

Homework 6

Thomas Kim tsk389 51835

David Munoz dam2989 51840

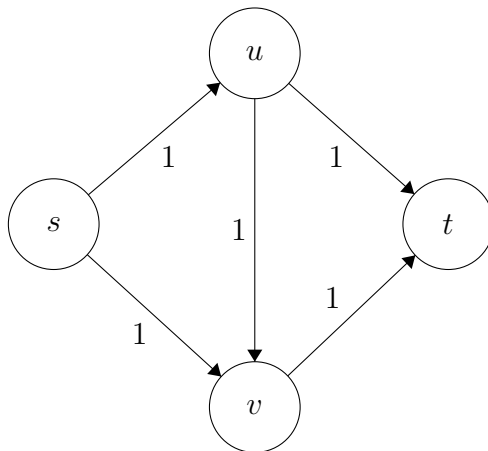
CS331 Algorithms and Complexity

Problem Q1. Given integers a_1, \dots, a_n , design a dynamic programming algorithm that determines whether there exists a partition of the numbers into 3 disjoint subsets P, Q, R such that the sum of the numbers in each set are equal. In other words,

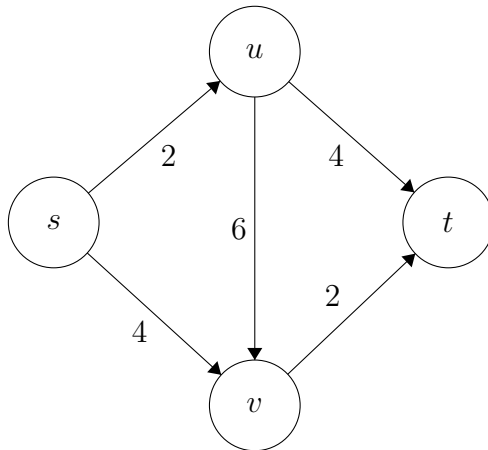
$$\sum_{a_i \in P} a_i = \sum_{a_i \in Q} a_i = \sum_{a_i \in R} a_i$$

Problem Q2. Given positive integers n and W , design a dynamic programming algorithm that finds the number of possible n element sets $\{x_1, \dots, x_n\}$ for which $\sum_i x_i^2 = W$ where each x_i is a nonnegative integer.

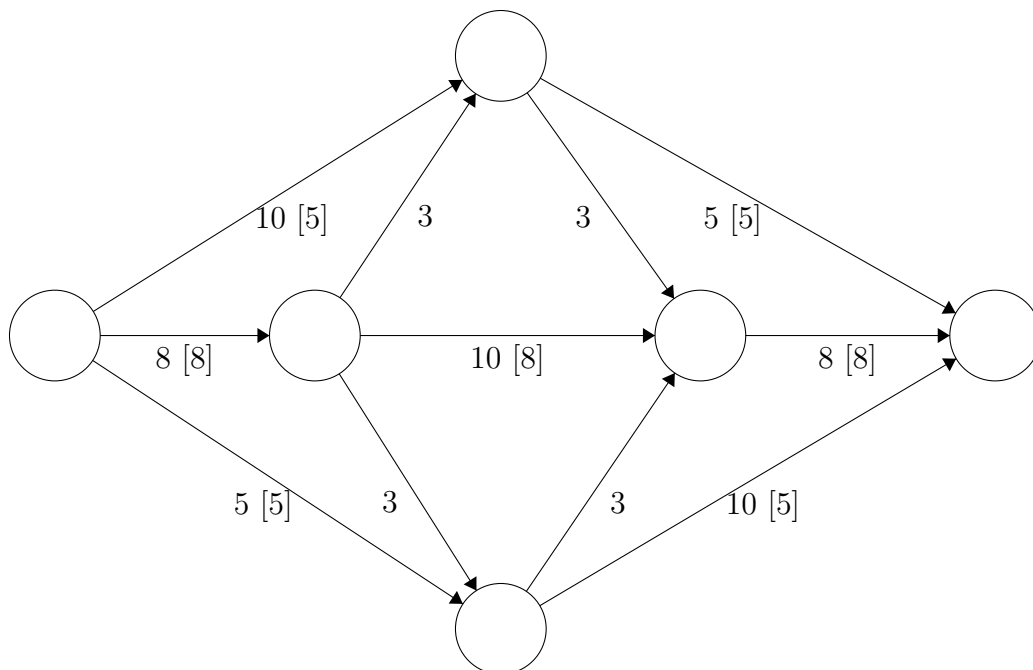
Problem Q3(a). List all the minimum $s - t$ cuts in the flow network in figure 7.24 (reproduced below).



Problem Q3(b). What is the minimum capacity of an $s - t$ cut in the flow network in Figure 7.25 (reproduced below)?



Problem Q4(a). What is the value of the $s - t$ flow depicted in figure 7.26? Is this a maximum (s, t) flow in this graph?



Problem Q4(b). Find a minimum $s - t$ cut in the flow network pictured in figure 7.26, and also say what its capacity is.

Problem Q5. Consider a set of mobile computing clients in a certain town who each need to be connected to one of several possible *base stations*. We'll suppose there are n clients, with the position of each client specified by its (x, y) coordinates in the plane. There are also k base stations; the positions of each of these is specified by (x, y) coordinates as well. For each client, we wish to connect it to exactly one of the base stations. Our choice of connections is constrained in the following ways.

- There is a *range parameter* r - a client can only be connected to a base station that is within distance r .
- There is also a *load parameter* L - no more than L clients can be connected to any single base station.

Your goal is to design a polynomial-time algorithm for the following problem. Given the positions of a set of clients and a set of base stations, as well as the range and load parameters, decide whether every client can be connected simultaneously to a base station, subject to the range and load conditions in the previous paragraph.