

1.9]

Two Sided PN Junction

$$\phi_{bi} = \phi_t \ln \left(\frac{N_A N_D}{n_i^2} \right)$$

From eq 1.5.1) $\phi_{bi} = \phi_{FP} - \phi_{FN}$

From eq 1.2.14a) $\phi_{FP} = \phi_t \ln \left(\frac{N_A}{n_i} \right)$

$$\phi_{FN} = -\phi_t \ln \left(\frac{N_D}{n_i} \right)$$

$$\phi_{bi} = \phi_t \ln \left(\frac{N_A}{n_i} \right) - \left(-\phi_t \ln \left(\frac{N_D}{n_i} \right) \right)$$

$$\phi_{bi} = \phi_t \ln \left(\frac{N_A N_D}{n_i^2} \right)$$

$$\psi_c = \psi_1 + \psi_2 \rightarrow \text{eq 1.5.11}$$

$$\psi_1 = \frac{q N_D d_1^2}{2 \epsilon_s} \rightarrow \text{eq 1.5.9}$$

$$\psi_2 = \frac{q N_A d_2^2}{2 \epsilon_s} \rightarrow \text{eq 1.5.10}$$

$$\psi_c = \frac{q N_D d_1^2}{2 \epsilon_s} + \frac{q N_A d_2^2}{2 \epsilon_s} = \frac{q N_D d_1^2 + q N_A d_2^2}{2 \epsilon_s}$$

$$\psi_c = \frac{q (N_D d_1^2 + N_A d_2^2)}{2 \epsilon_s}$$

$$\frac{\psi_c 2 \epsilon_s}{q} = N_D d_1^2 + N_A d_2^2$$

$$\frac{d_1}{d_2} = \frac{N_A}{N_D} \rightarrow \text{eq 1.5.7}$$

$$d_1 N_D = d_2 N_A$$

$$\frac{\psi_c 2 \epsilon_s}{q} = N_D d_1^2 + N_A d_2^2$$

$$\frac{d_1}{d_2} = \frac{N_A}{N_D}$$

$$\frac{\psi_c 2 \epsilon_s}{q} = N_D \left(\frac{N_A}{N_D} d_2 \right)^2 + N_A d_2^2$$

$$= \frac{N_A^2}{N_D} d_2^2 + N_A d_2^2$$

$$N_D d_1^2 + N_A d_2^2 = \frac{2 \epsilon_s \psi_c}{q}$$

$$N_D \cdot \frac{N_A}{N_D} \cdot d_2 \cdot d_1 + N_A d_2^2$$

$$N_D (N_D + N_A) =$$

$$N_A^2 + N_D^2 + 2 N_D N_A$$

$$(N_A \cdot d_2)^2 \cdot \frac{N_A + N_D}{N_D N_A} = \frac{2 \epsilon_s}{q} \psi_c$$

P.1.10)

C vs V_R

$0-2V$

n^+p

$$A = 200 \mu m^2$$

$$N_A = 5 \times 10^{17} cm^{-3}$$

$$\phi_{Fn} = -0.56V$$

We can replace ϕ_{bi} to be ϕ_{Fn} since it's an n^+p

$$C = \frac{1}{A} \cdot \frac{\sqrt{2 \cdot q \cdot \epsilon_s \cdot N_A}}{2 \cdot \sqrt{V_R + \phi_{Fn}}}$$

Picture attached

$$3) \quad V_{DD} = 5V \quad V_{IL} = 1.35V \quad V_{IH} = 3.15V$$

$$V_{OL} = 0.33V \quad V_{OH} = 3.84V$$

$$NM_L = V_{IL} - V_{OL} = 1.35V - 0.33 = 1.02V$$

$$NM_H = V_{OH} - V_{IH} = 3.84V - 3.15V = 0.69V$$

_____ 5V

—
NM_H
—

$$\rightarrow V_{OH} = 3.84V$$

$$\rightarrow V_{IH} = 3.15V$$

—
NM_L
—

$$\rightarrow V_{IL} = 1.35V$$

$$\rightarrow V_{OL} = 0.33V$$

we can't tolerate

1.5V noise
as our noise
margins are
below 1.5V

We can tolerate

0.78V on the
NM_L but not
on the NM_H

_____ 0V

4)

A	B	C	Y
0	0	0	1
0	0	1	1
0	1	0	1
1	0	0	1
0	1	1	0
1	0	1	0
1	1	0	0
1	1	1	0

$$Y = (A + B)(B + C)(A + C)$$

