Crossword Solving Algorithm

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Please read over Assignment 4 System Requirements document (which accompanies this report) first to gain understanding of program overview.

# Algorithms

The AI algorithm used for playing against with will be a minimax algorithm. A minimax algorithm is a decision rule used in AI system to minimize possible loss for a worst-case scenario. To use this algorithm the following algorithms were also created: selection algorithm (finds all possible moves from current system state) and node score (determines a quantifiable metric of board state for a given player). Using these algorithms, the minimax algorithm can determine possible states from current state and the score for root nodes.

## Selection Algorithm

The selection algorithm determines the set of next possible moves. The move set is used in minimax to determine next nodes. To determine the next possible move, the algorithm will first determine if there is more than remaining more left. If false (only move remaining), then the algorithm will save both possibilities: either the player makes the move or skips. If more than one move remaining, search for adjacent empty spaces to the last move made, and if no move is available the player has “freedom” to choose any empty space (appends any empty spaces as possible solutions). The pseudocode for the selection algorithm is below:

*Selection (curr state (CS), last stone pos (LSP), player (W or B))*

*selection node set (nodeSet) <-set of possible moves*

*// check if only one space remaining.*

*if CS only has remaining space empty:*

*// if player makes move on remaining space*

*append copy of CS with empty space = player*

*// if player does not make move on remaining space*

*append copy of CS*

*return nodeSet*

*// check for empty spaces around LSP*

*if CS[LSP.row, LSP.col - 1] == 0:*

*append copy of CS with CS[LSP.row, LSP.col - 1] = player*

*do same for the rest for:*

*r + 1, c*

*r - 1, c*

*r , c + 1*

*r , c - 1*

*r + 1, c + 1*

*r - 1, c + 1*

*r + 1, c - 1*

*r - 1, c – 1*

*if nodeSet size == 0:*

*append copy any empty space in CS where the empty space is respaced with player*

*return nodeSet*

## Node Scoring Algorithm

definitions:

* Active stone – a stone(s) that have the possibility to be a live
* player stone – black or white stone
* board – is a NxN matrix, therefore, row=0 and col=0 == north-west; row=N and col=0 == south-west; row=0 and col=N == north-east; row=N and col=N == south-east

Algorithm will search starting from row=0, col=0 to row=N, col=N for active stone(s). Where the number of active stones found in a group of 4 (possible live or live) will be associated with counter: single stone counter, double stone counter, triple stone counter, and live stone counter. These corresponding to, one stone found in group, two stones found in group, three stones found in group, and four stones found in group, respectively. Groups will not be counted twice. Algorithm will search for stones by searching SW, S, SE, & E 3-stones out from current stone position. Then it will decompose those four directions into sub directions by searching opposite of search direction by 1, 2, & 3-stones out still groups of 4-stones (remaining stones are searched in search direction). If at any point while searching in the opposite direction a player stone was found, the search is aborted. This is because that stone found (if current player stone) would have counted current stone in same domain (group). Therefore, eliminating redundant groups. Also, to be clear, if any stone was found in the direction of search (SW, S, SE, or E), it will not aborted since stone that has been found has not tested any domains yet (no grouping have been determined by that stone).

Once all stones have been searched, a weighted score is returned. Singles stones have a weight 1, double stones have a weight 2, triple stones have a weight 3, and lives have a weight 4. I did this so to increase the number of active stones in a group.

*Pseudocode*

*Node Score (board):*

*foreach r in row:*

*foreach c in col:*

*if board[r][c] == playerSymbol:*

*// checking south-direction*

*if r + 3 is viable and r + 4 either does not exist (past range) or not player symbol and r - 1 either does not exist (past range) or not… player symbol:*

*search and count number of stones player found r->(r+3) ...*

*if any other player stone found, stop search, stop search and abort this conditional (checking south)*

*if number of found stones is 1:*

*increase number of singles stones with possible live found*

*else if number of found stones is 2:*

*increase number of double stones with possible live found*

*else if number of found stones is 3:*

*increase number of triple stones with possible live found*

*else:*

*increase number of lives*

*// checking r - 3 (north) for active stones (first decomposioner)*

*if r - 3 is viable and r - 4 is either non-existent or non-player symbol and r + 1 is either non-existent or non-player symbol*

*search and count number of player stones found r->(r-3) ...*

*if any stone is found, stop search and abort conditional (checking north)*

*else:*

*increase number of single stones with possible live found*

*// checking north 2 and south 1 for active stones (2nd decomposioner)*

*if r - 2 and r + 1 are viable and (r - 3 and r + 2 (bounds) do not have player stones):*

*search and count number of player stones found (r-2)->(r+1)...*

*if any player stone found before r (r-2->r) or any other player stone found after or including r:*

*abort conditional search, no active stones in domain*

*else:*

*increase the associated number of active stones with stone counter (triple, double, single)*

*// checking north 1 and south 2 for active stones (3rd decomposioner)*

*if r - 1 and r + 2 are viable and (r - 2 and r + 3 do not contain player stones):*

*search and count number of stones found (r-1)->(r+2)...*

*if any player stone found before r (r-1->r) or any other player stone found after or including r:*

*abort conditional, no active stones in domain*

*else:*

*increase the associated number of active stones with stone counter (triple, double, single)*

*// Checking East*

*Same operations are performed only difference is domain checked is against columns instead of rows*

*// checking SE*

*Same operations are performed only difference is domain checked against is column and row. Where SE is*

*r->(r+3) and c->(c+3).*

*// checking SW*

*Same operations are performed only difference is domain checked against is column and row. Where SW is*

*r->(r-3) and c->(c-3).*

*return (number of singles \* 1) + (number of doubles \* 2) + (number of triples \* 3) + (number of lives \* 4)*

## Minimax Algorithm

The minimax algorithm is used for minimizing possible loss for a worst-case scenario by maxing your plays while taking into opposite player’s need to maximize their result. Hence, minimax, maximizing your result for one layer (your plays) and minimizing your results when another player is playing. To conduct minimax, the algorithm explores a state-tree starting at the root to leaves (which can be leaves of tree or max depth layer), and at the leaves, scores each leaf based on AI’s best interests. Then if the depth is even, choose the max value between all child nodes to individual parent nodes. The max value will then be assigned to the parents. If odd depth, choose the min value between all child nodes to individual parent nodes. The min value will then be assigned to the parents. Then it continues, when odd find min, when even find max, until depth zero at which the max value is found, and the path assigned with that max value is chosen as next move. Now to reduce the number of nodes to evaluate, alpha-beta pruning will be implemented.

Alpha-beta pruning is an adversarial search algorithm used commonly for machine playing of two-player games. It stops evaluating a move when at least one possibility has been found that proves the move to be worse than a previously examined move. Such moves need not be evaluated further. When applied to a standard minimax tree, it returns the same move as minimax would, but prunes away branches that cannot possibly influence the final decision. For more information, look at Wikipedia’s alpha-beta pruning <https://en.wikipedia.org/wiki/Alpha%E2%80%93beta_pruning>. Time complexity

Finally, to create a dynamic depth search, I implemented an anytime minimax algorithm using progressive deepening. This allows the algorithm to produce a result at any time. It does this by finding the results for depth = 1, depth = 2, …, depth = N and only stopping and returning a result either when time/computational resources have been used or when leaf nodes have been found (max depth has been achieved). For my implementation, I am giving the AI time limit of 5s. Now, this many seem computationally expensive, however, doing some basic algebra and calculus, it can be shown to be roughly the same complexity as alpha-bate pruning. The calculation is made by taking the limit has progressive depths get closer to max depth. Where each at each depth, is the alpha-beta pruning complexity. The following is the calculating:

The approximation is more accurate the larger gets.

Table . Minimax Algorithm Time Complexity (Winston, 2014)

|  |  |
| --- | --- |
| Algorithm | Time Complexity |
| Minimax |  |
| Minimax with Alpha-Beta Pruning | Worse Avg. |
| Minimax with Alpha-Beta and Progressive Deepening | Worse Avg. |

*NEXT\_MOVE <-pointer to best move*

*Minimax(node, depth, isMaxPlayer, alpha, beta):*

*if depth == max depth OR node is leaf:*

*return value of node (node score method)*

*if isMaxPlayer == MAX:*

*bestVal = -INF*

*foreach child node:*

*value = minimax(child, depth + 1, MIN, alpha, beta)*

*if depth == 0:*

*preVal = bestVal*

*bestVal = max(bestVal, value)*

*if preVal < bestVal:*

*NEXT\_MOVE = child*

*Else:*

*bestVal = max(bestVal, value)*

*alpha = max (alpha, bestVal)*

*if beta <= alpha:*

*break*

*return bestVal*

*else: <-isMaxPlayer == MIN*

*bestVal = +INF*

*foreach child node:*

*value = minimax(child, depth + 1, MAX, alpha, beta)*

*if depth == 0:*

*preVal = bestVal*

*bestVal = min(bestVal, value)*

*if preVal > bestVal:*

*NEXT\_MOVE = child*

*Else:*

*bestVal = min(bestVal, value)*

*beta = min (beta, bestVal)*

*if beta <= alpha:*

*break*

*return bestVal*

*END*

# Results