# The Optimal Design of Climate Agreements Inequality, Trade, and Incentives for Climate Policy

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- ▶ Proposals to fight climate inaction and the free-riding problem:
  - International cooperation through climate agreements, e.g. UN's COP
  - Trade sanctions needed to give incentives to countries to reduce emissions meaningfully
  - "Climate club", Nordhaus (2015): trade sanctions on non-participations to sustain larger "clubs"
  - Carbon Border Adjustment mechanisms (CBAM), EU policy: carbon tariffs

#### Introduction

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  - Trade-off:

    Intensive margin: a "climate club" with few countries and large emission reductions vs. Extensive margin: a larger set of countries, at the cost of lowering the carbon tax

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     Intensive margin: a "climate club" with few countries and large emission reductions vs. Extensive margin: a larger set of countries, at the cost of lowering the carbon tax
- ► In this paper:
  - I build a rich Integrated-Assessment Model (IAM) with heterogeneous countries, energy markets, international trade and countries' strategic behaviors
  - I study the strategic implications of climate agreements and the optimal club design

#### Preview of the results:

 The optimal agreement deters free-riding and balances the intensive – extensive margin tradeoff

#### • Optimal climate agreement:

- Participation of all the countries in the world at the exception of several fossil fuels producers: Russia, Saudi Arabia, Iran, and Nigeria.
- Carbon tax of  $$110/tCO_2$ , lower than the policy benchmark without free-riding
- Large trade tariffs on non-members to impose substantial retaliation

#### Impossibility result:

 Because of free-riding, we can not achieve both a high carbon tax and complete participation, despite arbitrary trade tariffs

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  - Climate clubs and cooperation: Nordhaus (2015), Barrett (1994, 2003, 2013, 2022), Carraro, Siniscalco (1993), Chander, Tulkens (1995, 1997), Dutta, Radner (2004, 2006), Harstad (2012), Maggi (2016), Hagen, Schneider (2021), Iverson (2024)
  - Coalition building: Ray, Vohra (2015), Nordhaus (2021), Harstad (2023), Maggi, Staiger (2022)
  - ⇒ Quantitative analysis of climate agreements and policy recommendation

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- ► IAM and macroeconomics of climate change and carbon taxation
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  - HA model: Bourany (2024), Krusell, Smith (2022), Kotlikoff, Kubler, Polbin, Scheidegger (2021)
  - Spatial models: Cruz, Rossi-Hansberg (2022, 2023) among others
  - ⇒ Strategic and constrained policy with heterogeneous countries & trade

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- ► Trade policy and environment policies:
  - Trade and carbon policies: Farrokhi, Lashkaripour (2024), Kortum, Weisbach (2023), Böhringer, Carbone, Rutherford (2012, 2016), Hsiao (2022), Shapiro (2021), Caliendo et al. (2024)
  - Tariff policy: Ossa (2014), Costinot et al. (2015), Adao, Costinot (2022), Antràs et al. (2022)
  - ⇒ Optimal design of climate agreements with free-riding incentives

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  - ⇒ Optimal design of climate agreements with free-riding incentives

#### Outline

- 1. Introduction
- 2. Model:

An Integrated Assessment Model with Heterogenous Countries and Trade

- 3. Climate Agreements Design
- 4. Quantification
- Policy Benchmarks: Optimal Policy without Free-riding Incentives
- 6. Main result:
  The Optimal Climate Agreement
- 7. Extensions
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#### Model – Household & Firms

- Deterministic Neoclassical economy
  - countries  $i \in \mathbb{I}$ , heterogeneous in many dimensions: income, temperature, energy production, etc.
  - In each country, five agents:
  - 1. Representative household  $U_i = \max_{c_{ij}} u(\mathcal{D}_i^u(\mathcal{E})c_i)$ , Trade, à la Armington

$$c_i = \left(\sum_{j} a_{ij}^{\frac{1}{\theta}} c_{ij}^{\frac{\theta-1}{\theta}}\right)^{\frac{\theta}{\theta-1}} \sum_{j \in \mathbb{I}} c_{ij} \underbrace{\left(1 + t_{ij}^b\right)}_{\text{tariff}} \underbrace{\tau_{ij}}_{\text{iceberg}} p_j = \underbrace{w_i \ell_i}_{\text{labor}} + \underbrace{\pi_i^f}_{\text{fossil firm}} + \underbrace{t_i^{ls}}_{\text{lump-sum profit}}$$

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2. Representative final good firm:

$$\max_{\ell_i, \mathbf{e}^f_i, \mathbf{e}^c_i, \mathbf{e}^c_i} p_i \, \mathcal{D}_i^{\mathbf{y}}(\mathcal{E}) \, z_i \, F(\ell_i, \mathbf{e}^f_i, e^c_i, e^r_i) - w_i \ell_i - (q^f_i + \mathsf{t}^\varepsilon_i) \mathbf{e}^f_i - (q^c_i + \mathsf{t}^\varepsilon_i) \mathbf{e}^c_i - q^r_i \mathbf{e}^r_i$$

- Externality: Damage function  $\mathcal{D}_i^y(\mathcal{E})$ , Income inequality from  $z_i$ , Carbon tax:  $t_i^{\varepsilon}$ 

## Model – Energy markets & Emissions

3. Representative fossil fuels (oil-gas) producer, extracting  $e_i^x$ 

$$\pi_i^f = \max_{e_i^x} q^f e_i^x - \mathcal{C}_i^f(e_i^x) \mathbb{P}_i$$

Energy traded competitively in international markets, at price q<sup>f</sup>

$$E^f = \sum_{i \in \mathbb{I}} e_i^f = \sum_{i \in \mathbb{I}} e_i^x$$

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- 4. Coal energy firm, CRS  $e_i^c$ :  $\Rightarrow$  price  $q_i^c = z_i^c \mathbb{P}_i$
- 5. Renewable energy firm, CRS  $e_i^r$ :  $\Rightarrow$  price  $q_i^r = z_i^r \mathbb{P}_i$

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- Climate system: mapping from emission  $\mathcal{E} = \sum_{\mathbb{I}} e_i^f + e_i^c$  to damages  $\mathcal{D}_i(\mathcal{E})$

- Model

## Model – Equilibrium

- Given policies  $\{t_i^c, t_{ij}^b, t_i^{ls}\}_i$ , a **competitive equilibrium** is a set of decisions  $\{c_{ij}, e_i^c, e_i^c, e_i^r, e_i^x\}_{ij}$ , emission  $\{\mathcal{E}\}_i$  changing climate and prices  $\{p_i, w_i, q_i^c, q_i^r\}_i$ ,  $q^f$  such that:
- Households choose  $\{c_{ij}\}_{ij}$  to max. utility s.t. budget constraint
- Firm choose inputs  $\{e_i^f, e_i^c, e_i^r\}_i$  to max. profit
- $\circ$  Oil-gas firms extract/produce  $\{e_i^x\}_i$  to max. profit. + Elastic renewable, coal supplies  $\{e_i^c, e_i^r\}_i$
- $\circ$  Emissions  $\mathcal E$  affects climate and damages  $\mathcal D_i^y(\mathcal E)$  and  $\mathcal D_i^u(\mathcal E)$
- o Government budget clear  $\sum_i \mathsf{t}_i^{ls} = \sum_i \mathsf{t}_i^\varepsilon (e_i^f + e_i^c) + \sum_{i,j} \mathsf{t}_{ij}^b c_{ij} \tau_{ij} \mathsf{p}_j$
- o Prices  $\{p_i, w_i, q^f\}$  adjust to clear the markets for energy  $\sum_{\mathbb{I}} e^x_{it} = \sum_{\mathbb{I}} e^f_{it}$  and for each good

$$y_i := \mathcal{D}_i^y(\mathcal{E}) z_i F(\ell_i, e_i^f, e_i^r, e_i^r) = \sum_{k \in \mathbb{I}} \tau_{ki} c_{ki} + \sum_{k \in \mathbb{I}} \tau_{ki} (x_{ki}^f + x_{ki}^c + x_{ki}^r)$$

with  $x_{ki}^{\ell}$  export of good i as input in  $\ell$ -energy production in k

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  - Countries  $i \in \mathbb{J}$  pay carbon tax:  $\mathbf{t}_i^{\varepsilon} = \mathbf{t}^{\varepsilon}$
  - If j exits the agreement, club members  $i \in \mathbb{J}$  impose uniform tariffs  $t_{ij}^b = t^b$  on goods from j
  - Countries in the club benefit from free-trade  $t_{ij}^b = 0$  (or "status-quo" policy).
  - All countries trade in oil-gas at price  $q^f$
  - Local, lump-sum rebate of taxes:  $\mathbf{t}_i^{ls} = \mathbf{t}^{\varepsilon}(e_i^f + e_i^c) + \sum_{j \notin \mathbb{J}} \mathbf{t}^b \tau_{ij} c_{ij} \mathbf{p}_j$
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    - Single uniform carbon tax. Corresponds to the Pigouvian (First-Best) benchmark

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    - Single uniform tariff on goods. Extension considering carbon-tariffs (∼ CBAM)

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    - Provides "issue linkage" between the trade and climate policies

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    - Assumption relaxed in an extension: oil-gas-specific tariffs

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  - Local, lump-sum rebate of taxes:  $\mathbf{t}_i^{ls} = \mathbf{t}^{\varepsilon}(e_i^f + e_i^c) + \sum_{j \notin \mathbb{J}} \mathbf{t}^b \tau_{ij} c_{ij} \mathbf{p}_j$

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    - No cross-countries transfers allowed. Assumption relaxed in an extension: "climate fund"

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  - Countries outside the club  $k \notin \mathbb{J}$  have passive policies,  $t_{ki}^b = 0$  and  $t_k^\varepsilon = 0$ .
    - No retaliation. Assumption relaxed in an extension: coordination to retaliate and trade wars

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### Climate agreements and endogenous participation

- **Definition:** A climate agreement is a set  $\{\mathbb{J}, t^{\varepsilon}, t^{b}\}$  of  $\mathbb{J} \subseteq \mathbb{I}$  countries and a C.E. s.t.:
  - Countries  $i \in \mathbb{J}$  pay carbon tax  $t_i^{\varepsilon} = t^{\varepsilon}$
  - If j exits the agreement, club members  $i \in \mathbb{J}$  impose uniform tariffs  $\mathbf{t}_{ij}^b = \mathbf{t}^b$  on goods from j
  - They still trade with club members in oil-gas at price  $q^f$
  - Local lump-sum rebate of taxes Free trade within the club Passive policies outside
  - Indirect utility  $\mathcal{U}_i(\mathbb{J}, \mathfrak{t}^{\varepsilon}, \mathfrak{t}^b) \equiv u(\mathcal{D}_i^{y}(\mathcal{E}(\mathbb{J}, \mathfrak{t}^{\varepsilon}, \mathfrak{t}^b)) c_i(\mathbb{J}, \mathfrak{t}^{\varepsilon}, \mathfrak{t}^b))$

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- ► Equilibrium concepts:
  - Exit from the agreement: unilateral deviation of i,  $\mathbb{J}\setminus\{i\}$ ,  $\Rightarrow$  *Nash equilibrium*

Coalition 
$$\mathbb{J}$$
 stable if  $\mathcal{U}_i(\mathbb{J}, \mathfrak{t}^{\varepsilon}, \mathfrak{t}^b) \geq \mathcal{U}_i(\mathbb{J} \setminus \{i\}, \mathfrak{t}^{\varepsilon}, \mathfrak{t}^b)$   $\forall i \in \mathbb{J}$ 

• Sub-coalitional deviation ⇒ Coalitional Nash equilibrium

## Optimal design with endogenous participation

▶ Objective: search for the optimal *and stable* climate agreement

$$\begin{split} \max_{\mathbb{J}, t^{\varepsilon}, t^{b}} \mathcal{W}(\mathbb{J}, t^{\varepsilon}, t^{b}) &= \max_{t^{\varepsilon}, t^{b}} \ \max_{\mathbb{J}} \ \sum_{i \in \mathbb{I}} \omega_{i} \, \mathcal{U}_{i}(\mathbb{J}, t^{\varepsilon}, t^{b}) \\ s.t. & \mathcal{U}_{i}(\mathbb{J}, t^{\varepsilon}, t^{b}) \geq \mathcal{U}_{i}(\mathbb{J} \setminus \{i\}, t^{\varepsilon}, t^{b}) \end{split}$$

- ► Current design:
  - (i) choose taxes  $\{t^{\varepsilon}, t^{b}\}$

[outer problem]

(ii) choose the coalition J s.t. participation constraints hold

[inner problem]

 $\Rightarrow$  Combinatorial Discrete Choice Problem for  $\mathbb{J} \in \mathcal{P}(\mathbb{I})$ 

#### Solution method

- ► Current design:  $\max_{\mathbf{t}} \max_{\mathbf{J}} \mathcal{W}(\mathbf{J}, \mathbf{t})$  s.t.  $\mathcal{U}_j(\mathcal{J}, \mathbf{t}) \ge \mathcal{U}_j(\mathcal{J} \setminus \{i\}, \mathbf{t})$
- ► Inner problem: CDCP Solution method
  - Use a "squeezing procedure", as in Jia (2008), Arkolakis, Eckert, Shi (2023) extended to handle participation constraints

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- ► Inner problem: CDCP Solution method
  - Use a "squeezing procedure", as in Jia (2008), Arkolakis, Eckert, Shi (2023) extended to handle participation constraints
    - Squeezing step:

$$\Phi(\mathcal{J}) \equiv \left\{ j \in \mathbb{I} \, \middle| \, \Delta_j \mathcal{W}(\mathcal{J}) > 0 \, \& \, \Delta_j \mathcal{U}_j(\mathcal{J}, \mathbf{t}) > 0, \forall j \in \mathcal{J} \right\}$$

where marginal values of  $j \in \mathcal{J}$  for global  $\Delta_i \mathcal{W}(\mathcal{J}, \mathbf{t})$  and individual welfare  $\Delta_i \mathcal{U}_i(\mathcal{J}, \mathbf{t})$  are:

$$\Delta_j \mathcal{W}(\mathcal{J}, \mathbf{t}) \equiv \mathcal{W}(\mathcal{J} \cup \{j\}, \mathbf{t}) - \mathcal{W}(\mathcal{J} \setminus \{j\}, \mathbf{t}) \qquad \qquad \Delta_j \mathcal{U}_j(\mathcal{J}, \mathbf{t}) \equiv \mathcal{U}_j(\mathcal{J} \cup \{j\}, \mathbf{t}) - \mathcal{U}_j(\mathcal{J} \setminus \{j\}, \mathbf{t})$$

#### Solution method

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- Iterative procedure build lower bound  $\mathcal J$  and upper bound  $\overline{\mathcal J}$  by successive squeezing steps

$$\underline{\mathcal{J}}^{(k+1)} = \Phi(\underline{\mathcal{J}}^{(k)}) \qquad \qquad \overline{\mathcal{J}}^{(k+1)} = \Phi(\overline{\mathcal{J}}^{(k)})$$

Squeezing procedure converges to the optimal set under *Complementarity* Assumption. Details

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### Quantification – Climate system and damage

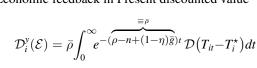
- Static economic model: decisions  $e_i^f + e_i^c$  taken "once and for all",  $\mathcal{E} = \sum_i e_i^f + e_i^c$ 
  - Climate system:

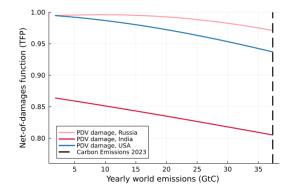
$$\dot{\mathcal{S}}_t = \mathcal{E} - \delta_s \mathcal{S}_t \ T_{it} = \bar{T}_{i0} + \Delta_i \mathcal{S}_t$$

 Path damages heterogeneous across countries Quadratic, c.f. Nordhaus-DICE / IAM

$$\mathcal{D}(T_{it}-T_i^{\star})=e^{-\gamma(T_{it}-T_i^{\star})^2}$$

• Economic feedback in Present discounted value





• Similarly for  $\mathcal{D}_i^u(\mathcal{E})$ , SCC and  $LCC_i$ ...

### Quantification

• Pareto weights  $\omega_i$ : Imply no redistribution motive  $\bar{c}_i$  conso in initial equilbrium t = 2020 w/o climate change

$$\omega_i = \frac{1}{u'(\bar{c}_i)}$$
  $\Leftrightarrow$   $C.E.(\bar{c}_i) \in \underset{\bar{c}_i}{\operatorname{argmax}} \sum_i \omega_i u(\bar{c}_i)$ 

Details Pareto weights

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#### Details Pareto weights

- Functional forms:
  - Utility: CRRA  $\eta$
  - Production function  $\bar{y} = zF(\ell_i, k_i, e_i^f, e_i^c, e_i^r)$
  - Nested CES energy  $e_i$  vs. labor-capital Cobb-Douglas bundle  $k_i^{\alpha} \ell_i^{1-\alpha}$ , elasticity  $\sigma_y < 1$
  - Energy: fossil/coal/renewable,  $CES(e_i^f, e_i^c, e_i^r)$ , elasticity  $\sigma_e > 1$
  - Energy extraction of oil-gas: isoelastic  $C^f(e^x) = \bar{\nu}_i (e^x_i/\mathcal{R}_i)^{1+\nu_i} \mathcal{R}_i$

More details

▶ Parameters calibrated from the literature

► Parameters to match "world" moments from the data Details calibration

► Parameters to match (exactly) country-level variables Details country-level moments

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  - Macro parameter: Household utility, Production function, Trade elasticity (CES):  $\theta = 5.5$
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- Parameters to match "world" moments from the data Details calibration

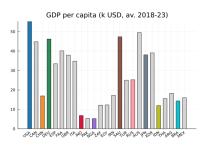
▶ Parameters to match (exactly) country-level variables Details country-level moments

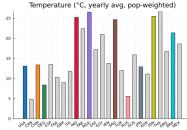
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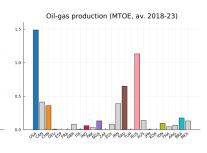
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- ► Parameters to match (exactly) country-level variables Details country-level moments
  - TFP  $z_i \Rightarrow$  GDP  $y_i$ , Population  $\mathcal{P}_i$ , Temperature  $T_{it_0}$ , Pattern scaling  $\Delta_i$
  - Mix: oil-gas  $e_i^f$ , Coal  $e_i^c$ , Low-carbon  $e_i^r$ , energy share, oil-gas prod°  $e_i^x$ , reserves  $\mathcal{R}_i$ , rents  $\pi_i^f$
  - Trade: cost  $\tau_{ij}$  projected on distance, preferences  $a_{ij}$  to match import shares  $s_{ij}$

### Quantitative application – Data and sample of countries

Sample of 32 "countries": (i) US, (ii) Canada, (iii) China, (iv) Germany, France, Spain, Italy, Rest of EU, (v) UK, (vi) India, (vii) Pakistan, (viii) Nigeria, (ix) South-Africa, (x) Rest of Africa, (xi), Egypt, (xii) Iran, (xiii) Saudi Arabia, (xiv) Turkey, (xv) Rest of Middle-East+Maghreb (xvi) Russia, (xvii) Rest of CIS, (xviii) Australia, (xix) Japan (xx) Korea, (xxi) Indonesia, (xxii) Thailand, (xxiii) Rest of South-East Asia, (xxiv) Argentina, (xxv) Brazil, (xxvi) Mexico, (xxvi) Rest of Latin America, Data: Avg. 2018-2023.







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### Optimal policy benchmarks

- ▶ Policy benchmarks, without free-riding incentives
  - First-Best, Social planner maximizing global welfare with unlimited instruments
    - Pigouvian result: Carbon tax = Social Cost of Carbon
    - Relies heavily on cross-country transfers to offset redistributive effects

### Optimal policy benchmarks

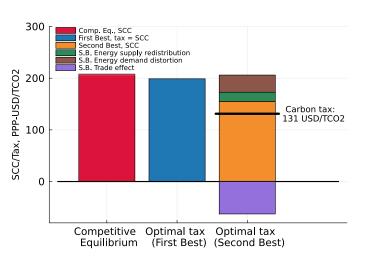
- ▶ Policy benchmarks, without free-riding incentives
  - First-Best, Social planner maximizing global welfare with unlimited instruments
    - Pigouvian result: Carbon tax = Social Cost of Carbon
    - Relies heavily on cross-country transfers to offset redistributive effects
  - Second-Best: Social planner, single carbon tax without transfers
    - Optimal carbon tax  $t^{\varepsilon}$  correct climate externality, but also accounts for:
      - (i) Redistribution motives, and G.E. effects on (ii) energy markets and (iii) trade leakage

$$\mathbf{t}^{\varepsilon} = \underbrace{\sum_{i} \phi_{i} LCC_{i}}_{=SCC} + \sum_{i} \phi_{i} \text{ Supply Redistrib}_{i}^{\circ} + \sum_{i} \phi_{i} \text{ Demand Distort}_{i}^{\circ} - \sum_{i} \text{Trade Redistrib}_{i}^{\circ} \qquad \phi_{i} \propto \omega_{i} u'(c_{i})$$

- Details: CE, First-Best, Second-Best, Club policy
- Companion paper: Bourany (2024), Climate Change, Inequality, and Optimal Climate Policy
- *Unilateral policy*: local planners choose their own optimal climate-trade policy,

see Farrokhi, Laksharipour (2024), Kortum, Weisbach (2022) Nash-Unilateral Policies

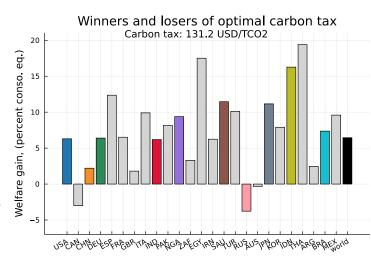
### Second-Best climate policy



- Accounting for redistribution and lack of transfers
  - $\Rightarrow$  implies a carbon tax lower than the Social Cost of Carbon (SCC), from \$155 to \$131/ $tCO_2$ .

## Gains from cooperation – World Optimal policy

- ► Optimal carbon tax Second Best:  $\sim \$131/tCO_2$
- Reduce fossil fuels / CO<sub>2</sub>
   emissions by 45% compared to the Competitive equilibrium (Business as Usual, BAU)
- Welfare difference between world optimal policy vs. comp. eq./BAU



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#### Main result and Intuition

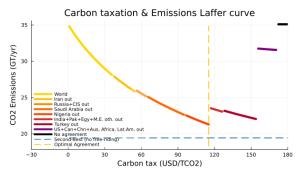
- ► The optimal climate agreement navigates the intensive and extensive margin tradeoff:
  - *Participation:* all the countries in the world with the exception of Russia, former Soviet countries, Saudi Arabia, Iran, Nigeria
  - Carbon tax: need to reduce tax level from \$131 to \$114/tCO<sub>2</sub>
  - *Trade tariffs:* impose substantial tariff 50% on the goods from non-members

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  - Participation: all the countries in the world with the exception of Russia, former Soviet countries, Saudi Arabia, Iran, Nigeria
  - Carbon tax: need to reduce tax level from \$131 to \$114/tCO<sub>2</sub>
  - *Trade tariffs:* impose substantial tariff 50% on the goods from non-members
- ► Mechanism:
  - Countries participate depending on { (i) the cost of distortionary carbon taxation
     (ii) the cost of tariffs (= the gains from trade)
  - Russia/Middle East/South Asia do not join the club for high carbon tax for any tariffs, because cost of taxing fossil-fuels >> cost of tariffs / autarky
  - ⇒ As a result, we need to decrease the carbon tax

#### Laffer curve for carbon taxation

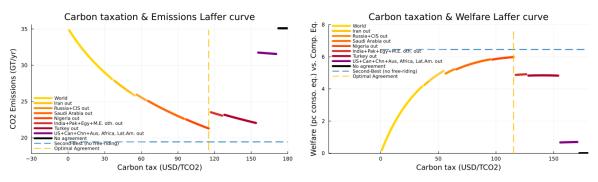
- Due to free-riding incentives, cannot reach globally optimal carbon tax  $t^{\varepsilon,\star} = \$131$ 



Emissions  $\mathcal{E}$  (in  $GtCO_2/yr$ ) and welfare  $\mathcal{W}$  as function of the carbon tax  $t^{\varepsilon}$ , with tariff  $t^b = 50\%$ .

#### Laffer curve for carbon taxation

- Due to free-riding incentives, cannot reach globally optimal carbon tax  $t^{\varepsilon,\star} = \$131$
- Need to lower the carbon tax to increase participation:
   Improve welfare by sharing the costs of carbon mitigation with *more countries*



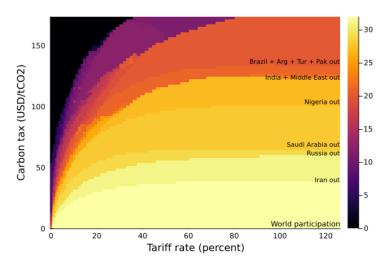
Emissions  $\mathcal{E}$  (in  $GtCO_2/yr$ ) and welfare  $\mathcal{W}$  as function of the carbon tax  $t^{\varepsilon}$ , with tariff  $t^b = 50\%$ .

### Climate Agreements: Intensive vs. Extensive Margin

Intensive margin: given a coalition: higher tax  $t^{\varepsilon}$ , emissions  $\mathcal{E} \downarrow$ , improve welfare  $\mathcal{W} \uparrow$ 

### ► Extensive margin:

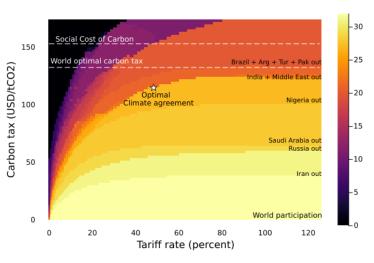
carbon tax also deters participation individual countries free-ride increasing emissions  $\mathcal{E} \uparrow$ 



### **Optimal Climate Agreement**

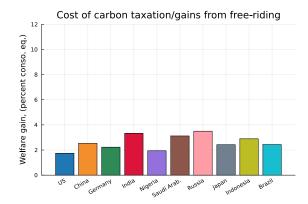
- Despite full discretion of instruments (t<sup>ε</sup>, t<sup>b</sup>), we cannot sustain an agreement with Russia, Middle East & South-Asia
- ⇒ need to reduce carbon tax from \$131 to \$114
- ⇒ Beneficial to leave several fossil-fuel producers outside the agreement e.g. no incentive for Russia to join: cold, closed to trade, large fossil-fuel producer





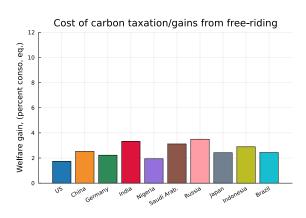
### Trade-off – Cost of Carbon Taxation vs. Gains from trade

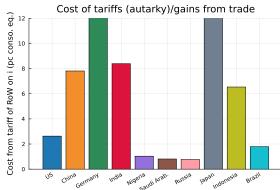
Gains from unilateral exit from agreement vs. Gains from trade, i.e. loss from tariffs/autarky



#### Trade-off – Cost of Carbon Taxation vs. Gains from trade

Gains from unilateral exit from agreement vs. Gains from trade, i.e. loss from tariffs/autarky

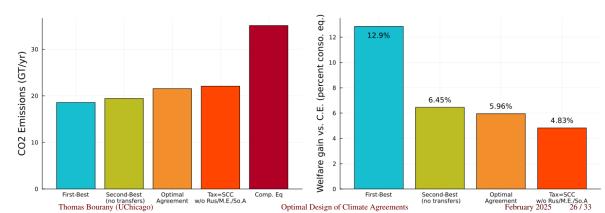




Welfare decomposition Linear decomposition, Comparison ACR ACR

#### Emission reduction vs. Welfare: Different metrics!

- Agreements with tariffs recover 92% of welfare gains from the Second-Best optimal carbon tax without transfers at a cost of increasing emissions by 11%
- Setting the policy "wrongly" at  $t^{\varepsilon} = SCC = \$155$  lowers the participation: India, Pakistan, Egypt, Turkey, Argentina, Brazil, Rest of Middle-East, all exit the agreement



Mechanisms behind participation

### Coalition building

- ► How to build sequentially the climate coalition?
  - Which countries have the most interest in joining the club?

### Coalition building

- ► Sequence of "rounds" of the static equilibrium
  - At each round (n), countries decide to enter or not depending on the gain

$$\Delta_{i}\mathcal{U}_{i}(\mathbb{J}^{(n)}) = \mathcal{U}_{i}(\mathbb{J}^{(n)} \cup \{i\}, t^{\varepsilon}, t^{b}) - \mathcal{U}_{i}(\mathbb{J}^{(n)} \setminus \{i\}, t^{\varepsilon}, t^{b})$$

- Construction evaluated at the optimal carbon tax  $t^{\varepsilon} = 114\$$ , and tariff  $t^{b} = 50\%$ .
- Sequential procedure coming for free from our CDCP algorithm / squeezing procedure
- Idea analogous to Farrokhi, Lashkaripour (2024)

# Coalition building

- ► Sequence of "rounds" of the static equilibrium
  - At each round (n), countries decide to enter or not depending on the gain

$$\Delta_i \mathcal{U}_i(\mathbb{J}^{(n)}) = \mathcal{U}_i(\mathbb{J}^{(n)} \cup \{i\}, \mathfrak{t}^{\varepsilon}, \mathfrak{t}^b) - \mathcal{U}_i(\mathbb{J}^{(n)} \setminus \{i\}, \mathfrak{t}^{\varepsilon}, \mathfrak{t}^b)$$

- Construction evaluated at the optimal carbon tax  $t^{\varepsilon} = 114$ \$, and tariff  $t^{b} = 50$ %.
- Sequential procedure coming for free from our CDCP algorithm / squeezing procedure
- Idea analogous to Farrokhi, Lashkaripour (2024)
- ▶ Result: sequence up to the optimal climate agreement
  - Round 1: European Union, i.e. Germany, France, Spain, Italy, Rest of EU
  - Round 2: China, UK, Turkey, Rest of South and South-East Asia
  - Round 3: USA, Japan, Korea, Australia, Thailand, Indonesia, Pakistan, Rest of Africa & Latin America
  - Round 4: Canada, South-Africa, Mexico
  - Round 5: India, Brazil, Egypt, Argentina, Rest of Middle-East
  - € Stay out of the agreement: Russia, CIS, Saudi Arabia, Iran, Nigeria

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#### **Extensions**

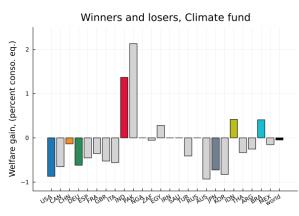
- 1. Transfers Climate fund, c.f. COP29
- 2. Carbon Border Adjustment Mechanism (CBAM), c.f. EU policy
- 3. Fossil-fuels specific tariffs  $\sim$  price cap on oil-gas exports
- 4. Retaliation Trade war between club and non-club members

#### Transfers – Climate fund

- COP29 Major policy proposal:
   New Collective Quantified Goal (NCQG) on Climate Finance for developing countries
- ► In our context: lump-sum rebate of carbon tax revenues (transfers from large to low emitters)

$$\mathbf{t}_{i}^{ls} = (1 - \alpha) \, \mathbf{t}^{\varepsilon} \varepsilon_{i} + \alpha \frac{1}{\mathcal{P}} \sum_{i} \mathbf{t}^{\varepsilon} \varepsilon_{j}$$

- Optimal transfers:
  - $\alpha^* = 0\%$ : Not optimal for rich countries to do lump-sum transfers.
  - I compare to the \$300 bn agreed in COP29: most countries looses, biggest winners (not shown) "Rest of Africa" and "Rest of South Asia"

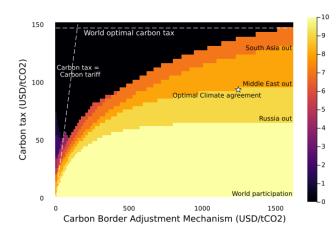


#### Carbon tariffs - EU's CBAM

- Carbon Border Adjustment Mechanism: European Union's "Carbon tariff"
  - Tariff  $t_{ii}^b$  scaling w/ carbon content  $\xi_i^y$

$$\mathbf{t}_{ij}^b = \xi_j^y \mathbf{t}^{b,\varepsilon} = \frac{\varepsilon_j}{y_j \mathbf{p}_j} \mathbf{t}^{b,\varepsilon} \qquad \text{if } i \in \mathbb{J}, j \notin \mathbb{J} ,$$

- ► Objective: fight carbon/trade leakage. But also has strategic effects (foster participation to the club)
- ► Optimal Carbon tariff:
  - Border price of carbon  $t^{b,\varepsilon} > $1000$
  - Additional constraint  $t^{\varepsilon} = t^{b,\varepsilon}$  $\Rightarrow$  prevents any large stable club



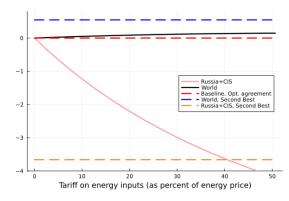
# Taxation of fossil fuels energy inputs

- Current climate club:
  Tariffs only on final goods, not energy imports
  - Empirically relevant, c.f. Shapiro (2021): inputs are more emission-intensives but trade policy is biased against final goods output
- Alternative: tax energy import  $t_{ij}^{bf}$  of non-members

$$q_{\mathbb{J}}^{f}=(1+\mathbf{t}^{bf})q_{\mathbb{I}\backslash\mathbb{J}}^{f}$$

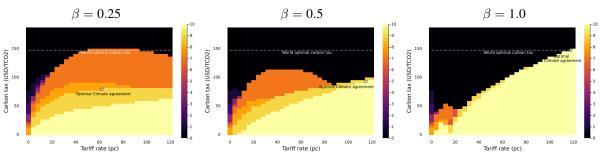
if non-members export fossil fuels to the club

- ▶ Optimal tariffs  $t^{bf}/q_{\parallel}^f = 40\%$ 
  - Compares to the \$60 price-cap from EU (out of ~ \$100 /barrel) on Russian oil (!)



#### Trade retaliation

- ► Trade war and policy retaliation: Suppose the regions outside the agreement impose retaliatory tariffs to club members
- **Exercise:** 
  - Countries outside the club  $j \notin \mathbb{J}$  impose tariffs  $t_{ii} = \beta t_{ij}$  on club members  $i \in \mathbb{J}$



#### Conclusion

- ► In this project, I solve for the optimal design of climate agreements
  - Accouting for *free-riding incentives*, as well as for inequality,
     GE effects through energy markets and trade leakage
- ► Climate agreement design jointly solves for:
  - The optimal choice of countries participating
  - The carbon tax and tariff levels, accounting for participation constraints
- ▶ The optimal climate club depends on the trade-off between:
  - the gains from climate cooperation and free-riding incentives
  - the gains from trade, i.e. the cost of retaliatory tariffs
  - ⇒ Need a large coalition at a cost of lowering the carbon tax from the world optimum \$130 to \$110
- ► Future research:
  - Dynamic policy games, bargaining, and coalition building

#### Conclusion

## Thank you!

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Optimal Design of Climate Agreements

# **Appendices**

#### Optimal design with endogenous participation

- Why uniform policy instruments  $t^{\varepsilon}$  and  $t^{b}$  for all club members:
  - Our social planner/designer solution represents the outcome of a "bargaining process" between countries (with bargaining weights  $\omega_i$ ).
  - Deviation from Coase theorem:
    - With transaction/bargaining cost: impossible to reach a consensual decision on  $I + I \times I$  instruments  $\{t_i^{\varepsilon}, t_{ii}^{b}\}_{ii}$
    - Such costs increase exponentially in the number of countries I

#### Optimal design with endogenous participation

- Why uniform policy instruments  $t^{\varepsilon}$  and  $t^{b}$  for all club members:
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  - Deviation from Coase theorem:
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    - Such costs increase exponentially in the number of countries I
- ► Optimal country specific carbon taxes:
  - Without free-riding / exogeneous participation

$$t_i^{\varepsilon} = \frac{1}{\phi_i} t^{\varepsilon} \propto \frac{1}{\omega_i u'(c_i)} \left[ SCC + SCF - SCT \right]$$

• With participation constraints: multiplier  $\nu_i(\mathbb{J})$ 

$$\mathsf{t}_i^{arepsilon} \propto rac{1}{ig(\omega_i + 
u_i(\mathbb{J})ig) u'(c_i)} ig[\mathit{SCC} + \mathit{SCF} - \mathit{SCT}ig]$$



#### Optimal design with endogenous participation

- ► Equilibrium concepts and participation constraints:
  - *Nash equilibrium*  $\Rightarrow$  unilateral deviation  $\mathbb{J}\setminus\{j\}$ ,  $\mathbb{J}\in\mathbb{S}(\mathfrak{t}^f,\mathfrak{t}^b)$  if:

$$\mathcal{U}_i(\mathbb{J}, \mathfrak{t}^{\varepsilon}, \mathfrak{t}^b) \geq \mathcal{U}_i(\mathbb{J} \setminus \{i\}, \mathfrak{t}^{\varepsilon}, \mathfrak{t}^b)$$
  $\forall i \in \mathbb{J}$ 

• *Coalitional Nash-equilibrium*  $\mathbb{C}(\mathfrak{t}^f,\mathfrak{t}^b)$ : robust of sub-coalitions deviations:

$$\mathcal{U}_{i}(\mathbb{J}, \mathfrak{t}^{f}, \mathfrak{t}^{b}) \geq \mathcal{U}_{i}(\mathbb{J} \backslash \hat{\mathbb{J}}, \mathfrak{t}^{f}, \mathfrak{t}^{b}) \ \forall i \in \hat{\mathbb{J}} \& \forall \hat{\mathbb{J}} \subseteq \mathbb{J} \cup \{i\}$$

- Stability requires to check all potential coalitions  $\mathbb{J} \in \mathcal{P}(\mathbb{I})$  as all sub-coalitions  $\mathbb{J} \setminus \hat{\mathbb{J}}$  are considered as deviations in the equilibrium
- Requires to solve all the combination  $\mathbb{J}$ ,  $t^f$ ,  $t^b$ , by exhaustive enumeration.
  - $\Rightarrow$  becomes very computationally costly for  $I = \#(\mathbb{I}) > 10$



#### Climate club design:

• Separation of the joint problem into inner and outer problems, s.t. participation constraints

$$\max_{\mathbb{J}, \mathfrak{t}^{\varepsilon}, \mathfrak{t}^{b}} \mathcal{W}(\mathbb{J}, \mathfrak{t}^{\varepsilon}, \mathfrak{t}^{b}) = \max_{\mathfrak{t}^{\varepsilon}, \mathfrak{t}^{b}} \max_{\mathbb{J}} \sum_{i \in \mathbb{I}} \omega_{i} \, \mathcal{U}_{i}(\mathbb{J}, \mathfrak{t}^{\varepsilon}, \mathfrak{t}^{b}) = \max_{\mathfrak{t}^{\varepsilon}, \mathfrak{t}^{b}} \sum_{i \in \mathbb{I}} \omega_{i} \, \mathcal{U}_{i}(\mathbb{J}, \mathfrak{t}^{\varepsilon}, \mathfrak{t}^{b})$$

$$s.t. \qquad \mathcal{U}_{i}(\mathbb{J}, \mathfrak{t}^{\varepsilon}, \mathfrak{t}^{b}) \geq \mathcal{U}_{i}(\mathbb{J} \setminus \{i\}, \mathfrak{t}^{\varepsilon}, \mathfrak{t}^{b})$$

- Current design:
  - (i) choose taxes  $\{t^{\varepsilon}, t^{b}\}$

[outer problem]

(ii) choose the coalition J s.t. participation constraints hold

[inner problem]

Computation:
 M policies (grid search), 2<sup>N</sup> choices of coalition (include both unilateral and subcoalition dev.)

- Alternative
  - (i) choose the coalition J

[outer problem]

(ii) choose taxes  $\{t^{\varepsilon}, t^{b}\}$ 

[inner problem]

- (iii) check participation constraints for  $(\mathbb{J}, t^{\varepsilon}, t^{b})$
- $\triangleright$  Computation:  $2^N$  choices of coalition, M policies (grid search?), N unilateral deviations

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#### Country deviation and policy

- $\blacktriangleright$  Consider coalition  $\mathbb{J}$ . Suppose we search for optimal policy  $t^{\varepsilon}(\mathbb{J}), t^{b}(\mathbb{J})$ 
  - Requires to compute allocation  $U_i(\mathbb{J}, t^{\varepsilon}(\mathbb{J}), t^b(\mathbb{J}))$
  - Participation constraints  $\mathcal{U}_i(\mathbb{J}, \mathsf{t}^{\varepsilon}(\mathbb{J}), \mathsf{t}^b(\mathbb{J})) \geq \mathcal{U}_i(\mathbb{J} \setminus \{i\}, \mathsf{t}^{\varepsilon}(\mathbb{J} \setminus \{i\}), \mathsf{t}^b(\mathbb{J} \setminus \{i\}))$  with multiplier  $\nu_{\mathbb{J},i}$
  - Requires to compute allocation  $U_i(\mathbb{J}\setminus\{i\}, \mathsf{t}^{\varepsilon}(\mathbb{J}\setminus\{i\}), \mathsf{t}^{b}(\mathbb{J}\setminus\{i\}))$
  - Participation constraints  $\mathcal{U}_j(\mathbb{J}\setminus\{i\}, \mathsf{t}^{\varepsilon}(\mathbb{J}\setminus\{i\}), \mathsf{t}^{b}(\mathbb{J}\setminus\{i\})) \geq \mathcal{U}_j(\mathbb{J}\setminus\{i,j\}, \mathsf{t}^{\varepsilon}(\mathbb{J}\setminus\{i,j\}), \mathsf{t}^{b}(\mathbb{J}\setminus\{i,j\}))$  with multiplier  $\nu_{\mathbb{J}\setminus\{i\},j}$
  - Etc etc.
- ▶ Implies that we would need to solve *jointly* for  $2^{\mathbb{I}}$  allocations and policy for coalitions  $\mathbb{J}$ , and each of them with  $2^{\mathbb{J}}$  constraints and multipliers  $\Rightarrow$  untractable



#### Complementarity

- Application of *Squeezing procedure* as in Arkolakis, Eckert, Shi (2023)
- Condition: Single Crossing Differences in choice (SCD-C), that I extend to account for participation constraints (SCD-C,PC)
- In our setting, condition as follows:

IF the coalition  $\mathcal J$  makes (i) allocation outcomes better for welfare with  $\{j\}$ , if both  $\mathcal J$  and  $\mathcal J \cup \{j\}$  are stable, or (ii) the coalition  $\mathcal J \cup \{j\}$  is stable if  $\mathcal J$  is unstable THEN one of these conditions should also be respected for larger coalitions  $\mathcal J' \supseteq \mathcal J$ .

$$\begin{cases} & \Delta_{i}\mathcal{U}_{i}(\mathcal{J} \cup \{j\}) \geq 0 \\ & \& \left[ \begin{array}{c} \left( \Delta_{j}\mathcal{W}(\mathcal{J} \cup \{j\}) \geq 0 & \& \ \Delta_{i}\mathcal{U}_{i}(\mathcal{J}) \geq 0 \right) \\ \text{or } \Delta_{i}\mathcal{U}_{i}(\mathcal{J}) < 0 \end{array} \right] \Rightarrow \begin{cases} & \Delta_{i}\mathcal{U}_{i}(\mathcal{J}' \cup \{j\}) \geq 0 \\ & \& \left[ \left( \Delta_{j}\mathcal{W}(\mathcal{J}' \cup \{j\}) \geq 0 & \& \ \Delta_{i}\mathcal{U}_{i}(\mathcal{J}') \geq 0 \right) \\ \text{or } \Delta_{i}\mathcal{U}_{i}(\mathcal{J}') < 0 \end{array}$$

#### Welfare and Pareto weights

Welfare:

$$\mathcal{W}(\mathbb{J}) = \sum_{i \in \mathbb{I}} \omega_i \ u(c_i)$$

• Pareto weights  $\omega_i$ :

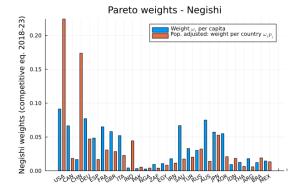
$$\omega_i = \frac{1}{u'(\bar{c}_i)}$$

for  $\bar{c}_i$  consumption in initial equilibrium "without climate change", i.e. year = 2020

• Imply no redistribution motive in t = 2020

$$\omega_i u'(\bar{c}_i) = \omega_j u'(\bar{c}_j) \quad \forall i, j \in \mathbb{I}$$

 Climate change, taxation, and climate agreement (tax + tariffs) have redistributive effects
 ⇒ change distribution of c<sub>i</sub>



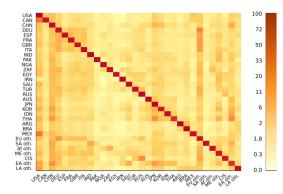
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#### Quantification – Trade model

• Armington Trade model:

$$s_{ij} \equiv \frac{c_{ij}p_{ij}}{c_{i}\mathbb{P}_{i}} = a_{ij}\frac{((1+t_{ij})\tau_{ij}p_{j})^{1-\theta}}{\sum_{k}a_{ik}((1+t_{ik})\tau_{ik}p_{k})^{1-\theta}}$$

- Estimated gravity equation regression:  $\log(s_{ij}) = f_i + f_j + \underbrace{\beta(1-\theta)}_{} \log d_{ij}$
- Get  $\kappa = -1.43$ , CES  $\theta = 5$  minimizing variance of  $a_{ii}$
- Iceberg cost  $\tau_{ij}$  as projection of distance  $\log \tau_{ii} = \beta \log d_{ii}$
- Preferences  $a_{ij}$  captures the remaining variation in trade shares  $s_{ij}$ , i.e.  $a_{ij} \propto (1+\bar{\mathsf{t}}_{ij})\bar{\tau}_{ij}\bar{a}_{ij}$   $\Rightarrow$  invariant to the club policies



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#### Step 0: Competitive equilibrium & Trade

- Each household in country i maximize utility and firms maximize profit
- Standard trade model results:
- Consumption and trade:

$$s_{ij} = \frac{c_{ij}p_{ij}}{c_{i}\mathbb{P}_{i}} = a_{ij}\frac{(\tau_{ij}(1+t_{ij}^{b})p_{j})^{1-\theta}}{\sum_{k} a_{ik}(\tau_{ik}(1+t_{ik}^{b})p_{k})^{1-\theta}} \qquad \qquad \& \qquad \mathbb{P}_{i} = \left(\sum_{j} a_{ij}(\tau_{ij}p_{j})^{1-\theta}\right)^{\frac{1}{1-\theta}}$$

Energy consumption doesn't internalize climate damage:

$$p_iMPe_i=q^e$$

Inequality, as measured in local welfare units:

$$\lambda_i = u'(c_i)$$

• "Local Social Cost of Carbon", for region i

$$LCC_{i} = -\frac{\partial \mathcal{W}_{i}/\partial \mathcal{E}}{\partial \mathcal{W}_{i}/\partial c_{i}} = \frac{\psi_{i}^{\mathcal{E}}}{\lambda_{i}} \rightarrow \frac{\Delta_{i}\chi}{\rho - n + (1 - \eta)\bar{g}} (T_{i} - T_{i}^{\star}) \left[ \gamma^{y} \, \mathsf{p}_{i} \mathsf{y}_{i} + \gamma^{u} c_{i} \mathbb{P}_{i} \right] \qquad (> 0 \, \text{for warm regions})$$

## Step 1: World First-best policy

► Maximizing welfare of the world Social Planner:

$$\mathcal{W} = \max_{\{\mathbf{t}, \mathbf{e}, \mathbf{q}\}_i} \sum_{i \in \mathbb{I}} \omega_i \ u(c_i) = \sum_{\mathbb{I}} \mathcal{W}_i$$

- Full array of instruments: cross-countries lump-sum transfers  $\mathbf{t}_i^{ls}$ , unrestricted individual carbon taxes  $\mathbf{t}_i^{\varepsilon}$  on energy  $e_i^f, e_i^c$ , unrestricted bilateral tariffs  $\mathbf{t}_{ii}^{ls}$
- Budget constraint:  $\sum_i t_i^{ls} = \sum_i t_i^f e_i^f + \sum_{i,j} t_{ij}^b c_{ij} \tau_{ij} p_j$
- Maximize welfare subject to
  - Market clearing for good i,  $[\mu_i]$ , market clearing for energy  $\mu^e$

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#### Step 1: World First-best policy

- ► Social planner allocation and decentralization:
  - Consumption:

$$\omega_i u'(c_i) = \bar{\lambda} \left[ \sum_j a_{ij} (\tau_{ij} \omega_j \mu_j)^{1-\theta} \right]^{\frac{1}{1-\theta}} = \bar{\lambda} \mathbb{P}_i \qquad \qquad \omega_i \frac{u'(c_i)}{\mathbb{P}_i} = \bar{\lambda}$$

• Energy use:

$$\omega_i \mu_i MPe_i = \mu^e + SCC$$

Social cost of carbon:

$$SCC 
ightarrow \sum_{j} \omega_{j} \frac{\Delta_{j} \chi}{\rho - n + (1 - \eta) \overline{g}} (T_{j} - T_{j}^{\star}) \left[ \gamma^{y} \mu_{j} y_{j} + \gamma^{u} c_{j} \mathbb{P}_{j} \right]$$

Decentralization:
 large transfers to equalize marg. utility + carbon tax = SCC

$$\mathbf{t}^{\varepsilon} = SCC = \sum_{i} \omega_{j} LCC_{j} \qquad \mathbf{t}_{i}^{lb} = c_{i}^{\star} \mathbb{P}_{i} - w_{i} \ell_{i} - \pi_{i}^{f} \qquad s.t. \quad \omega_{i} u'(c_{i}^{\star}) = \bar{\lambda} \mathbb{P}_{i}$$

## Step 2: World optimal Ramsey policy

Maximizing welfare of the world Social Planner:

$$\mathcal{W} = \max_{\{\mathbf{t}, \mathbf{e}, \mathbf{q}\}_i} \sum_{i \in \mathbb{I}} \omega_i \ u(c_i) = \sum_{\mathbb{I}} \mathcal{W}_i$$

- One single instrument: uniform carbon tax  $t^f$  on energy  $e_i^f$
- Rebate tax lump-sum to HHs  $t_i^{ls} = t^{\varepsilon} e_i^f + t^{\varepsilon} e_i^c$
- Ramsey policy: Primal approach, maximize welfare subject to
  - Budget constraint  $[\lambda_i]$ , Market clearing for good  $[\mu_i]$ , market clearing for energy

  - Optimality (FOC) conditions for good demands  $[\eta_{ii}]$ , energy demand  $[v_i]$  & supply  $[\theta_i]$ , etc.
  - Trade-off faced by the planner:
    - (i) Correcting climate externality, (ii) Redistributive effects, (iii) Distort energy demand and supply (iv) Distort/reallocate final good demand



## Step 2: World optimal Ramsey policy

- ► The planner takes into account
  - (i) the marginal value of wealth  $\lambda_i$
  - (ii) the shadow value of good i, from market clearing,  $\mu_i$ :
  - (iii) the shadow value of bilateral trade ij, from household FOC,  $\eta_{ij}$ :

w/ free trade 
$$u'(c_i) = \lambda_i$$
 vs. w/ Armington trade 
$$u'(c_i) = \lambda_i \Big( \sum_{j \in \mathbb{I}} a_{ij} (\tau_{ij} \mathbf{p}_j)^{1-\theta} \Big[ 1 + \frac{\omega_j}{\omega_i} \frac{\mu_j}{\lambda_i} - \frac{\eta_{ij}}{\theta \lambda_i} (1 - s_{ij}) \Big]^{1-\theta} \Big)^{\frac{1}{1-\theta}}$$

Relative welfare weights, representing inequality

$$\widehat{\lambda}_i = \frac{\omega_i \lambda_i}{\overline{\lambda}} = \frac{\omega_i u'(c_i)}{\frac{1}{I} \sum_{\overline{1}} \omega_j u'(c_j)} \leq 1 \qquad \Rightarrow \qquad \begin{array}{c} \text{ceteris paribus, poorer} \\ \text{countries have higher } \widehat{\lambda}_i \end{array}$$

#### Step 2: Optimal policy – Social Cost of Carbon

- ► Key objects: Local vs. Global Social Cost of Carbon:
  - Marginal cost of carbon  $\psi_i^{\mathcal{E}}$  for country i
  - "Local social cost of carbon" (LCC) for region *i*:

$$LCC_{i} := \frac{\partial \mathcal{W}_{i}/\partial \mathcal{E}}{\partial \mathcal{W}_{i}/\partial w_{i}} = \frac{\psi_{i}^{\mathcal{E}}}{\lambda_{i}} \rightarrow \frac{\Delta_{i}\chi}{\rho - n + (1 - \eta)\bar{g}} (T_{i} - T_{i}^{\star}) \left[ \gamma^{y} p_{i} y_{i} + \gamma^{u} c_{i} \mathbb{P}_{i} \right]$$

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• Social Cost of Carbon for the planner:

$$SCC := \frac{\partial \mathcal{W}/\partial \mathcal{E}}{\partial \mathcal{W}/\partial w} = \frac{\sum_{\mathbb{I}} \omega_i \psi_i^{\mathcal{E}}}{\frac{1}{I} \sum_{\mathbb{I}} \omega_i \lambda_i}$$

Social Cost of Carbon integrates these inequalities:

$$SCC = \sum_{\mathbb{T}} \widehat{\lambda}_i LCC_i = \sum_{\mathbb{T}} \omega_i LCC_i + \mathbb{C}ov_i(\widehat{\lambda}_i, LCC_i)$$

#### Step 2: Optimal policy – Other motives

- ► Taxing fossil energy has additional redistributive effects:
  - 1. Through energy markets: distort supply, lowers eq. fossil price, benefit net importers
  - 2. Distort energy demand, of countries that need more or less energy
  - 3. Reallocate goods production, which is then supplied internationally

Supply Redistrib 
$$^{\circ sb}$$
 + Demand Distort  $^{\circ sb}$  - Trade effect  $^{sb}$  =  $\underbrace{\mathcal{C}_{EE}^{f}}_{\text{agg. supply}}\underbrace{\mathbb{C}\text{ov}_{i}\left(\widehat{\lambda}_{i},e_{i}^{f}-e_{i}^{x}\right)}_{\text{energy T-o-T}}$  -  $\underbrace{\mathbb{C}\text{ov}_{i}\left(\widehat{\upsilon}_{i},\frac{d\left(1-s_{i}^{e}\right)}{\sigma_{i}e_{i}}\right)}_{\text{demand distortion}}$  -  $\underbrace{q^{f}\underbrace{\mathbb{E}_{j}\left[\widehat{\mu}_{j}\right]}_{\text{good T-o-T redistrib}^{\circ}}$ 

 $\circ$  Params:  $\mathcal{C}_{EE}^f$  agg. fossil inv. elasticity,  $s_i^e$  energy cost share and  $\sigma_i$  energy demand elasticity

## Step 2: Optimal policy – Other motives

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Supply Redistrib sb + Demand Distort - Trade effect 
$$effect^{sb} = \underbrace{\mathcal{C}_{EE}^f}_{agg. supply} \underbrace{\mathbb{C}ov_i\left(\widehat{\lambda}_i, e_i^f - e_i^x\right)}_{energy \text{ T-o-T}} - \underbrace{\mathbb{C}ov_i\left(\widehat{v}_i, \frac{d'(1-s_i^e)}{\sigma_i e_i}\right)}_{demand \\ distortion} - \underbrace{q^f \underbrace{\mathbb{E}_j\left[\widehat{\mu}_j\right]}_{good \text{ T-o-T}}}_{redistrib}$$

- $\circ$  Params:  $\mathcal{C}_{EE}^f$  agg. fossil inv. elasticity,  $s_i^e$  energy cost share and  $\sigma_i$  energy demand elasticity
- ► *Proposition 2:* Optimal fossil energy tax:

$$\Rightarrow$$
  $\mathbf{t}^f = SCC^{sb} + \text{Supply Redistribution}^{sb} + \mathbf{Demand Distortion}^{sb} - \mathbf{Trade effect}^{sb}$ 

Reexpressing demand terms:

$$\mathbf{t}^{\varepsilon} = \left(1 + \mathbb{C}\mathrm{ov}_{i}(\widehat{\lambda}_{i}^{w}, \frac{\widehat{\sigma_{i}e_{i}}}{1 - s_{i}^{\varepsilon}})\right)^{-1} \left[\sum_{\mathbb{I}} \omega_{i} LCC_{i} + \mathbb{C}\mathrm{ov}_{i}(\widehat{\lambda}_{i}^{w}, LCC_{i}) + \mathcal{C}_{EE}^{f} \mathbb{C}\mathrm{ov}_{i}(\widehat{\lambda}_{i}^{w}, e_{i}^{f} - e_{i}^{x}) - q^{f} \mathbb{E}_{j}[\widehat{\mu}_{j}]\right]$$

## Step 3: Ramsey Problem with participation constraints

- Consider that countries can "exit" climate agreement.
- ▶ For a climate "club" of  $\mathbb{J} \subset \mathbb{I}$  countries:
  - Countries  $i \in \mathbb{J}$  are subject to a carbon tax  $t^f$
  - Countries  $i \in \mathbb{J}$  can unilaterally leave, subject to retaliation tariff  $\mathbf{t}^{b,r}$  on goods and get consumption  $\tilde{c}_i$
  - Countries  $i \notin \mathbb{J}$  trade in goods subject to tariff  $t^b$  with club members and countries outside the club. They still trade with the club members in energy at price  $q^f$

# Step 3: Ramsey Problem with participation constraints

- ► Consider that countries can "exit" climate agreement.
- ▶ For a climate "club" of  $\mathbb{J} \subset \mathbb{I}$  countries:
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  - Countries  $i \notin \mathbb{J}$  trade in goods subject to tariff  $t^b$  with club members and countries outside the club. They still trade with the club members in energy at price  $q^f$
- ► Participation constraints:

$$u(c_i) \geq u(\tilde{c}_i)$$
  $[\nu_i]$ 

► Welfare:

$$\mathcal{W} = \max_{\{\mathbf{t}, \mathbf{e}, \mathbf{q}\}_i} \sum_{\mathbb{J}} \omega_i \ u(c_i) + \sum_{\mathbb{J}^c} \alpha \omega_i \ u(c_i)$$

# Step 3: Ramsey Problem with participation constraints

► Participation constraints

$$u(c_i) \geq u(\tilde{c}_i)$$
  $[\nu_i]$ 

- ► Second-Best social valuation with participation constraints
  - Participation incentives change our "social welfare weights"  $\widehat{\widetilde{\lambda}}_i \propto \omega_i (1+\nu_i) u'(c_i)$

w/ Armington trade 
$$(1+\nu_i)u'(c_i) = \lambda_i \Big( \sum_{j \in \mathbb{I}} a_{ij} (\tau_{ij} \mathbf{p}_j)^{1-\theta} \Big[ 1 + \frac{\omega_j}{\omega_i} \frac{\mu_j}{\lambda_i} - \frac{\eta_{ij}}{\theta \lambda_i} (1-s_{ij}) \Big]^{1-\theta} \Big)^{\frac{1}{1-\theta}} = \lambda_i \mathbb{P}_i$$

$$\Rightarrow \qquad \qquad \widehat{\lambda}_i = \frac{\omega_i (1+\nu_i)u'(c_i)}{\frac{1}{J} \sum_{\mathbb{J}} \omega_j (1+\nu_j)u'(c_j)} \neq \widehat{\lambda}_i$$

• Similarly, the "effective Pareto weights" are  $\alpha\omega_i$  for countries outside the club  $i \notin \mathbb{J}$ 

## Step 3: Participation constraints & Optimal policy

- ► *Proposition 3.2:* Second-Best taxes:
  - Taxation with imperfect instruments:
    - Climate change & general equilibrium effects on fossil market affects all countries  $i \in \mathbb{I}$
    - Need to adjust for the "outside" countries  $i \notin \mathbb{J}$  not subject to the tax, which weight on the energy market as  $\vartheta_{\mathbb{J}^c} \approx \frac{E_{\mathbb{J}^c}}{E_{\mathbb{I}}} \frac{\nu \sigma}{q^f(1-s^f)}$  with  $\nu$  fossil supply elasticity,  $\sigma$  energy demand elasticity and  $s^f$  energy cost share.
  - Optimal fossil energy tax  $t^f(\mathbb{J})$ :

$$\Rightarrow \quad \mathfrak{t}^f(\mathbb{J}) = SCC + \text{Supply Redistrib}^{\circ sb} + \text{Demand Distort}^{\circ sb} - \text{Trade effect}^{sb}$$

$$= \frac{1}{1 - \vartheta_{\mathbb{J}^c}} \sum_{i \in \mathbb{J}} \widetilde{\lambda}_i LCC_i + \frac{1}{1 - \vartheta_{\mathbb{J}^c}} \mathcal{C}_{EE}^f \sum_{i \in \mathbb{J}} \widetilde{\lambda}_i (e_i^f - e_i^x) - \sum_{i \in \mathbb{J}} \widetilde{\upsilon}_i \frac{q^f (1 - s_i^f)}{\sigma e_i^f}$$

• Optimal tariffs/export taxes  $t_{ij}^b(\mathbb{J})$  for  $j \notin \mathbb{J}$ As of now, only opaque system of equations (fixed point w/ demand/multipliers)

#### Step 4: Unilateral optimal policy

Unilateral Social Planner maximizing local welfare

$$\mathcal{W}_i = \max_{\mathbf{t}_i, c_i} u(c_i)$$

- Instruments: local carbon taxes  $t_i^{\varepsilon}$  on energy  $e_i^f, e_i^c$ , unrestricted bilateral tariffs  $t_{ij}^b$ , and lump-sum rebate to the household.
- Maximize welfare subject to the market clearing for good j,  $[\mu_j^{(i)}]$ , market clearing for fossil energy  $\mu^{f(i)}$  and local optimality conditions
- Unilateral tariffs:

$$\mathbf{t}_{ij}^b = \omega_j^{(i)} \frac{\mu_j^{(i)}}{\lambda_i}$$

• Terms of trade manipulation weighted by  $\omega_j^{(i)}$ : the more planner i internalizes the good j's market clearing, the higher the tariffs. Small Open Econ:  $\omega_j^{(i)} := 0$ 

#### Step 4: Unilateral optimal policy

- ► Social planner *i* allocation and local social cost of carbon:
  - Local Cost of Carbon:

$$LCC_{i} = -\frac{\partial W_{i}/\partial \mathcal{E}}{\partial W_{i}/\partial c_{i}} \rightarrow \frac{\chi}{\rho - n + (1 - \eta)\bar{g}} \left( \Delta_{i} (T_{i} - T_{i}^{\star}) \left[ \gamma^{y} p_{i} y_{i} + \gamma^{u} c_{i} \mathbb{P}_{i} \right] + \sum_{j} \omega_{j}^{(i)} \frac{\mu_{j}^{(i)}}{\lambda_{i}} \Delta_{j} (T_{j} - T_{j}^{\star}) \gamma^{y} p_{j} y_{j} \right)$$

- International trade makes the LCC<sub>i</sub> correlated across regions due to goods-trade linkages (≈ spatial diffusion of climate shocks from region j)
- ► Optimal local carbon tax:

$$\mathsf{t}_i^\varepsilon = -q^f \frac{\mu_i^{(i)}}{\lambda_i} + q^f \nu_i \frac{e_i^f - e_i^x}{e_i^x} + LCC_i$$

- Internalizes (i) good production distortion  $\mu_i^{(i)}$ , (ii) energy supply redistribution (w/  $\nu_i$  inverse supply elasticity), and (iii) Pigouvian motives  $LCC_i$ .
- The tax becomes a carbon *subsidy* if oil-gas exports are large  $e_i^x > e_i^f$ , and if the local cost of carbon  $LCC_i$  is small

#### Quantification – Firms

▶ Production function  $y_i = \mathcal{D}_i^y(T_i)z_iF(k,\varepsilon(e^f,e^r))$ 

$$F_{i}(\varepsilon(e^{f}, e^{c}, e^{r}), \ell) = \left[ (1 - \epsilon)^{\frac{1}{\sigma_{y}}} (\bar{k}^{\alpha} \ell^{1 - \alpha})^{\frac{\sigma_{y} - 1}{\sigma_{y}}} + \epsilon^{\frac{1}{\sigma_{y}}} (z_{i}^{e} \varepsilon_{i}(e^{f}, e^{c}, e^{r}))^{\frac{\sigma_{y} - 1}{\sigma_{y}}} \right]^{\frac{\sigma_{y}}{\sigma_{y} - 1}}$$

$$\varepsilon_{i}(e^{f}, e^{c}, e^{r}) = \left[ (\omega^{f})^{\frac{1}{\sigma_{e}}} (e^{f})^{\frac{\sigma_{e} - 1}{\sigma_{e}}} + (\omega^{c})^{\frac{1}{\sigma_{e}}} (e^{c})^{\frac{\sigma_{e} - 1}{\sigma_{e}}} + (\omega^{r})^{\frac{1}{\sigma_{e}}} (e^{r})^{\frac{\sigma_{e} - 1}{\sigma_{e}}} \right]^{\frac{\sigma_{e}}{\sigma_{e} - 1}}$$

- Calibrate TFP  $z_i$  to match  $y_i = GDP_i$  per capita in 2019-23 (avg. PPP).
- Technology:  $\omega^f = 56\%$ ,  $\omega^c = 27\%$ ,  $\omega^f = 17\%$ ,  $\epsilon = 12\%$  for all i
- Calibrate  $(z_i^e)$  to match Energy/GDP  $q^e e_i/p_i v_i$
- ▶ Damage functions in production function *y*:

$$\mathcal{D}_{i}^{y}(T) = e^{-\gamma_{i}^{\pm,y}(T - T_{i}^{\star})^{2}}$$

- Asymmetry in damage to match empirics with  $\gamma^y = \gamma^{+,y} \mathbb{1}_{\{T > T^*\}} + \gamma^{-,y} \mathbb{1}_{\{T < T^*\}}$
- Symmetric damage:  $\gamma_i^{\pm,y} = \bar{\gamma}^{\pm,y} \& T_i^{\star} = \bar{\alpha} T_{it_0} + (1 \bar{\alpha}) T^{\star}$

# Quantification – Energy markets

- ► Fossil production  $e_{it}^x$  and reserve  $\mathcal{R}_{it}$ 
  - Cost  $C_i(e^x, \mathcal{R}) = \frac{\bar{\nu}_i}{1+\nu_i} \left(\frac{e^x}{\mathcal{R}}\right)^{1+\nu_i} \mathcal{R}$
  - Now:  $\bar{\nu}_i$  to match extraction data  $e_i^x$ ,  $\mathcal{R}_{it}$  calibrated to *proven reserves* data from BP.  $\nu_i$  extraction cost curvature to match profit  $\pi_i^f = \frac{\bar{\nu}_i \nu_i}{1 + \nu_i} (\frac{e_i^x}{\mathcal{R}_i})^{\nu_i} \mathcal{R}_i \mathbb{P}_i$
  - Future: Choose  $(\bar{\nu}_i, \nu_i, \mathcal{R}_i)$  to match marginal cost  $C_e$  & extraction data  $e_i^x$  (BP, IEA)
- ► Coal and Renewable: Production  $\bar{e}_i^r$ ,  $\bar{e}_i^x$  and price  $q_i^c$ ,  $q_i^r$ 
  - Calibrate  $q_i^c = z^c \mathbb{P}_i$ ,  $q_{it}^r = z^r \mathbb{P}_i$ Choose  $z_i^c$ ,  $z_i^r$  to match the energy mix  $(e_i^f, e_i^c, e_i^r)$
- ► Population dynamics
  - Match UN forecast for growth rate / fertility

back

#### Calibration Table: Baseline calibration ( $\star$ = subject to future changes) back

Techno	ology & Energy m	narkets		
$\alpha$	0.35	Capital share in $F(\cdot)$	Capital/Output ratio	
$\epsilon$	0.12	Energy share in $F(\cdot)$	Energy cost share (8.5%)	
$\sigma$	0.3	Elasticity capital-labor vs. energy	Complementarity in production (c.f. Bourany 2022)	
$\omega^f$	0.56	Fossil energy share in $e(\cdot)$	Oil-gas/Energy ratio	
$\omega^c$	0.27	Coal energy share in $e(\cdot)$	Coal/Energy ratio	
$\omega^r$	0.17	Non-carbon energy share in $e(\cdot)$	Non-carbon/Energy ratio	
$\sigma_e$	2.0	Elasticity fossil-renewable	Slight substitutability & Study by Stern	
$\delta$	0.06	Depreciation rate	Investment/Output ratio	
$\bar{g}$	0.01*	Long run TFP growth	Conservative estimate for growth	
Preferences & Time horizon				
$\rho$	0.015	HH Discount factor	Long term interest rate & usual calib. in IAMs	
$\eta$	1.5	Risk aversion	Standard Calibration	
n	0.0035	Long run population growth	Average world population growth	
Climate parameters				
$\xi^f, \xi^c$	2.761 & 3.961	Emission factor - Oil+nat. gas vs. Coal	Conversion 1 $MTOE \Rightarrow 1 MT CO_2$	
χ	2.3/1e6	Climate sensitivity	Pulse experiment: $100  GtC \equiv 0.23^{\circ} C$ medium-term warming	
$egin{array}{c} \chi \ \delta_s \ \gamma^\oplus \end{array}$	0.0004	Carbon exit from atmosphere	Pulse experiment: $100  GtC \equiv 0.15^{\circ}  C  \text{long-term warming}$	
$\gamma^\oplus$	0.003406	Damage sensitivity	Nordhaus, Barrage (2023)	
$\alpha^T$	0.5	Weight historical climate for optimal temp.	Marginal damage correlated with initial temp.	
$T^{\star}$	14.5	Optimal yearly temperature	Average yearly temperature/Developed economies	

# Matching country-level moments

#### Table: Heterogeneity across countries

Model parameter	Matched variable from the data	Source
Country size $P_i$ Firm productivity $z_i$	Population GDP per capita (2019-PPP)	UN WDI
Energy-augmenting productivity $z_i^e$ Cost of coal production $C_i^c$ Cost of non-carbon production $C_i^r$	Energy cost share Energy mix/coal share $e_i^c/e_i$ Energy mix/coal share $e_i^r/e_i$	SRE SRE SRE
Initial temperature $T_{it_0}$ Pattern scaling $\Delta_i$	Pop-weighted yearly temperature Sensitivity of $T_{it}$ to world $T_t$	Burke et al Burke et al
Reserves $\mathcal{R}_i$ Slope of extraction cost $\bar{\nu}_i$ Curvature of extraction cost $\nu_i$	Proved Oil-gas reserves Oil-gas extracted/produced $e_i^x$ Profit $\pi_i^f$ / energy rent	SRE SRE WDI
Distance iceberg costs $\tau_{ij}$ CES preferences $a_{ij}$	Geographical distance $ au_{ij} = d_{ij}^{eta}$ Trade flows	CEPII CEPII
	Country size $\mathcal{P}_i$ Firm productivity $z_i$ Energy-augmenting productivity $z_i^e$ Cost of coal production $\mathcal{C}_i^c$ Cost of non-carbon production $\mathcal{C}_i^r$ Initial temperature $T_{it_0}$ Pattern scaling $\Delta_i$ Reserves $\mathcal{R}_i$ Slope of extraction cost $\bar{\nu}_i$ Curvature of extraction cost $\nu_i$ Distance iceberg costs $\tau_{ij}$	Country size $\mathcal{P}_i$ Population Firm productivity $z_i$ Energy-augmenting productivity $z_i^e$ Energy cost share Cost of coal production $\mathcal{C}_i^c$ Energy mix/coal share $e_i^c/e_i$ Cost of non-carbon production $\mathcal{C}_i^r$ Energy mix/coal share $e_i^c/e_i$ Initial temperature $T_{it_0}$ Pop-weighted yearly temperature Pattern scaling $\Delta_i$ Sensitivity of $T_{it}$ to world $\mathcal{T}_i$ Reserves $\mathcal{R}_i$ Proved Oil-gas reserves Slope of extraction cost $\bar{\nu}_i$ Oil-gas extracted/produced $e_i^x$ Curvature of extraction cost $\nu_i$ Profit $\pi_i^f$ / energy rent Distance iceberg costs $\tau_{ij}$ Geographical distance $\tau_{ij} = d_{ij}^{\beta}$

#### Theoretical investigation: decomposing the welfare effects

- **Experiment:** 
  - Start from the equilibrium where carbon tax  $\mathbf{t}_{j}^{\varepsilon} = 0, \mathbf{t}_{jk}^{b} = 0, \forall j,$
  - Change in welfare: Linear approximation around that point  $\Rightarrow$  small changes in carbon tax  $dt_i^{\varepsilon}$ ,  $\forall j$  and tariffs  $dt_{i,k}^{b}$ ,  $\forall j, k$  for a club  $J_i$

$$\frac{d\mathcal{U}_{i}}{u'(c_{i})} = \eta_{i}^{c} d \ln p_{i} + \left[ -\eta_{i}^{c} \bar{\gamma}_{i} \frac{1}{\bar{\nu}} - \eta_{i}^{c} s_{i}^{e} s_{i}^{f} + \eta_{i}^{\pi} (1 + \frac{1}{\bar{\nu}}) \right] d \ln q^{f} - \left[ \eta_{i}^{c} s_{i}^{e} (s_{i}^{c} + s_{i}^{r}) + \eta_{i}^{\pi} \frac{1}{\bar{\nu}} + 1 \right] d \ln \mathbb{P}_{i}$$

• GE effect on energy markets  $d \ln q^f \approx \bar{\nu} d \ln E^f + \dots$ , due to taxation

$$d \ln q^f = -\frac{\bar{\nu}}{1 + \bar{\gamma} + \mathbb{C}\text{ov}_i(\widetilde{\lambda}_i^f, \bar{\gamma}_i) + \bar{\nu}\overline{\lambda}^{\sigma,f}} \sum_i \widetilde{\lambda}_i^f \mathbf{J}_i d\mathfrak{t}^{\varepsilon} + \sum_i \beta_i d \ln \mathfrak{p}_i$$

- Climate damage  $\bar{\gamma}_i = \gamma (T_i T_i^{\star}) T_i s^{E/S}$
- Trade and leakage effect: GE impact of  $t_i^{\varepsilon}$  and  $t_i^{b}$  on  $y_i$  and  $p_i$
- $\circ$  Params:  $\sigma$  energy demand elast<sup>y</sup>,  $s^e$  energy cost share,  $\bar{\nu}$  energy supply inverse elas<sup>y</sup>



# Welfare decomposition

- ► Armington model of trade with energy:
  - Linearized market clearing

$$\left( \frac{d\mathbf{p}_{i}}{d\mathbf{p}_{i}} + \frac{dy_{i}}{y_{i}} \right) = \sum_{k} t_{ik} \left[ \left( \frac{\mathbf{p}_{k}y_{k}}{v_{k}} \right) (d \ln \mathbf{p}_{k} + d \ln y_{k}) + \frac{q^{f}e_{k}^{x}}{v_{k}} d \ln e_{k}^{x} - \frac{q^{f}e_{k}^{f}}{v_{k}} d \ln e_{k}^{f} + \frac{q^{f}(e_{k}^{x} - e_{k}^{f})}{v_{k}} d \ln q^{f} \right.$$

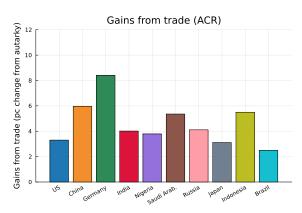
$$\left. + \theta \sum_{h} \left( s_{kh} d \ln t_{kh} - (1 + s_{ki}) d \ln t_{ki} \right) + (\theta - 1) \sum_{h} \left( s_{kh} d \ln \mathbf{p}_{h} - d \ln \mathbf{p}_{i} \right) \right]$$

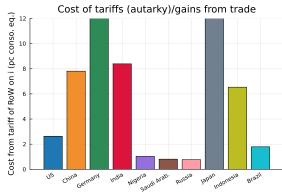
• Fixed point for price level 
$$d \ln p_i$$

$$\left[ (\mathbf{I} - \mathbf{T} \odot v^y) [\mathbf{I} - \alpha^{y,p} \odot \mathbf{I}] + \mathbf{T} (v^{e^x} \odot \frac{1}{\nu}) + \mathbf{T} v^{e^f} \frac{\sigma^y}{1 - s^e} - (\theta - 1) (\mathbf{T} \mathbf{S} - \mathbf{T}') - \left( (\mathbf{I} - \mathbf{T} \odot v^y) \alpha^{y,z} - \frac{\sigma^y}{1 - s^e} \right) \odot \bar{\gamma} \mathbf{I} \odot (\frac{\lambda^x}{\nu})' \right] d \ln p = \left[ - (\mathbf{I} - \mathbf{T} \odot v^y) \alpha^{y,qf} + \mathbf{T} (v^{e^x} \odot \frac{1}{\nu} + v^{e^f} \frac{\sigma^y}{1 - s^e} + v^{ne}) - \left( (\mathbf{I} - \mathbf{T} \odot v^y) \alpha^{y,z} - \frac{\sigma^y}{1 - s^e} \right) \bar{\gamma} \frac{1}{\bar{\nu}} \right] d \ln q^f + \left[ - (\mathbf{I} - \mathbf{T} \odot v^y) \alpha^{y,qf} + \mathbf{T} (v^{e^f} \odot \frac{\sigma^y}{1 - s^e}) \right] \odot J d \ln t^{\varepsilon} + \theta \left( \mathbf{T} \mathbf{S} \odot \mathbf{J} \odot d \ln t^b - \mathbf{T} (\mathbf{1} + \mathbf{S}') \odot (\mathbf{J} \odot d \ln t^b)' \right)$$

#### Trade-off – Gains from trade

Gains from trade (ACR) vs. loss from tariffs/autarky in this model back





#### Climate agreement and welfare

Recover 92% of welfare gains, i.e. 6% out of 6.5% conso equivalent.

