 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	2.191	1.891	1.951 3.144 %	1.832 -3.144 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.033	1.228	1.285 4.624 %	1.171 -4.624 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1128 4.046 %	0.1041 -4.046 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.2253 2.379 %	0.2148 -2.379 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.573 3.651 %	3.322 -3.651 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09337 3.26 %	0.08747 -3.26 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.08005 3.141 %	0.07518 -3.141 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.1734 3.205 %	0.1627 -3.205 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0 \leq E_t < 0.4\text{GeV}$)	0.1056	0.09981	0.09981 0 %	0.09981 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.04076	0.03888	0.03888 0 %	0.03888 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.005182	0.005009	0.005009 0 %	0.005009 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.01328	0.01312	0.01312 0 %	0.01312 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.7 \leq E_t < 1\text{GeV}$)	0.2604	0.2585	0.2585 0 %	0.2585 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($1 \leq E_t < 1.5\text{GeV}$)	0.8119	0.8223	0.8223 0 %	0.8223 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($1.5 \leq E_t < 2.5\text{GeV}$)	1.292	1.184	1.315 11.08 %	1.053 -11.08 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.6451	0.5646	0.5646 0 %	0.5646 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($3.5 \leq E_t < 5\text{GeV}$)	0.3945	0.4515	0.4515 0 %	0.4515 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($5 \leq E_t < 7\text{GeV}$)	0.1361	0.1492	0.1492 0 %	0.1492 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($7 \leq E_t < 30\text{GeV}$)	0.02811	0.02864	0.02864 0 %	0.02864 0 %
NS_K (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01507 0 %	0.01507 0 %
NS_K (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.01243 0 %	0.01243 0 %
NS_K (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004036 0 %	0.0004036 0 %
NS_K (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003007 0 %	0.003007 0 %
NS_K (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.0309 0 %	0.0309 0 %
NS_K (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942 0 %	0.04942 0 %
NS_K (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768 0 %	0.05768 0 %
NS_K (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071 0 %	0.1071 0 %
NS_K (1 μ -like ring): ν_e all ($0 \leq E_t < 0.5\text{GeV}$)	0.004149	0.004058	0.004058 0 %	0.004058 0 %
NS_K (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.7\text{GeV}$)	0.006751	0.007069	0.007069 0 %	0.007069 0 %
NS_K (1 μ -like ring): ν_e all ($0.7 \leq E_t < 0.8\text{GeV}$)	0.003714	0.004002	0.004002 0 %	0.004002 0 %
NS_K (1 μ -like ring): ν_e all ($0.8 \leq E_t < 1.5\text{GeV}$)	0.02648	0.02808	0.02808 0 %	0.02808 0 %
NS_K (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.03854	0.03916	0.03916 0 %	0.03916 0 %
NS_K (1 μ -like ring): ν_e all ($2.5 \leq E_t < 4\text{GeV}$)	0.03613	0.03644	0.03644 0 %	0.03644 0 %
NS_K (1 μ -like ring): ν_e all ($4 \leq E_t < 30\text{GeV}$)	0.01889	0.0192	0.0192 0 %	0.0192 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.0007554 0 %	0.0007554 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0005852	0.0007237	0.0007237 0 %	0.0007237 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	7.028e-05 0 %	7.028e-05 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0002168 0 %	0.0002168 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.001766 0 %	0.001766 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916 0 %	0.005916 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954 0 %	0.005954 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187 0 %	0.01187 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ all ($0 \leq E_t < 2.5\text{GeV}$)	0.005225	0.005338	0.005338 0 %	0.005338 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ all ($2.5 \leq E_t < 30\text{GeV}$)	0.008161	0.008298	0.008298 0 %	0.008298 0 %
NS_K (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.08288 0 %	0.08288 0 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.03527 0 %	0.03527 0 %
NS_K (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.001949 0 %	0.001949 0 %
NS_K (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006716 0 %	0.0006716 0 %
NS_K (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.1208 0 %	0.1208 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0 \leq E_t < 0.4\text{GeV}$)	0.001862	0.001811	0.001811 0 %	0.001811 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.01178	0.01191	0.01191 0 %	0.01191 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.0301	0.03129	0.03129 0 %	0.03129 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.03551	0.03652	0.03652 0 %	0.03652 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	0.0326	0.03309	0.03309 0 %	0.03309 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	0.004319	0.004798	0.004798 0 %	0.004798 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.001024	0.001061	0.001061 0 %	0.001061 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.000191	0.0001771	0.0001771 0 %	0.0001771 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	7.323e-05	7.676e-05	7.676e-05 0 %	7.676e-05 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($5 \leq E_t < 7\text{GeV}$)	3.281e-05	3.708e-05	3.708e-05 0 %	3.708e-05 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($7 \leq E_t < 30\text{GeV}$)	5.487e-06	6.152e-06	6.152e-06 0 %	6.152e-06 0 %

Table 90: Effect of $f_{14;t,r}^{banff}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
N_{SK} (1 μ -like ring)	59.41	58.37	58.5 0.2232 %	58.24 -0.2232 %
N_{SK} (1 μ -like ring): ν_μ CCQE	33.28	30.29	30.29 0 %	30.29 0 %
N_{SK} (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	16.93 0 %	16.93 0 %
N_{SK} (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.3997 0 %	0.3997 0 %
N_{SK} (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	3.771 0 %	3.771 0 %
N_{SK} (1 μ -like ring): ν_μ CC all	52.19	51.39	51.39 0 %	51.39 0 %
N_{SK} (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625 0 %	1.625 0 %
N_{SK} (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466 0 %	1.466 0 %
N_{SK} (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092 0 %	3.092 0 %
N_{SK} (1 μ -like ring): ν_μ all ($0 \leq E_t < 0.4\text{GeV}$)	4.38	4.212	4.212 0 %	4.212 0 %
N_{SK} (1 μ -like ring): ν_μ all ($0.4 \leq E_t < 0.5\text{GeV}$)	3.276	3.209	3.209 0 %	3.209 0 %
N_{SK} (1 μ -like ring): ν_μ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.5893	0.5811	0.5811 0 %	0.5811 0 %
N_{SK} (1 μ -like ring): ν_μ all ($0.6 \leq E_t < 0.7\text{GeV}$)	1.578	1.54	1.54 0 %	1.54 0 %
N_{SK} (1 μ -like ring): ν_μ all ($0.7 \leq E_t < 1\text{GeV}$)	10.46	9.917	9.917 0 %	9.917 0 %
N_{SK} (1 μ -like ring): ν_μ all ($1 \leq E_t < 1.5\text{GeV}$)	9.362	9.414	9.414 0 %	9.414 0 %
N_{SK} (1 μ -like ring): ν_μ all ($1.5 \leq E_t < 2.5\text{GeV}$)	9.824	9.316	9.316 0 %	9.316 0 %
N_{SK} (1 μ -like ring): ν_μ all ($2.5 \leq E_t < 3.5\text{GeV}$)	6.285	5.575	5.575 0 %	5.575 0 %
N_{SK} (1 μ -like ring): ν_μ all ($3.5 \leq E_t < 5\text{GeV}$)	6.729	7.556	7.556 0 %	7.556 0 %
N_{SK} (1 μ -like ring): ν_μ all ($5 \leq E_t < 7\text{GeV}$)	2.408	2.62	2.62 0 %	2.62 0 %
N_{SK} (1 μ -like ring): ν_μ all ($7 \leq E_t < 30\text{GeV}$)	0.5198	0.5386	0.5386 0 %	0.5386 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	2.191	1.891	1.942 2.702 %	1.84 -2.702 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.033	1.228	1.277 3.981 %	1.179 -3.981 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1117 3.039 %	0.1051 -3.039 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.238 8.172 %	0.2021 -8.172 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.569 3.517 %	3.326 -3.517 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09463 4.654 %	0.08621 -4.654 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.08243 6.204 %	0.0728 -6.204 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.1771 5.37 %	0.159 -5.37 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0 \leq E_t < 0.4\text{GeV}$)	0.1056	0.09981	0.09981 0 %	0.09981 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.04076	0.03888	0.03888 0 %	0.03888 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.005182	0.005009	0.005009 0 %	0.005009 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.01328	0.01312	0.01312 0 %	0.01312 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.7 \leq E_t < 1\text{GeV}$)	0.2604	0.2585	0.2585 0 %	0.2585 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($1 \leq E_t < 1.5\text{GeV}$)	0.8119	0.8223	0.8223 0 %	0.8223 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($1.5 \leq E_t < 2.5\text{GeV}$)	1.292	1.184	1.184 0 %	1.184 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.6451	0.5646	0.6262 10.91 %	0.5029 -10.91 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($3.5 \leq E_t < 5\text{GeV}$)	0.3945	0.4515	0.5008 10.91 %	0.4022 -10.91 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($5 \leq E_t < 7\text{GeV}$)	0.1361	0.1492	0.1654 10.91 %	0.1329 -10.91 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($7 \leq E_t < 30\text{GeV}$)	0.02811	0.02864	0.03176 10.91 %	0.02551 -10.91 %
N_{SK} (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01507 0 %	0.01507 0 %
N_{SK} (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.01243 0 %	0.01243 0 %
N_{SK} (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004036 0 %	0.0004036 0 %
N_{SK} (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003007 0 %	0.003007 0 %
N_{SK} (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.0309 0 %	0.0309 0 %
N_{SK} (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942 0 %	0.04942 0 %
N_{SK} (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768 0 %	0.05768 0 %
N_{SK} (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071 0 %	0.1071 0 %
N_{SK} (1 μ -like ring): ν_e all ($0 \leq E_t < 0.5\text{GeV}$)	0.004149	0.004058	0.004058 0 %	0.004058 0 %
N_{SK} (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.7\text{GeV}$)	0.006751	0.007069	0.007069 0 %	0.007069 0 %
N_{SK} (1 μ -like ring): ν_e all ($0.7 \leq E_t < 0.8\text{GeV}$)	0.003714	0.004002	0.004002 0 %	0.004002 0 %
N_{SK} (1 μ -like ring): ν_e all ($0.8 \leq E_t < 1.5\text{GeV}$)	0.02648	0.02808	0.02808 0 %	0.02808 0 %
N_{SK} (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.03854	0.03916	0.03916 0 %	0.03916 0 %
N_{SK} (1 μ -like ring): ν_e all ($2.5 \leq E_t < 4\text{GeV}$)	0.03613	0.03644	0.03644 0 %	0.03644 0 %
N_{SK} (1 μ -like ring): ν_e all ($4 \leq E_t < 30\text{GeV}$)	0.01889	0.0192	0.0192 0 %	0.0192 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.0007554 0 %	0.0007554 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0005852	0.0007237	0.0007237 0 %	0.0007237 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	7.028e-05 0 %	7.028e-05 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0002168 0 %	0.0002168 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.001766 0 %	0.001766 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916 0 %	0.005916 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954 0 %	0.005954 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187 0 %	0.01187 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ all ($0 \leq E_t < 2.5\text{GeV}$)	0.005225	0.005338	0.005338 0 %	0.005338 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ all ($2.5 \leq E_t < 30\text{GeV}$)	0.008161	0.008298	0.008298 0 %	0.008298 0 %
N_{SK} (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.08288 0 %	0.08288 0 %
N_{SK} (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.03527 0 %	0.03527 0 %
N_{SK} (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.001949 0 %	0.001949 0 %
N_{SK} (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006716 0 %	0.0006716 0 %
N_{SK} (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.1208 0 %	0.1208 0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($0 \leq E_t < 0.4\text{GeV}$)	0.001862	0.001811	0.001811 0 %	0.001811 0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.01178	0.01191	0.01191 0 %	0.01191 0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.0301	0.03129	0.03129 0 %	0.03129 0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.03551	0.03652	0.03652 0 %	0.03652 0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	0.0326	0.03309	0.03309 0 %	0.03309 0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	0.004319	0.004798	0.004798 0 %	0.004798 0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.001024	0.001061	0.001061 0 %	0.001061 0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.000191	0.0001771	0.0001771 0 %	0.0001771 0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	7.323e-05	7.676e-05	7.676e-05 0 %	7.676e-05 0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($5 \leq E_t < 7\text{GeV}$)	3.281e-05	3.708e-05	3.708e-05 0 %	3.708e-05 0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($7 \leq E_t < 30\text{GeV}$)	5.487e-06	6.152e-06	6.152e-06 0 %	6.152e-06 0 %

Table 91: Effect of $f_{15;t,r}^{banff}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NS_K (1 μ -like ring)	59.41	58.37	62.07	6.349 %
NS_K (1 μ -like ring): ν_μ CCQE	33.28	30.29	33.74	11.39 %
NS_K (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	16.93	0 %
NS_K (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.3997	0 %
NS_K (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	3.771	0 %
NS_K (1 μ -like ring): ν_μ CC all	52.19	51.39	54.84	6.714 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625	0 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466	0 %
NS_K (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	2.191	1.891	2.137	13.01 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.033	1.228	1.228	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1084	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.22	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.694	7.137 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %
NS_K (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01678	11.38 %
NS_K (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.01243	0 %
NS_K (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004036	0 %
NS_K (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003007	0 %
NS_K (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.03262	5.549 %
NS_K (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %
NS_K (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %
NS_K (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.0008544	13.1 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0005852	0.0007237	0.0007237	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	7.028e-05	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0002168	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.001865	5.603 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %
NS_K (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.09093	9.704 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.03527	0 %
NS_K (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.001949	0 %
NS_K (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006716	0 %
NS_K (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.1288	6.66 %

Table 92: Effect of $f_{16:t,r}^{banff}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NS_K (1 μ -like ring)	59.41	58.37	60.91	4.363 %
NS_K (1 μ -like ring): ν_μ CCQE	33.28	30.29	30.29	0 %
NS_K (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	18.98	12.09 %
NS_K (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.3997	0 %
NS_K (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	3.805	0.8981 %
NS_K (1 μ -like ring): ν_μ CC all	52.19	51.39	53.47	4.048 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.827	12.39 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.534	4.608 %
NS_K (1 μ -like ring): ν_μ NC all	3.218	3.092	3.361	8.699 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	2.191	1.891	1.891	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.033	1.228	1.388	13.03 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1084	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.2228	1.252 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.61	4.721 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.1061	17.33 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.08173	5.309 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.1878	11.78 %
NS_K (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01507	0 %
NS_K (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.01355	9.079 %
NS_K (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004036	0 %
NS_K (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.00303	0.7741 %
NS_K (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.03206	3.726 %
NS_K (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.05699	15.32 %
NS_K (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.06045	4.798 %
NS_K (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1174	9.652 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.0007554	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0005852	0.0007237	0.0008187	13.14 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	7.028e-05	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0002178	0.489 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.001862	5.444 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.007048	19.13 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.006334	6.376 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01338	12.73 %
NS_K (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.08288	0 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.03667	3.974 %
NS_K (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.001949	0 %
NS_K (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006779	0.9377 %
NS_K (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.1222	1.166 %

Table 93: Effect of $f_{17;t,r}^{banff}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NS_K (1 μ -like ring)	59.41	58.37	60.42	3.512 %
NS_K (1 μ -like ring): ν_μ CCQE ($E_t < 1.5$ GeV)	23.56	21.77	23.73	9.012 %
NS_K (1 μ -like ring): ν_μ CCQE ($1.5 \leq E_t < 3.5$ GeV)	7.324	5.153	5.153	0 %
NS_K (1 μ -like ring): ν_μ CCQE ($E_t \geq 3.5$ GeV)	2.39	3.366	3.366	0 %
NS_K (1 μ -like ring): ν_μ CCQE	33.28	30.29	32.25	6.477 %
NS_K (1 μ -like ring): ν_μ CC 1 π ($E_t < 2.5$ GeV)	8.121	10.34	10.34	0 %
NS_K (1 μ -like ring): ν_μ CC 1 π ($E_t \geq 2.5$ GeV)	6.508	6.593	6.593	0 %
NS_K (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	16.93	0 %
NS_K (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.3997	0 %
NS_K (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	3.771	0 %
NS_K (1 μ -like ring): ν_μ CC all	52.19	51.39	53.35	3.817 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625	0 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466	0 %
NS_K (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092	0 %
NS_K (1 μ -like ring): ν_μ CCQE ($E_t < 1.5$ GeV)	0.9457	0.8864	0.9663	9.012 %
NS_K (1 μ -like ring): ν_μ CCQE ($1.5 \leq E_t < 3.5$ GeV)	1.069	0.7597	0.7597	0 %
NS_K (1 μ -like ring): ν_μ CCQE ($E_t \geq 3.5$ GeV)	0.1759	0.245	0.245	0 %
NS_K (1 μ -like ring): ν_μ CCQE	2.191	1.891	1.971	4.224 %
NS_K (1 μ -like ring): ν_μ CC 1 π ($E_t < 2.5$ GeV)	0.5917	0.78	0.78	0 %
NS_K (1 μ -like ring): ν_μ CC 1 π ($E_t \geq 2.5$ GeV)	0.4412	0.448	0.448	0 %
NS_K (1 μ -like ring): ν_μ CC 1 π	1.033	1.228	1.228	0 %
NS_K (1 μ -like ring): ν_μ CC coherent	0.1129	0.1084	0.1084	0 %
NS_K (1 μ -like ring): ν_μ CC other (ν_μ disp)	0.2251	0.22	0.22	0 %
NS_K (1 μ -like ring): ν_μ CC all	3.562	3.448	3.527	2.317 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %
NS_K (1 μ -like ring): ν_μ NC all	0.1716	0.168	0.168	0 %
NS_K (1 μ -like ring): ν_e CCQE ($E_t < 1.5$ GeV)	0.01298	0.01279	0.01394	9.012 %
NS_K (1 μ -like ring): ν_e CCQE ($1.5 \leq E_t < 3.5$ GeV)	0.002466	0.001848	0.001848	0 %
NS_K (1 μ -like ring): ν_e CCQE ($E_t \geq 3.5$ GeV)	0.0003071	0.0004311	0.0004311	0 %
NS_K (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01622	7.649 %
NS_K (1 μ -like ring): ν_e CC 1 π ($E_t < 2.5$ GeV)	0.007737	0.01069	0.01069	0 %
NS_K (1 μ -like ring): ν_e CC 1 π ($E_t \geq 2.5$ GeV)	0.001683	0.00174	0.00174	0 %
NS_K (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.01243	0 %
NS_K (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004036	0 %
NS_K (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003007	0 %
NS_K (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.03206	3.729 %
NS_K (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %
NS_K (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %
NS_K (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %
NS_K (1 μ -like ring): ν_e CCQE ($E_t < 1.5$ GeV)	0.0004358	0.0004278	0.0004663	9.012 %
NS_K (1 μ -like ring): ν_e CCQE ($1.5 \leq E_t < 3.5$ GeV)	0.0002594	0.0001935	0.0001935	0 %
NS_K (1 μ -like ring): ν_e CCQE ($E_t \geq 3.5$ GeV)	9.51e-05	0.0001341	0.0001341	0 %
NS_K (1 μ -like ring): ν_e CCQE	0.0007903	0.0007554	0.000794	5.103 %
NS_K (1 μ -like ring): ν_e CC 1 π ($E_t < 2.5$ GeV)	0.0003394	0.0004699	0.0004699	0 %
NS_K (1 μ -like ring): ν_e CC 1 π ($E_t \geq 2.5$ GeV)	0.0002458	0.0002537	0.0002537	0 %
NS_K (1 μ -like ring): ν_e CC 1 π	0.0005852	0.0007237	0.0007237	0 %
NS_K (1 μ -like ring): ν_e CC coherent	7.028e-05	7.028e-05	7.028e-05	0 %
NS_K (1 μ -like ring): ν_e CC other (ν_μ disp)	0.0002167	0.0002168	0.0002168	0 %
NS_K (1 μ -like ring): ν_e CC all	0.001662	0.001766	0.001805	2.183 %
NS_K (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %
NS_K (1 μ -like ring): ν_e NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %
NS_K (1 μ -like ring): ν_e NC all	0.01172	0.01187	0.01187	0 %
NS_K (1 μ -like ring): oscillation ν_e CCQE ($E_t < 1.5$ GeV)	0.08705	0.08261	0.09005	9.012 %
NS_K (1 μ -like ring): oscillation ν_e CCQE ($1.5 \leq E_t < 3.5$ GeV)	0.0003506	0.0002471	0.0002471	0 %
NS_K (1 μ -like ring): oscillation ν_e CCQE ($E_t \geq 3.5$ GeV)	2.00e-05	2.838e-05	2.838e-05	0 %
NS_K (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.09033	8.982 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π ($E_t < 2.5$ GeV)	0.02723	0.03519	0.03519	0 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π ($E_t \geq 2.5$ GeV)	8.409e-05	8.452e-05	8.452e-05	0 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.03527	0 %
NS_K (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.001949	0 %
NS_K (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006716	0 %
NS_K (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.1282	6.164 %
				0.1133 -6.164 %

Table 94: Effect of $f_{18;t,r}^{banff}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5e-05$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NSK (1 μ -like ring)	59.41	58.37	60.12	2.997 %
NSK (1 μ -like ring): ν_μ CCQE ($E_t < 1.5$ GeV)	23.56	21.77	21.77	0 %
NSK (1 μ -like ring): ν_μ CCQE ($1.5 \leq E_t < 3.5$ GeV)	7.324	5.153	6.677	29.57 %
NSK (1 μ -like ring): ν_μ CCQE ($E_t \geq 3.5$ GeV)	2.39	3.366	3.366	0 %
NSK (1 μ -like ring): ν_μ CCQE	33.28	30.29	31.81	5.032 %
NSK (1 μ -like ring): ν_μ CC 1 π ($E_t < 2.5$ GeV)	8.121	10.34	10.34	0 %
NSK (1 μ -like ring): ν_μ CC 1 π ($E_t \geq 2.5$ GeV)	6.508	6.593	6.593	0 %
NSK (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	16.93	0 %
NSK (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.3997	0 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	3.771	0 %
NSK (1 μ -like ring): ν_μ CC all	52.19	51.39	52.91	2.965 %
NSK (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625	0 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466	0 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092	0 %
NSK (1 μ -like ring): ν_μ CCQE ($E_t < 1.5$ GeV)	0.9457	0.8864	0.8864	0 %
NSK (1 μ -like ring): ν_μ CCQE ($1.5 \leq E_t < 3.5$ GeV)	1.069	0.7597	0.9843	29.57 %
NSK (1 μ -like ring): ν_μ CCQE ($E_t \geq 3.5$ GeV)	0.1759	0.245	0.245	0 %
NSK (1 μ -like ring): ν_μ CCQE	2.191	1.891	2.116	11.88 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π ($E_t < 2.5$ GeV)	0.5917	0.78	0.78	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π ($E_t \geq 2.5$ GeV)	0.4412	0.448	0.448	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.033	1.228	1.228	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1084	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.22	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.672	6.516 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %
NSK (1 μ -like ring): ν_e CCQE ($E_t < 1.5$ GeV)	0.01298	0.01279	0.01279	0 %
NSK (1 μ -like ring): ν_e CCQE ($1.5 \leq E_t < 3.5$ GeV)	0.002466	0.001848	0.002394	29.57 %
NSK (1 μ -like ring): ν_e CCQE ($E_t \geq 3.5$ GeV)	0.0003071	0.0004311	0.0004311	0 %
NSK (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01561	3.626 %
NSK (1 μ -like ring): ν_e CC 1 π ($E_t < 2.5$ GeV)	0.007737	0.01069	0.01069	0 %
NSK (1 μ -like ring): ν_e CC 1 π ($E_t \geq 2.5$ GeV)	0.001683	0.00174	0.00174	0 %
NSK (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.01243	0 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004036	0 %
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003007	0 %
NSK (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.03145	1.768 %
NSK (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE ($E_t < 1.5$ GeV)	0.0004358	0.0004278	0.0004278	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE ($1.5 \leq E_t < 3.5$ GeV)	0.0002594	0.0001935	0.0002508	29.57 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE ($E_t \geq 3.5$ GeV)	9.51e-05	0.0001341	0.0001341	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.0008127	7.576 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π ($E_t < 2.5$ GeV)	0.0003394	0.0004699	0.0004699	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π ($E_t \geq 2.5$ GeV)	0.0002458	0.0002537	0.0002537	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0005852	0.0007237	0.0007237	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	7.028e-05	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0002168	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.001823	3.24 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE ($E_t < 1.5$ GeV)	0.08705	0.08261	0.08261	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE ($1.5 \leq E_t < 3.5$ GeV)	0.0003506	0.0002471	0.0003202	29.57 %
NSK (1 μ -like ring): oscillation ν_e CCQE ($E_t \geq 3.5$ GeV)	2.006e-05	2.838e-05	2.838e-05	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.08296	0.08817 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π ($E_t < 2.5$ GeV)	0.02723	0.03519	0.03519	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π ($E_t \geq 2.5$ GeV)	8.409e-05	8.452e-05	8.452e-05	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.03527	0 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.001949	0 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006716	0 %
NSK (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.1208	0.06051 %
				0.1207
				-0.06051 %

Table 95: Effect of $f_{19;t,r}^{banff}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5e-05$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NSK (1 μ -like ring)	59.41	58.37	58.97	1.033 %
NSK (1 μ -like ring): ν_μ CCQE ($E_t < 1.5$ GeV)	23.56	21.77	21.77	0 %
NSK (1 μ -like ring): ν_μ CCQE ($1.5 \leq E_t < 3.5$ GeV)	7.324	5.153	5.153	0 %
NSK (1 μ -like ring): ν_μ CCQE ($E_t \geq 3.5$ GeV)	2.39	3.366	3.928	16.7 %
NSK (1 μ -like ring): ν_μ CCQE	33.28	30.29	30.85	1.856 %
NSK (1 μ -like ring): ν_μ CC 1 π ($E_t < 2.5$ GeV)	8.121	10.34	10.34	0 %
NSK (1 μ -like ring): ν_μ CC 1 π ($E_t \geq 2.5$ GeV)	6.508	6.593	6.593	0 %
NSK (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	16.93	0 %
NSK (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.3997	0 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	3.771	0 %
NSK (1 μ -like ring): ν_μ CC all	52.19	51.39	51.95	1.094 %
NSK (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625	0 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466	0 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092	0 %
NSK (1 μ -like ring): ν_μ CCQE ($E_t < 1.5$ GeV)	0.9457	0.8864	0.8864	0 %
NSK (1 μ -like ring): ν_μ CCQE ($1.5 \leq E_t < 3.5$ GeV)	1.069	0.7597	0.7597	0 %
NSK (1 μ -like ring): ν_μ CCQE ($E_t \geq 3.5$ GeV)	0.1759	0.245	0.2859	16.7 %
NSK (1 μ -like ring): ν_μ CCQE	2.191	1.891	1.932	2.164 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π ($E_t < 2.5$ GeV)	0.5917	0.78	0.78	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π ($E_t \geq 2.5$ GeV)	0.4412	0.448	0.448	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.033	1.228	1.228	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1084	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.22	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.488	1.187 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %
NSK (1 μ -like ring): ν_e CCQE ($E_t < 1.5$ GeV)	0.01298	0.01279	0.01279	0 %
NSK (1 μ -like ring): ν_e CCQE ($1.5 \leq E_t < 3.5$ GeV)	0.002466	0.001848	0.001848	0 %
NSK (1 μ -like ring): ν_e CCQE ($E_t \geq 3.5$ GeV)	0.0003071	0.0004311	0.0005032	16.7 %
NSK (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01514	0.4779 %
NSK (1 μ -like ring): ν_e CC 1 π ($E_t < 2.5$ GeV)	0.007737	0.01069	0.01069	0 %
NSK (1 μ -like ring): ν_e CC 1 π ($E_t \geq 2.5$ GeV)	0.001683	0.00174	0.00174	0 %
NSK (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.01243	0 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004036	0 %
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003007	0 %
NSK (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.03098	0.233 %
NSK (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE ($E_t < 1.5$ GeV)	0.0004358	0.0004278	0.0004278	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE ($1.5 \leq E_t < 3.5$ GeV)	0.0002594	0.0001935	0.0001935	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE ($E_t \geq 3.5$ GeV)	9.515e-05	0.0001341	0.0001565	16.7 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.0007778	2.965 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π ($E_t < 2.5$ GeV)	0.0003394	0.0004699	0.0004699	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π ($E_t \geq 2.5$ GeV)	0.0002458	0.0002537	0.0002537	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0005852	0.0007237	0.0007237	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	7.028e-05	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0002168	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.001789	1.268 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE ($E_t < 1.5$ GeV)	0.08705	0.08261	0.08261	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE ($1.5 \leq E_t < 3.5$ GeV)	0.0003506	0.0002471	0.0002471	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE ($E_t \geq 3.5$ GeV)	2.006e-05	2.838e-05	3.311e-05	16.7 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.08289	0.005718 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π ($E_t < 2.5$ GeV)	0.02723	0.03519	0.03519	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π ($E_t \geq 2.5$ GeV)	8.409e-05	8.452e-05	8.452e-05	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.03527	0 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.001949	0 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006716	0 %
NSK (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.1208	0.003924 %
				0.1208 -0.003924 %

Table 96: Effect of $f_{20;t,r}^{bannff}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5e-05$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NS_K (1 μ -like ring)	59.41	58.37	60.03	2.85 %
NS_K (1 μ -like ring): ν_μ CCQE ($E_t < 1.5$ GeV)	23.56	21.77	21.77	0 %
NS_K (1 μ -like ring): ν_μ CCQE ($1.5 \leq E_t < 3.5$ GeV)	7.324	5.153	5.153	0 %
NS_K (1 μ -like ring): ν_μ CCQE ($E_t \geq 3.5$ GeV)	2.39	3.366	3.366	0 %
NS_K (1 μ -like ring): ν_μ CCQE	33.28	30.29	30.29	0 %
NS_K (1 μ -like ring): ν_μ CC 1 π ($E_t < 2.5$ GeV)	8.121	10.34	11.88	14.9 %
NS_K (1 μ -like ring): ν_μ CC 1 π ($E_t \geq 2.5$ GeV)	6.508	6.593	6.593	0 %
NS_K (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	18.47	9.097 %
NS_K (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.3997	0 %
NS_K (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	3.771	0 %
NS_K (1 μ -like ring): ν_μ CC all	52.19	51.39	52.93	2.997 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625	0 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466	0 %
NS_K (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092	0 %
NS_K (1 μ -like ring): ν_μ CCQE ($E_t < 1.5$ GeV)	0.9457	0.8864	0.8864	0 %
NS_K (1 μ -like ring): ν_μ CCQE ($1.5 \leq E_t < 3.5$ GeV)	1.069	0.7597	0.7597	0 %
NS_K (1 μ -like ring): ν_μ CCQE ($E_t \geq 3.5$ GeV)	0.1759	0.245	0.245	0 %
NS_K (1 μ -like ring): ν_μ CCQE	2.191	1.891	1.891	0 %
NS_K (1 μ -like ring): ν_μ CC 1 π ($E_t < 2.5$ GeV)	0.5917	0.78	0.8962	14.9 %
NS_K (1 μ -like ring): ν_μ CC 1 π ($E_t \geq 2.5$ GeV)	0.4412	0.448	0.448	0 %
NS_K (1 μ -like ring): ν_μ CC 1 π	1.033	1.228	1.344	9.463 %
NS_K (1 μ -like ring): ν_μ CC coherent	0.1129	0.1084	0.1084	0 %
NS_K (1 μ -like ring): ν_μ CC other (ν_μ disp)	0.2251	0.22	0.22	0 %
NS_K (1 μ -like ring): ν_μ CC all	3.562	3.448	3.564	3.371 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %
NS_K (1 μ -like ring): ν_μ NC all	0.1716	0.168	0.168	0 %
NS_K (1 μ -like ring): ν_e CCQE ($E_t < 1.5$ GeV)	0.01298	0.01279	0.01279	0 %
NS_K (1 μ -like ring): ν_e CCQE ($1.5 \leq E_t < 3.5$ GeV)	0.002466	0.001848	0.001848	0 %
NS_K (1 μ -like ring): ν_e CCQE ($E_t \geq 3.5$ GeV)	0.0003071	0.0004311	0.0004311	0 %
NS_K (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01507	0 %
NS_K (1 μ -like ring): ν_e CC 1 π ($E_t < 2.5$ GeV)	0.007737	0.01069	0.01228	14.9 %
NS_K (1 μ -like ring): ν_e CC 1 π ($E_t \geq 2.5$ GeV)	0.001683	0.00174	0.00174	0 %
NS_K (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.01402	12.81 %
NS_K (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004036	0 %
NS_K (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003007	0 %
NS_K (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.0325	5.151 %
NS_K (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %
NS_K (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %
NS_K (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %
NS_K (1 μ -like ring): ν_e CCQE ($E_t < 1.5$ GeV)	0.0004358	0.0004278	0.0004278	0 %
NS_K (1 μ -like ring): ν_e CCQE ($1.5 \leq E_t < 3.5$ GeV)	0.0002594	0.0001935	0.0001935	0 %
NS_K (1 μ -like ring): ν_e CCQE ($E_t \geq 3.5$ GeV)	9.51e-05	0.0001341	0.0001341	0 %
NS_K (1 μ -like ring): ν_e CCQE	0.0007903	0.0007554	0.0007554	0 %
NS_K (1 μ -like ring): ν_e CC 1 π ($E_t < 2.5$ GeV)	0.0003394	0.0004699	0.0005399	14.9 %
NS_K (1 μ -like ring): ν_e CC 1 π ($E_t \geq 2.5$ GeV)	0.0002458	0.0002537	0.0002537	0 %
NS_K (1 μ -like ring): ν_e CC 1 π	0.0005852	0.0007237	0.0007937	9.674 %
NS_K (1 μ -like ring): ν_e CC coherent	7.028e-05	7.028e-05	7.028e-05	0 %
NS_K (1 μ -like ring): ν_e CC other (ν_μ disp)	0.0002167	0.0002168	0.0002168	0 %
NS_K (1 μ -like ring): ν_e CC all	0.001662	0.001766	0.001836	3.964 %
NS_K (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %
NS_K (1 μ -like ring): ν_e NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %
NS_K (1 μ -like ring): ν_e NC all	0.01172	0.01187	0.01187	0 %
NS_K (1 μ -like ring): oscillation ν_e CCQE ($E_t < 1.5$ GeV)	0.08705	0.08261	0.08261	0 %
NS_K (1 μ -like ring): oscillation ν_e CCQE ($1.5 \leq E_t < 3.5$ GeV)	0.0003506	0.0002471	0.0002471	0 %
NS_K (1 μ -like ring): oscillation ν_e CCQE ($E_t \geq 3.5$ GeV)	2.00e-05	2.838e-05	2.838e-05	0 %
NS_K (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.08288	0 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π ($E_t < 2.5$ GeV)	0.02723	0.03519	0.04043	14.9 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π ($E_t \geq 2.5$ GeV)	8.409e-05	8.452e-05	8.452e-05	0 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.04051	14.86 %
NS_K (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.001949	0 %
NS_K (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006716	0 %
NS_K (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.126	4.34 %
				0.1155 -4.34 %

Table 97: Effect of $f_{21;t,r}^{bannff}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5e-05$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NSK (1 μ -like ring)	59.41	58.37	60.32	3.347 %
NSK (1 μ -like ring): ν_μ CCQE ($E_t < 1.5$ GeV)	23.56	21.77	21.77	0 %
NSK (1 μ -like ring): ν_μ CCQE ($1.5 \leq E_t < 3.5$ GeV)	7.324	5.153	5.153	0 %
NSK (1 μ -like ring): ν_μ CCQE ($E_t \geq 3.5$ GeV)	2.39	3.366	3.366	0 %
NSK (1 μ -like ring): ν_μ CCQE	33.28	30.29	30.29	0 %
NSK (1 μ -like ring): ν_μ CC 1 π ($E_t < 2.5$ GeV)	8.121	10.34	10.34	0 %
NSK (1 μ -like ring): ν_μ CC 1 π ($E_t \geq 2.5$ GeV)	6.508	6.593	8.422	27.74 %
NSK (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	18.76	10.8 %
NSK (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.3997	0 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	3.771	0 %
NSK (1 μ -like ring): ν_μ CC all	52.19	51.39	53.22	3.559 %
NSK (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625	0 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466	0 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092	0 %
NSK (1 μ -like ring): ν_μ CCQE ($E_t < 1.5$ GeV)	0.9457	0.8864	0.8864	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($1.5 \leq E_t < 3.5$ GeV)	1.069	0.7597	0.7597	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($E_t \geq 3.5$ GeV)	0.1759	0.245	0.245	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	2.191	1.891	1.891	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π ($E_t < 2.5$ GeV)	0.5917	0.78	0.78	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π ($E_t \geq 2.5$ GeV)	0.4412	0.448	0.5722	27.74 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.033	1.228	1.352	10.12 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1084	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.22	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.572	3.605 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %
NSK (1 μ -like ring): ν_e CCQE ($E_t < 1.5$ GeV)	0.01298	0.01279	0.01279	0 %
NSK (1 μ -like ring): ν_e CCQE ($1.5 \leq E_t < 3.5$ GeV)	0.002466	0.001848	0.001848	0 %
NSK (1 μ -like ring): ν_e CCQE ($E_t \geq 3.5$ GeV)	0.0003071	0.0004311	0.0004311	0 %
NSK (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01507	0 %
NSK (1 μ -like ring): ν_e CC 1 π ($E_t < 2.5$ GeV)	0.007737	0.01069	0.01069	0 %
NSK (1 μ -like ring): ν_e CC 1 π ($E_t \geq 2.5$ GeV)	0.001683	0.00174	0.002222	27.74 %
NSK (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.01291	3.884 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004036	0 %
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003007	0 %
NSK (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.03139	1.562 %
NSK (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE ($E_t < 1.5$ GeV)	0.0004358	0.0004278	0.0004278	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE ($1.5 \leq E_t < 3.5$ GeV)	0.0002594	0.0001935	0.0001935	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE ($E_t \geq 3.5$ GeV)	9.51e-05	0.0001341	0.0001341	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.0007554	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π ($E_t < 2.5$ GeV)	0.0003394	0.0004699	0.0004699	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π ($E_t \geq 2.5$ GeV)	0.0002458	0.0002537	0.0003241	27.74 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0005852	0.0007237	0.000794	9.727 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	7.028e-05	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0002168	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.001837	3.985 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE ($E_t < 1.5$ GeV)	0.08705	0.08261	0.08261	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE ($1.5 \leq E_t < 3.5$ GeV)	0.0003506	0.0002471	0.0002471	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE ($E_t \geq 3.5$ GeV)	2.00e-05	2.838e-05	2.838e-05	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.08288	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π ($E_t < 2.5$ GeV)	0.02723	0.03519	0.03519	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π ($E_t \geq 2.5$ GeV)	8.409e-05	8.452e-05	0.000108	27.74 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.03529	0.06647 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.001949	0 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006716	0 %
NSK (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.1208	0.01941 %
				0.1208
				-0.01941 %

Table 98: Effect of $f_{22;t,r}^{bannff}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5e-05$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
N_{SK} (1 μ -like ring)	59.41	58.37	58.45 0.1368 %	58.36 -0.01948 %
N_{SK} (1 μ -like ring): ν_μ CCQE	33.28	30.29	30.36 0.2604 %	30.28 -0.03448 %
N_{SK} (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	16.93 0 %	16.93 0 %
N_{SK} (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.3997 0 %	0.3997 0 %
N_{SK} (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	3.771 0 %	3.771 0 %
N_{SK} (1 μ -like ring): ν_μ CC all	52.19	51.39	51.47 0.1535 %	51.38 -0.02032 %
N_{SK} (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625 0 %	1.625 0 %
N_{SK} (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466 0 %	1.466 0 %
N_{SK} (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092 0 %	3.092 0 %
N_{SK} (1 μ -like ring): ν_μ all ($0 \leq E_t < 0.4\text{GeV}$)	4.38	4.212	4.023 -4.496 %	4.376 3.888 %
N_{SK} (1 μ -like ring): ν_μ all ($0.4 \leq E_t < 0.5\text{GeV}$)	3.276	3.209	3.163 -1.446 %	3.241 0.9892 %
N_{SK} (1 μ -like ring): ν_μ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.5893	0.5811	0.5791 -0.35 %	0.5822 0.1908 %
N_{SK} (1 μ -like ring): ν_μ all ($0.6 \leq E_t < 0.7\text{GeV}$)	1.578	1.54	1.542 0.08115 %	1.539 -0.1143 %
N_{SK} (1 μ -like ring): ν_μ all ($0.7 \leq E_t < 1\text{GeV}$)	10.46	9.917	9.944 0.2715 %	9.91 -0.08004 %
N_{SK} (1 μ -like ring): ν_μ all ($1 \leq E_t < 1.5\text{GeV}$)	9.362	9.414	9.495 0.8618 %	9.371 -0.4521 %
N_{SK} (1 μ -like ring): ν_μ all ($1.5 \leq E_t < 2.5\text{GeV}$)	9.824	9.316	9.395 0.8475 %	9.254 -0.6598 %
N_{SK} (1 μ -like ring): ν_μ all ($2.5 \leq E_t < 3.5\text{GeV}$)	6.285	5.575	5.621 0.8127 %	5.545 -0.5411 %
N_{SK} (1 μ -like ring): ν_μ all ($3.5 \leq E_t < 5\text{GeV}$)	6.729	7.556	7.632 1.01 %	7.498 -0.767 %
N_{SK} (1 μ -like ring): ν_μ all ($5 \leq E_t < 7\text{GeV}$)	2.408	2.62	2.627 0.2579 %	2.615 -0.1995 %
N_{SK} (1 μ -like ring): ν_μ all ($7 \leq E_t < 30\text{GeV}$)	0.5198	0.5386	0.5386 0 %	0.5386 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	2.191	1.891	1.891 0 %	1.891 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.033	1.228	1.228 0 %	1.228 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1084 0 %	0.1084 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.22 0 %	0.22 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.448 0 %	3.448 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042 0 %	0.09042 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761 0 %	0.07761 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168 0 %	0.168 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0 \leq E_t < 0.4\text{GeV}$)	0.1056	0.09981	0.09981 0 %	0.09981 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.04076	0.03888	0.03888 0 %	0.03888 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.005182	0.005009	0.005009 0 %	0.005009 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.01328	0.01312	0.01312 0 %	0.01312 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.7 \leq E_t < 1\text{GeV}$)	0.2604	0.2585	0.2585 0 %	0.2585 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($1 \leq E_t < 1.5\text{GeV}$)	0.8119	0.8223	0.8223 0 %	0.8223 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($1.5 \leq E_t < 2.5\text{GeV}$)	1.292	1.184	1.184 0 %	1.184 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.6451	0.5646	0.5646 0 %	0.5646 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($3.5 \leq E_t < 5\text{GeV}$)	0.3945	0.4515	0.4515 0 %	0.4515 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($5 \leq E_t < 7\text{GeV}$)	0.1361	0.1492	0.1492 0 %	0.1492 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_\mu$ all ($7 \leq E_t < 30\text{GeV}$)	0.02811	0.02864	0.02864 0 %	0.02864 0 %
N_{SK} (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01521 0.9551 %	0.01495 -0.7809 %
N_{SK} (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.01243 0 %	0.01243 0 %
N_{SK} (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004036 0 %	0.0004036 0 %
N_{SK} (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003007 0 %	0.003007 0 %
N_{SK} (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.03105 0.4657 %	0.03079 -0.3808 %
N_{SK} (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942 0 %	0.04942 0 %
N_{SK} (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768 0 %	0.05768 0 %
N_{SK} (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071 0 %	0.1071 0 %
N_{SK} (1 μ -like ring): ν_e all ($0 \leq E_t < 0.5\text{GeV}$)	0.004149	0.004058	0.003999 -1.466 %	0.004093 0.865 %
N_{SK} (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.7\text{GeV}$)	0.006751	0.007069	0.007117 0.686 %	0.007022 -0.6567 %
N_{SK} (1 μ -like ring): ν_e all ($0.7 \leq E_t < 0.8\text{GeV}$)	0.003714	0.004002	0.00402 0.439 %	0.003992 -0.2601 %
N_{SK} (1 μ -like ring): ν_e all ($0.8 \leq E_t < 1.5\text{GeV}$)	0.02648	0.02808	0.02816 0.2899 %	0.02802 -0.2069 %
N_{SK} (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.03854	0.03916	0.03919 0.09375 %	0.03912 -0.08711 %
N_{SK} (1 μ -like ring): ν_e all ($2.5 \leq E_t < 4\text{GeV}$)	0.03613	0.03644	0.03645 0.04073 %	0.03643 -0.02808 %
N_{SK} (1 μ -like ring): ν_e all ($4 \leq E_t < 30\text{GeV}$)	0.01889	0.0192	0.01921 0.02281 %	0.01921 0.03387 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.0007554 0 %	0.0007554 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0005852	0.0007237	0.0007237 0 %	0.0007237 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	7.028e-05 0 %	7.028e-05 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0002168 0 %	0.0002168 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.001766 0 %	0.001766 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916 0 %	0.005916 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954 0 %	0.005954 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187 0 %	0.01187 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ all ($0 \leq E_t < 2.5\text{GeV}$)	0.005225	0.005338	0.005338 0 %	0.005338 0 %
N_{SK} (1 μ -like ring): $\bar{\nu}_e$ all ($2.5 \leq E_t < 30\text{GeV}$)	0.008161	0.008298	0.008298 0 %	0.008298 0 %
N_{SK} (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.08371 0.9973 %	0.08207 -0.9817 %
N_{SK} (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.03527 0 %	0.03527 0 %
N_{SK} (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.001949 0 %	0.001949 0 %
N_{SK} (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006716 0 %	0.0006716 0 %
N_{SK} (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.1216 0.6844 %	0.12 -0.6737 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($0 \leq E_t < 0.4\text{GeV}$)	0.001862	0.001811	0.001786 -1.378 %	0.001818 0.4177 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.01178	0.01191	0.01188 -0.2625 %	0.01191 0.04628 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.0301	0.03129	0.03148 0.5952 %	0.03109 -0.6541 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.03551	0.03652	0.03678 0.7113 %	0.03626 -0.7098 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	0.0326	0.03309	0.03347 0.1162 %	0.03277 -0.9728 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	0.004319	0.004798	0.004843 0.9202 %	0.004764 -0.7067 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.001024	0.001061	0.001068 0.6336 %	0.001056 -0.5061 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.000191	0.0001771	0.0001782 0.5877 %	0.0001759 -0.7071 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	7.323e-05	7.676e-05	7.723e-05 0.6132 %	7.637e-05 0.5165 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($5 \leq E_t < 7\text{GeV}$)	3.281e-05	3.708e-05	3.708e-05 0 %	3.708e-05 0 %
N_{SK} (1 μ -like ring): oscillation ν_e all ($7 \leq E_t < 30\text{GeV}$)	5.487e-06	6.152e-06	6.152e-06 0 %	6.152e-06 0 %

Table 99: Effect of $f_{pF;t,r}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NS_K (1 μ -like ring)	59.41	58.37	57.98	-0.6702 %
NS_K (1 μ -like ring): ν_μ CCQE	33.28	30.29	29.9	-1.269 %
NS_K (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	16.93	0 %
NS_K (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.3997	0 %
NS_K (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	3.771	0 %
NS_K (1 μ -like ring): ν_μ CC all	52.19	51.39	51	-0.7477 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625	0 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466	0 %
NS_K (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092	0 %
NS_K (1 μ -like ring): ν_μ all ($0 \leq E_t < 0.4\text{GeV}$)	4.38	4.212	4.389	4.203 %
NS_K (1 μ -like ring): ν_μ all ($0.4 \leq E_t < 0.5\text{GeV}$)	3.276	3.209	2.967	-7.541 %
NS_K (1 μ -like ring): ν_μ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.5893	0.5811	0.5473	-5.814 %
NS_K (1 μ -like ring): ν_μ all ($0.6 \leq E_t < 0.7\text{GeV}$)	1.578	1.54	1.504	-2.363 %
NS_K (1 μ -like ring): ν_μ all ($0.7 \leq E_t < 1\text{GeV}$)	10.46	9.917	9.668	-2.512 %
NS_K (1 μ -like ring): ν_μ all ($1 \leq E_t < 1.5\text{GeV}$)	9.362	9.414	9.414	0 %
NS_K (1 μ -like ring): ν_μ all ($1.5 \leq E_t < 2.5\text{GeV}$)	9.824	9.316	9.316	0 %
NS_K (1 μ -like ring): ν_μ all ($2.5 \leq E_t < 3.5\text{GeV}$)	6.285	5.575	5.575	0 %
NS_K (1 μ -like ring): ν_μ all ($3.5 \leq E_t < 5\text{GeV}$)	6.729	7.556	7.556	0 %
NS_K (1 μ -like ring): ν_μ all ($5 \leq E_t < 7\text{GeV}$)	2.408	2.62	2.62	0 %
NS_K (1 μ -like ring): ν_μ all ($7 \leq E_t < 30\text{GeV}$)	0.5198	0.5386	0.5386	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	2.191	1.891	1.891	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.033	1.228	1.228	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1084	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.22	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.448	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0 \leq E_t < 0.4\text{GeV}$)	0.1056	0.09981	0.09981	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.04076	0.03888	0.03888	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.005182	0.005009	0.005009	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.01328	0.01312	0.01312	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.7 \leq E_t < 1\text{GeV}$)	0.2604	0.2585	0.2585	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($1 \leq E_t < 1.5\text{GeV}$)	0.8119	0.8223	0.8223	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($1.5 \leq E_t < 2.5\text{GeV}$)	1.292	1.184	1.184	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.6451	0.5646	0.5646	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($3.5 \leq E_t < 5\text{GeV}$)	0.3945	0.4515	0.4515	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($5 \leq E_t < 7\text{GeV}$)	0.1361	0.1492	0.1492	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($7 \leq E_t < 30\text{GeV}$)	0.02811	0.02864	0.02864	0 %
NS_K (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.0142	-5.74 %
NS_K (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.01243	0 %
NS_K (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004036	0 %
NS_K (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003007	0 %
NS_K (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.03004	-2.799 %
NS_K (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %
NS_K (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %
NS_K (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %
NS_K (1 μ -like ring): ν_e all ($0 \leq E_t < 0.5\text{GeV}$)	0.004149	0.004058	0.003859	-4.919 %
NS_K (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.7\text{GeV}$)	0.006751	0.007069	0.006564	-7.136 %
NS_K (1 μ -like ring): ν_e all ($0.7 \leq E_t < 0.8\text{GeV}$)	0.003714	0.004002	0.003902	-2.506 %
NS_K (1 μ -like ring): ν_e all ($0.8 \leq E_t < 1.5\text{GeV}$)	0.02648	0.02808	0.02802	-0.2157 %
NS_K (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.03854	0.03916	0.03916	0 %
NS_K (1 μ -like ring): ν_e all ($2.5 \leq E_t < 4\text{GeV}$)	0.03613	0.03644	0.03644	0 %
NS_K (1 μ -like ring): ν_e all ($4 \leq E_t < 30\text{GeV}$)	0.01889	0.0192	0.0192	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.0007554	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0005852	0.0007237	0.0007237	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	7.028e-05	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0002168	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.001766	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ all ($0 \leq E_t < 2.5\text{GeV}$)	0.005225	0.005338	0.005338	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ all ($2.5 \leq E_t < 30\text{GeV}$)	0.008161	0.008298	0.008298	0 %
NS_K (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.07678	-7.358 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.03527	0 %
NS_K (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.001949	0 %
NS_K (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006716	0 %
NS_K (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.1147	-5.05 %
NS_K (1 μ -like ring): oscillation ν_e all ($0 \leq E_t < 0.4\text{GeV}$)	0.001862	0.001811	0.001759	-2.848 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.01178	0.01191	0.01165	-2.146 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.0301	0.03129	0.02883	-7.86 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.03551	0.03652	0.03413	-6.534 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	0.0326	0.03309	0.03214	-2.858 %
NS_K (1 μ -like ring): oscillation ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	0.004319	0.004798	0.004798	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.001024	0.001061	0.001061	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.000191	0.0001771	0.0001771	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	7.323e-05	7.676e-05	7.676e-05	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($5 \leq E_t < 7\text{GeV}$)	3.281e-05	3.708e-05	3.708e-05	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($7 \leq E_t < 30\text{GeV}$)	5.487e-06	6.152e-06	6.152e-06	0 %

Table 100: Effect of $f_{SF;t,r}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NS_K (1 μ -like ring)	59.41	58.37	58.58 0.3599 %	58.13 -0.4122 %
NS_K (1 μ -like ring): ν_μ CCQE	33.28	30.29	30.29 0 %	30.29 0 %
NS_K (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	16.93 0 %	16.93 0 %
NS_K (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.3997 0 %	0.3997 0 %
NS_K (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	3.771 0 %	3.771 0 %
NS_K (1 μ -like ring): ν_μ CC all	52.19	51.39	51.39 0 %	51.39 0 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.753 7.821 %	1.49 -8.335 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.522 3.763 %	1.395 -4.898 %
NS_K (1 μ -like ring): ν_μ NC all	3.218	3.092	3.274 5.896 %	2.885 -6.705 %
NS_K (1 μ -like ring): ν_μ all ($0 \leq E_t < 0.4\text{GeV}$)	4.38	4.212	4.212 0 %	4.212 0 %
NS_K (1 μ -like ring): ν_μ all ($0.4 \leq E_t < 0.5\text{GeV}$)	3.276	3.209	3.204 -0.1712 %	3.219 0.2923 %
NS_K (1 μ -like ring): ν_μ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.5893	0.5811	0.5631 -3.095 %	0.6071 4.479 %
NS_K (1 μ -like ring): ν_μ all ($0.6 \leq E_t < 0.7\text{GeV}$)	1.578	1.54	1.514 -1.73 %	1.579 2.534 %
NS_K (1 μ -like ring): ν_μ all ($0.7 \leq E_t < 1\text{GeV}$)	10.46	9.917	9.912 -0.05341 %	9.927 0.09512 %
NS_K (1 μ -like ring): ν_μ all ($1 \leq E_t < 1.5\text{GeV}$)	9.362	9.414	9.448 0.3603 %	9.372 -0.4473 %
NS_K (1 μ -like ring): ν_μ all ($1.5 \leq E_t < 2.5\text{GeV}$)	9.824	9.316	9.381 0.6963 %	9.235 -0.867 %
NS_K (1 μ -like ring): ν_μ all ($2.5 \leq E_t < 3.5\text{GeV}$)	6.285	5.575	5.619 0.7853 %	5.523 -0.9308 %
NS_K (1 μ -like ring): ν_μ all ($3.5 \leq E_t < 5\text{GeV}$)	6.729	7.556	7.609 0.7092 %	7.493 -0.8371 %
NS_K (1 μ -like ring): ν_μ all ($5 \leq E_t < 7\text{GeV}$)	2.408	2.62	2.648 1.059 %	2.585 -1.345 %
NS_K (1 μ -like ring): ν_μ all ($7 \leq E_t < 30\text{GeV}$)	0.5198	0.5386	0.5524 2.571 %	0.5207 -3.327 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	2.191	1.891	1.891 0 %	1.891 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.033	1.228	1.228 0 %	1.228 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1084 0 %	0.1084 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.22 0 %	0.22 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.448 0 %	3.448 0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.1036 14.54 %	0.07507 -16.98 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.08124 4.668 %	0.07302 -5.917 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.1848 9.981 %	0.1481 -11.87 %
NS_K (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01507 0 %	0.01507 0 %
NS_K (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.01243 0 %	0.01243 0 %
NS_K (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004036 0 %	0.0004036 0 %
NS_K (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003007 0 %	0.003007 0 %
NS_K (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.0309 0 %	0.0309 0 %
NS_K (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.05687 15.07 %	0.04059 -17.87 %
NS_K (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05983 3.724 %	0.05482 -4.967 %
NS_K (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1167 8.961 %	0.09541 -10.92 %
NS_K (1 μ -like ring): ν_e all ($0 \leq E_t < 0.5\text{GeV}$)	0.004149	0.004058	0.004034 -0.5959 %	0.004091 0.8125 %
NS_K (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.7\text{GeV}$)	0.006751	0.007069	0.006849 -3.107 %	0.007389 4.531 %
NS_K (1 μ -like ring): ν_e all ($0.7 \leq E_t < 0.8\text{GeV}$)	0.003714	0.004002	0.003921 -2.045 %	0.004143 3.511 %
NS_K (1 μ -like ring): ν_e all ($0.8 \leq E_t < 1.5\text{GeV}$)	0.02648	0.02808	0.02918 3.908 %	0.02662 -5.208 %
NS_K (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.03854	0.03916	0.04288 9.514 %	0.03445 -12.01 %
NS_K (1 μ -like ring): ν_e all ($2.5 \leq E_t < 4\text{GeV}$)	0.03613	0.03644	0.03987 9.427 %	0.03239 -11.1 %
NS_K (1 μ -like ring): ν_e all ($4 \leq E_t < 30\text{GeV}$)	0.01889	0.0192	0.02087 8.671 %	0.01722 -10.31 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.0007554 0 %	0.0007554 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0005852	0.0007237	0.0007237 0 %	0.0007237 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	7.028e-05 0 %	7.028e-05 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0002168 0 %	0.0002168 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.001766 0 %	0.001766 0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.007015 18.57 %	0.004631 -21.72 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.006256 5.079 %	0.005584 -6.213 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01327 11.81 %	0.01022 -13.94 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ all ($0 \leq E_t < 2.5\text{GeV}$)	0.005225	0.005338	0.005802 8.687 %	0.004786 -10.35 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ all ($2.5 \leq E_t < 30\text{GeV}$)	0.008161	0.008298	0.009236 11.3 %	0.007196 -13.29 %
NS_K (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.08288 0 %	0.08288 0 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.03527 0 %	0.03527 0 %
NS_K (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.001949 0 %	0.001949 0 %
NS_K (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006716 0 %	0.0006716 0 %
NS_K (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.1208 0 %	0.1208 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0 \leq E_t < 0.4\text{GeV}$)	0.001862	0.001811	0.001811 0 %	0.001811 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.01178	0.01191	0.01191 0 %	0.01191 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.0301	0.03129	0.03129 0 %	0.03129 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.03551	0.03652	0.03652 0 %	0.03652 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	0.0326	0.03309	0.03309 0 %	0.03309 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	0.004319	0.004798	0.004798 0 %	0.004798 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.001024	0.001061	0.001061 0 %	0.001061 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.000191	0.0001771	0.0001771 0 %	0.0001771 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	7.323e-05	7.676e-05	7.676e-05 0 %	7.676e-05 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($5 \leq E_t < 7\text{GeV}$)	3.281e-05	3.708e-05	3.708e-05 0 %	3.708e-05 0 %
NS_K (1 μ -like ring): oscillation ν_e all ($7 \leq E_t < 30\text{GeV}$)	5.487e-06	6.152e-06	6.152e-06 0 %	6.152e-06 0 %

Table 101: Effect of $f_{Wshape;t,r}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NS_K (1 μ -like ring)	59.41	58.37	58.85	0.8194 %
NS_K (1 μ -like ring): ν_μ CCQE	33.28	30.29	30.29	0 %
NS_K (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	16.93	0 %
NS_K (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.3997	0 %
NS_K (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	4.22	11.91 %
NS_K (1 μ -like ring): ν_μ CC all	52.19	51.39	51.84	0.8741 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625	0 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466	0 %
NS_K (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092	0 %
NS_K (1 μ -like ring): ν_μ all ($0 \leq E_t < 0.4\text{GeV}$)	4.38	4.212	4.212	0 %
NS_K (1 μ -like ring): ν_μ all ($0.4 \leq E_t < 0.5\text{GeV}$)	3.276	3.209	3.209	0 %
NS_K (1 μ -like ring): ν_μ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.5893	0.5811	0.5811	0 %
NS_K (1 μ -like ring): ν_μ all ($0.6 \leq E_t < 0.7\text{GeV}$)	1.578	1.54	1.54	0.001597 %
NS_K (1 μ -like ring): ν_μ all ($0.7 \leq E_t < 1\text{GeV}$)	10.46	9.917	9.921	0.03359 %
NS_K (1 μ -like ring): ν_μ all ($1 \leq E_t < 1.5\text{GeV}$)	9.362	9.414	9.459	0.4748 %
NS_K (1 μ -like ring): ν_μ all ($1.5 \leq E_t < 2.5\text{GeV}$)	9.824	9.316	9.425	1.174 %
NS_K (1 μ -like ring): ν_μ all ($2.5 \leq E_t < 3.5\text{GeV}$)	6.285	5.575	5.677	1.817 %
NS_K (1 μ -like ring): ν_μ all ($3.5 \leq E_t < 5\text{GeV}$)	6.729	7.556	7.681	1.652 %
NS_K (1 μ -like ring): ν_μ all ($5 \leq E_t < 7\text{GeV}$)	2.408	2.62	2.673	2.034 %
NS_K (1 μ -like ring): ν_μ all ($7 \leq E_t < 30\text{GeV}$)	0.5198	0.5386	0.5509	2.284 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	2.191	1.891	1.891	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.033	1.228	1.228	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1084	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.2484	12.9 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.476	0.8236 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0 \leq E_t < 0.4\text{GeV}$)	0.1056	0.09981	0.09981	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.04076	0.03888	0.03888	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.005182	0.005009	0.005009	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.01328	0.01312	0.01312	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.7 \leq E_t < 1\text{GeV}$)	0.2604	0.2585	0.2587	0.06552 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($1 \leq E_t < 1.5\text{GeV}$)	0.8119	0.8223	0.8246	0.2852 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($1.5 \leq E_t < 2.5\text{GeV}$)	1.292	1.184	1.194	0.7922 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.6451	0.5646	0.5719	1.308 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($3.5 \leq E_t < 5\text{GeV}$)	0.3945	0.4515	0.4575	1.325 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($5 \leq E_t < 7\text{GeV}$)	0.1361	0.1492	0.1517	1.701 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($7 \leq E_t < 30\text{GeV}$)	0.02811	0.02864	0.02924	2.086 %
NS_K (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01507	0 %
NS_K (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.01243	0 %
NS_K (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004036	0 %
NS_K (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003469	15.36 %
NS_K (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.03137	1.494 %
NS_K (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %
NS_K (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %
NS_K (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %
NS_K (1 μ -like ring): ν_e all ($0 \leq E_t < 0.5\text{GeV}$)	0.004149	0.004058	0.004058	0 %
NS_K (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.7\text{GeV}$)	0.006751	0.007069	0.007069	0 %
NS_K (1 μ -like ring): ν_e all ($0.7 \leq E_t < 0.8\text{GeV}$)	0.003714	0.004002	0.004009	0.1562 %
NS_K (1 μ -like ring): ν_e all ($0.8 \leq E_t < 1.5\text{GeV}$)	0.02648	0.02808	0.02818	0.3352 %
NS_K (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.03854	0.03916	0.03931	0.4012 %
NS_K (1 μ -like ring): ν_e all ($2.5 \leq E_t < 4\text{GeV}$)	0.03613	0.03644	0.03658	0.3965 %
NS_K (1 μ -like ring): ν_e all ($4 \leq E_t < 30\text{GeV}$)	0.01889	0.0192	0.01926	0.3118 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.0007554	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0005852	0.0007237	0.0007237	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	7.028e-05	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0002455	13.25 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.001795	1.626 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ all ($0 \leq E_t < 2.5\text{GeV}$)	0.005225	0.005338	0.005351	0.2427 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ all ($2.5 \leq E_t < 30\text{GeV}$)	0.008161	0.008298	0.008314	0.1899 %
NS_K (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.08288	0 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.03527	0 %
NS_K (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.001949	0 %
NS_K (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0008655	28.87 %
NS_K (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.121	0.1605 %
NS_K (1 μ -like ring): oscillation ν_e all ($0 \leq E_t < 0.4\text{GeV}$)	0.001862	0.001811	0.001811	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.01178	0.01191	0.01191	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.0301	0.03129	0.03129	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.03551	0.03652	0.03652	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	0.0326	0.03309	0.03317	0.244 %
NS_K (1 μ -like ring): oscillation ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	0.004319	0.004798	0.004852	1.113 %
NS_K (1 μ -like ring): oscillation ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.001024	0.001061	0.001104	4.052 %
NS_K (1 μ -like ring): oscillation ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.000191	0.0001771	0.000189	6.701 %
NS_K (1 μ -like ring): oscillation ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	7.323e-05	7.676e-05	8.059e-05	4.981 %
NS_K (1 μ -like ring): oscillation ν_e all ($5 \leq E_t < 7\text{GeV}$)	3.281e-05	3.708e-05	3.806e-05	2.624 %
NS_K (1 μ -like ring): oscillation ν_e all ($7 \leq E_t < 30\text{GeV}$)	5.487e-06	6.152e-06	6.222e-06	1.134 %

Table 102: Effect of $f_{CCothShape;t,r}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NS_K (1 μ -like ring)	59.41	58.37	61.98	6.184 %
NS_K (1 μ -like ring): ν_μ CCQE	33.28	30.29	30.29	0 %
NS_K (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	20.83	23 %
NS_K (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.3997	0 %
NS_K (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	3.771	0 %
NS_K (1 μ -like ring): ν_μ CC all	52.19	51.39	55.28	7.578 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.317	-18.97 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.379	-5.958 %
NS_K (1 μ -like ring): ν_μ NC all	3.218	3.092	2.696	-12.8 %
NS_K (1 μ -like ring): ν_μ all ($0 \leq E_t < 0.4\text{GeV}$)	4.38	4.212	4.212	0 %
NS_K (1 μ -like ring): ν_μ all ($0.4 \leq E_t < 0.5\text{GeV}$)	3.276	3.209	3.205	-0.1297 %
NS_K (1 μ -like ring): ν_μ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.5893	0.5811	0.5635	-3.031 %
NS_K (1 μ -like ring): ν_μ all ($0.6 \leq E_t < 0.7\text{GeV}$)	1.578	1.54	1.531	-0.6329 %
NS_K (1 μ -like ring): ν_μ all ($0.7 \leq E_t < 1\text{GeV}$)	10.46	9.917	10.24	3.291 %
NS_K (1 μ -like ring): ν_μ all ($1 \leq E_t < 1.5\text{GeV}$)	9.362	9.414	10.14	7.675 %
NS_K (1 μ -like ring): ν_μ all ($1.5 \leq E_t < 2.5\text{GeV}$)	9.824	9.316	10.39	11.56 %
NS_K (1 μ -like ring): ν_μ all ($2.5 \leq E_t < 3.5\text{GeV}$)	6.285	5.575	6.228	11.71 %
NS_K (1 μ -like ring): ν_μ all ($3.5 \leq E_t < 5\text{GeV}$)	6.729	7.556	8.137	7.69 %
NS_K (1 μ -like ring): ν_μ all ($5 \leq E_t < 7\text{GeV}$)	2.408	2.62	2.77	5.708 %
NS_K (1 μ -like ring): ν_μ all ($7 \leq E_t < 30\text{GeV}$)	0.5198	0.5386	0.5585	3.705 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	2.191	1.891	1.891	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.033	1.228	1.374	11.86 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1084	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.22	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.593	4.223 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.07284	-19.45 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07297	-5.987 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.1458	-13.23 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0 \leq E_t < 0.4\text{GeV}$)	0.1056	0.09981	0.09981	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.04076	0.03888	0.03886	-0.04908 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.005182	0.005009	0.004841	-3.351 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.01328	0.01312	0.01289	-1.73 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($0.7 \leq E_t < 1\text{GeV}$)	0.2604	0.2585	0.261	0.9679 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($1 \leq E_t < 1.5\text{GeV}$)	0.8119	0.8223	0.8389	2.016 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($1.5 \leq E_t < 2.5\text{GeV}$)	1.292	1.184	1.243	4.959 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.6451	0.5646	0.5916	4.788 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($3.5 \leq E_t < 5\text{GeV}$)	0.3945	0.4515	0.4665	3.329 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($5 \leq E_t < 7\text{GeV}$)	0.1361	0.1492	0.1527	2.352 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ all ($7 \leq E_t < 30\text{GeV}$)	0.02811	0.02864	0.02903	1.361 %
NS_K (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01507	0 %
NS_K (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.0132	6.198 %
NS_K (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004036	0 %
NS_K (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003007	0 %
NS_K (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.03168	2.492 %
NS_K (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.0398	-19.46 %
NS_K (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.0548	-4.999 %
NS_K (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.0946	-11.67 %
NS_K (1 μ -like ring): ν_e all ($0 \leq E_t < 0.5\text{GeV}$)	0.004149	0.004058	0.004033	-0.6155 %
NS_K (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.7\text{GeV}$)	0.006751	0.007069	0.006962	-1.51 %
NS_K (1 μ -like ring): ν_e all ($0.7 \leq E_t < 0.8\text{GeV}$)	0.003714	0.004002	0.003825	-4.428 %
NS_K (1 μ -like ring): ν_e all ($0.8 \leq E_t < 1.5\text{GeV}$)	0.02648	0.02808	0.0255	-9.186 %
NS_K (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.03854	0.03916	0.03531	-9.825 %
NS_K (1 μ -like ring): ν_e all ($2.5 \leq E_t < 4\text{GeV}$)	0.03613	0.03644	0.03308	-9.209 %
NS_K (1 μ -like ring): ν_e all ($4 \leq E_t < 30\text{GeV}$)	0.01889	0.0192	0.01756	-8.539 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.0007554	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0005852	0.0007237	0.0007506	3.723 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	7.028e-05	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0002168	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.001793	1.526 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.004761	-19.52 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005621	-5.585 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01038	-12.53 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ all ($0 \leq E_t < 2.5\text{GeV}$)	0.005225	0.005338	0.004781	-10.43 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ all ($2.5 \leq E_t < 30\text{GeV}$)	0.008161	0.008298	0.007395	-10.89 %
NS_K (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.08288	0 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.03634	3.035 %
NS_K (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.001949	0 %
NS_K (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006716	0 %
NS_K (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.1218	0.8862 %
NS_K (1 μ -like ring): oscillation ν_e all ($0 \leq E_t < 0.4\text{GeV}$)	0.001862	0.001811	0.001811	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.01178	0.01191	0.01179	-0.9772 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.0301	0.03129	0.03075	-1.723 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.03551	0.03652	0.03693	1.117 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	0.0326	0.03309	0.03357	1.45 %
NS_K (1 μ -like ring): oscillation ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	0.004319	0.004798	0.005418	12.91 %
NS_K (1 μ -like ring): oscillation ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.001024	0.001061	0.001282	20.78 %
NS_K (1 μ -like ring): oscillation ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.000191	0.0001771	0.0001695	-4.337 %
NS_K (1 μ -like ring): oscillation ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	7.323e-05	7.676e-05	8.485e-05	10.53 %
NS_K (1 μ -like ring): oscillation ν_e all ($5 \leq E_t < 7\text{GeV}$)	3.281e-05	3.708e-05	3.579e-05	-3.496 %
NS_K (1 μ -like ring): oscillation ν_e all ($7 \leq E_t < 30\text{GeV}$)	5.487e-06	6.152e-06	5.494e-06	-10.7 %

Table 103: Effect of $f_{\pi-less\Delta;t,r}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ		BANFF tuned -1 σ	
NS_K (1 μ -like ring)	59.41	58.37	58.34	-0.05097 %	58.5	0.2182 %
NS_K (1 μ -like ring): ν_μ CCQE	33.28	30.29	30.26	-0.09564 %	30.41	0.4186 %
NS_K (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	16.93	0 %	16.93	0 %
NS_K (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.3997	0 %	0.3997	0 %
NS_K (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	3.771	0 %	3.771	0 %
NS_K (1 μ -like ring): ν_μ CC all	52.19	51.39	51.36	-0.05637 %	51.51	0.2467 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625	0 %	1.625	0 %
NS_K (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466	0 %	1.466	0 %
NS_K (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092	0 %	3.092	0 %
NS_K (1 μ -like ring): ν_μ all ($0 \leq E_t < 0.4\text{GeV}$)	4.38	4.212	4.718	12.01 %	3.747	-11.04 %
NS_K (1 μ -like ring): ν_μ all ($0.4 \leq E_t < 0.5\text{GeV}$)	3.276	3.209	3.456	7.691 %	2.969	-7.485 %
NS_K (1 μ -like ring): ν_μ all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.5893	0.5811	0.6	3.256 %	0.5609	-3.482 %
NS_K (1 μ -like ring): ν_μ all ($0.6 \leq E_t < 0.7\text{GeV}$)	1.578	1.54	1.511	-1.871 %	1.563	1.499 %
NS_K (1 μ -like ring): ν_μ all ($0.7 \leq E_t < 1\text{GeV}$)	10.46	9.917	9.459	-4.626 %	10.4	4.83 %
NS_K (1 μ -like ring): ν_μ all ($1 \leq E_t < 1.5\text{GeV}$)	9.362	9.414	9.184	-2.443 %	9.666	2.681 %
NS_K (1 μ -like ring): ν_μ all ($1.5 \leq E_t < 2.5\text{GeV}$)	9.824	9.316	9.259	-0.6097 %	9.379	0.6832 %
NS_K (1 μ -like ring): ν_μ all ($2.5 \leq E_t < 3.5\text{GeV}$)	6.285	5.575	5.568	-0.1285 %	5.585	0.171 %
NS_K (1 μ -like ring): ν_μ all ($3.5 \leq E_t < 5\text{GeV}$)	6.729	7.556	7.539	-0.2166 %	7.578	0.2944 %
NS_K (1 μ -like ring): ν_μ all ($5 \leq E_t < 7\text{GeV}$)	2.408	2.62	2.617	-0.09818 %	2.622	0.08395 %
NS_K (1 μ -like ring): ν_μ all ($7 \leq E_t < 30\text{GeV}$)	0.5198	0.5386	0.5386	0 %	0.5386	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	2.191	1.891	1.891	0 %	1.891	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.033	1.228	1.228	0 %	1.228	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1084	0 %	0.1084	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.22	0 %	0.22	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.448	0 %	3.448	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %	0.09042	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %	0.07761	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC all	0.1716	0.168	0.168	0 %	0.168	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($0 \leq E_t < 0.4\text{GeV}$)	0.1056	0.09981	0.09981	0 %	0.09981	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.04076	0.03888	0.03888	0 %	0.03888	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.005182	0.005009	0.005009	0 %	0.005009	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.01328	0.01312	0.01312	0 %	0.01312	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($0.7 \leq E_t < 1\text{GeV}$)	0.2604	0.2585	0.2585	0 %	0.2585	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($1 \leq E_t < 1.5\text{GeV}$)	0.8119	0.8223	0.8223	0 %	0.8223	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($1.5 \leq E_t < 2.5\text{GeV}$)	1.292	1.184	1.184	0 %	1.184	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.6451	0.5646	0.5646	0 %	0.5646	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($3.5 \leq E_t < 5\text{GeV}$)	0.3945	0.4515	0.4515	0 %	0.4515	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($5 \leq E_t < 7\text{GeV}$)	0.1361	0.1492	0.1492	0 %	0.1492	0 %
NS_K (1 μ -like ring): $\bar{\nu}_\mu$ NC all ($7 \leq E_t < 30\text{GeV}$)	0.02811	0.02864	0.02864	0 %	0.02864	0 %
NS_K (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01501	-0.3628 %	0.01513	0.405 %
NS_K (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.01243	0 %	0.01243	0 %
NS_K (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004036	0 %	0.0004036	0 %
NS_K (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003007	0 %	0.003007	0 %
NS_K (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.03085	-0.1769 %	0.03097	0.1975 %
NS_K (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %	0.04942	0 %
NS_K (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %	0.05768	0 %
NS_K (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %	0.1071	0 %
NS_K (1 μ -like ring): ν_e all ($0 \leq E_t < 0.5\text{GeV}$)	0.004149	0.004058	0.004391	8.205 %	0.003737	-7.91 %
NS_K (1 μ -like ring): ν_e all ($0.5 \leq E_t < 0.7\text{GeV}$)	0.006751	0.007069	0.00704	-0.4042 %	0.007078	0.1358 %
NS_K (1 μ -like ring): ν_e all ($0.7 \leq E_t < 0.8\text{GeV}$)	0.003714	0.004002	0.003913	-2.239 %	0.004092	2.228 %
NS_K (1 μ -like ring): ν_e all ($0.8 \leq E_t < 1.5\text{GeV}$)	0.02648	0.02808	0.02785	-0.8333 %	0.02833	0.8735 %
NS_K (1 μ -like ring): ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.03854	0.03916	0.03913	-0.0683 %	0.03919	0.07268 %
NS_K (1 μ -like ring): ν_e all ($2.5 \leq E_t < 4\text{GeV}$)	0.03613	0.03644	0.03643	-0.01515 %	0.03644	0.01695 %
NS_K (1 μ -like ring): ν_e all ($4 \leq E_t < 30\text{GeV}$)	0.01889	0.0192	0.0192	-0.01678 %	0.01921	0.0174 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.0007554	0 %	0.0007554	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0005852	0.0007237	0.0007237	0 %	0.0007237	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	7.028e-05	0 %	7.028e-05	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0002168	0 %	0.0002168	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.001766	0 %	0.001766	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %	0.005916	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %	0.005954	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %	0.01187	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ all ($0 \leq E_t < 2.5\text{GeV}$)	0.005225	0.005338	0.005338	0 %	0.005338	0 %
NS_K (1 μ -like ring): $\bar{\nu}_e$ all ($2.5 \leq E_t < 30\text{GeV}$)	0.008161	0.008298	0.008298	0 %	0.008298	0 %
NS_K (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.08215	-0.8807 %	0.08337	0.5927 %
NS_K (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.03527	0 %	0.03527	0 %
NS_K (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.001949	0 %	0.001949	0 %
NS_K (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006716	0 %	0.0006716	0 %
NS_K (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.12	-0.6044 %	0.1213	0.4068 %
NS_K (1 μ -like ring): oscillation ν_e all ($0 \leq E_t < 0.4\text{GeV}$)	0.001862	0.001811	0.001972	8.897 %	0.001654	-8.668 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.4 \leq E_t < 0.5\text{GeV}$)	0.01178	0.01191	0.0125	5.011 %	0.0113	-5.07 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.5 \leq E_t < 0.6\text{GeV}$)	0.0301	0.03129	0.0316	0.9744 %	0.03085	-1.415 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.6 \leq E_t < 0.7\text{GeV}$)	0.03551	0.03652	0.03592	-1.637 %	0.037	1.31 %
NS_K (1 μ -like ring): oscillation ν_e all ($0.7 \leq E_t < 1\text{GeV}$)	0.0326	0.03309	0.032	-3.291 %	0.03418	3.31 %
NS_K (1 μ -like ring): oscillation ν_e all ($1 \leq E_t < 1.5\text{GeV}$)	0.004319	0.004798	0.004698	-2.099 %	0.004913	2.382 %
NS_K (1 μ -like ring): oscillation ν_e all ($1.5 \leq E_t < 2.5\text{GeV}$)	0.001024	0.001061	0.001057	-0.4298 %	0.001067	0.5779 %
NS_K (1 μ -like ring): oscillation ν_e all ($2.5 \leq E_t < 3.5\text{GeV}$)	0.000191	0.0001771	0.0001768	-0.2112 %	0.0001773	0.06669 %
NS_K (1 μ -like ring): oscillation ν_e all ($3.5 \leq E_t < 5\text{GeV}$)	7.323e-05	7.676e-05	7.667e-05	-0.1223 %	7.691e-05	0.1913 %
NS_K (1 μ -like ring): oscillation ν_e all ($5 \leq E_t < 7\text{GeV}$)	3.281e-05	3.708e-05	3.708e-05	0 %	3.708e-05	0 %
NS_K (1 μ -like ring): oscillation ν_e all ($7 \leq E_t < 30\text{GeV}$)	5.487e-06	6.152e-06	6.152e-06	0 %	6.152e-06	0 %

Table 104: Effect of $f_{bindE;t,r}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ		BANFF tuned -1 σ	
NSK (1 μ -like ring)	59.41	58.37	58.88	0.8748 %	57.86	-0.8748 %
NSK (1 μ -like ring): ν_μ CCQE	33.28	30.29	30.29	0 %	30.29	0 %
NSK (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	16.93	0 %	16.93	0 %
NSK (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.7994	100 %	0	-100 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	3.771	0 %	3.771	0 %
NSK (1 μ -like ring): ν_μ CC all	52.19	51.39	51.79	0.7778 %	50.99	-0.7778 %
NSK (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625	0 %	1.625	0 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466	0 %	1.466	0 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092	0 %	3.092	0 %
NSK (1 μ -like ring): ν_μ CCQE	2.191	1.891	1.891	0 %	1.891	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.033	1.228	1.228	0 %	1.228	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.2169	100 %	0	-100 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.22	0 %	0.22	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.556	3.146 %	3.339	-3.146 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %	0.09042	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %	0.07761	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %	0.168	0 %
NSK (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01507	0 %	0.01507	0 %
NSK (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.01243	0 %	0.01243	0 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0008072	100 %	0	-100 %
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003007	0 %	0.003007	0 %
NSK (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.03131	1.306 %	0.0305	-1.306 %
NSK (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %	0.04942	0 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %	0.05768	0 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %	0.1071	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.0007554	0 %	0.0007554	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0005852	0.0007237	0.0007237	0 %	0.0007237	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	0.0001406	100 %	0	-100 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0002168	0 %	0.0002168	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.001836	3.979 %	0.001696	-3.979 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %	0.005916	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %	0.005954	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %	0.01187	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.08288	0 %	0.08288	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.03527	0 %	0.03527	0 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.003897	100 %	0	-100 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006716	0 %	0.0006716	0 %
NSK (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.1227	1.613 %	0.1188	-1.613 %

Table 105: Effect of $f_{CCcoh;t}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ		BANFF tuned -1 σ	
NSK (1 μ -like ring)	59.41	58.37	58.9	0.9104 %	57.84	-0.9104 %
NSK (1 μ -like ring): ν_μ CCQE	33.28	30.29	30.29	0 %	30.29	0 %
NSK (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	16.93	0 %	16.93	0 %
NSK (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.3997	0 %	0.3997	0 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	3.771	0 %	3.771	0 %
NSK (1 μ -like ring): ν_μ CC all	52.19	51.39	51.39	0 %	51.39	0 %
NSK (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	2.113	30 %	1.138	-30 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466	0 %	1.466	0 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	3.58	15.77 %	2.604	-15.77 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	2.191	1.891	1.891	0 %	1.891	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.033	1.228	1.228	0 %	1.228	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1084	0 %	0.1084	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.22	0 %	0.22	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.448	0 %	3.448	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.1175	30 %	0.0633	-30 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %	0.07761	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.1952	16.14 %	0.1409	-16.14 %
NSK (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01507	0 %	0.01507	0 %
NSK (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.01243	0 %	0.01243	0 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004036	0 %	0.0004036	0 %
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003007	0 %	0.003007	0 %
NSK (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.0309	0 %	0.0309	0 %
NSK (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.06425	30 %	0.03459	-30 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %	0.05768	0 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1219	13.84 %	0.09228	-13.84 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.0007554	0 %	0.0007554	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0005852	0.0007237	0.0007237	0 %	0.0007237	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	7.028e-05	0 %	7.028e-05	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0002168	0 %	0.0002168	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.001766	0 %	0.001766	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.007691	30 %	0.004141	-30 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %	0.005954	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01365	14.95 %	0.0101	-14.95 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.08288	0 %	0.08288	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.03527	0 %	0.03527	0 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.001949	0 %	0.001949	0 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006716	0 %	0.0006716	0 %
NSK (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.1208	0 %	0.1208	0 %

Table 106: Effect of $f_{NC1\pi^\pm,t}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ		BANFF tuned -1 σ	
NSK (1 μ -like ring)	59.41	58.37	58.85	0.8264 %	57.89	-0.8264 %
NSK (1 μ -like ring): ν_μ CCQE	33.28	30.29	30.29	0 %	30.29	0 %
NSK (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	16.93	0 %	16.93	0 %
NSK (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.3997	0 %	0.3997	0 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	3.771	0 %	3.771	0 %
NSK (1 μ -like ring): ν_μ CC all	52.19	51.39	51.39	0 %	51.39	0 %
NSK (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625	0 %	1.625	0 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.906	30 %	1.027	-30 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	3.532	14.23 %	2.652	-14.23 %
NSK (1 μ -like ring): ν_μ CCQE	2.191	1.891	1.891	0 %	1.891	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.033	1.228	1.228	0 %	1.228	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1084	0 %	0.1084	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.22	0 %	0.22	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.448	0 %	3.448	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %	0.09042	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.1009	30 %	0.05433	-30 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.1913	13.86 %	0.1448	-13.86 %
NSK (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01507	0 %	0.01507	0 %
NSK (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.01243	0 %	0.01243	0 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004036	0 %	0.0004036	0 %
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003007	0 %	0.003007	0 %
NSK (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.0309	0 %	0.0309	0 %
NSK (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %	0.04942	0 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.07499	30 %	0.04038	-30 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1244	16.16 %	0.0898	-16.16 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.0007554	0 %	0.0007554	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0005852	0.0007237	0.0007237	0 %	0.0007237	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	7.028e-05	0 %	7.028e-05	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0002168	0 %	0.0002168	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.001766	0 %	0.001766	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %	0.005916	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.00774	30 %	0.004168	-30 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01366	15.05 %	0.01008	-15.05 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.08288	0 %	0.08288	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.03527	0 %	0.03527	0 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.001949	0 %	0.001949	0 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006716	0 %	0.0006716	0 %
NSK (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.1208	0 %	0.1208	0 %

Table 107: Effect of $f_{NCoth;t}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NSK (1 μ -like ring)	59.41	58.37	58.37 0.007887 %	58.36 -0.007887 %
NSK (1 μ -like ring): ν_μ CCQE	33.28	30.29	30.29 0 %	30.29 0 %
NSK (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	16.93 0 %	16.93 0 %
NSK (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.3997 0 %	0.3997 0 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	3.771 0 %	3.771 0 %
NSK (1 μ -like ring): ν_μ CC all	52.19	51.39	51.39 0 %	51.39 0 %
NSK (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625 0 %	1.625 0 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466 0 %	1.466 0 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092 0 %	3.092 0 %
NSK (1 μ -like ring): ν_μ CCQE	2.191	1.891	1.891 0 %	1.891 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.033	1.228	1.228 0 %	1.228 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1084 0 %	0.1084 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.22 0 %	0.22 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.448 0 %	3.448 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042 0 %	0.09042 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761 0 %	0.07761 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168 0 %	0.168 0 %
NSK (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01552 3 %	0.01462 -3 %
NSK (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.0128 3 %	0.01205 -3 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004157 3 %	0.0003915 -3 %
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003097 3 %	0.002917 -3 %
NSK (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.03183 3 %	0.02998 -3 %
NSK (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942 0 %	0.04942 0 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768 0 %	0.05768 0 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071 0 %	0.1071 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.0007781 3 %	0.0007328 -3 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0005852	0.0007237	0.0007454 3 %	0.0007019 -3 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	7.239e-05 3 %	6.817e-05 -3 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0002233 3 %	0.0002103 -3 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.001819 3 %	0.001713 -3 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916 0 %	0.005916 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954 0 %	0.005954 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187 0 %	0.01187 0 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.08537 3 %	0.0804 -3 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.03633 3 %	0.03421 -3 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.002007 3 %	0.00189 -3 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006917 3 %	0.0006515 -3 %
NSK (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.1244 3 %	0.1172 -3 %

Table 108: Effect of $f_{CC\nu_{S;T}}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ	
NSK (1 μ -like ring)	59.41	58.37	59.75	2,364 %	56.99
NSK (1 μ -like ring): ν_μ CCQE	33.28	30.29	30.29	0 %	30.29
NSK (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	16.93	0 %	16.93
NSK (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.3997	0 %	0.3997
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	3.771	0 %	3.771
NSK (1 μ -like ring): ν_μ CC all	52.19	51.39	51.39	0 %	51.39
NSK (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625	0 %	1.625
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466	0 %	1.466
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092	0 %	3.092
NSK (1 μ -like ring): ν_μ CCQE	2.191	1.891	2.648	40 %	1.135
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.033	1.228	1.719	40 %	0.7368
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1518	40 %	0.06507
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.3081	40 %	0.132
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	4.827	40 %	2.069
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %	0.09042
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %	0.07761
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %	0.168
NSK (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01507	0 %	0.01507
NSK (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.01243	0 %	0.01243
NSK (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004036	0 %	0.0004036
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003007	0 %	0.003007
NSK (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.0309	0 %	0.0309
NSK (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %	0.04942
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %	0.05768
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %	0.1071
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.001058	40 %	0.0004533
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0005852	0.0007237	0.001013	40 %	0.0004342
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	9.839e-05	40 %	4.217e-05
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0003035	40 %	0.0001301
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.002473	40 %	0.00106
NSK (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %	0.005916
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %	0.005954
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %	0.01187
NSK (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.08288	0 %	0.08288
NSK (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.03527	0 %	0.03527
NSK (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.001949	0 %	0.001949
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006716	0 %	0.0006716
NSK (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.1208	0 %	0.1208

Table 109: Effect of $f_{CC\bar{\nu};t}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5e-05$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ		BANFF tuned -1 σ	
NSK (1 μ -like ring)	59.41	58.37	58.37	0.000233 %	58.37	-0.000233 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r < 0.4$ GeV)	3.802	3.653	3.654	0.00363 %	3.653	-0.00363 %
NSK (1 μ -like ring): ν_μ CCQE ($0.4 \leq E_r < 1.1$ GeV)	14.98	13.78	13.78	0 %	13.78	0 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r \geq 1.1$ GeV)	14.5	12.85	12.85	0 %	12.85	0 %
NSK (1 μ -like ring): ν_μ CCQE	33.28	30.29	30.29	0.0004379 %	30.29	-0.0004379 %
NSK (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	16.93	0 %	16.93	0 %
NSK (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.3997	0 %	0.3997	0 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	3.771	0 %	3.771	0 %
NSK (1 μ -like ring): ν_μ CC all	52.19	51.39	51.39	0.0002581 %	51.39	-0.0002581 %
NSK (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625	0 %	1.625	0 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466	0 %	1.466	0 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092	0 %	3.092	0 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r < 0.4$ GeV)	0.09866	0.09305	0.09306	0.00363 %	0.09305	-0.00363 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($0.4 \leq E_r < 1.1$ GeV)	0.3816	0.3585	0.3585	0 %	0.3585	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($E_r \geq 1.1$ GeV)	1.71	1.44	1.44	0 %	1.44	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	2.191	1.891	1.891	0.0001786 %	1.891	-0.0001786 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.033	1.228	1.228	0 %	1.228	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1084	0 %	0.1084	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.22	0 %	0.22	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.448	9.799e-05 %	3.448	-9.799e-05 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %	0.09042	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %	0.07761	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %	0.168	0 %
NSK (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01507	0 %	0.01507	0 %
NSK (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.01243	0 %	0.01243	0 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004036	0 %	0.0004036	0 %
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003007	0 %	0.003007	0 %
NSK (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.0309	0 %	0.0309	0 %
NSK (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %	0.04942	0 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %	0.05768	0 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %	0.1071	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.0007554	0 %	0.0007554	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0005852	0.0007237	0.0007237	0 %	0.0007237	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	7.028e-05	0 %	7.028e-05	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0002168	0 %	0.0002168	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.001766	0 %	0.001766	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %	0.005916	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %	0.005954	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %	0.01187	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.08288	0 %	0.08288	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.03527	0 %	0.03527	0 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.001949	0 %	0.001949	0 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006716	0 %	0.0006716	0 %
NSK (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.1208	0 %	0.1208	0 %

Table 110: Effect of $f_{0;t,r}^{FSI}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5e-05$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NSK (1 μ -like ring)	59.41	58.37	58.38 0.01726 %	58.36 -0.01726 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r < 0.4$ GeV)	3.802	3.653	3.653 0 %	3.653 0 %
NSK (1 μ -like ring): ν_μ CCQE ($0.4 \leq E_r < 1.1$ GeV)	14.98	13.78	13.79 0.07128 %	13.77 -0.07128 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r \geq 1.1$ GeV)	14.5	12.85	12.85 0 %	12.85 0 %
NSK (1 μ -like ring): ν_μ CCQE	33.28	30.29	30.3 0.03243 %	30.28 -0.03243 %
NSK (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	16.93 0 %	16.93 0 %
NSK (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.3997 0 %	0.3997 0 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	3.771 0 %	3.771 0 %
NSK (1 μ -like ring): ν_μ CC all	52.19	51.39	51.4 0.01911 %	51.38 -0.01911 %
NSK (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625 0 %	1.625 0 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466 0 %	1.466 0 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092 0 %	3.092 0 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r < 0.4$ GeV)	0.09866	0.09305	0.09305 0 %	0.09305 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($0.4 \leq E_r < 1.1$ GeV)	0.3816	0.3585	0.3587 0.07128 %	0.3582 -0.07128 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($E_r \geq 1.1$ GeV)	1.71	1.44	1.44 0 %	1.44 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	2.191	1.891	1.891 0.01351 %	1.891 -0.01351 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.033	1.228	1.228 0 %	1.228 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1084 0 %	0.1084 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.22 0 %	0.22 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.448 0.007411 %	3.447 -0.007411 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042 0 %	0.09042 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761 0 %	0.07761 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168 0 %	0.168 0 %
NSK (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01507 0 %	0.01507 0 %
NSK (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.01243 0 %	0.01243 0 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004036 0 %	0.0004036 0 %
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003007 0 %	0.003007 0 %
NSK (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.0309 0 %	0.0309 0 %
NSK (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942 0 %	0.04942 0 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768 0 %	0.05768 0 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071 0 %	0.1071 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.0007554 0 %	0.0007554 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0005852	0.0007237	0.0007237 0 %	0.0007237 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	7.028e-05 0 %	7.028e-05 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0002168 0 %	0.0002168 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.001766 0 %	0.001766 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916 0 %	0.005916 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954 0 %	0.005954 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187 0 %	0.01187 0 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.08288 0 %	0.08288 0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.03527 0 %	0.03527 0 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.001949 0 %	0.001949 0 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006716 0 %	0.0006716 0 %
NSK (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.1208 0 %	0.1208 0 %

Table 111: Effect of $f_{1;t,r}^{FSI}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5e-05$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NSK (1 μ -like ring)	59.41	58.37	58.41 0.06803 %	58.33 -0.06803 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r < 0.4$ GeV)	3.802	3.653	3.653 0 %	3.653 0 %
NSK (1 μ -like ring): ν_μ CCQE ($0.4 \leq E_r < 1.1$ GeV)	14.98	13.78	13.78 0 %	13.78 0 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r \geq 1.1$ GeV)	14.5	12.85	12.89 0.2778 %	12.82 -0.2778 %
NSK (1 μ -like ring): ν_μ CCQE	33.28	30.29	30.32 0.1179 %	30.25 -0.1179 %
NSK (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	16.93 0 %	16.93 0 %
NSK (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.3997 0 %	0.3997 0 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	3.771 0 %	3.771 0 %
NSK (1 μ -like ring): ν_μ CC all	52.19	51.39	51.42 0.06949 %	51.35 -0.06949 %
NSK (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625 0 %	1.625 0 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466 0 %	1.466 0 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092 0 %	3.092 0 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r < 0.4$ GeV)	0.09866	0.09305	0.09305 0 %	0.09305 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($0.4 \leq E_r < 1.1$ GeV)	0.3816	0.3585	0.3585 0 %	0.3585 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($E_r \geq 1.1$ GeV)	1.71	1.44	1.444 0.2778 %	1.436 -0.2778 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	2.191	1.891	1.895 0.2115 %	1.887 -0.2115 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.033	1.228	1.228 0 %	1.228 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1084 0 %	0.1084 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.22 0 %	0.22 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.452 0.116 %	3.444 -0.116 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042 0 %	0.09042 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761 0 %	0.07761 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168 0 %	0.168 0 %
NSK (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01507 0 %	0.01507 0 %
NSK (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.01243 0 %	0.01243 0 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004036 0 %	0.0004036 0 %
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003007 0 %	0.003007 0 %
NSK (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.0309 0 %	0.0309 0 %
NSK (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942 0 %	0.04942 0 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768 0 %	0.05768 0 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071 0 %	0.1071 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.0007554 0 %	0.0007554 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0005852	0.0007237	0.0007237 0 %	0.0007237 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	7.028e-05 0 %	7.028e-05 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0002168 0 %	0.0002168 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.001766 0 %	0.001766 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916 0 %	0.005916 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954 0 %	0.005954 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187 0 %	0.01187 0 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.08288 0 %	0.08288 0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.03527 0 %	0.03527 0 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.001949 0 %	0.001949 0 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006716 0 %	0.0006716 0 %
NSK (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.1208 0 %	0.1208 0 %

Table 112: Effect of $f_{2;t,r}^{FSI}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5e-05$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ		BANFF tuned -1 σ	
NSK (1 μ -like ring)	59.41	58.37	60.33	3.362 %	56.41	-3.362 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r < 0.4$ GeV)	3.802	3.653	3.653	0 %	3.653	0 %
NSK (1 μ -like ring): ν_μ CCQE ($0.4 \leq E_r < 1.1$ GeV)	14.98	13.78	13.78	0 %	13.78	0 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r \geq 1.1$ GeV)	14.5	12.85	12.85	0 %	12.85	0 %
NSK (1 μ -like ring): ν_μ CCQE	33.28	30.29	30.29	0 %	30.29	0 %
NSK (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	18.4	8.66 %	15.47	-8.66 %
NSK (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.4343	8.66 %	0.3651	-8.66 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	4.098	8.66 %	3.444	-8.66 %
NSK (1 μ -like ring): ν_μ CC all	52.19	51.39	53.22	3.556 %	49.56	-3.556 %
NSK (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625	0 %	1.625	0 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466	0 %	1.466	0 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092	0 %	3.092	0 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r < 0.4$ GeV)	0.09866	0.09305	0.09305	0 %	0.09305	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($0.4 \leq E_r < 1.1$ GeV)	0.3816	0.3585	0.3585	0 %	0.3585	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($E_r \geq 1.1$ GeV)	1.71	1.44	1.44	0 %	1.44	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	2.191	1.891	1.891	0 %	1.891	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.033	1.228	1.334	8.66 %	1.122	-8.66 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1178	8.66 %	0.09905	-8.66 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.2391	8.66 %	0.201	-8.66 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.582	3.91 %	3.313	-3.91 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042	0 %	0.09042	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761	0 %	0.07761	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168	0 %	0.168	0 %
NSK (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01507	0 %	0.01507	0 %
NSK (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.01243	0 %	0.01243	0 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004036	0 %	0.0004036	0 %
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003007	0 %	0.003007	0 %
NSK (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.0309	0 %	0.0309	0 %
NSK (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942	0 %	0.04942	0 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768	0 %	0.05768	0 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071	0 %	0.1071	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.0007554	0 %	0.0007554	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0005852	0.0007237	0.0007237	0 %	0.0007237	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	7.028e-05	0 %	7.028e-05	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0002168	0 %	0.0002168	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.001766	0 %	0.001766	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916	0 %	0.005916	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954	0 %	0.005954	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187	0 %	0.01187	0 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.08288	0 %	0.08288	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.03527	0 %	0.03527	0 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.001949	0 %	0.001949	0 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006716	0 %	0.0006716	0 %
NSK (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.1208	0 %	0.1208	0 %

Table 113: Effect of $f_{3;t,r}^{FSI}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5e-05$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ	BANFF tuned -1 σ
NSK (1 μ -like ring)	59.41	58.37	58.37 0.002964 %	58.37 -0.002964 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r < 0.4$ GeV)	3.802	3.653	3.653 0 %	3.653 0 %
NSK (1 μ -like ring): ν_μ CCQE ($0.4 \leq E_r < 1.1$ GeV)	14.98	13.78	13.78 0 %	13.78 0 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r \geq 1.1$ GeV)	14.5	12.85	12.85 0 %	12.85 0 %
NSK (1 μ -like ring): ν_μ CCQE	33.28	30.29	30.29 0 %	30.29 0 %
NSK (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	16.93 0 %	16.93 0 %
NSK (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.3997 0 %	0.3997 0 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	3.771 0 %	3.771 0 %
NSK (1 μ -like ring): ν_μ CC all	52.19	51.39	51.39 0 %	51.39 0 %
NSK (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.625 0 %	1.625 0 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.466 0 %	1.466 0 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	3.092 0 %	3.092 0 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r < 0.4$ GeV)	0.09866	0.09305	0.09305 0 %	0.09305 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($0.4 \leq E_r < 1.1$ GeV)	0.3816	0.3585	0.3585 0 %	0.3585 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($E_r \geq 1.1$ GeV)	1.71	1.44	1.44 0 %	1.44 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	2.191	1.891	1.891 0 %	1.891 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.033	1.228	1.228 0 %	1.228 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1084 0 %	0.1084 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.22 0 %	0.22 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.448 0 %	3.448 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09042 0 %	0.09042 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.07761 0 %	0.07761 0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.168 0 %	0.168 0 %
NSK (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01524 1.128 %	0.0149 -1.128 %
NSK (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.01257 1.128 %	0.01229 -1.128 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004082 1.128 %	0.0003991 -1.128 %
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003041 1.128 %	0.002973 -1.128 %
NSK (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.03125 1.128 %	0.03056 -1.128 %
NSK (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.04942 0 %	0.04942 0 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.05768 0 %	0.05768 0 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1071 0 %	0.1071 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.000764 1.128 %	0.0007469 -1.128 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0005852	0.0007237	0.0007318 1.128 %	0.0007155 -1.128 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	7.107e-05 1.128 %	6.949e-05 -1.128 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0002192 1.128 %	0.0002143 -1.128 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.001786 1.128 %	0.001746 -1.128 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.005916 0 %	0.005916 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.005954 0 %	0.005954 0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01187 0 %	0.01187 0 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.08382 1.128 %	0.08195 -1.128 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.03567 1.128 %	0.03487 -1.128 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.001971 1.128 %	0.001927 -1.128 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006792 1.128 %	0.000664 -1.128 %
NSK (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.1221 1.128 %	0.1194 -1.128 %

Table 114: Effect of $f_{4;t,r}^{FSI}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5e-05$; $\Delta m_{32}^2 = 0.0024$.

Component	Nominal	BANFF tuned	BANFF tuned +1 σ		BANFF tuned -1 σ	
			58.63	0.4479 %	58.11	-0.4479 %
NSK (1 μ -like ring)	59.41	58.37				
NSK (1 μ -like ring): ν_μ CCQE ($E_r < 0.4$ GeV)	3.802	3.653	3.653	0 %	3.653	0 %
NSK (1 μ -like ring): ν_μ CCQE ($0.4 \leq E_r < 1.1$ GeV)	14.98	13.78	13.78	0 %	13.78	0 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r \geq 1.1$ GeV)	14.5	12.85	12.85	0 %	12.85	0 %
NSK (1 μ -like ring): ν_μ CCQE	33.28	30.29	30.29	0 %	30.29	0 %
NSK (1 μ -like ring): ν_μ CC 1 π	14.63	16.93	16.93	0 %	16.93	0 %
NSK (1 μ -like ring): ν_μ CC coherent	0.4206	0.3997	0.3997	0 %	0.3997	0 %
NSK (1 μ -like ring): ν_μ CC other (ν_μ disp)	3.862	3.771	3.771	0 %	3.771	0 %
NSK (1 μ -like ring): ν_μ CC all	52.19	51.39	51.39	0 %	51.39	0 %
NSK (1 μ -like ring): ν_μ/ν_τ NC 1 $\pi^{+/-}$	1.697	1.625	1.751	7.737 %	1.5	-7.737 %
NSK (1 μ -like ring): ν_μ/ν_τ NC other (ν_μ app)	1.522	1.466	1.58	7.737 %	1.353	-7.737 %
NSK (1 μ -like ring): ν_μ NC all	3.218	3.092	3.331	7.737 %	2.853	-7.737 %
NSK (1 μ -like ring): ν_μ CCQE ($E_r < 0.4$ GeV)	0.09866	0.09305	0.09305	0 %	0.09305	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($0.4 \leq E_r < 1.1$ GeV)	0.3816	0.3585	0.3585	0 %	0.3585	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE ($E_r \geq 1.1$ GeV)	1.71	1.44	1.44	0 %	1.44	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CCQE	2.191	1.891	1.891	0 %	1.891	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC 1 π	1.033	1.228	1.228	0 %	1.228	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC coherent	0.1129	0.1084	0.1084	0 %	0.1084	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC other (ν_μ disp)	0.2251	0.22	0.22	0 %	0.22	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ CC all	3.562	3.448	3.448	0 %	3.448	0 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC 1 $\pi^{+/-}$	0.09198	0.09042	0.09742	7.737 %	0.08343	-7.737 %
NSK (1 μ -like ring): $\bar{\nu}_\mu/\bar{\nu}_\tau$ NC other (ν_μ app)	0.07958	0.07761	0.08362	7.737 %	0.07161	-7.737 %
NSK (1 μ -like ring): $\bar{\nu}_\mu$ NC all	0.1716	0.168	0.181	7.737 %	0.155	-7.737 %
NSK (1 μ -like ring): ν_e CCQE	0.01575	0.01507	0.01507	0 %	0.01507	0 %
NSK (1 μ -like ring): ν_e CC 1 π	0.009421	0.01243	0.01243	0 %	0.01243	0 %
NSK (1 μ -like ring): ν_e CC coherent	0.0004036	0.0004036	0.0004036	0 %	0.0004036	0 %
NSK (1 μ -like ring): ν_e CC other (ν_μ disp)	0.003005	0.003007	0.003007	0 %	0.003007	0 %
NSK (1 μ -like ring): ν_e CC all	0.02858	0.0309	0.0309	0 %	0.0309	0 %
NSK (1 μ -like ring): ν_e NC 1 $\pi^{+/-}$	0.04865	0.04942	0.05324	7.737 %	0.0456	-7.737 %
NSK (1 μ -like ring): ν_e NC other (ν_μ app)	0.05741	0.05768	0.06215	7.737 %	0.05322	-7.737 %
NSK (1 μ -like ring): ν_e NC all	0.1061	0.1071	0.1154	7.737 %	0.09882	-7.737 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CCQE	0.0007903	0.0007554	0.0007554	0 %	0.0007554	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC 1 π	0.0005852	0.0007237	0.0007237	0 %	0.0007237	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC coherent	7.028e-05	7.028e-05	7.028e-05	0 %	7.028e-05	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC other (ν_μ disp)	0.0002167	0.0002168	0.0002168	0 %	0.0002168	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ CC all	0.001662	0.001766	0.001766	0 %	0.001766	0 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC 1 $\pi^{+/-}$	0.005805	0.005916	0.006374	7.737 %	0.005458	-7.737 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC other (ν_μ app)	0.005918	0.005954	0.006415	7.737 %	0.005493	-7.737 %
NSK (1 μ -like ring): $\bar{\nu}_e$ NC all	0.01172	0.01187	0.01279	7.737 %	0.01095	-7.737 %
NSK (1 μ -like ring): oscillation ν_e CCQE	0.08742	0.08288	0.08288	0 %	0.08288	0 %
NSK (1 μ -like ring): oscillation ν_e CC 1 π	0.02732	0.03527	0.03527	0 %	0.03527	0 %
NSK (1 μ -like ring): oscillation ν_e CC coherent	0.002039	0.001949	0.001949	0 %	0.001949	0 %
NSK (1 μ -like ring): oscillation ν_e CC other (ν_μ app)	0.0007229	0.0006716	0.0006716	0 %	0.0006716	0 %
NSK (1 μ -like ring): oscillation ν_e CC all	0.1175	0.1208	0.1208	0 %	0.1208	0 %

Table 115: Effect of $f_{5;t,r}^{FSI}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5e-05$; $\Delta m_{32}^2 = 0.0024$.

1342 **F. Detailed study of the effect of systematics on the predicted reconstructed energy spectrum of 1 μ -like ring
1343 events**

1344 In this section, the effect of systematics on the predicted reconstructed energy spectrum in SuperK is presented in a
1345 number of figures. Each figure shows the total nominal predicted spectrum (the sum of all SuperK MC modes) and the
1346 total spectra resulting from -3, -1, +1, and $+3\sigma$ variations of a single systematic parameter. For correlated systematic
1347 parameters, σ is defined as the square root of the diagonal entry in the corresponding covariance matrix.

1348 Figs. 198-245 show the effects of systematics on the SuperK E_{reco} spectrum with no oscillations applied (all
1349 mixing angles set to zero). Figs. 246-293 show the effect of systematics on the SuperK E_{reco} spectrum with 3-flavour
1350 oscillations in matter, using the following values of the oscillation parameters:

- 1351 • $\sin^2 2\theta_{12} = 0.857$
- 1352 • $\sin^2 2\theta_{13} = 0.098$
- 1353 • $\sin^2 2\theta_{23} = 1.0$
- 1354 • $\delta_{CP} = 0$
- 1355 • $\Delta m_{12}^2 = 7.5 \times 10^{-5} \text{ eV}^2/\text{c}^4$
- 1356 • $\Delta m_{32}^2 = 2.4 \times 10^{-3} \text{ eV}^2/\text{c}^4$

1357 It should be noted that, for ease of comparison, there are only two vertical axis scales used in the lower 'ratio' plots.
1358 For systematics with a small effect, the vertical axis runs from 0.75 to 1.25; for systematics with a larger effect, the
1359 vertical axis runs from 0.25 to 1.75.

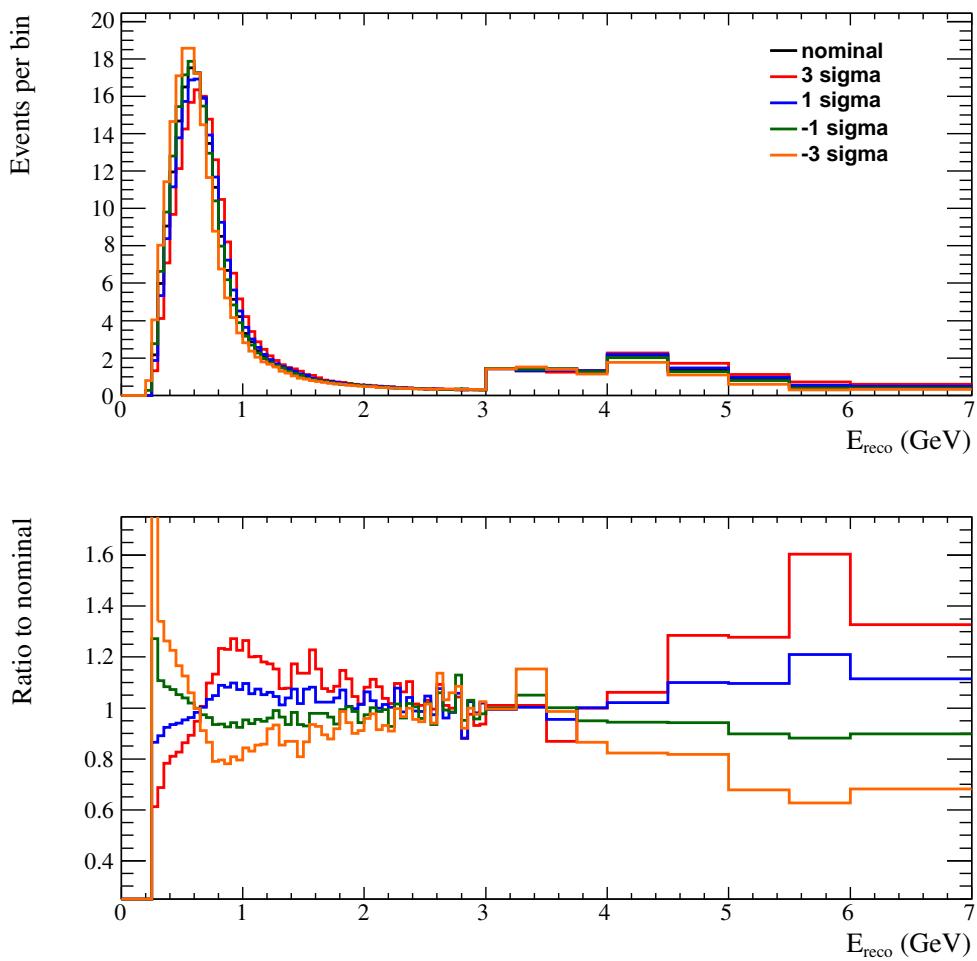


Figure 198: Effect of $f_{E;r}^{SK}$ for no oscillations (all mixing angles set to 0).

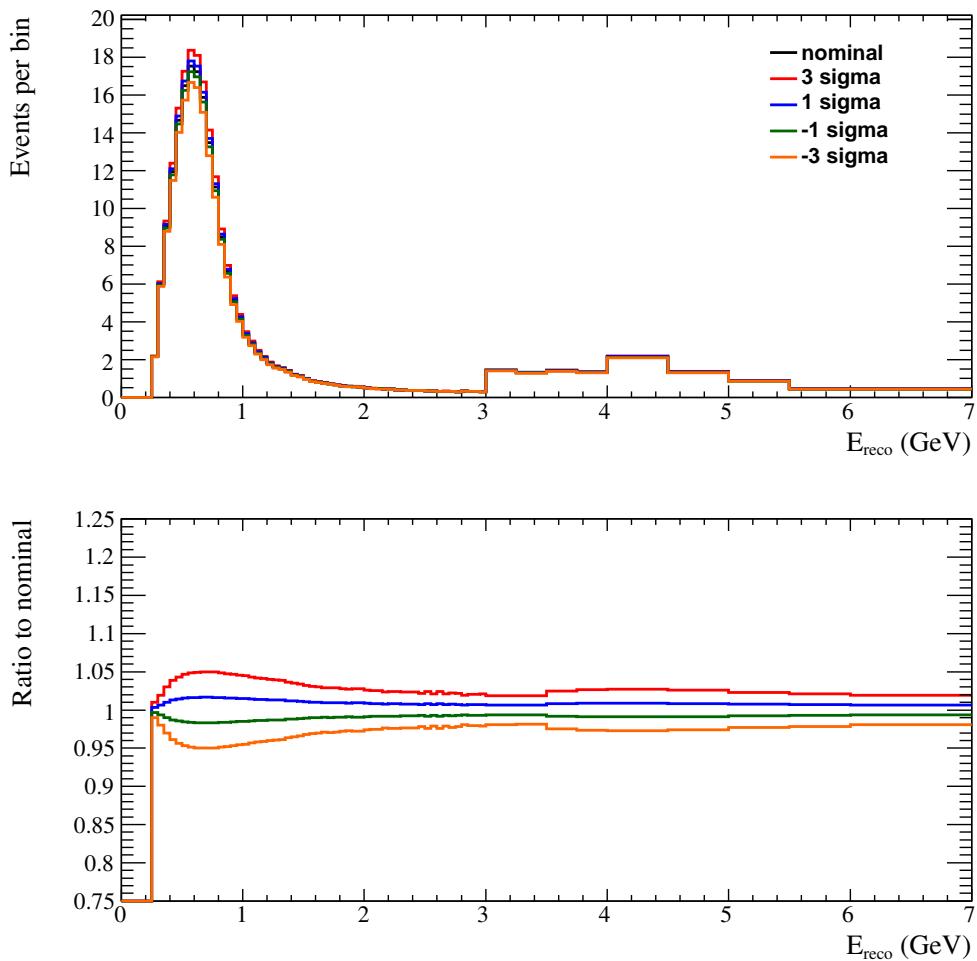


Figure 199: Effect of $f_{CCQEoth;r}^{SK}$ for no oscillations (all mixing angles set to 0).

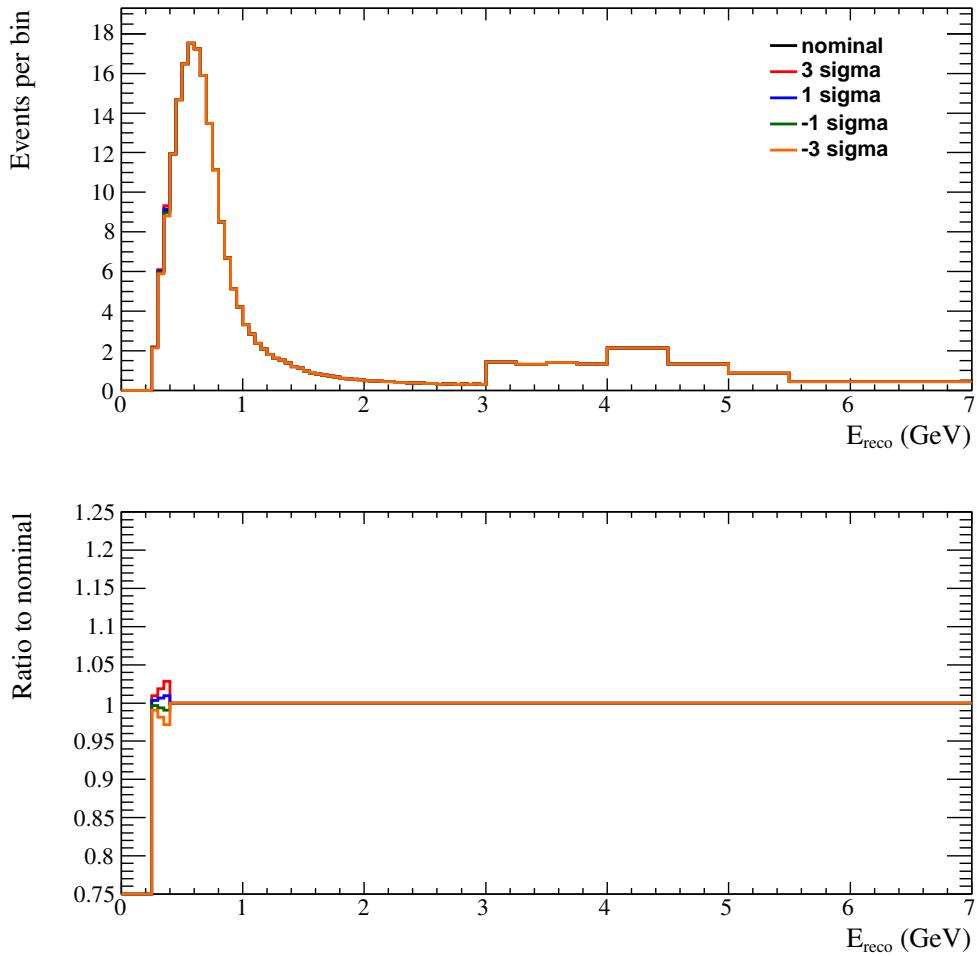


Figure 200: Effect of $f_{CCQERC0;r}^{SK}$ for no oscillations (all mixing angles set to 0).

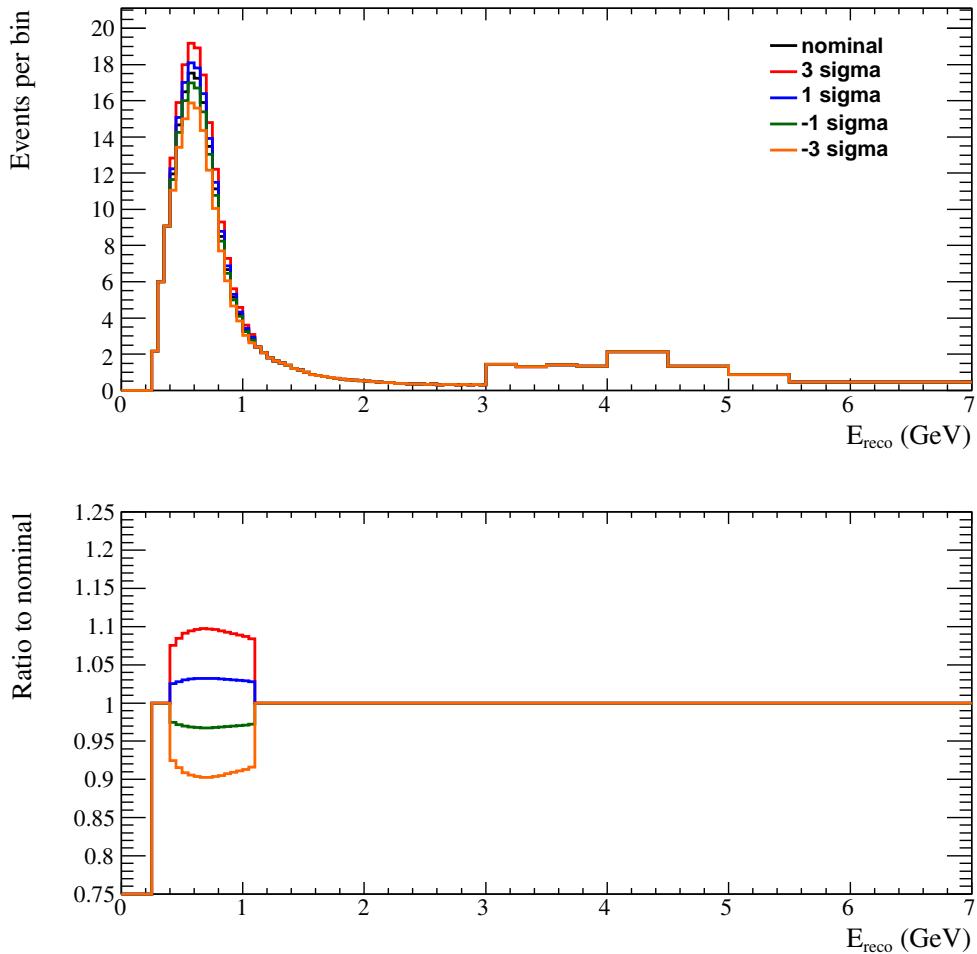


Figure 201: Effect of $f_{CCERC1;r}^{SK}$ for no oscillations (all mixing angles set to 0).

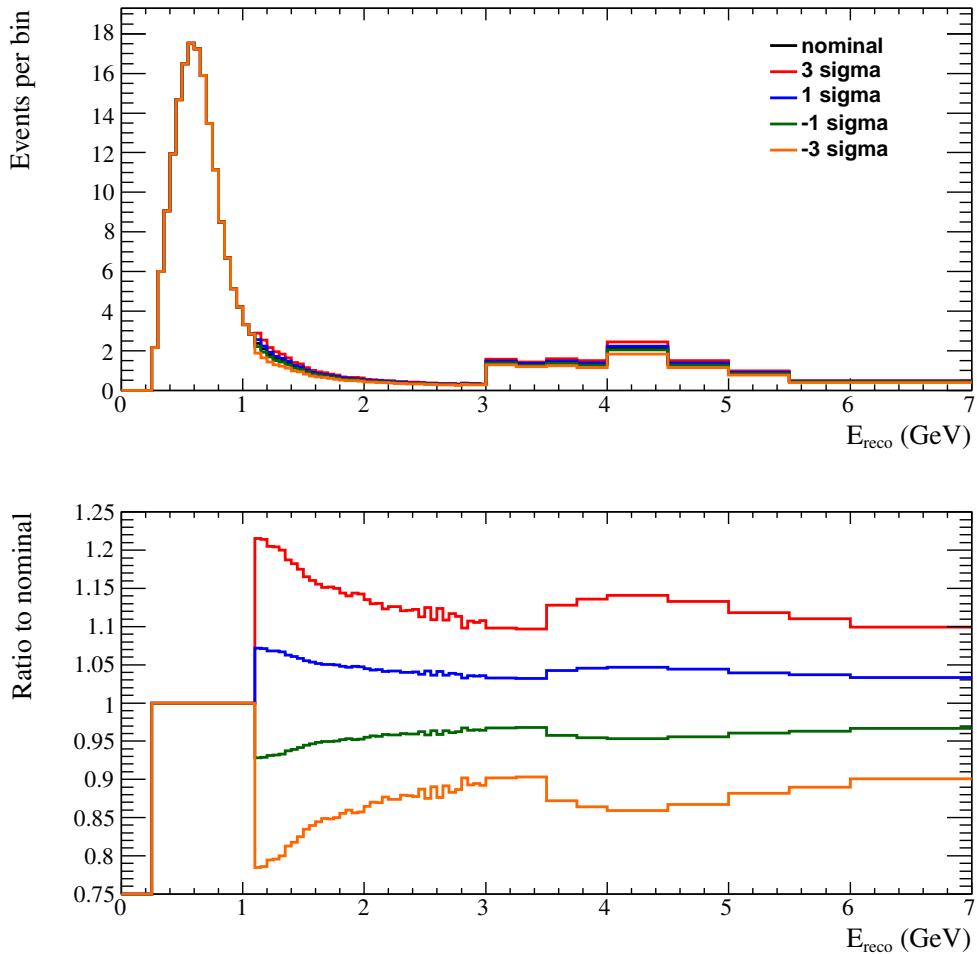


Figure 202: Effect of $f_{CCQERC2;r}^{SK}$ for no oscillations (all mixing angles set to 0).

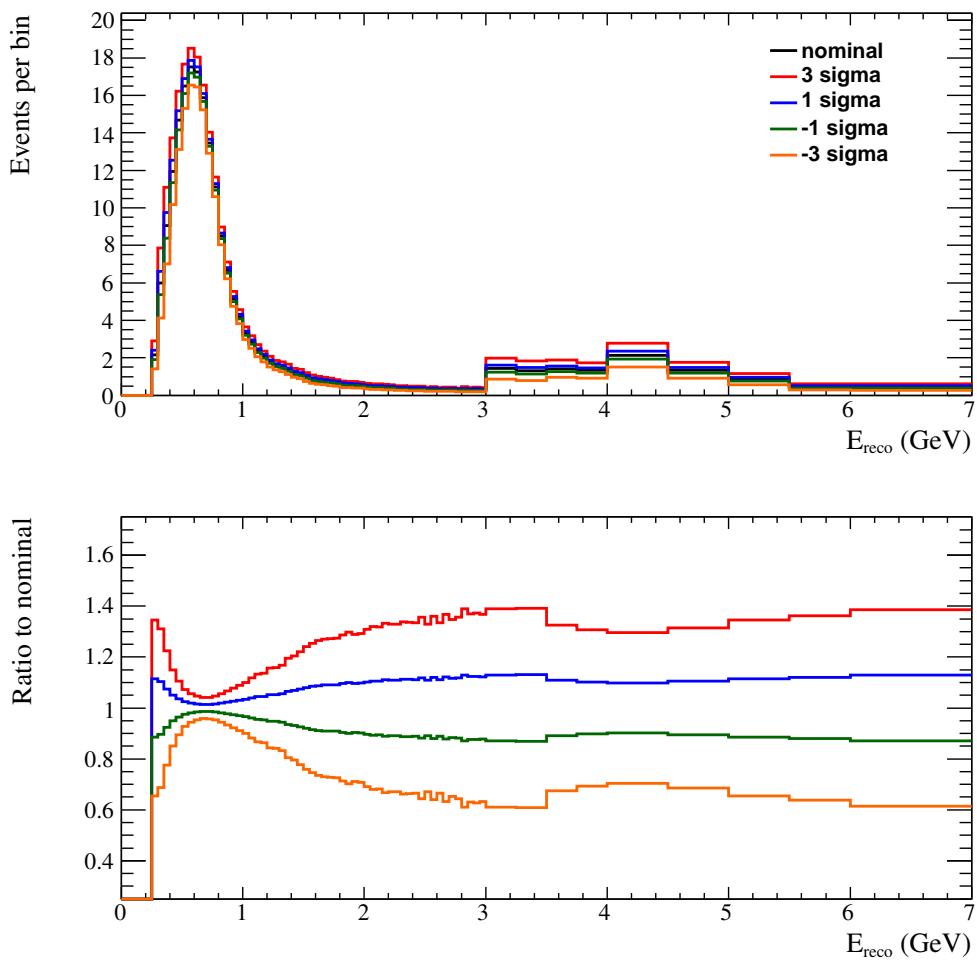


Figure 203: Effect of $f_{CCnQE;r}^{SK}$ for no oscillations (all mixing angles set to 0).

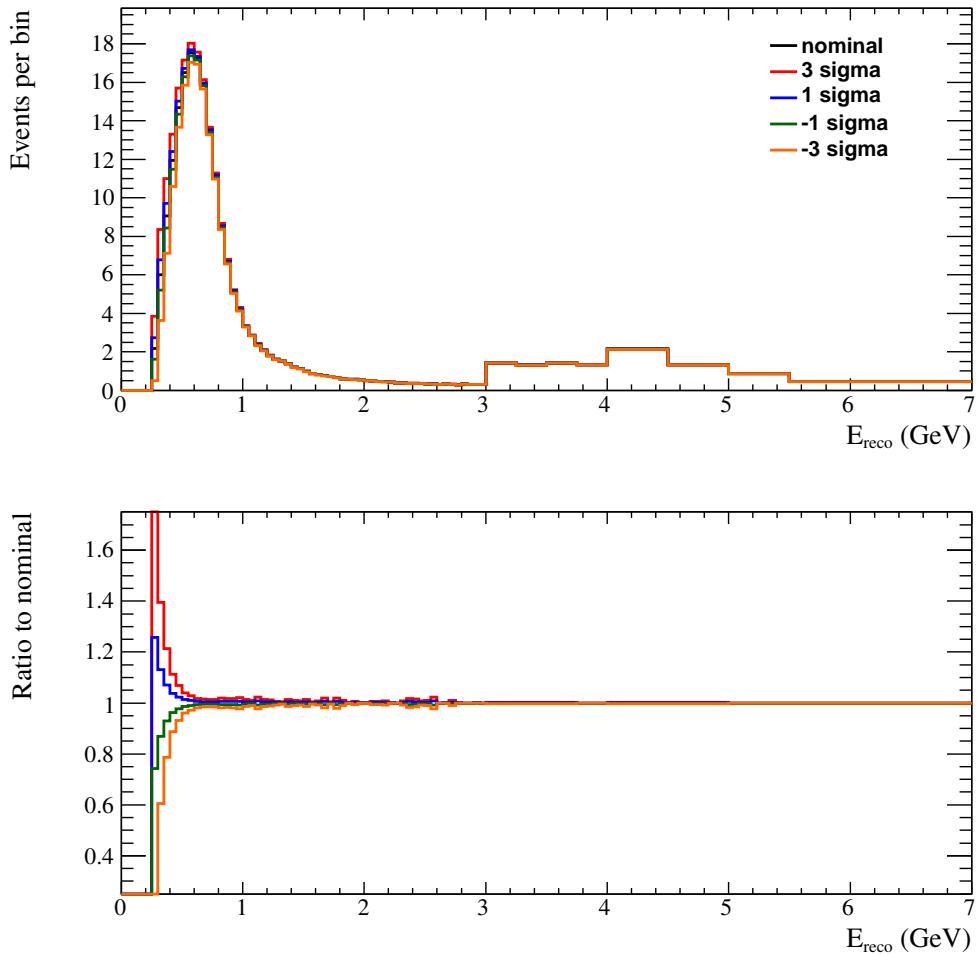


Figure 204: Effect of $f_{NC;r}^{SK}$ for no oscillations (all mixing angles set to 0).

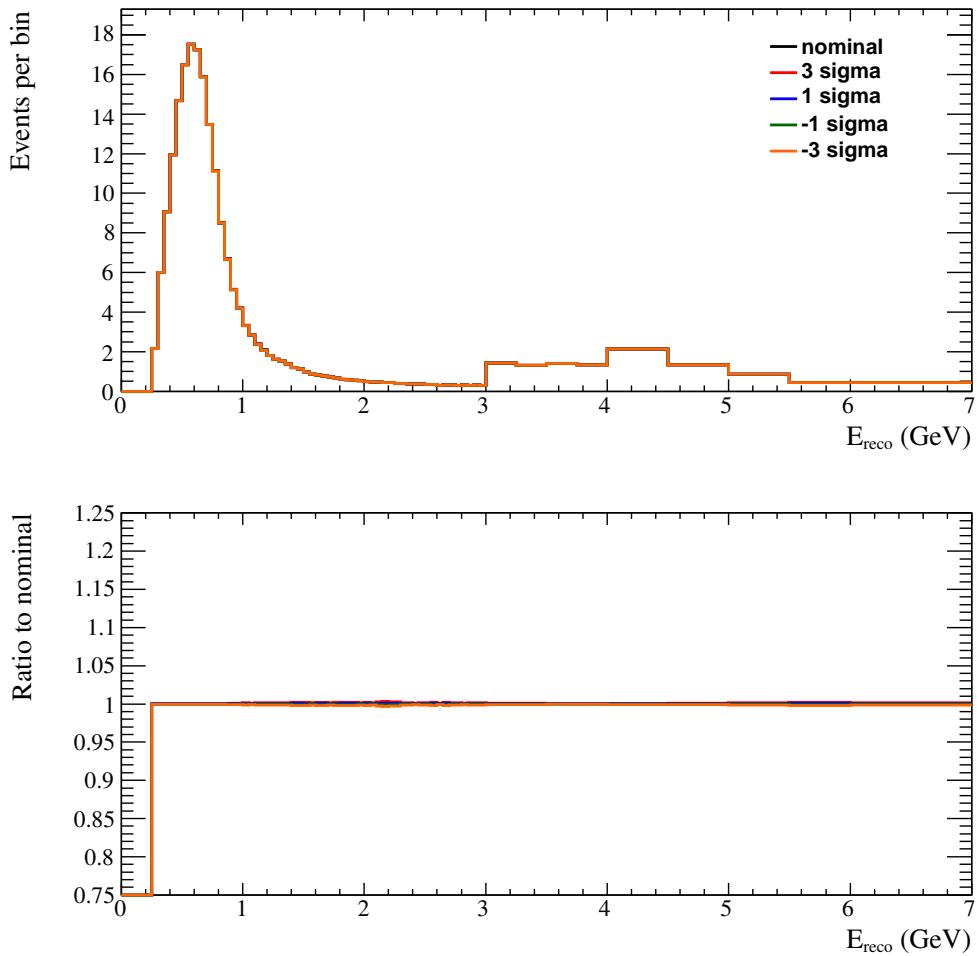


Figure 205: Effect of $f_{\nu_e; r}^{SK}$ for no oscillations (all mixing angles set to 0).

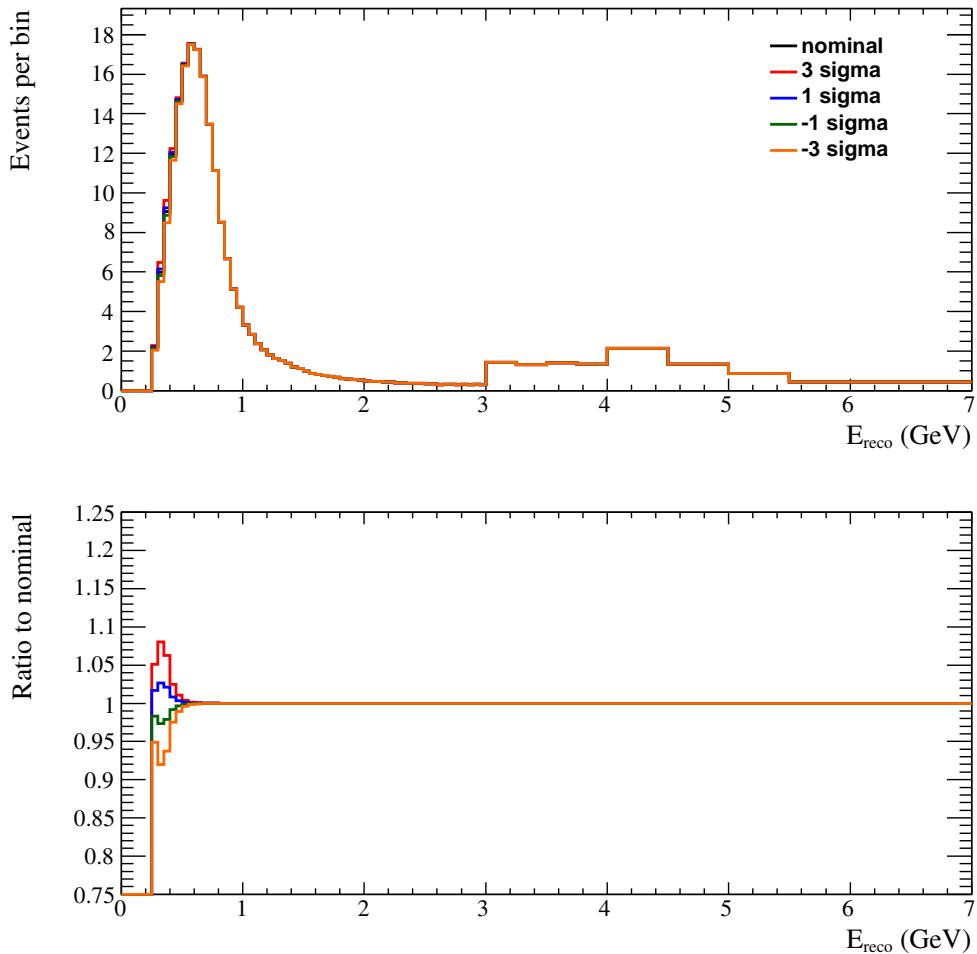


Figure 206: Effect of $f_{0;t,r}^{\text{banff}}$ for no oscillations (all mixing angles set to 0).

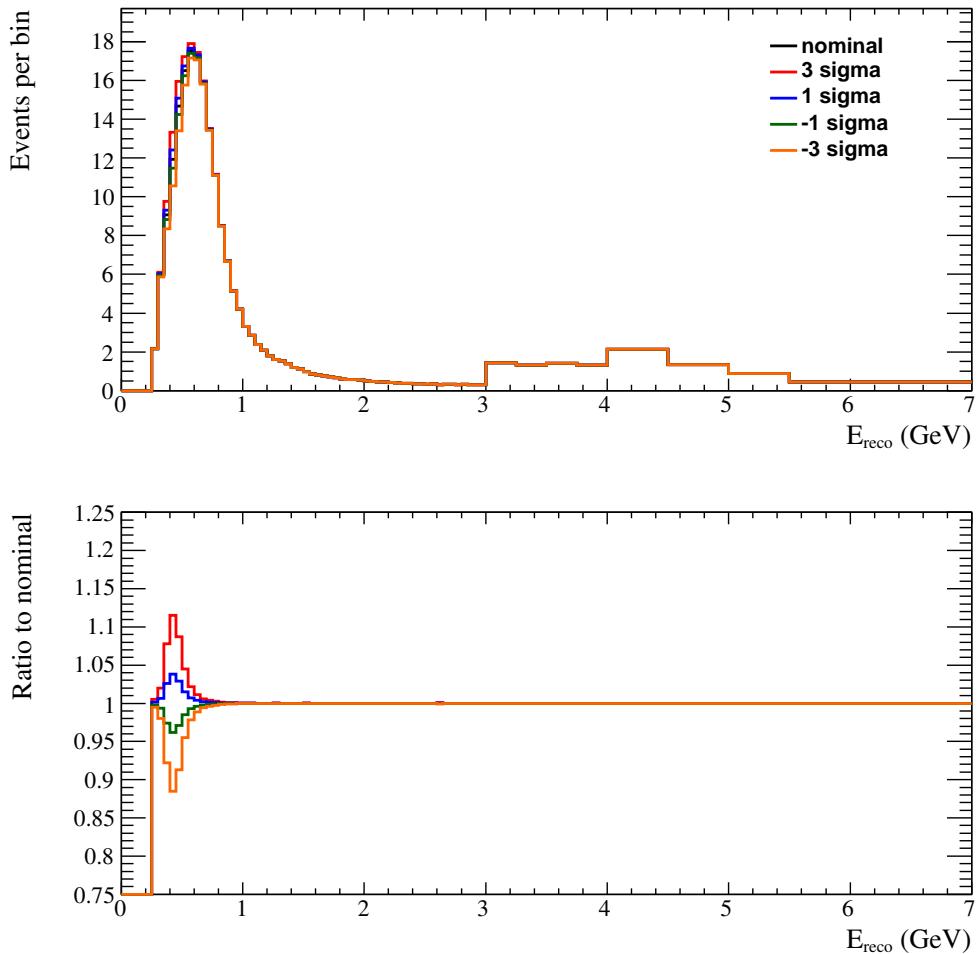


Figure 207: Effect of $f_{1;t,r}^{\text{banff}}$ for no oscillations (all mixing angles set to 0).

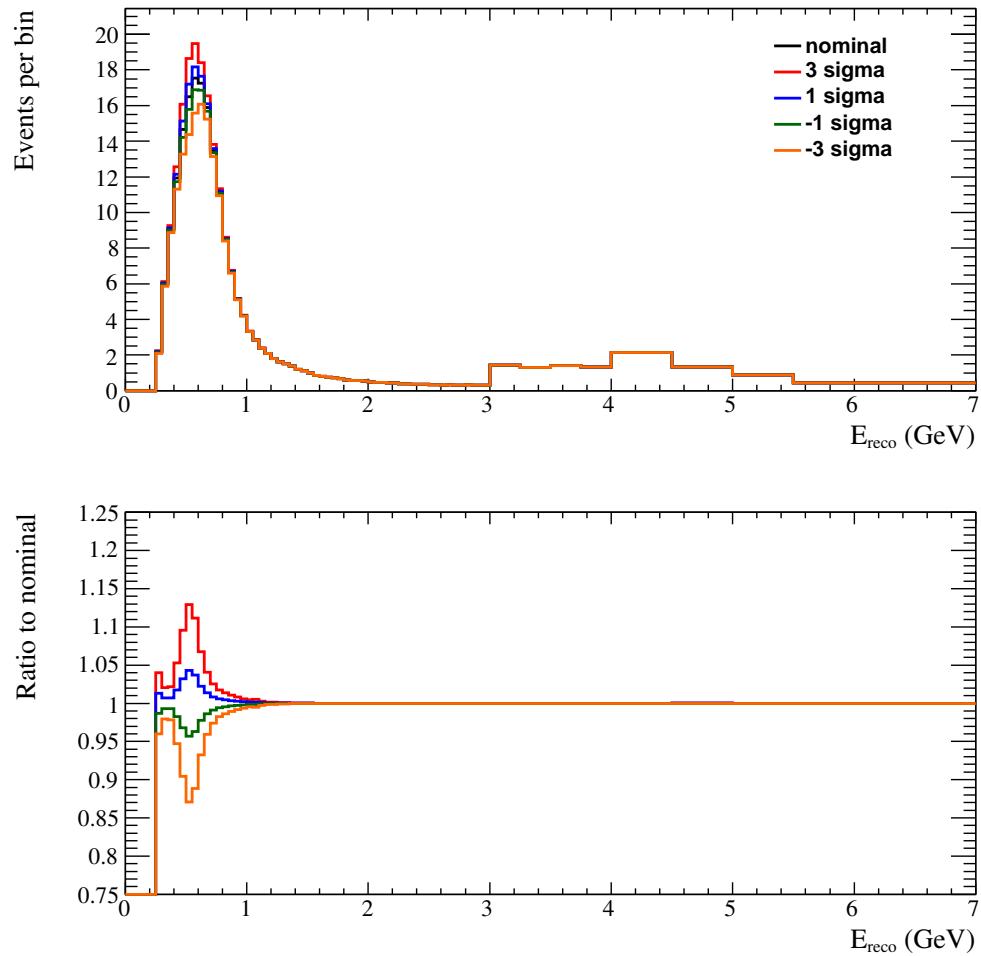


Figure 208: Effect of $f_{2;t,r}^{\text{banff}}$ for no oscillations (all mixing angles set to 0).

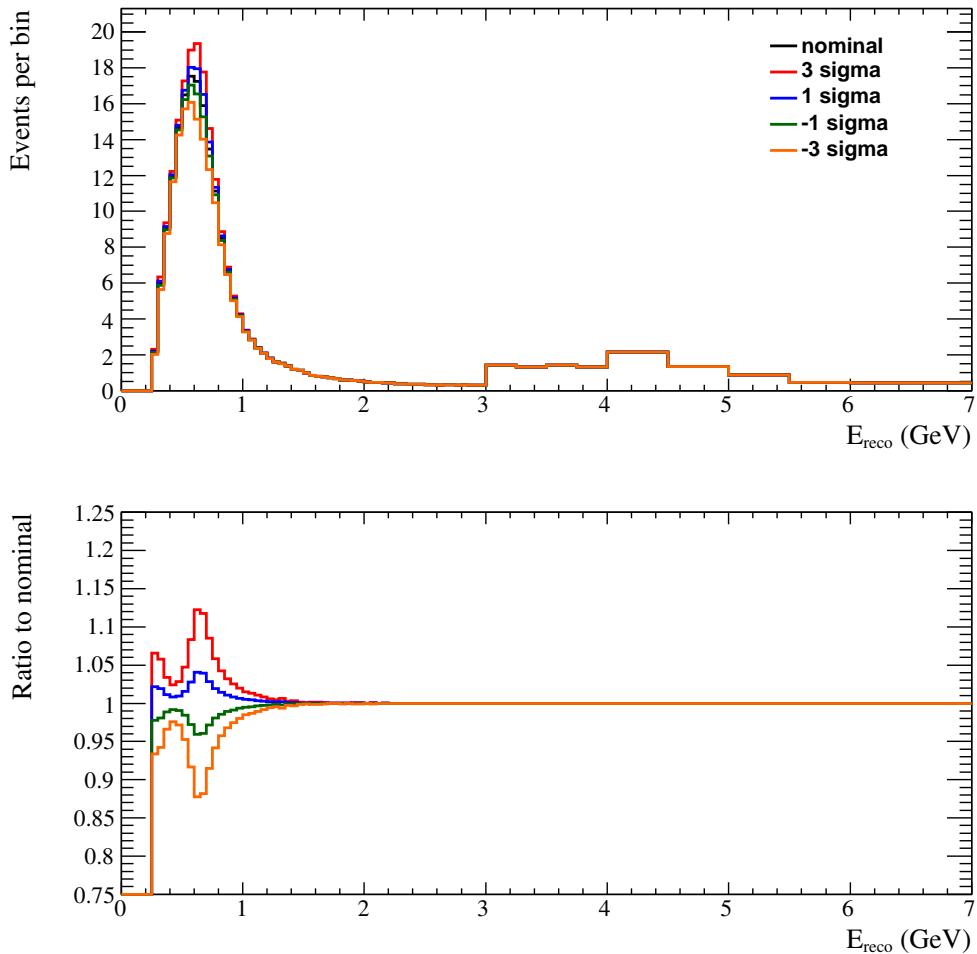


Figure 209: Effect of $f_{3;t,r}^{\text{banff}}$ for no oscillations (all mixing angles set to 0).

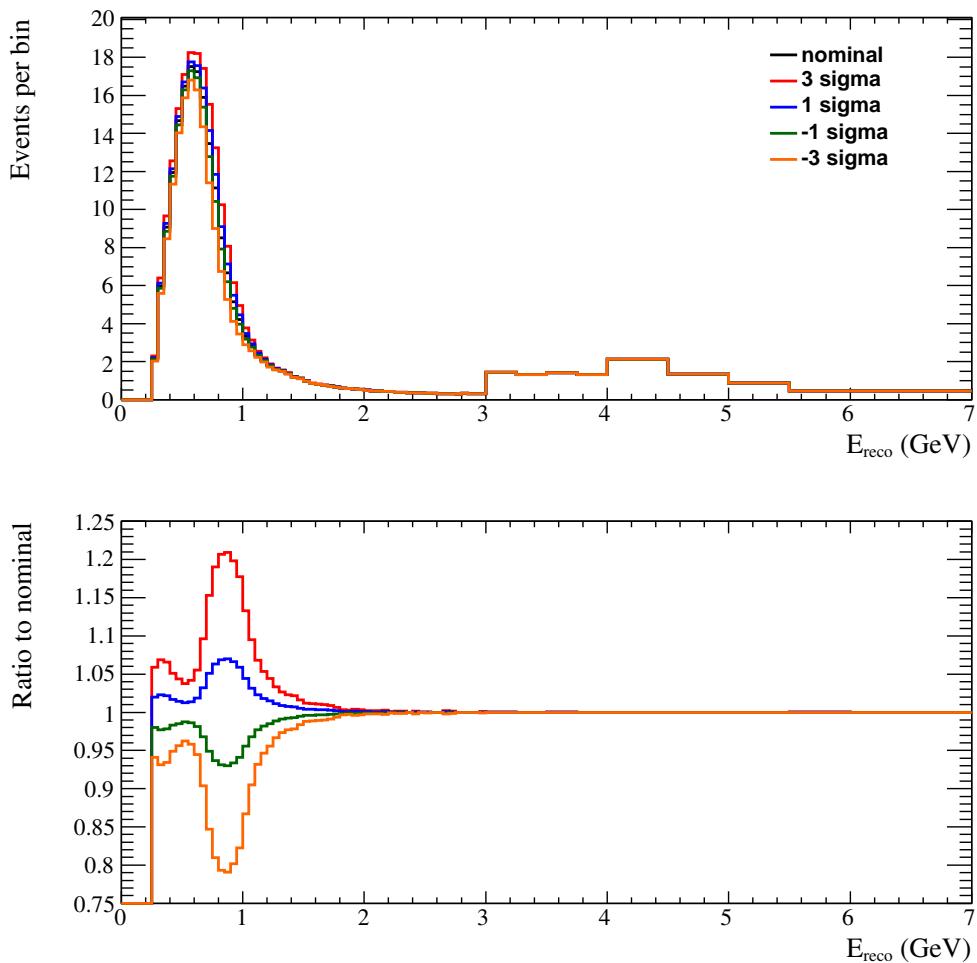


Figure 210: Effect of $f_{4;t,r}^{\text{banff}}$ for no oscillations (all mixing angles set to 0).

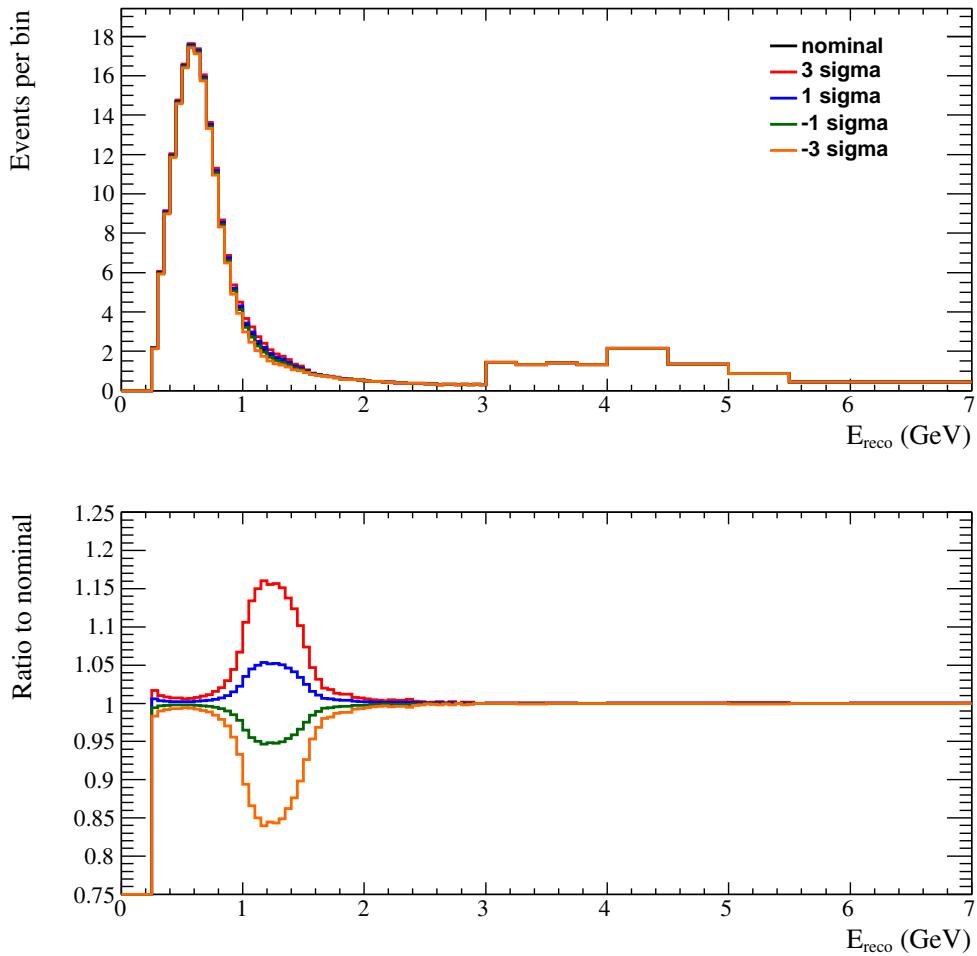


Figure 211: Effect of $f_{5;t,r}^{\text{banff}}$ for no oscillations (all mixing angles set to 0).

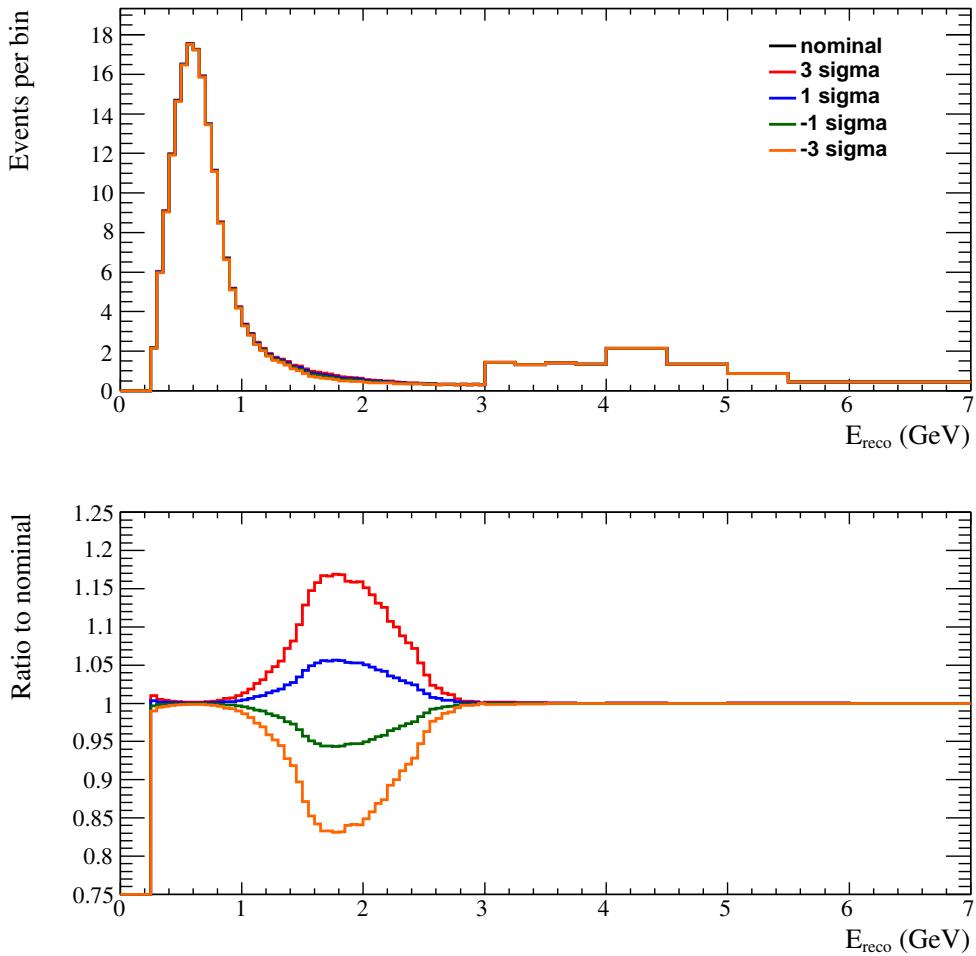


Figure 212: Effect of $f_{6;t,r}^{\text{banff}}$ for no oscillations (all mixing angles set to 0).

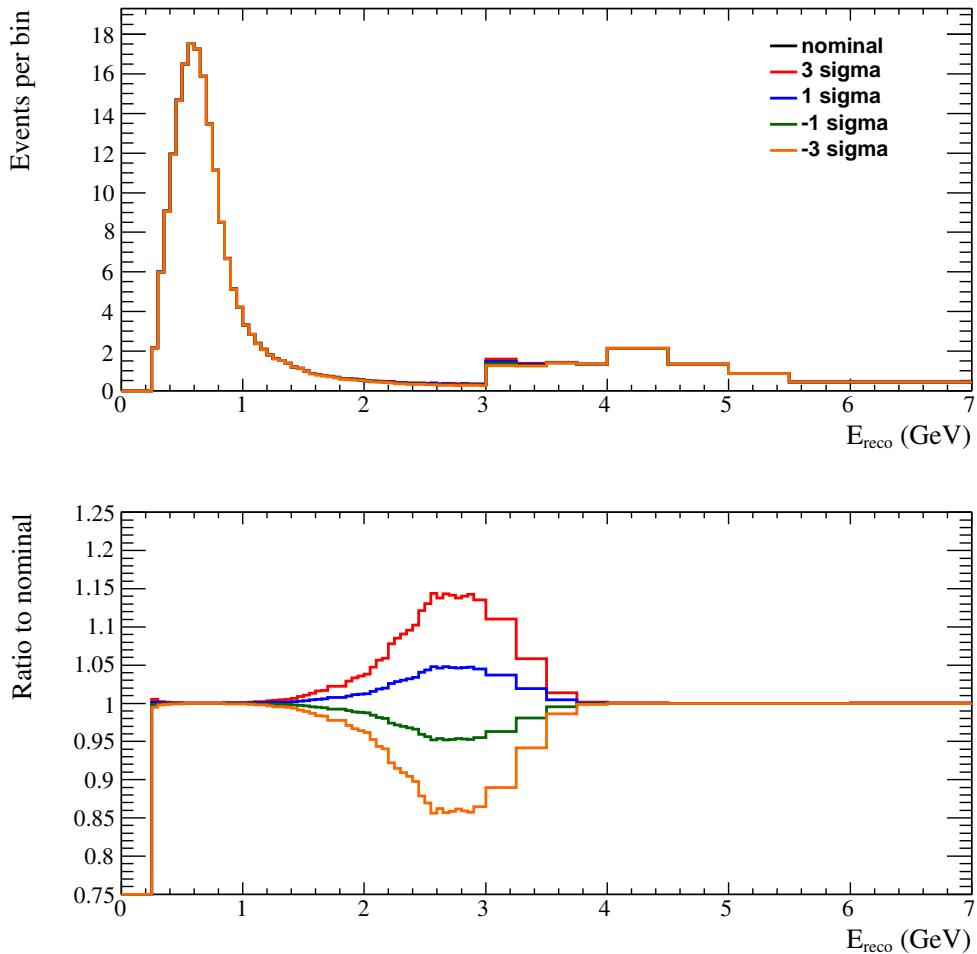


Figure 213: Effect of $f_{7;t,r}^{\text{banff}}$ for no oscillations (all mixing angles set to 0).

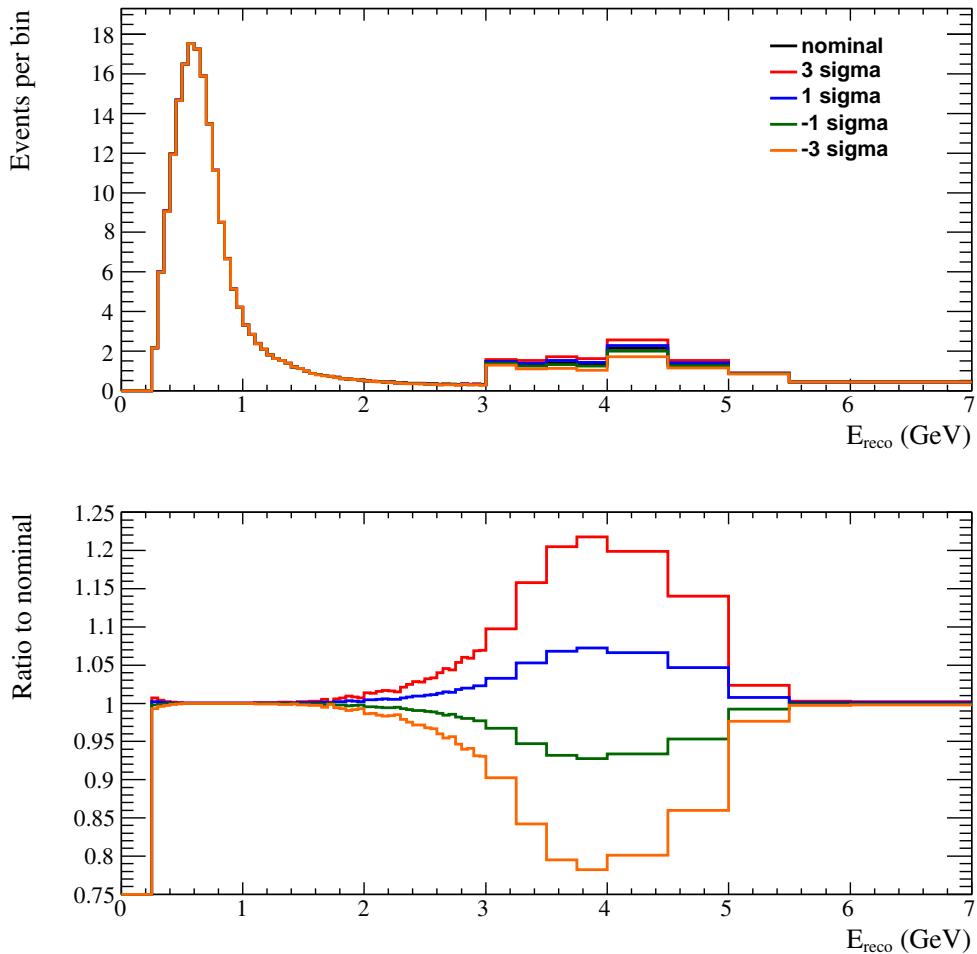


Figure 214: Effect of $f_{8;t,r}^{\text{banff}}$ for no oscillations (all mixing angles set to 0).

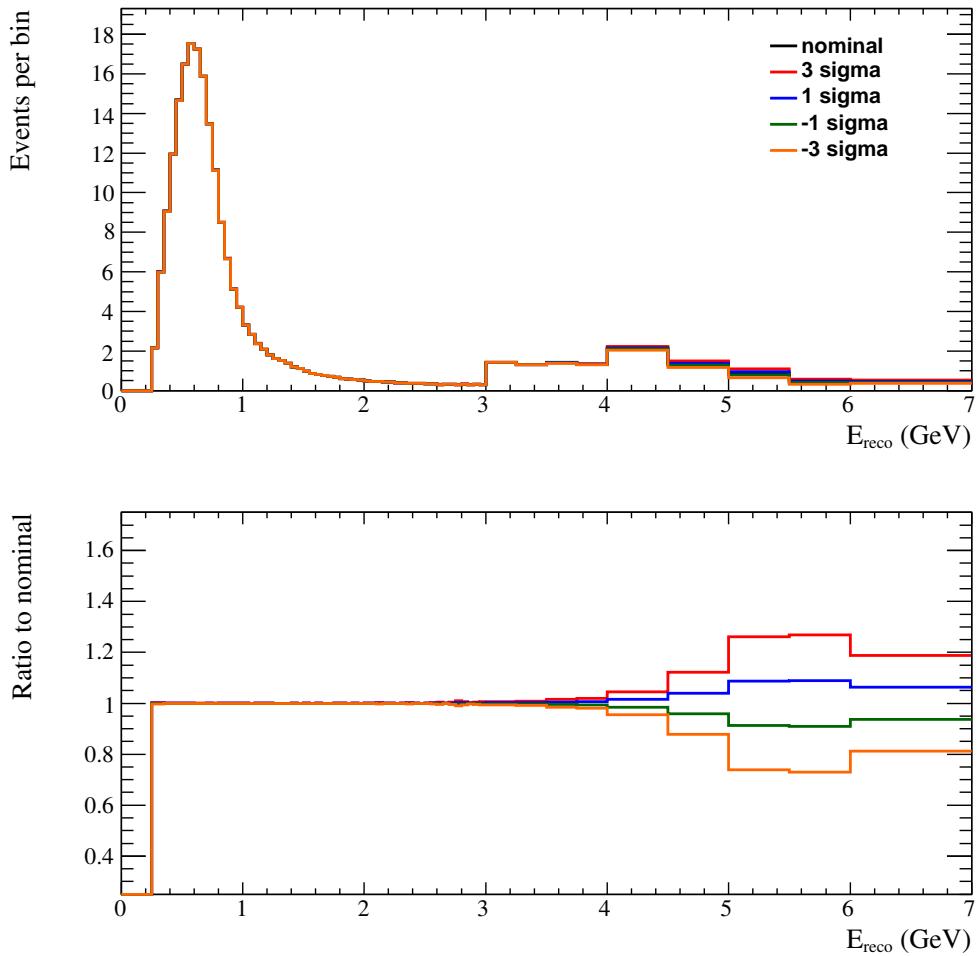


Figure 215: Effect of $f_{9;t,r}^{\text{banff}}$ for no oscillations (all mixing angles set to 0).

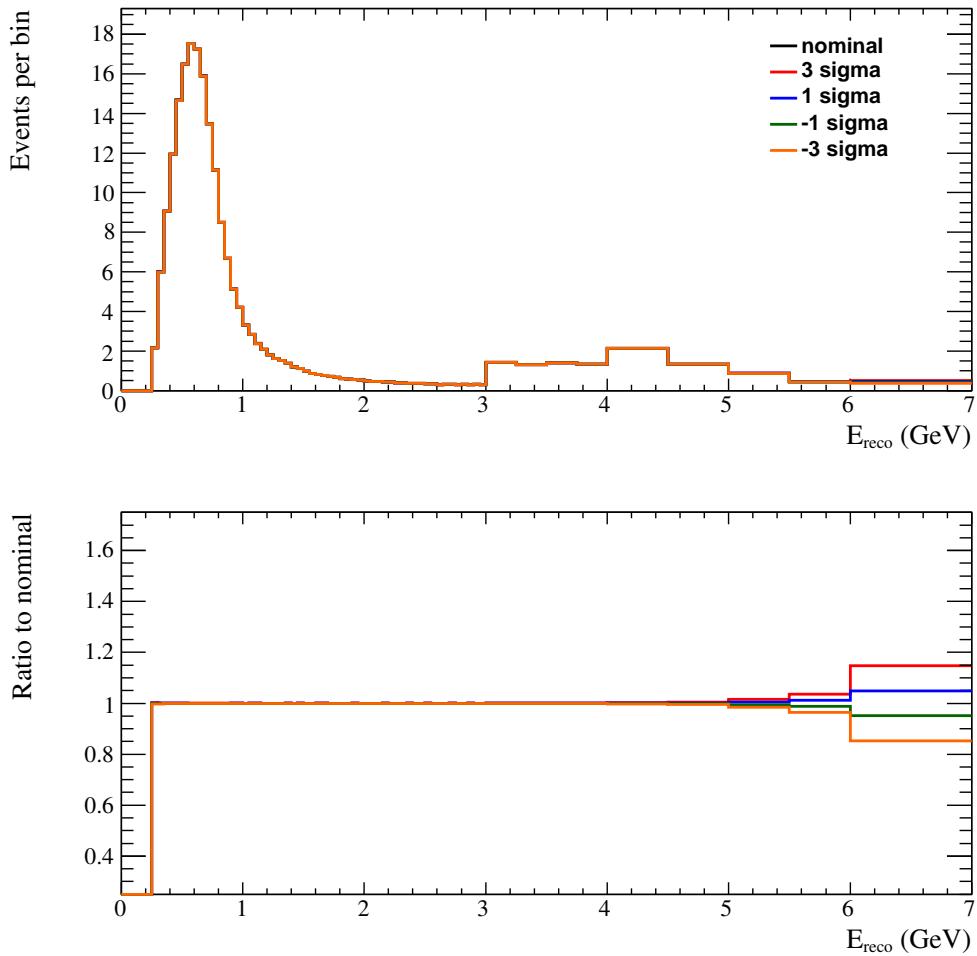


Figure 216: Effect of $f_{10;t,r}^{\text{banff}}$ for no oscillations (all mixing angles set to 0).

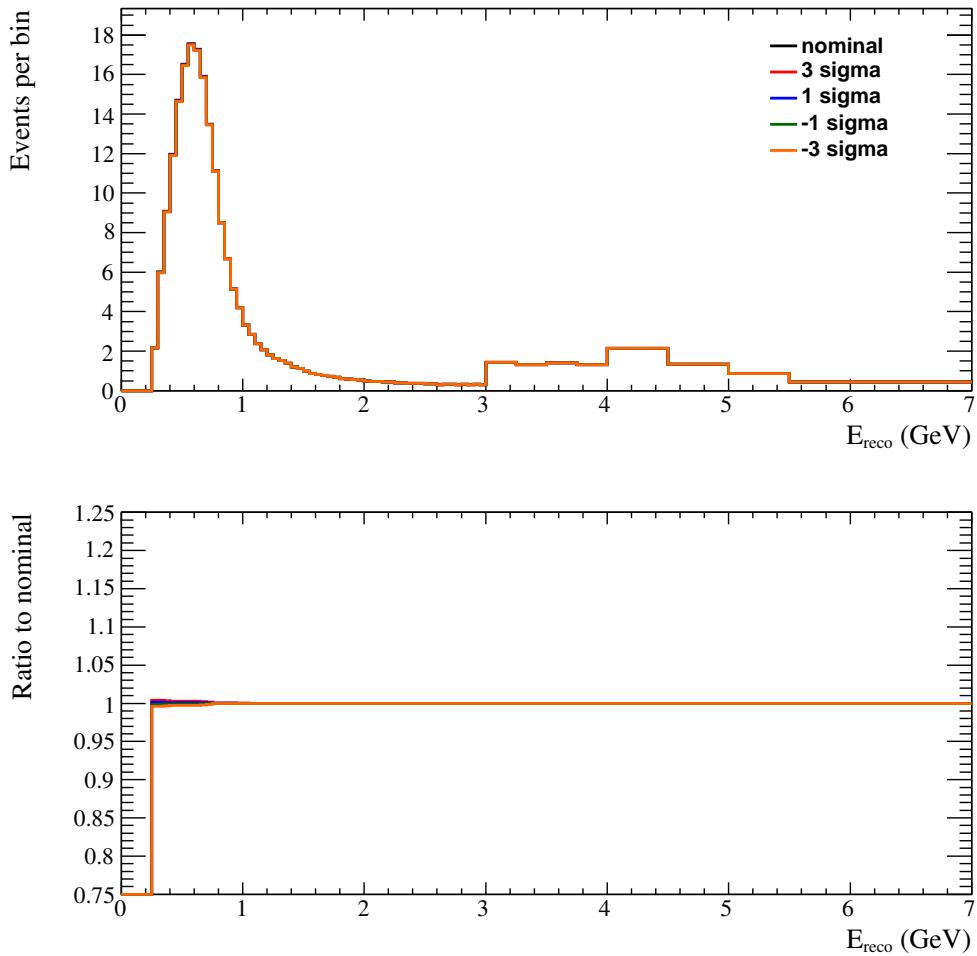


Figure 217: Effect of $f_{11;t,r}^{\text{banff}}$ for no oscillations (all mixing angles set to 0).

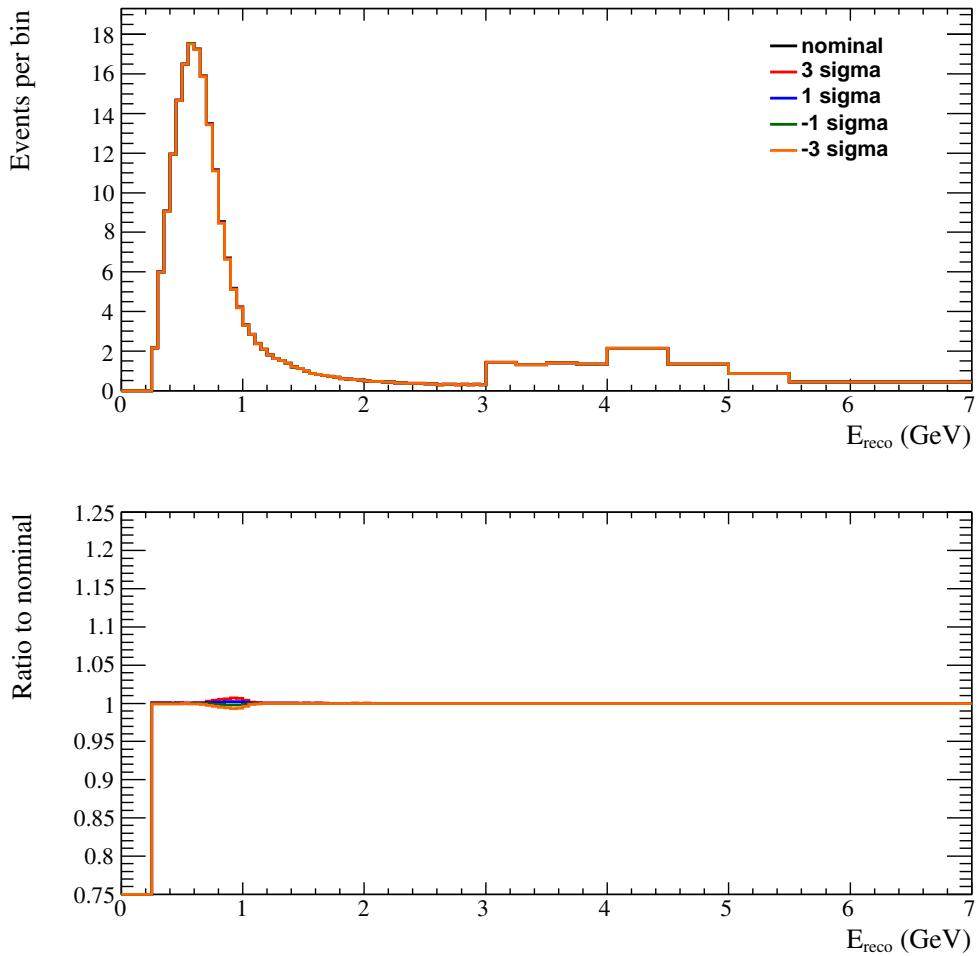


Figure 218: Effect of $f_{12;t,r}^{\text{banff}}$ for no oscillations (all mixing angles set to 0).

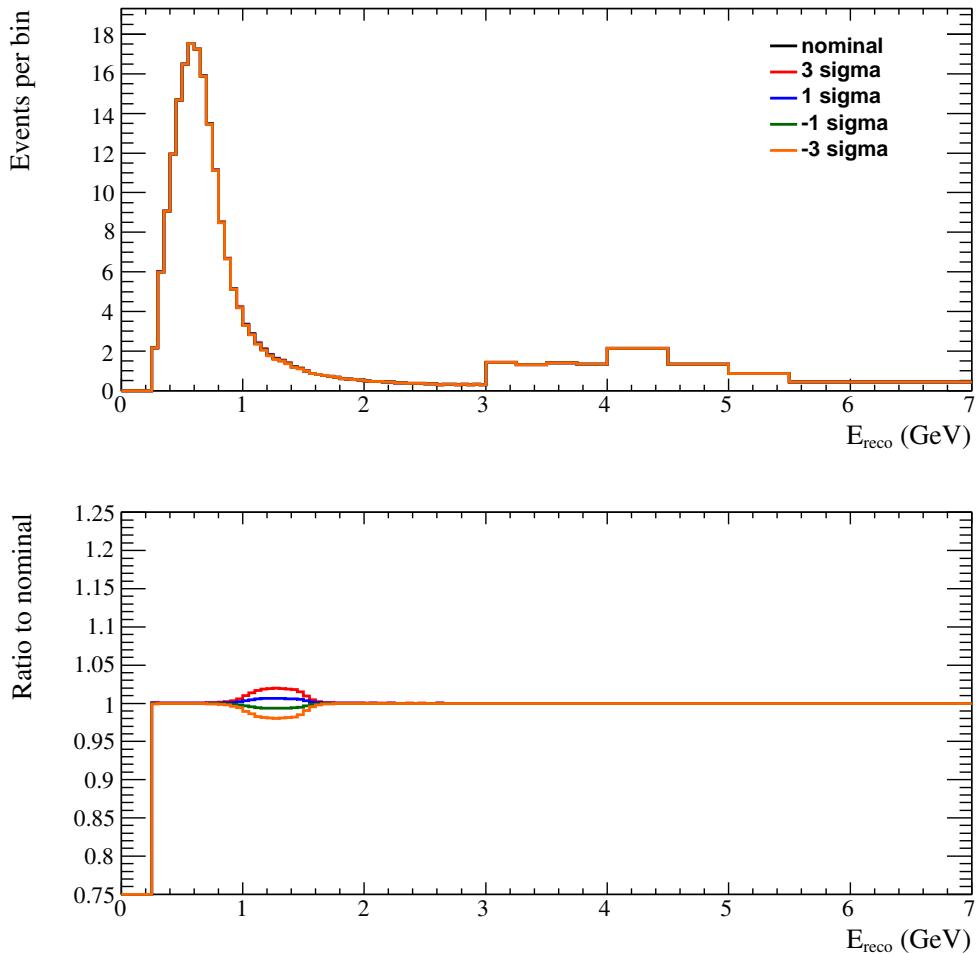


Figure 219: Effect of $f_{13;t,r}^{\text{banff}}$ for no oscillations (all mixing angles set to 0).

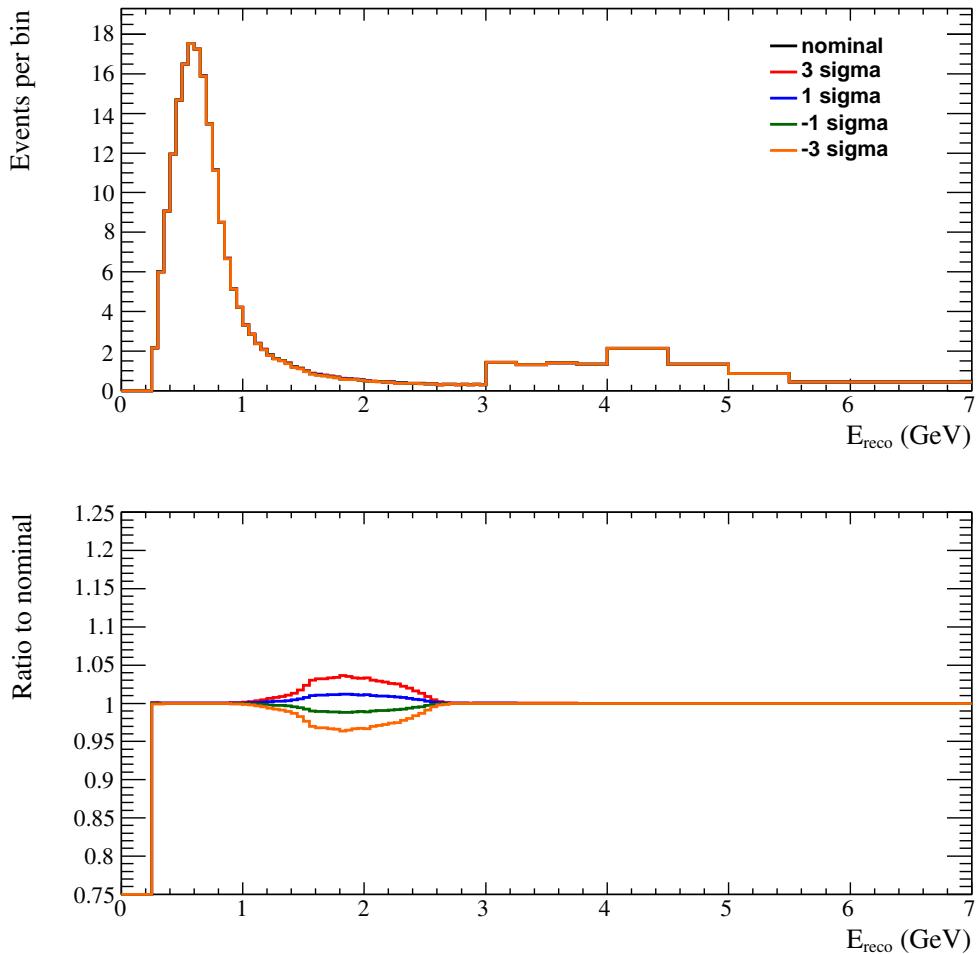


Figure 220: Effect of $f_{14;t,r}^{\text{banff}}$ for no oscillations (all mixing angles set to 0).

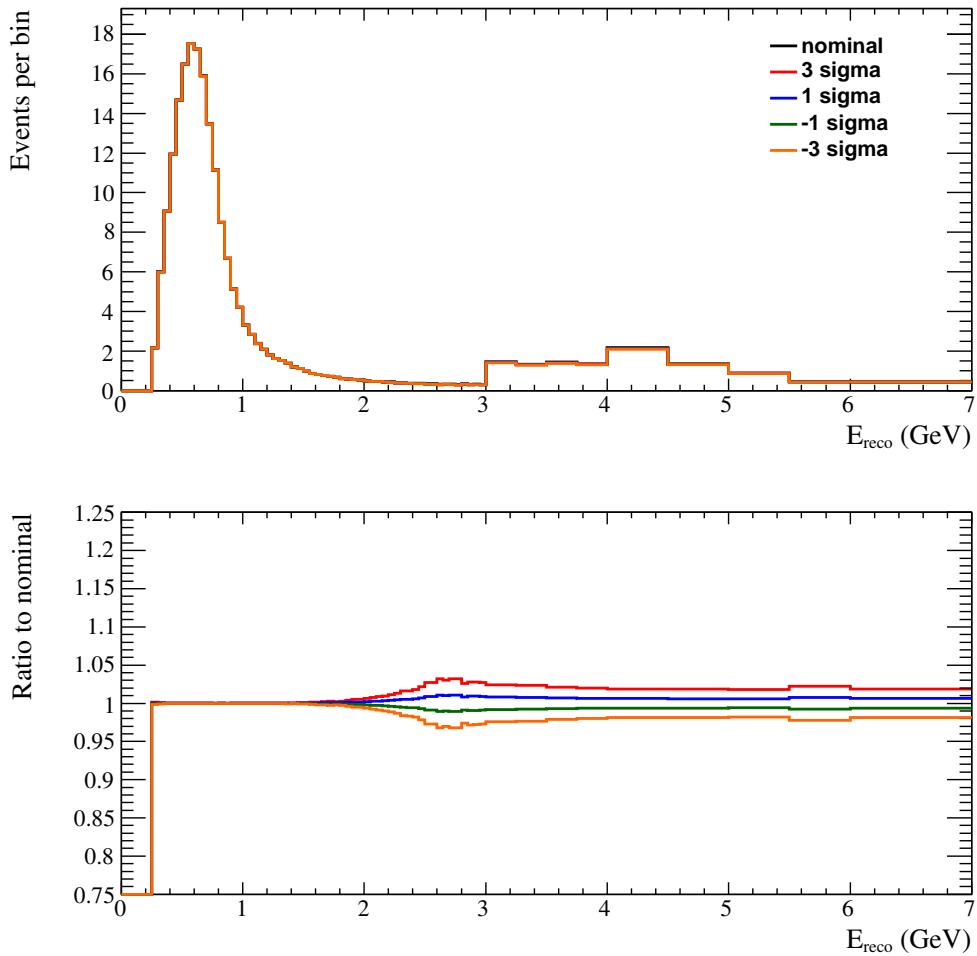


Figure 221: Effect of $f_{15;t,r}^{\text{banff}}$ for no oscillations (all mixing angles set to 0).

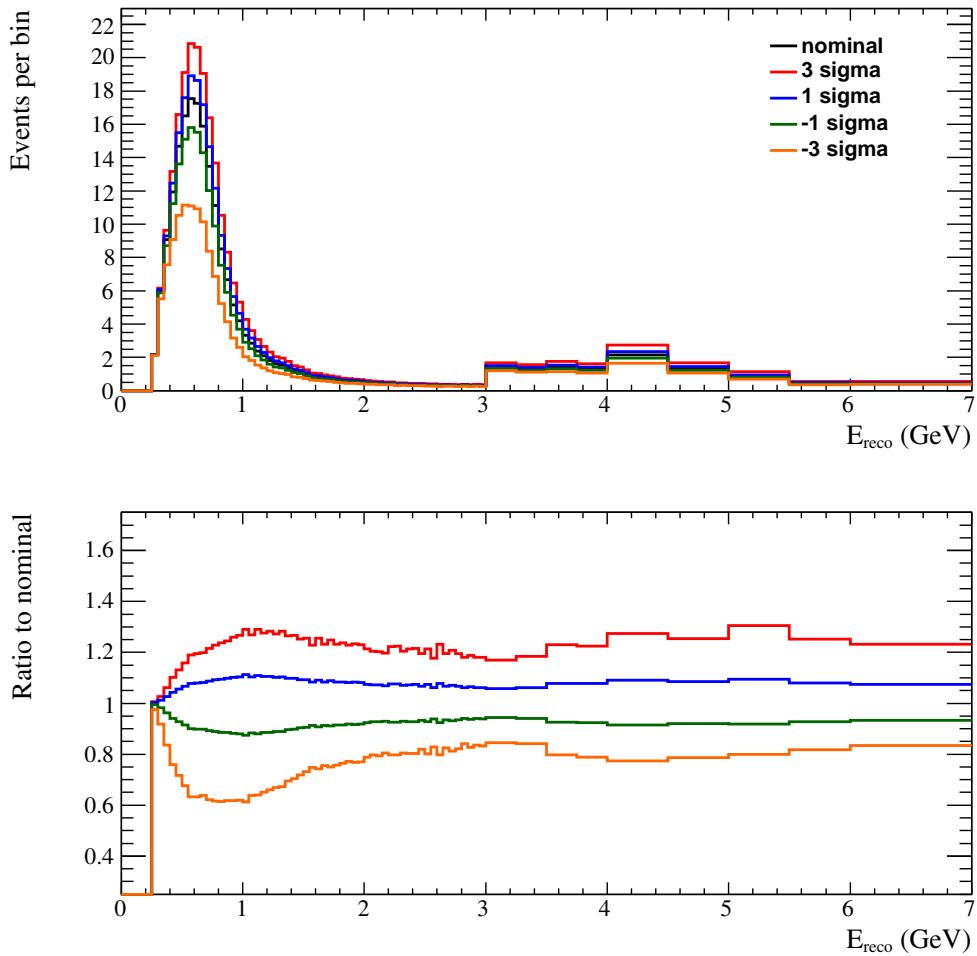


Figure 222: Effect of $f_{16;t,r}^{\text{banff}}$ for no oscillations (all mixing angles set to 0).

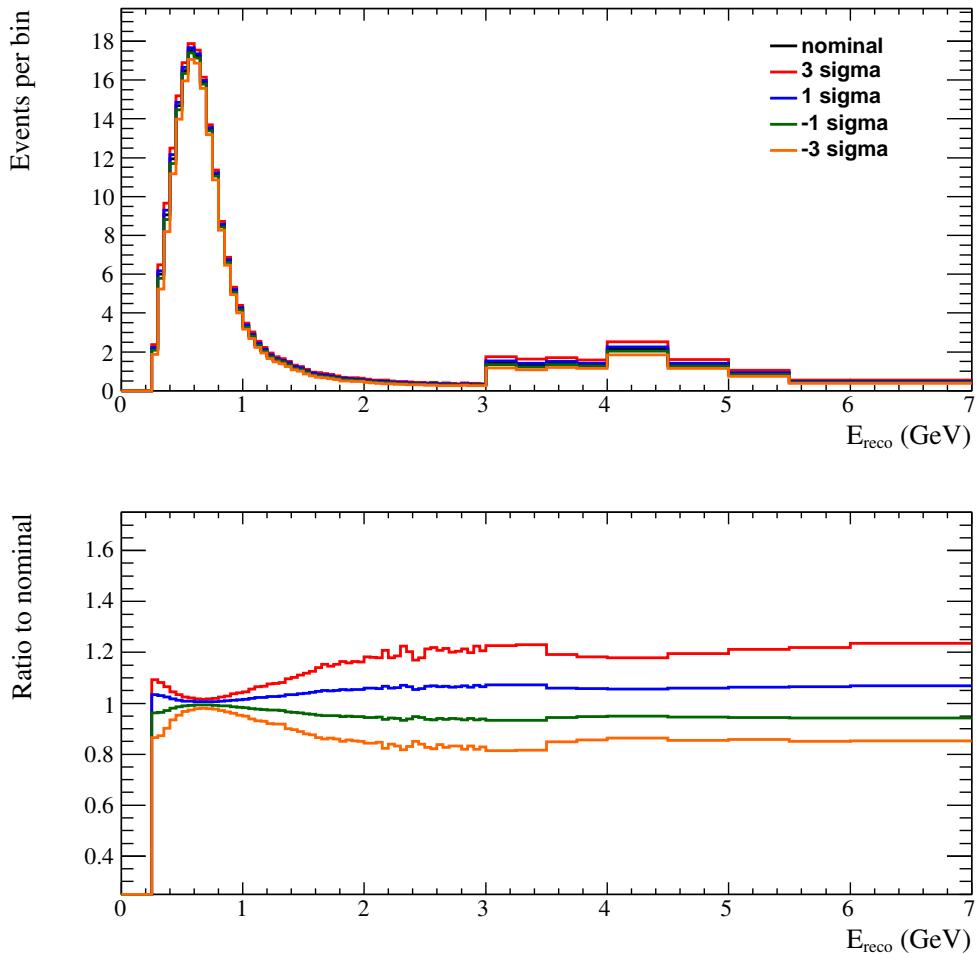


Figure 223: Effect of $f_{17;t,r}^{\text{banff}}$ for no oscillations (all mixing angles set to 0).

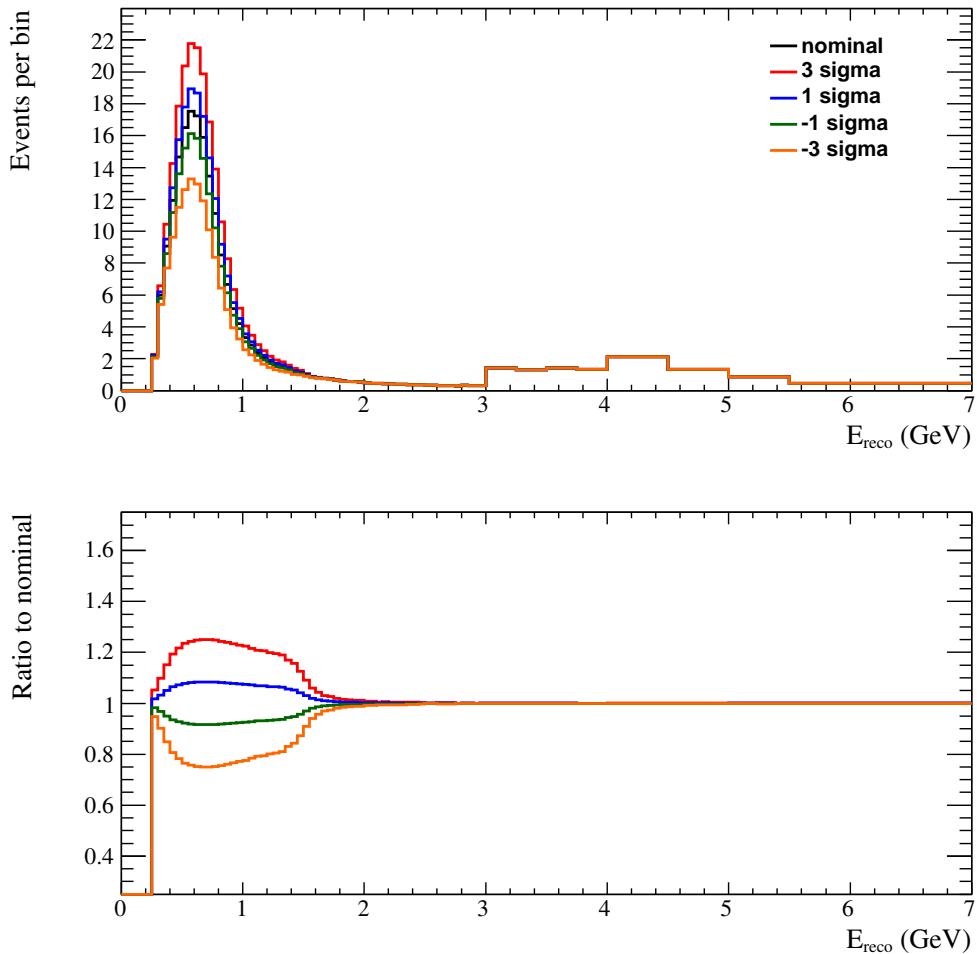


Figure 224: Effect of $f_{18;t,r}^{\text{banff}}$ for no oscillations (all mixing angles set to 0).

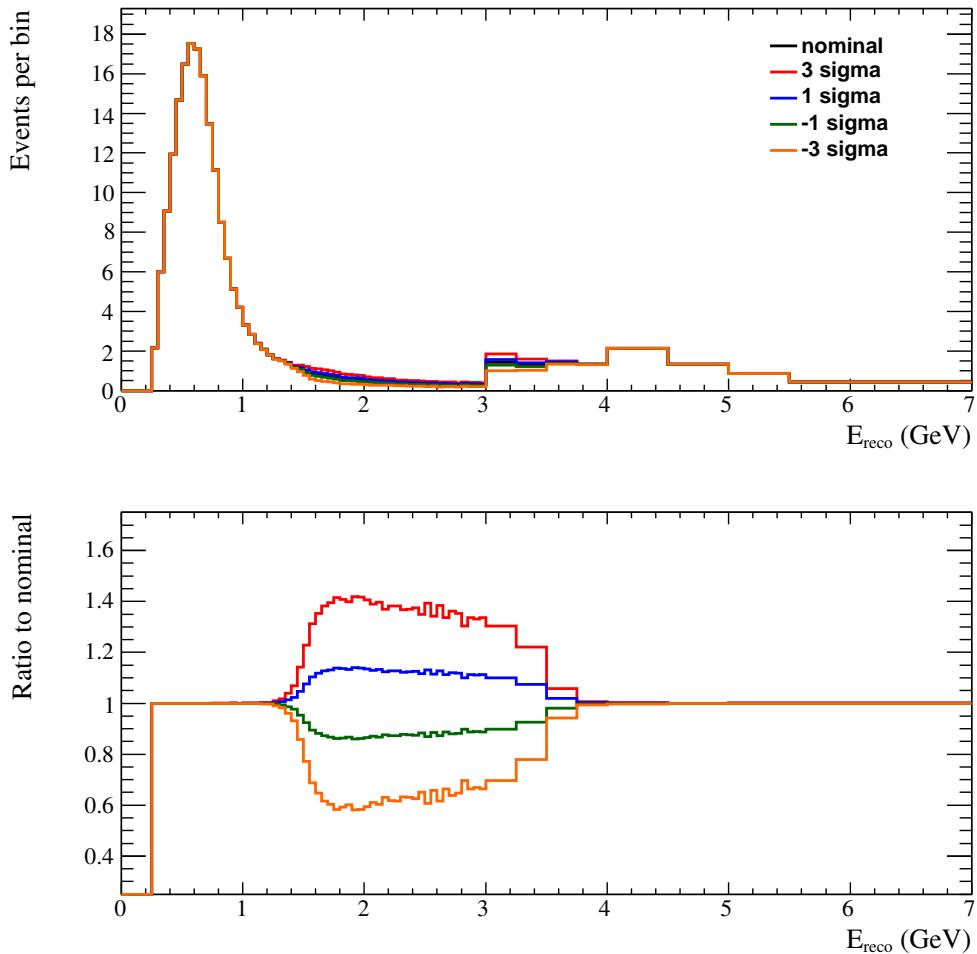


Figure 225: Effect of $f_{19;t,r}^{\text{banff}}$ for no oscillations (all mixing angles set to 0).

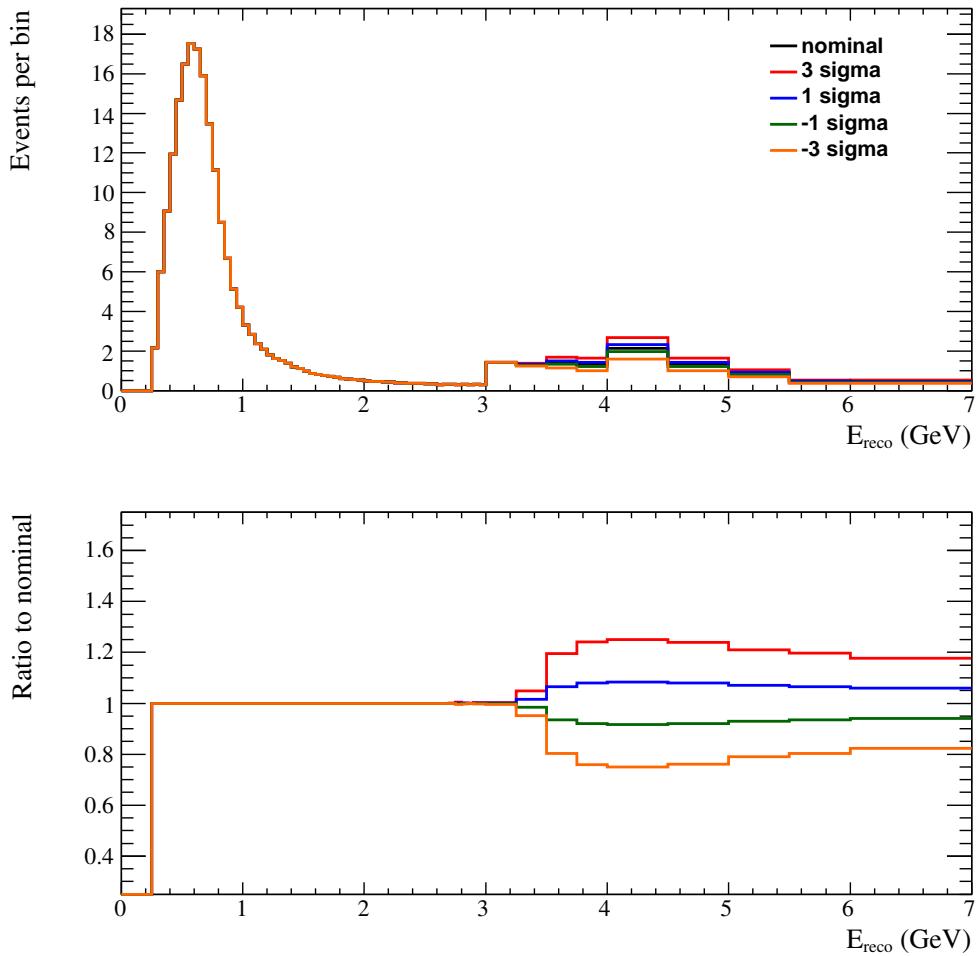


Figure 226: Effect of $f_{20;t,r}^{\text{banff}}$ for no oscillations (all mixing angles set to 0).

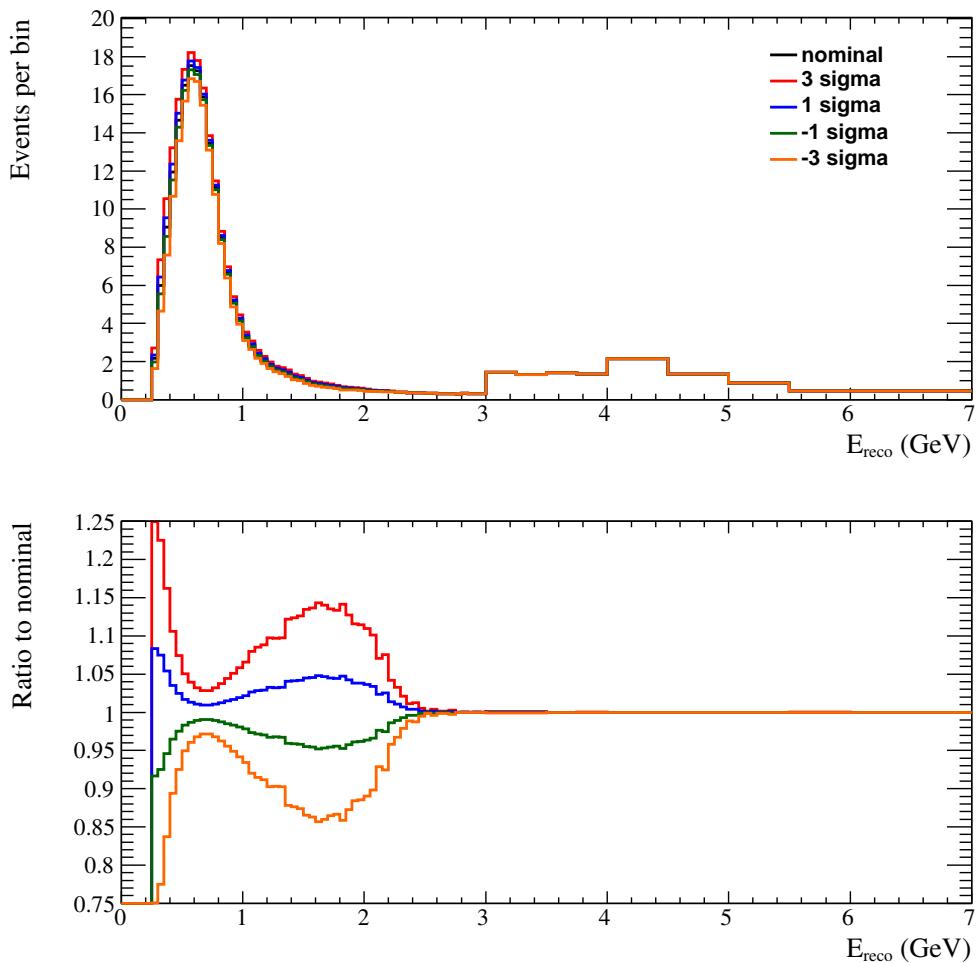


Figure 227: Effect of $f_{21;t,r}^{\text{banff}}$ for no oscillations (all mixing angles set to 0).

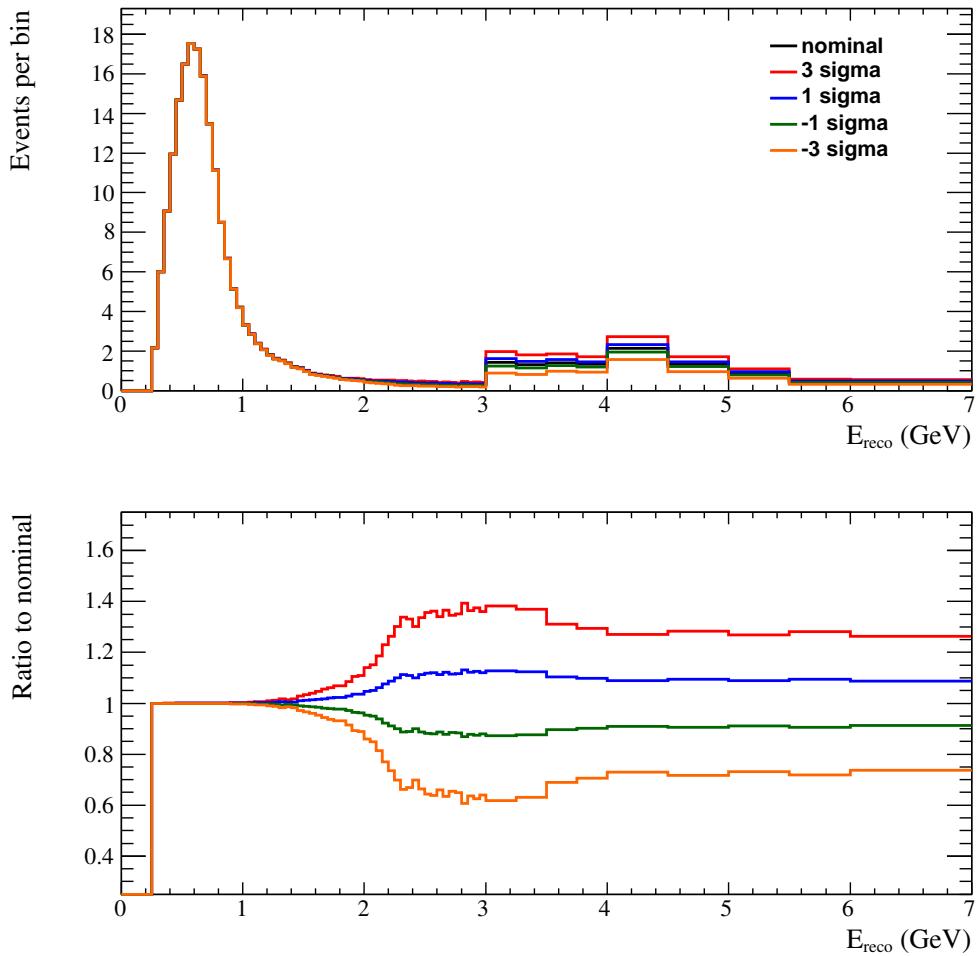


Figure 228: Effect of $f_{22;t,r}^{\text{banff}}$ for no oscillations (all mixing angles set to 0).

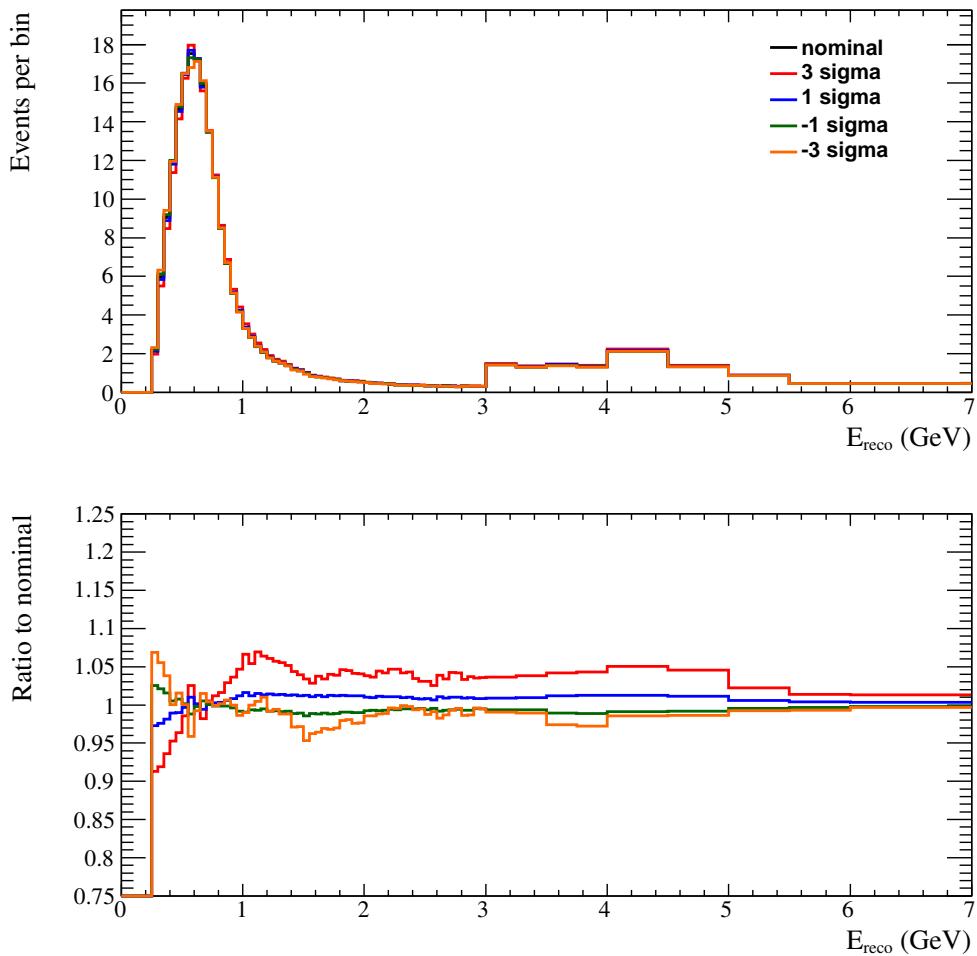


Figure 229: Effect of $f_{pF;t,r}$ for no oscillations (all mixing angles set to 0).

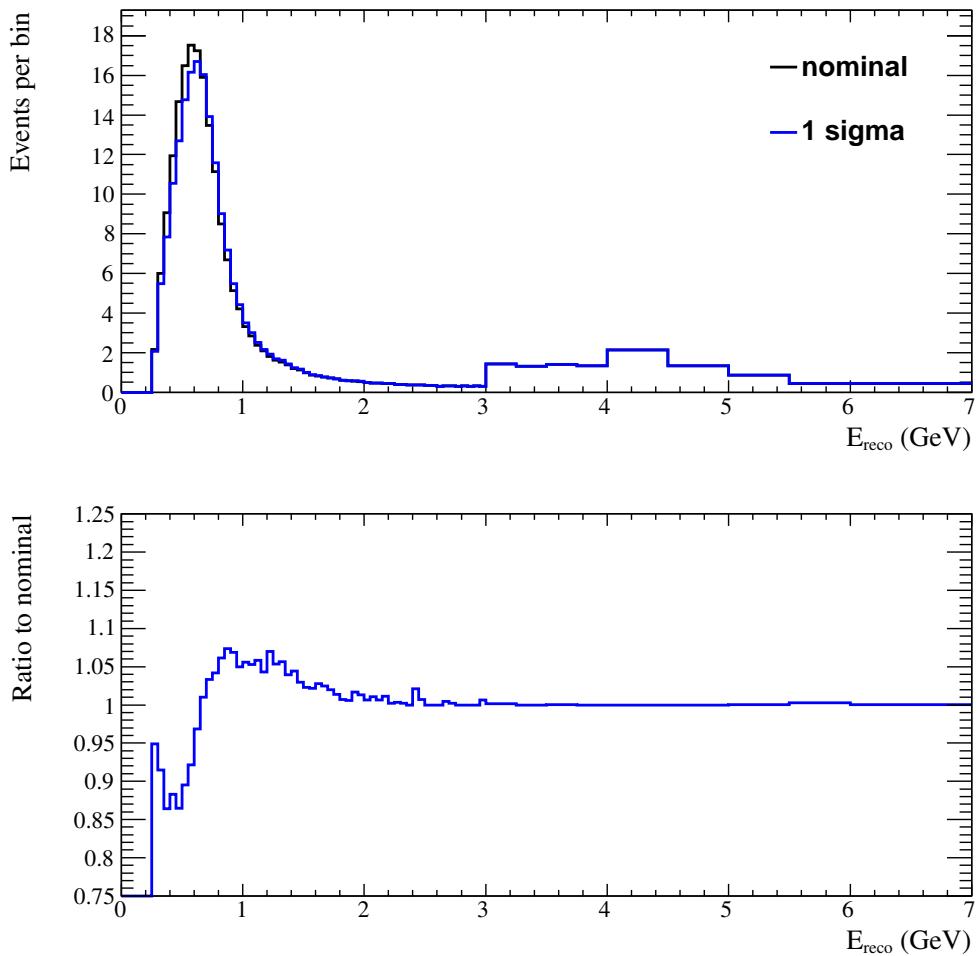


Figure 230: Effect of $f_{SF;t,r}$ for no oscillations (all mixing angles set to 0).

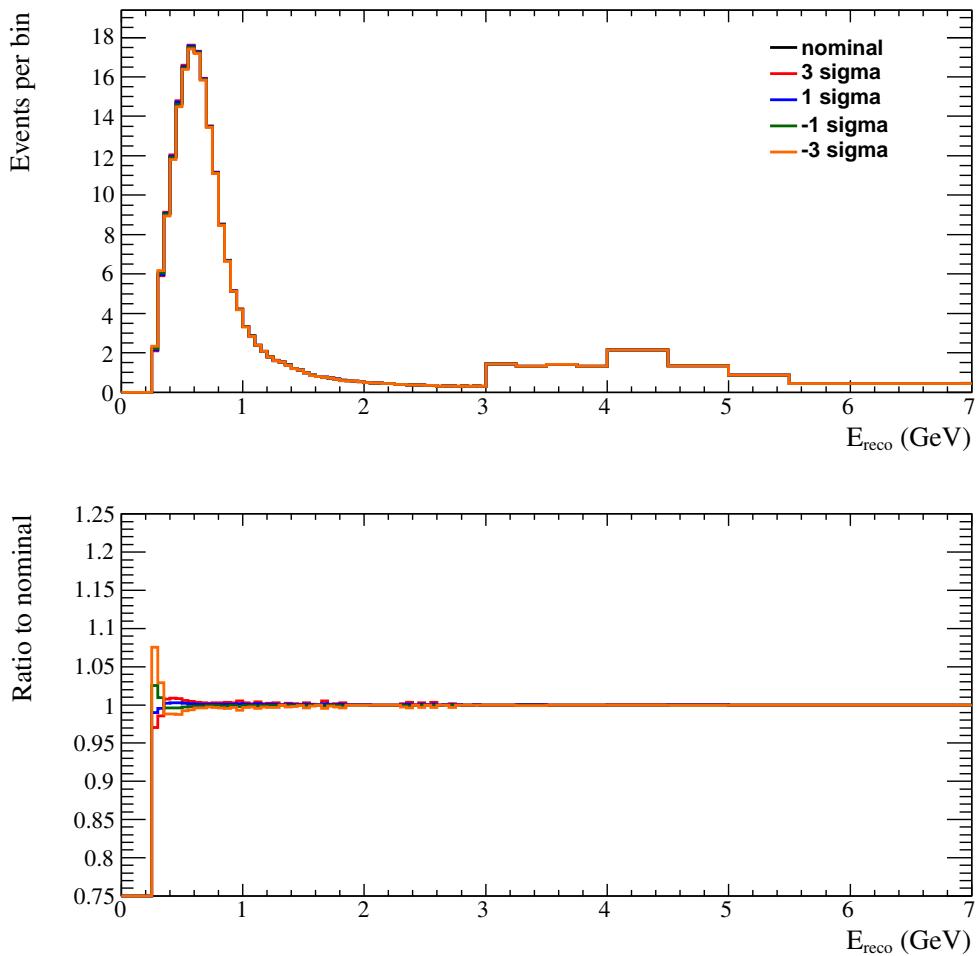


Figure 231: Effect of $f_{W\text{shape};t,r}$ for no oscillations (all mixing angles set to 0).

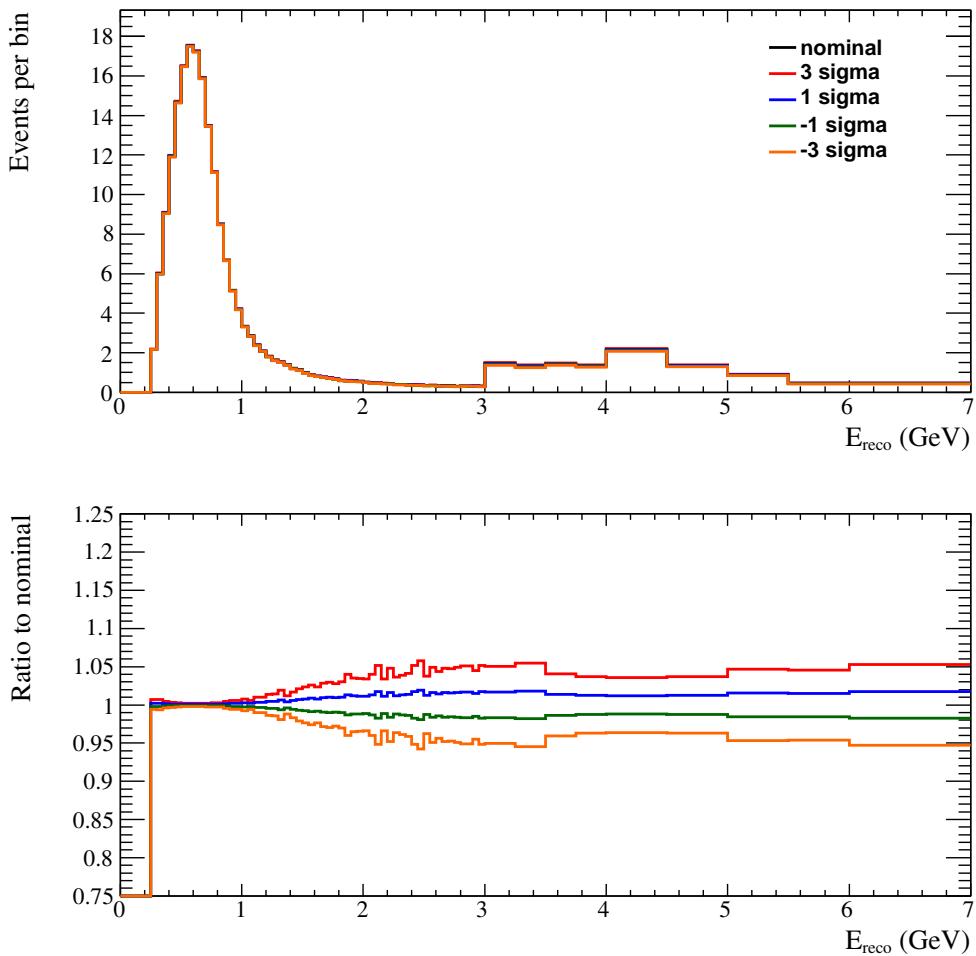


Figure 232: Effect of $f_{CC\coth Shape;t,r}$ for no oscillations (all mixing angles set to 0).

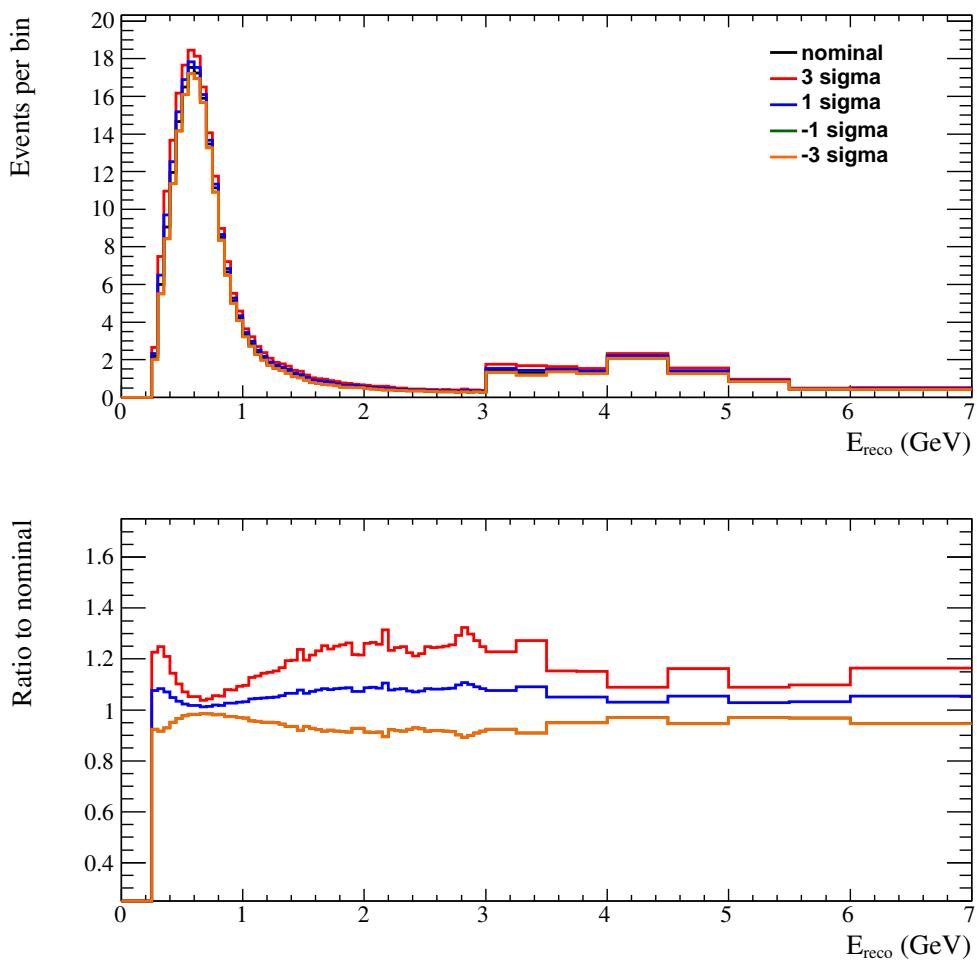


Figure 233: Effect of $f_{\pi-\text{less}} \Delta_{t,r}$ for no oscillations (all mixing angles set to 0).

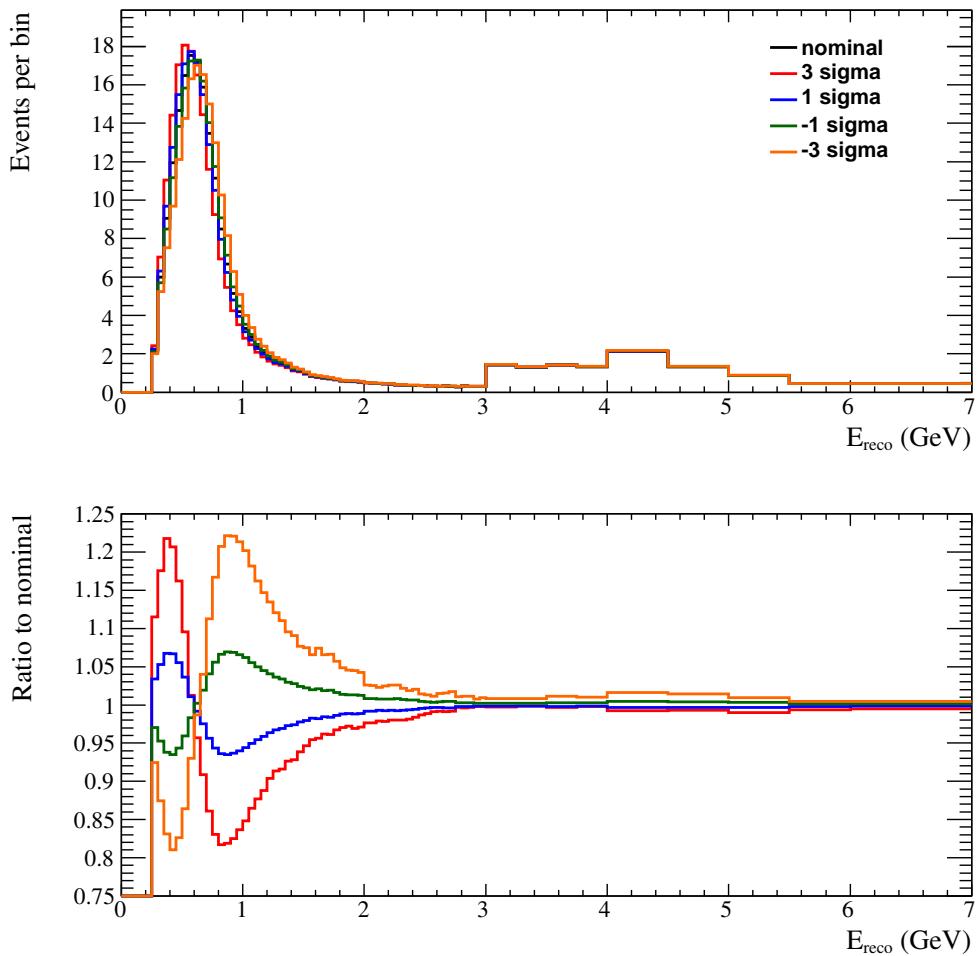


Figure 234: Effect of $f_{\text{bind}E;t,r}$ for no oscillations (all mixing angles set to 0).

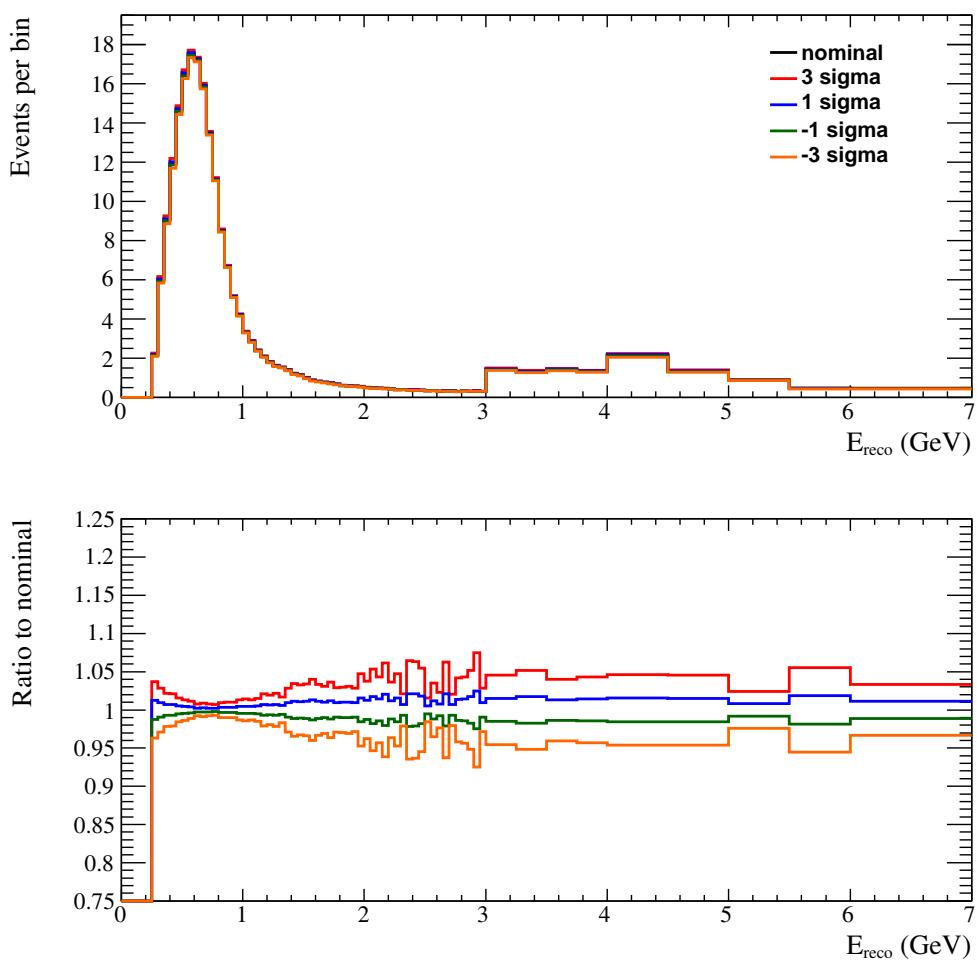


Figure 235: Effect of $f_{CCcoh;t}$ for no oscillations (all mixing angles set to 0).

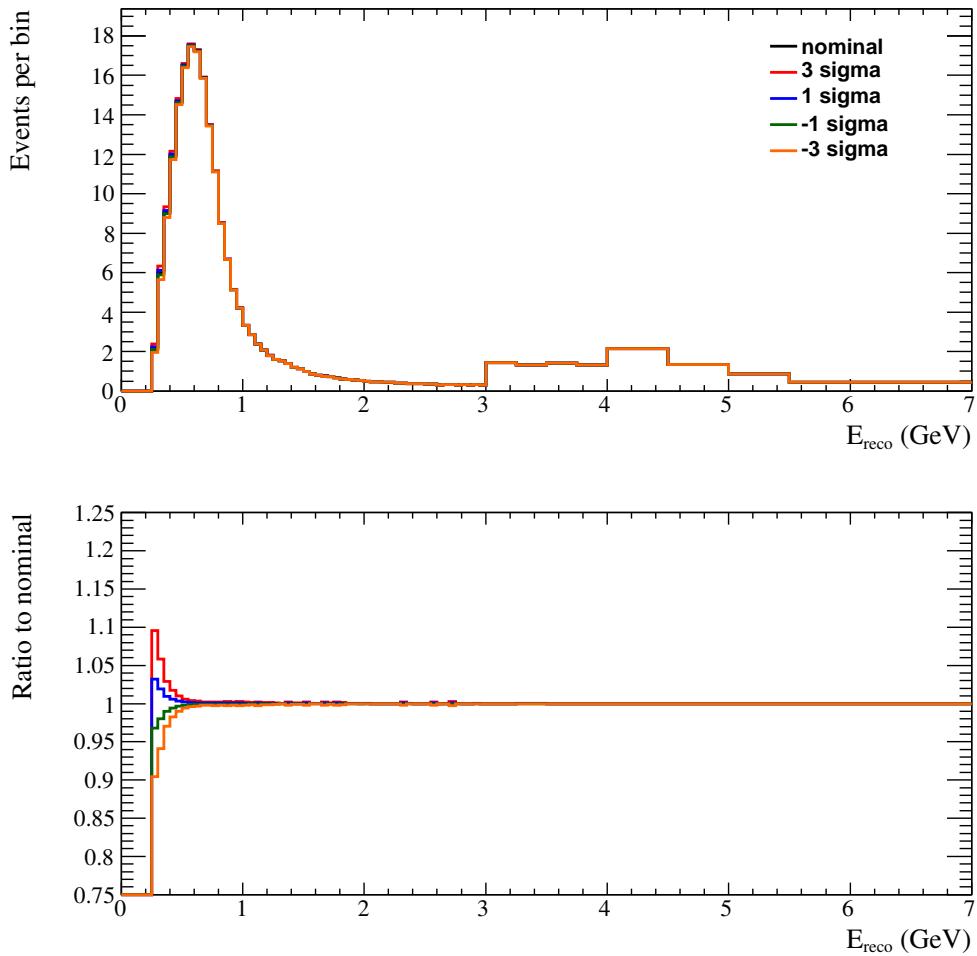


Figure 236: Effect of $f_{NC1\pi^\pm;t}$ for no oscillations (all mixing angles set to 0).

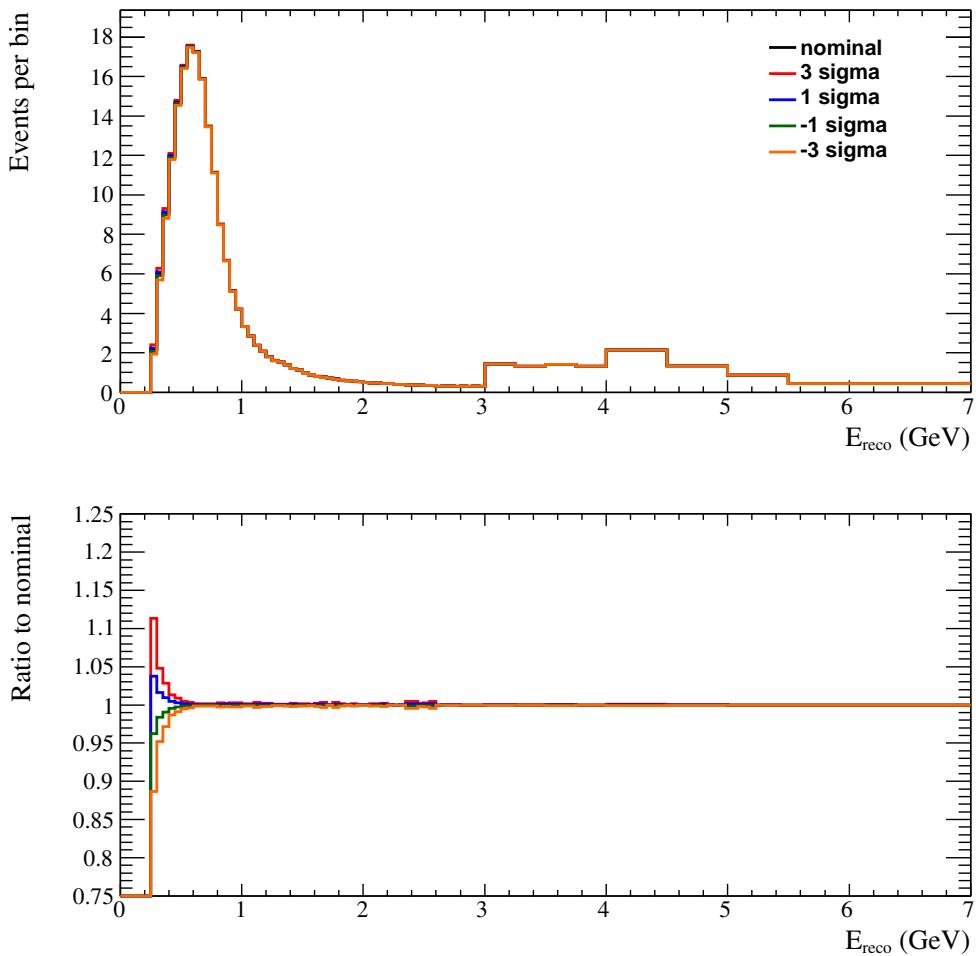


Figure 237: Effect of $f_{NCo_{th;t}}$ for no oscillations (all mixing angles set to 0).

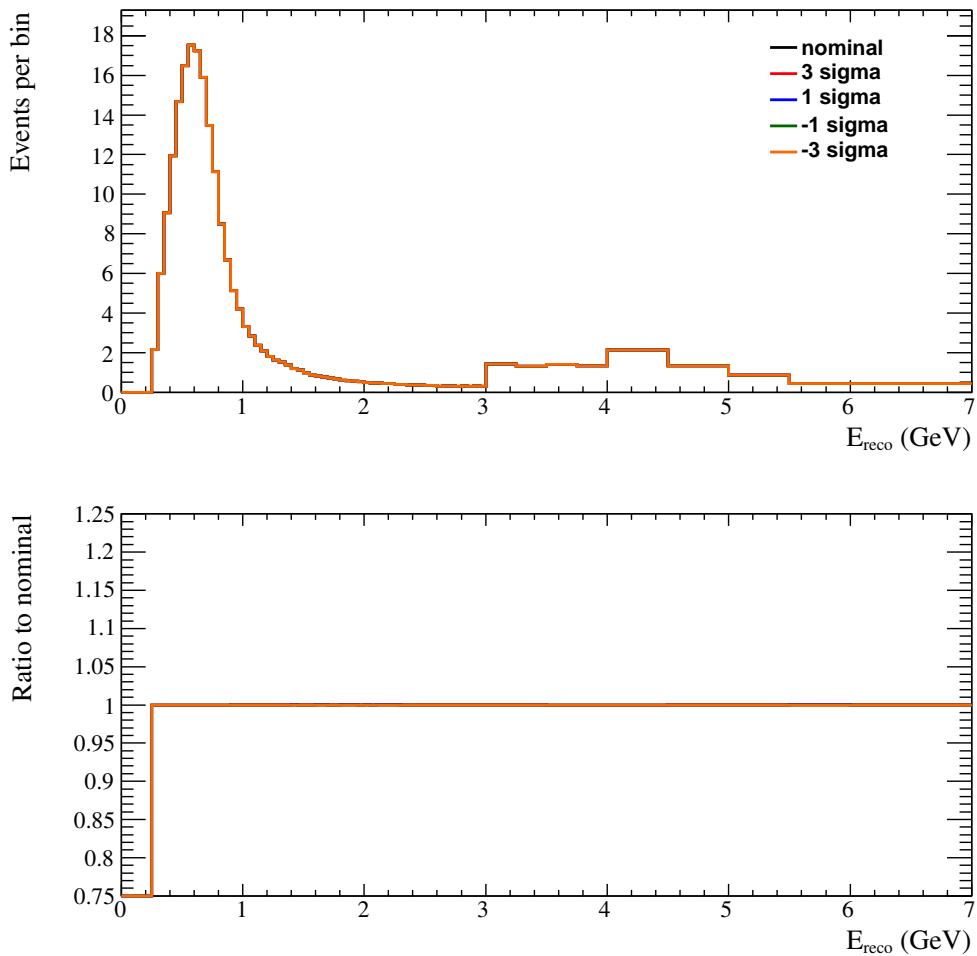


Figure 238: Effect of $f_{CC\nu_e;t}$ for no oscillations (all mixing angles set to 0).

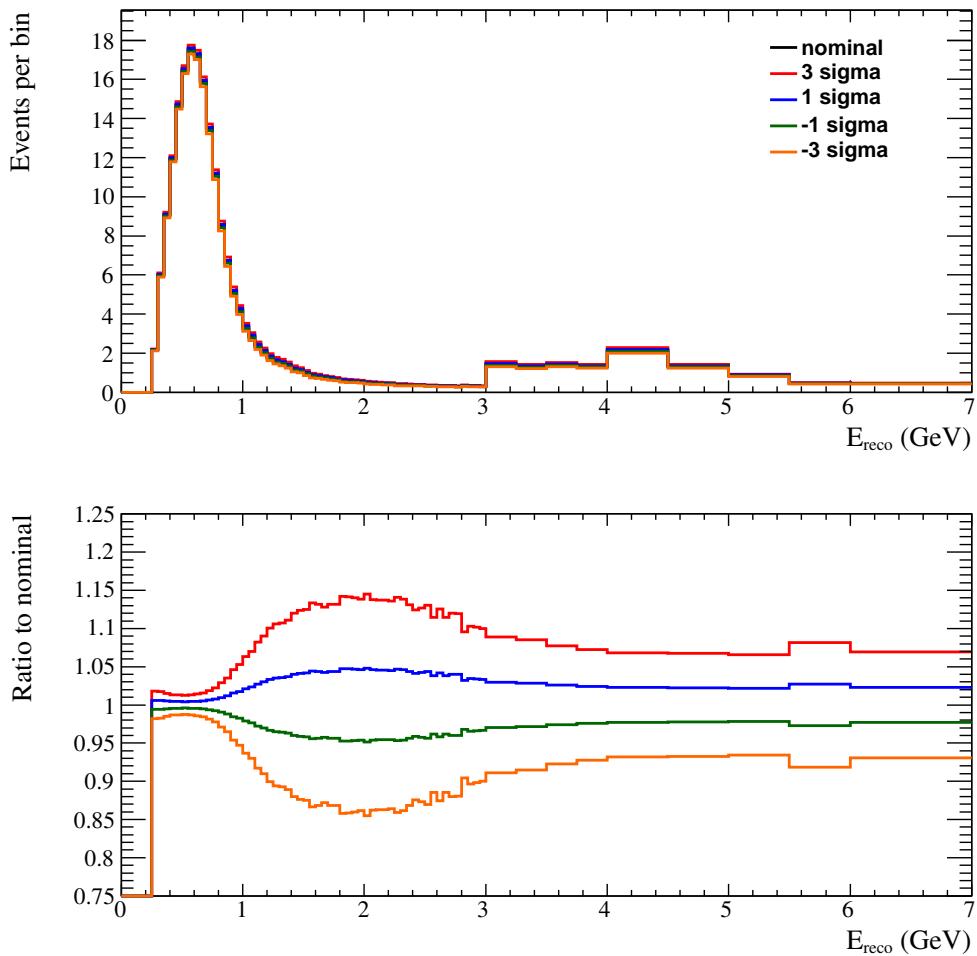


Figure 239: Effect of $f_{CC\bar{\nu};t}$ for no oscillations (all mixing angles set to 0).

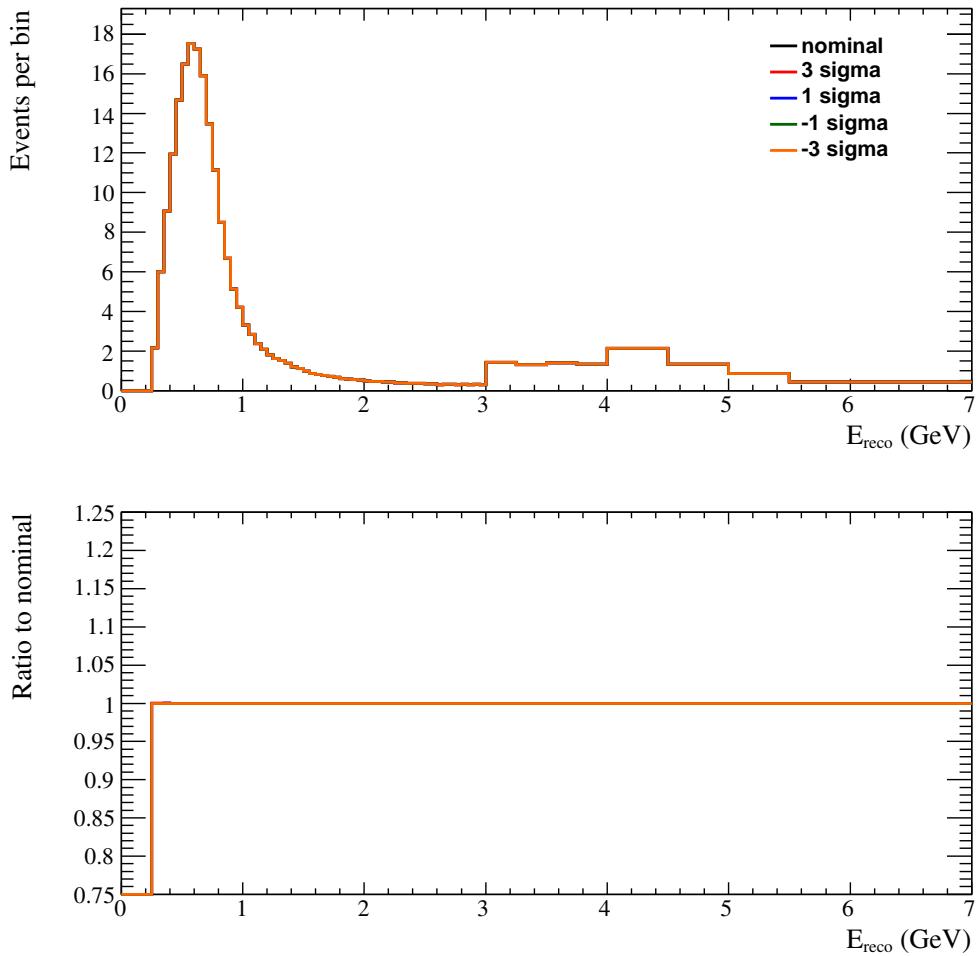


Figure 240: Effect of $f_{0;t,r}^{\text{FSI}}$ for no oscillations (all mixing angles set to 0).

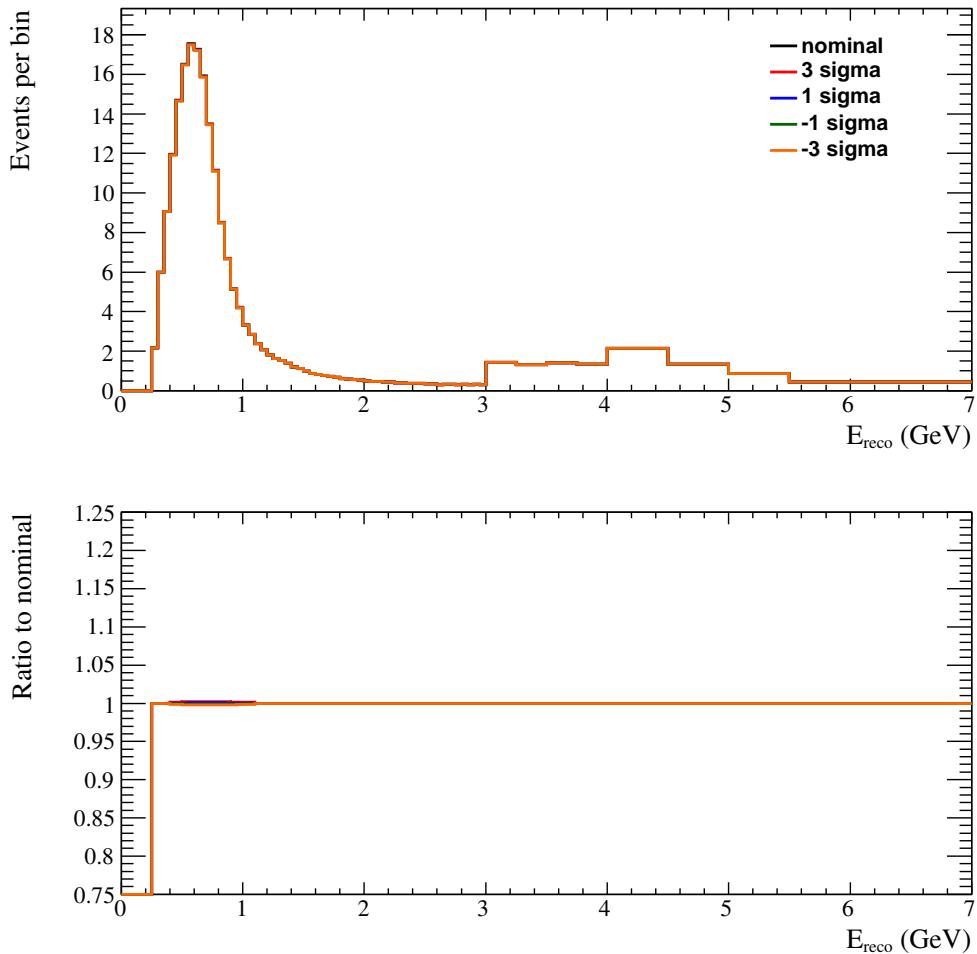


Figure 241: Effect of $f_{1;t,r}^{FSI}$ for no oscillations (all mixing angles set to 0).

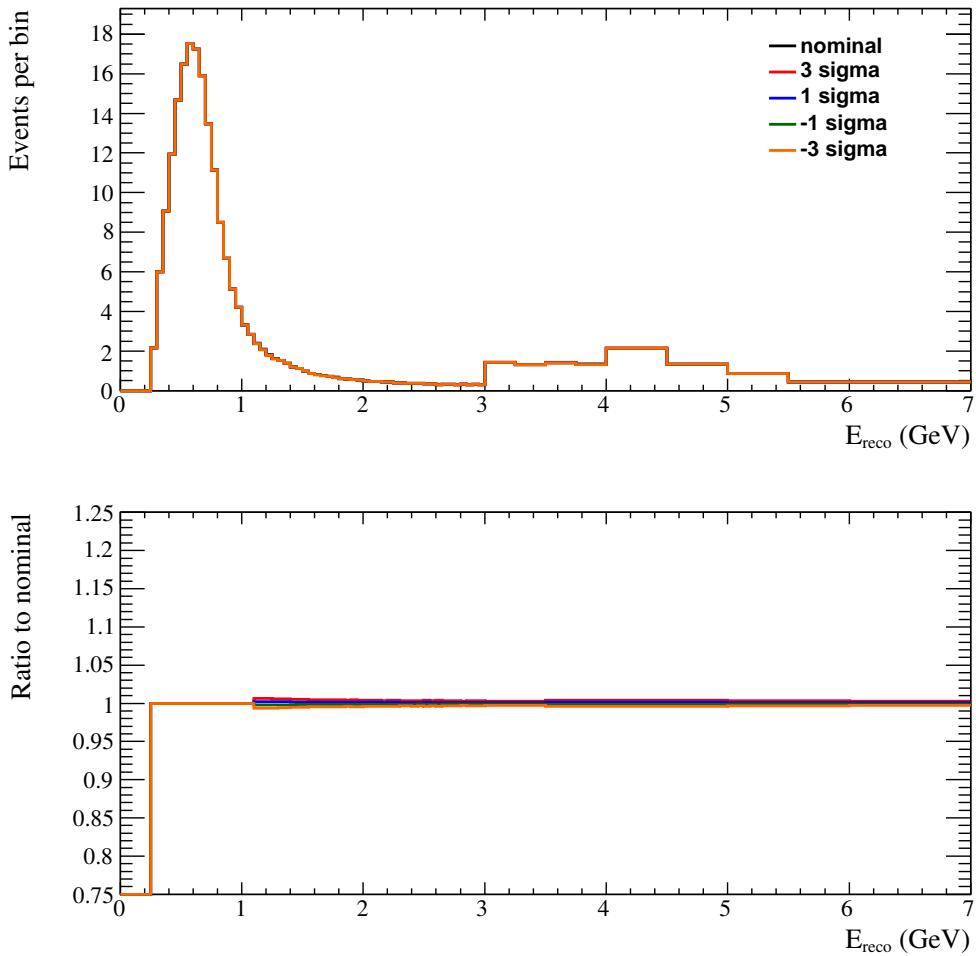


Figure 242: Effect of $f_{2;t,r}^{\text{FSI}}$ for no oscillations (all mixing angles set to 0).

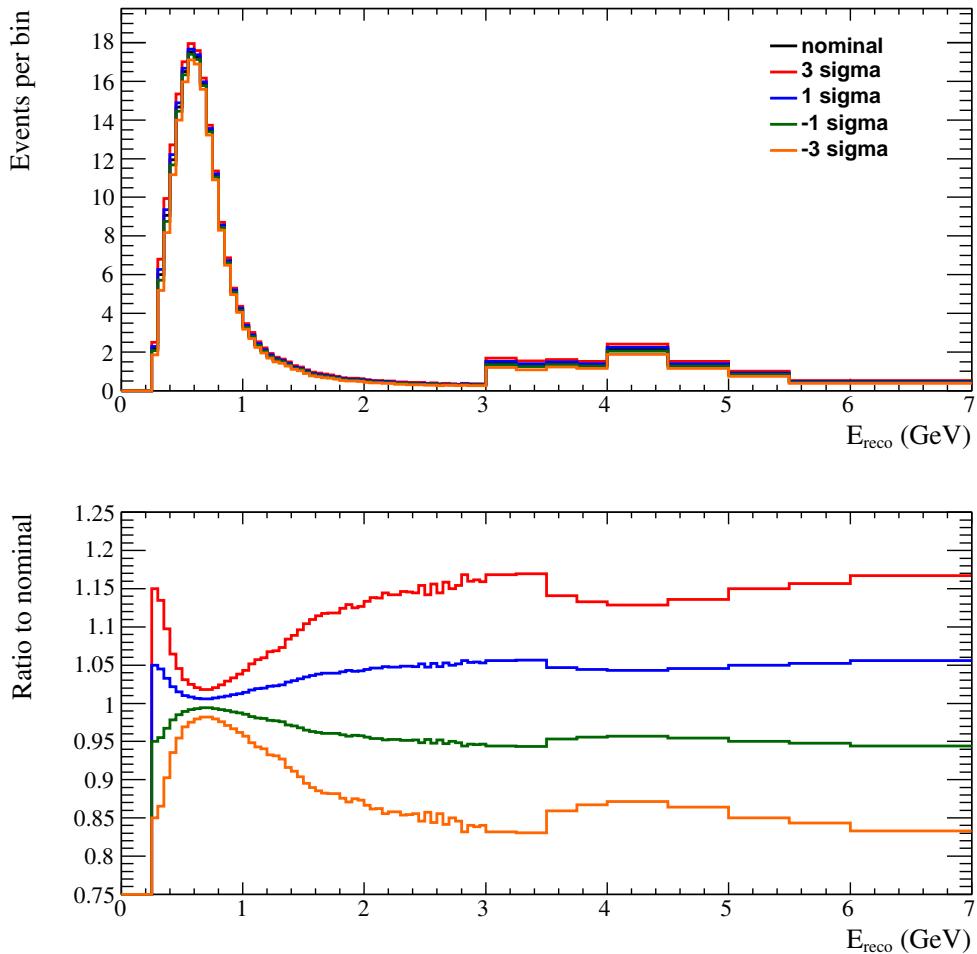


Figure 243: Effect of $f_{3;t,r}^{\text{FSI}}$ for no oscillations (all mixing angles set to 0).

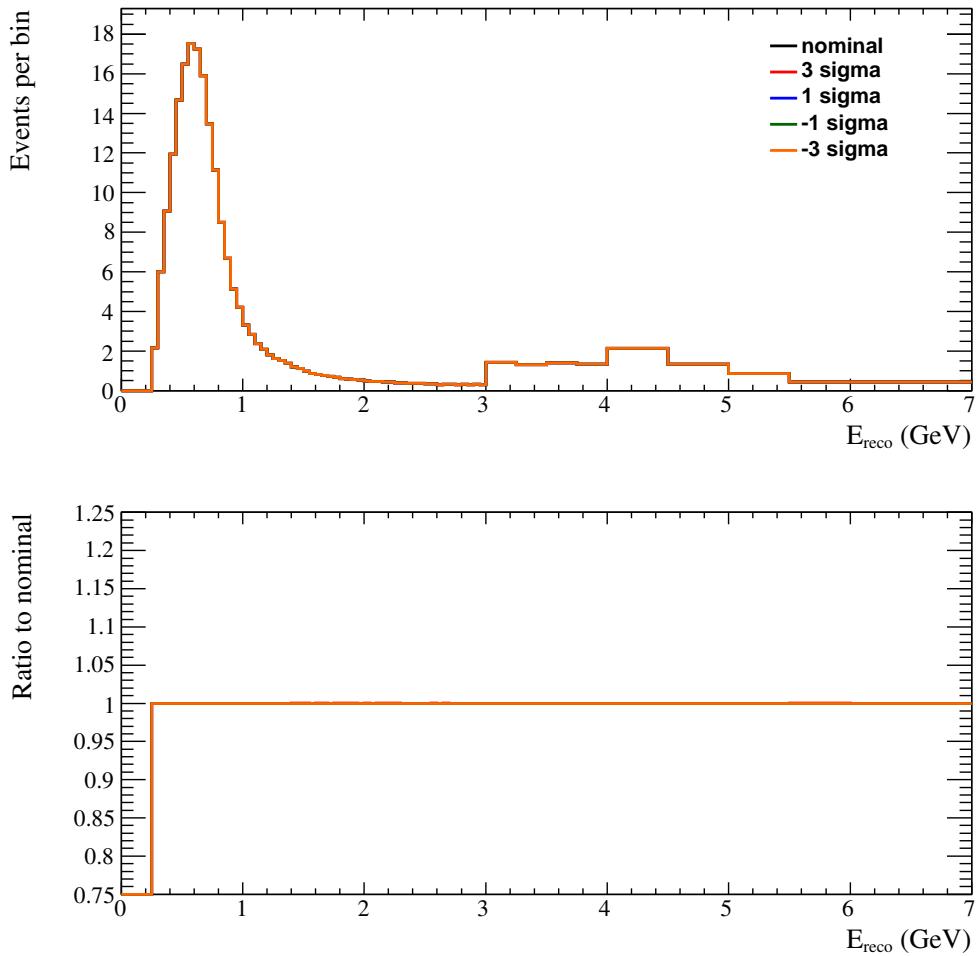


Figure 244: Effect of $f_{4;t,r}^{\text{FSI}}$ for no oscillations (all mixing angles set to 0).

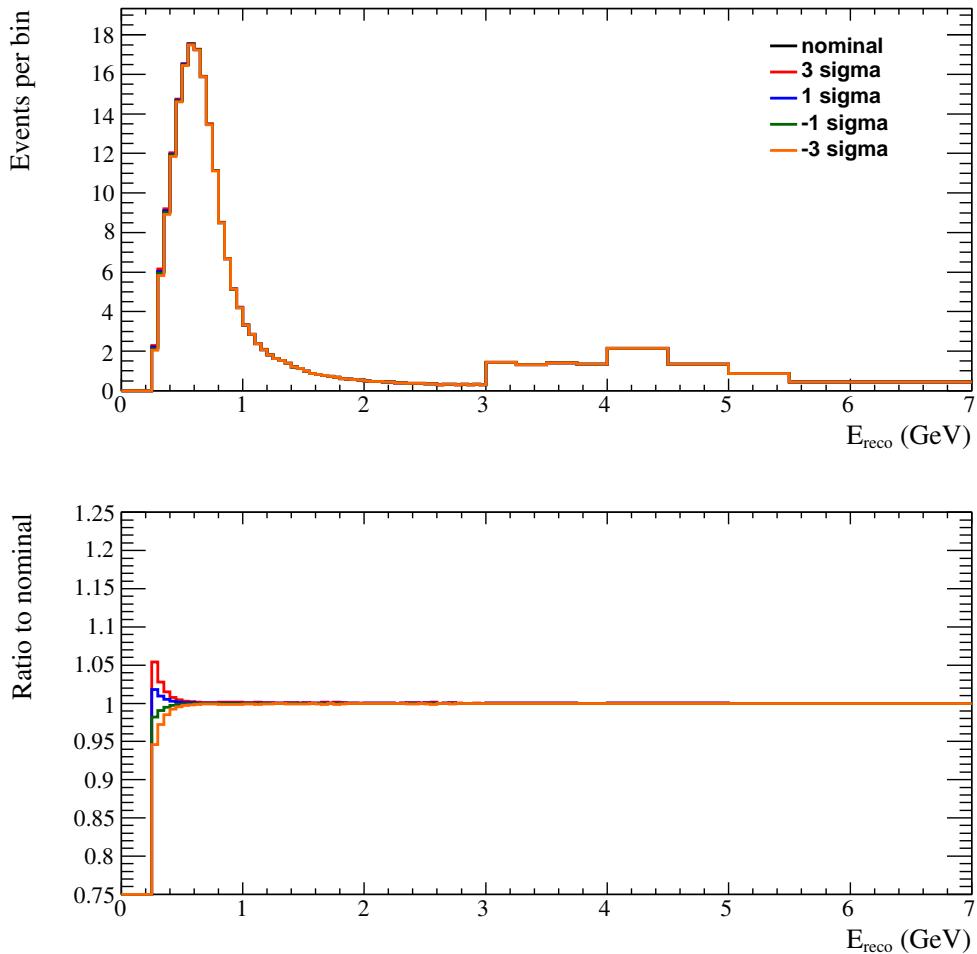


Figure 245: Effect of $f_{5;t,r}^{\text{FSI}}$ for no oscillations (all mixing angles set to 0).

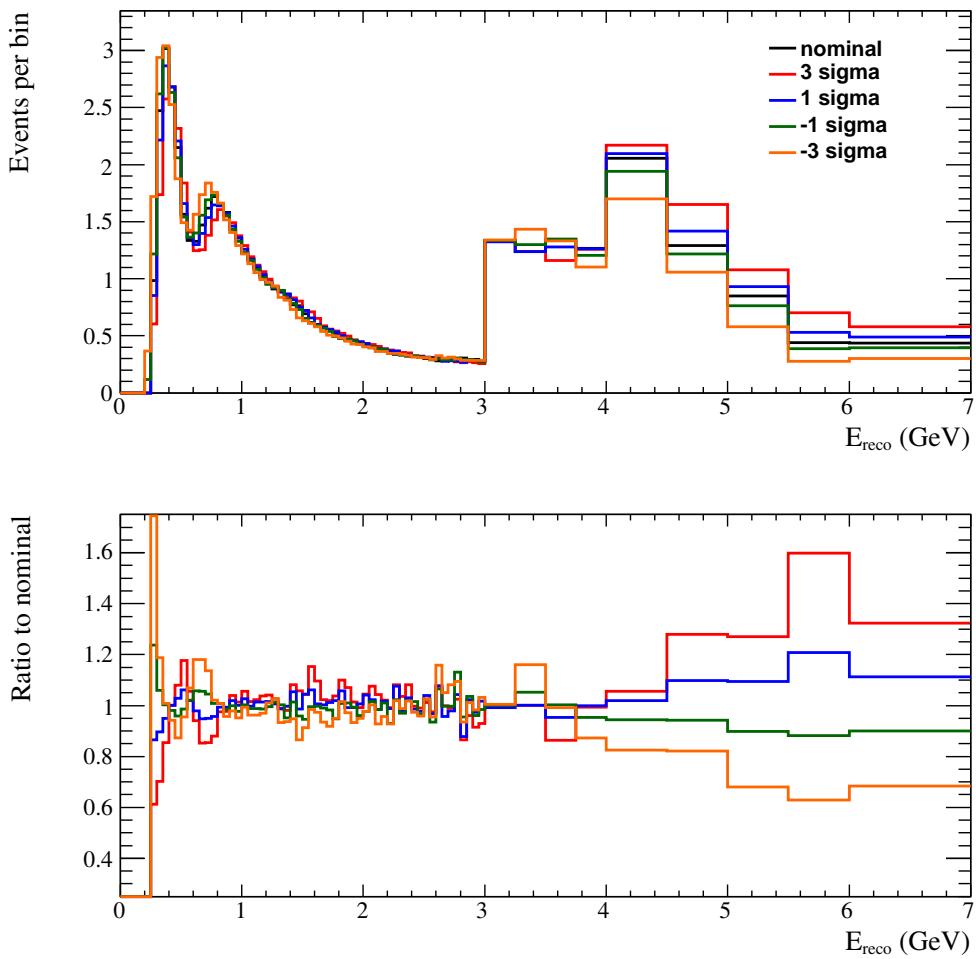


Figure 246: Effect of $f_{E;r}^{SK}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

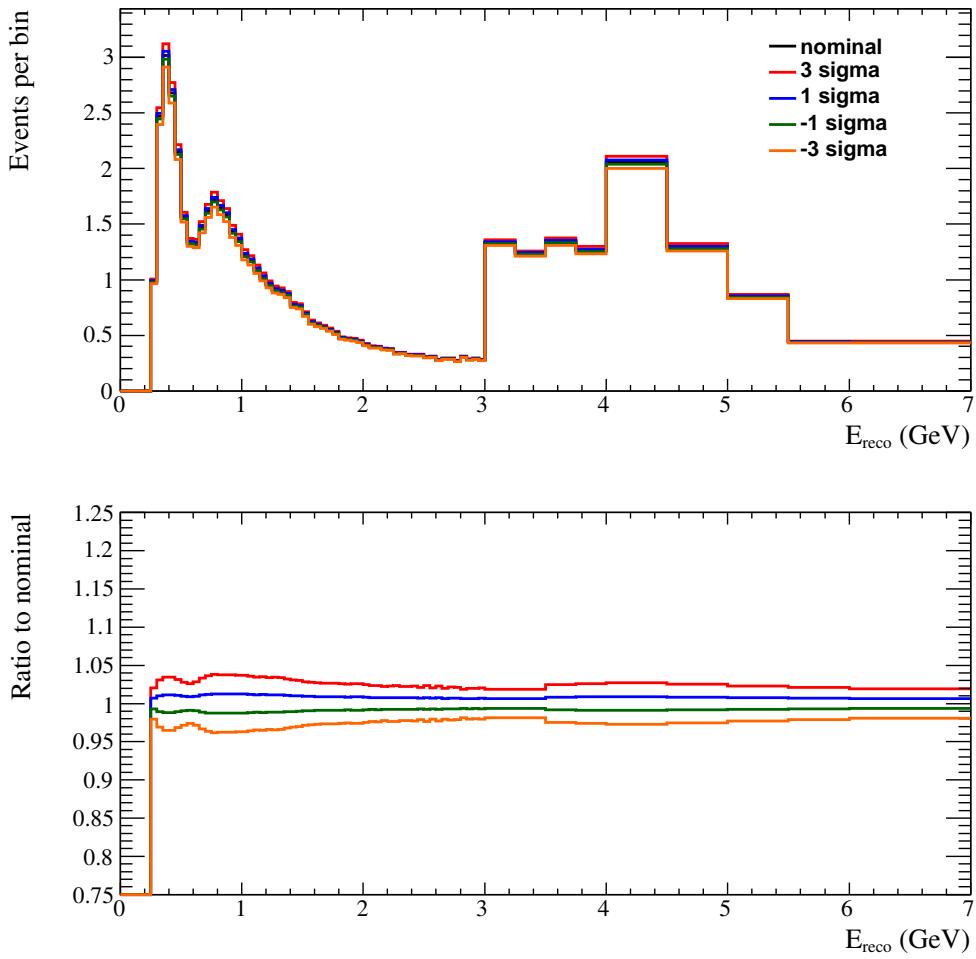


Figure 247: Effect of $f_{CCQE;oth;r}^{SK}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

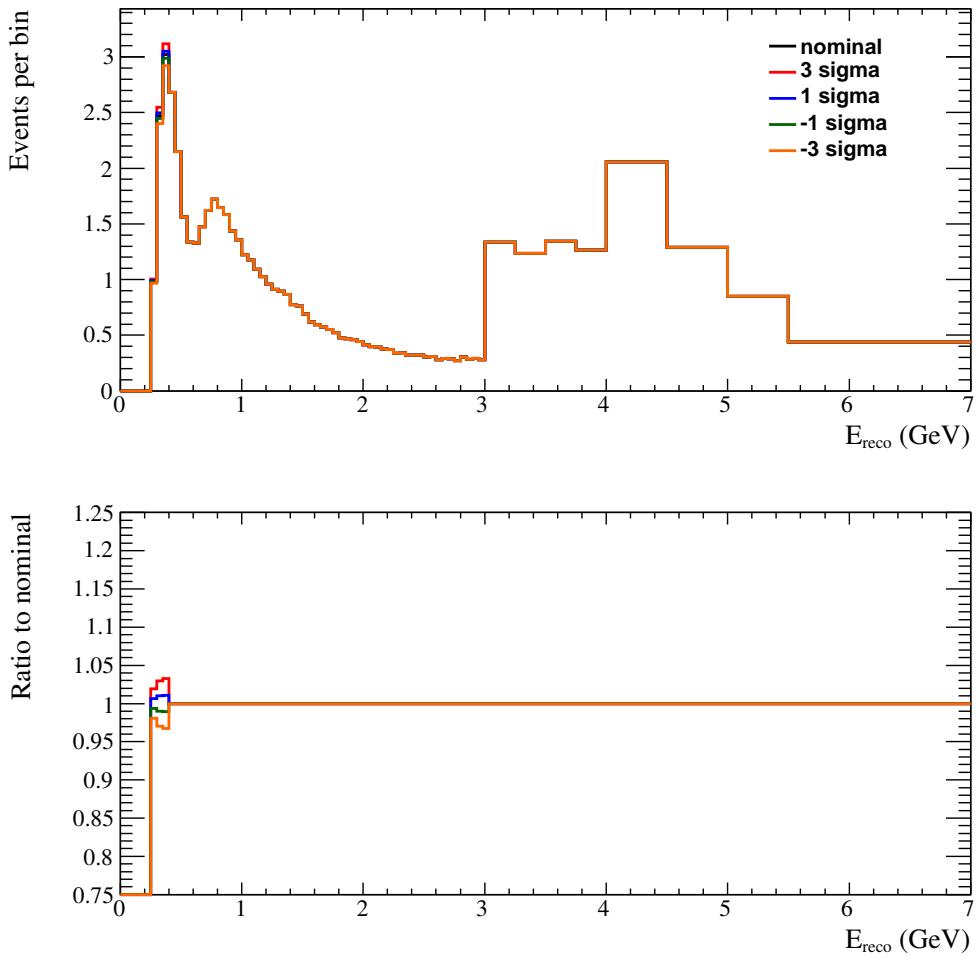


Figure 248: Effect of $f_{CCQERC0;r}^{SK}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

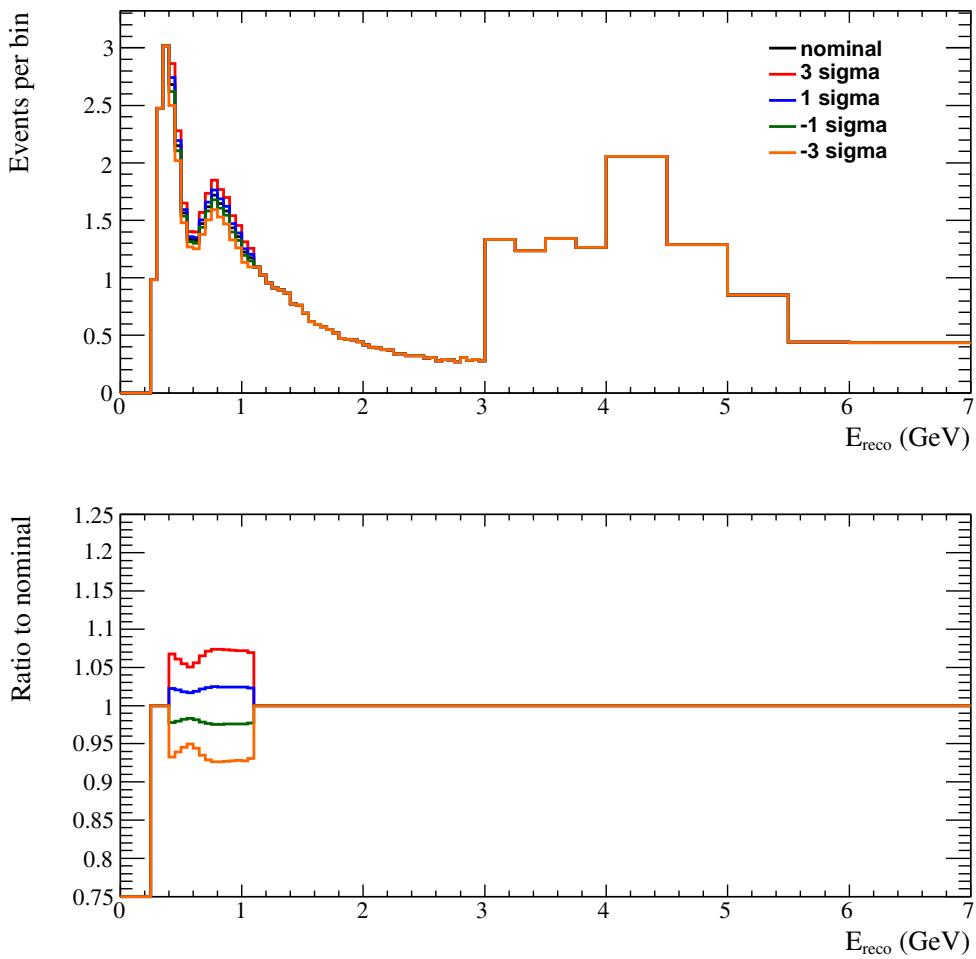


Figure 249: Effect of $f_{CCQERC1;r}^{SK}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

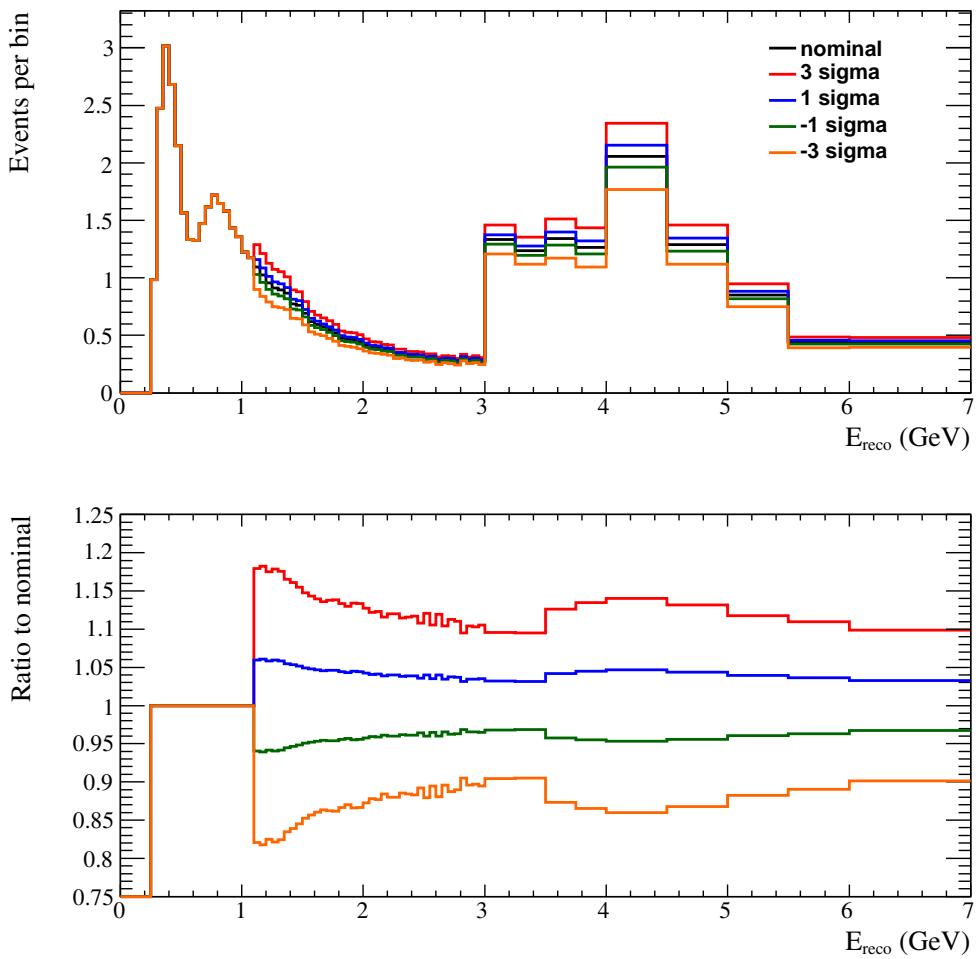


Figure 250: Effect of $f_{CCQERC2;r}^{SK}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

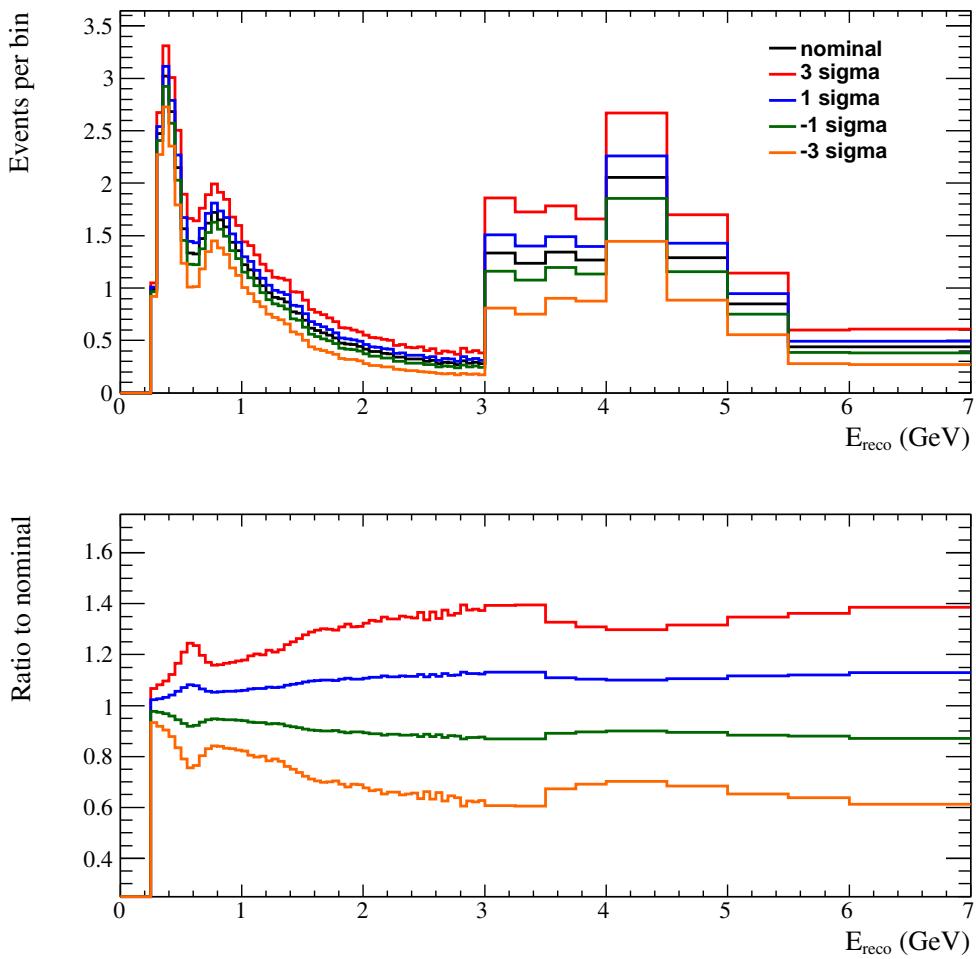


Figure 251: Effect of $f_{CCnQE;r}^{SK}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

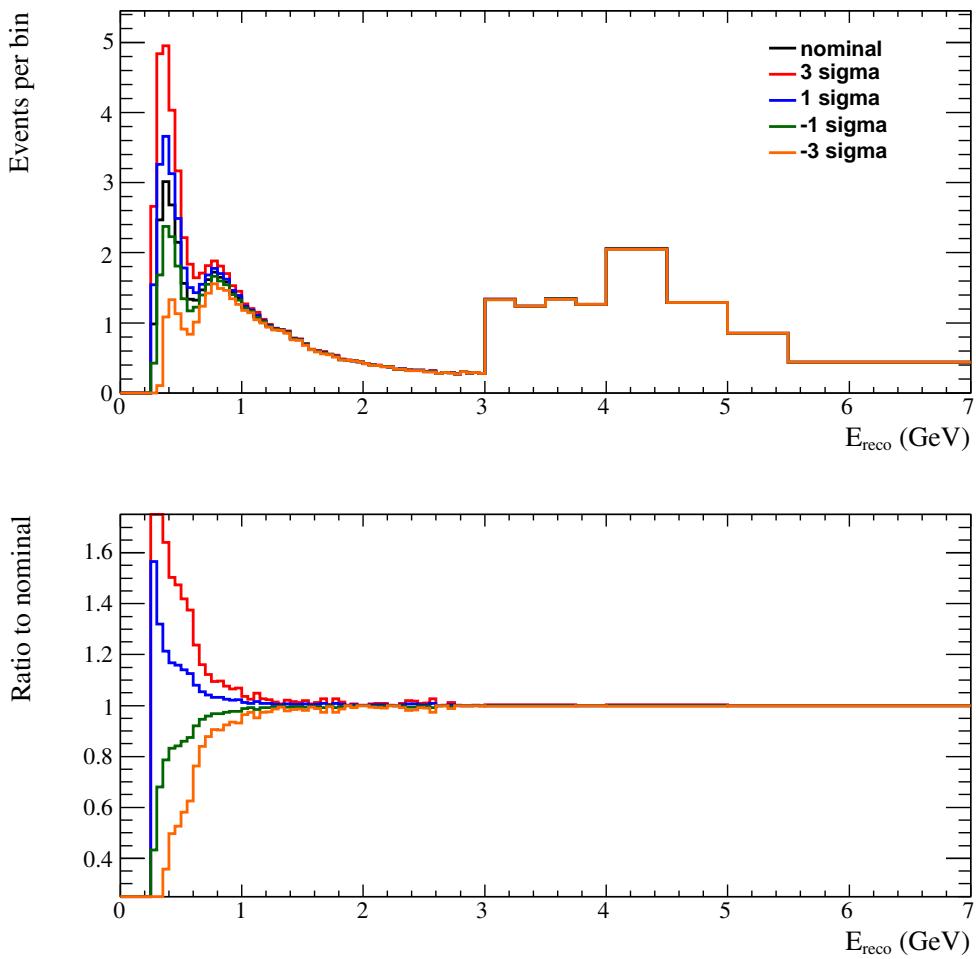


Figure 252: Effect of $f_{NC;r}^{SK}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

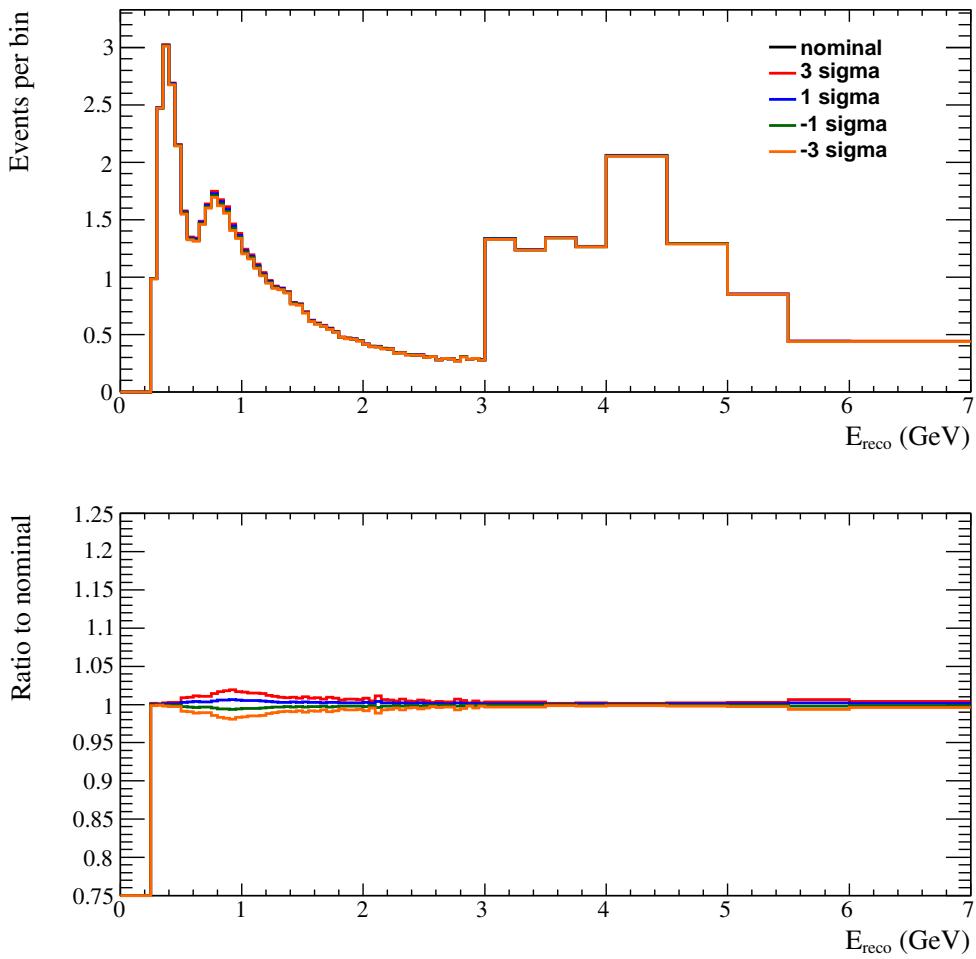


Figure 253: Effect of $f_{\nu_e; r}^{SK}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

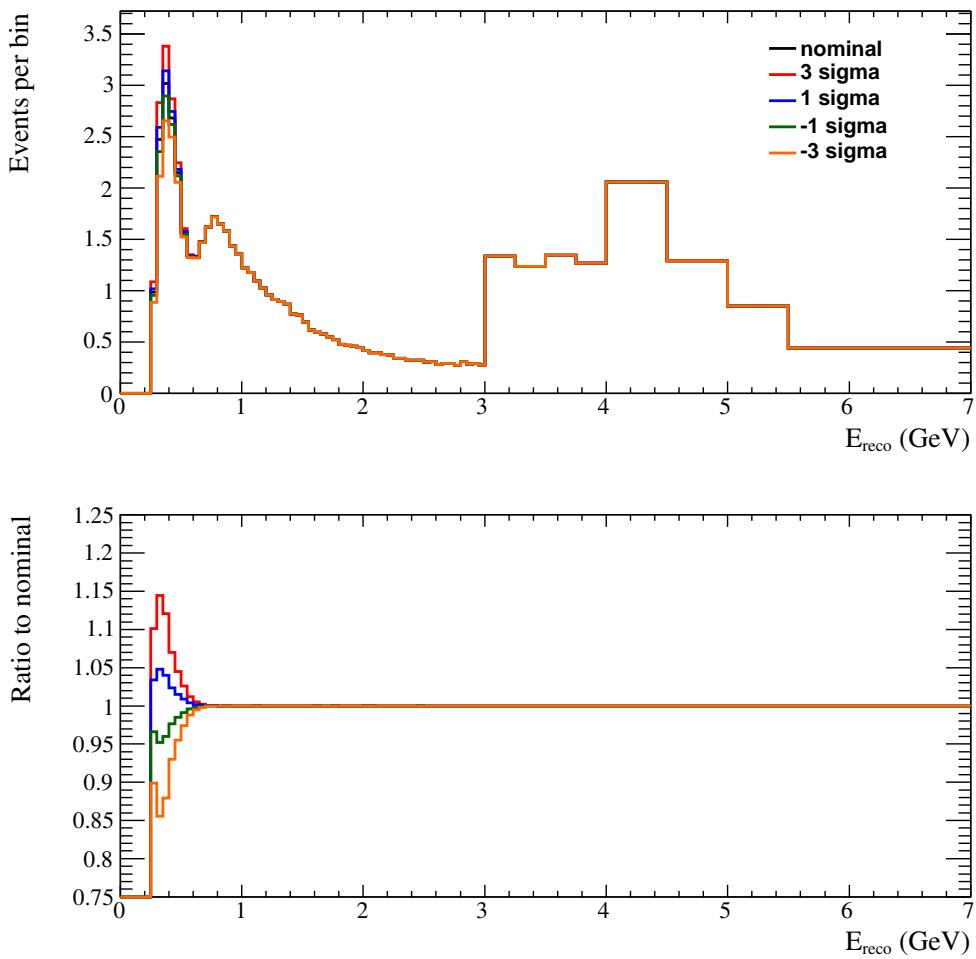


Figure 254: Effect of $f_{0;t,r}^{\text{baff}}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

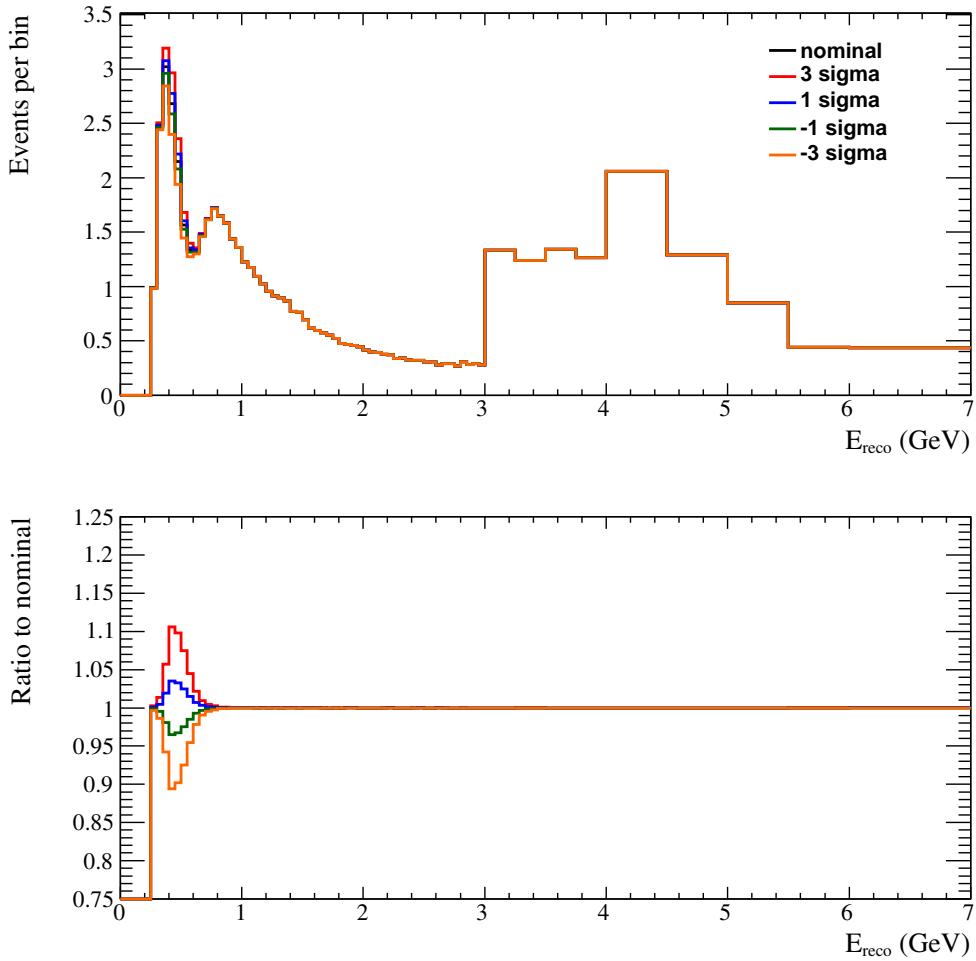


Figure 255: Effect of $f_{1;t,r}^{\text{baff}}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

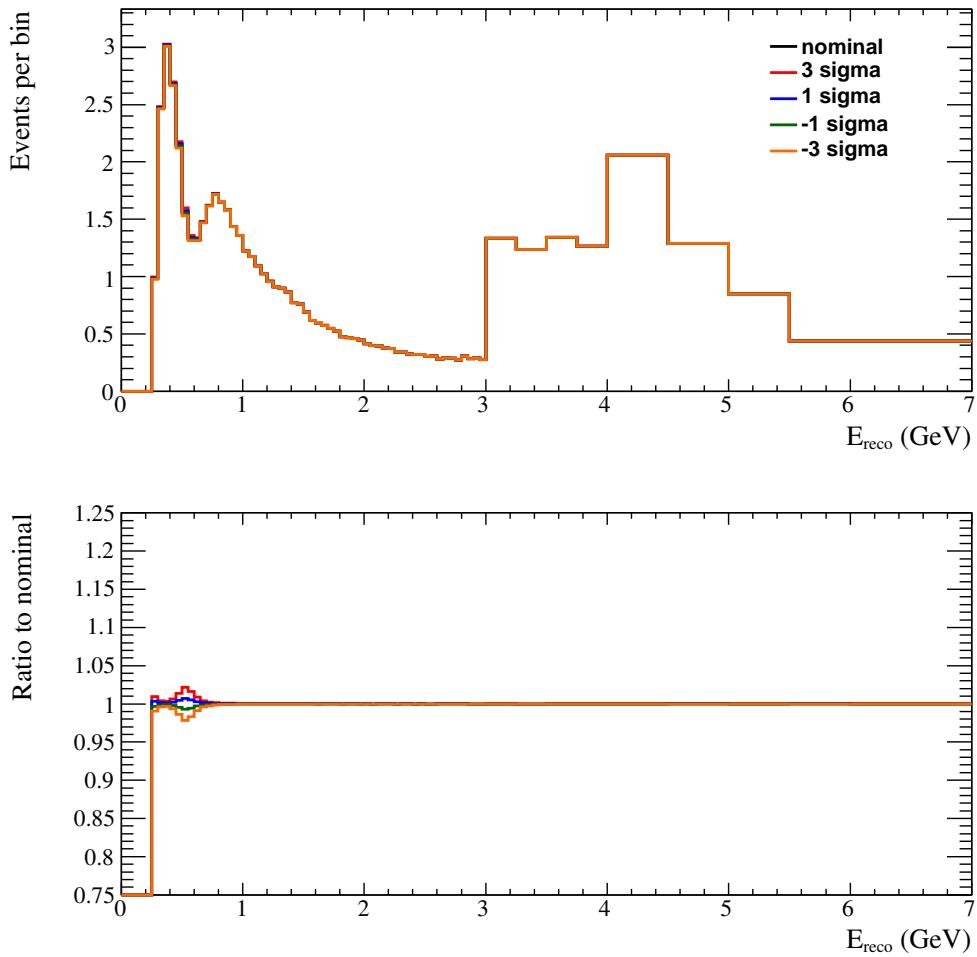


Figure 256: Effect of $f_{2;t,r}^{\text{baff}}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

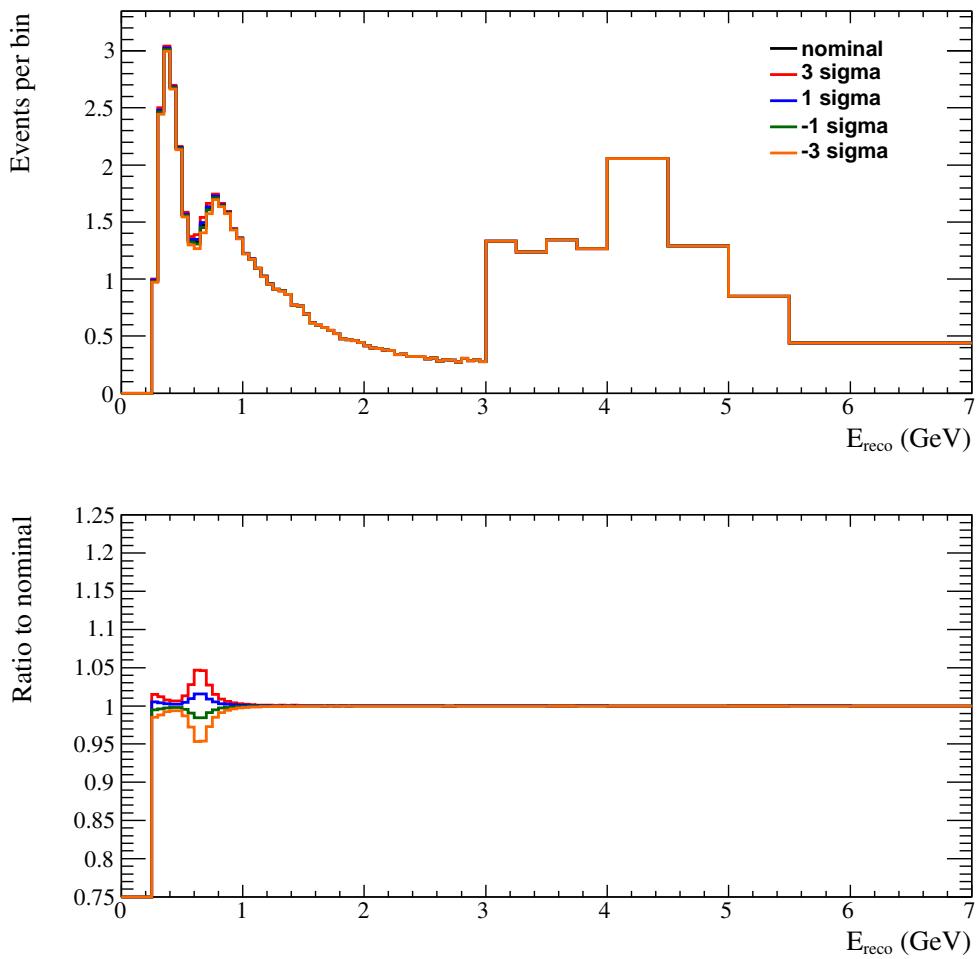


Figure 257: Effect of $f_{3;t,r}^{\text{baff}}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

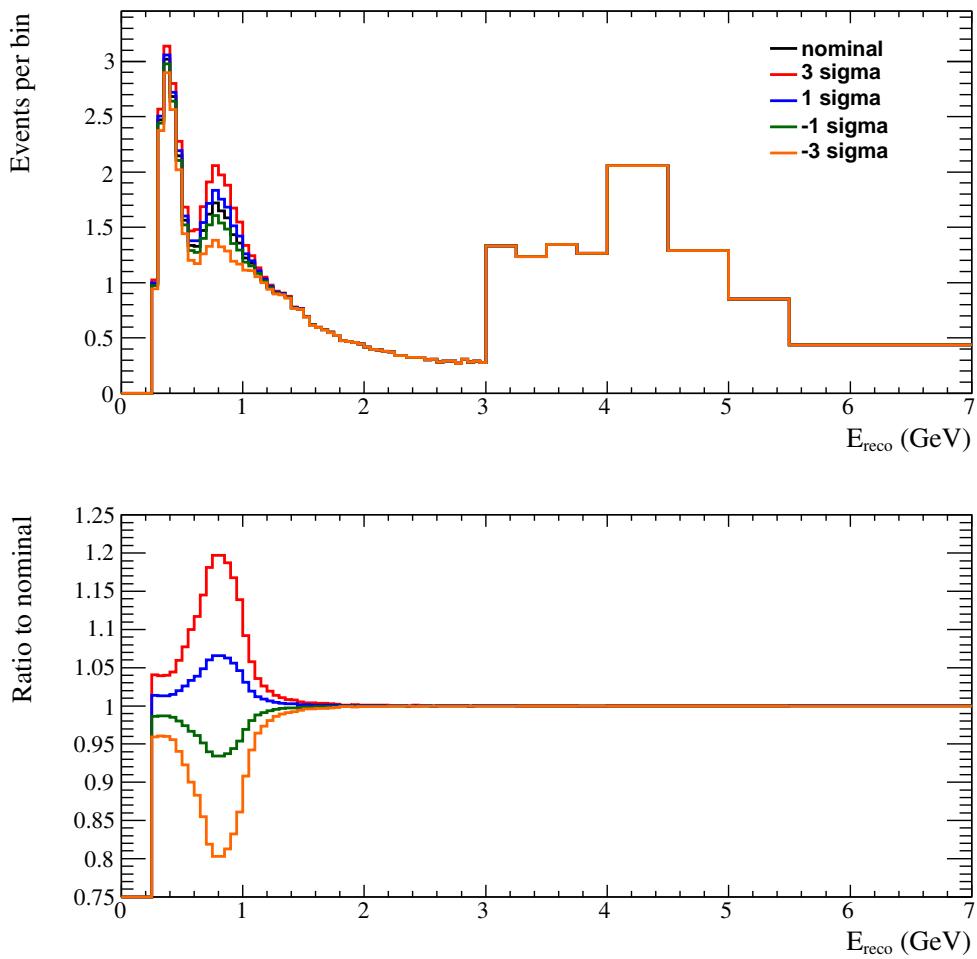


Figure 258: Effect of $f_{4;t,r}^{\text{baff}}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

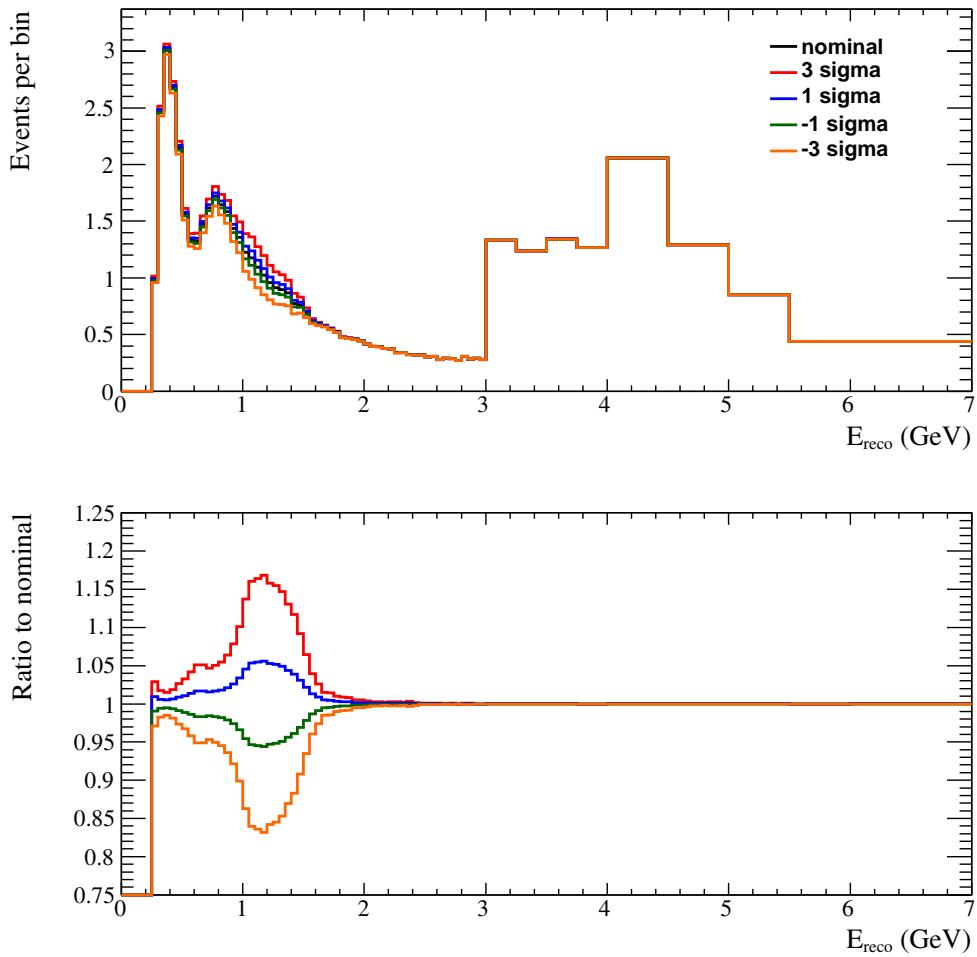


Figure 259: Effect of $f_{5;t,r}^{\text{baff}}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

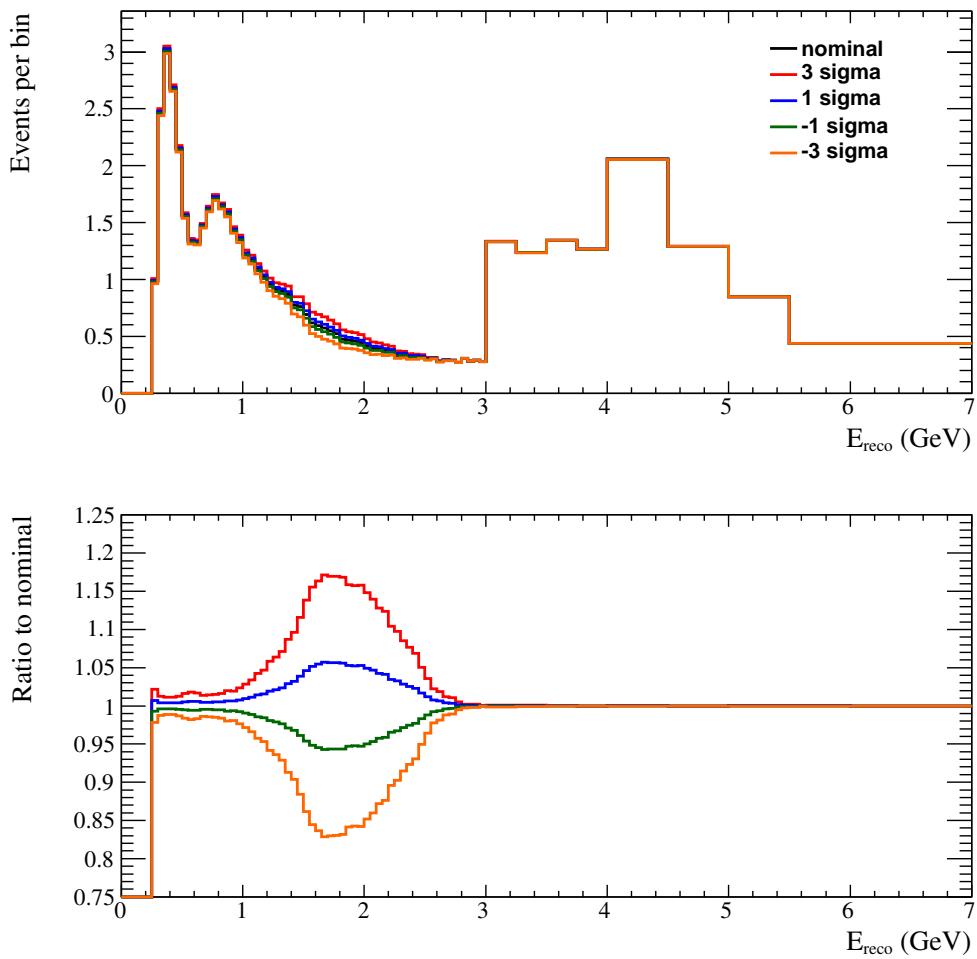


Figure 260: Effect of $f_{6;t,r}^{\text{baff}}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

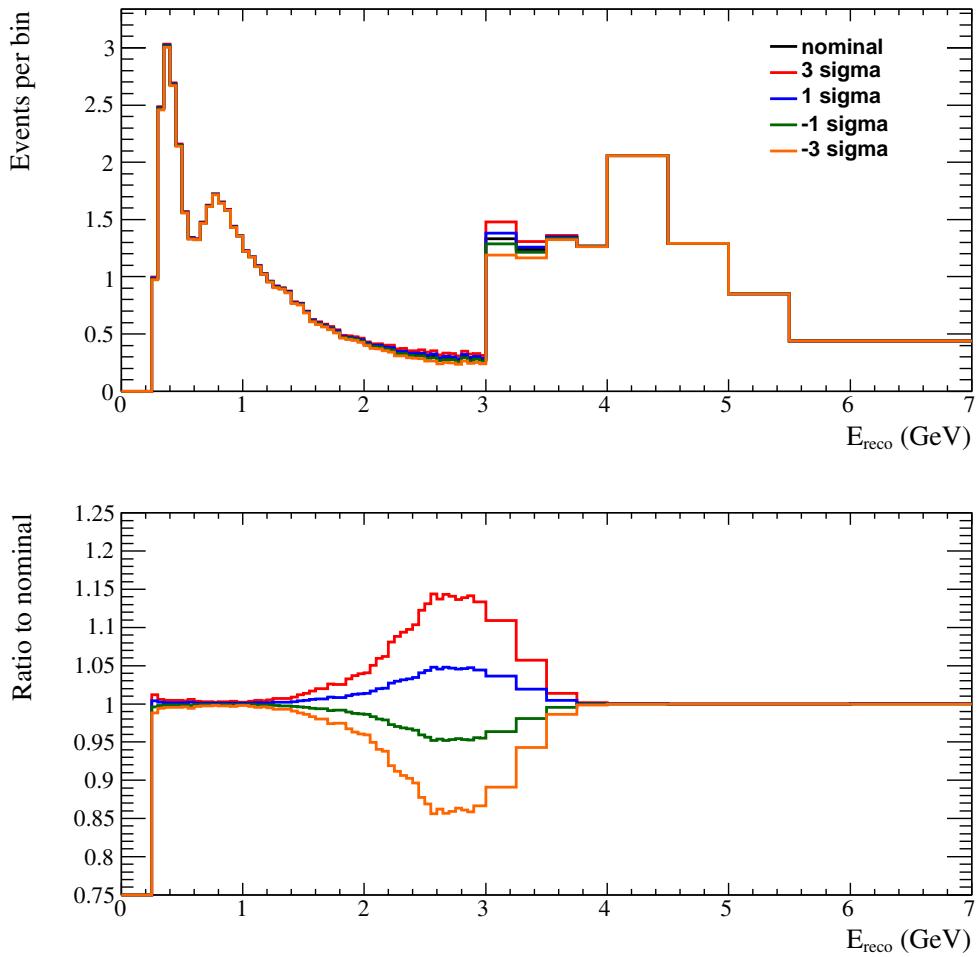


Figure 261: Effect of $f_{7;t,r}^{\text{baff}}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

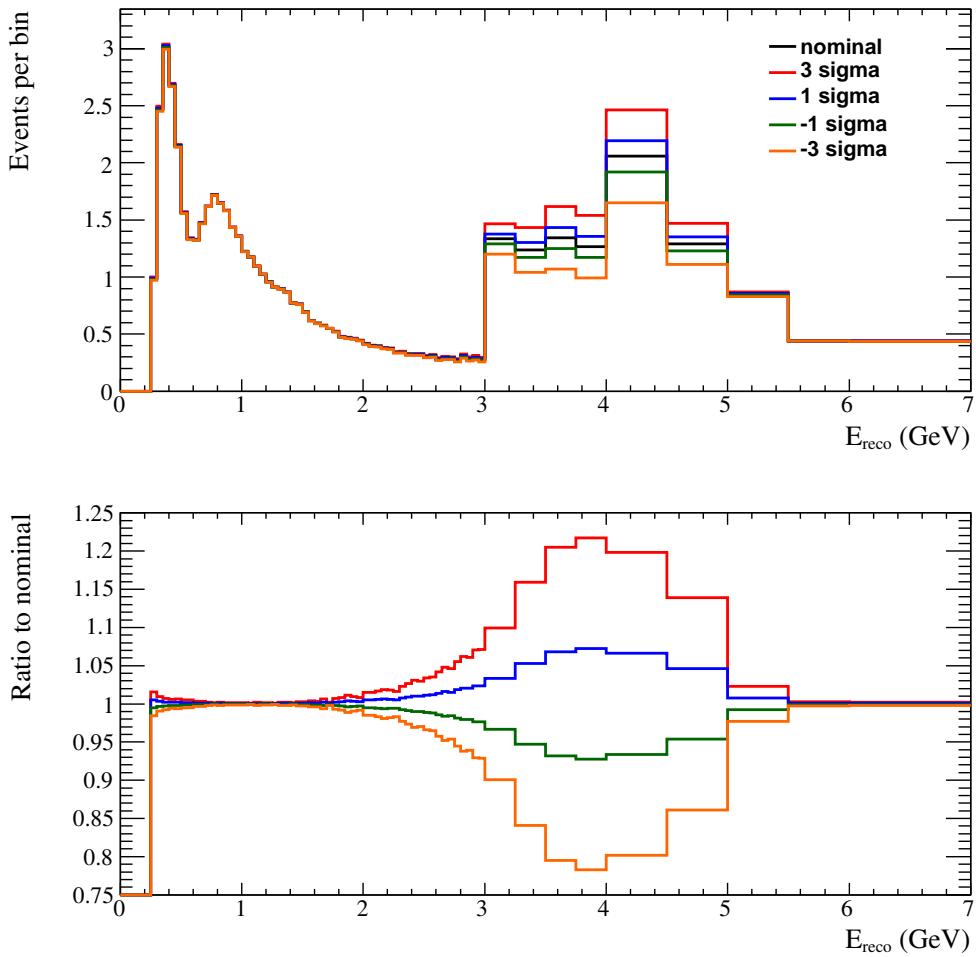


Figure 262: Effect of $f_{g;t,r}^{\text{baff}}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

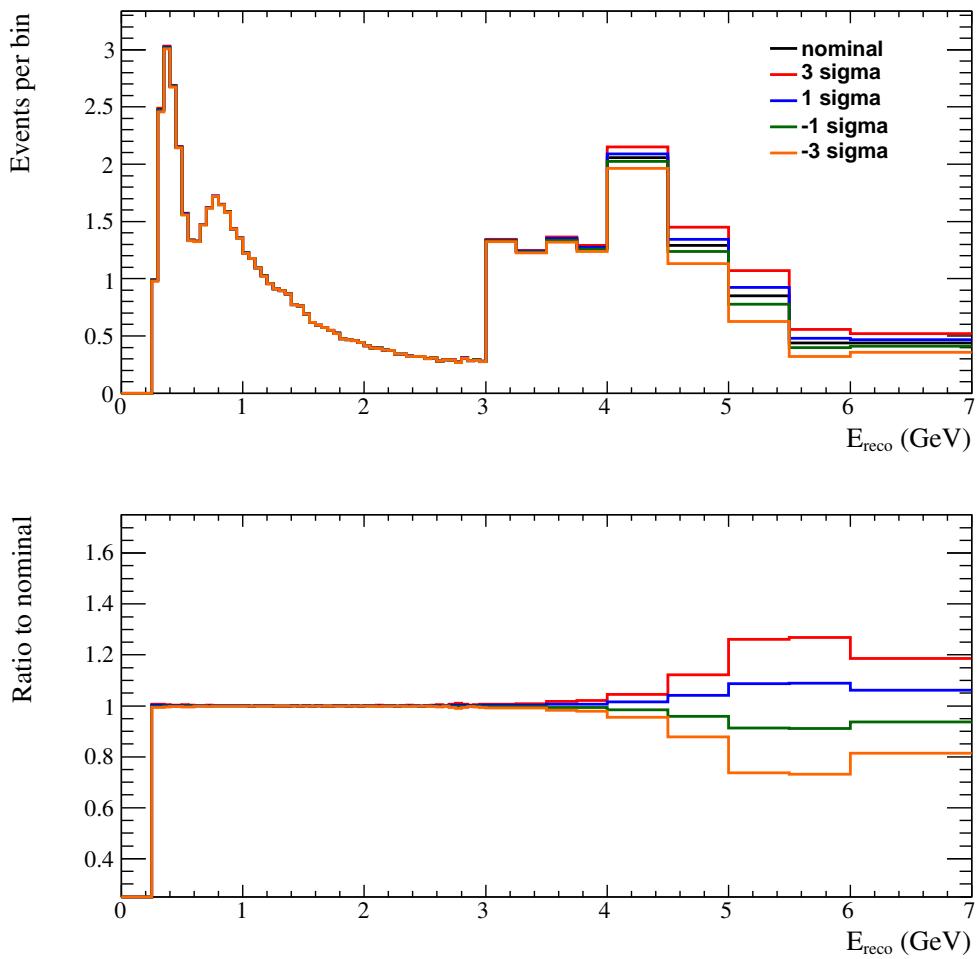


Figure 263: Effect of $f_{9;t,r}^{\text{baff}}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

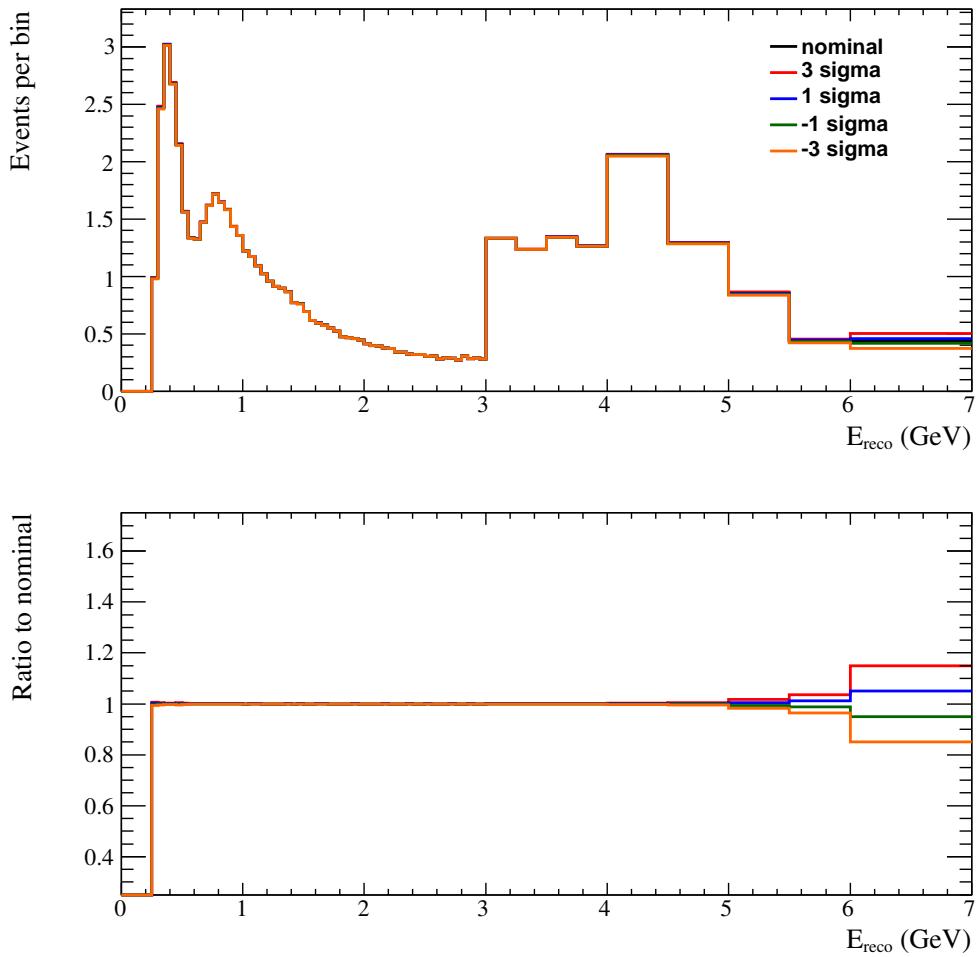


Figure 264: Effect of $f_{10;t,r}^{\text{baff}}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

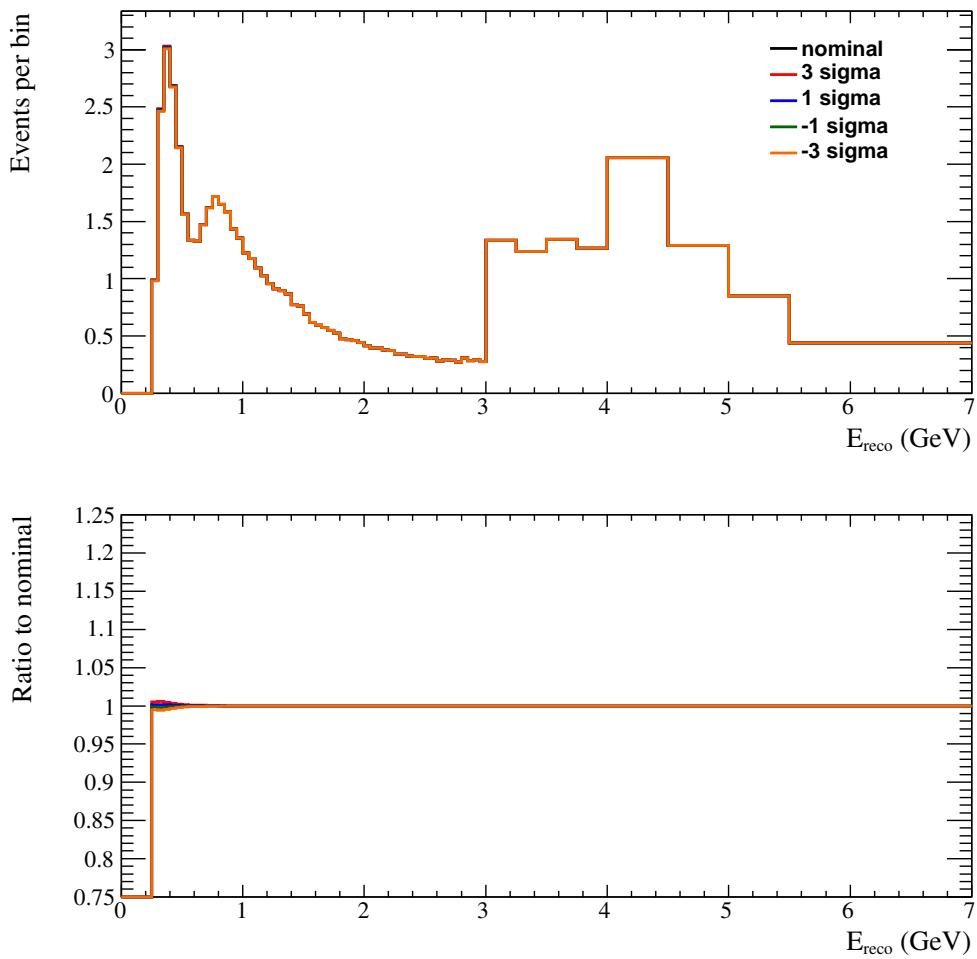


Figure 265: Effect of $f_{11;t,r}^{\text{baff}}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

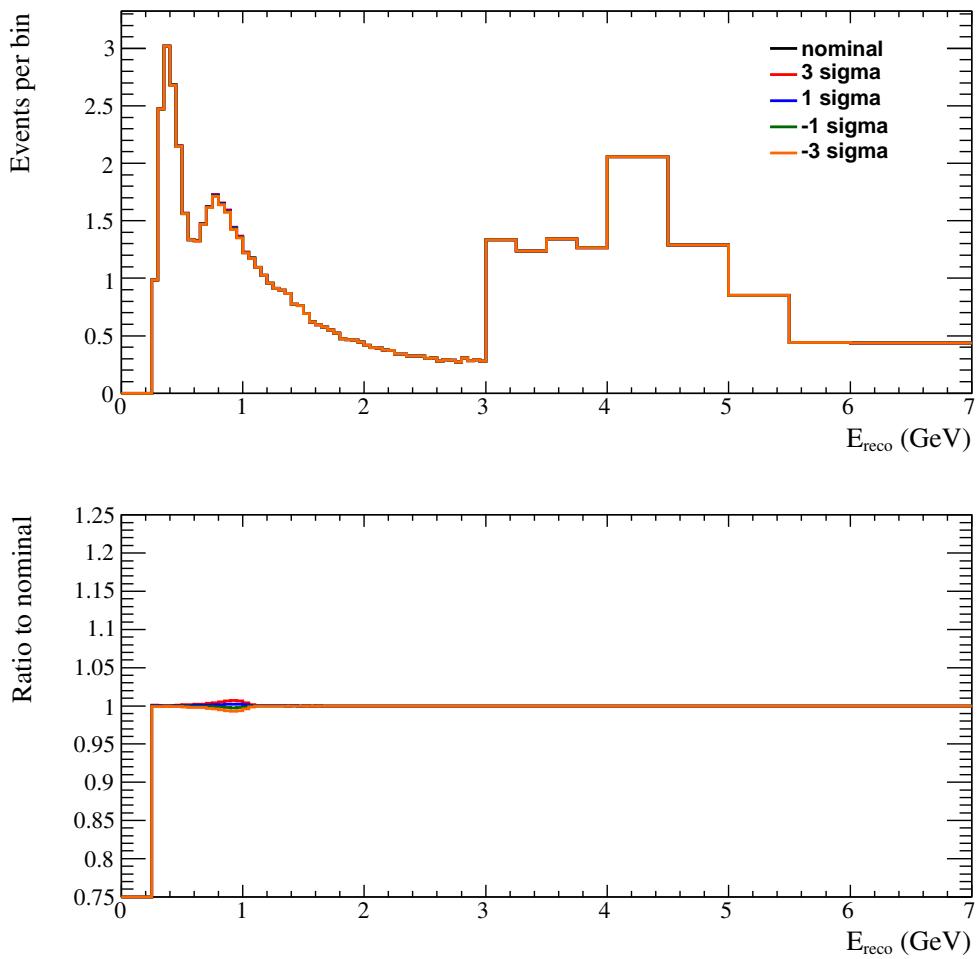


Figure 266: Effect of $f_{12;t,r}^{\text{baff}}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

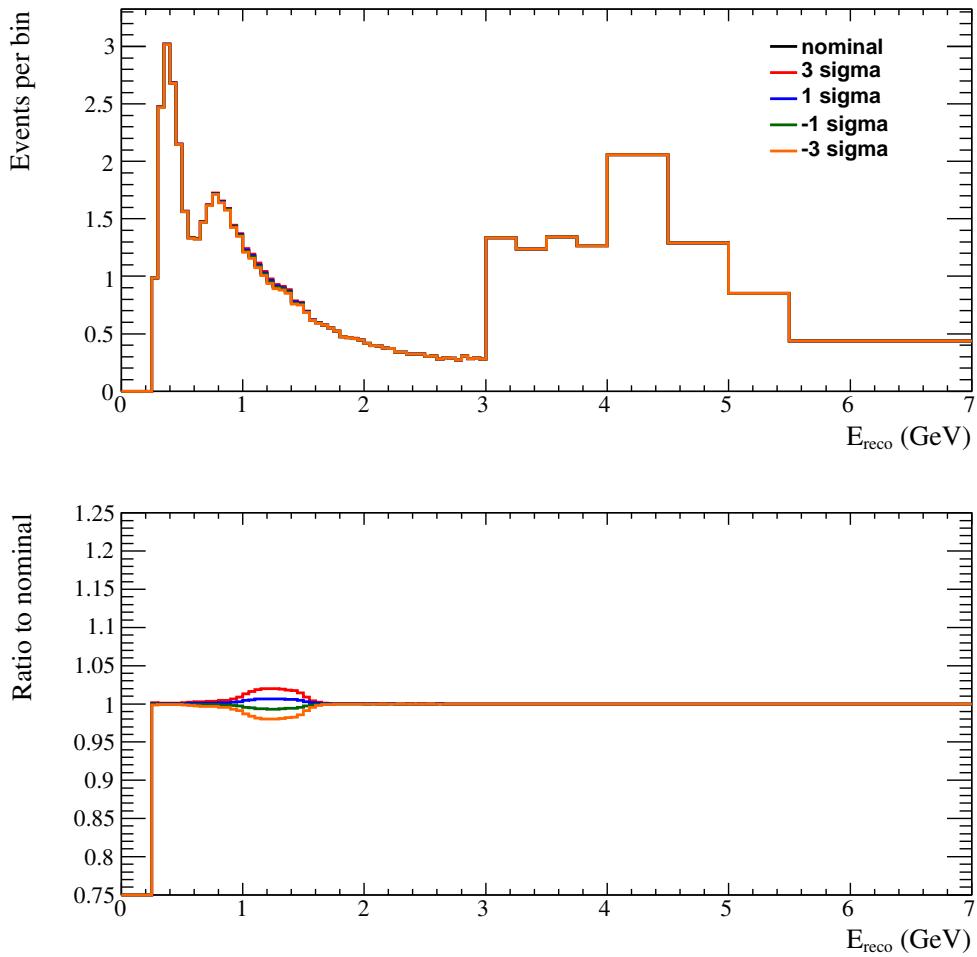


Figure 267: Effect of $f_{13;t,r}^{\text{baff}}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

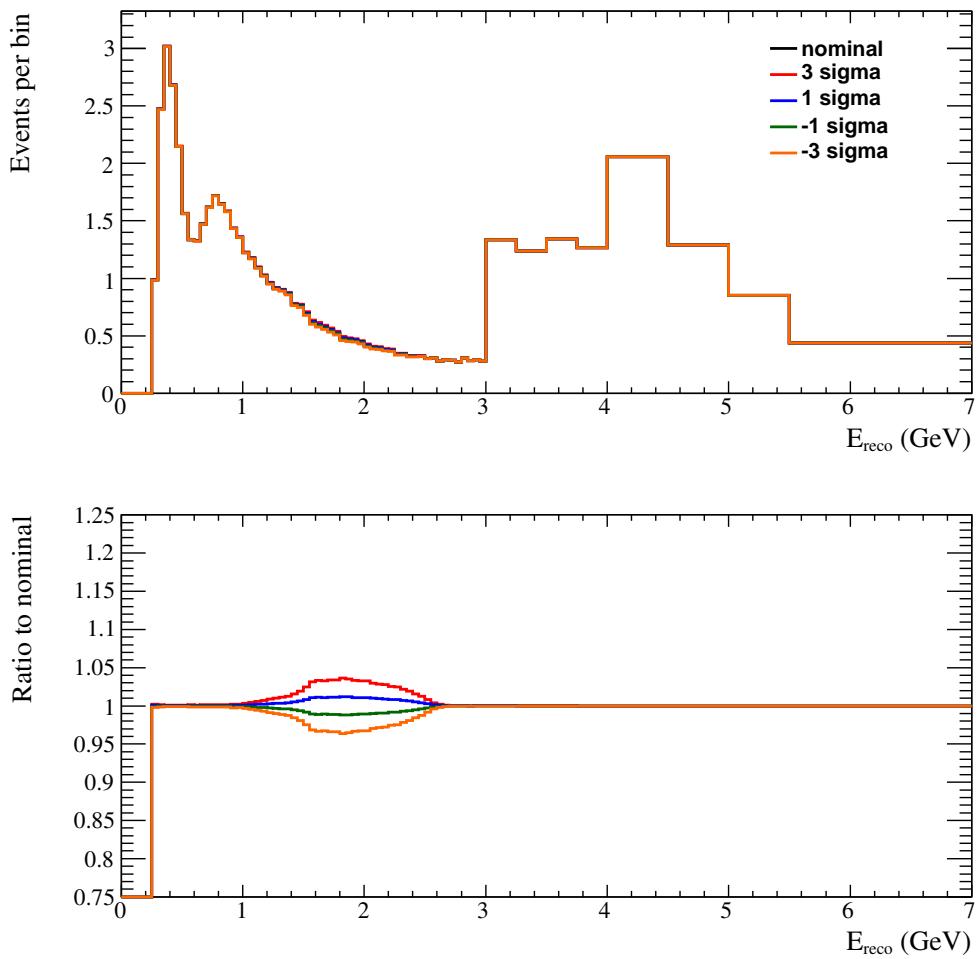


Figure 268: Effect of $f_{14;t,r}^{\text{baff}}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

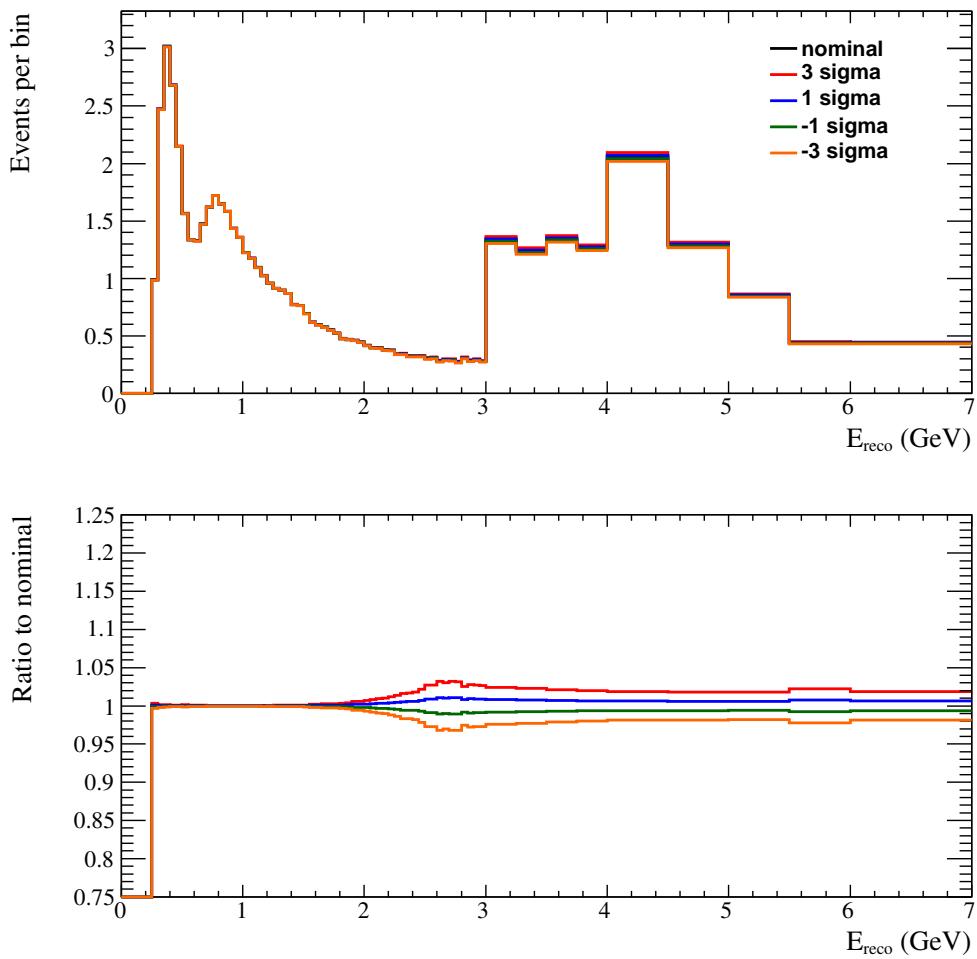


Figure 269: Effect of $f_{15;t,r}^{\text{baff}}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

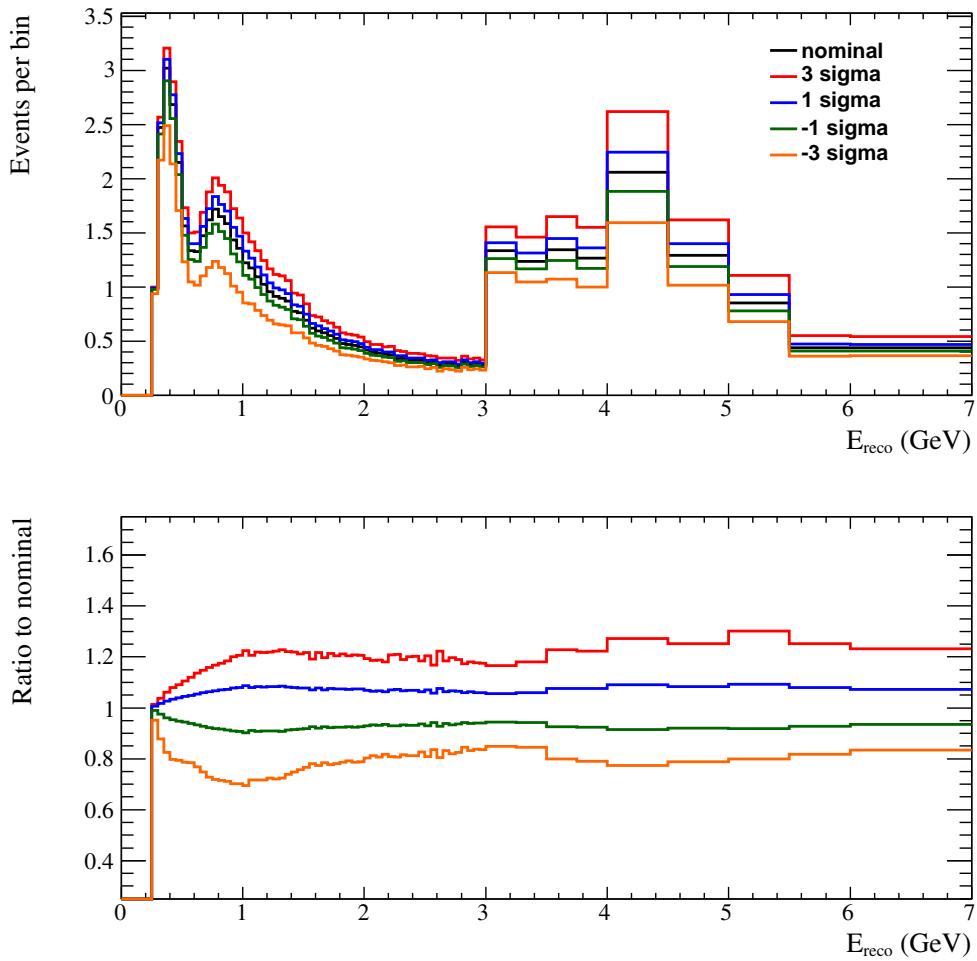


Figure 270: Effect of $f_{16;t,r}^{\text{baff}}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

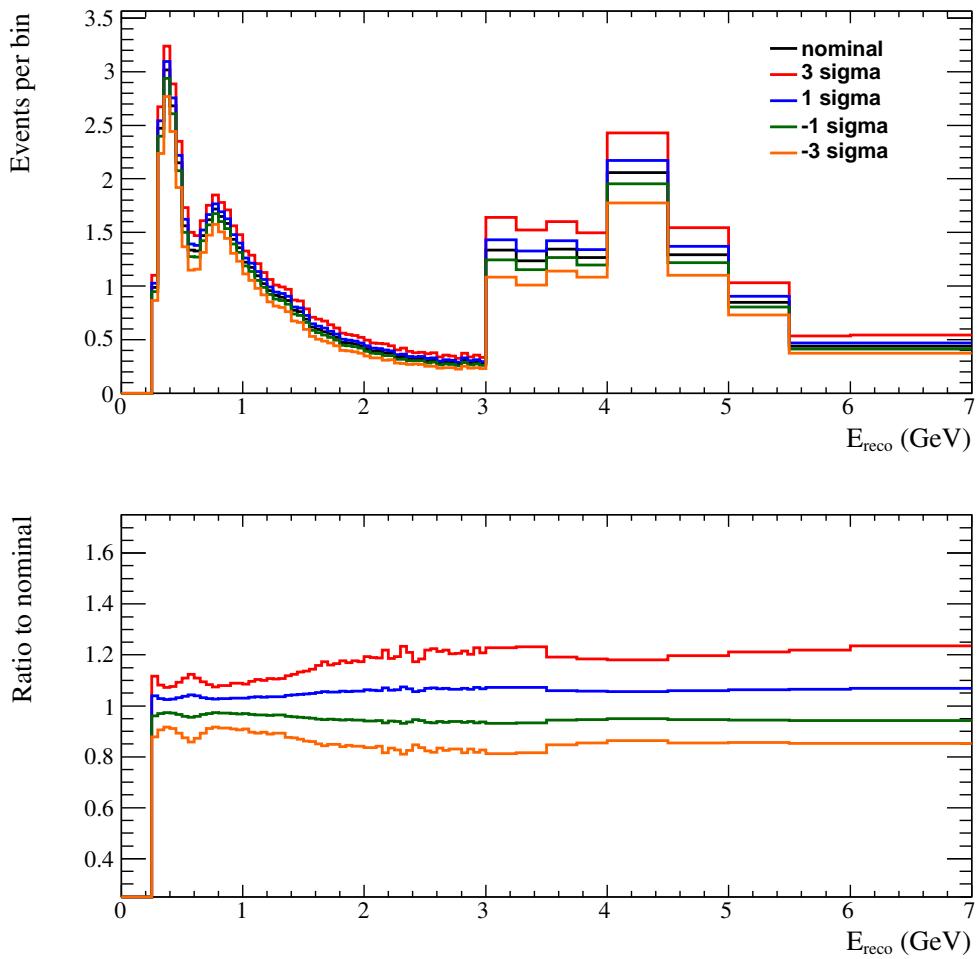


Figure 271: Effect of $f_{17;t,r}^{\text{baff}}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

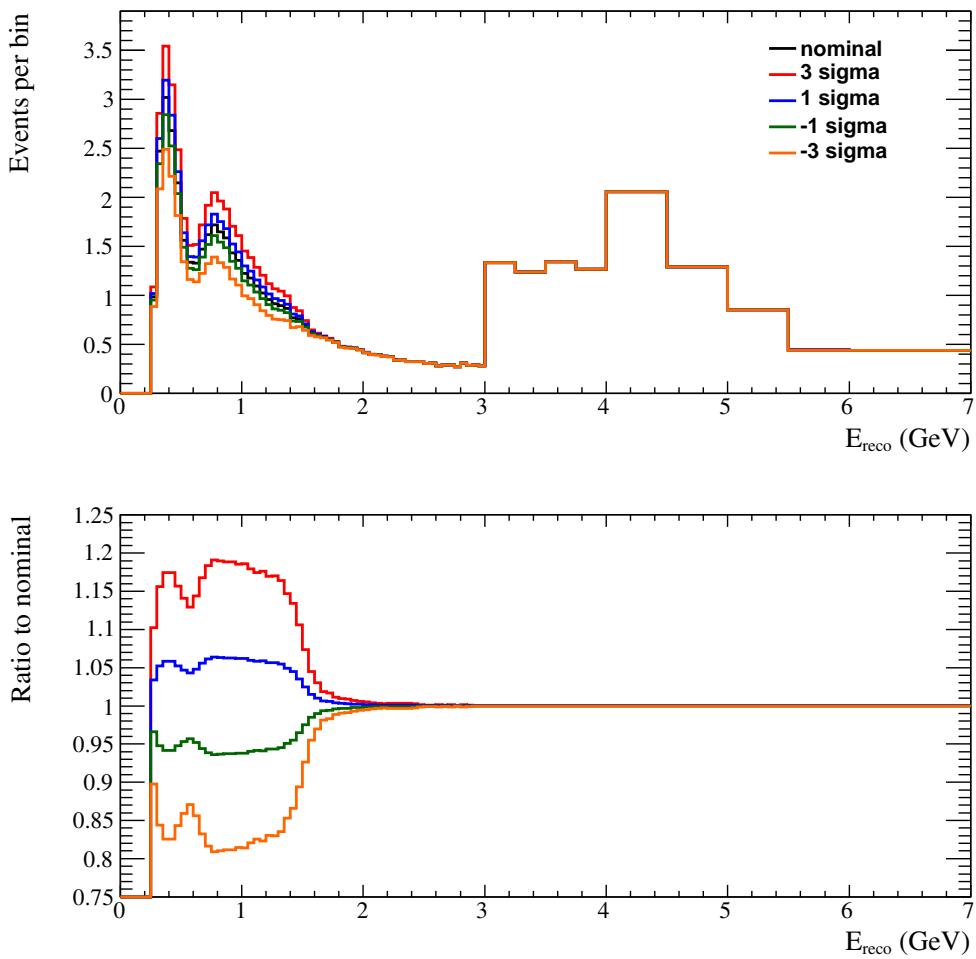


Figure 272: Effect of $f_{18;t,r}^{\text{baff}}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

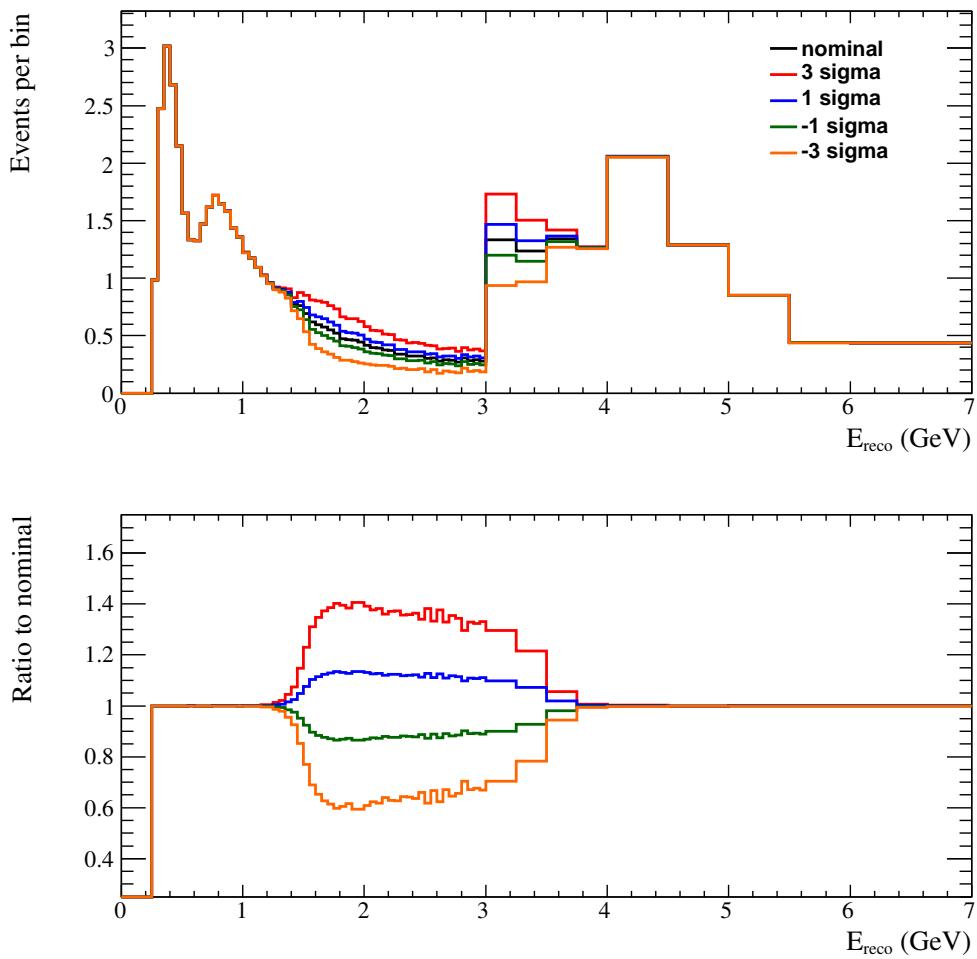


Figure 273: Effect of $f_{19;t,r}^{\text{baff}}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

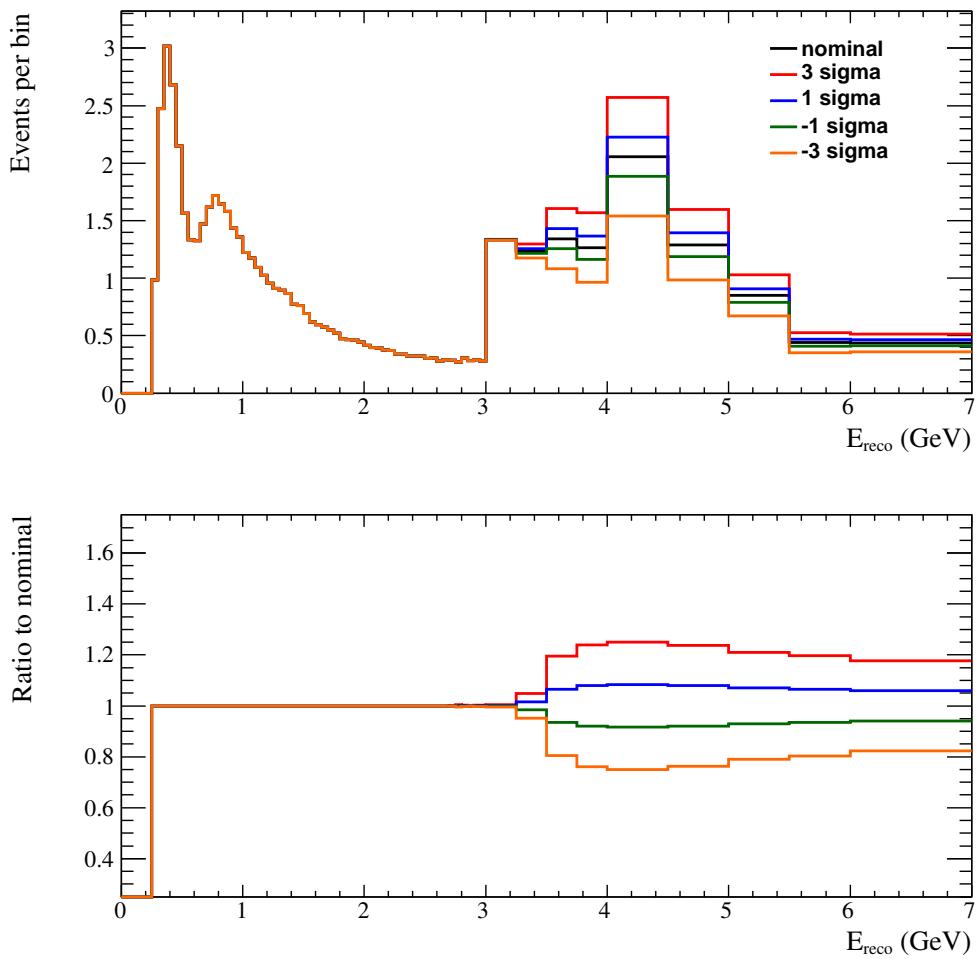


Figure 274: Effect of $f_{20;t,r}^{\text{baff}}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

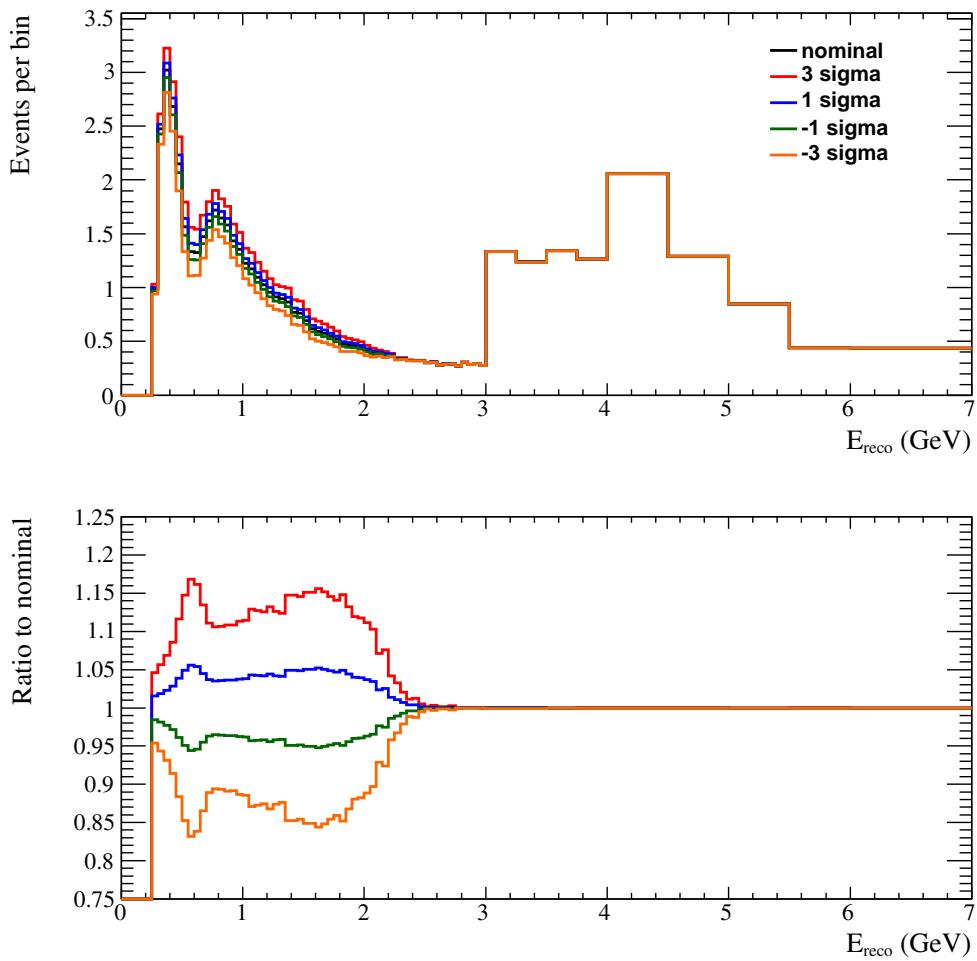


Figure 275: Effect of $f_{21;t,r}^{\text{baff}}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

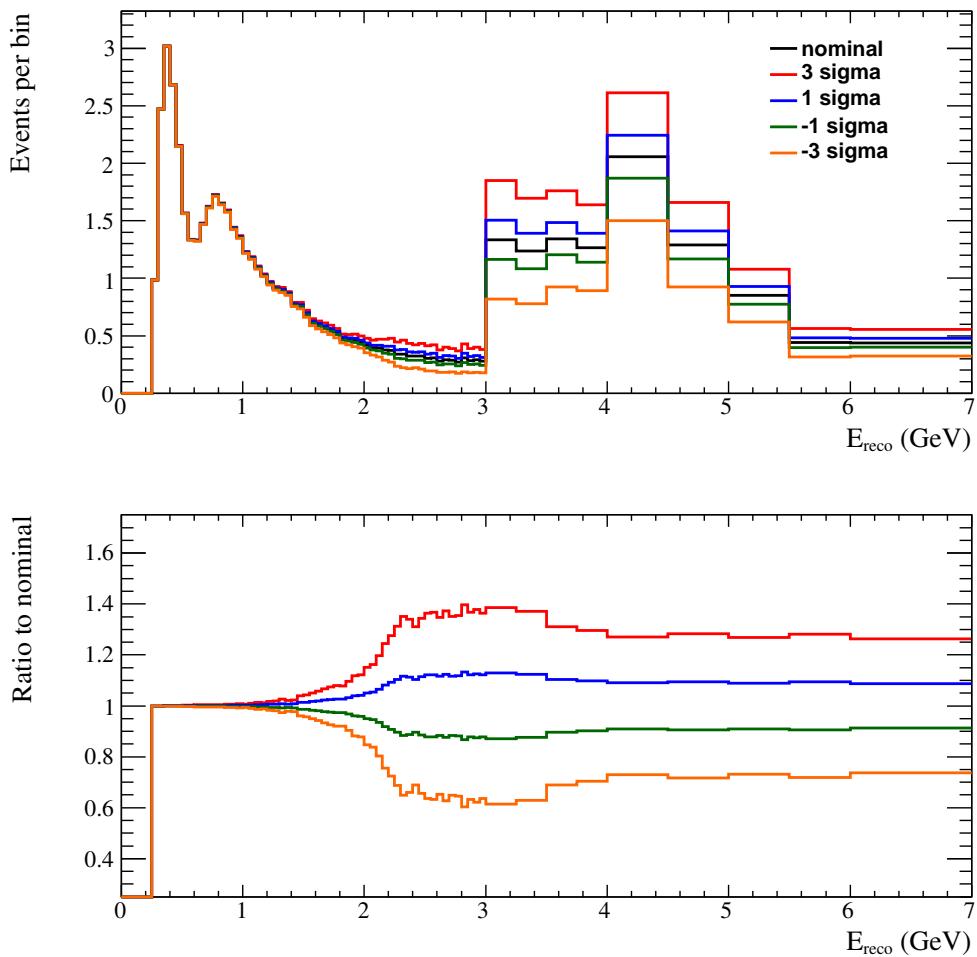


Figure 276: Effect of $f_{22;t,r}^{baff}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

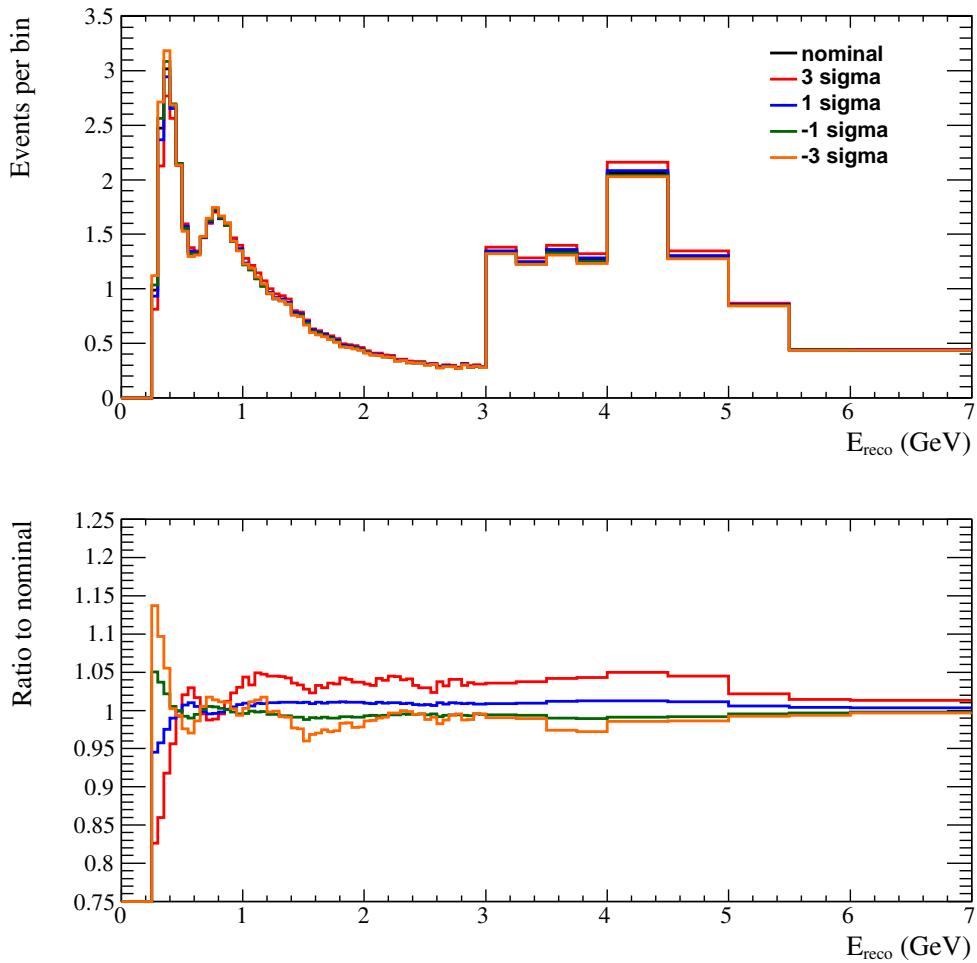


Figure 277: Effect of $f_p F_{t,r}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

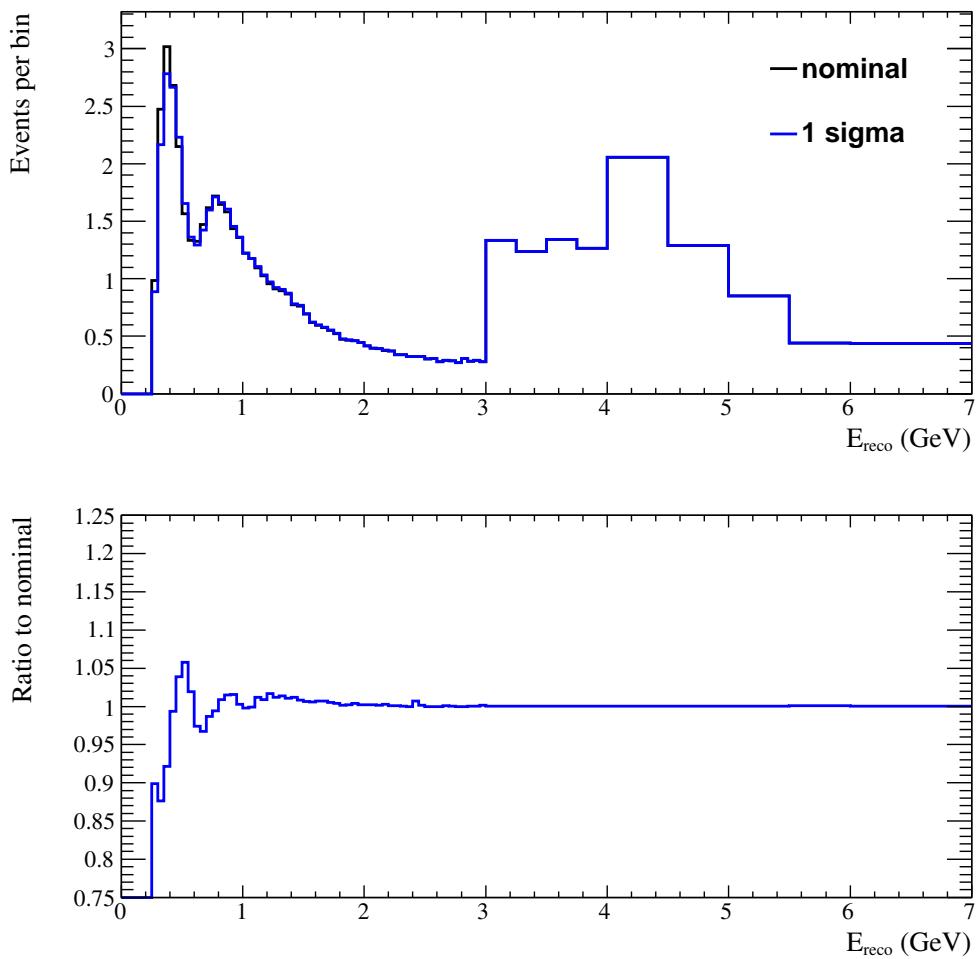


Figure 278: Effect of $f_{SF; t, r}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

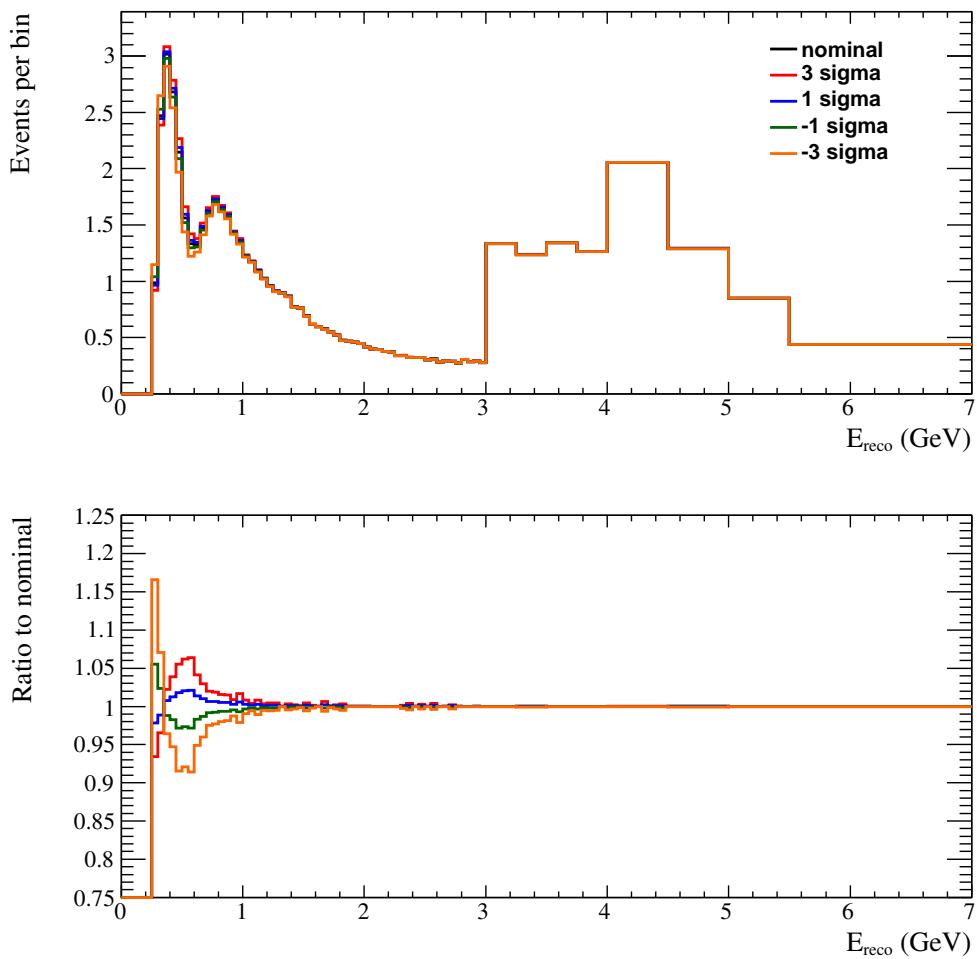


Figure 279: Effect of $f_{W^{shape;t,r}}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

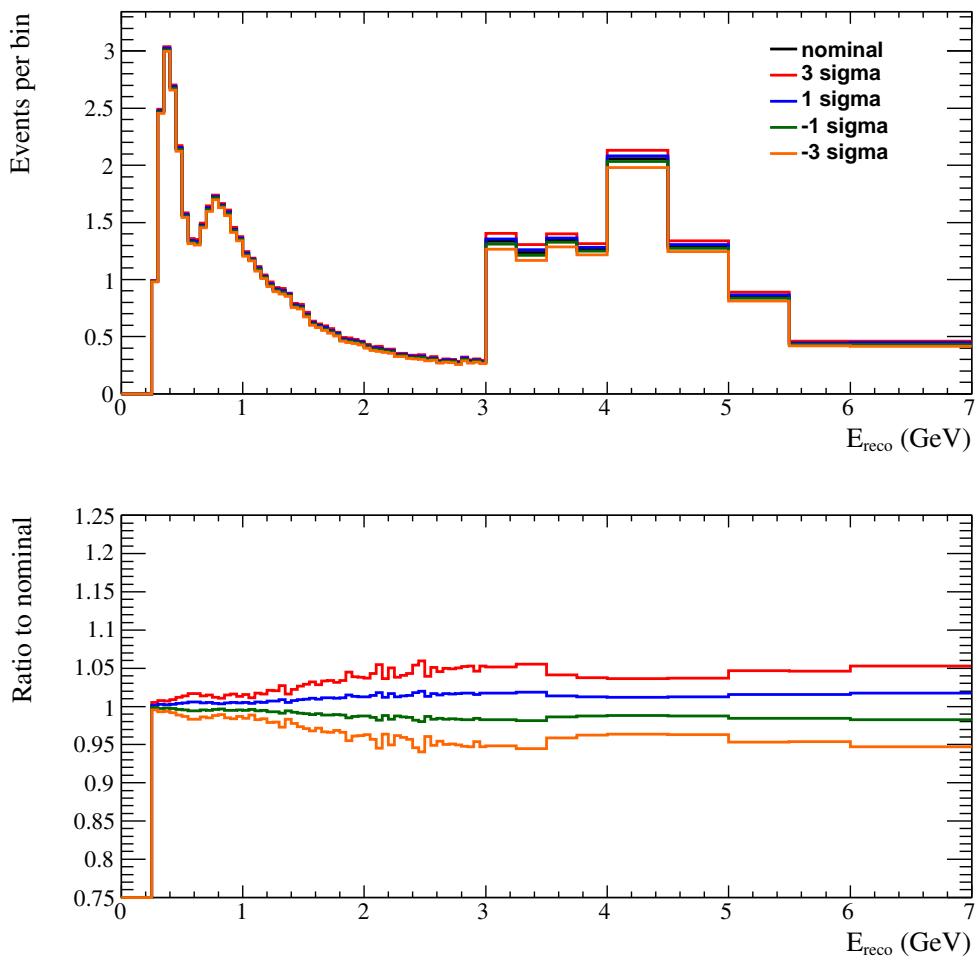


Figure 280: Effect of $f_{CCo\text{oth}Shape;t,r}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

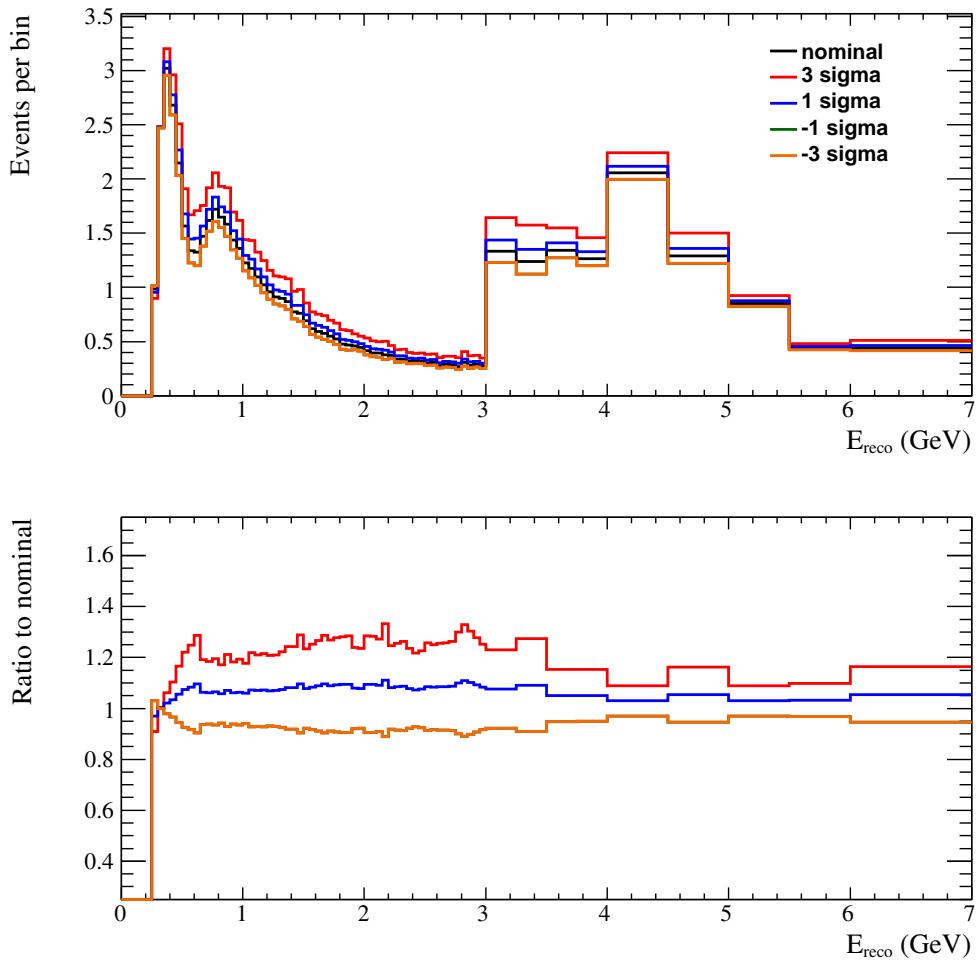


Figure 281: Effect of $f_{\pi\text{-}less}\Delta_{t,r}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

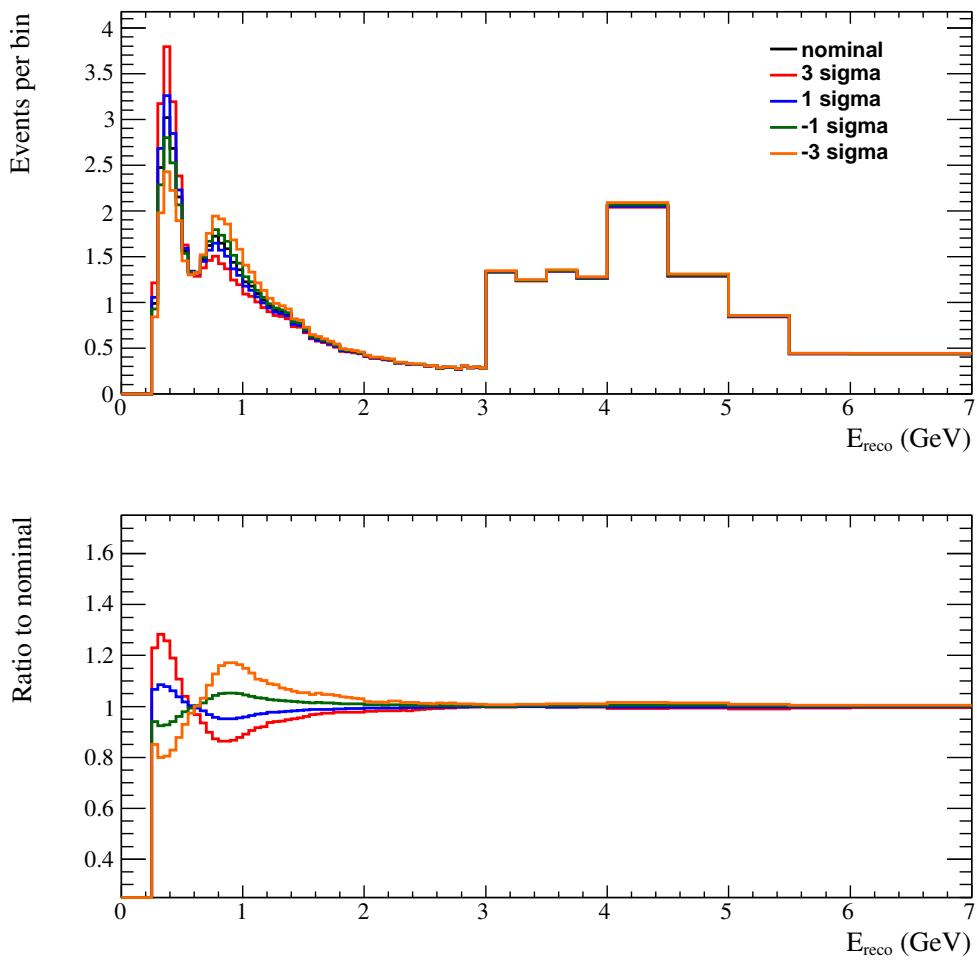


Figure 282: Effect of $f_{bindE;t,r}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

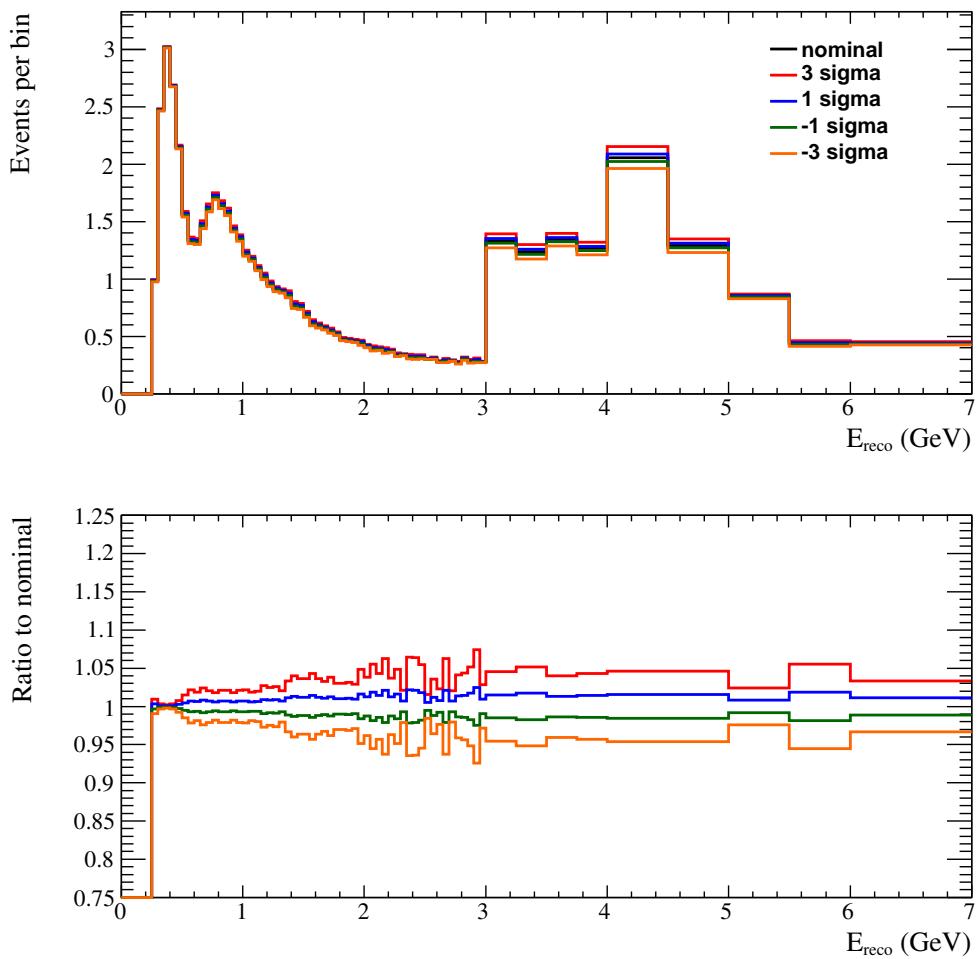


Figure 283: Effect of $f_{CCcoh;t}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

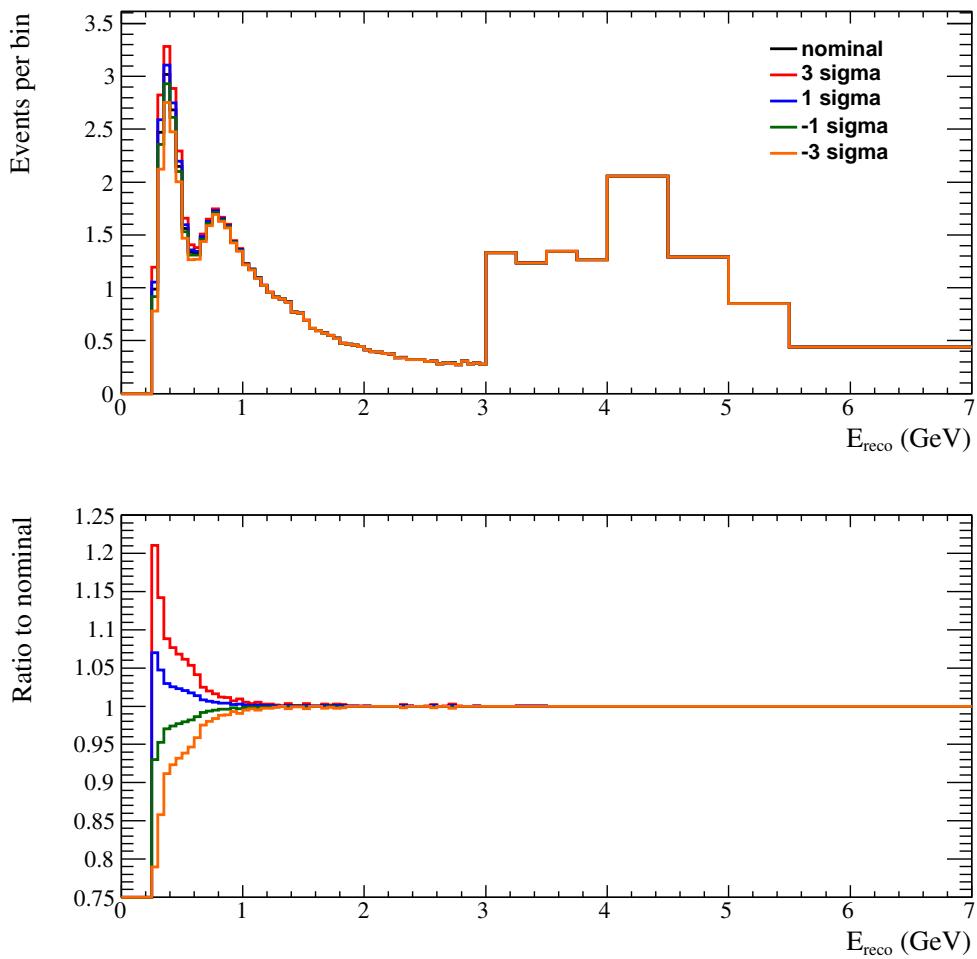


Figure 284: Effect of $f_{NC1\pi^\pm;t}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

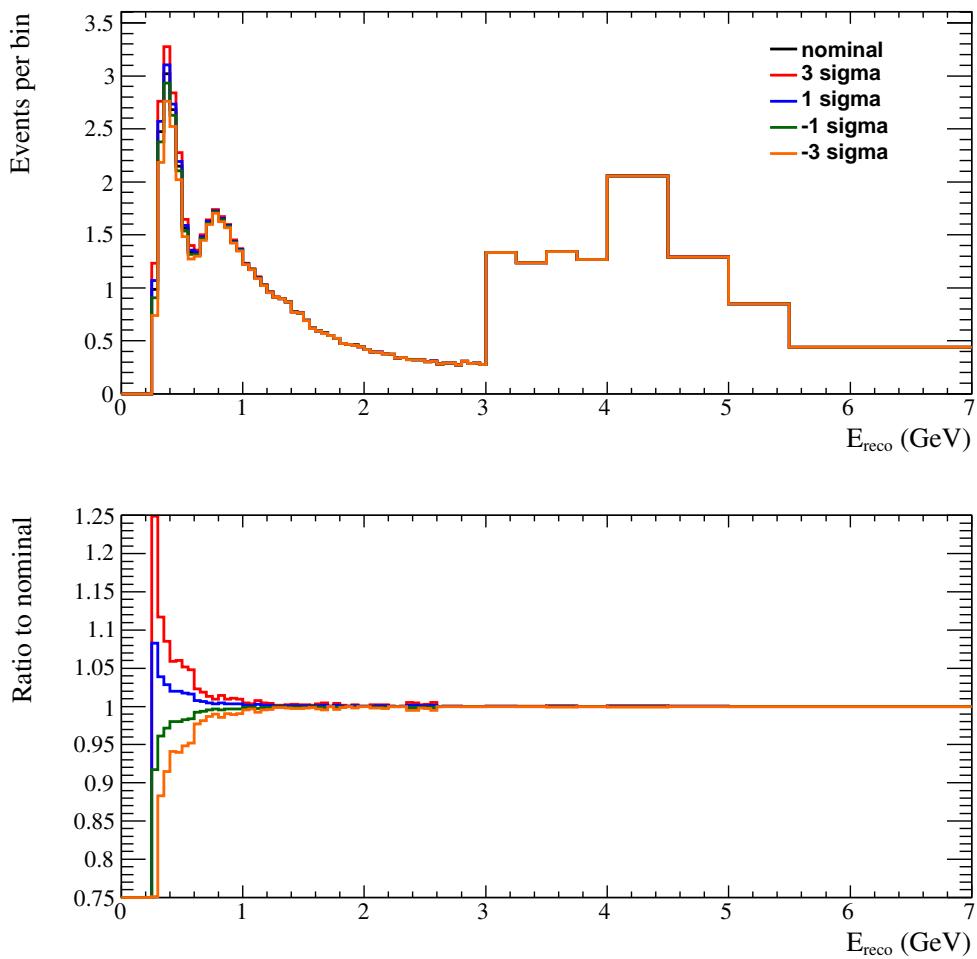


Figure 285: Effect of f_{NCoth_t} for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

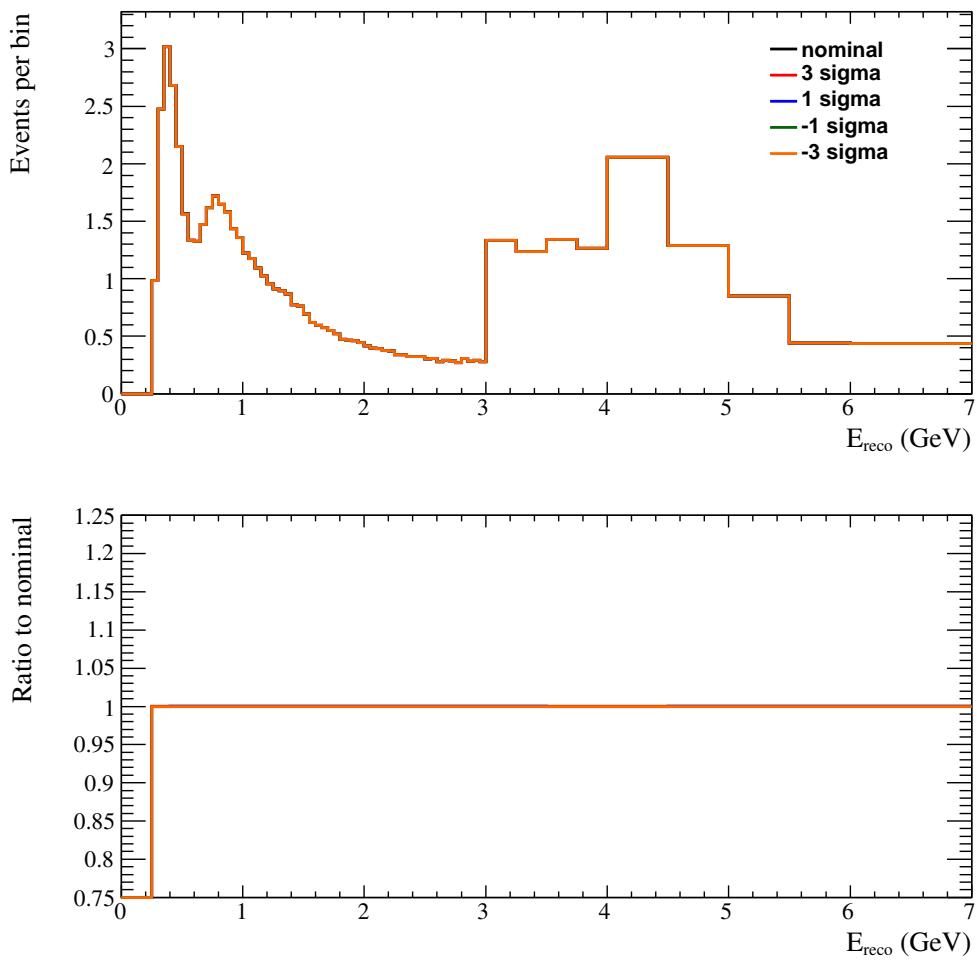


Figure 286: Effect of $f_{CC\nu_e;t}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

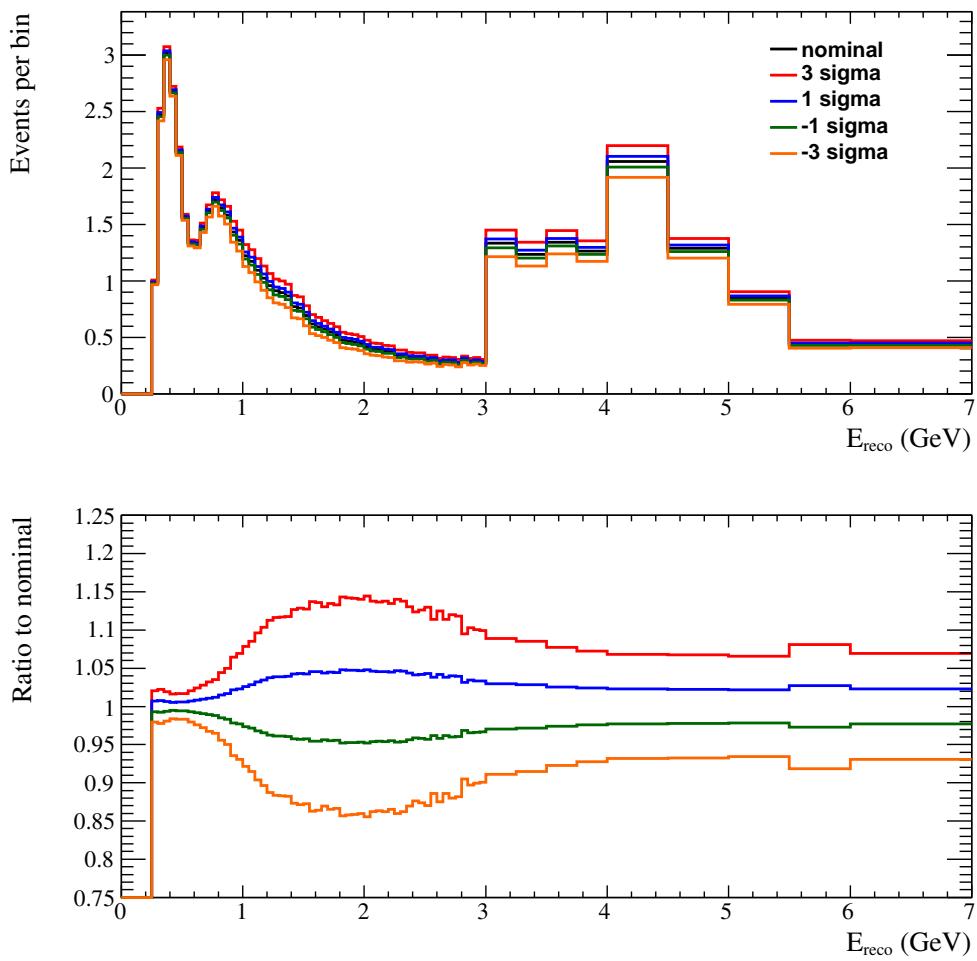


Figure 287: Effect of $f_{CC\bar{C};t}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

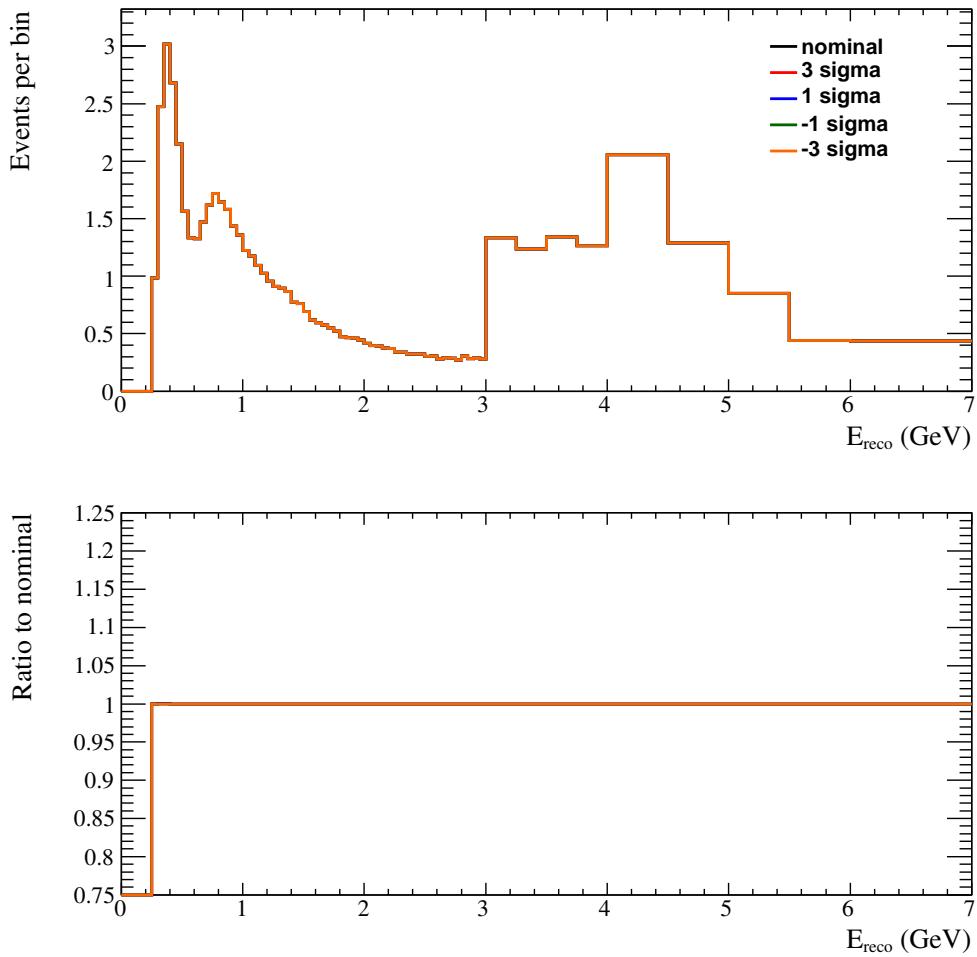


Figure 288: Effect of $f_{0;t,r}^{FSI}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

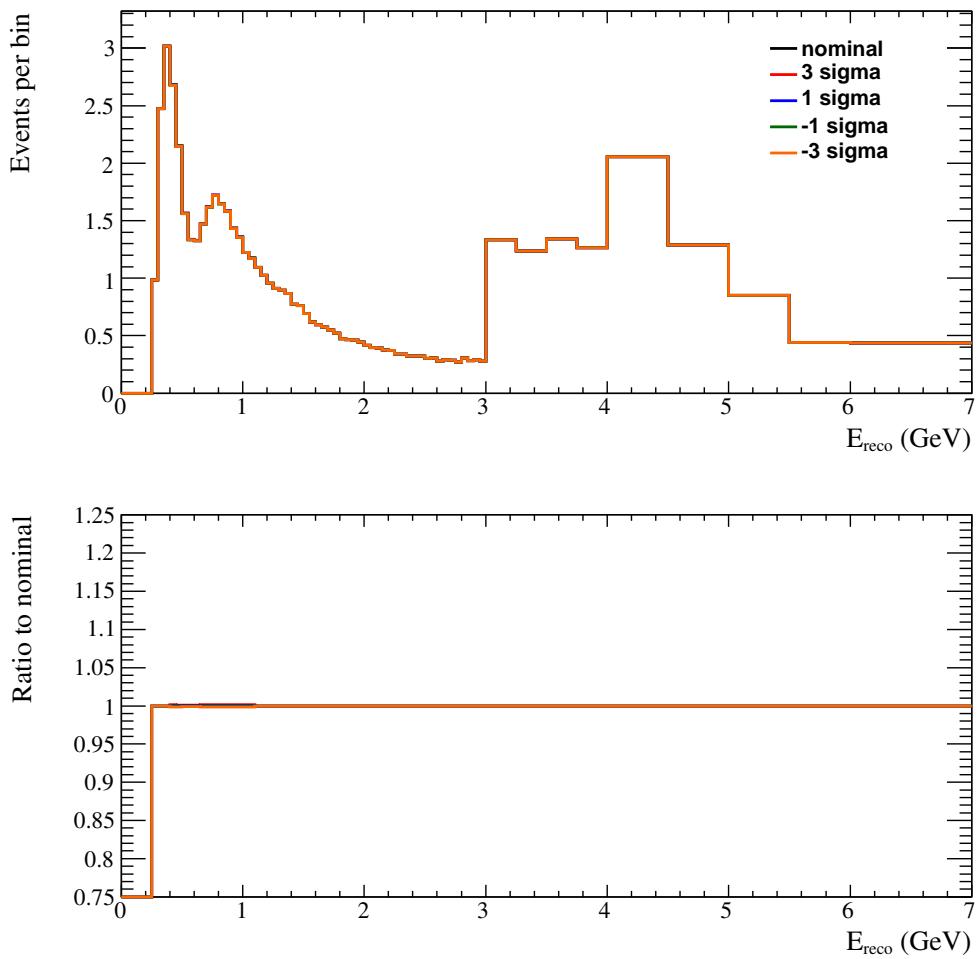


Figure 289: Effect of $f_{1;t,r}^{FSI}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

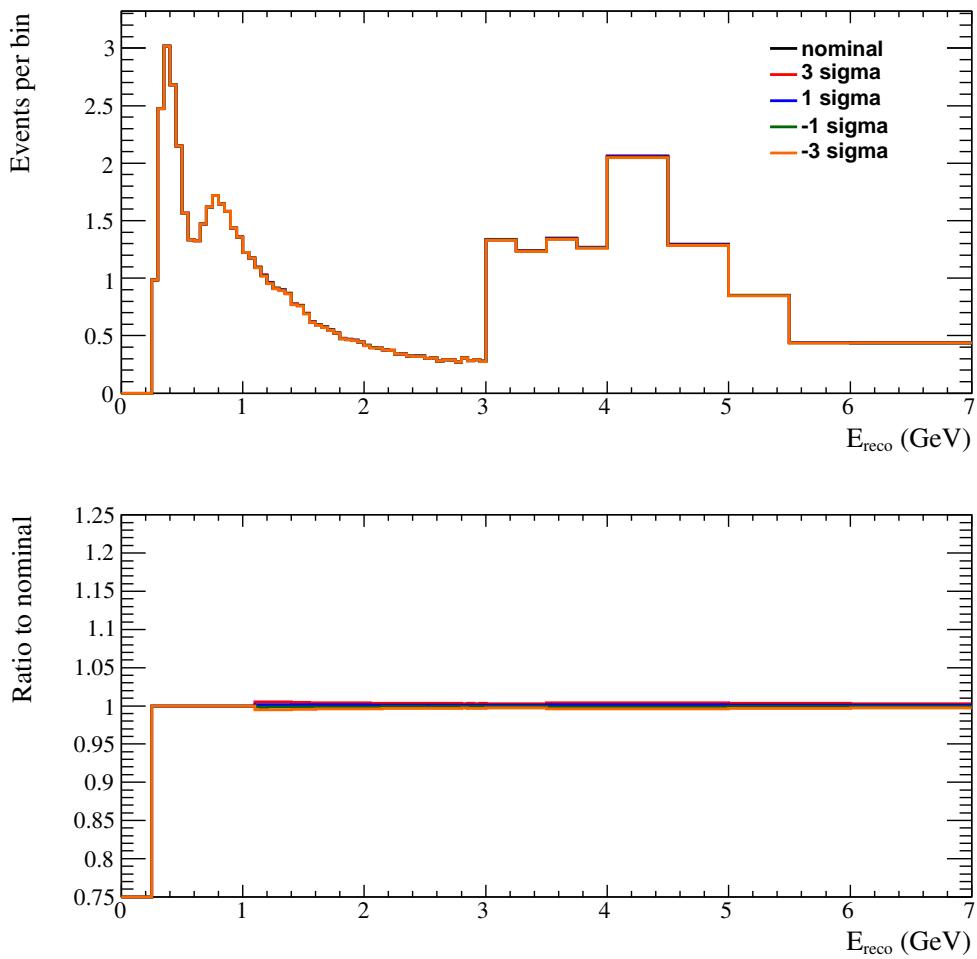


Figure 290: Effect of $f_{2;t,r}^{FSI}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

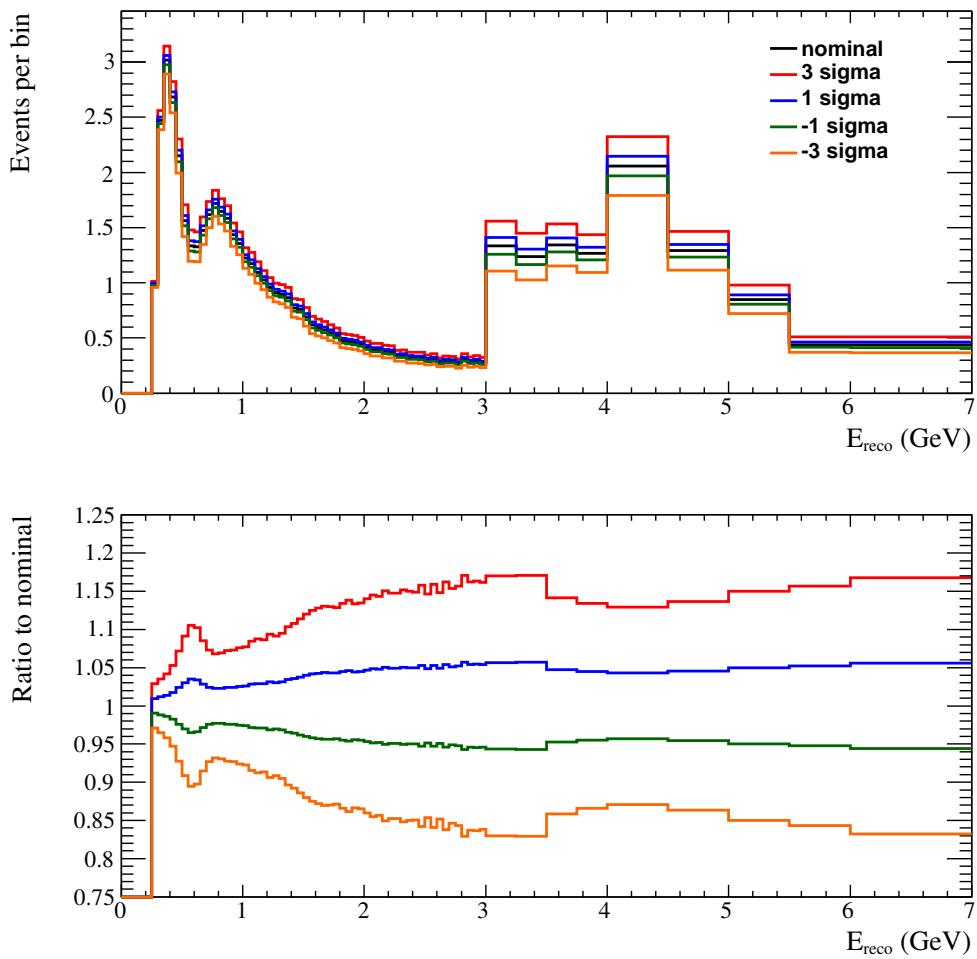


Figure 291: Effect of $f_{3;t,r}^{FSI}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

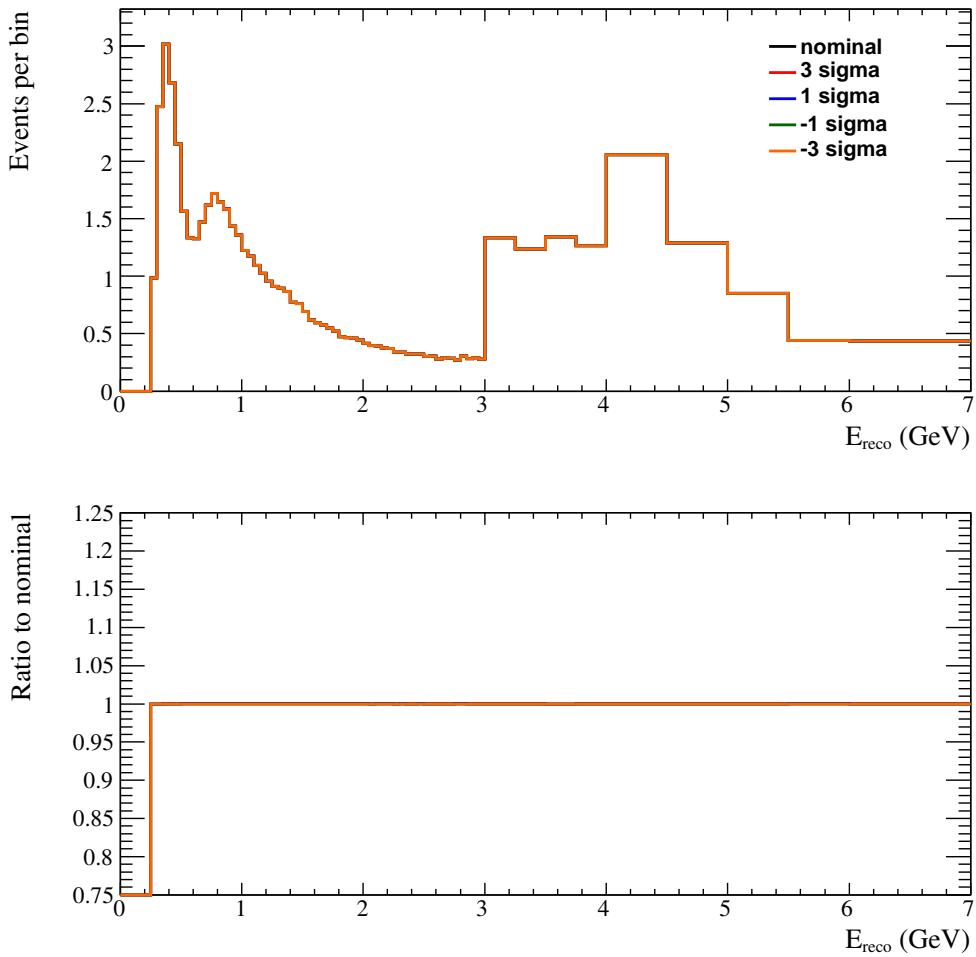


Figure 292: Effect of $f_{4;t,r}^{FSI}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

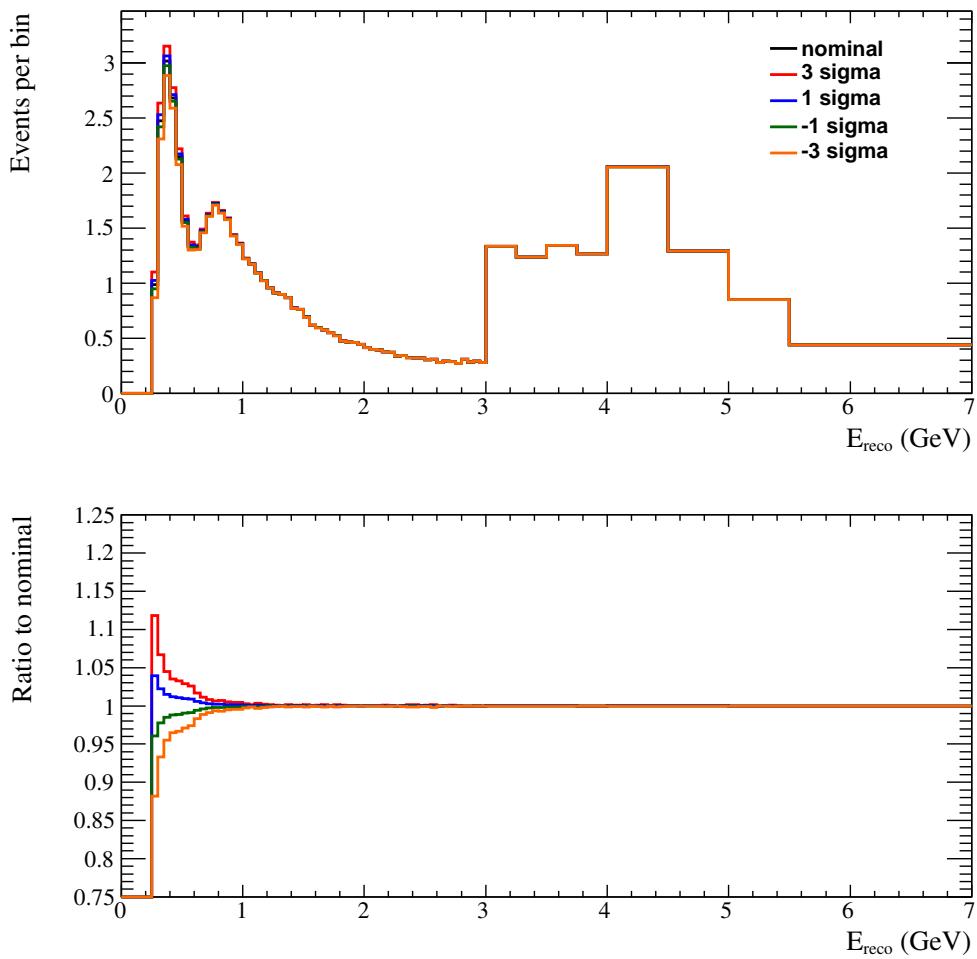


Figure 293: Effect of $f_{5;t,r}^{FSI}$ for 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

1360 **G. Detailed study of the effect of systematics on the best-fit oscillation parameters**

1361 This section describes a study into the effect of systematics on the best-fit oscillation parameters. It was used to
 1362 determine which systematic parameters to include in the 2+8 fit. Before doing the study, it was decided to include a
 1363 systematic if its effect on the best-fit oscillation parameters is greater than one-quarter the size of the statistical error at
 1364 one or more oscillation parameter points. The statistical error was evaluated using 2+0 fits of 10000 toy experiments
 1365 with no systematic fluctuations at each oscillation parameter point. The oscillation parameter points used in this study
 1366 are shown in Fig. 294.

1367 In the study, a 2+0 fit was done on a toy MC experiment created without statistical fluctuations and with a single
 1368 systematic parameter tweaked by $\pm 1\sigma$. For correlated systematic parameters, σ was defined as the square root of the
 1369 corresponding covariance matrix diagonal entry. The best-fit values of the oscillation parameters from the 2+0 fit are
 1370 plotted as an arrow whose origin is at the input point of the study. For ease of reading, no more than 11 systematics are
 1371 included on a single plot; for this reason, the plots are split into the following categories:

- 1372 • parameters used in the 2+8 fit, Figs. 295-308;
- 1373 • SuperK detector parameters, Figs. 309-322;
- 1374 • BANFF ν_μ flux parameters, Figs. 323-336;
- 1375 • BANFF $\bar{\nu}_\mu$ flux parameters, Figs. 337-350;
- 1376 • BANFF cross section parameters, Figs. 351-364;
- 1377 • uncorrelated cross section parameters, Figs. 365-378;
- 1378 • FSI+SI parameters, Figs. 379-392;
- 1379 • non-23 sector oscillation parameters, Figs. 393-406.

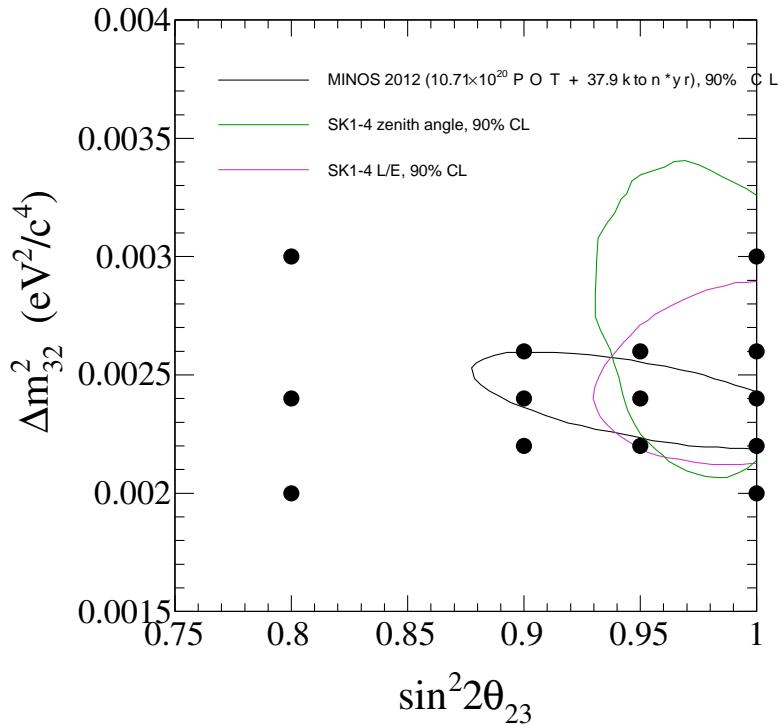


Figure 294: True oscillation parameter points used in the study on the effect of systematics on the best-fit oscillation parameters.

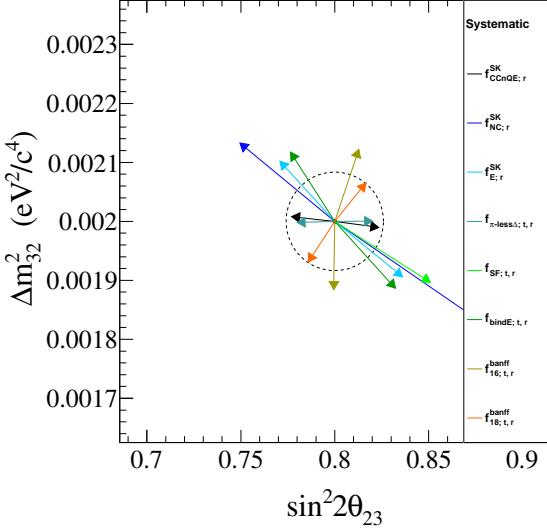


Figure 295: Effect of parameters used in the 2+8 fit on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.8$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{-}05$; $\Delta m_{32}^2 = 0.002$.

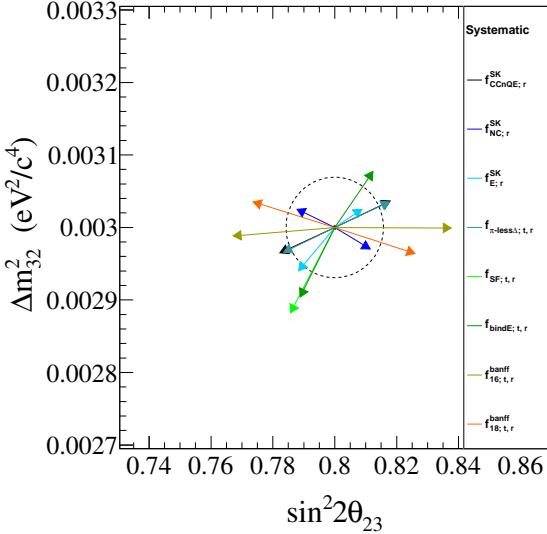


Figure 297: Effect of parameters used in the 2+8 fit on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.8$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{-}05$; $\Delta m_{32}^2 = 0.003$.

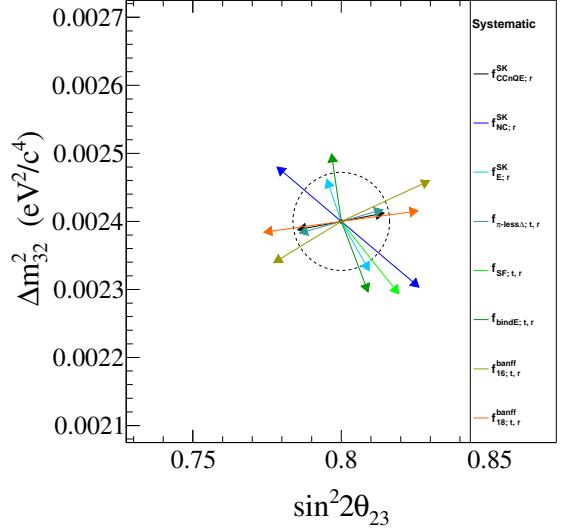


Figure 296: Effect of parameters used in the 2+8 fit on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.8$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{-}05$; $\Delta m_{32}^2 = 0.0024$.

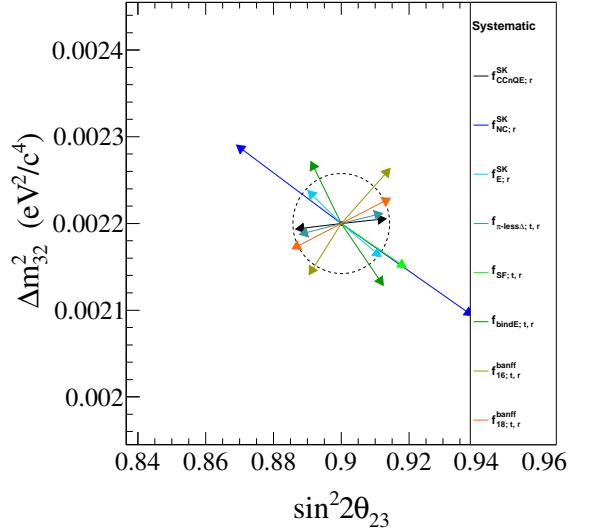


Figure 298: Effect of parameters used in the 2+8 fit on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{-}05$; $\Delta m_{32}^2 = 0.0022$.

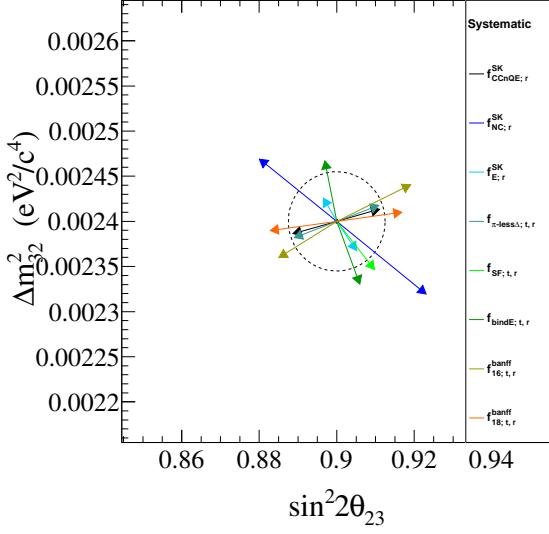


Figure 299: Effect of parameters used in the 2+8 fit on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

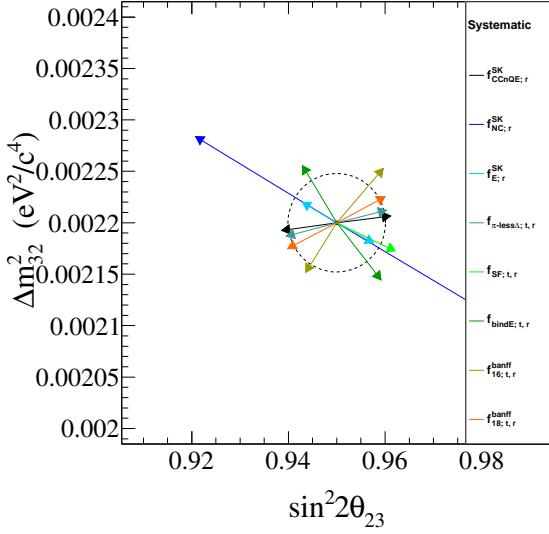


Figure 301: Effect of parameters used in the 2+8 fit on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.95$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \text{e-}05$; $\Delta m_{32}^2 = 0.0022$.

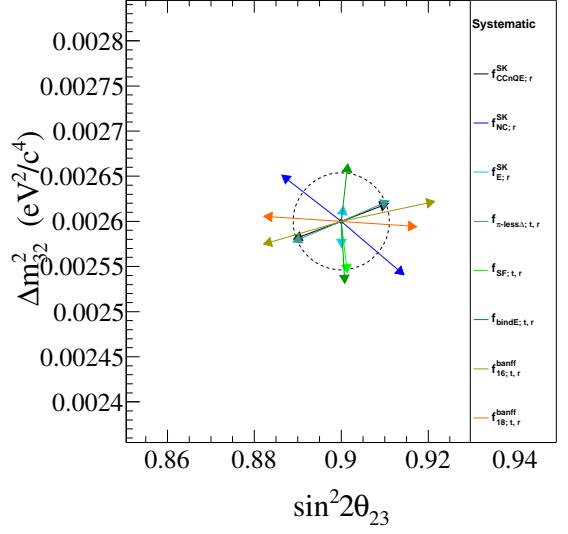


Figure 300: Effect of parameters used in the 2+8 fit on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \text{e-}05$; $\Delta m_{32}^2 = 0.0026$.

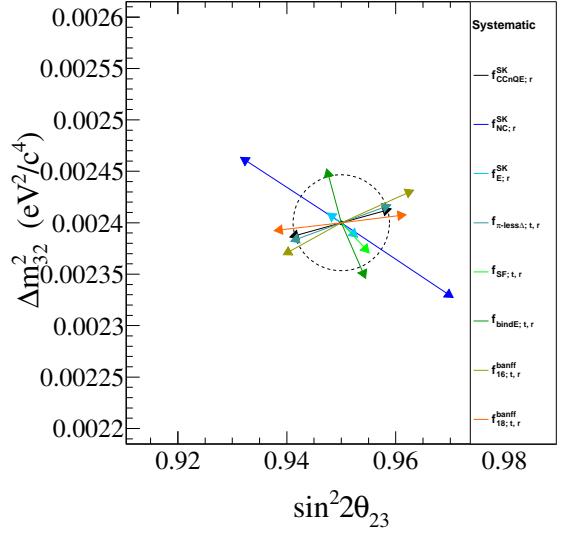


Figure 302: Effect of parameters used in the 2+8 fit on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.95$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

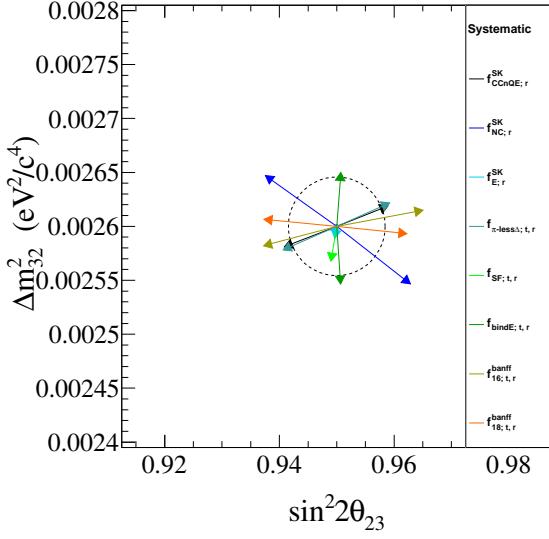


Figure 303: Effect of parameters used in the 2+8 fit on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.95$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0026$.

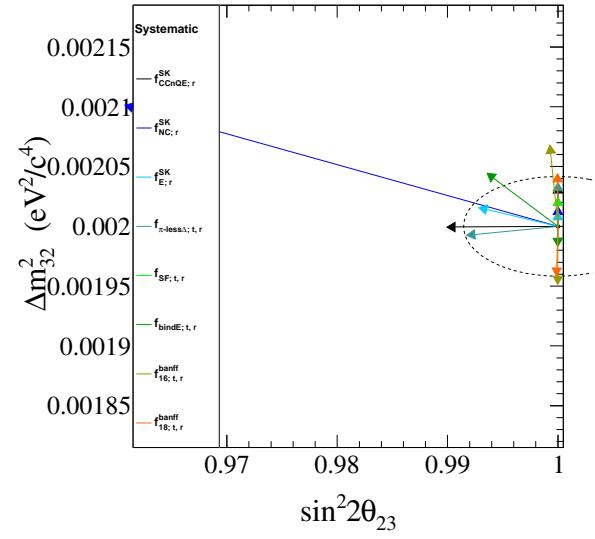


Figure 304: Effect of parameters used in the 2+8 fit on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.002$.

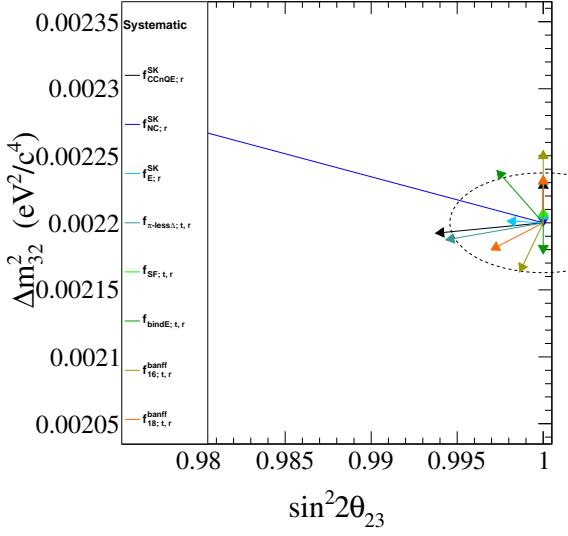


Figure 305: Effect of parameters used in the 2+8 fit on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0022$.

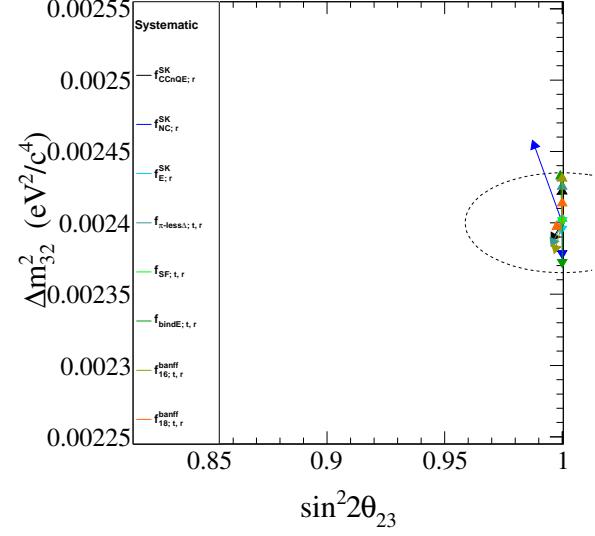


Figure 306: Effect of parameters used in the 2+8 fit on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

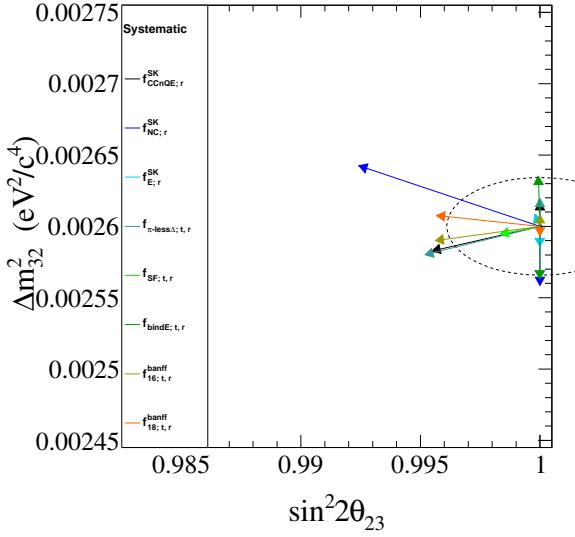


Figure 307: Effect of parameters used in the 2+8 fit on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0026$.

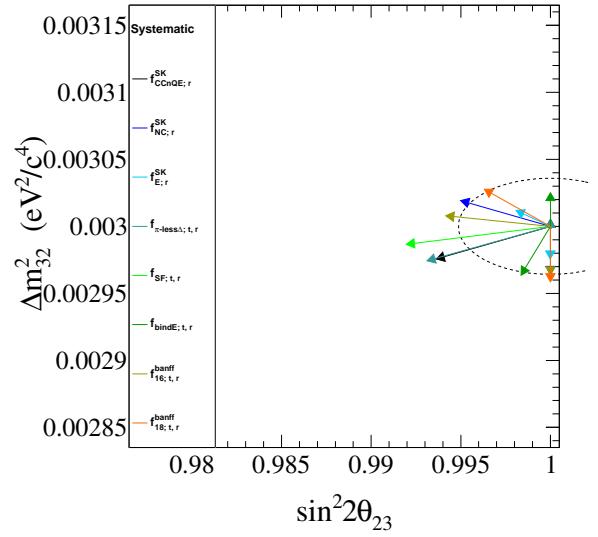


Figure 308: Effect of parameters used in the 2+8 fit on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.003$.

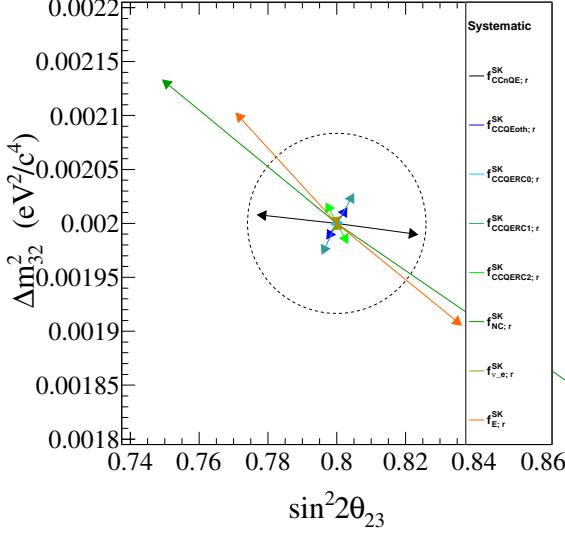


Figure 309: Effect of SuperK detector parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.8$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.002$.

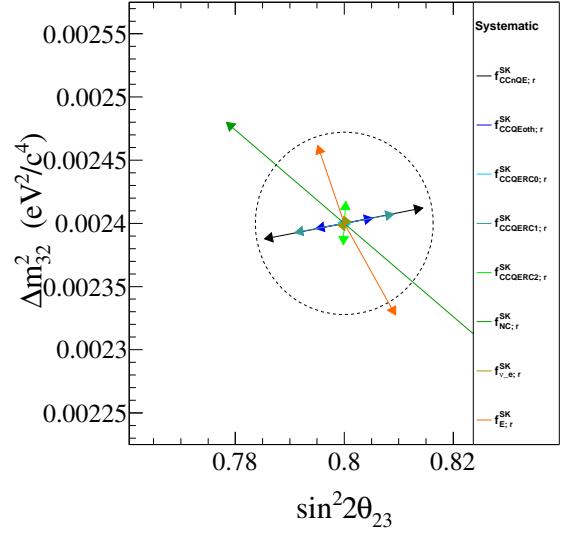


Figure 310: Effect of SuperK detector parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.8$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

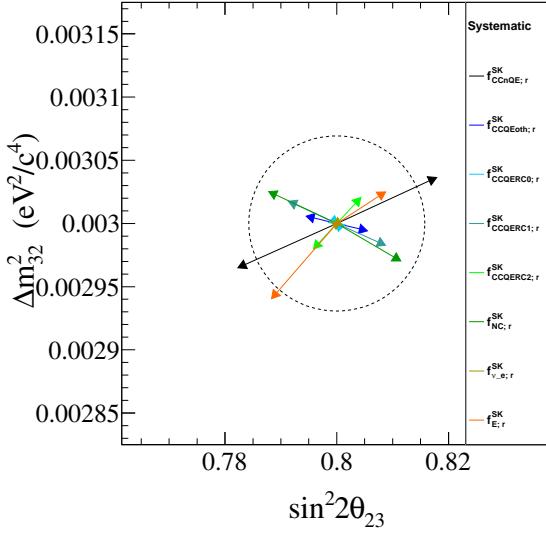


Figure 311: Effect of SuperK detector parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.8$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.003$.

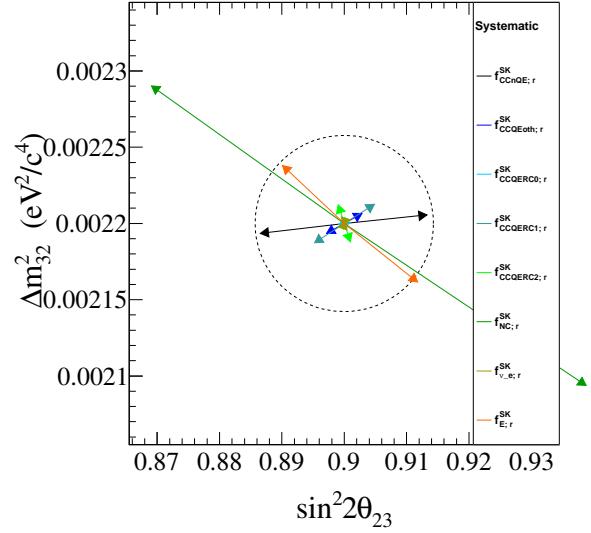


Figure 312: Effect of SuperK detector parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0022$.

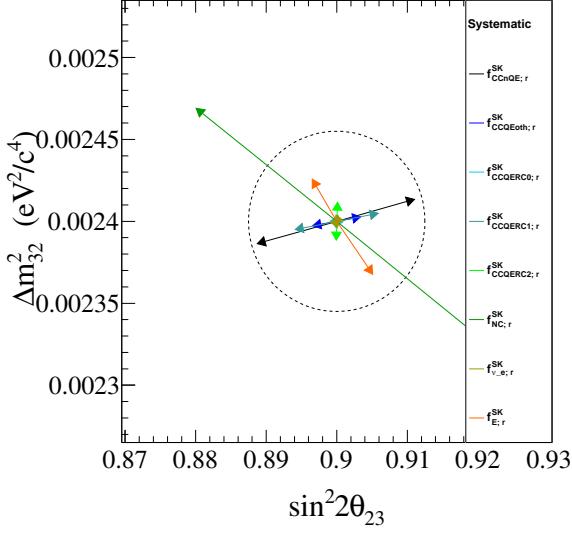


Figure 313: Effect of SuperK detector parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

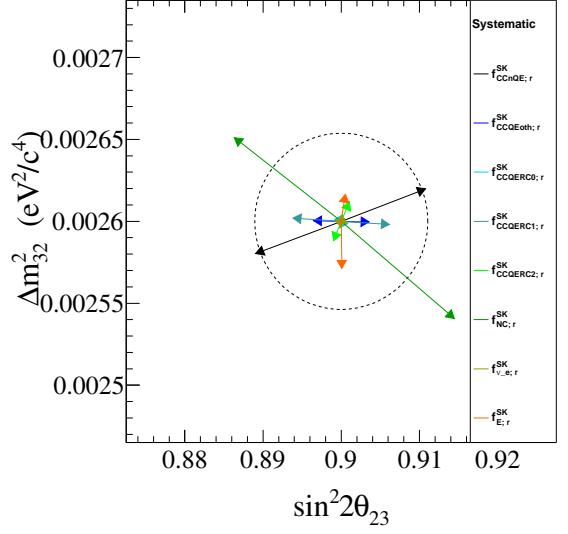


Figure 314: Effect of SuperK detector parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0026$.

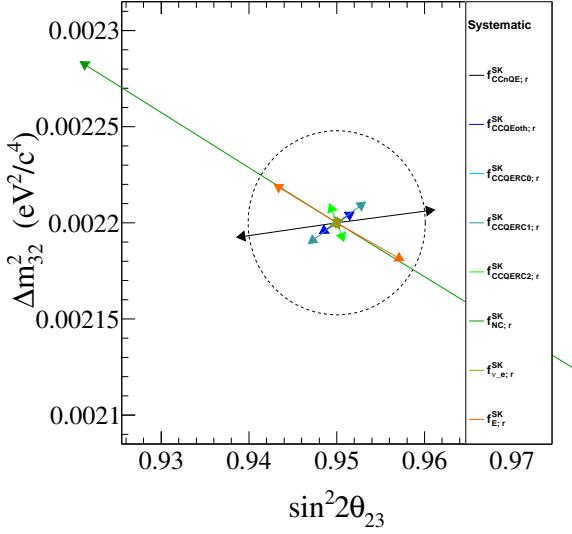


Figure 315: Effect of SuperK detector parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.95$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0022$.

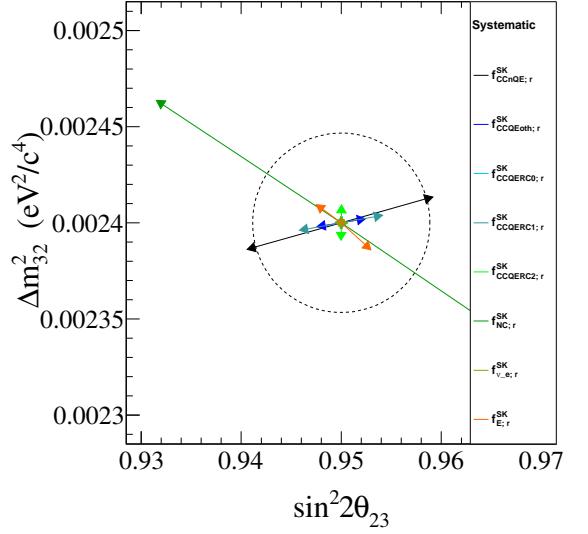


Figure 316: Effect of SuperK detector parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.95$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

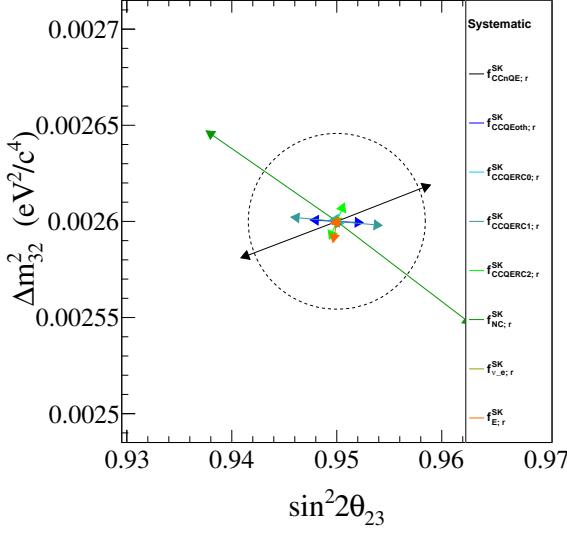


Figure 317: Effect of SuperK detector parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.95$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0026$.

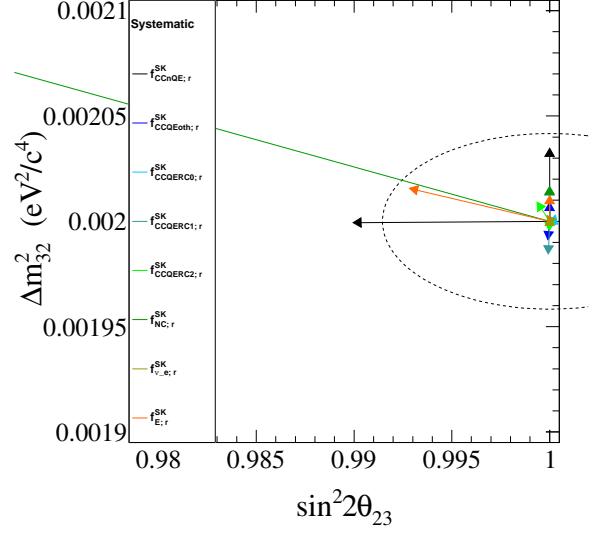


Figure 318: Effect of SuperK detector parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.002$.

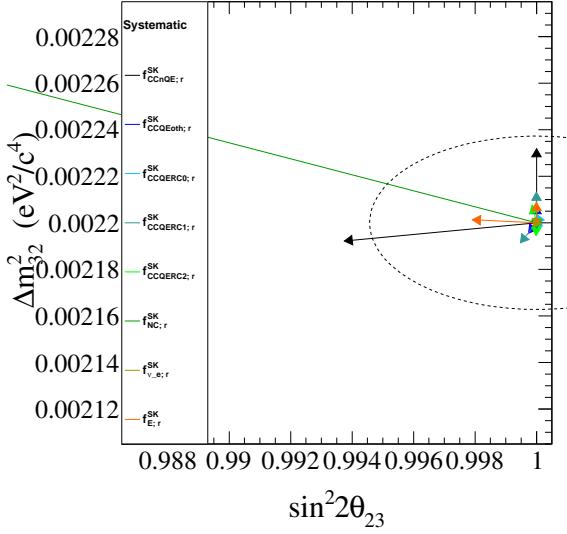


Figure 319: Effect of SuperK detector parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0022$.

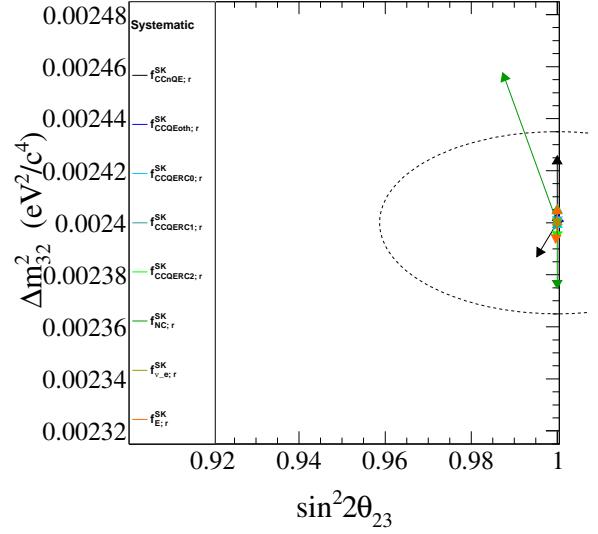


Figure 320: Effect of SuperK detector parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

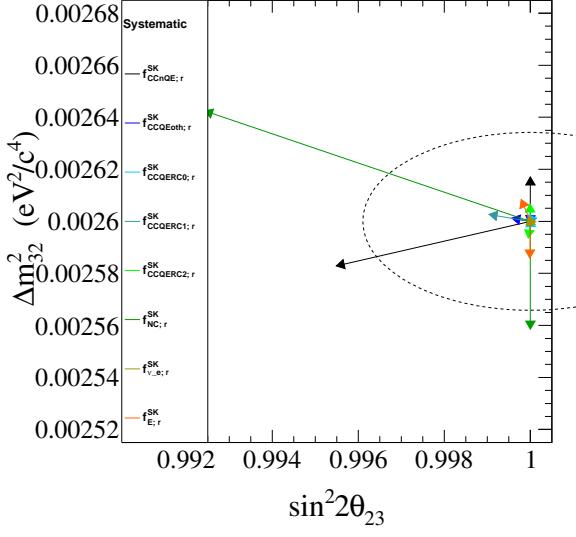


Figure 321: Effect of SuperK detector parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0026$.

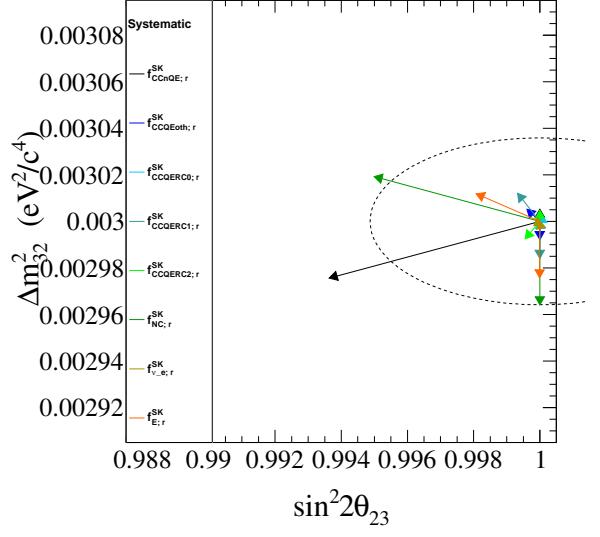


Figure 322: Effect of SuperK detector parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.003$.

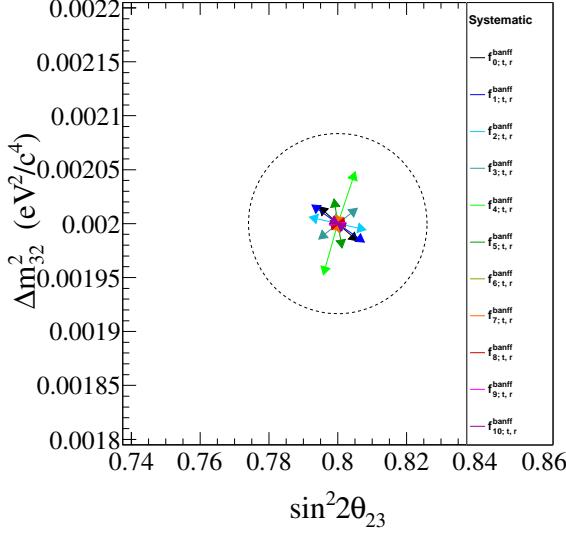


Figure 323: Effect of BANFF ν_μ flux parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.8$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.002$.

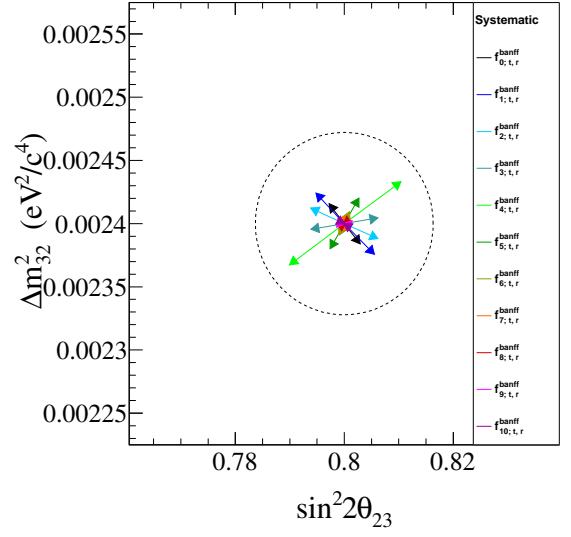


Figure 324: Effect of BANFF ν_μ flux parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.8$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

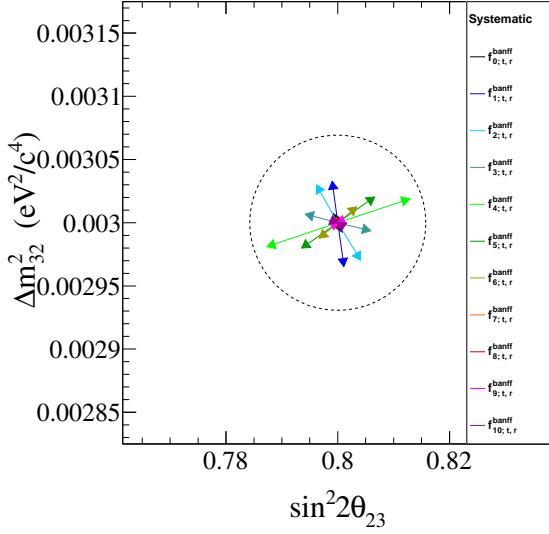


Figure 325: Effect of BANFF ν_μ flux parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.8$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.003$.

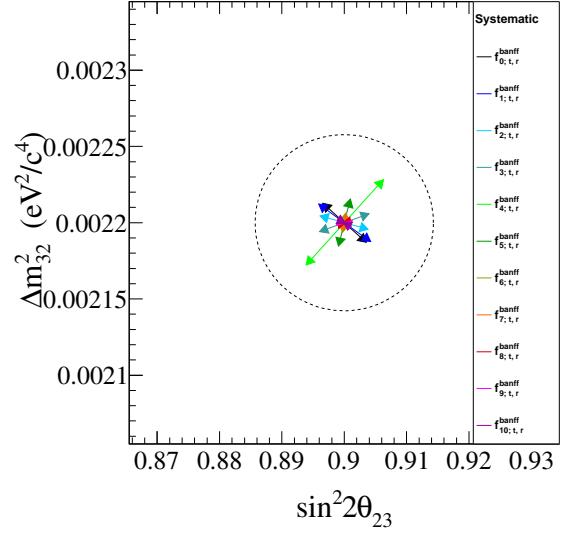


Figure 326: Effect of BANFF ν_μ flux parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0022$.

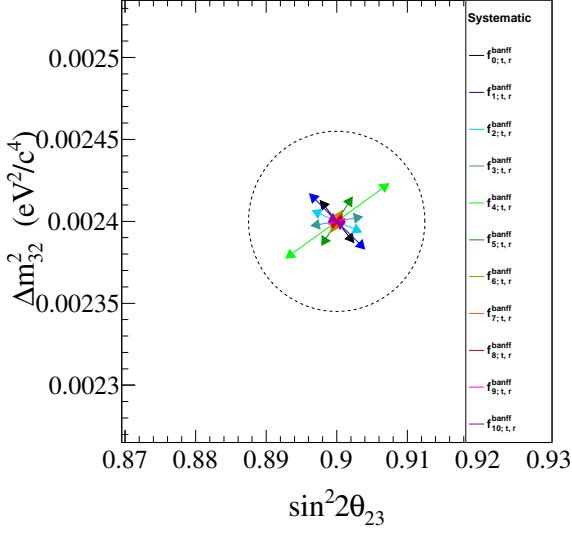


Figure 327: Effect of BANFF ν_μ flux parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

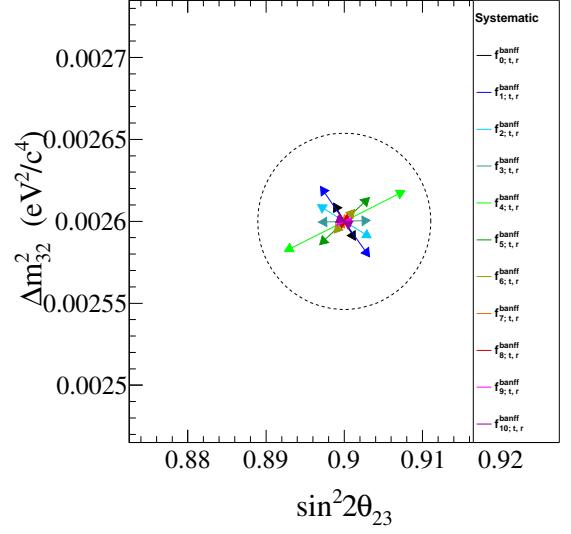


Figure 328: Effect of BANFF ν_μ flux parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0026$.

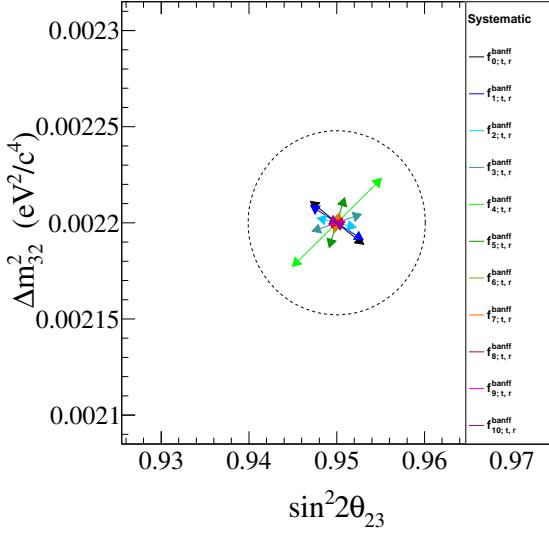


Figure 329: Effect of BANFF ν_μ flux parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.95$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0022$.

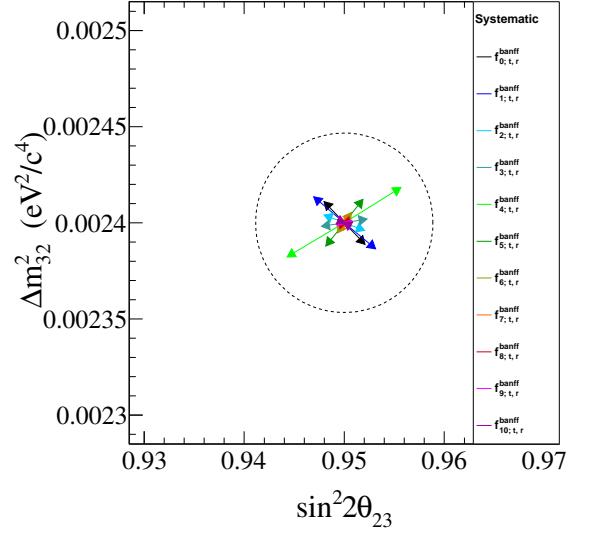


Figure 330: Effect of BANFF ν_μ flux parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.95$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

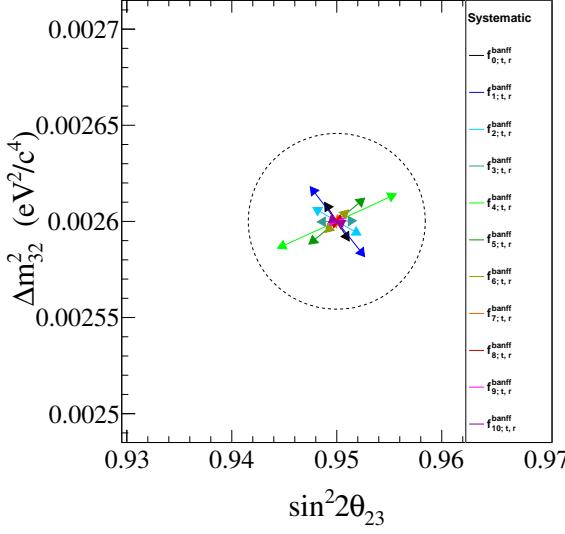


Figure 331: Effect of BANFF ν_μ flux parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.95$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0026$.

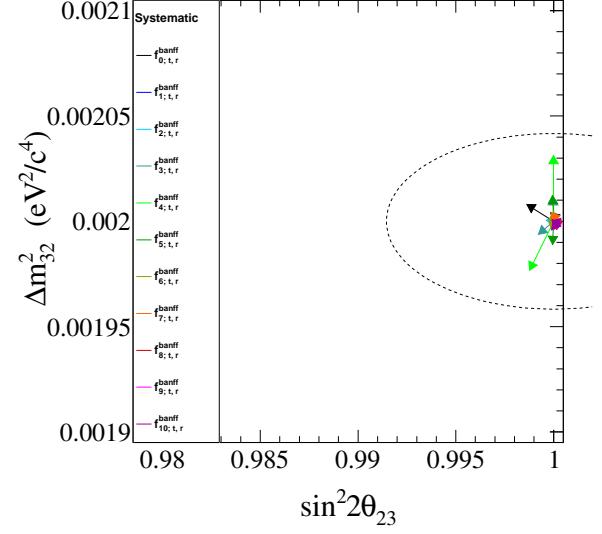


Figure 332: Effect of BANFF ν_μ flux parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.002$.

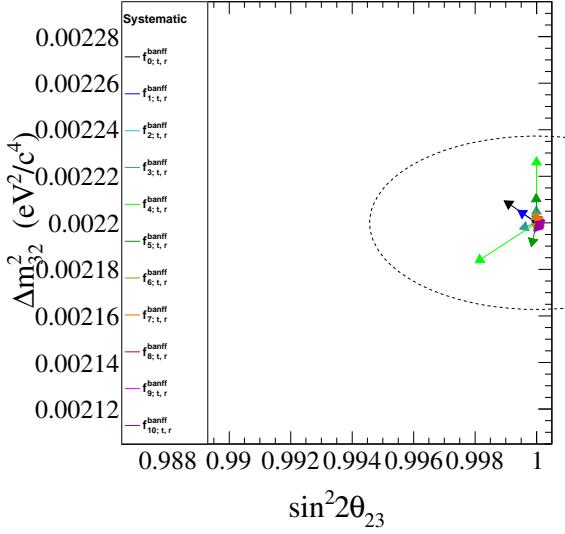


Figure 333: Effect of BANFF ν_μ flux parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0022$.

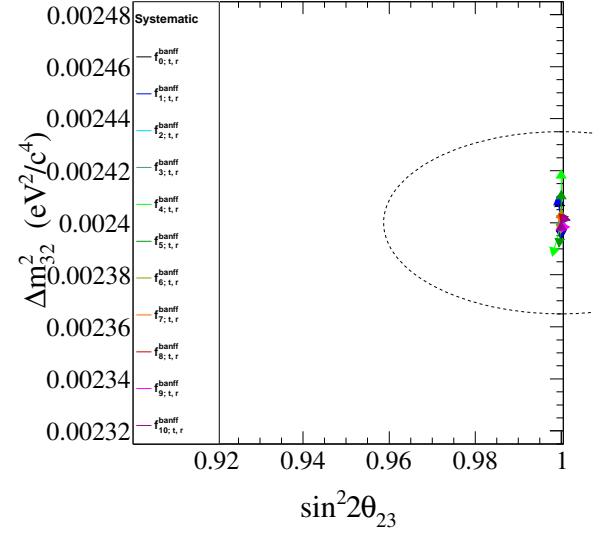


Figure 334: Effect of BANFF ν_μ flux parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

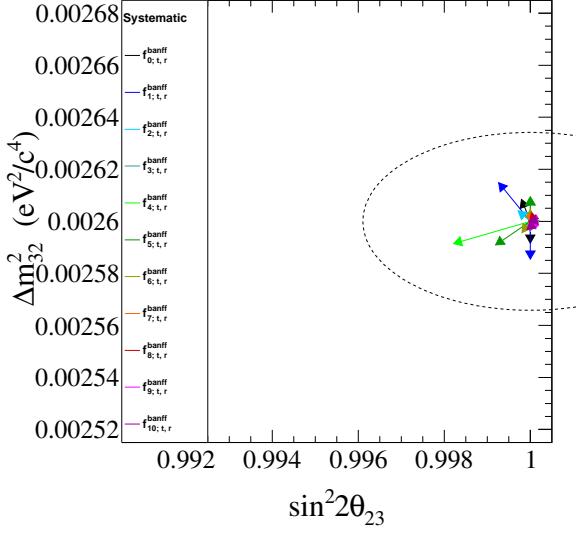


Figure 335: Effect of BANFF ν_μ flux parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0026$.

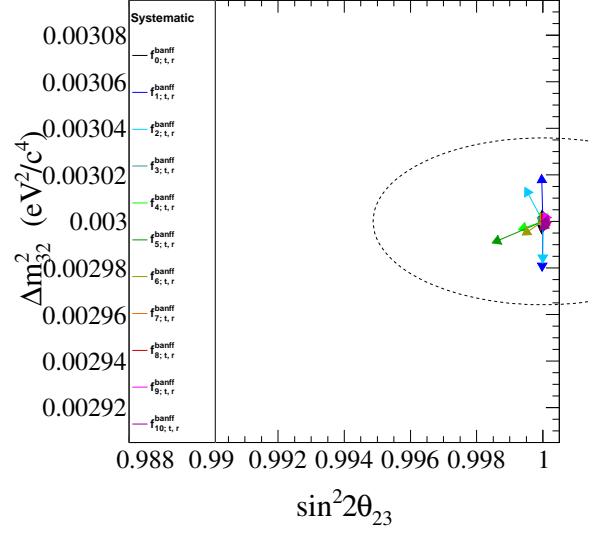


Figure 336: Effect of BANFF ν_μ flux parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.003$.

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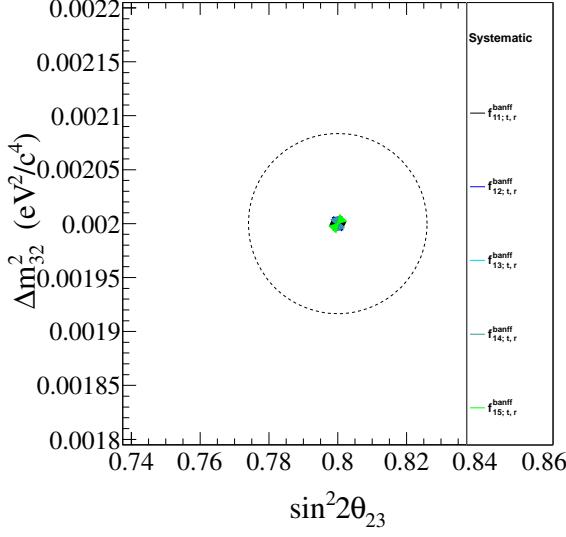


Figure 337: Effect of BANFF $\bar{\nu}_\mu$ flux parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.8$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5e-05$; $\Delta m_{32}^2 = 0.002$.

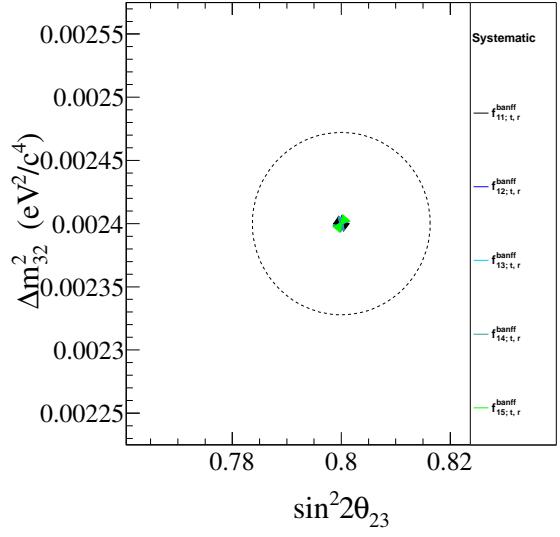


Figure 338: Effect of BANFF $\bar{\nu}_\mu$ flux parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.8$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5e-05$; $\Delta m_{32}^2 = 0.0024$.

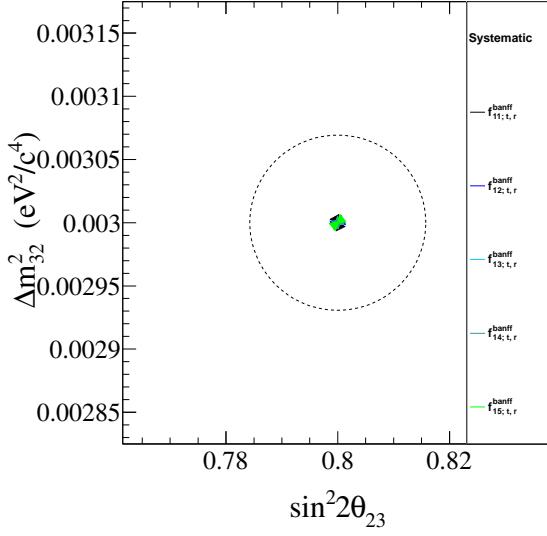


Figure 339: Effect of BANFF $\bar{\nu}_\mu$ flux parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.8$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5e-05$; $\Delta m_{32}^2 = 0.003$.

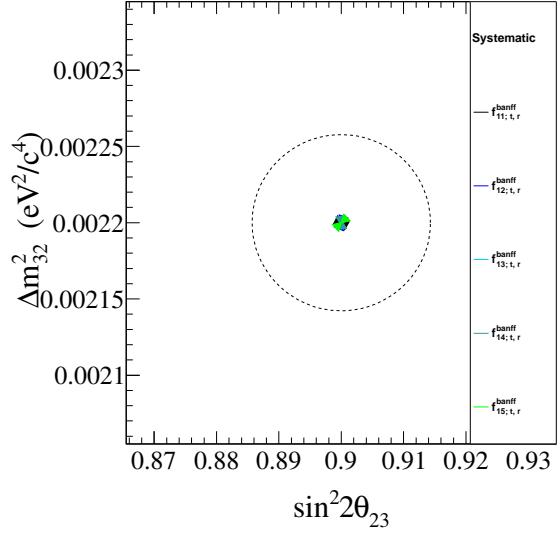


Figure 340: Effect of BANFF $\bar{\nu}_\mu$ flux parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5e-05$; $\Delta m_{32}^2 = 0.0022$.

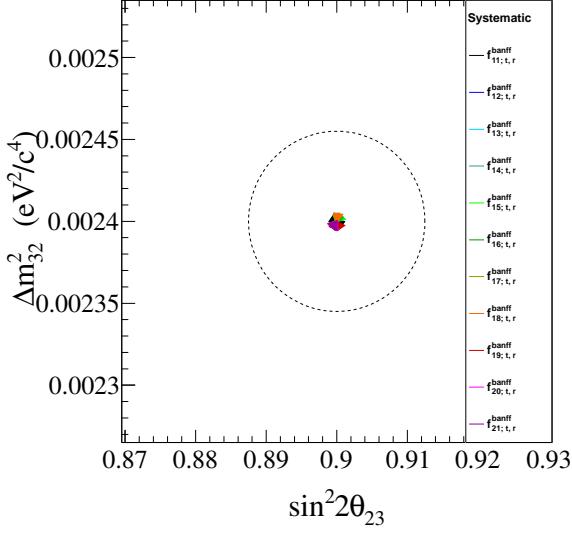


Figure 341: Effect of BANFF $\bar{\nu}_\mu$ flux parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

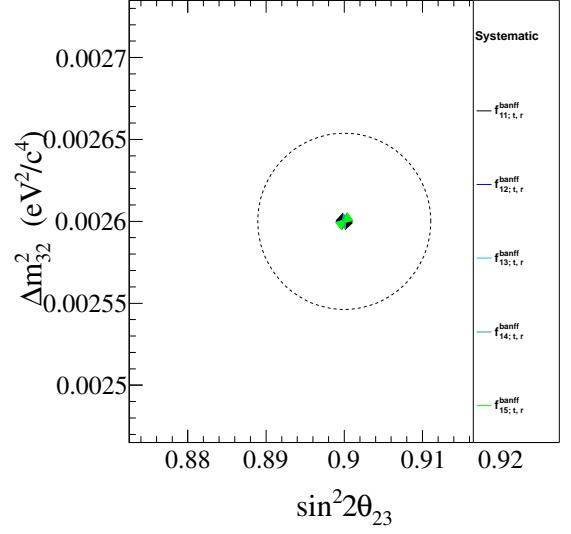


Figure 342: Effect of BANFF $\bar{\nu}_\mu$ flux parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0026$.

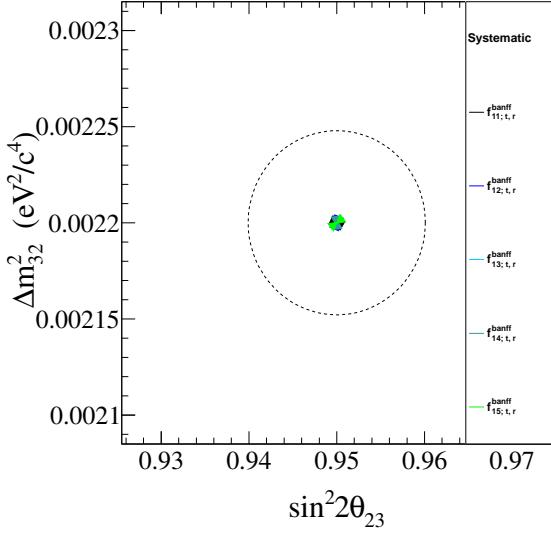


Figure 343: Effect of BANFF $\bar{\nu}_\mu$ flux parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.95$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0022$.

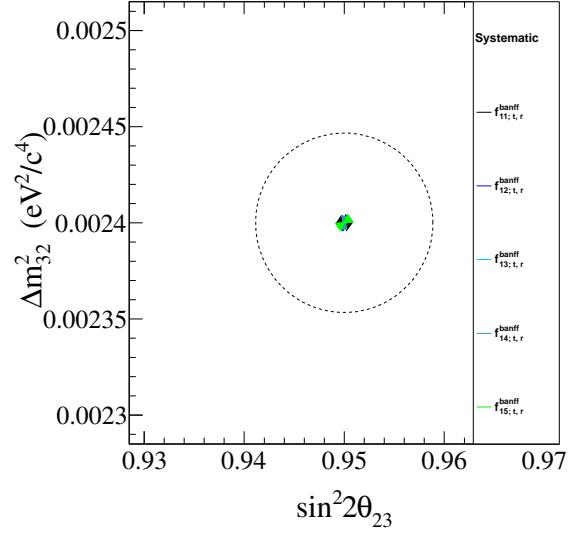


Figure 344: Effect of BANFF $\bar{\nu}_\mu$ flux parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.95$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

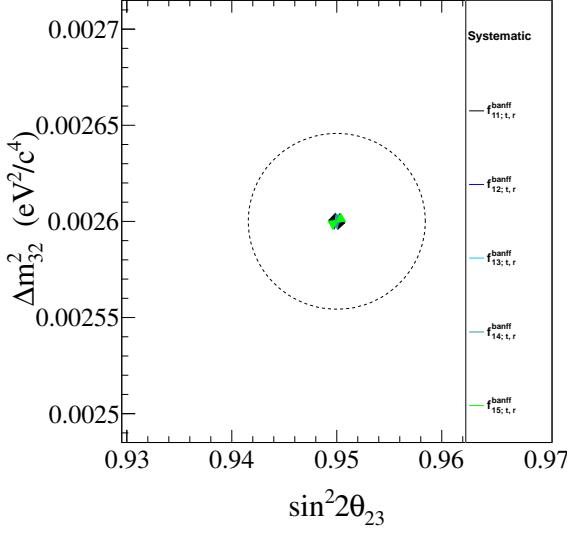


Figure 345: Effect of BANFF $\bar{\nu}_\mu$ flux parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.95$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0026$.

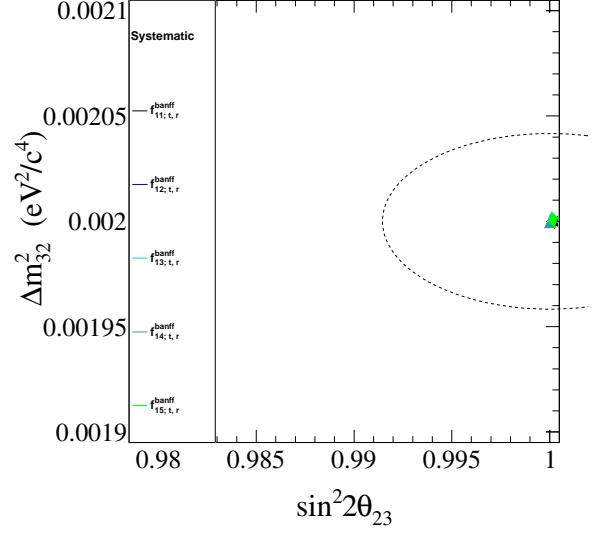


Figure 346: Effect of BANFF $\bar{\nu}_\mu$ flux parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.002$.

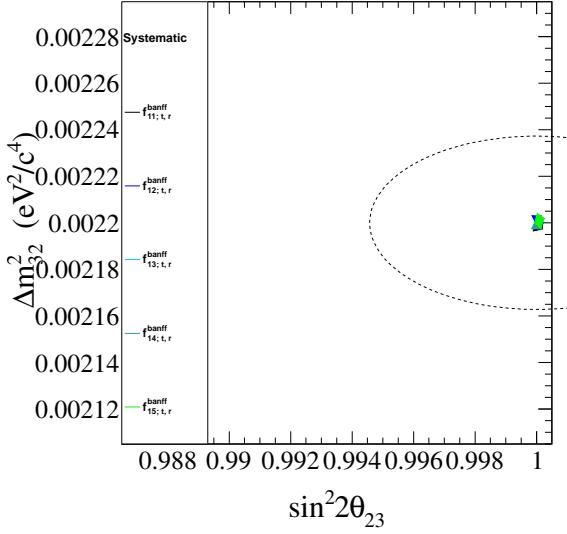


Figure 347: Effect of BANFF $\bar{\nu}_\mu$ flux parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0022$.

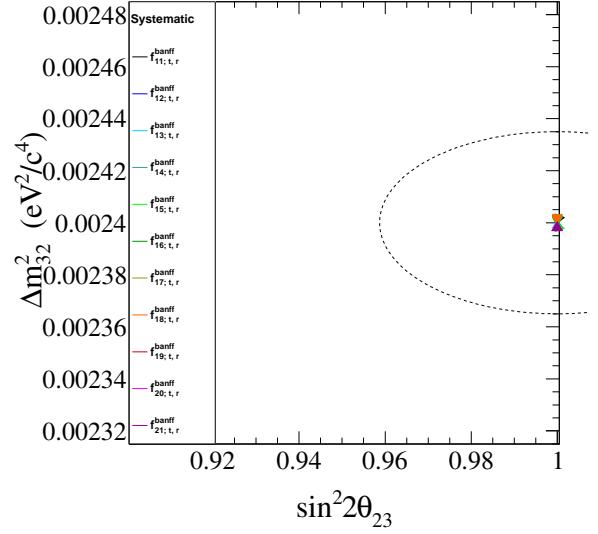


Figure 348: Effect of BANFF $\bar{\nu}_\mu$ flux parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

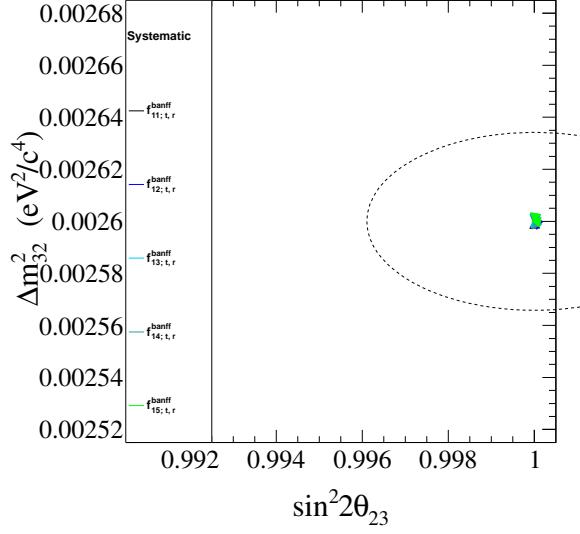


Figure 349: Effect of BANFF $\bar{\nu}_\mu$ flux parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0026$.

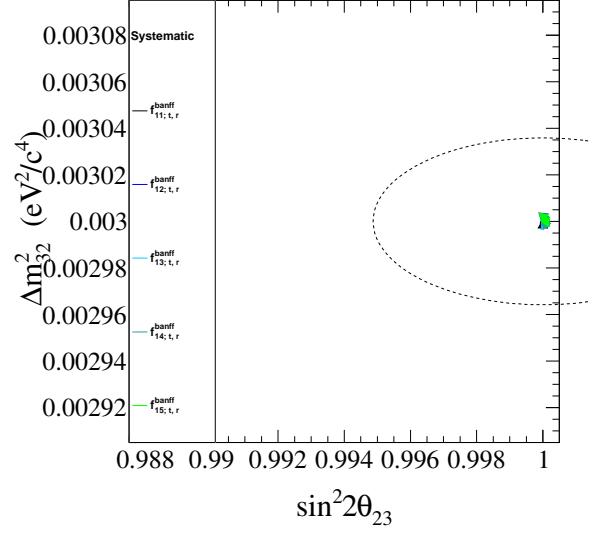


Figure 350: Effect of BANFF $\bar{\nu}_\mu$ flux parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.003$.

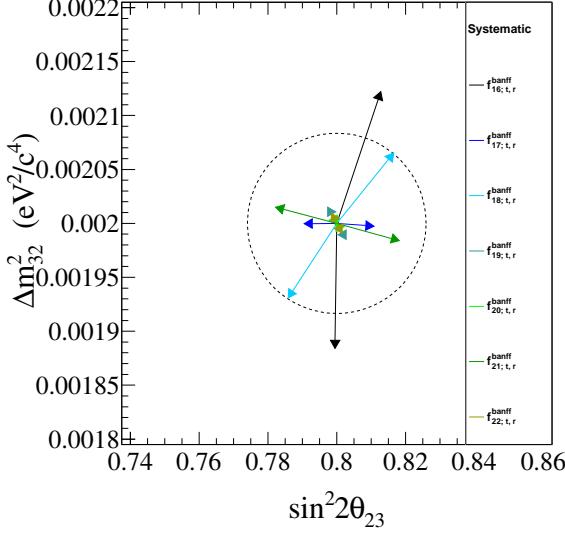


Figure 351: Effect of BANFF cross section parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.8$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5e-05$; $\Delta m_{32}^2 = 0.002$.

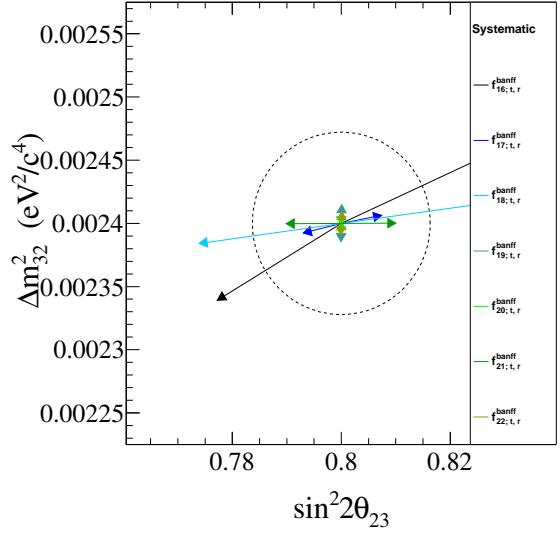


Figure 352: Effect of BANFF cross section parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.8$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5e-05$; $\Delta m_{32}^2 = 0.0024$.

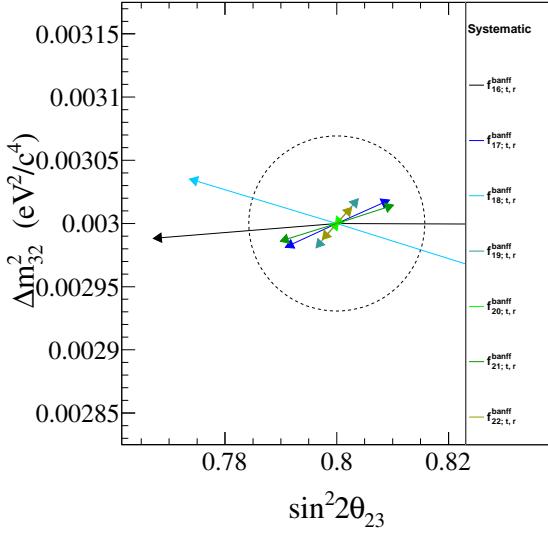


Figure 353: Effect of BANFF cross section parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.8$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5e-05$; $\Delta m_{32}^2 = 0.003$.

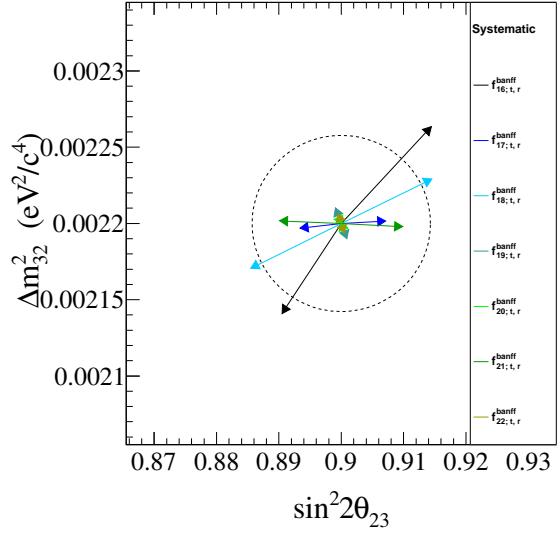


Figure 354: Effect of BANFF cross section parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5e-05$; $\Delta m_{32}^2 = 0.0022$.

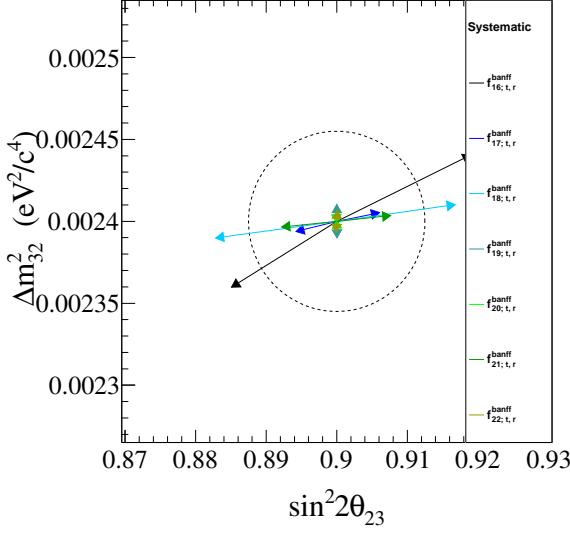


Figure 355: Effect of BANFF cross section parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

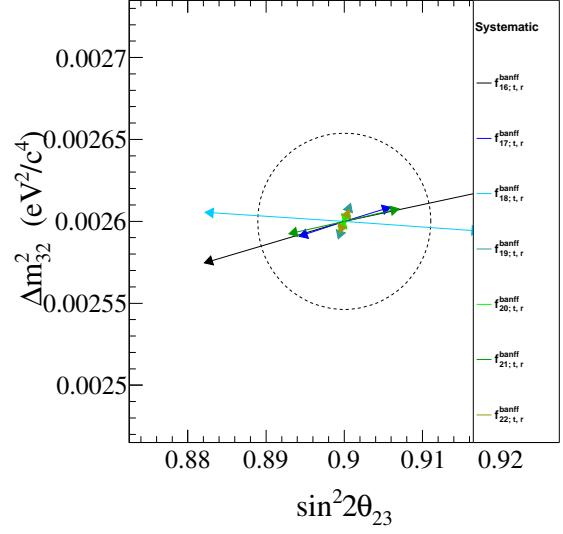


Figure 356: Effect of BANFF cross section parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0026$.

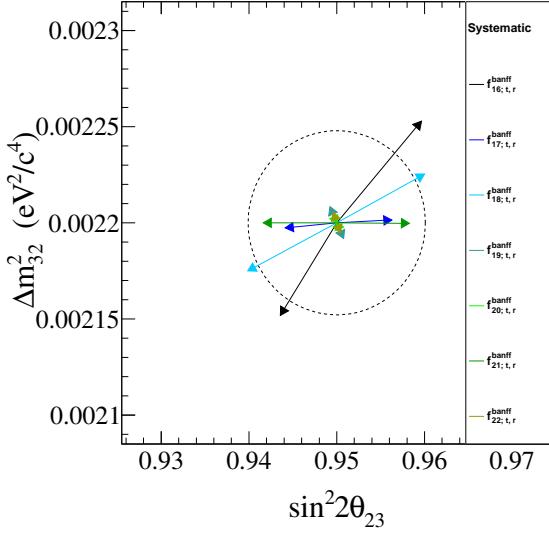


Figure 357: Effect of BANFF cross section parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.95$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0022$.

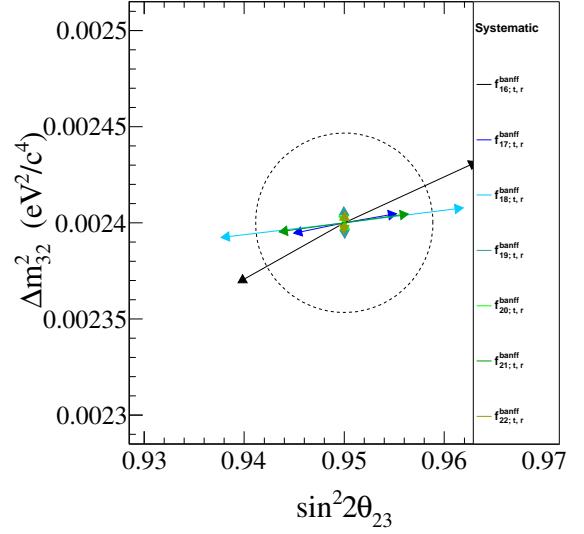


Figure 358: Effect of BANFF cross section parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.95$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

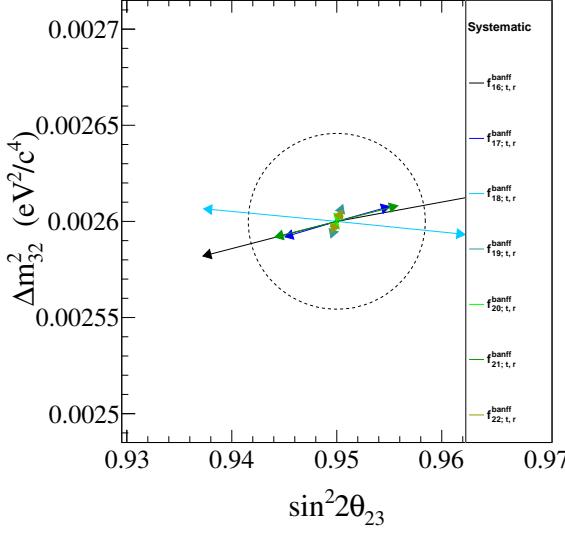


Figure 359: Effect of BANFF cross section parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.95$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0026$.

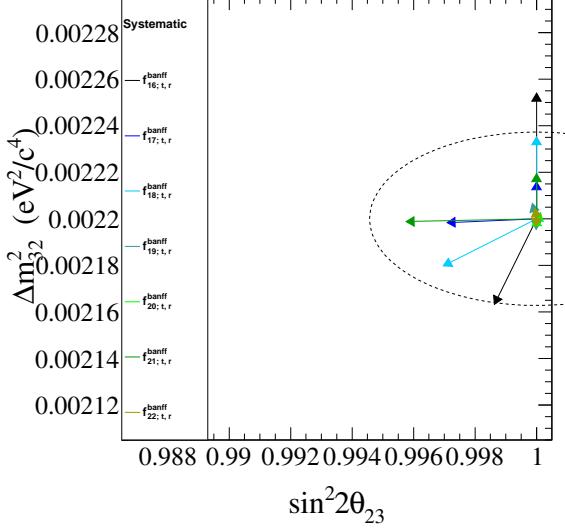


Figure 361: Effect of BANFF cross section parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0022$.

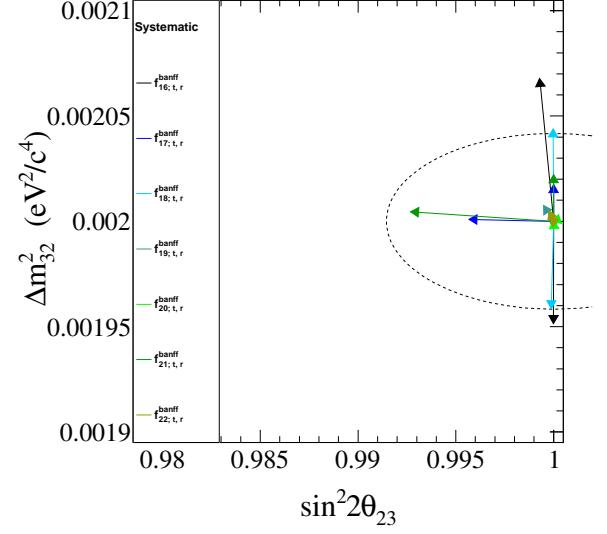


Figure 360: Effect of BANFF cross section parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.002$.

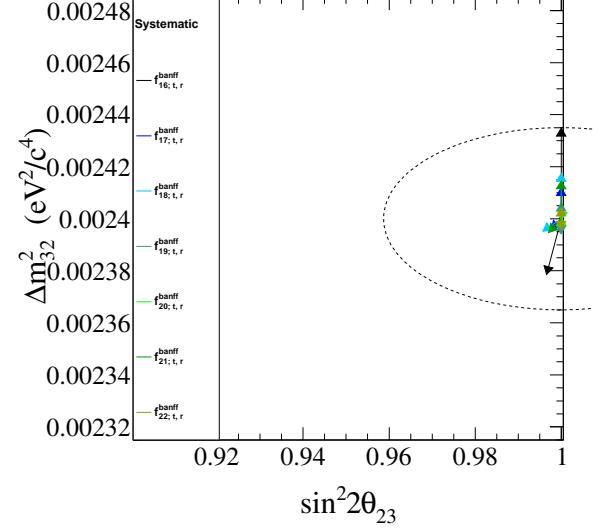


Figure 362: Effect of BANFF cross section parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

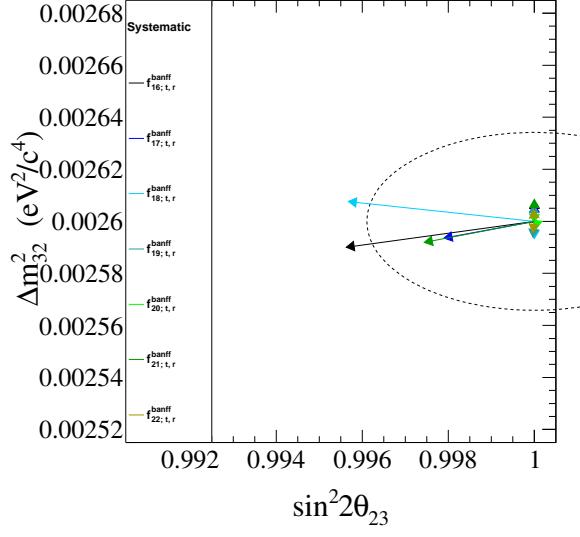


Figure 363: Effect of BANFF cross section parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0026$.

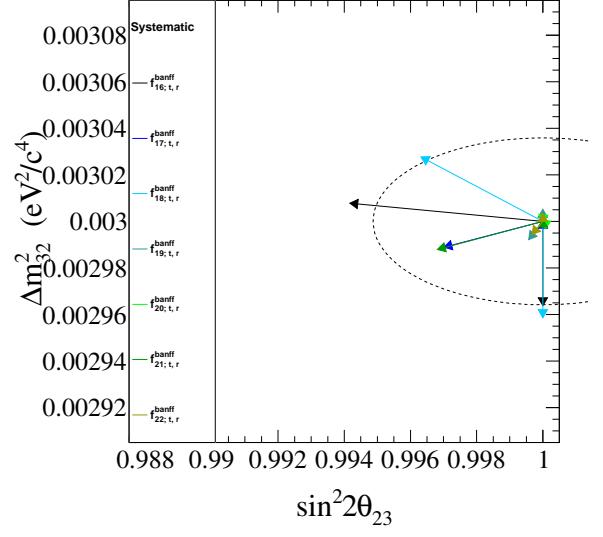


Figure 364: Effect of BANFF cross section parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.003$.

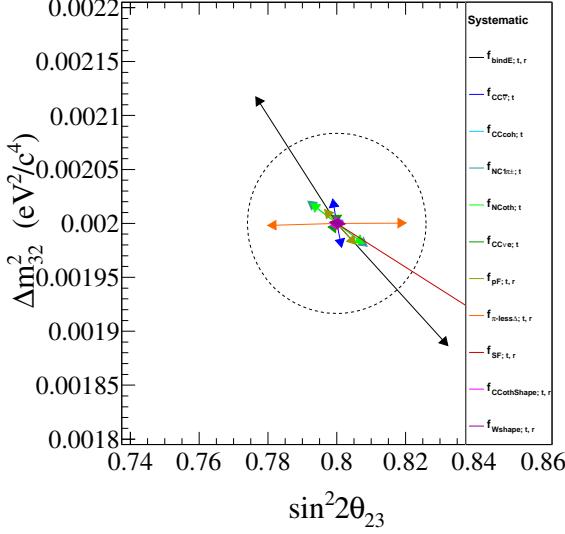


Figure 365: Effect of uncorrelated cross section parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.8$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{-}05$; $\Delta m_{32}^2 = 0.002$.

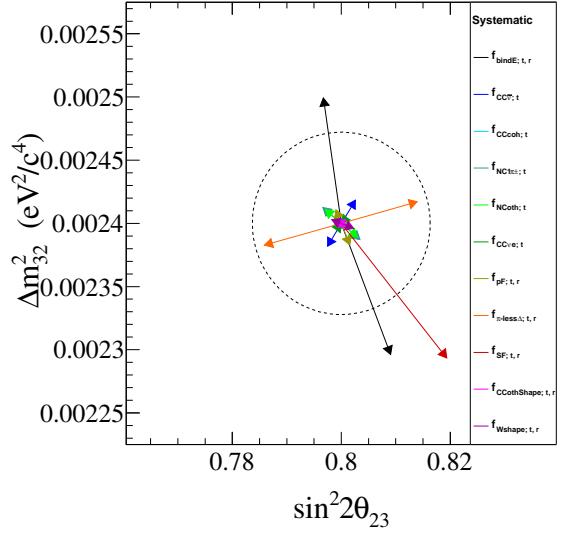


Figure 366: Effect of uncorrelated cross section parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.8$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{-}05$; $\Delta m_{32}^2 = 0.0024$.

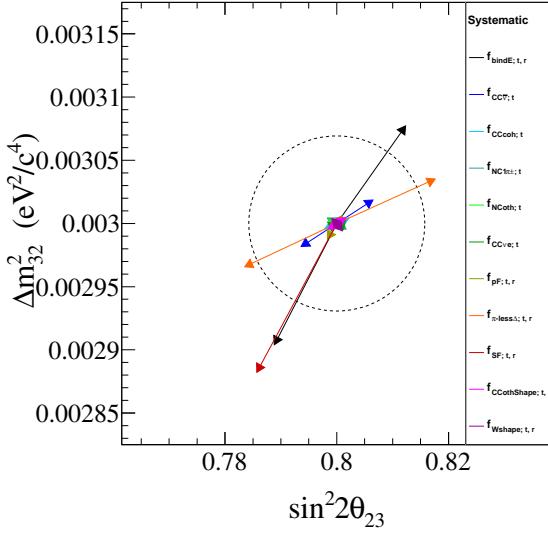


Figure 367: Effect of uncorrelated cross section parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.8$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{-}05$; $\Delta m_{32}^2 = 0.003$.

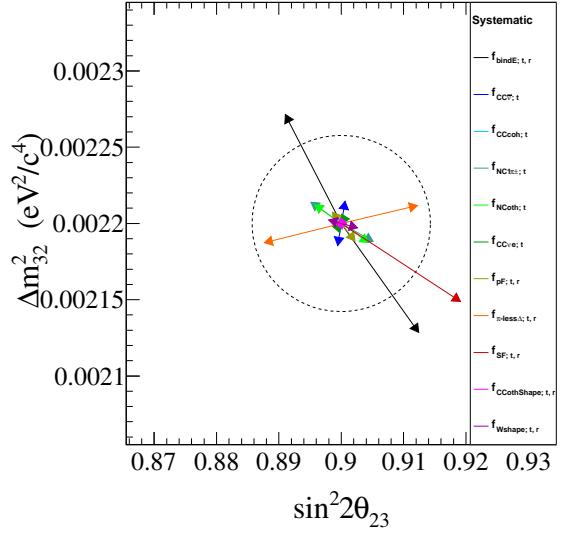


Figure 368: Effect of uncorrelated cross section parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{-}05$; $\Delta m_{32}^2 = 0.0022$.

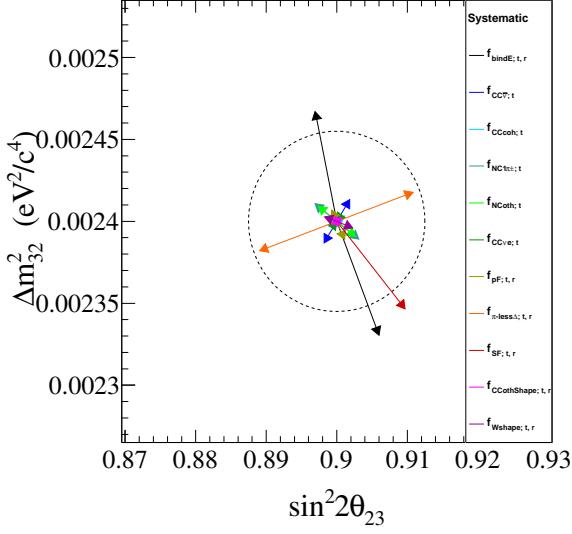


Figure 369: Effect of uncorrelated cross section parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

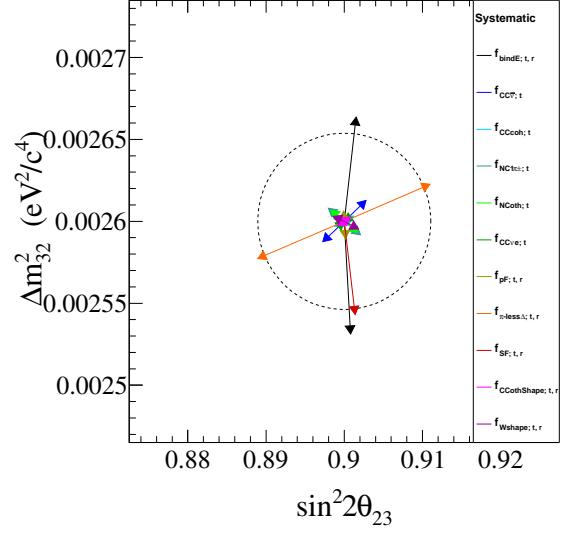


Figure 370: Effect of uncorrelated cross section parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0026$.

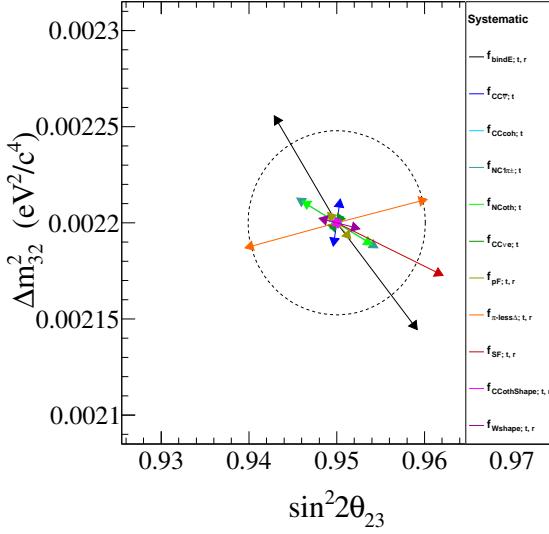


Figure 371: Effect of uncorrelated cross section parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.95$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0022$.

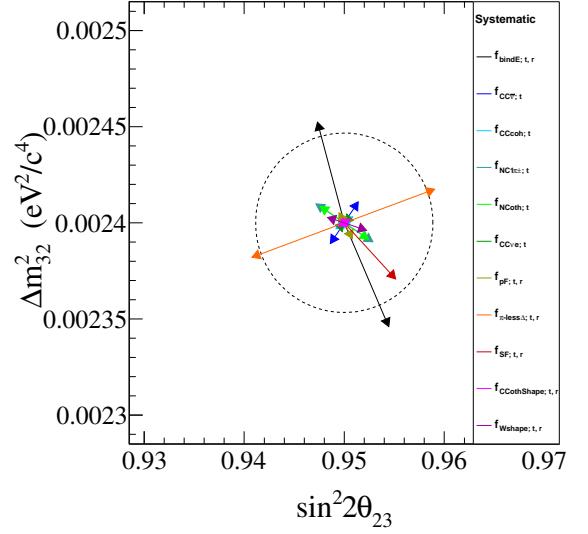


Figure 372: Effect of uncorrelated cross section parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.95$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

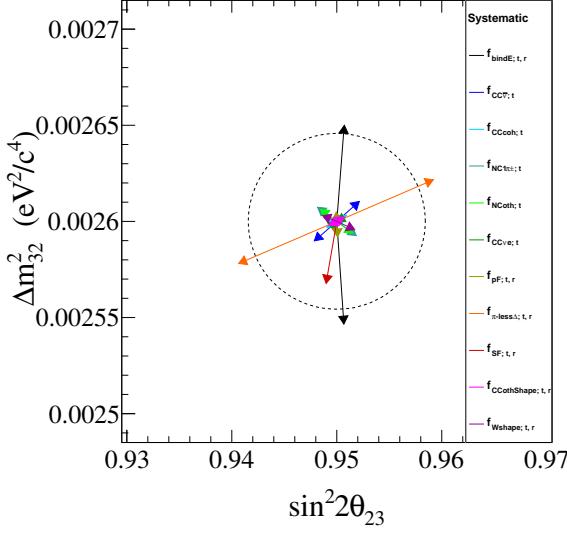


Figure 373: Effect of uncorrelated cross section parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.95$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0026$.

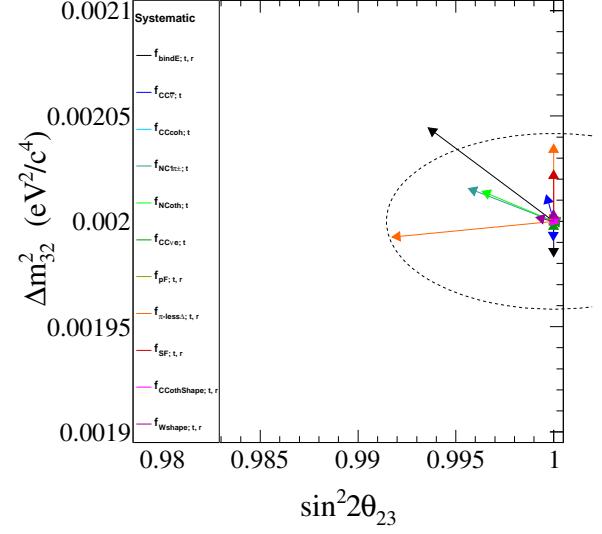


Figure 374: Effect of uncorrelated cross section parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.002$.

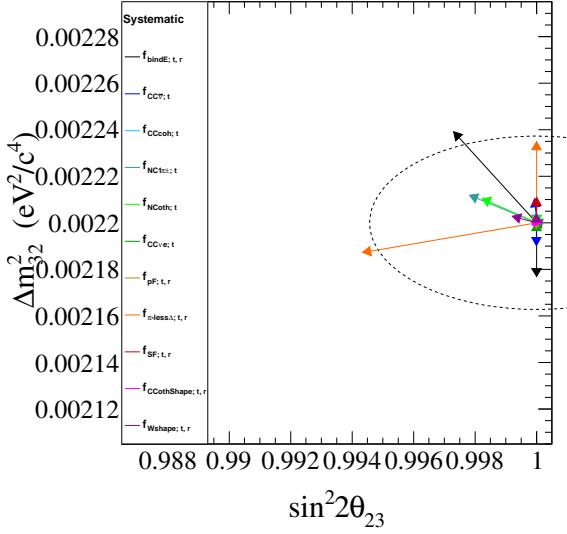


Figure 375: Effect of uncorrelated cross section parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0022$.

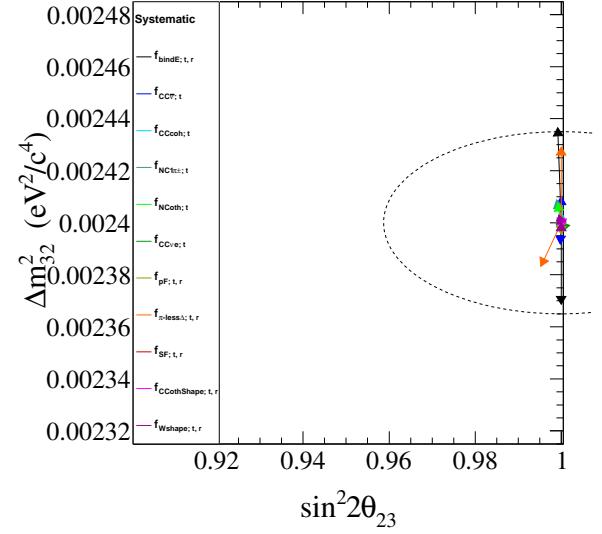


Figure 376: Effect of uncorrelated cross section parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

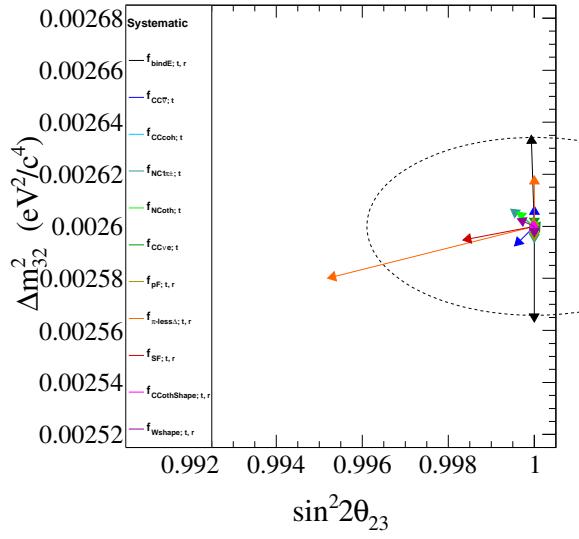


Figure 377: Effect of uncorrelated cross section parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0026$.

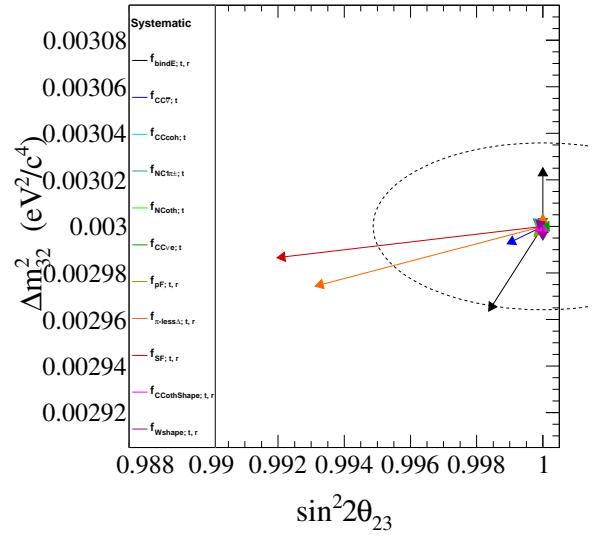


Figure 378: Effect of uncorrelated cross section parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.003$.

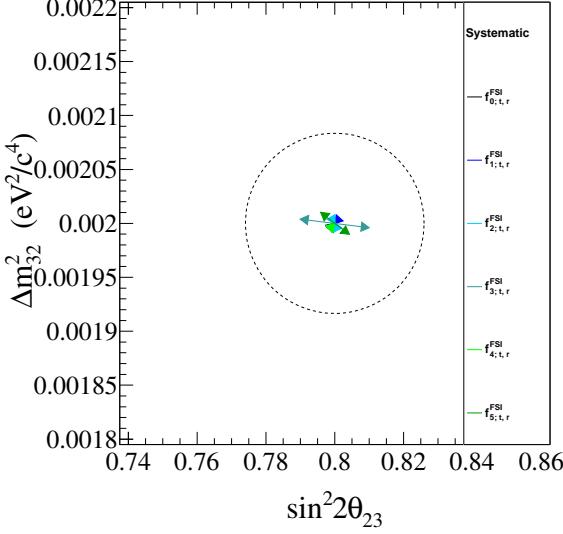


Figure 379: Effect of FSI+SI parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.8$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.002$.

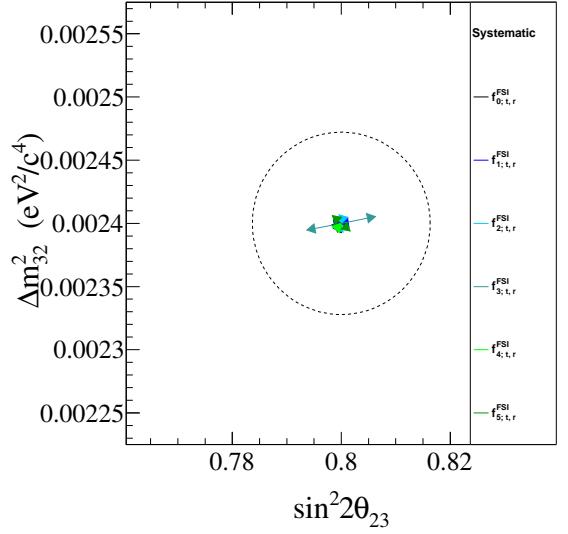


Figure 380: Effect of FSI+SI parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.8$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

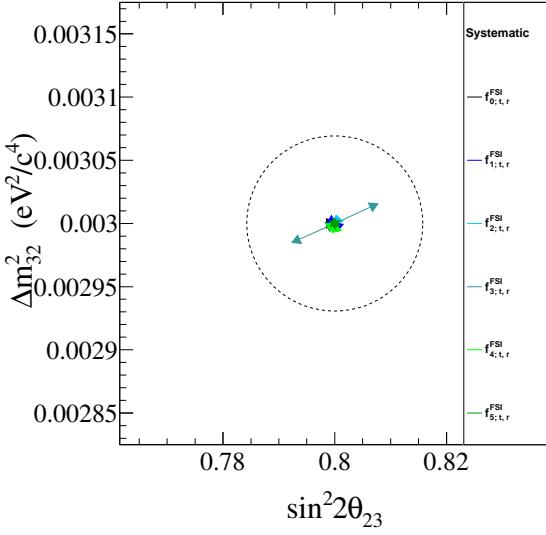


Figure 381: Effect of FSI+SI parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.8$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.003$.

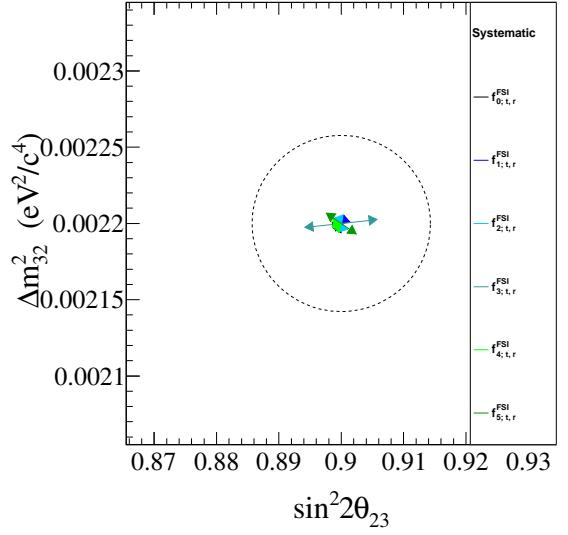


Figure 382: Effect of FSI+SI parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0022$.

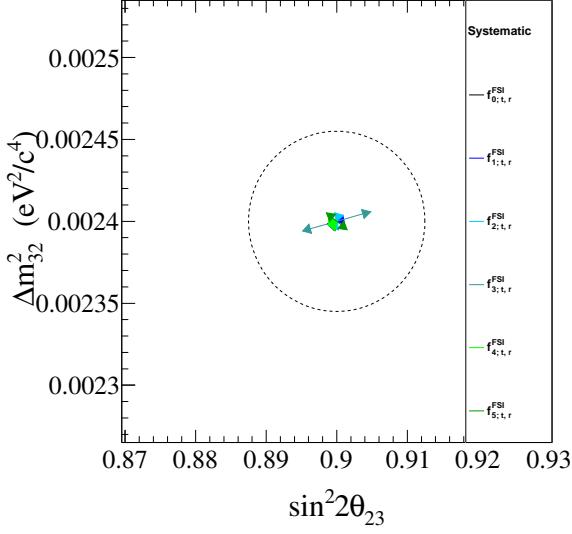


Figure 383: Effect of FSI+SI parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

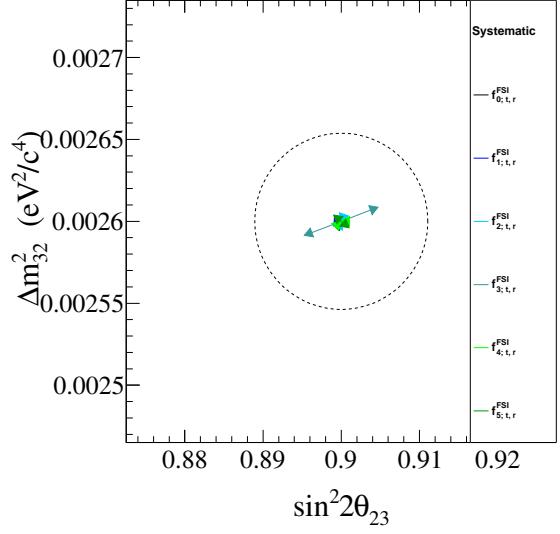


Figure 384: Effect of FSI+SI parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0026$.

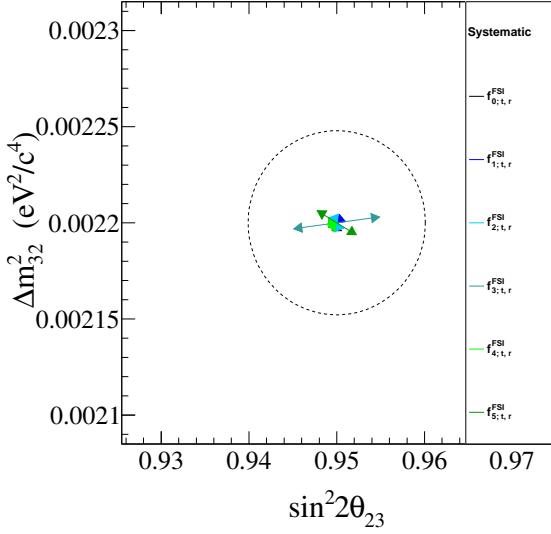


Figure 385: Effect of FSI+SI parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.95$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0022$.

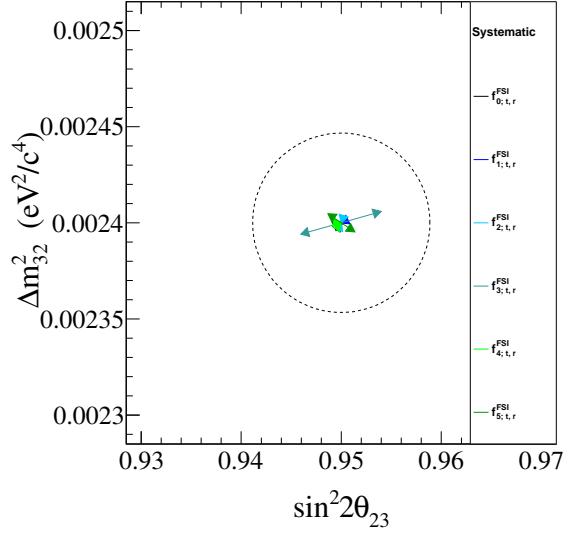


Figure 386: Effect of FSI+SI parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.95$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

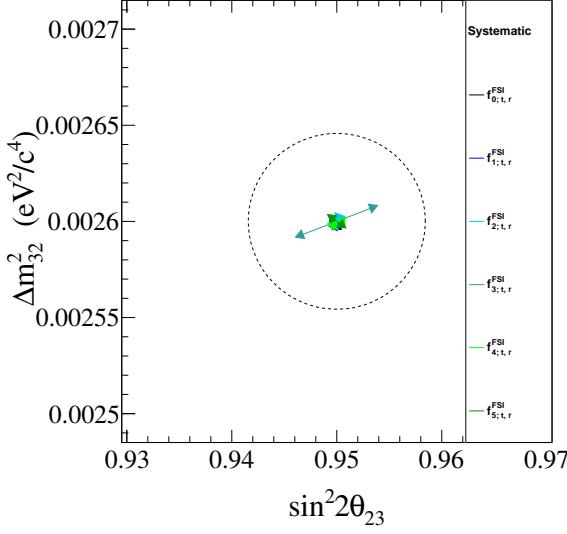


Figure 387: Effect of FSI+SI parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.95$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0026$.

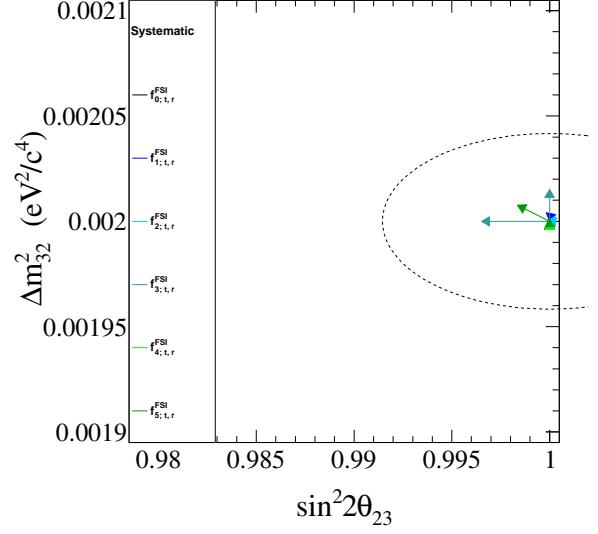


Figure 388: Effect of FSI+SI parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.002$.

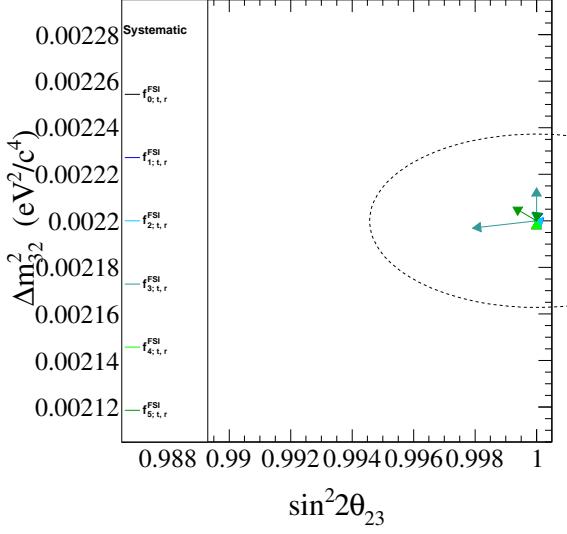


Figure 389: Effect of FSI+SI parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0022$.

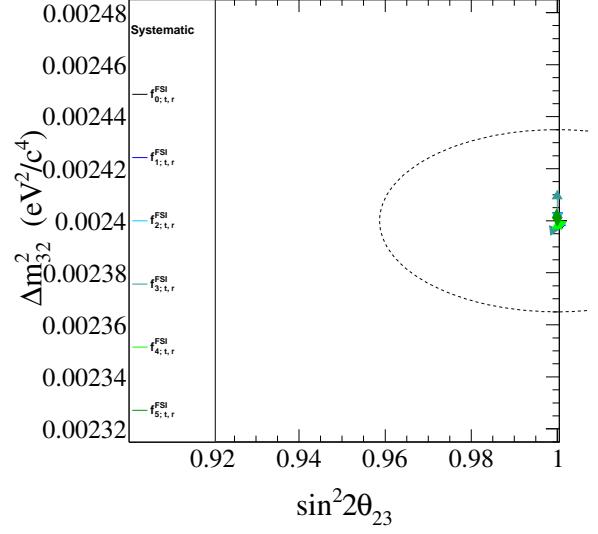


Figure 390: Effect of FSI+SI parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0024$.

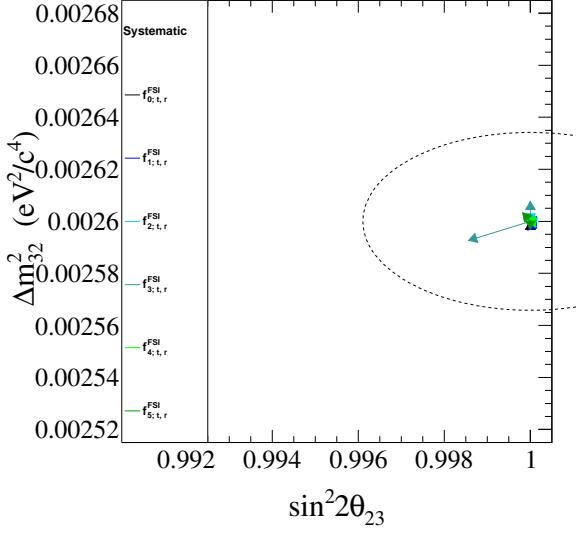


Figure 391: Effect of FSI+SI parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0026$.

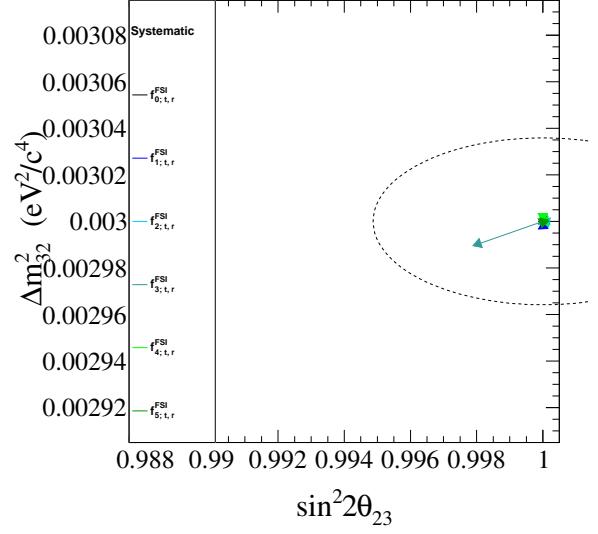


Figure 392: Effect of FSI+SI parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.003$.

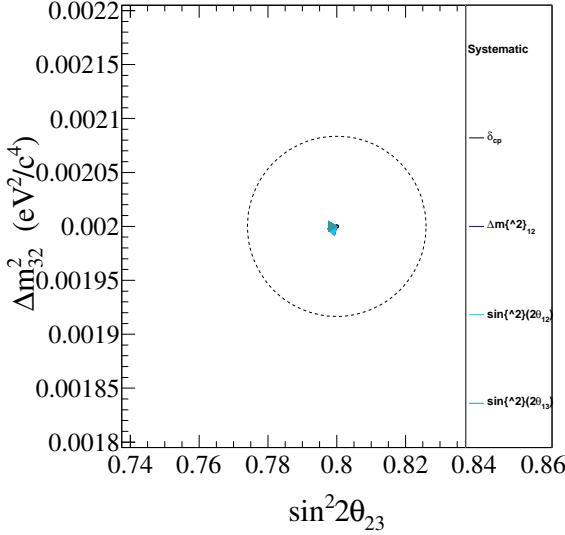


Figure 393: Effect of non-23 sector oscillation parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.8$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{-}05$; $\Delta m_{32}^2 = 0.002$.

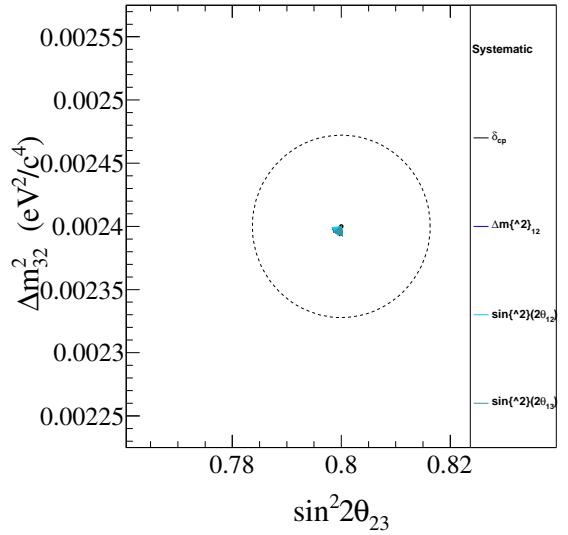


Figure 394: Effect of non-23 sector oscillation parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.8$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{-}05$; $\Delta m_{32}^2 = 0.0024$.

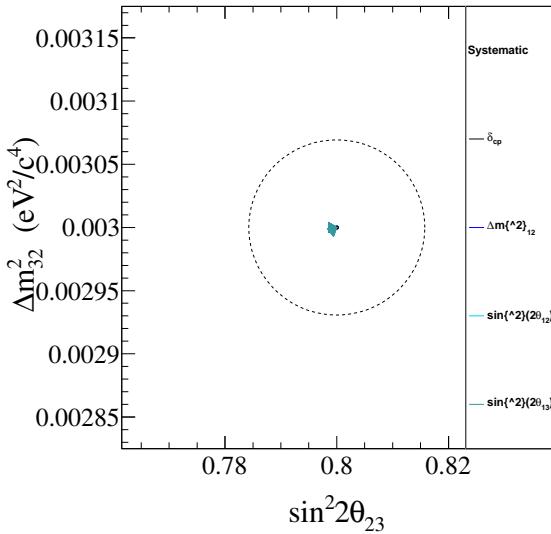


Figure 395: Effect of non-23 sector oscillation parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.8$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{-}05$; $\Delta m_{32}^2 = 0.003$.

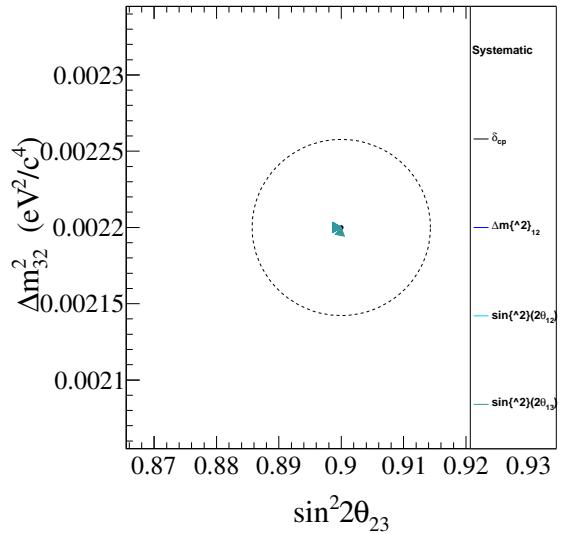


Figure 396: Effect of non-23 sector oscillation parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{-}05$; $\Delta m_{32}^2 = 0.0022$.

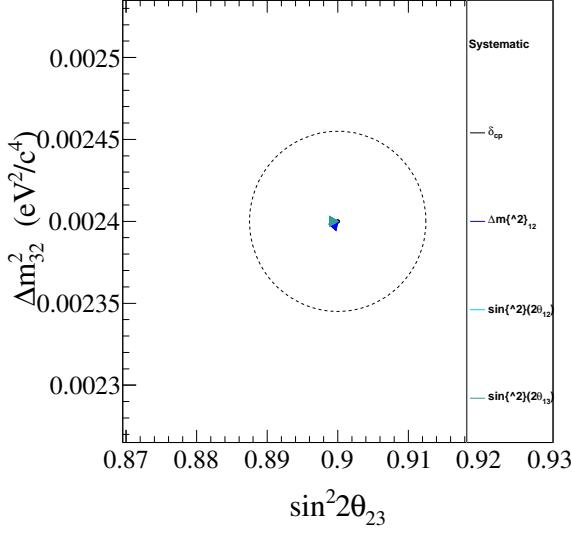


Figure 397: Effect of non-23 sector oscillation parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

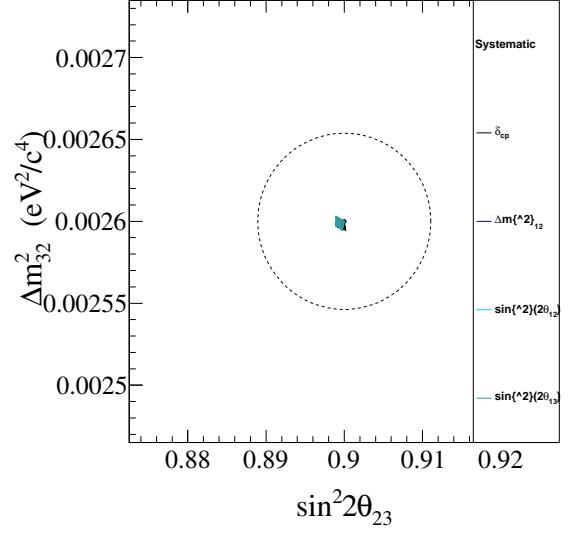


Figure 398: Effect of non-23 sector oscillation parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0026$.

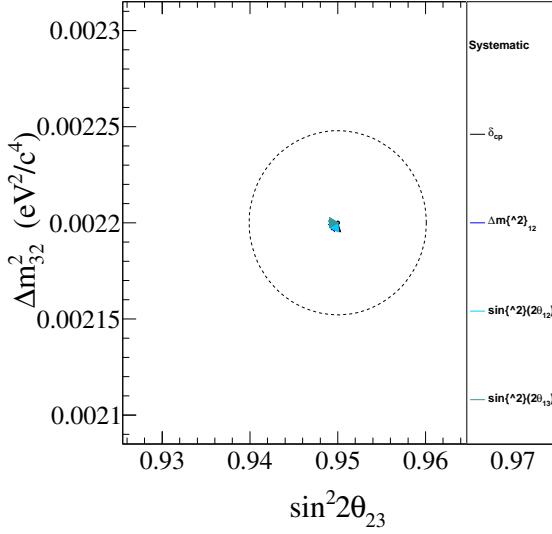


Figure 399: Effect of non-23 sector oscillation parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.95$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0022$.

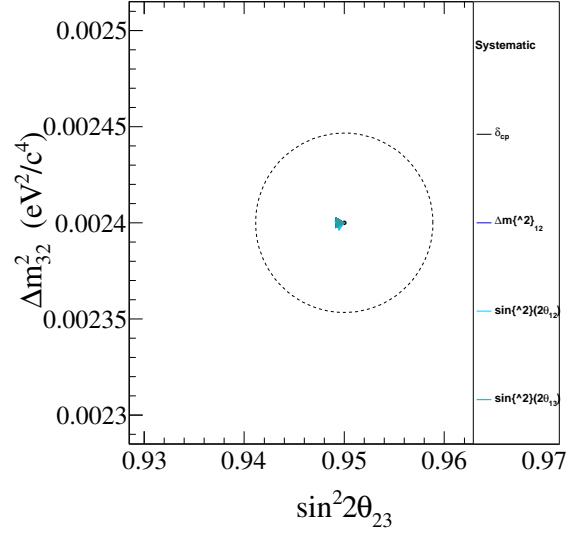


Figure 400: Effect of non-23 sector oscillation parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.95$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

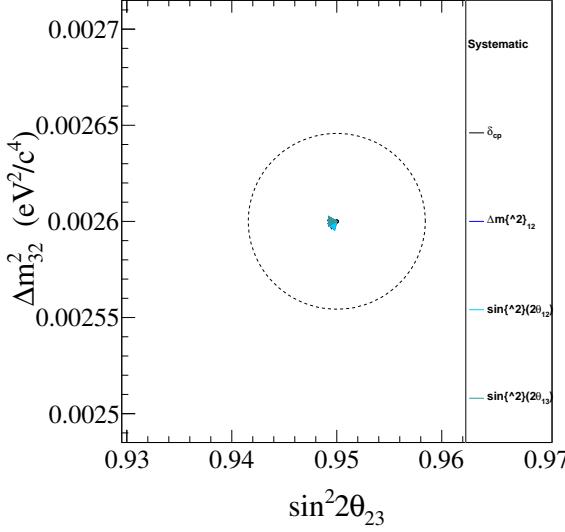


Figure 401: Effect of non-23 sector oscillation parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.95$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0026$.

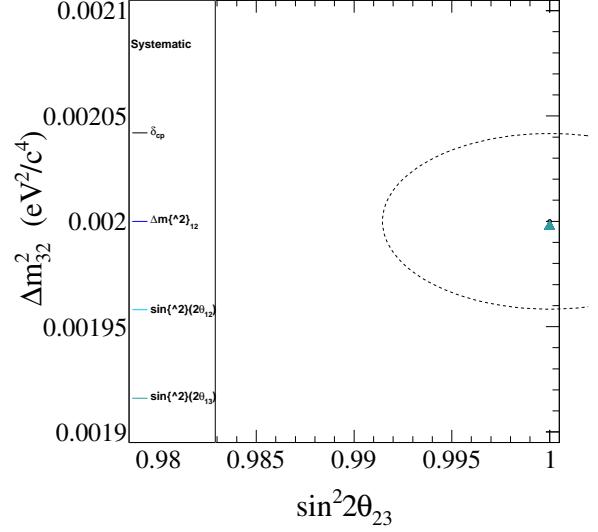


Figure 402: Effect of non-23 sector oscillation parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.002$.

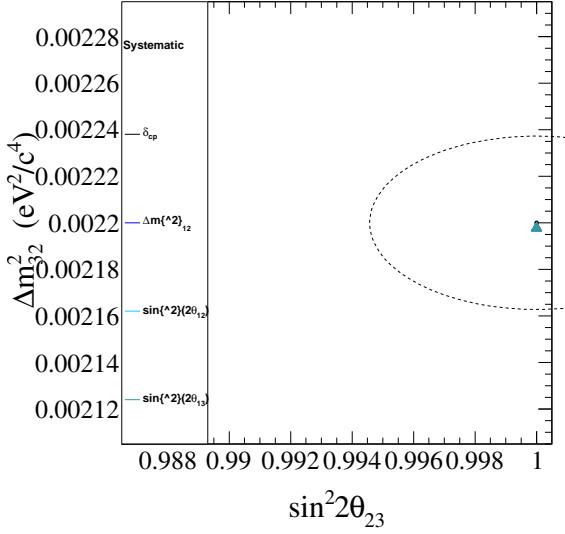


Figure 403: Effect of non-23 sector oscillation parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0022$.

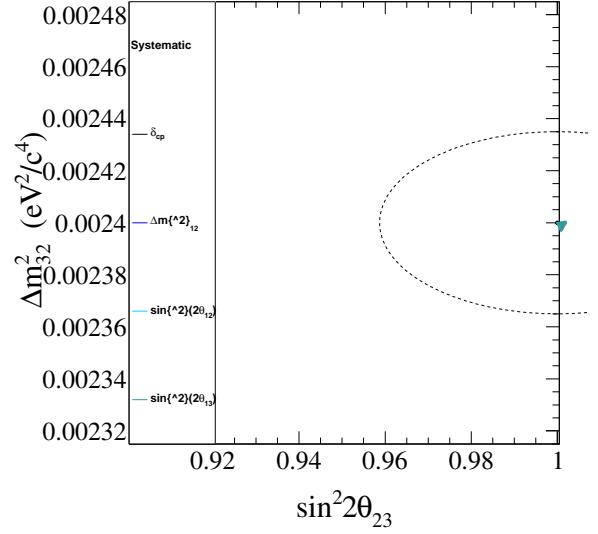


Figure 404: Effect of non-23 sector oscillation parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5 \times 10^{-5}$; $\Delta m_{32}^2 = 0.0024$.

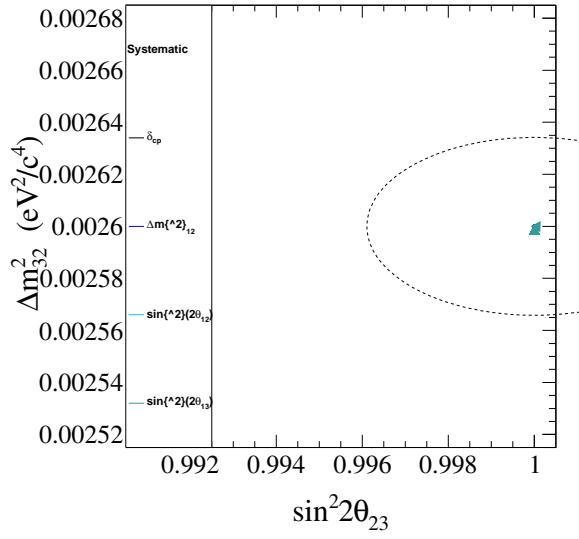


Figure 405: Effect of non-23 sector oscillation parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.0026$.

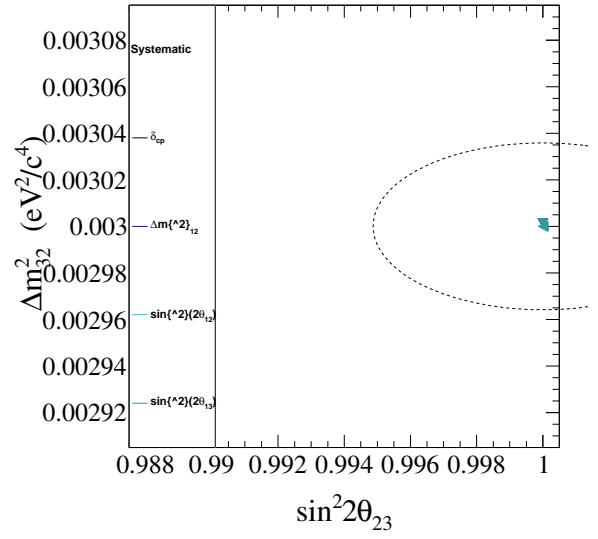


Figure 406: Effect of non-23 sector oscillation parameters on the best fit point, using a 2+0 fit, with a single systematic changed by ± 1 sigma. The ellipse shown is one quarter the size of the statistical error. For 3 flavour oscillations, using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{12}^2 = 7.5\text{e-}05$; $\Delta m_{32}^2 = 0.003$.

1388 **H. Fitter performance**

1389 The performance of the fitter has been evaluated at various oscillation points, using various POT, various levels
1390 of throwing systematics, and various fitters. For each study, 10000 toy datasets were created, and were fitted using
1391 MINUIT. Residual and pull distributions are presented in the following sections. The following three pull definitions
1392 are used:

$$1393 \text{Pull}_1 = \frac{(\text{best-fit parameter}) - (\text{input parameter})}{\sigma_{\text{fit}}} \quad (18)$$

$$1394 \text{Pull}_2 = \frac{(\text{best-fit parameter}) - (\text{input parameter})}{\sqrt{\sigma_{\text{prior}}^2 - \sigma_{\text{fit}}^2}}, \quad (19)$$

1395 and

$$1396 \text{Pull}_3 = \frac{(\text{best-fit parameter}) - (\text{nominal parameter})}{\sigma_{\text{fit}}} \quad (20)$$

1397 where σ_{fit} is output MINUIT/HESSE error and σ_{prior} is the prior assumed error. When Pull_2 is shown for a correlated
1398 systematic parameter, σ_{prior} is defined as the square root of the corresponding diagonal element of the covariance
1399 matrix.

1400 The various pull definitions are used as shown below

- 1401
- 1402 • Definition 1 is used for the pulls of both oscillation and systematic parameters in toy-MC studies.
 - Definition 2 is used for the pulls of systematic parameters in toy-MC studies.
 - Definition 3 is used for the pulls of systematic parameters both in toy-MC studies and for the fit to the actual
1401 data.

1403 **H.1. '2+0' fit, no systematic fluctuations**

1404 Figs. 407-408 show the pull and fitted values of $\sin^2 2\theta_{23}$. Figs. 409-410 show the corresponding plots for $|\Delta m_{32}^2|$.
 1405 The input values are $\sin^2 2\theta_{23} = 0.9$, $|\Delta m_{32}^2| = 2.4 \times 10^{-3} \text{ eV}^2/c^4$. A bias towards higher $\sin^2 2\theta_{23}$ can be seen, which
 1406 is present even when the pileup near the physical boundary is removed. This bias is due to low statistics at 3.01×20
 1407 POT. When Poisson fluctuations are made of a small number of events in a bin of the reconstructed energy distribution,
 1408 a downward fluctuation is more likely than an upward fluctuation. For example, a Poisson distribution with mean 3 has
 1409 $P(1) = 0.149$ and $P(2) = 0.224$, whereas $P(4) = 0.168$ and $P(5) = 0.101$. A downward fluctuation in a few bins around
 1410 the oscillation maximum increases the fitted value of $\sin^2(2\theta_{23})$, and this is the reason for the bias towards high values
 1411 of this parameter.

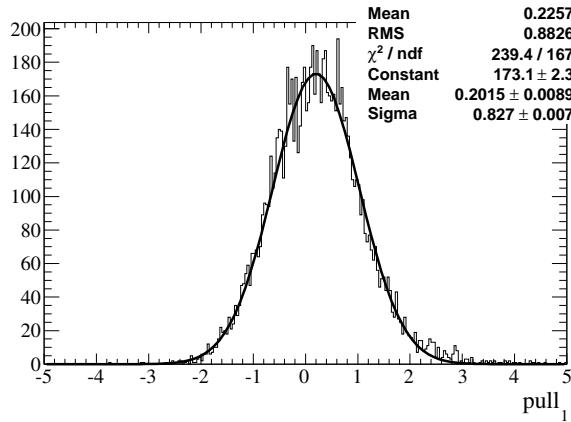


Figure 407: Pull₁ of $\sin^2 2\theta_{23}$ for a 2+0 fit, with oscillation parameters $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5 \times 10^{-5} \text{ eV}^2/c^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/c^4$ and for an exposure of 3.010×10^{20} POT. No systematic fluctuations are included.

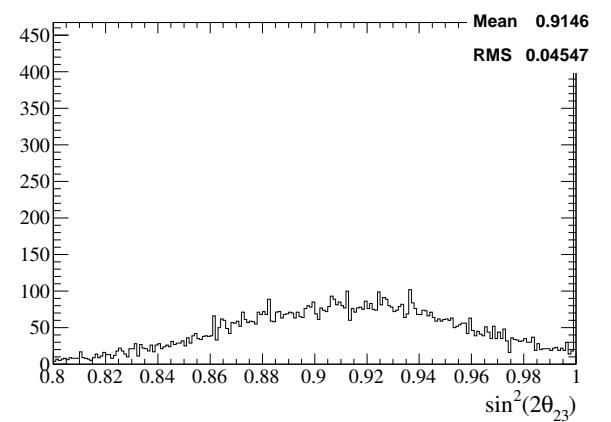


Figure 408: Fitted value of $\sin^2 2\theta_{23}$ for a 2+0 fit, with oscillation parameters $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5 \times 10^{-5} \text{ eV}^2/c^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/c^4$ and for an exposure of 3.010×10^{20} POT. No systematic fluctuations are included.

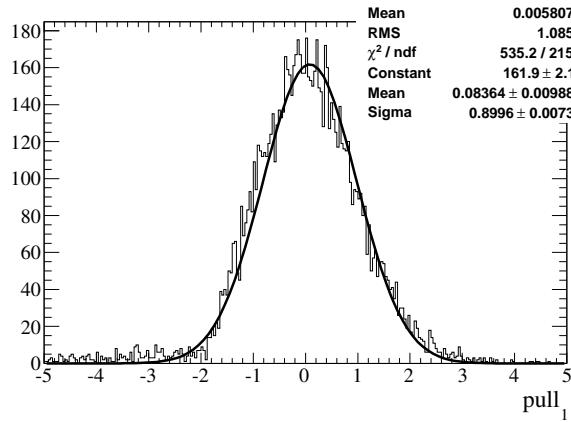


Figure 409: Pull₁ of $|\Delta m_{32}^2|$ for a 2+0 fit, with oscillation parameters $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5 \times 10^{-5} \text{ eV}^2/c^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/c^4$ and for an exposure of 3.010×10^{20} POT. No systematic fluctuations are included.

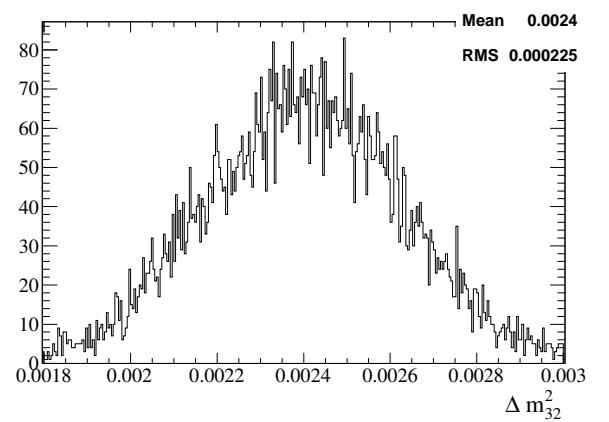


Figure 410: Fitted value of $|\Delta m_{32}^2|$ for a 2+0 fit, with oscillation parameters $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5 \times 10^{-5} \text{ eV}^2/c^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/c^4$ and for an exposure of 3.010×10^{20} POT. No systematic fluctuations are included.

¹⁴¹² **H.2. '2+0' fit, no systematic fluctuations, 100× RunI-III POT**

¹⁴¹³ Figs. 411-412 show the pull and fitted values of $\sin^2 2\theta_{23}$. Figs. 413-414 show the corresponding plots for $|\Delta m_{32}^2|$.
¹⁴¹⁴ The input values are $\sin^2 2\theta_{23} = 0.9$, $|\Delta m_{32}^2| = 2.4 \times 10^{-3} \text{ eV}^2/c^4$. The bias in $\sin^2 2\theta_{23}$ seen at current POT has
¹⁴¹⁵ gone.

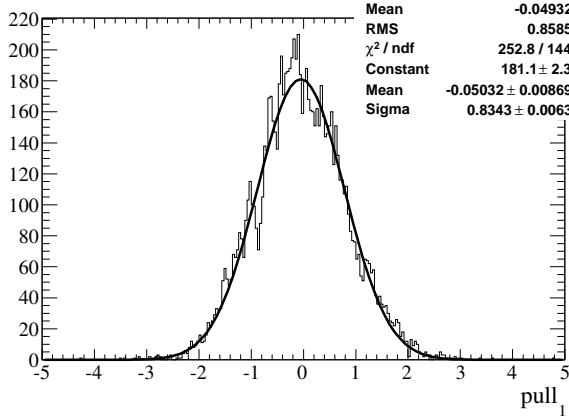


Figure 411: Pull₁ of $\sin^2 2\theta_{23}$ for a 2+0 fit, with oscillation parameters $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5 \times 10^{-5} \text{ eV}^2/c^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/c^4$ and for an exposure of 3.010×10^{22} POT. No systematic fluctuations are included.

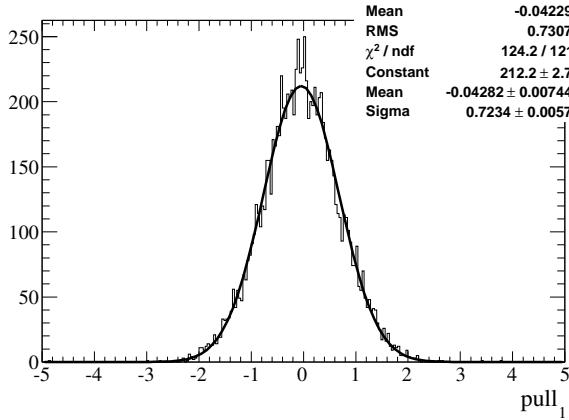


Figure 413: Pull₁ of $|\Delta m_{32}^2|$ for a 2+0 fit, with oscillation parameters $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5 \times 10^{-5} \text{ eV}^2/c^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/c^4$ and for an exposure of 3.010×10^{22} POT. No systematic fluctuations are included.

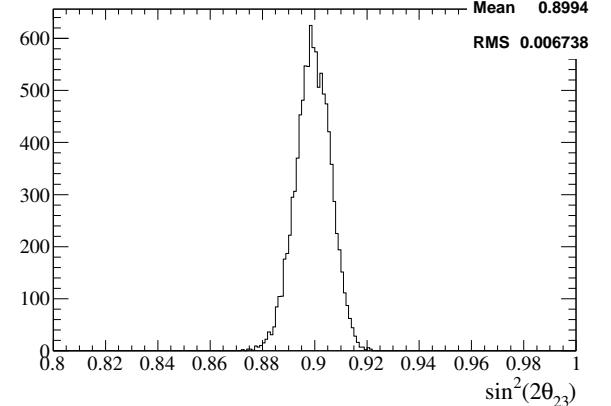


Figure 412: Fitted value of $\sin^2 2\theta_{23}$ for a 2+0 fit, with oscillation parameters $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5 \times 10^{-5} \text{ eV}^2/c^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/c^4$ and for an exposure of 3.010×10^{22} POT. No systematic fluctuations are included.

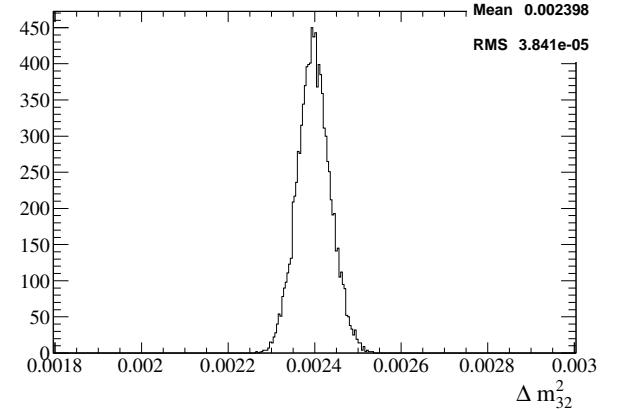


Figure 414: Fitted value of $|\Delta m_{32}^2|$ for a 2+0 fit, with oscillation parameters $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5 \times 10^{-5} \text{ eV}^2/c^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/c^4$ and for an exposure of 3.010×10^{22} POT. No systematic fluctuations are included.

1416 **H.3. '2+8' fit, no systematic fluctuations**

1417 Figs. 415-416 show the pull and fitted values of $\sin^2 2\theta_{23}$. Figs. 417-418 show the corresponding plots for $|\Delta m_{32}^2|$.
 1418 The input values are $\sin^2 2\theta_{23} = 0.9$, $|\Delta m_{32}^2| = 2.4 \times 10^{-3} \text{ eV}^2/c^4$. The results are similar to the '2+0' case (a bias
 1419 towards higher $\sin^2 2\theta_{23}$ can be seen, which is present even when the pileup near the physical boundary is removed)
 1420 but no additional biases are present. Therefore, adding systematics to the fit does not cause significant changes to the
 1421 performance of the oscillation part of the fit.

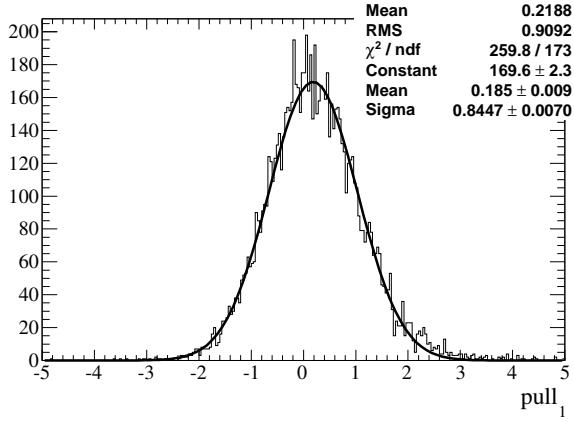


Figure 415: Pull₁ of $\sin^2 2\theta_{23}$ for a 2+8 fit, with oscillation parameters $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5 \times 10^{-5} \text{ eV}^2/c^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/c^4$ and for an exposure of 3.010×10^{20} POT. No systematic fluctuations are included.

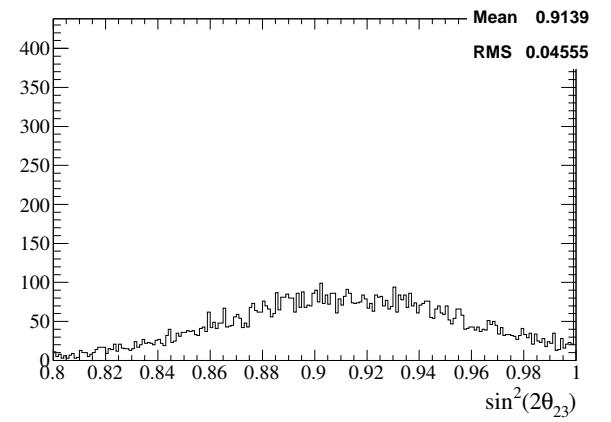


Figure 416: Fitted value of $\sin^2 2\theta_{23}$ for a 2+8 fit, with oscillation parameters $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5 \times 10^{-5} \text{ eV}^2/c^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/c^4$ and for an exposure of 3.010×10^{20} POT. No systematic fluctuations are included.

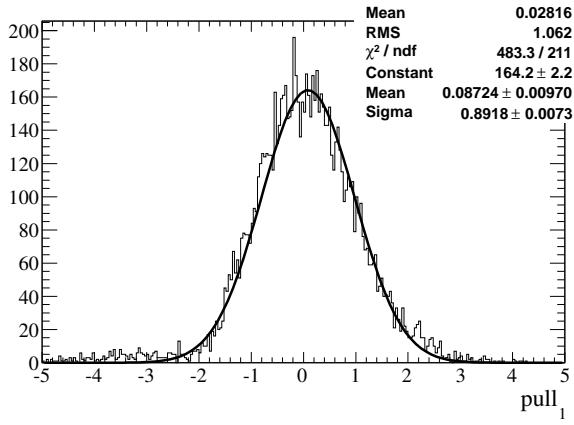


Figure 417: Pull₁ of $|\Delta m_{32}^2|$ for a 2+8 fit, with oscillation parameters $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5 \times 10^{-5} \text{ eV}^2/c^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/c^4$ and for an exposure of 3.010×10^{20} POT. No systematic fluctuations are included.

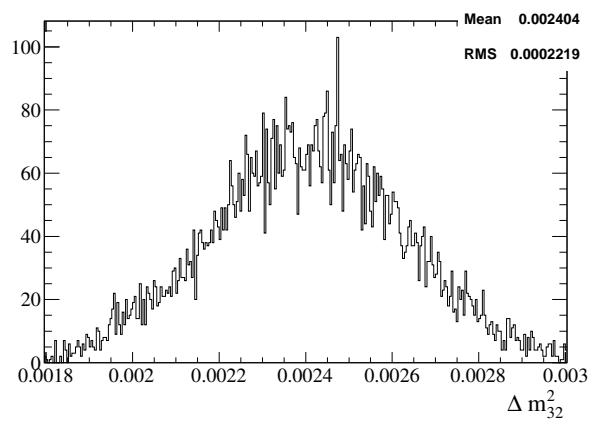


Figure 418: Fitted value of $|\Delta m_{32}^2|$ for a 2+8 fit, with oscillation parameters $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5 \times 10^{-5} \text{ eV}^2/c^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/c^4$ and for an exposure of 3.010×10^{20} POT. No systematic fluctuations are included.

1422 **H.4. '2+8' fit, dominant systematic fluctuations**

1423 Figs. 419-420 show the pull and fitted values of $\sin^2 2\theta_{23}$. Figs. 421-422 show the corresponding plots for $|\Delta m_{32}^2|$.
 1424 The input values are $\sin^2 2\theta_{23} = 0.9$, $|\Delta m_{32}^2| = 2.4 \times 10^{-3} \text{ eV}^2/c^4$. The bias in $\sin^2 2\theta_{23}$ is still present.

1425 Fig. 423 shows the residuals of the systematic parameters. Figs. 424-426 show the pulls distributions of the sys-
 1426 tematic parameters. Some of the distributions are wide, but there are no unexpected features in the plots. $f_{E;v}^{SK}$ in Fig.
 1427 424 is non-Gaussian, but this is not unexpected; the energy scale systematic has a discontinuous derivative, leading to
 1428 issues with the Hesse error. It should be noted that the spectral function is not expected to give a Gaussian distribution
 1429 since the throws are uniform between 0 and 1, and the fitted value is strictly confined to the range [0,1]. The plots show
 1430 that a best-fit value of 0 is favoured.

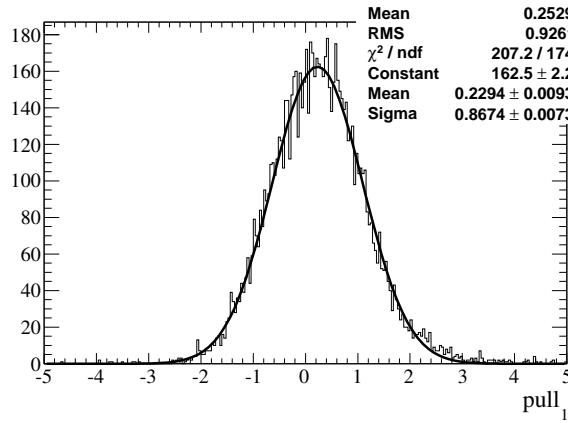


Figure 419: Pull₁ of $\sin^2 2\theta_{23}$ for a 2+8 fit, with oscillation parameters $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5e-05 \text{ eV}^2/c^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/c^4$ and for an exposure of 3.010×10^{20} POT. The 8 dominant systematics are fluctuated.

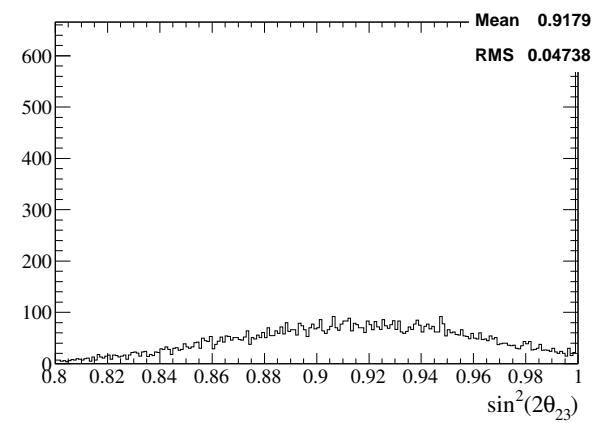


Figure 420: Fitted value of $\sin^2 2\theta_{23}$ for a 2+8 fit, with oscillation parameters $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5e-05 \text{ eV}^2/c^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/c^4$ and for an exposure of 3.010×10^{20} POT. The 8 dominant systematics are fluctuated.

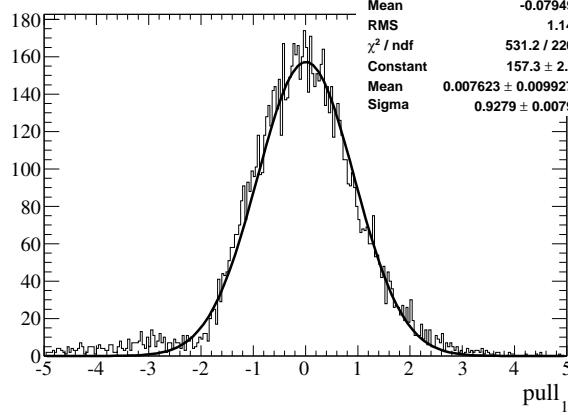


Figure 421: Pull₁ of $|\Delta m_{32}^2|$ for a 2+8 fit, with oscillation parameters $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5e-05 \text{ eV}^2/c^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/c^4$ and for an exposure of 3.010×10^{20} POT. The 8 dominant systematics are fluctuated.

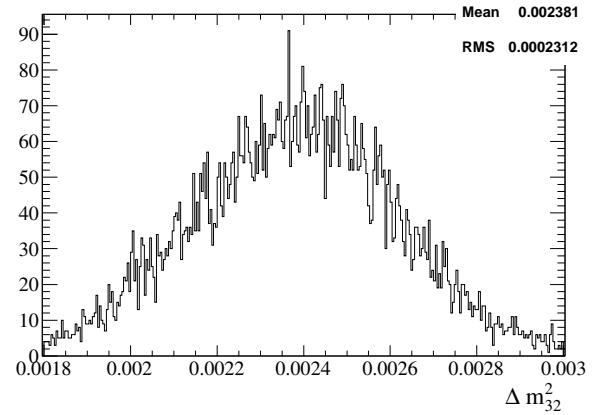


Figure 422: Fitted value of $|\Delta m_{32}^2|$ for a 2+8 fit, with oscillation parameters $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5e-05 \text{ eV}^2/c^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/c^4$ and for an exposure of 3.010×10^{20} POT. The 8 dominant systematics are fluctuated.

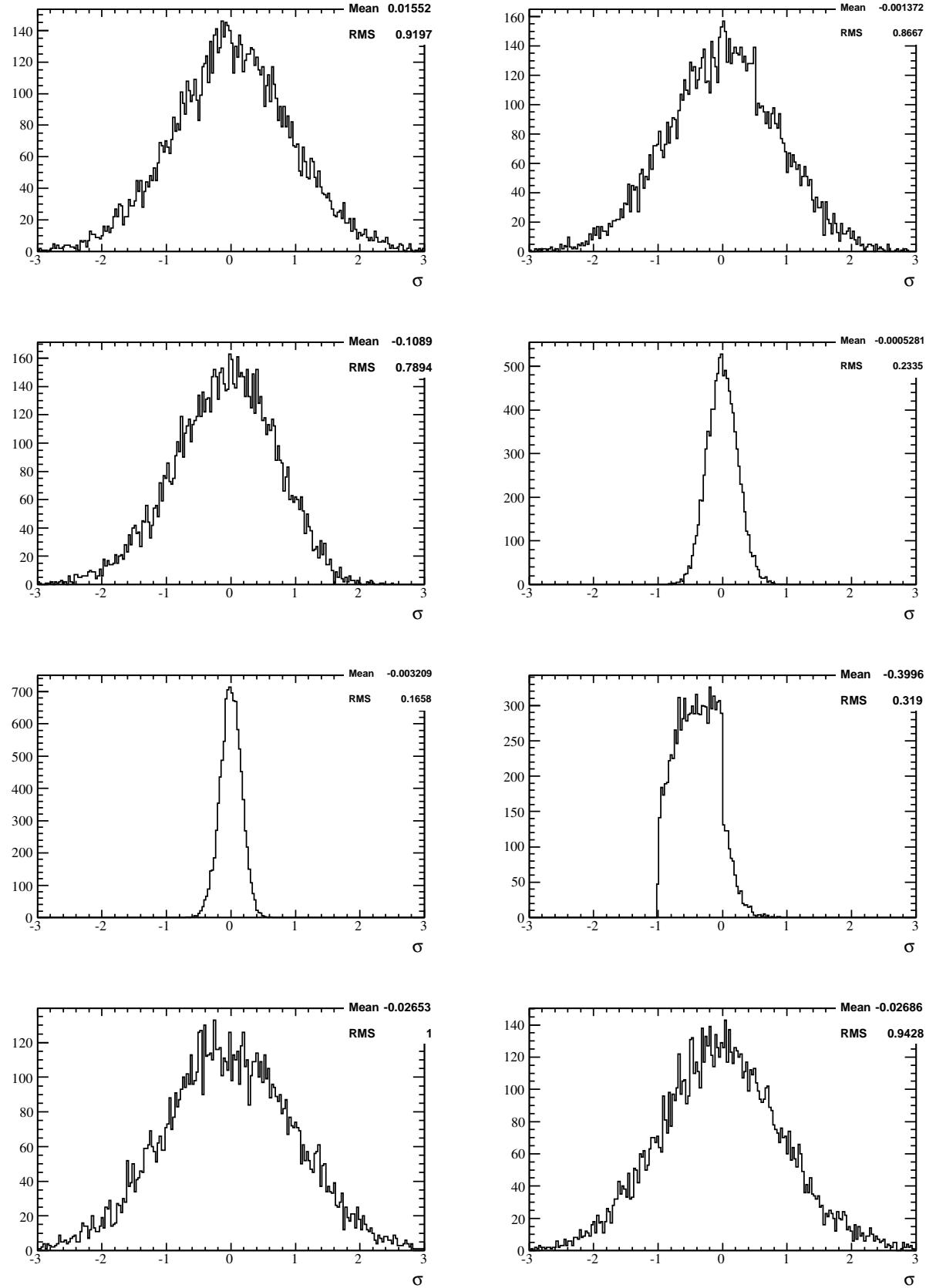


Figure 423: Residuals of the systematic parameters for a 2+8 fit, with oscillation parameters $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5 \times 10^{-5} \text{ eV}^2/c^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/c^4$ and for an exposure of 3.010×10^{20} POT. The 8 dominant systematics are fluctuated. The plots correspond to (line by line, left to right): $f_{E;r}^{SK}$; $f_{CCnonQE;r}^{SK}$; $f_{NC;r}^{SK}$; $f_{16;t,r}^{banff}$ (MA QE); $f_{18;t,r}^{banff}$ (CCQE norm $< 1.5 \text{ GeV}$); $f_{SF;t,r}$; $f_{bindE;t,r}$; $f_{\pi-less\Delta;t,r}$.

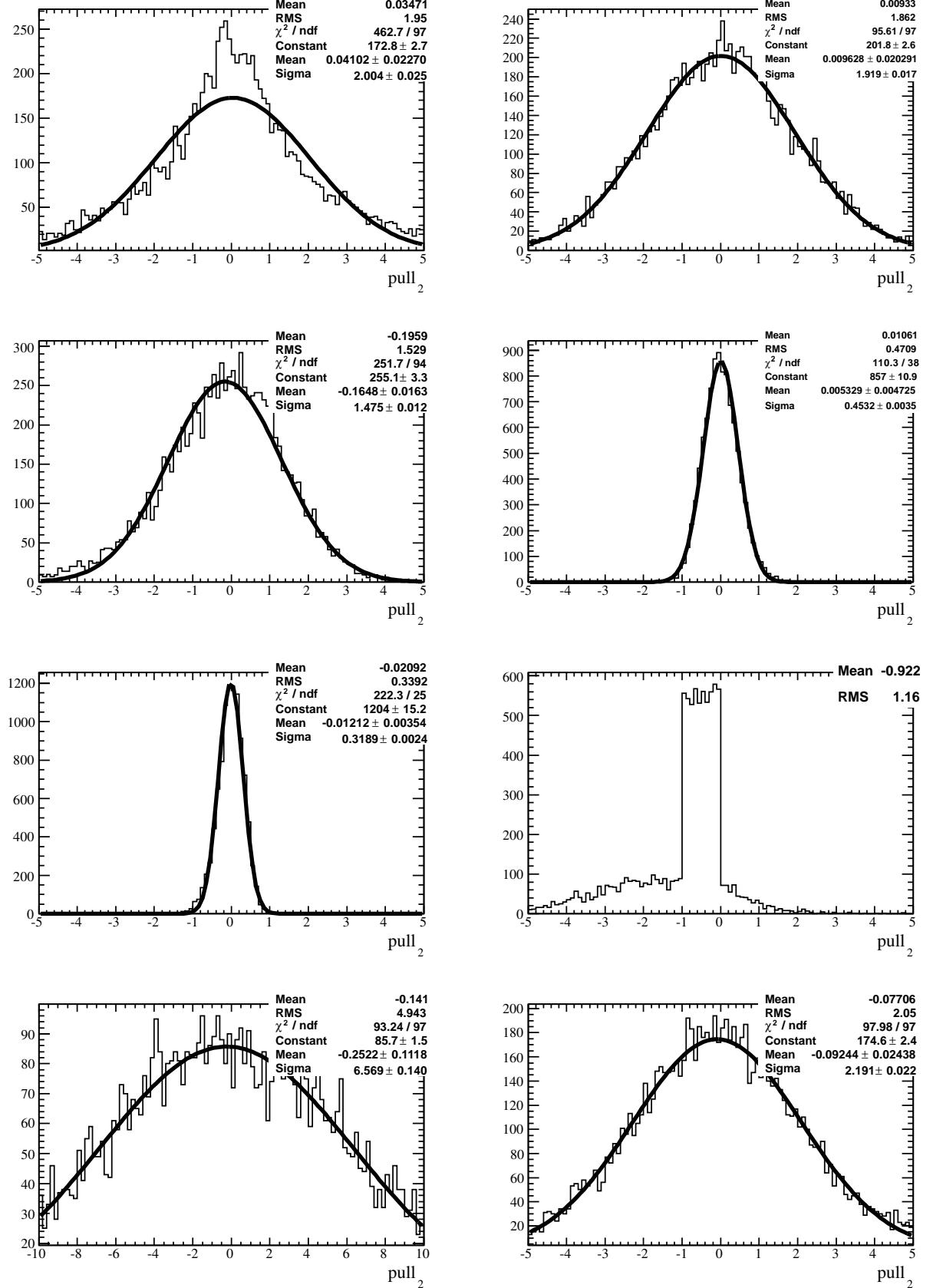


Figure 424: Pull₂ of the systematic parameters for a 2+8 fit, with oscillation parameters $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5e-05 \text{ eV}^2/c^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/c^4$ and for an exposure of 3.010×10^{20} POT. The 8 dominant systematics are fluctuated. The plots correspond to (line by line, left to right): $f_{E;r}^{SK}$; $f_{CCnonQE;r}^{SK}$; $f_{NC;r}^{SK}$; $f_{16;t;r}^{banff}$ (M_A QE); $f_{18;t,r}^{banff}$ (CCQE norm < 1.5 GeV); $f_{SF;t,r}$; $f_{bindE;t,r}$; $f_{\pi-less\Delta;t,r}$.

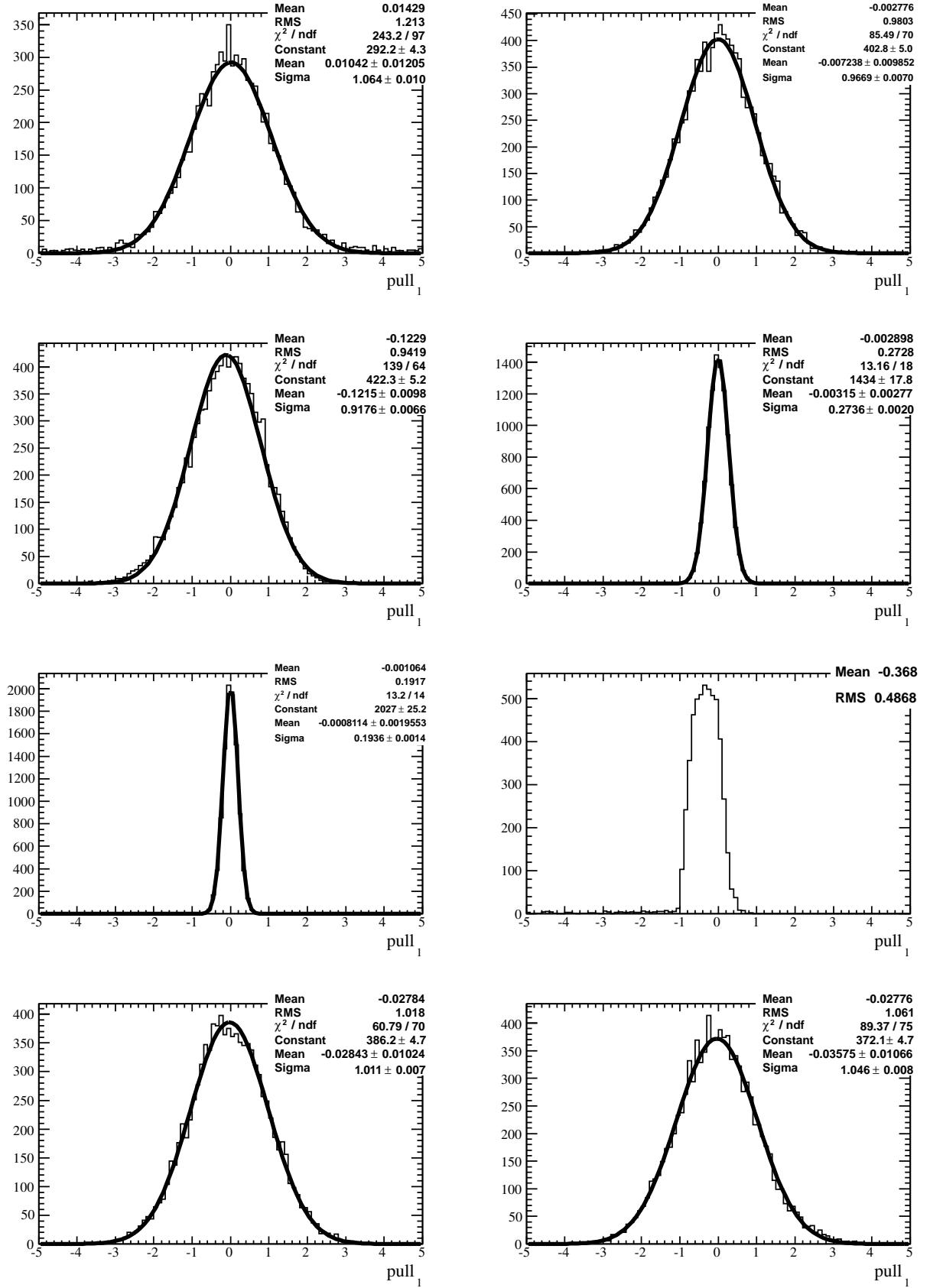


Figure 425: pull_1 of the systematic parameters for a 2+8 fit, with oscillation parameters $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5e-05 \text{ eV}^2/c^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/c^4$ and for an exposure of 3.010×10^{20} POT. The 8 dominant systematics are fluctuated. The plots correspond to (line by line, left to right): $f_{E;r}^{SK}$; $f_{CCnonQE;r}^{SK}$; $f_{NC;r}^{SK}$; $f_{16;t;r}^{banff}$ (MA QE); $f_{18;t,r}^{banff}$ (CCQE norm < 1.5 GeV); $f_{SF;t,r}$; $f_{bindE;t,r}$; $f_{\pi-less\Delta;t,r}$.

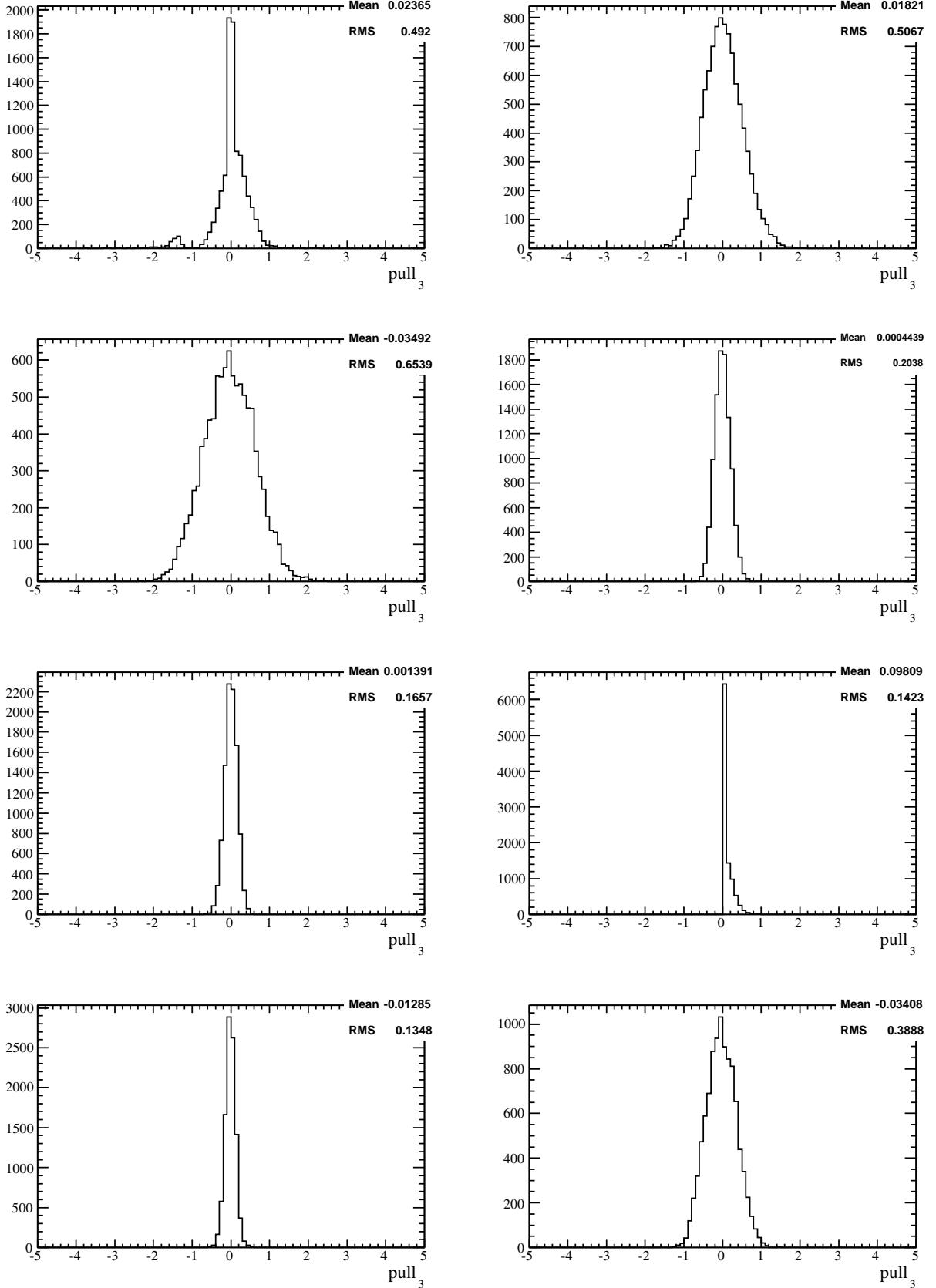


Figure 426: pull_3 of the systematic parameters for a 2+8 fit, with oscillation parameters $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5 \times 10^{-5} \text{ eV}^2/\text{c}^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/\text{c}^4$ and for an exposure of 3.010×10^{20} POT. The 8 dominant systematics are fluctuated. The plots correspond to (line by line, left to right): $f_{E;r}^{SK}$; $f_{CCnonQE;r}^{SK}$; $f_{NC;r}^{SK}$; $f_{16;t;r}^{banff}$ (MAQE); $f_{18;t,r}^{banff}$ (CCQE norm < 1.5 GeV); $f_{SF;t,r}$; $f_{bindE;t,r}$; $f_{\pi-less\Delta;t,r}$.

1431 *H.5. '2+8' fit, all systematic fluctuations*

1432 Figs. 427-428 show the pull and fitted values of $\sin^2 2\theta_{23}$. Figs. 429-430 show the corresponding plots for $|\Delta m_{32}^2|$.
 1433 The input values are $\sin^2 2\theta_{23} = 0.9$, $|\Delta m_{32}^2| = 2.4 \times 10^{-3} \text{ eV}^2/c^4$. The bias in $\sin^2 2\theta_{23}$ is still present.

1434 Fig. 431 shows the residuals of the systematic parameters. Figs. 432-434 show the pull distributions of the system-
 1435 atic parameters. The distributions have widened, but this is as to be expected (the parameters that are thrown but not
 1436 fitted are *absorbed* by the parameters that are fitted). There are still no unexpected features.

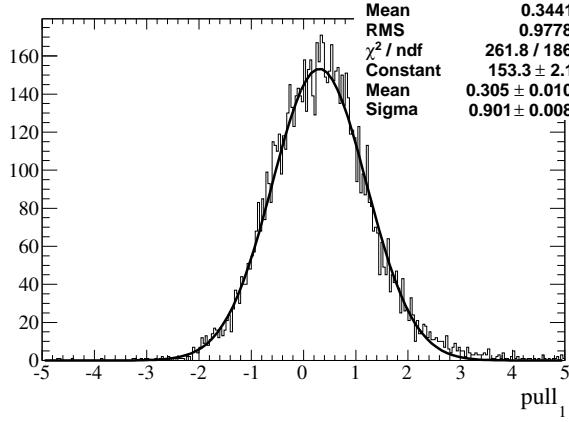


Figure 427: Pull₁ of $\sin^2 2\theta_{23}$ for a 2+8 fit, with oscillation parameters $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5 \times 10^{-5} \text{ eV}^2/c^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/c^4$ and for an exposure of 3.010×10^{20} POT. All systematic fluctuations are included.

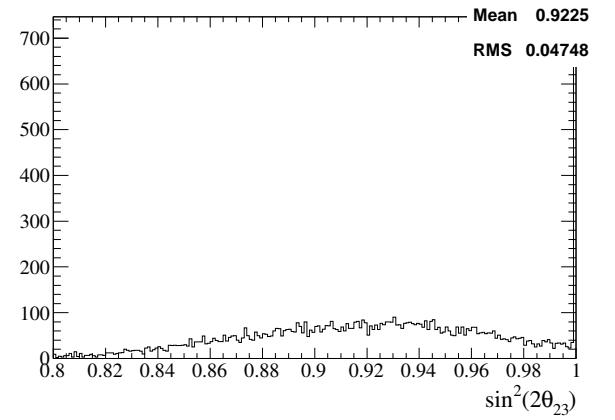


Figure 428: Fitted value of $\sin^2 2\theta_{23}$ for a 2+8 fit, with oscillation parameters $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5 \times 10^{-5} \text{ eV}^2/c^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/c^4$ and for an exposure of 3.010×10^{20} POT. All systematic fluctuations are included.

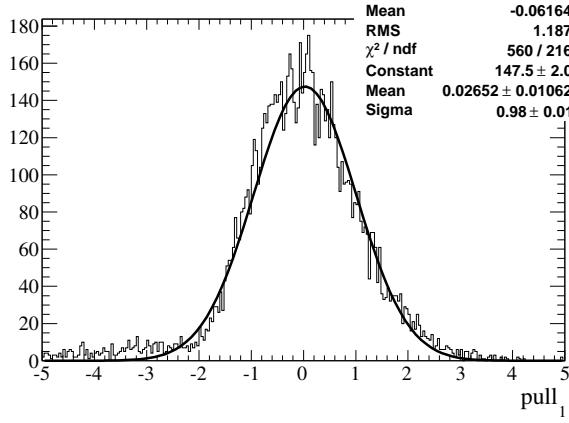


Figure 429: Pull₁ of $|\Delta m_{32}^2|$ for a 2+8 fit, with oscillation parameters $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5 \times 10^{-5} \text{ eV}^2/c^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/c^4$ and for an exposure of 3.010×10^{20} POT. All systematic fluctuations are included.

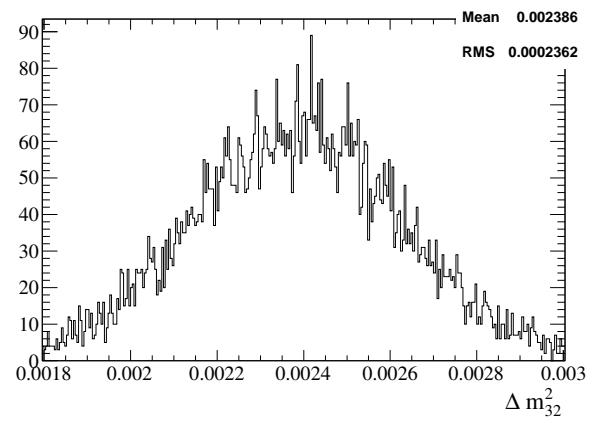


Figure 430: Fitted value of $|\Delta m_{32}^2|$ for a 2+8 fit, with oscillation parameters $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5 \times 10^{-5} \text{ eV}^2/c^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/c^4$ and for an exposure of 3.010×10^{20} POT. All systematic fluctuations are included.

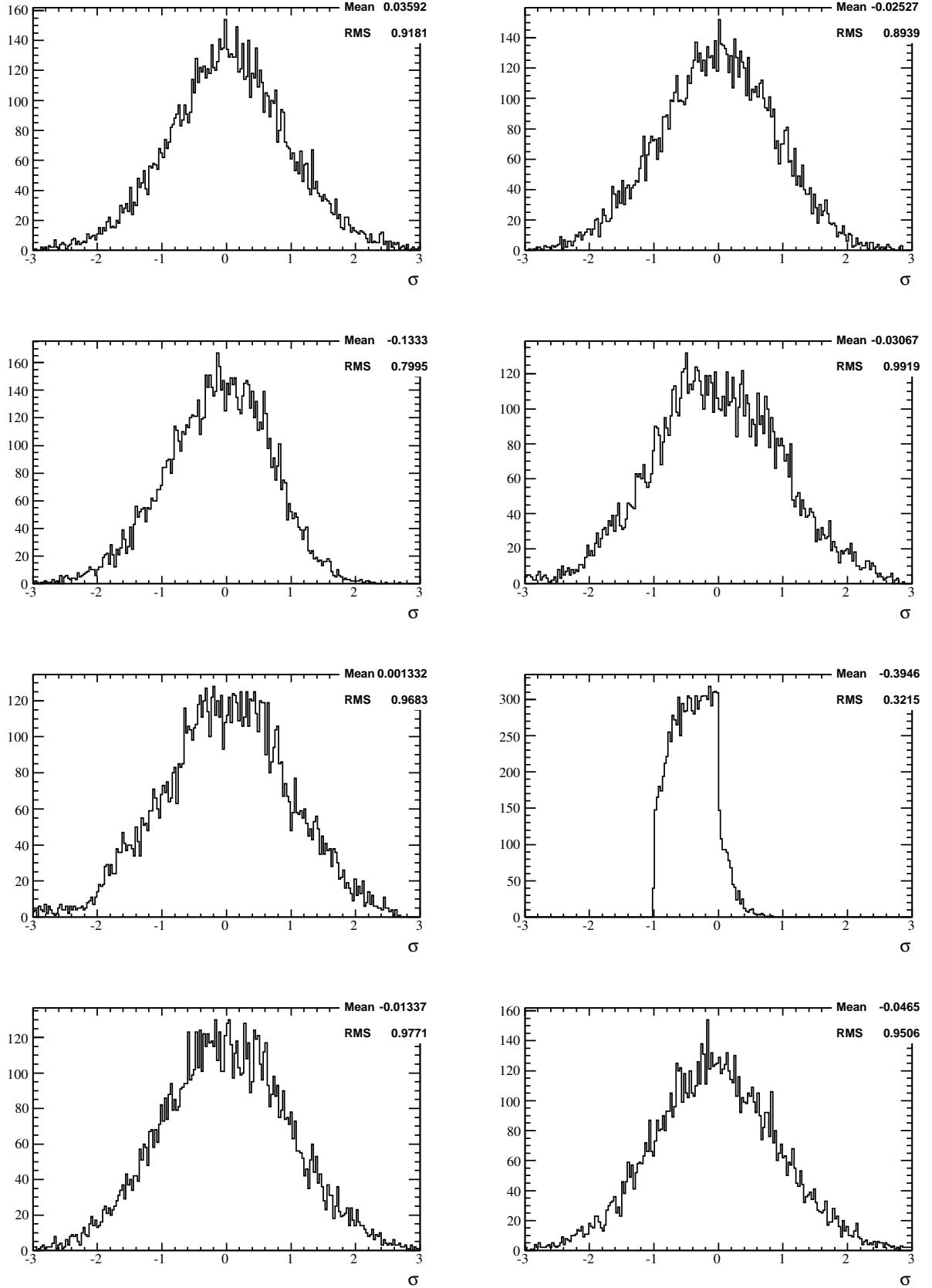


Figure 431: Residual of the systematic parameters for a 2+8 fit, with oscillation parameters $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5 \times 10^{-5} \text{ eV}^2/c^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/c^4$ and for an exposure of 3.010×10^{20} POT. All systematic fluctuations are included. The plots correspond to (line by line, left to right): $f_{E;r}^{SK}$; $f_{CCnonQE;r}^{SK}$; $f_{NC;r}^{SK}$; $f_{16;t;r}^{banff}$ (M_A QE); $f_{18;t;r}^{banff}$ (CCQE norm < 1.5 GeV); $f_{SF;t,r}$; $f_{bindE;t,r}$; $f_{\pi-less\Delta;t,r}$.

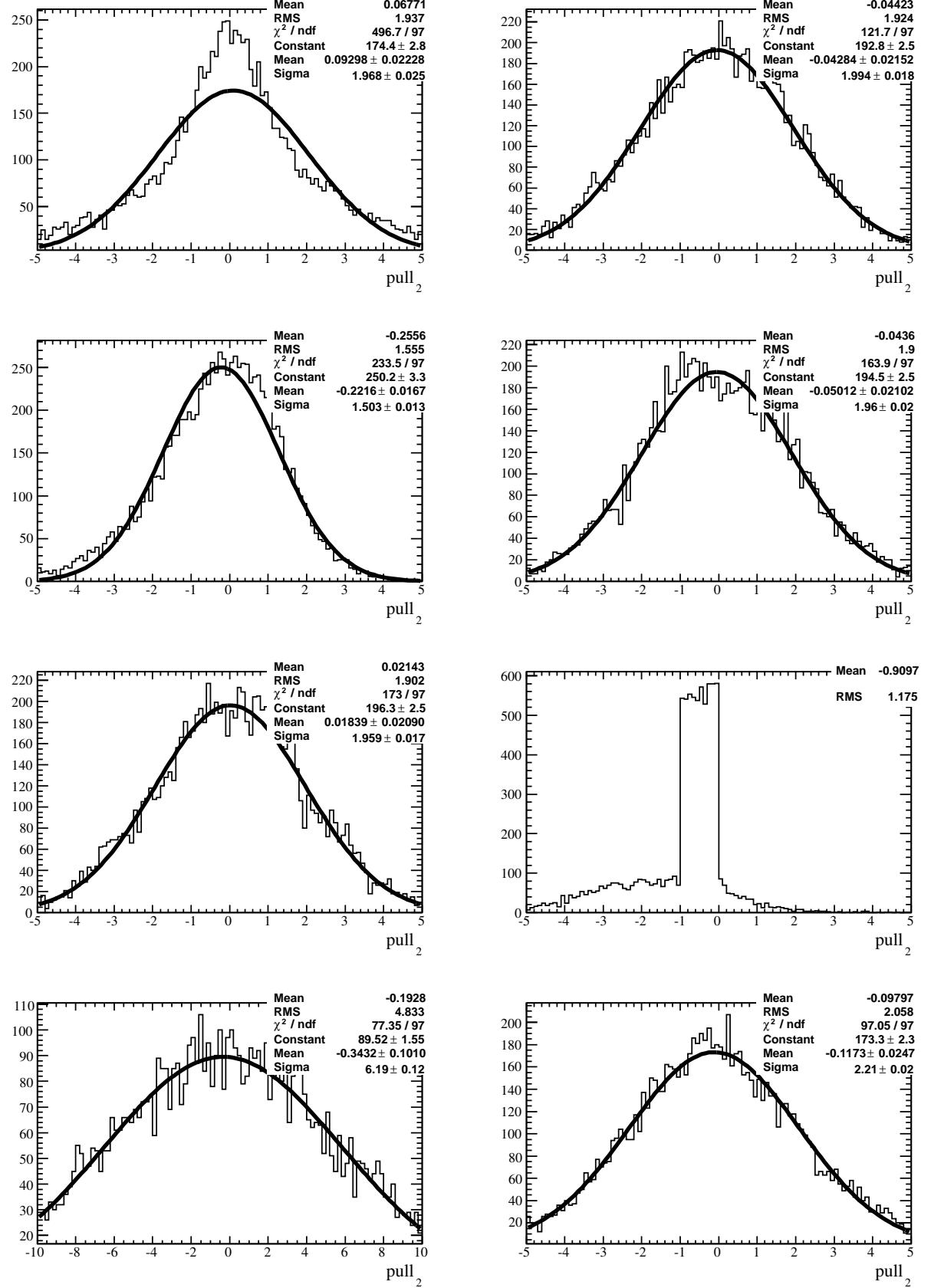


Figure 432: Pull₂ of the systematic parameters for a 2+8 fit, with oscillation parameters $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5 \times 10^{-5} \text{ eV}^2/\text{c}^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/\text{c}^4$ and for an exposure of 3.010×10^{20} POT. All systematic fluctuations are included. The plots correspond to (line by line, left to right): $f_{E;r}^{SK}$; $f_{CCnonQE;r}^{SK}$; $f_{NC;t,r}^{SK}$; $f_{16;t,r}^{baff}$ (M_A QE); $f_{18;t,r}^{baff}$ (CCQE norm < 1.5 GeV); $f_{SF;t,r}$; $f_{bindE;t,r}$; $f_{\pi-lessDelta;t,r}$.

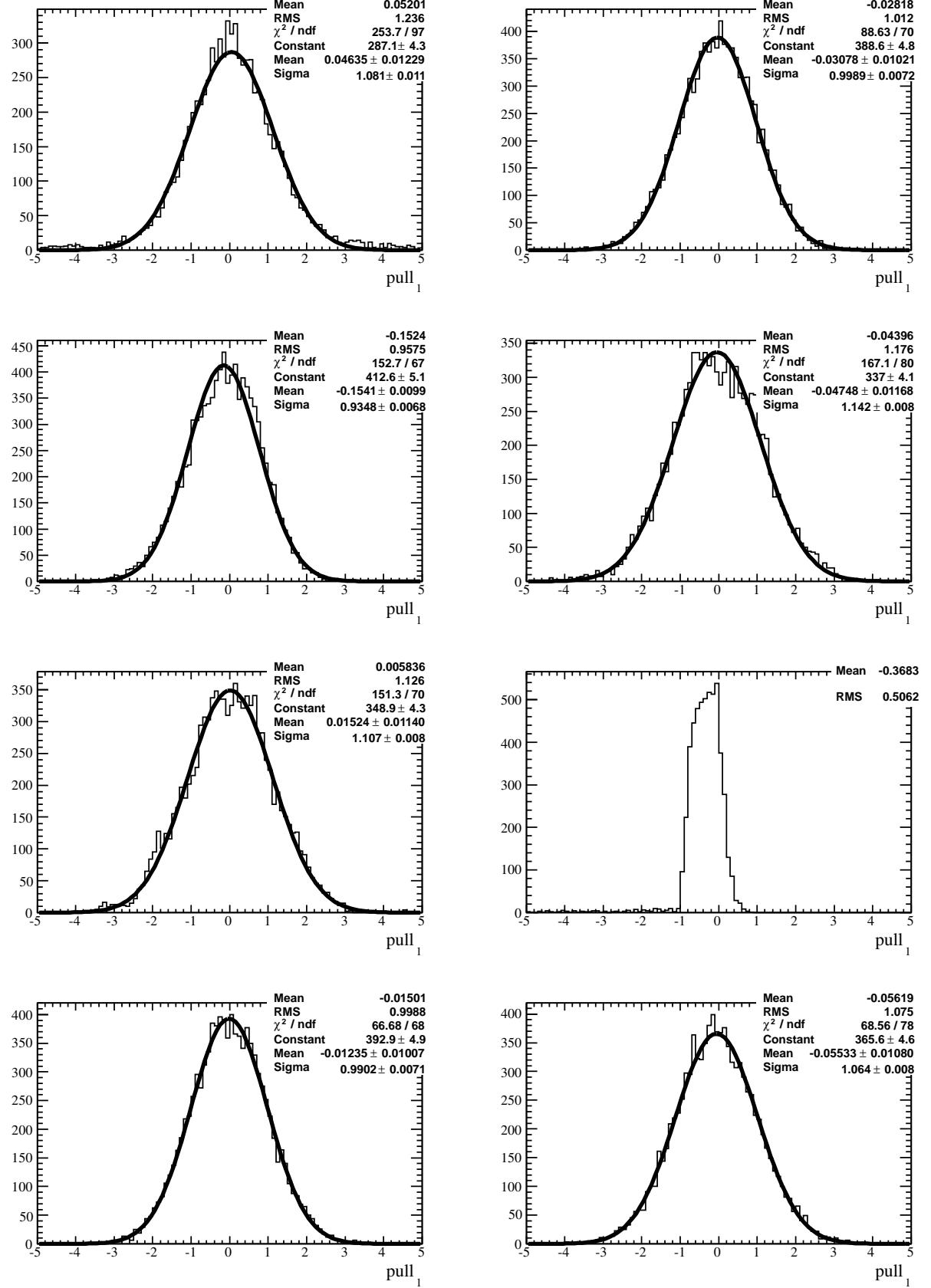


Figure 433: pull_1 of the systematic parameters for a 2+8 fit, with oscillation parameters $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5 \times 10^{-5} \text{ eV}^2/\text{c}^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/\text{c}^4$ and for an exposure of 3.010×10^{20} POT. All systematic fluctuations are included. The plots correspond to (line by line, left to right): $f_{E;r}^{SK}$; $f_{CCnonQE;r}^{SK}$; $f_{NC;r}^{SK}$; $f_{16;t;r}^{baff}$ (MA QE); $f_{18;t,r}^{baff}$ (CCQE norm < 1.5 GeV); $f_{SF;t,r}$; $f_{bindE;t,r}$; $f_{\pi-less\Delta;t,r}$.

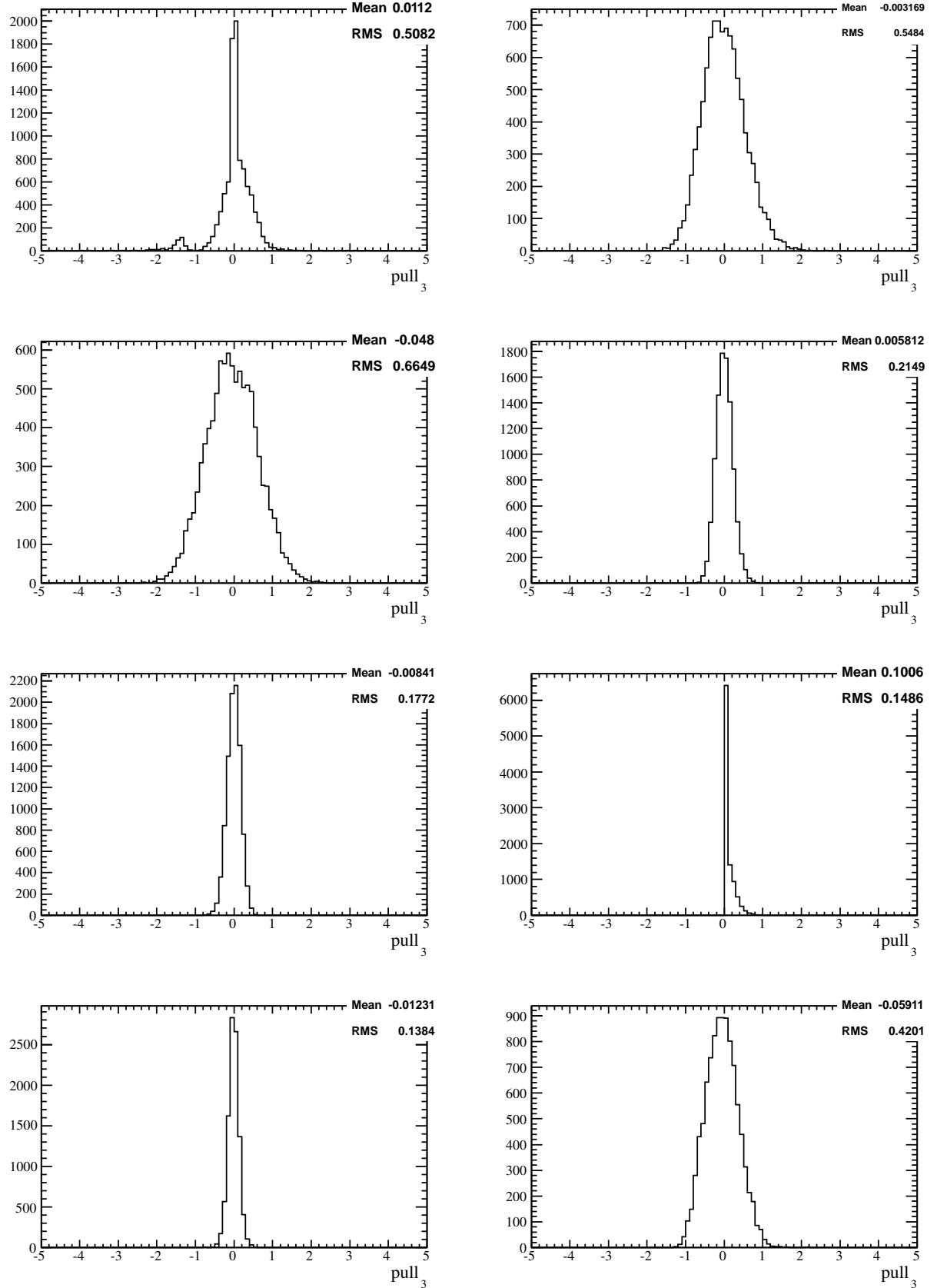


Figure 434: pull_3 of the systematic parameters for a 2+8 fit, with oscillation parameters $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 0.9$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5 \times 10^{-5} \text{ eV}^2/\text{c}^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/\text{c}^4$ and for an exposure of 3.010×10^{20} POT. All systematic fluctuations are included. The plots correspond to (line by line, left to right): $f_{E;r}^{SK}$; $f_{CCnonQE;r}^{SK}$; $f_{NC;r}^{SK}$; $f_{16;t;r}^{banff}$ (MAQE); $f_{18;t;r}^{banff}$ (CCQE norm < 1.5 GeV); $f_{SF;t,r}$; $f_{bindE;t,r}$; $f_{\pi-less\Delta;t,r}$.

1437 **I. Binning studies**

1438 *I.1. True energy binning*

1439 The chosen true neutrino energy binning scheme needs to have enough granularity for precise application of os-
1440 cillation probabilities and of systematic parameter response functions (with the former proven to be the primary con-
1441 sideration). The chosen 84-bin scheme is described in Section 2.2.5. This binning scheme was selected as a trade-off
1442 between CPU efficiency and accuracy, as oscillation probabilities are calculated at the centre of each true energy bin.
1443 Single μ -like ring event reconstructed energy spectra obtained with the chosen binning scheme were compared against
1444 spectra obtained with an alternative, much finer, binning scheme. The alternative scheme uses 780 bins as follows:
1445 200 5-MeV bins in 0-1 GeV and 580 50-MeV bins in 1-30 GeV. Figs. 435-454 show the ratio of individual SuperK MC
1446 mode E_{reco} spectra, made with 84-bin E_{true} and 780-bin E_{true} . While there are some >1% differences, these occur
1447 in modes that are a small contribution to the total E_{reco} spectrum. This is reiterated in Fig. 455, which shows the same
1448 ratio, but for the total E_{reco} spectrum.

1449 *I.2. Reconstructed energy binning*

1450 The chosen reconstructed neutrino energy binning scheme needs to have sufficient granularity (considering the
1451 experimental reconstructed neutrino energy resolution and the current statistics) to allow a precise determination of
1452 neutrino oscillation parameters while, at the same time, a reasonable CPU efficiency is retained. The binning also needs
1453 to be fine enough to allow the precise application of systematic parameter response functions in the p.d.f. (discussed
1454 in Appendix I.4). The selected reconstructed neutrino energy binning scheme (73 bins) is shown in Appendix 2.2.5. A
1455 sensitivity study (see Appendix C for details) at the MINOS 2012 best fit point has been performed with an alternative,
1456 much finer, reconstructed energy binning scheme: 600 50 MeV bins, 0 - 30 GeV. The result can be seen in Fig. 456.
1457 The plot shows that the chosen 73-bin scheme is sufficient.

1458 *I.3. SuperK MC templates in the chosen binning*

1459 The nominal SuperK MC templates, in the chosen binning, are shown in Figs. 457-461.

1460 *I.4. True and reconstructed energy binning for systematic parameter response functions*

1461 Systematic parameter response functions (cubic splines) were constructed in bins of true and reconstructed energy.
1462 This binning is given in Sec. 3.1.3. A study was performed to check the effect of this binning. This was done by
1463 creating tweaked single μ -like ring event reconstructed energy spectra using the splines, and comparing them with the
1464 equivalent tweaked spectra made with event-by-event reweighting (the latter being too CPU-demanding to be used in
1465 the oscillation parameter fit). Both the spline spectra and the event-by-event spectra were made for no oscillations. The
1466 73-bin scheme for the Monte Carlo templates given in Sec. 2.2.5 was used. Some examples of the ratios of the spline
1467 spectra to the event-by-event reweighted spectra are shown in Figs. 462-468. They show that the ratios are very close
1468 to 1.0 for the ν_μ and $\bar{\nu}_\mu$ spectra, which comprise the bulk of the total predicted single μ -like ring spectrum.

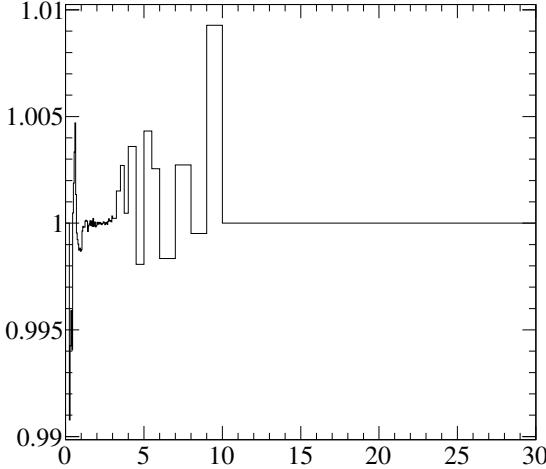


Figure 435: Ratio of SuperK MC E_{reco} spectra, for mode ν_μ CCQE made with 84 bin E_{true} and 780 bin E_{true} , for an exposure of $3.010 \text{imes} 10^{20}$ POT. The number of events was calculated using the BANFF-tuned MC templates. Using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5 \text{e-}05 \text{ eV}^2/c^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/c^4$.

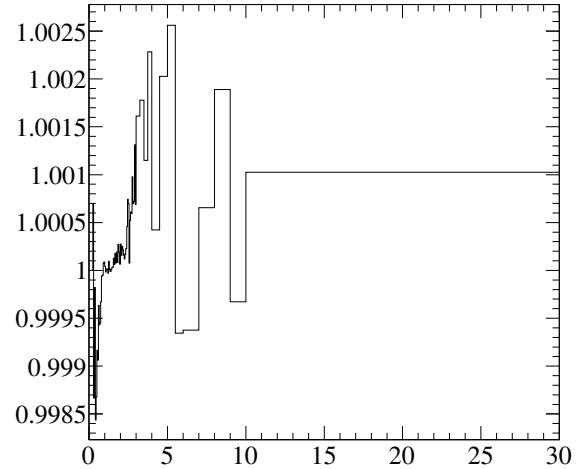


Figure 436: Ratio of SuperK MC E_{reco} spectra, for mode ν_μ CC 1π made with 84 bin E_{true} and 780 bin E_{true} , for an exposure of $3.010 \text{imes} 10^{20}$ POT. The number of events was calculated using the BANFF-tuned MC templates. Using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5 \text{e-}05 \text{ eV}^2/c^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/c^4$.

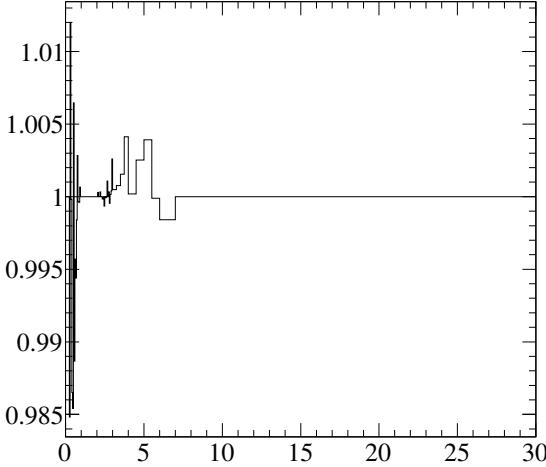


Figure 437: Ratio of SuperK MC E_{reco} spectra, for mode ν_μ CC coherent made with 84 bin E_{true} and 780 bin E_{true} , for an exposure of $3.010 \text{imes} 10^{20}$ POT. The number of events was calculated using the BANFF-tuned MC templates. Using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5 \text{e-}05 \text{ eV}^2/c^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/c^4$.

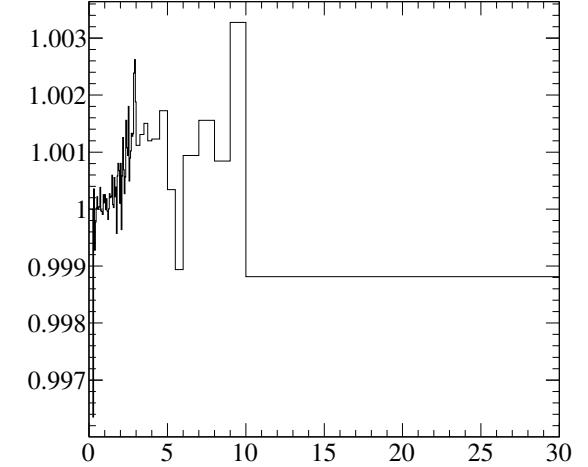


Figure 438: Ratio of SuperK MC E_{reco} spectra, for mode ν_μ CC other (ν_μ disap) made with 84 bin E_{true} and 780 bin E_{true} , for an exposure of $3.010 \text{imes} 10^{20}$ POT. The number of events was calculated using the BANFF-tuned MC templates. Using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5 \text{e-}05 \text{ eV}^2/c^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/c^4$.

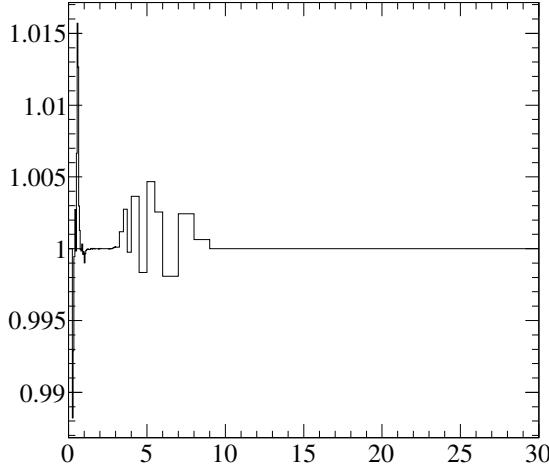


Figure 439: Ratio of SuperK MC E_{reco} spectra, for mode $\bar{\nu}_\mu$ CCQE made with 84 bin E_{true} and 780 bin E_{true} , for an exposure of 3.010×10^{20} POT. The number of events was calculated using the BANFF-tuned MC templates. Using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5 \times 10^{-5} \text{ eV}^2/c^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/c^4$.

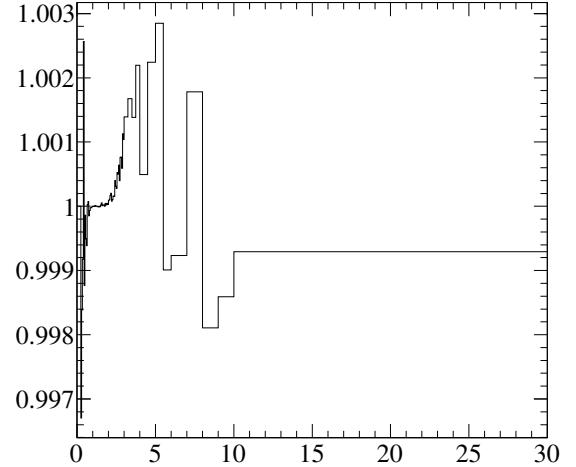


Figure 440: Ratio of SuperK MC E_{reco} spectra, for mode $\bar{\nu}_\mu$ CC 1π made with 84 bin E_{true} and 780 bin E_{true} , for an exposure of 3.010×10^{20} POT. The number of events was calculated using the BANFF-tuned MC templates. Using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5 \times 10^{-5} \text{ eV}^2/c^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/c^4$.

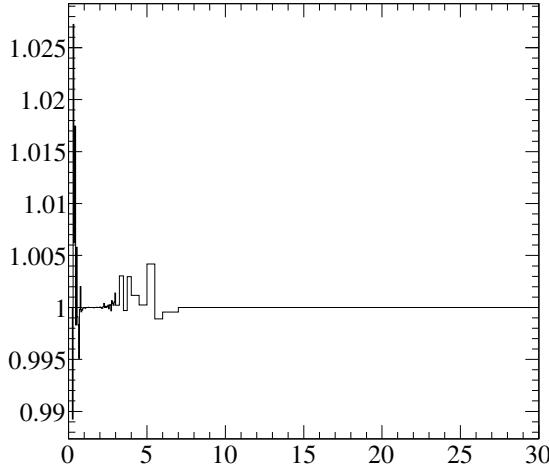


Figure 441: Ratio of SuperK MC E_{reco} spectra, for mode $\bar{\nu}_\mu$ CC coherent made with 84 bin E_{true} and 780 bin E_{true} , for an exposure of 3.010×10^{20} POT. The number of events was calculated using the BANFF-tuned MC templates. Using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5 \times 10^{-5} \text{ eV}^2/c^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/c^4$.

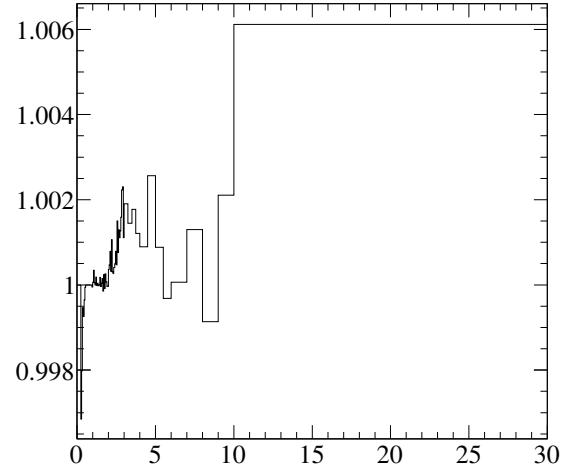


Figure 442: Ratio of SuperK MC E_{reco} spectra, for mode $\bar{\nu}_\mu$ CC other (ν_μ disap) made with 84 bin E_{true} and 780 bin E_{true} , for an exposure of 3.010×10^{20} POT. The number of events was calculated using the BANFF-tuned MC templates. Using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5 \times 10^{-5} \text{ eV}^2/c^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/c^4$.

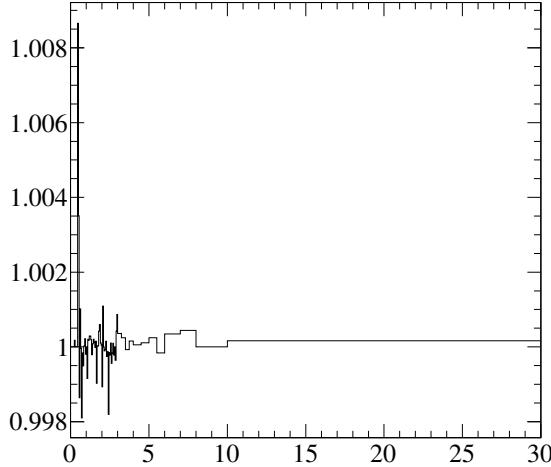


Figure 443: Ratio of SuperK MC E_{reco} spectra, for mode ν_e CCQE made with 84 bin E_{true} and 780 bin E_{true} , for an exposure of $3.010imes10^{20}$ POT. The number of events was calculated using the BANFF-tuned MC templates. Using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5e-05 \text{ eV}^2/c^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/c^4$.

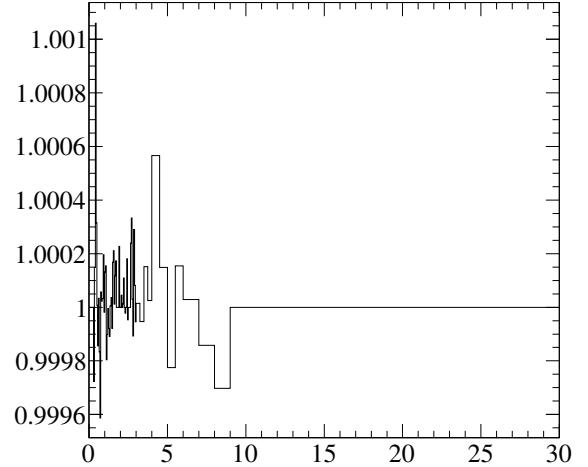


Figure 444: Ratio of SuperK MC E_{reco} spectra, for mode ν_e CC 1π made with 84 bin E_{true} and 780 bin E_{true} , for an exposure of $3.010imes10^{20}$ POT. The number of events was calculated using the BANFF-tuned MC templates. Using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5e-05 \text{ eV}^2/c^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/c^4$.

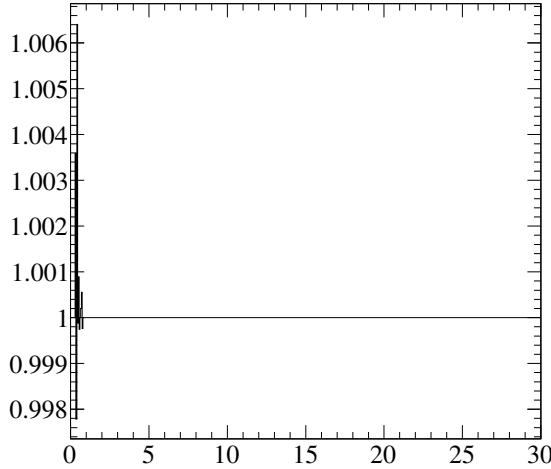


Figure 445: Ratio of SuperK MC E_{reco} spectra, for mode ν_e CC coherent made with 84 bin E_{true} and 780 bin E_{true} , for an exposure of $3.010imes10^{20}$ POT. The number of events was calculated using the BANFF-tuned MC templates. Using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5e-05 \text{ eV}^2/c^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/c^4$.

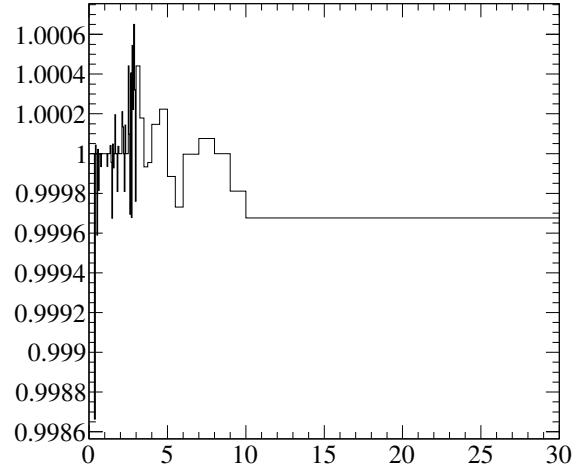


Figure 446: Ratio of SuperK MC E_{reco} spectra, for mode ν_e CC other (ν_μ disap) made with 84 bin E_{true} and 780 bin E_{true} , for an exposure of $3.010imes10^{20}$ POT. The number of events was calculated using the BANFF-tuned MC templates. Using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5e-05 \text{ eV}^2/c^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/c^4$.

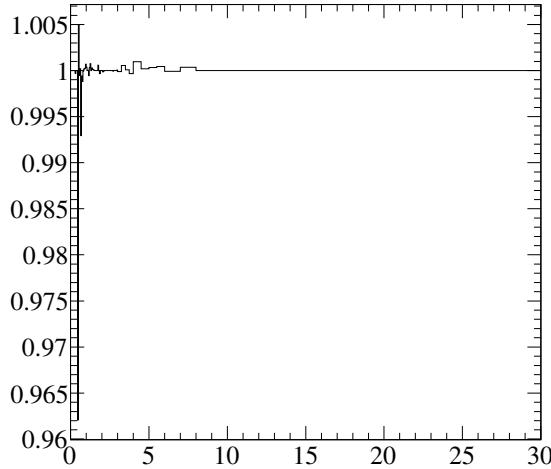


Figure 447: Ratio of SuperK MC E_{reco} spectra, for mode $\bar{\nu}_e$ CCQE made with 84 bin E_{true} and 780 bin E_{true} , for an exposure of $3.010imes10^{20}$ POT. The number of events was calculated using the BANFF-tuned MC templates. Using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5e-05 \text{ eV}^2/c^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/c^4$.

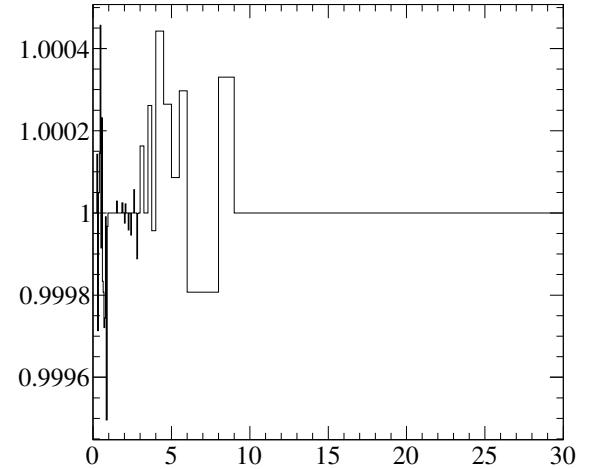


Figure 448: Ratio of SuperK MC E_{reco} spectra, for mode $\bar{\nu}_e$ CC 1π made with 84 bin E_{true} and 780 bin E_{true} , for an exposure of $3.010imes10^{20}$ POT. The number of events was calculated using the BANFF-tuned MC templates. Using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5e-05 \text{ eV}^2/c^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/c^4$.

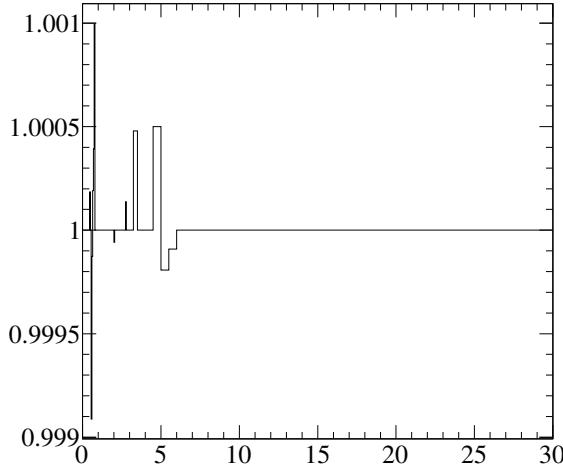


Figure 449: Ratio of SuperK MC E_{reco} spectra, for mode $\bar{\nu}_e$ CC coherent made with 84 bin E_{true} and 780 bin E_{true} , for an exposure of $3.010imes10^{20}$ POT. The number of events was calculated using the BANFF-tuned MC templates. Using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5e-05 \text{ eV}^2/c^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/c^4$.

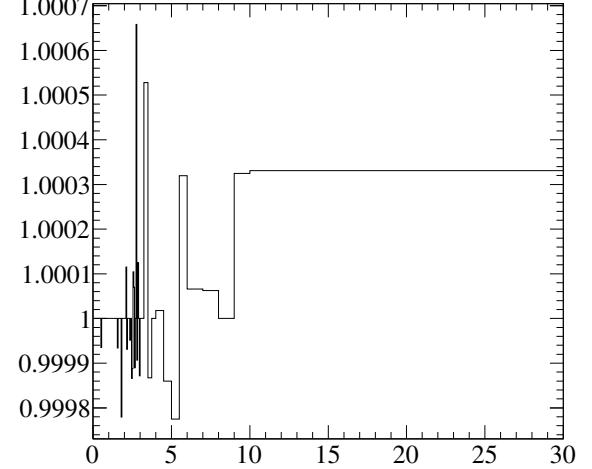


Figure 450: Ratio of SuperK MC E_{reco} spectra, for mode $\bar{\nu}_e$ CC other (ν_μ disap) made with 84 bin E_{true} and 780 bin E_{true} , for an exposure of $3.010imes10^{20}$ POT. The number of events was calculated using the BANFF-tuned MC templates. Using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5e-05 \text{ eV}^2/c^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/c^4$.

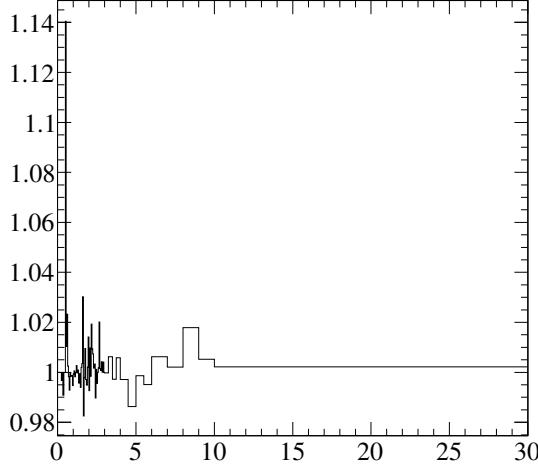


Figure 451: Ratio of SuperK MC E_{reco} spectra, for mode oscillation ν_e CCQE made with 84 bin E_{true} and 780 bin E_{true} , for an exposure of 3.010×10^{20} POT. The number of events was calculated using the BANFF-tuned MC templates. Using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5 \times 10^{-5} \text{ eV}^2/\text{c}^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/\text{c}^4$.

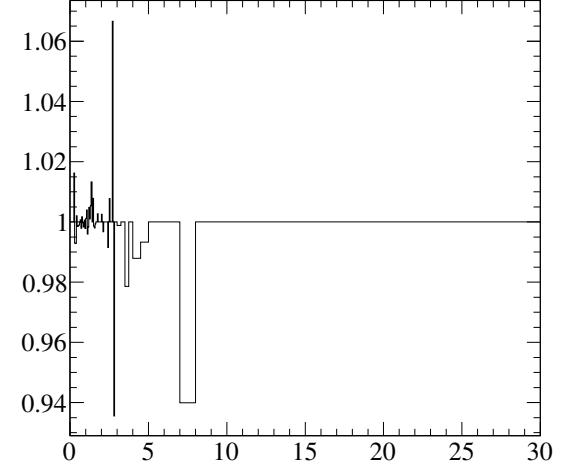


Figure 452: Ratio of SuperK MC E_{reco} spectra, for mode oscillation ν_e CC 1π made with 84 bin E_{true} and 780 bin E_{true} , for an exposure of 3.010×10^{20} POT. The number of events was calculated using the BANFF-tuned MC templates. Using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5 \times 10^{-5} \text{ eV}^2/\text{c}^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/\text{c}^4$.

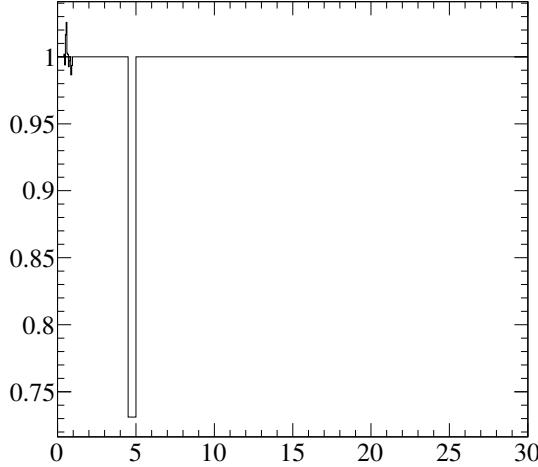


Figure 453: Ratio of SuperK MC E_{reco} spectra, for mode oscillation ν_e CC coherent made with 84 bin E_{true} and 780 bin E_{true} , for an exposure of 3.010×10^{20} POT. The number of events was calculated using the BANFF-tuned MC templates. Using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5 \times 10^{-5} \text{ eV}^2/\text{c}^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/\text{c}^4$.

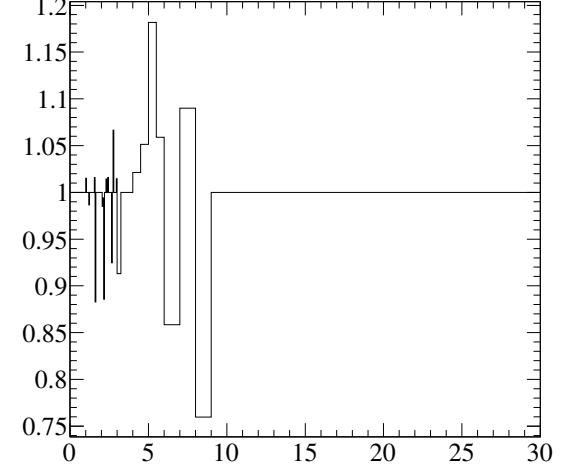


Figure 454: Ratio of SuperK MC E_{reco} spectra, for mode oscillation ν_e CC other (ν_μ app) made with 84 bin E_{true} and 780 bin E_{true} , for an exposure of 3.010×10^{20} POT. The number of events was calculated using the BANFF-tuned MC templates. Using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5 \times 10^{-5} \text{ eV}^2/\text{c}^4$; $\Delta m_{32}^2 = 0.0024 \text{ eV}^2/\text{c}^4$.

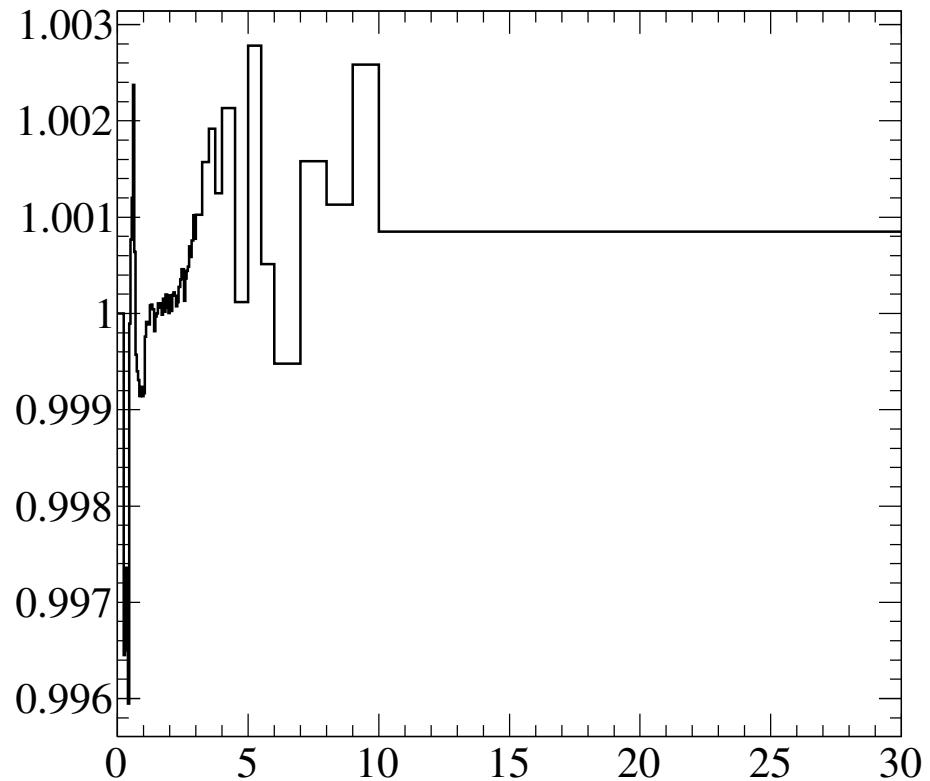


Figure 455: Ratio of total SuperK MC E_{reco} spectra, made with 84-bin E_{true} and 780-bin E_{true} , for an exposure of 3.010×10^{20} POT. The number of events was calculated using the BANFF-tuned MC templates. Using oscillation parameters: $\sin^2 2\theta_{12} = 0.857$; $\sin^2 2\theta_{13} = 0.098$; $\sin^2 2\theta_{23} = 1$; $\delta_{CP} = 0$; $\Delta m_{21}^2 = 7.5 \text{e-}05 \text{ eV}^2/c^4$; $|\Delta m_{32}^2| = 0.0024 \text{ eV}^2/c^4$.

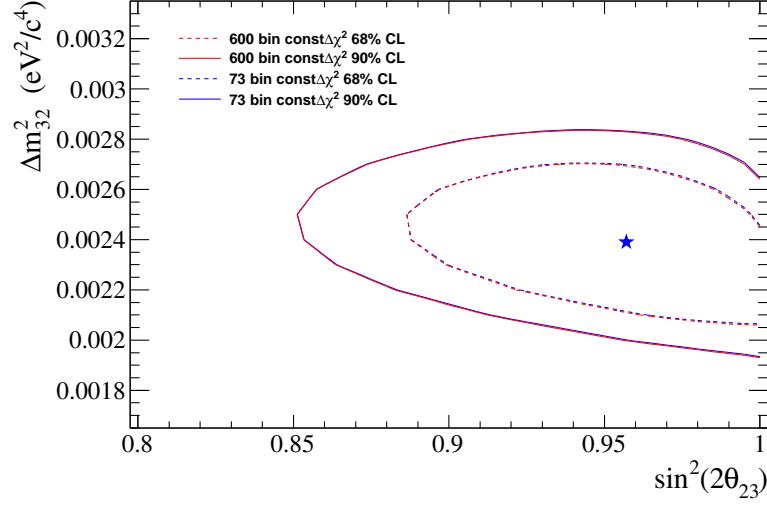


Figure 456: Sensitivity study using the 2+8 constant $\Delta\chi^2$ method. The 68% and 90% CL contours are shown. The input point is $(\sin^2 2\theta_{23}, |\Delta m_{32}^2|) = (0.957, 0.00239 \text{ eV}^2/\text{c}^4)$. The sensitivity has been calculated for both the *normal* 73 E_{reco} binning, as well as for 600 50 MeV bins from 0 - 30 GeV.

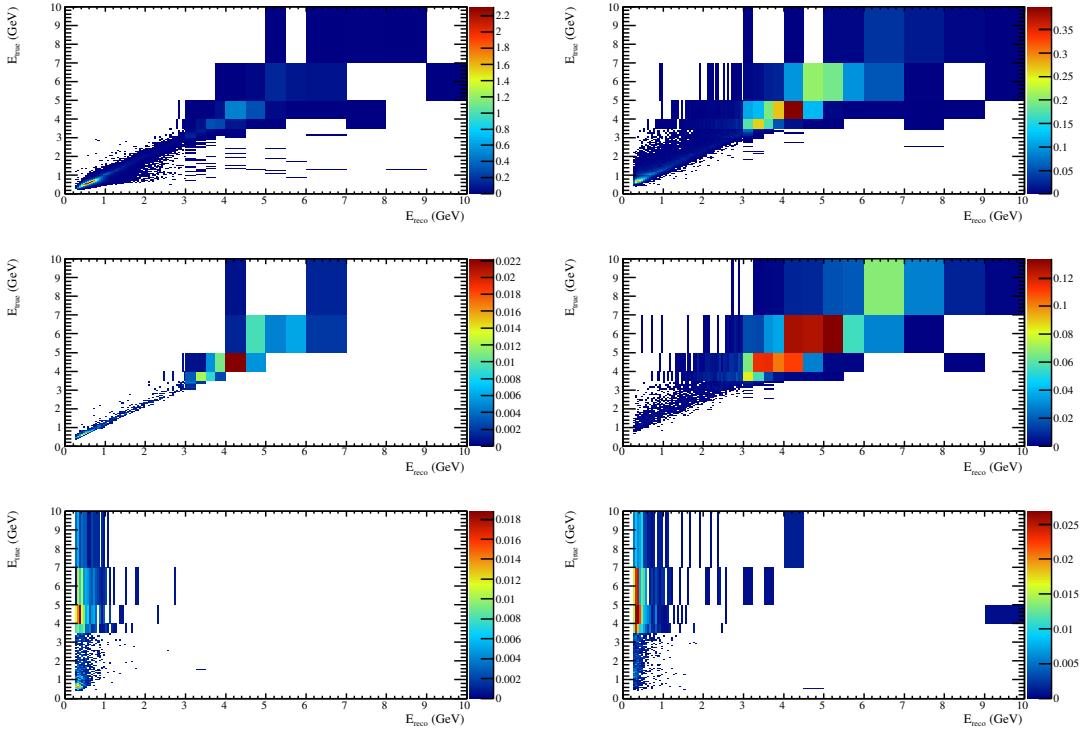


Figure 457: Nominal (E_t , E_r) 1-ring μ -like MC templates. The templates are shown for ν_μ CCQE (1) ν_μ CC $1\pi^-$ (2), ν_μ CC coherent (3), ν_μ CC other (4), ν_μ NC $1\pi^\pm$ (5), ν_μ NC other (6).

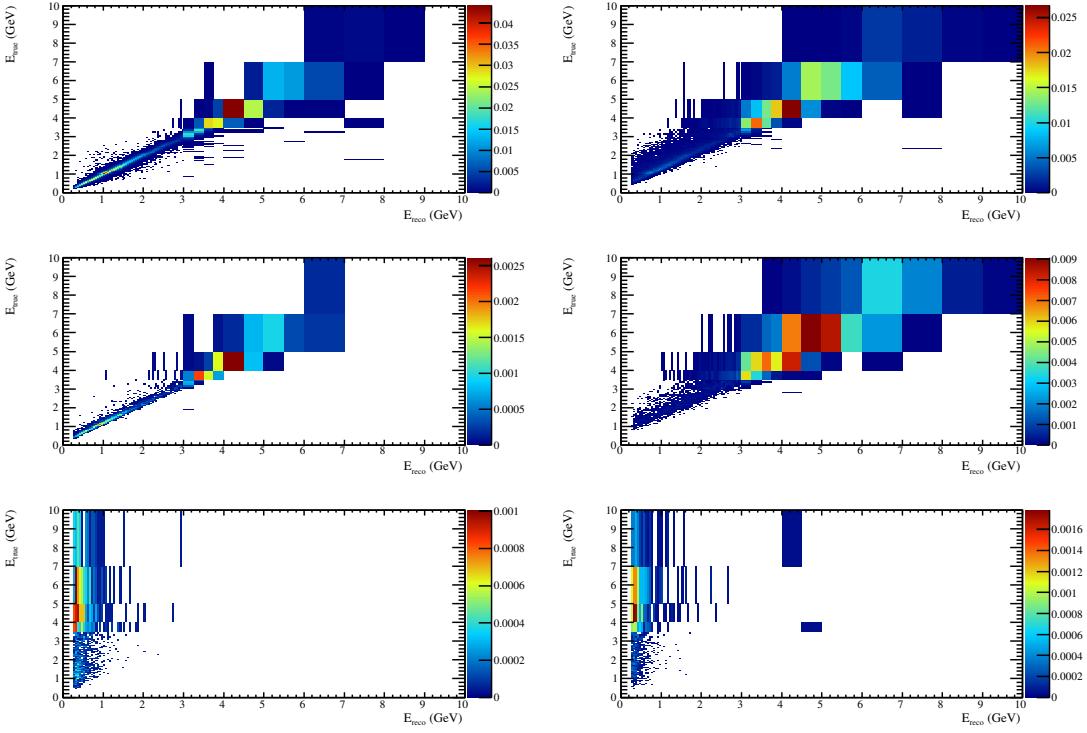


Figure 458: Nominal (E_t, E_r) 1-ring μ -like MC templates. The templates are shown for $\bar{\nu}_\mu$ CCQE (7), $\bar{\nu}_\mu$ CC1 π (8), $\bar{\nu}_\mu$ CC coherent (9), $\bar{\nu}_\mu$ CC other (10), $\bar{\nu}_\mu$ NC1 π^\pm (11), $\bar{\nu}_\mu$ NC other (12).

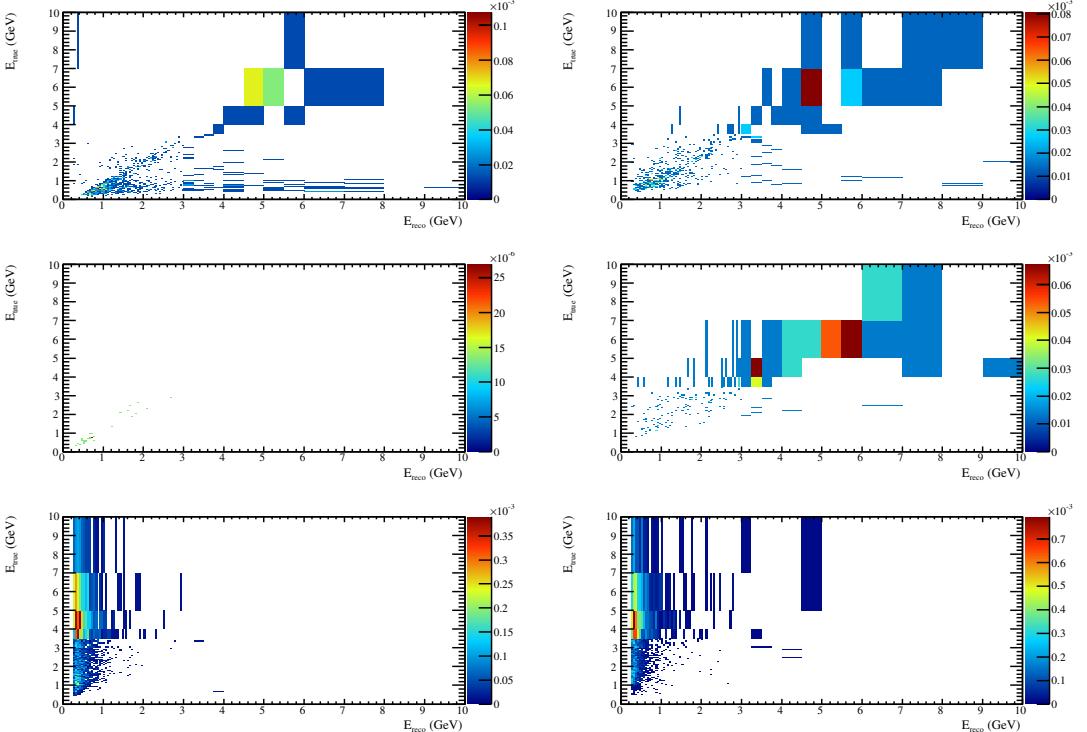


Figure 459: Nominal (E_t, E_r) 1-ring μ -like MC templates. The templates are shown for ν_e CCQE (13), ν_e CC1 π (14), ν_e CC coherent (15), ν_e CC other (16), ν_e NC1 π^\pm (17), ν_e NC other (18).

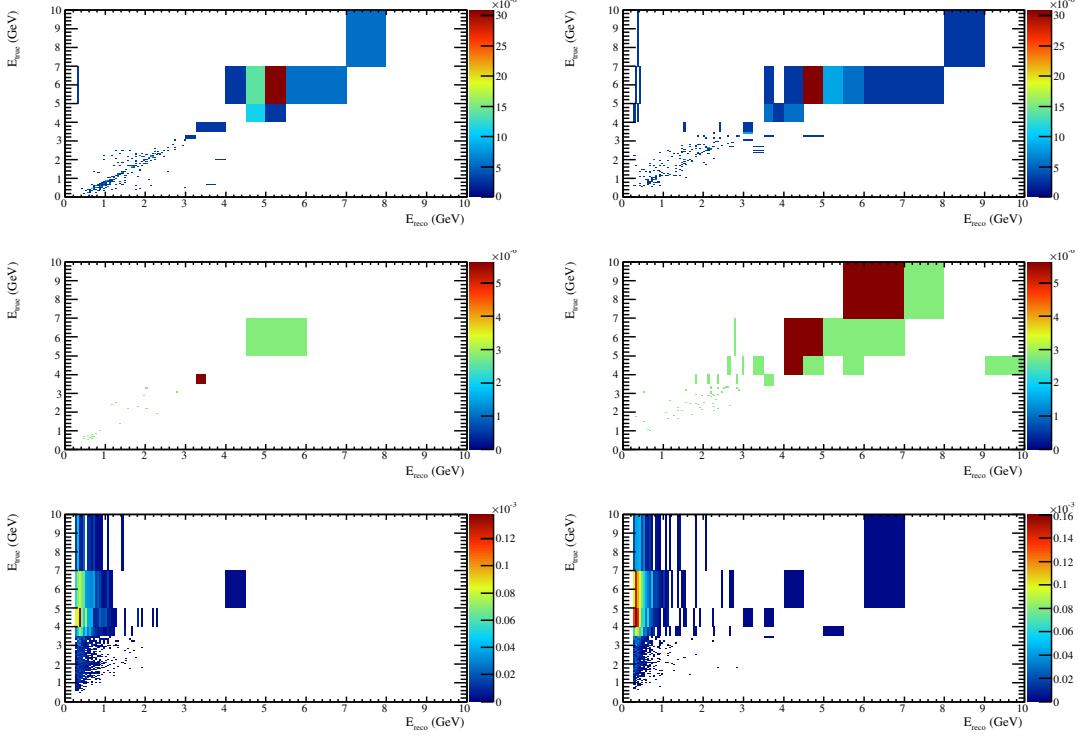


Figure 460: Nominal (E_t, E_r) 1-ring μ -like MC templates. The templates are shown for $\bar{\nu}_e$ CCQE (19), $\bar{\nu}_e$ CC1 π (20), $\bar{\nu}_e$ CC coherent (21), $\bar{\nu}_e$ CC other (22), $\bar{\nu}_e$ NC1 π^\pm (23), $\bar{\nu}_e$ NC other (24).

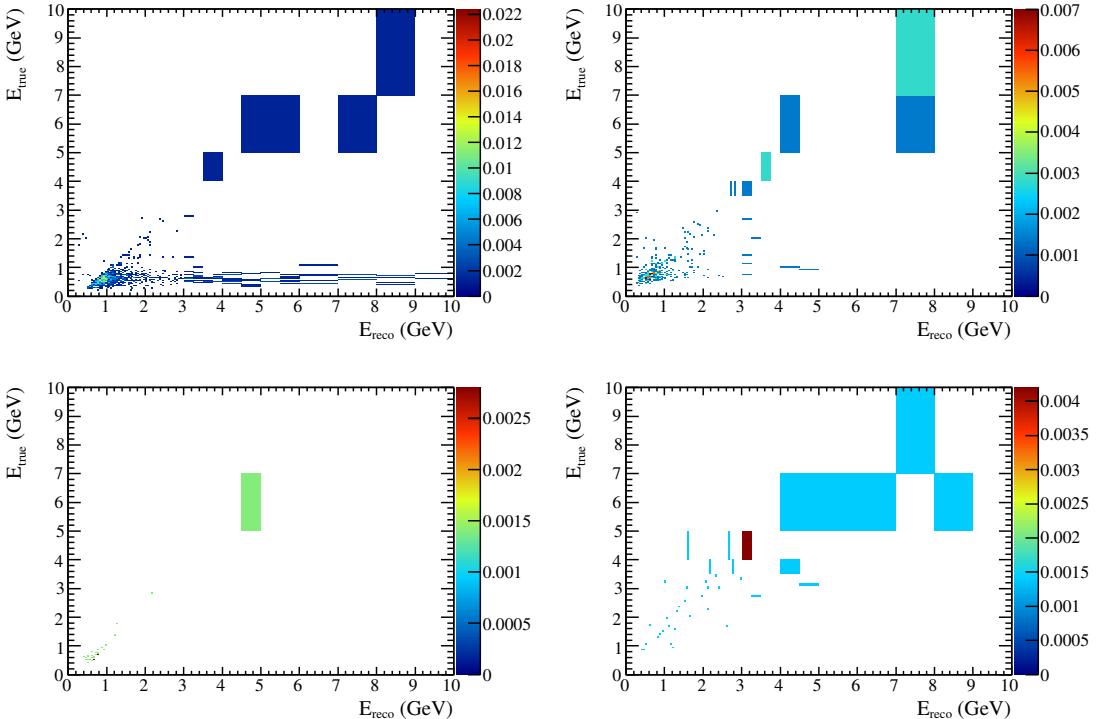


Figure 461: Nominal (E_t, E_r) 1-ring μ -like MC templates. The templates are shown for osc. ν_e CCQE (25), osc. ν_e CC1 π (26), osc. ν_e CC coherent (27) and osc. ν_e CC other (28).

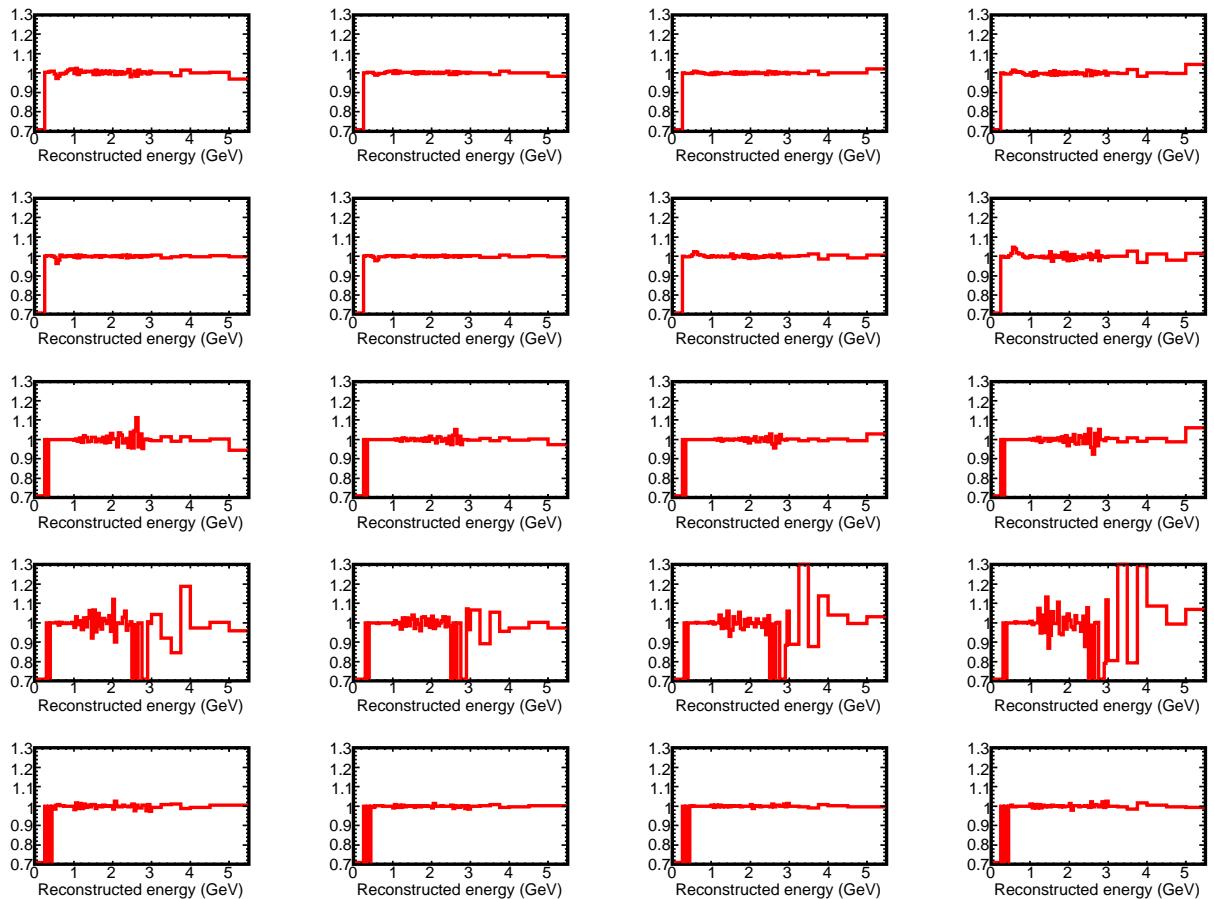


Figure 462: Ratios of non-oscillated tweaked total SuperK MC E_{reco} spectra made with the cross-section splines to those made with event-by-event reweighting for MaQE. Each row represents one neutrino species, and these are ν_μ , $\bar{\nu}_\mu$, ν_e and $\bar{\nu}_e$ and oscillated ν_e in that order. Each column represents a tweak value, and these are -2σ , -1σ , $+1\sigma$ and $+2\sigma$ in that order. Both the spline spectra and the event-by-event spectra are made with the 73-bin scheme given in Sec. 2.2.5.

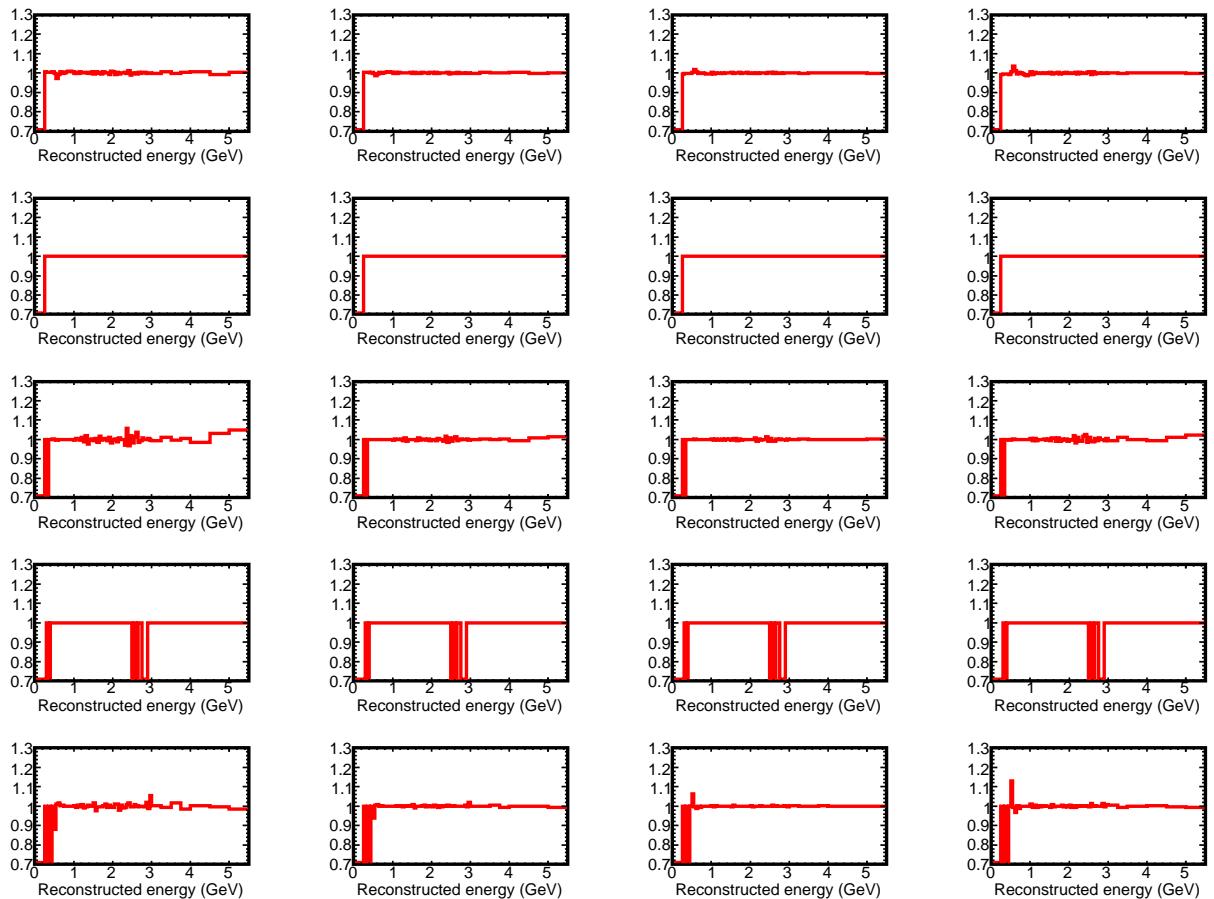


Figure 463: Ratios of non-oscillated tweaked total SuperK MC E_{reco} spectra made with the cross-section splines to those made with event-by-event reweighting for the Fermi momentum. Each row represents one neutrino species, and these are ν_μ , $\bar{\nu}_\mu$, ν_e and $\bar{\nu}_e$ and oscillated ν_e in that order. Each column represents a tweak value, and these are -2σ , -1σ , $+1\sigma$ and $+2\sigma$ in that order. Both the spline spectra and the event-by-event spectra are made with the 73-bin scheme given in Sec. 2.2.5.

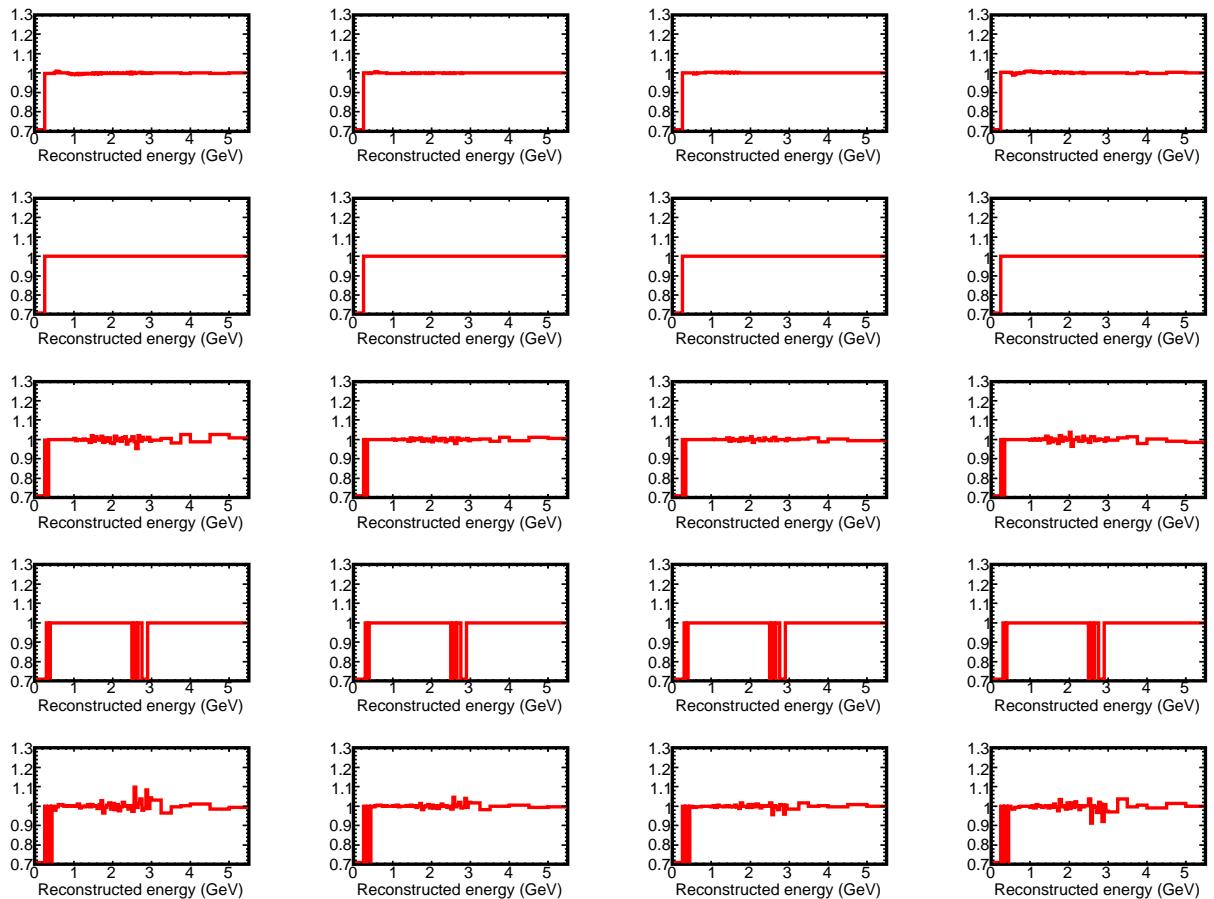


Figure 464: Ratios of non-oscillated tweaked total SuperK MC E_{reco} spectra made with the cross-section splines to those made with event-by-event reweighting for the binding energy. Each row represents one neutrino species, and these are ν_μ , $\bar{\nu}_\mu$, ν_e and $\bar{\nu}_e$ and oscillated ν_e in that order. Each column represents a tweak value, and these are -2σ , -1σ , $+1\sigma$ and $+2\sigma$ in that order. Both the spline spectra and the event-by-event spectra are made with the 73-bin scheme given in Sec. 2.2.5.

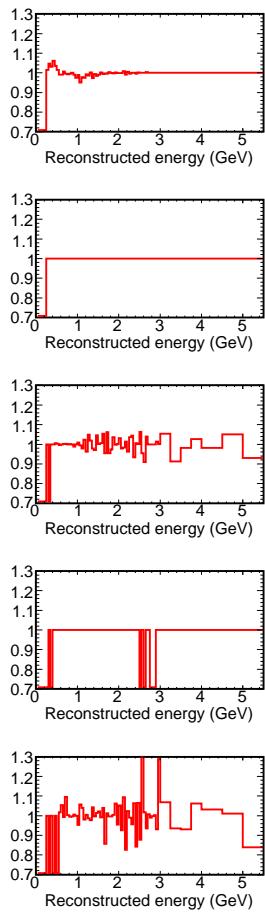


Figure 465: Ratios of non-oscillated tweaked total SuperK MC E_{reco} spectra made with the cross-section splines to those made with event-by-event reweighting for the spectral function. Each histogram represents one neutrino species, and these are ν_μ , $\bar{\nu}_\mu$, ν_e and $\bar{\nu}_e$ in that order. Both the spline spectra and the event-by-event spectra are made with the 73-bin scheme given in Sec. 2.2.5.

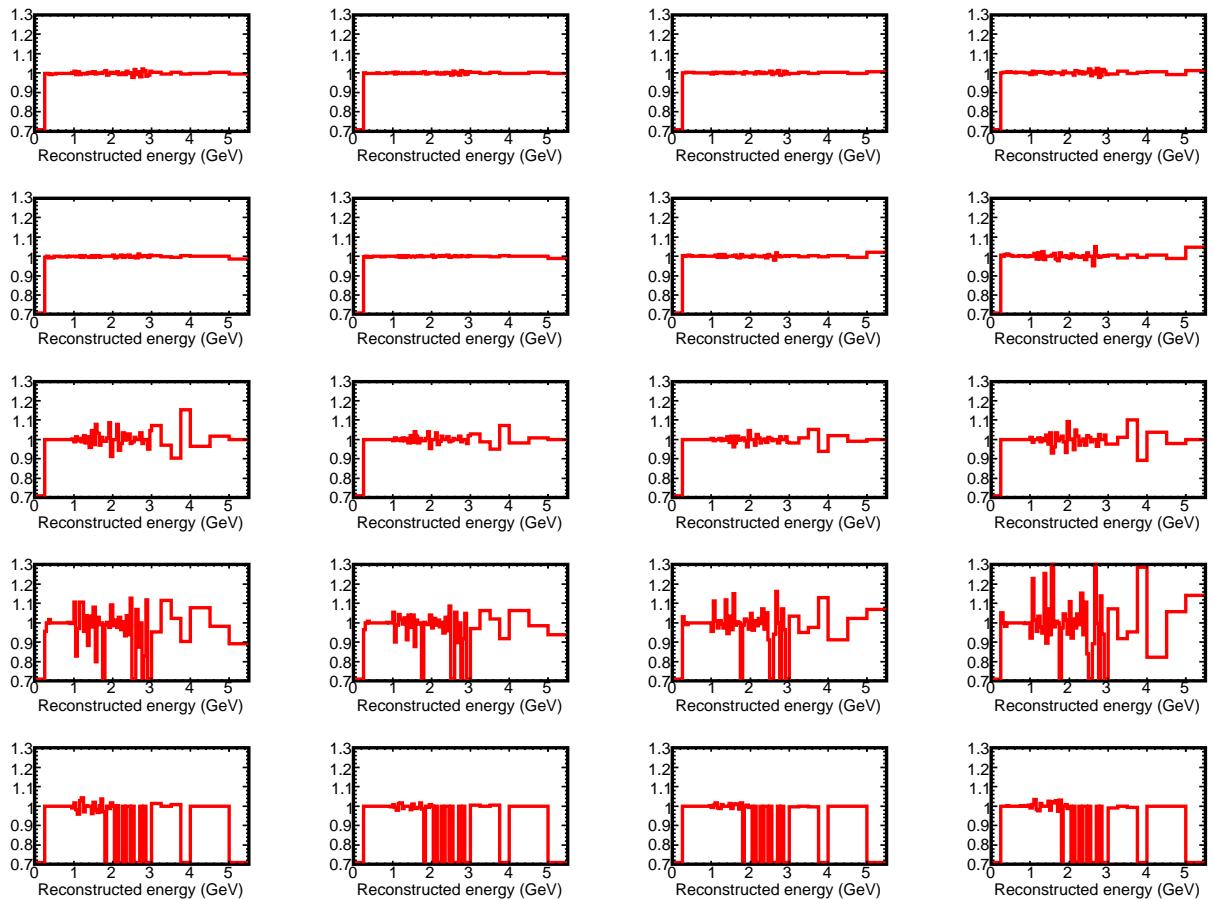


Figure 466: Ratios of non-oscillated tweaked total SuperK MC E_{reco} spectra made with the cross-section splines to those made with event-by-event reweighting for MaRes for CC1 π interactions. Each row represents one neutrino species, and these are ν_μ , $\bar{\nu}_\mu$, ν_e and $\bar{\nu}_e$ in that order. Each column represents a tweak value, and these are -2σ , -1σ , $+1\sigma$ and $+2\sigma$ in that order. Both the spline spectra and the event-by-event spectra are made with the 73-bin scheme given in Sec. 2.2.5.

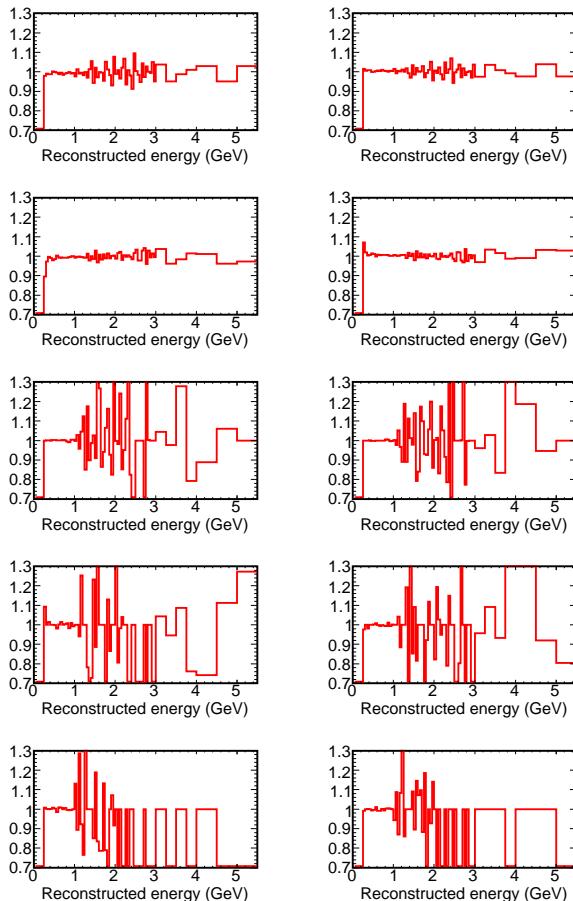


Figure 467: Ratios of non-oscillated tweaked total SuperK MC E_{reco} spectra made with the cross-section splines to those made with event-by-event reweighting for the pileless delta systematic for CC1 π interactions. Each row represents one neutrino species, and these are ν_μ , $\bar{\nu}_\mu$, ν_e and $\bar{\nu}_e$ and oscillated ν_e in that order. Each column represents a tweak value, and these are -1σ , and $+1\sigma$ in that order. Both the spline spectra and the event-by-event spectra are made with the 73-bin scheme given in Sec. 2.2.5.

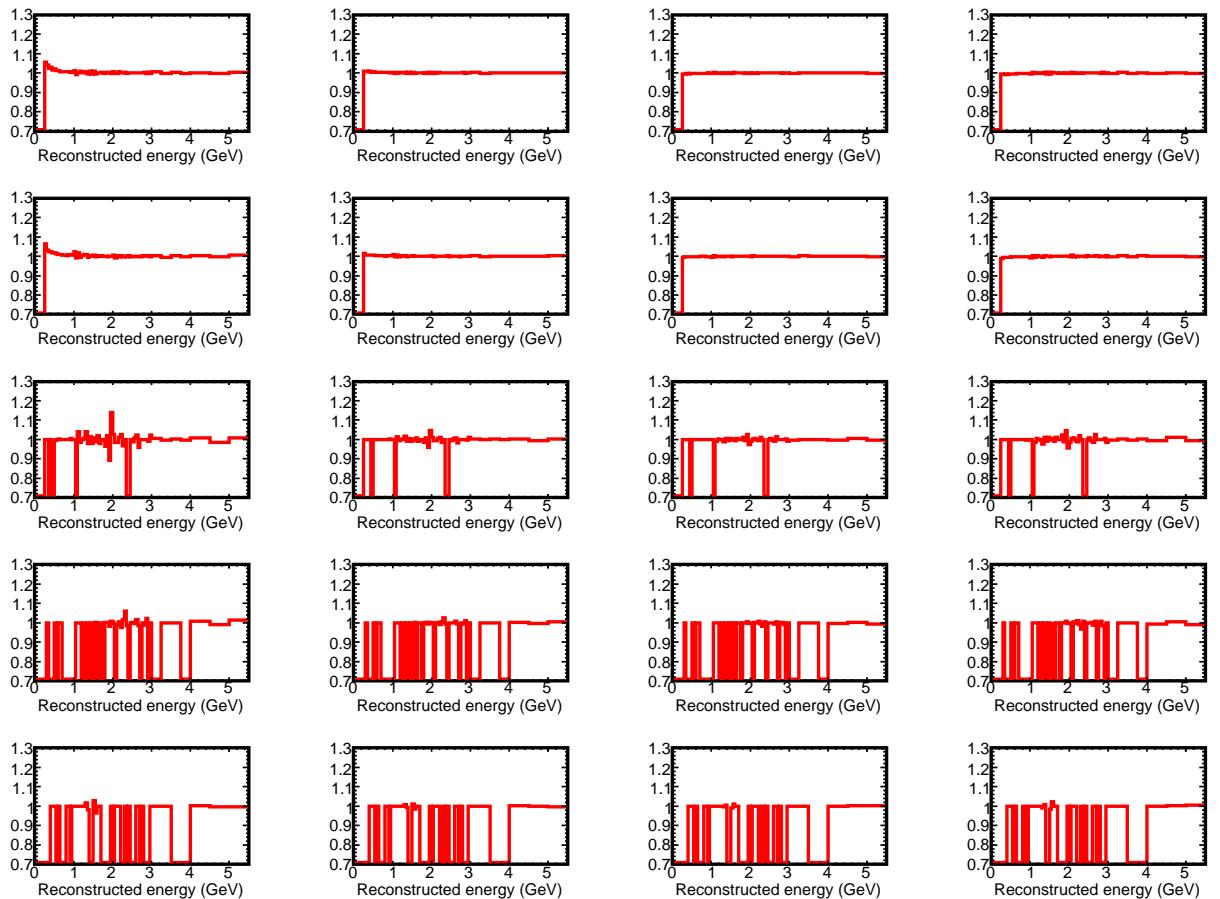


Figure 468: Ratios of non-oscillated tweaked total SuperK MC E_{reco} spectra made with the cross-section splines to those made with event-by-event reweighting for the CC other shape systematic. Each row represents one neutrino species, and these are ν_μ , $\bar{\nu}_\mu$, ν_e and $\bar{\nu}_e$ in that order. Each column represents a tweak value, and these are -2σ , -1σ , $+1\sigma$ and $+2\sigma$ in that order. Both the spline spectra and the event-by-event spectra are made with the 73-bin scheme given in Sec. 2.2.5.

1469 **J. 2-flavour results**

1470 ‘2+N’ ν_μ -disappearance fits were performed on the combined 3.010×10^{20} POT Run 1+2+3 dataset using the
1471 method described in section 4 and the 2-flavour approximation for the oscillation probabilities. This analysis found
1472 $|\Delta m_{32}^2| = 2.475 \times 10^{-3} \text{ eV}^2/c^4$ and $\sin^2 2\theta_{23} = 1.000$ to be the best-fit values. At the best-fit point, N_{exp} is 57.87 and
1473 $\chi^2_{bf}/ndf = 56.03/71$.

1474 The pulls, defined in Eq. 9, of all 48 systematic parameters allowed to float in the fit are shown in Fig. 469. From
1475 this figure, it is apparent that most systematic parameters barely move from their nominal values.

1476 The reconstructed neutrino energy distribution of the single μ -like ring events in the Run 1+2+3 dataset is shown in
1477 Fig. 470 along with the ‘2+N’ 2-flavour best-fit prediction and the prediction made under the no-oscillation hypothesis.
1478 Also shown is the ratio between the data and the no-oscillation spectrum and the ratio between the ‘2+N’ 2-flavour
1479 best-fit spectrum and the no-oscillation spectrum; in both of these ratios, the characteristic energy-dependent deficit
1480 can be clearly seen. These distributions are shown in the 73-bin scheme in reconstructed neutrino energy that was used
1481 in the fitting procedure (see Sec. 2.2.5). Fig. 471 shows the same distributions in the coarse binning scheme (see Sec.
1482 5.3).

1483 The $\Delta\chi^2$ surface for the the ‘2+N’ 2-flavour fit to the Run 1+2+3 dataset is shown in Fig. 472, as a function of
1484 $\sin^2 2\theta_{23}$ and $|\Delta m_{32}^2|$.

1485 The 68% and 90% CL regions for the ‘2+N’ 2-flavour fit to the Run 1+2+3 dataset are shown using the constant-
1486 $\Delta\chi^2$ method in Fig. 473.

1487 A comparison is shown in Fig. 474 between 90% C. L. constant- $\Delta\chi^2$ method contours for the 2-flavour fit and
1488 3-flavour fits assuming θ_{23} to be in the first and second octants.

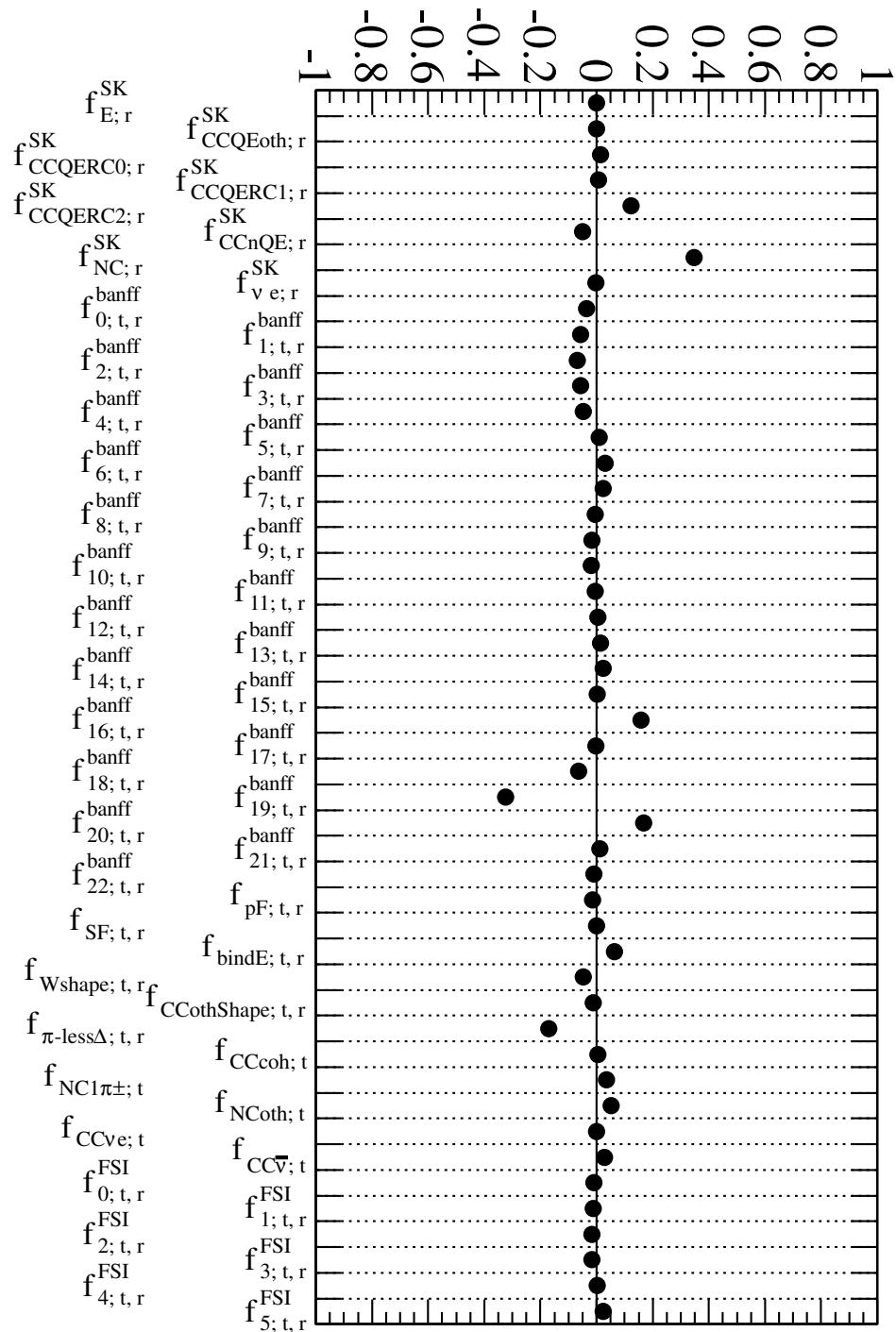


Figure 469: Systematic parameter pulls for the '2+N' 2-flavour fit to the Run 1+2+3 dataset.

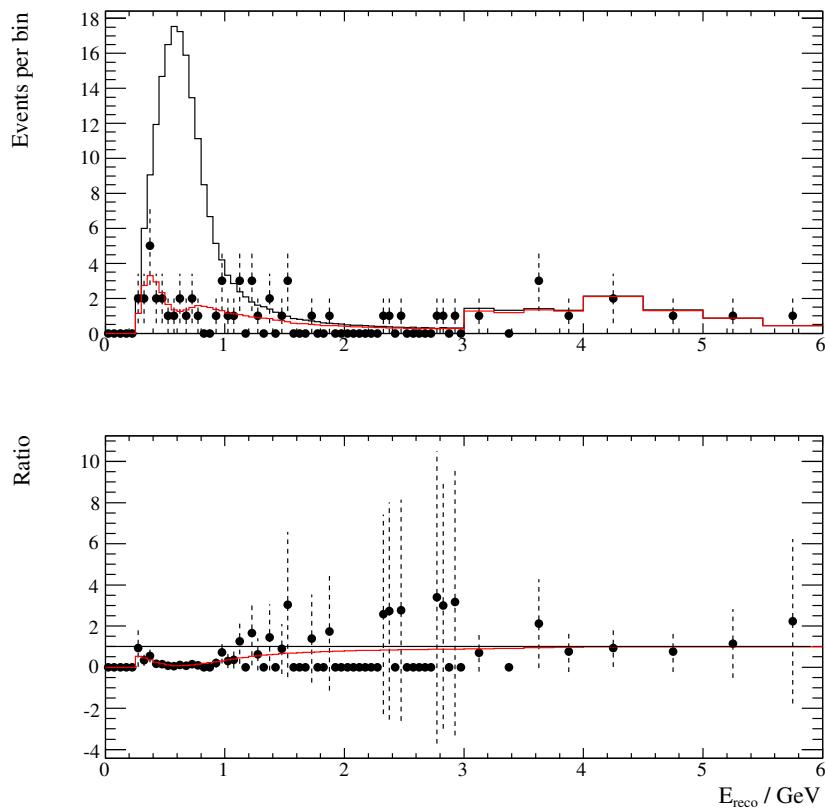


Figure 470: Best-fit reconstructed energy spectrum (top) obtained from the ‘2+N’ 2-flavour fit to the combined Run 1+2+3 dataset. The Run 1+2+3 dataset and the prediction obtained from the no-oscillation hypothesis are also shown. The spectra are shown using the 73 bins used in the fit (see Sec. 2.2.5). The ratio of the data and best-fit distribution to the no-oscillation hypothesis is shown in the bottom plot. The characteristic energy-dependent deficit can be clearly seen.

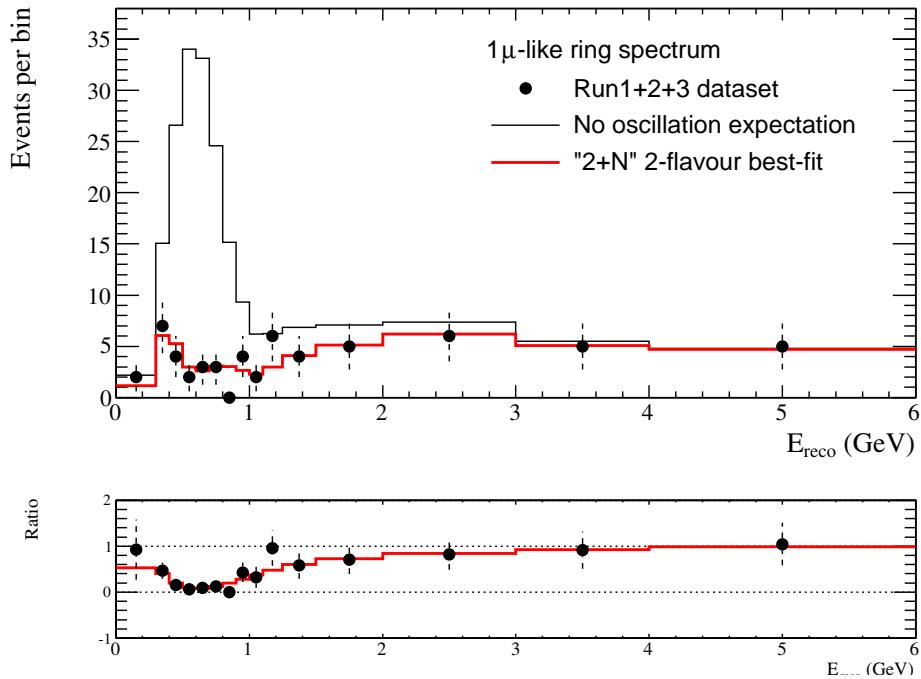


Figure 471: Best-fit reconstructed energy spectrum using the coarse binning scheme (see Sec. 5.3) obtained from the ‘2+N’ 2-flavour fit to the Run 1+2+3 dataset. Also shown are the spectrum obtained under the no-oscillation hypothesis and the ratios of the data and best-fit spectrum to it.

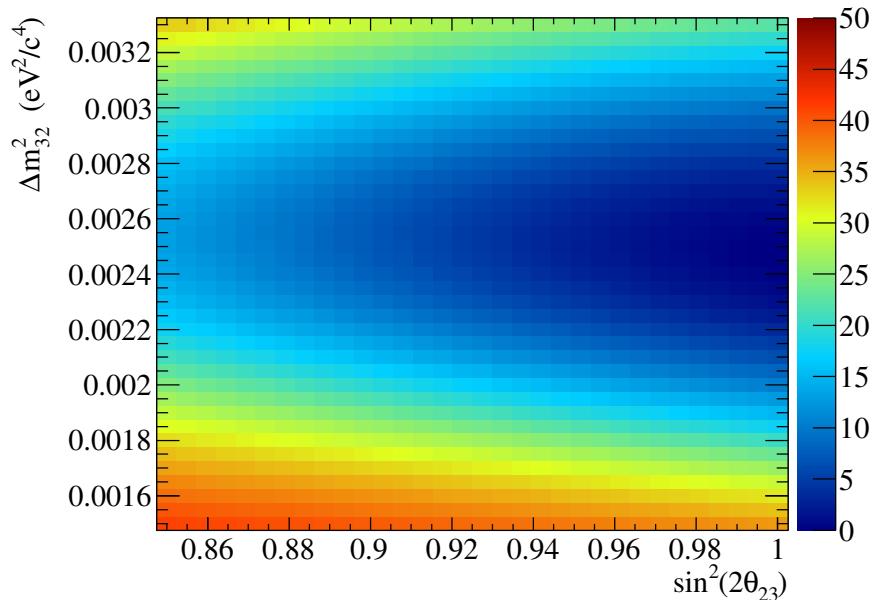


Figure 472: $\Delta\chi^2$ surface for the ‘2+N’ 2-flavour fit to the Run 1+2+3 dataset.

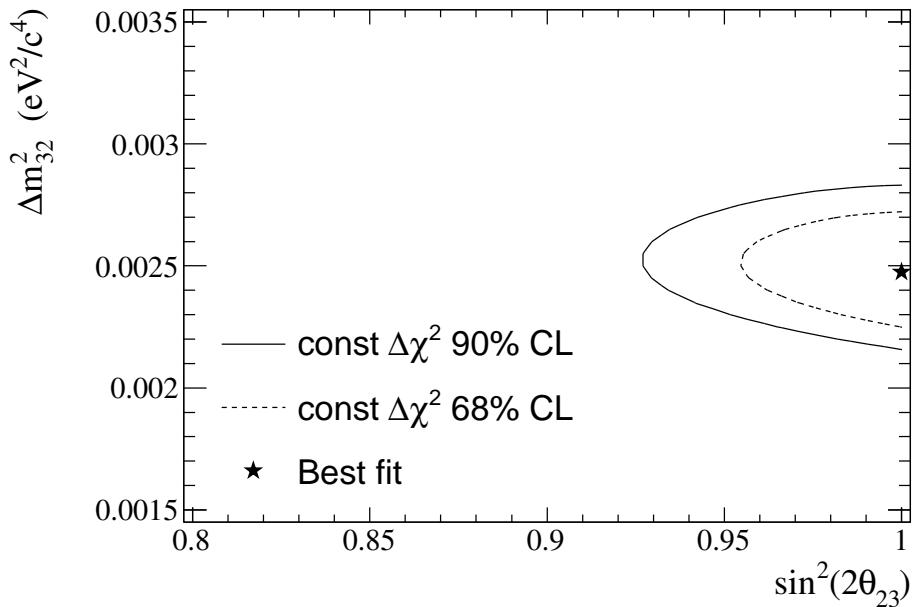


Figure 473: 68% CL and 90% CL allowed region (including systematics), constructed with the constant- $\Delta\chi^2$ method, for the ‘2+N’ 2-flavour fit to the Run 1+2+3 dataset. The ‘2+N’ best-fit point is also shown.

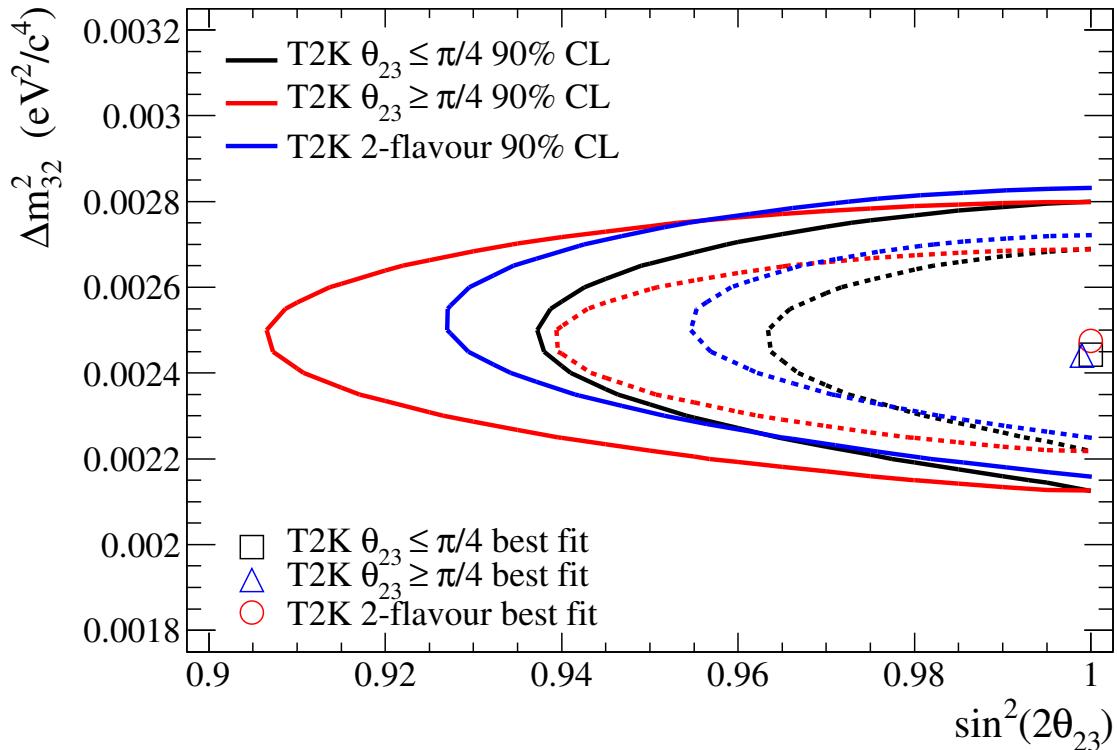


Figure 474: Comparison between the ‘2+N’ 68% CL and 90% CL allowed regions for 3-flavour fits with θ_{23} in the first and second octants, and the 2-flavour fit, obtained using the constant- $\Delta\chi^2$ method. The comparison is shown for the fits to the Run 1+2+3 dataset.

1489 **K. Results for $\sin^2 \theta_{23}$ and vacuum oscillation probabilities**

1490 ‘2+N’ 3-flavour ν_μ -disappearance fits were performed on the combined 3.010×10^{20} POT Run 1+2+3 dataset using
1491 the method described in section 4, $\sin^2 \theta_{23}$ instead of $\sin^2 2\theta_{23}$, and 3-flavour oscillation probabilities in vacuum
1492 instead of matter. This analysis found $|\Delta m_{32}^2| = 2.442 \times 10^{-3} \text{ eV}^2/c^4$ and $\sin^2 \theta_{23} = 0.513$ to be the best-fit values. At
1493 the best-fit point, N_{exp} is 57.90 and $\chi^2_{bf}/ndf = 56.03/71$.

1494 The pulls, defined in Eq. 9, of all 48 systematic parameters allowed to float in the fit are shown in Fig. 475. From
1495 this figure, it is apparent that most systematic parameters barely move from their nominal values.

1496 The reconstructed neutrino energy distribution of the single μ -like ring events in the Run 1+2+3 dataset is shown in
1497 Fig. 476 along with the ‘2+N’ $\sin^2 \theta_{23}$ in vacuum best-fit prediction and the prediction made under the no-oscillation
1498 hypothesis. Also shown is the ratio between the data and the no-oscillation spectrum and the ratio between the ‘2+N’
1499 $\sin^2 \theta_{23}$ in vacuum best-fit spectrum and the no-oscillation spectrum; in both of these ratios, the characteristic
1500 energy-dependent deficit can be clearly seen. These distributions are shown in the 73-bin scheme in reconstructed
1501 neutrino energy that was used in the fitting procedure (see Sec. 2.2.5). Fig. 477 shows the same distributions in the
1502 coarse binning scheme (see Sec. 5.3).

1503 The $\Delta\chi^2$ surface for the ‘2+N’ $\sin^2 \theta_{23}$ in vacuum fit to the Run 1+2+3 dataset is shown in Fig. 478, as a
1504 function of $\sin^2 \theta_{23}$ and $|\Delta m_{32}^2|$.

1505 The 68% and 90% CL regions for the ‘2+N’ $\sin^2 \theta_{23}$ in vacuum fit to the Run 1+2+3 dataset are shown using the
1506 constant- $\Delta\chi^2$ method in Fig. 479.

1507 A comparison between the $\sin^2 \theta_{23}$ contours assuming vacuum and matter using the constant- $\Delta\chi^2$ method is shown
1508 in Fig. 480.

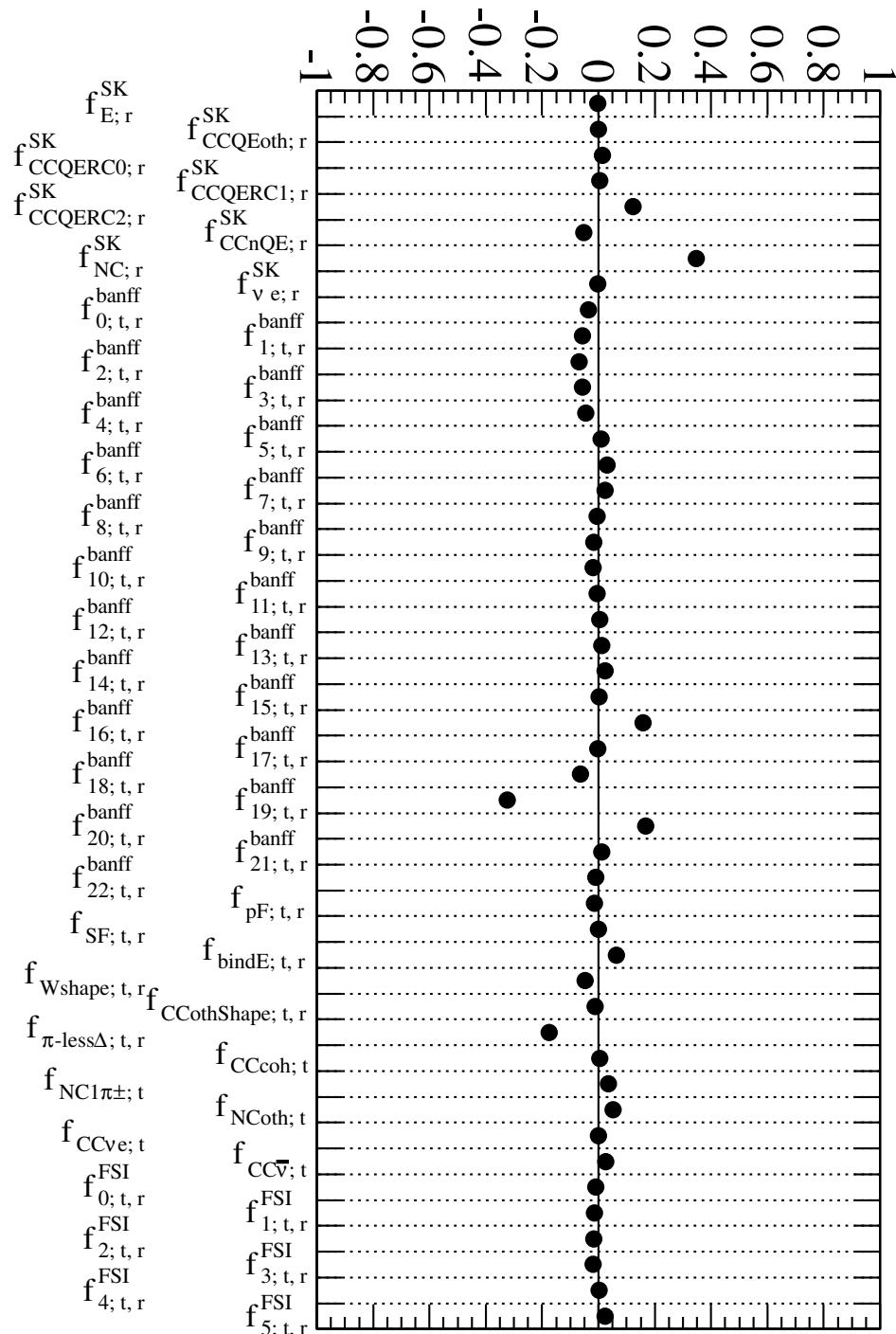


Figure 475: Systematic parameter pulls for the '2+N' $\sin^2 \theta_{23}$ in vacuum fit to the Run 1+2+3 dataset.

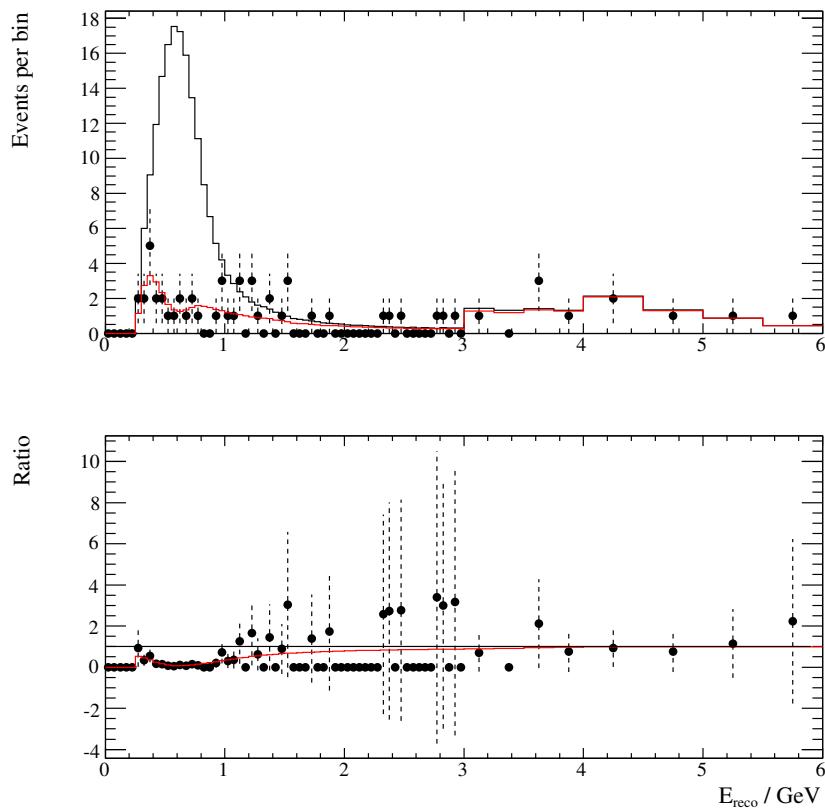


Figure 476: Best-fit reconstructed energy spectrum (top) obtained from the ‘2+N’ $\sin^2 \theta_{23}$ in vacuum fit to the combined Run 1+2+3 dataset. The Run 1+2+3 dataset and the prediction obtained from the no-oscillation hypothesis are also shown. The spectra are shown using the 73 bins used in the fit (see Sec. 2.2.5). The ratio of the data and best-fit distribution to the no-oscillation hypothesis is shown in the bottom plot. The characteristic energy-dependent deficit can be clearly seen.

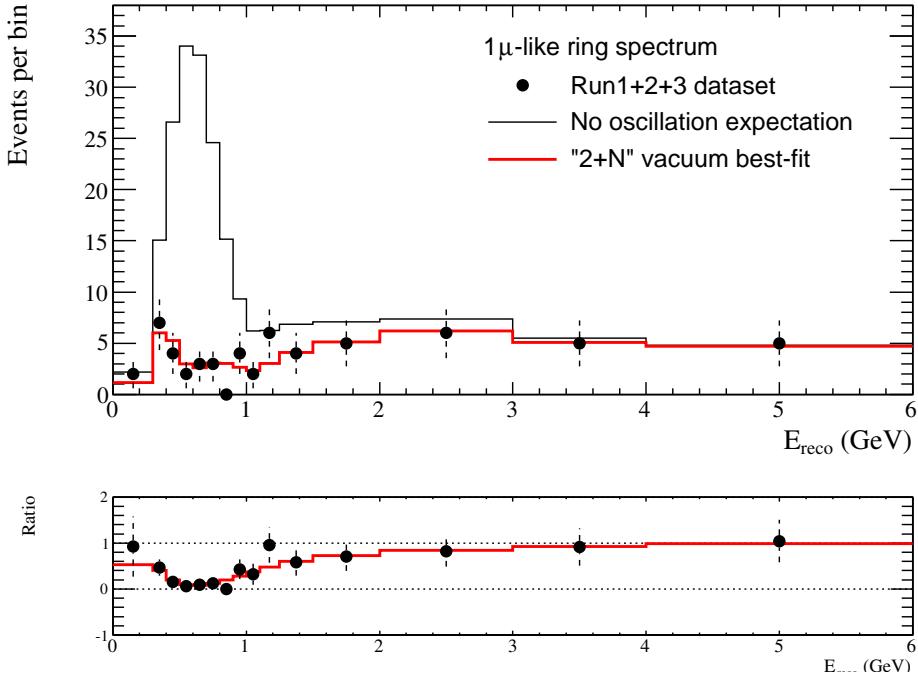


Figure 477: Best-fit reconstructed energy spectrum using the coarse binning scheme (see Sec. 5.3) obtained from the '2+N' $\sin^2 \theta_{23}$ in vacuum fit to the Run 1+2+3 dataset. Also shown are the spectrum obtained under the no-oscillation hypothesis and the ratios of the data and best-fit spectrum to it.

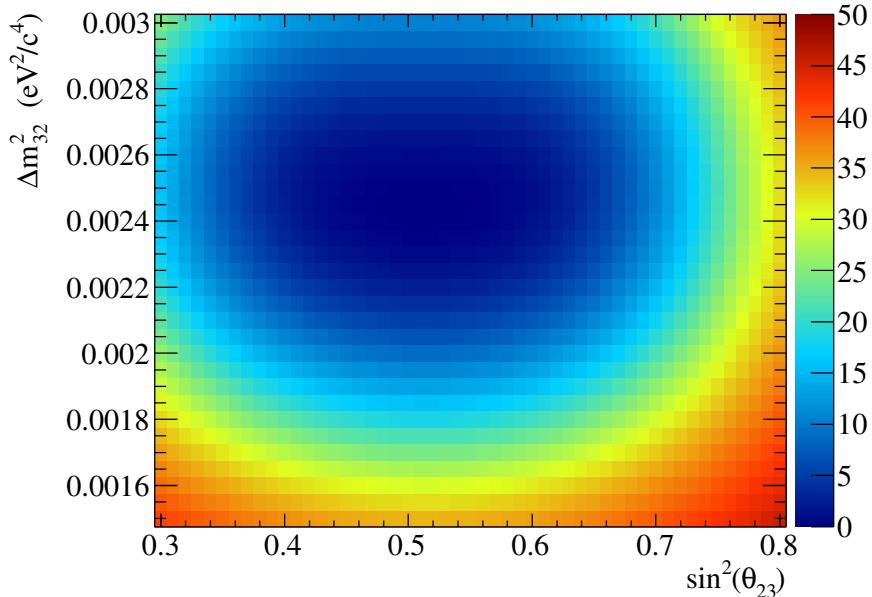


Figure 478: $\Delta\chi^2$ surface for the '2+N' $\sin^2 \theta_{23}$ in vacuum fit to the Run 1+2+3 dataset.

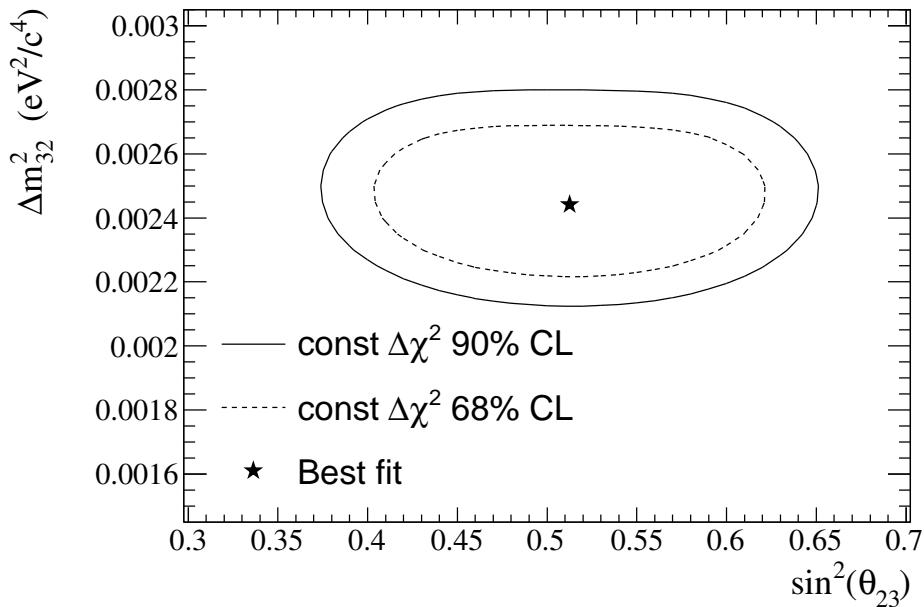


Figure 479: 68% CL and 90% CL allowed region (including systematics), constructed with the constant- $\Delta\chi^2$ method, for the ‘2+N’ $\sin^2\theta_{23}$ in vacuum fit to the Run 1+2+3 dataset. The ‘2+N’ best-fit point is also shown.

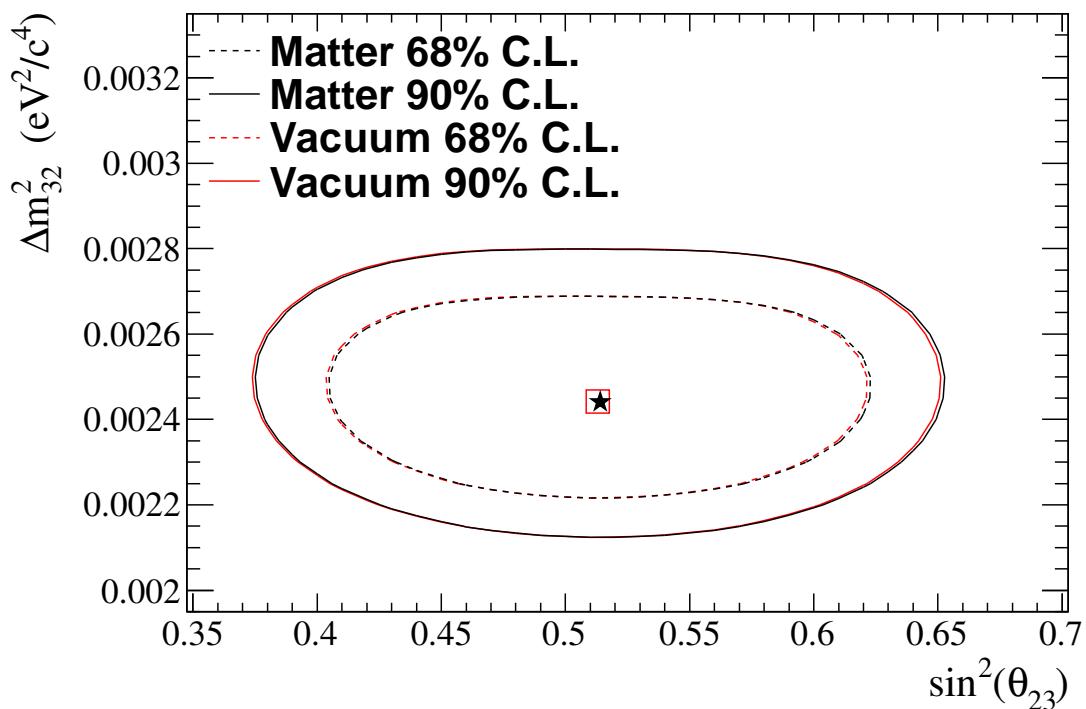


Figure 480: Comparison between the ‘2+N’ 68% CL and 90% CL allowed regions for the $\sin^2\theta_{23}$ in vacuum and $\sin^2\theta_{23}$ in matter fits obtained using the constant- $\Delta\chi^2$ method. The comparison is shown for the fits to the Run 1+2+3 dataset.