

# **Programs as Data 6**

## **Imperative languages, environment and store, micro-C**

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# Today

- Course overview
- A naïve imperative language
- C concepts
  - Pointers and pointer arithmetics, arrays
  - Lvalue and rvalue
  - Parameter passing by value and by reference
  - Expression statements
- Micro-C, a subset of C
  - abstract syntax
  - lexing and parsing
  - interpretation

# The overall course plan

- F# and functional programming
- Interpreting an expression language
- Lexing and parsing tools
- Interpreting a functional language, micro-ML
  - Higher-order functions
- Type checking and type inference
- Interpreting an imperative language, micro-C
- Compiling micro-C to stack machine code
- Real-world abstract machines: JVM and .NET
  - Garbage collection techniques
- Continuations, exceptions and backtracking
- (Programs that generate programs, Scheme)
- Or maybe Scala, a functional/OO language on JVM

# A naive-store imperative language

- **Naive** store model:
  - a variable name maps to an integer value
  - so store is just a runtime environment

```
sum = 0;  
for i = 0 to 100 do  
    sum = sum + i;
```

|     |      |
|-----|------|
| i   | 100  |
| sum | 5050 |

```
i = 1;  
sum = 0;  
while sum < 10000 do begin  
    sum = sum + i;  
    i = 1 + i;  
end;
```

|     |       |
|-----|-------|
| i   | 142   |
| sum | 10011 |

# Naïve-store statement execution, 1

- Executing a statement gives a new store
- Assignment  $x=e$  updates the store
- Expressions do not affect the store

```
let rec exec stmt (store : naivestore) : naivestore =  
  match stmt with  
  | Asgn(x, e) ->  
    setSto store (x, eval e store)  
  | If(e1, stmt1, stmt2) ->  
    if eval e1 store <> 0 then exec stmt1 store  
    else exec stmt2 store  
  | ...
```

Update store  
at x with  
value of e

## Naïve-store statement execution, 2

- A block  $\{s_1; \dots; s_n\}$  executes  $s_1$  then  $s_2 \dots$
- Example:

```
exec (Block [s1; s2]) store
= loop [s1; s2] store
= exec s2 (exec s1 store)
```

```
let rec exec stmt (store : naivestore) : naivestore =
  match stmt with
  | Block stmts ->
    let rec loop ss sto =
      match ss with
      | [] -> sto
      | s1::sr -> loop sr (exec s1 sto)
    loop stmts store
  | ...
```

# Naïve-store statement execution, 3

- **for** and **while** update the store sequentially

```
let rec exec stmt (store : naivestore) : naivestore =  
  match stmt with  
  | ...  
  | For(x, estart, estop, stmt) -> ...  
  | While(e, stmt) ->  
    let rec loop sto =  
      if eval e sto = 0 then sto  
      else loop (exec stmt sto)  
    loop store
```

# Environment and store, micro-C

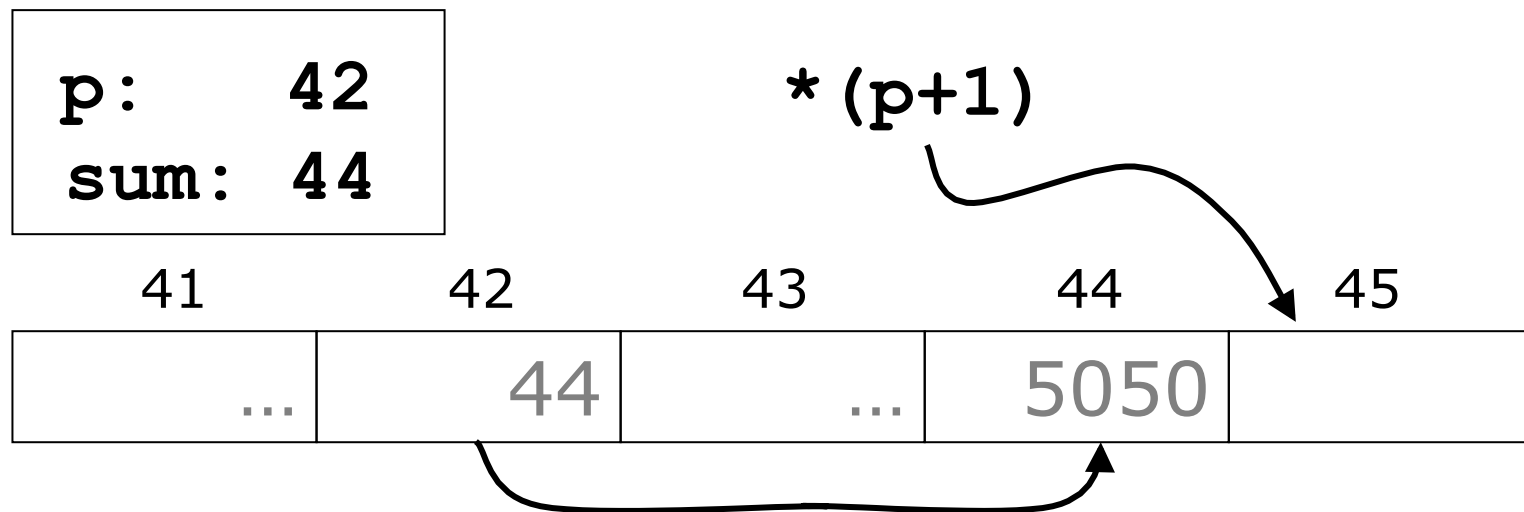
- The naive model cannot describe *pointers* and *variable aliasing*
- A more realistic store model:
  - *Environment* maps a variable name to an address
  - *Store* maps address to value





# The essence of C: Pointers

- Main innovations of C (1972) over Algol 60:
  - Structs, as in COBOL and Pascal
  - Pointers, pointer arithmetics, pointer types, array indexing as pointer indexing
  - Syntax: { } for blocks, as in C++, Java, C#



- Very different from Java and C#, which have no pointer arithmetics, but garbage collection

# Desirable language features

|                                   | C | C++ | F#/ML | Smtalk | Haskell | Java | C# |
|-----------------------------------|---|-----|-------|--------|---------|------|----|
| Garbage collection                |   |     |       |        |         |      |    |
| Exceptions                        |   |     |       |        |         |      |    |
| Bounds checks                     |   |     |       |        |         |      |    |
| Static types                      |   |     |       |        |         |      |    |
| Generic types (para. polym.)      |   |     |       |        |         |      |    |
| Pattern matching                  |   |     |       |        |         |      |    |
| Reflection                        |   |     |       |        |         |      |    |
| Refl. on type parameters          |   |     |       |        |         |      |    |
| Anonymous functions ( $\lambda$ ) |   |     |       |        |         |      |    |
| Streams                           |   |     |       |        |         |      |    |
| Lazy eval.                        |   |     |       |        |         |      |    |

# C pointer basics

- A pointer `p` refers to a storage location
- The dereference expression `*p` means:
  - *the content of the location* (rvalue) as in  
`*p + 4`
  - *the storage location itself* (lvalue), as in  
`*p = x+4`
- The pointer that points to `x` is `&x`
- Pointer arithmetics:
  - `*(p+1)` is the location just after `*p`
- If `p` equals `&a[0]`  
then `*(p+i)` equals `p[i]` equals `a[i]`,  
so an array is a pointer
- Strange fact: `a[2]` can be written `2[a]` too

# Using pointers for return values

- Example ex5.c, computing square(x):

```
void main(int n) {  
    ...  
    int r;  
    square(n, &r);  
    print r;  
}  
  
void square(int i, int *rp) {  
    *rp = i * i;  
}
```

for input

for return value: a  
pointer to where to  
put the result

# Recursion and return values

- Computing factorial with MicroC/ex9.c

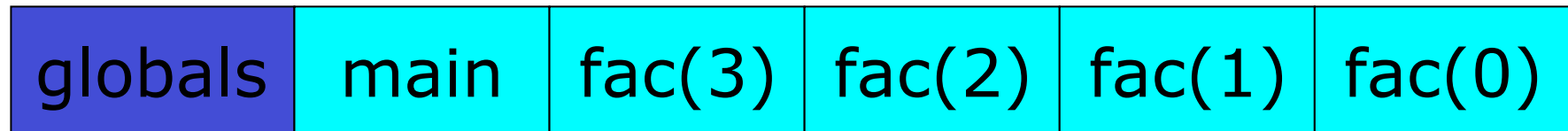
```
void main(int i) {
    int r;
    fac(i, &r);
    print r;
}

void fac(int n, int *res) {
    if (n == 0)
        *res = 1;
    else {
        int tmp;
        fac(n-1, &tmp);
        *res = tmp * n;
    }
}
```

- **n** is input parameter
- **res** is output parameter:  
a pointer to where to  
put the result
- **tmp** holds the result  
of the recursive call
- **&tmp** gets a pointer  
to **tmp**

# Storage model for micro-C

- The store is an indexable stack
  - Bottom: global variables at fixed addresses
  - Plus, a stack of activation records



- An *activation record* is an executing function
  - return address and other administrative data
  - parameters and local variables
  - temporary results



# Lvalue and rvalue of an expression

- Rvalue is “normal” value, right-hand side of assignment: `17`, `true`
- Lvalue is “location”, left-hand side of assignment: `x`, `a[2]`
- In assignment `e1=e2`, expression `e1` must have lvalue
- Where else must an expression have lvalue in C#? In C?

|                     | Has<br>lvalue | Has<br>rvalue |
|---------------------|---------------|---------------|
| <code>x</code>      | yes           | yes           |
| <code>a[2]</code>   | yes           | yes           |
| <code>*p</code>     | yes           | yes           |
| <code>x+2</code>    | no            | yes           |
| <code>&amp;x</code> | no            | yes           |

# Call-by-value and call-by-reference, C#

```
int a = 11;  
int b = 22;  
swapV(a, b);  
swapR(ref a, ref b);
```

a: 41  
b: 42

addresses

by value

```
static void swapV(int x, int y) {  
    int tmp = x; x = y; y = tmp;  
}
```

x: 43  
y: 44  
tmp: 45

by reference

```
static void swapR(ref int x, ref int y) {  
    int tmp = x; x = y; y = tmp;  
}
```

x: 41  
y: 42  
tmp: 43

store

| 41 | 42 | 43 | 44 | 45 |
|----|----|----|----|----|
| 11 | 22 | 22 | 11 | 11 |



# C variable declarations

| Declaration     | Meaning  |
|-----------------|--|
| int n           | n is an integer                                |
| int *p          | p is a pointer to integer                      |
| int ia[3]       | ia is array of 3 integers                      |
| int *ipa[4]     | ipa is array of 4 pointers to integers         |
| int (*iap)[3]   | iap is pointer to array of 3 integers          |
| int *(*ipap)[4] | ipap is pointer to array of 4 pointers to ints |

Unix program `cdecl` or [www.cdecl.org](http://www.cdecl.org) may help:

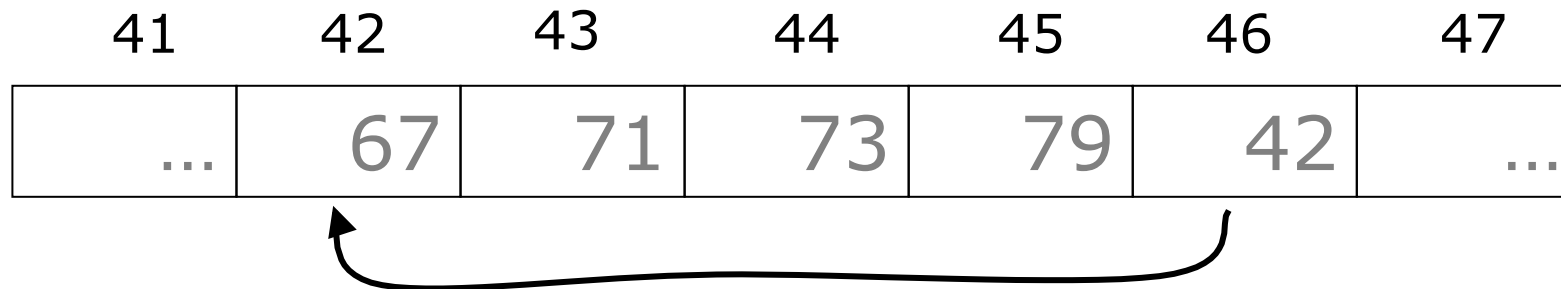
```
cdecl> explain int *(*ipap)[4]
declare ipap as pointer to array 4 of pointer to int
cdecl> declare n as array 7 of pointer to pointer to int
int **n[7]
```

# Micro-C array layout

- An array `int arr[4]` consists of

- its 4 int elements
- a pointer to `arr[0]`

**arr: 46**



- This is the uniform array representation of B
- Real C treats array parameters and local arrays differently; complicates compiler
- Strachey's CPL -> Richards's BCPL -> B -> C

# Micro-C syntactic concepts

- Types

|                       |                                  |
|-----------------------|----------------------------------|
| <code>int</code>      | <code>TypI</code>                |
| <code>int *x</code>   | <code>TypP (TypI)</code>         |
| <code>int x[4]</code> | <code>TypA (TypI, Some 4)</code> |

- Expressions

`(*p + 1) * 12`

- Statements

`if (x!=0) y = 1/x;`

- Declarations

- of global or local variables

`int x;`

- of global functions

`void swap(int *x, int *y) { ... }`

# Micro-C abstract syntax

|  |                               |         |
|--|-------------------------------|---------|
| type typ =   |                               |         |
| TypI   | (* Type int                   | *)      |
| TypC   | (* Type char                  | *)      |
| TypA of typ * int option                                   | (* Array type                 | *)      |
| TypP of typ  | (* Pointer type               | *)      |
| and expr =   |                               |         |
| Access of access   | (* x or *p or a[e]            | *)      |
| Assign of access * expr                                    | (* x=e or *p=e or a[e]=e      | *)      |
| Addr of access   | (* &x or *&p or &a[e]         | *)      |
| CstI of int  | (* Constant                   | *)      |
| Prim1 of string * expr                                     | (* Unary primitive operator   | *)      |
| Prim2 of string * expr * expr                              | (* Binary primitive operator  | *)      |
| Andalso of expr * expr                                     | (* Sequential and             | *)      |
| Orelse of expr * expr                                      | (* Sequential or              | *)      |
| Call of string * expr list                                 | (* Function call f(...)       | *)      |
| and access =   |                               |         |
| AccVar of string   | (* Variable access            | x *)    |
| AccDeref of expr   | (* Pointer dereferencing      | *p *)   |
| AccIndex of access * expr                                  | (* Array indexing             | a[e] *) |
| and stmt =   |                               |         |
| If of expr * stmt * stmt                                   | (* Conditional                | *)      |
| While of expr * stmt                                       | (* While loop                 | *)      |
| Expr of expr   | (* Expression statement       | e; *)   |
| Return of expr option                                      | (* Return from method         | *)      |
| Block of stmtordec list                                    | (* Block: grouping and scope  | *)      |
| and stmtordec =  |                               |         |
| Dec of typ * string  | (* Local variable declaration | *)      |
| Stmt of stmt   | (* A statement                | *)      |
| and topdec =   |                               |         |
| Fundec of typ option * string * (typ * string) list * stmt |                               |         |
| Vardec of typ * string                                     |                               |         |
| and program =  |                               |         |
| Prog of topdec list  |                               |         |

Types

rvalue

Expressions

lvalue

Statements

Declarations

# Lexer specification for micro-C

- New: endline comments     // blah blah  
and delimited comments   if (x /\* y? \*/)

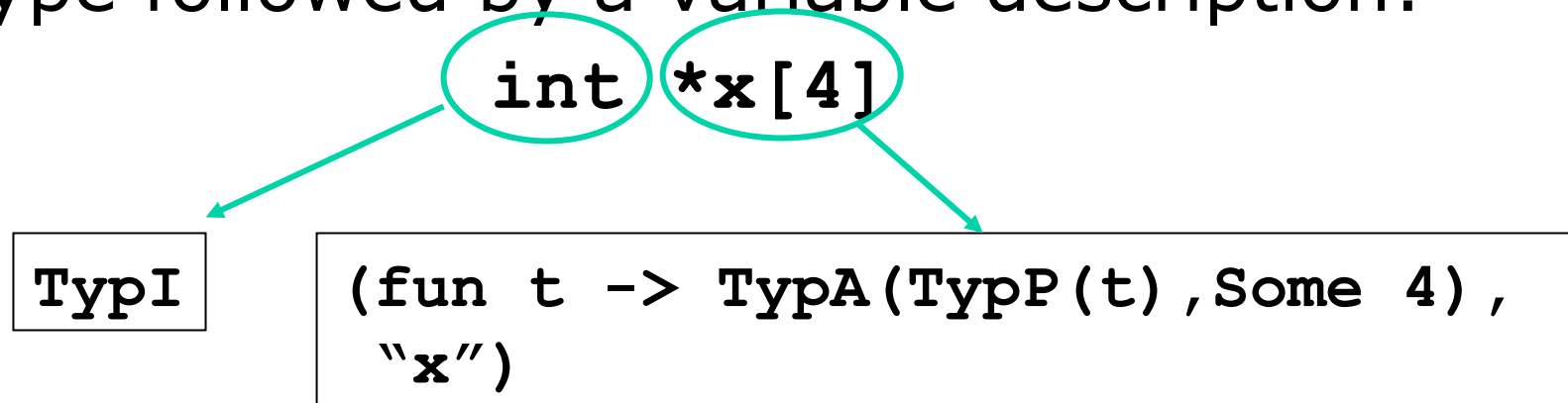
```
rule Token = parse
| ...
| "//"          { EndLineComment lexbuf; Token lexbuf }
| "/*"          { Comment lexbuf; Token lexbuf }
```

```
and EndLineComment = parse
| ['\n' '\r']   { () }
| (eof | '\026') { () }
| _             { EndLineComment lexbuf }
```

```
and Comment = parse
| "/*"          { Comment lexbuf; Comment lexbuf }
| "*/"          { () }
| ['\n' '\r']   { Comment lexbuf }
| (eof | '\026') { lexerError lexbuf "Unterminated" }
| _             { Comment lexbuf }
```

# Parsing C variable declarations

- Hard, declarations are *mixfix*: `int *x[4]`
- Parser trick: Parse a variable declaration as a type followed by a variable description:



- Parse var description to get pair  $(\mathbf{f}, \mathbf{x})$  of type function  $\mathbf{f}$ , and variable name  $\mathbf{x}$
- Apply  $\mathbf{f}$  to the declared type to get type of  $\mathbf{x}$   
`Vardec(TypA(TypP(TypI), Some 4), "x")`

# Interpreting micro-C

- Interpreter data:
  - *locEnv, environment* mapping local variable names to store addresses
  - *gloEnv, environment* mapping global variable names to store addresses, and global function names to (parameter list, body statement)
  - *store*, mapping addresses to (integer) values
- Main interpreter functions:
  - exec: `stmt -> locEnv -> gloEnv -> store -> store`
  - eval: `expr -> locEnv -> gloEnv -> store -> int * store`
  - access: `access -> locEnv -> gloEnv -> store -> address * store`

# Micro-C statement execution

- As for the naïve language, but two envs:

```
let rec exec stmt locEnv gloEnv store : store =  
  match stmt with  
  | If(e, stmt1, stmt2) ->  
    let (v, store1) = eval e locEnv gloEnv store  
    if v<>0 then exec stmt1 locEnv gloEnv store1  
    else exec stmt2 locEnv gloEnv store1  
  | While(e, body) ->  
    let rec loop store1 =  
      let (v, store2) = eval e locEnv gloEnv store1  
      if v<>0 then loop (exec body locEnv gloEnv store2)  
      else store2  
    in loop store1  
  | ...
```



# Expression statements in C, C++, Java and C#

- The “assignment statement”

**x = 2+y;**

is really an expression

**x = 2+y**

followed by a semicolon

Value: none  
Effect: change x

Value: 2+y  
Effect: change x

- The semicolon means: ignore value

```
let rec exec stmt locEnv gloEnv store : store =  
  match stmt with  
  | ...  
  | Expr e ->  
    let (_, store1) = eval e locEnv gloEnv store  
    store1
```

Evaluate expression  
then ignore its value

# Micro-C expression evaluation, 1

- Evaluation of an expression
  - takes local and global env and a store
  - gives a resulting *rvalue* and a *new store*

```
and eval e locEnv gloEnv store : int * store =  
  match e with  
  | ...  
  | CstI i          -> (i, store)  
  | Prim2(ope, e1, e2) ->  
    let (i1, store1) = eval e1 locEnv gloEnv store  
    let (i2, store2) = eval e2 locEnv gloEnv store1  
    let res =  
      match ope with  
      | "*" -> i1 * i2  
      | "+" -> i1 + i2  
      | ...  
    (res, store2)
```

## Micro-C expression evaluation, 2

- To evaluate access expression **x**, **\*p**, **arr[i]**
  - find its lvalue, as an address **loc**
  - look up the rvalue in the store, as **store1[loc]**
- To evaluate **&e**
  - just evaluate **e** as lvalue
  - return the lvalue

rvalue

```
and eval e locEnv gloEnv store : int * store =  
  match e with  
  | Access acc ->  
    let (loc, store1) = access acc locEnv gloEnv store  
    (getSto store1 loc, store1)  
  | Addr acc -> access acc locEnv gloEnv store  
  | ...
```

# Micro-C access evaluation, to *lvalue*

- A variable **x** is looked up in environment
- A dereferencing **\*e** just evaluates **e** to an address
- An array indexing **arr[idx]**
  - evaluates **arr** to address **a**, then gets **aval=store[a]**
  - evaluates **e** to rvalue index **i**
  - returns address **(aval+i)**

**lvalue**

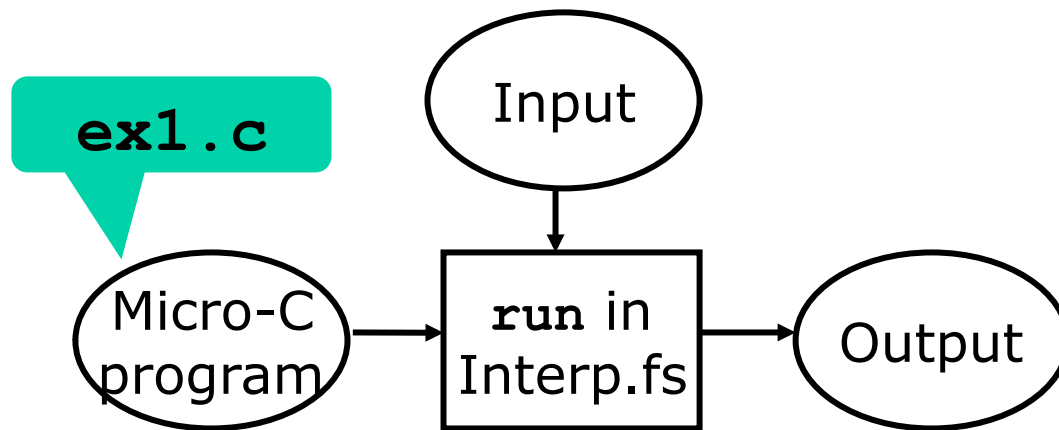
```
and access acc locEnv gloEnv store : int * store =  
  match acc with  
  | AccVar x                -> (lookup (fst locEnv) x, store)  
  | AccDeref e              -> eval e locEnv gloEnv store  
  | AccIndex(acc, idx) ->  
    let (a, store1) = access acc locEnv gloEnv store  
    let aval = getSto store1 a  
    let (i, store2) = eval idx locEnv gloEnv store1  
    (aval + i, store2)
```

# Operators $\&x$ and $*p$ are inverses

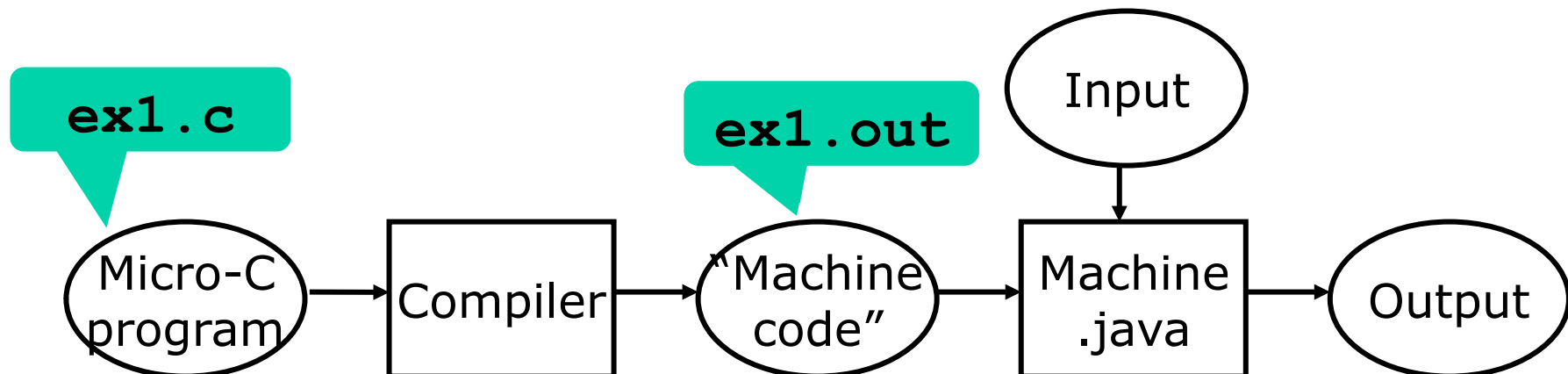
- The address-of operator  $\&e$ 
  - evaluates  $e$  to its lvalue
  - returns the lvalue (address) as if it were an rvalue
- The dereferencing operator  $*e$ 
  - evaluates  $e$  to its rvalue
  - returns the rvalue as if it were an lvalue
- It follows
  - that  $\&(*e)$  equals  $e$
  - that  $*(&e)$  equals  $e$ , provided  $e$  has lvalue

# Micro-C, interpreter and compiler

- This lecture: Interpretation of micro-C



- Next lecture: Compilation of micro-C



# Reading and homework

- This week's lecture:
  - PLCSD chapter 7
  - Strachey: Fundamental Concepts ...
  - Kernighan & Ritchie: The C programming language, chapter 5.1-5.5
- Next lecture
  - PLCSD chapter 8