

Redistribution and the wage-price dynamics: Optimal fiscal and monetary policy

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Introduction

Motivation: Surge in inflation since 2020 partly handled with fiscal tools in Europe (tax shields) – but also more standard monetary tools.

→ **What is the right fiscal-monetary mix to deal with inflation while accounting for distributional issues?**

HANK models: credible setup to analyze these questions. But with rigidities?

- Debate about the “right” rigidity ([Auclert et al. 2023a](#)).
- With price rigidity alone: small role for inflation ([LeGrand et al. 2023](#)).

→ introduce both *wage* and *price* rigidities.

Introduction

Question: **What is the optimal joint monetary and fiscal policy with a rich set of tools, when both prices and wages are rigid after negative TFP (energy) shock?**

A small literature (with RANK and TANK) mostly.

- Blanchard (1986), Blanchard and Galí (2007a and 2007b).
- Optimal policies in Erceg et al. (2000), Galí (2015, chap. 6), Ascari et al. (2017), Lorenzoni and Werning (2023).

What we do

Theory side.

- Study HANK model with both sticky prices and sticky wages.
- Derive optimal monetary and fiscal policies with many fiscal instruments (see below).
- Compare HANK and RANK.

Quantitative side. Full-fledged quantitative model, with time-varying tax and monetary policy.

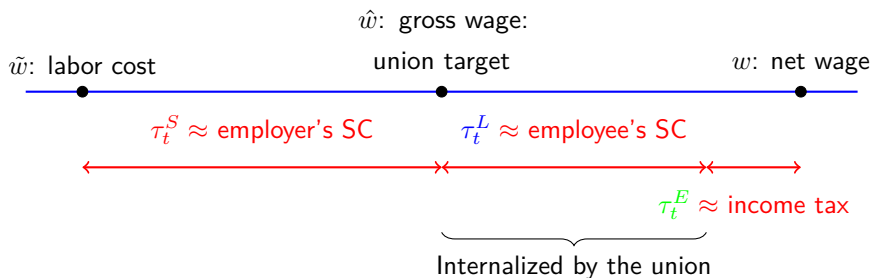
- Computation: Factorization of Lagrangian ([Marcet & Marimon, 2019](#) and [LeGrand and Ragot, 2022a](#)).
- **Refined truncation** (improving on [LeGrand and Ragot, 2022b](#)) to solve for the curse of dimensionality.

What we find

- When the fiscal system is sufficiently rich, we restore price and/or wage stability.
- Prove equivalence results (in the spirit of Correia et al. 2008-2013 for RA and LeGrand et al. 2022 for HA) but need surprisingly *many* tools.
- Identification of a fiscal instrument that is key for the monetary response: the **time-varying social contribution**.
 - When *present*, almost price-wage stability.
 - When *absent*, important deviations from price stability + $RA \neq HA$ for policy recommendations.

The Model: Households

- Stochastic idiosyncratic productivity y_t^i , first-order Markov chain (Mitman, Krueger, Perri, 2018). Aggregate TFP shock.
- Separable utility function $u(c) - v(l)$ with constant IES and constant Frisch elast. (Auclert et al., 2023b or Lorenzoni and Werning, 2023).
- Labor unions set the common labor supply L_t .
- **A rich fiscal system:**



+ capital tax τ_t^K .

The Model: Households

- agent's choices: consumption $c_{i,t} > 0$ and savings $a_{i,t} \geq 0$.
- agent's budget constraint:

$$\begin{aligned} c_{i,t} + a_{i,t} &= a_{i,t-1} + (1 - \tau_t^E) \left(\underbrace{(1 - \hat{\tau}_t^K) \tilde{r}_t a_{i,t-1}}_{\text{capital income}} + \underbrace{(1 - \tau_t^L) \hat{w}_t y_{i,t} L_t}_{\text{labor income}} \right), \\ &= a_{i,t-1} + (1 - \tau_t^K) \tilde{r}_t a_{i,t-1} + (1 - \tau_t^E)(1 - \tau_t^L) \hat{w}_t y_{i,t} L_t, \\ \hat{w}_t &= (1 - \tau_t^S) \underbrace{\tilde{w}_t}_{\text{labor cost}}. \end{aligned}$$

Sticky wages

Unions bargain for workers, same hours for all workers, Rotemberg adjustment cost for workers, as in [Auclert et al. \(2023b\)](#).

Wage Phillips curve:

$$\pi_t^W (\pi_t^W + 1) = \frac{\varepsilon_W}{\psi_W} \left(v'(L_t) - \frac{\varepsilon_W - 1}{\varepsilon_W} \frac{w_t}{1 - \tau_t^E} \int_i y_{i,t} u'(c_{i,t}) \ell(di) \right) L_t, \\ + \beta \mathbb{E}_t \left[\pi_{t+1}^W (\pi_{t+1}^W + 1) \right].$$

- π_t^W : wage inflation;
- ψ_W : cost of wage inflation and $\frac{\varepsilon_W}{\psi_W}$: slope of the Phillips curve.

Sticky prices

Firms produce with labor (CRS) with productivity Z . Rotemberg pricing for firms.

Price Phillips curve:

$$\pi_t^P(1 + \pi_t^P) = \frac{\varepsilon_P - 1}{\psi_P} \left(\frac{w_t}{Z_t(1 - \tau_t^E)(1 - \tau_t^L)(1 - \tau_t^S)} - 1 \right) + \beta \mathbb{E}_t \left[\pi_{t+1}^P(1 + \pi_{t+1}^P) \frac{Y_{t+1}}{Y_t} \right].$$

- π_t^P : price inflation;
- ψ_P : cost of wage inflation and $\frac{\varepsilon_P - 1}{\psi_P}$: slope of the Phillips curve.

Planner

Governmental budget constraint: financing of a public spending stream $(G_t)_t$:

$$G_t + (1 + r_t) \int_i a_{i,t-1} \ell(di) + w_t L_t \leq \left(1 - \frac{\psi_P}{2} (\pi_t^P)^2\right) Z_t L_t + \int_i a_{i,t} \ell(di).$$

Objective:

$$\mathbb{E}_0 \left[\sum_{t=0}^{\infty} \beta^t \int_i \omega(y_t^i) (u(c_t^i) - v(L_t)) \ell(di) - \frac{\psi_W}{2} (\pi_t^W)^2 \right]$$

- $\omega(y_t^i)$: planner's weights associated to productivity level y_t^i for solving the *inverse optimum taxation problem*, as in Heathcote and Tsujiyama (2021).

The Ramsey problem

$$\max \text{ over } (\tau_t^S, \tau_t^E, \tau_t^L, \pi_t^P, \pi_t^W, w_t, r_t, L_t, (c_{i,t}, a_{i,t})_{t \geq 0}) \text{ of} \\ \mathbb{E}_0 \left[\sum_{t=0}^{\infty} \beta^t \int_i \omega(y_t^i) (u(c_t^i) - v(L_t)) \ell(di) - \frac{\psi_W}{2} (\pi_t^W)^2 \right] \text{ s.t.:}$$

$$G_t + (1 + r_t) \int_i a_{i,t-1} \ell(di) + w_t L_t \leq \left(1 - \frac{\psi_P}{2} (\pi_t^P)^2 \right) Z_t L_t + \int_i a_{i,t} \ell(di),$$

$$\text{for all } i \in \mathcal{I}: c_{i,t} + a_{i,t} = (1 + r_t) a_{i,t-1} + w_t y_{i,t} L_t,$$

$$u'(c_{i,t}) = \beta \mathbb{E}_t \left[(1 + r_{t+1}) u'(c_{i,t+1}) \right] + \nu_{i,t},$$

$$\pi_t^W (\pi_t^W + 1) = \frac{\varepsilon_W}{\psi_W} \left(v'(L_t) - \frac{\varepsilon_W - 1}{\varepsilon_W} \frac{w_t}{1 - \tau_t^E} \int_i y_{i,t} u'(c_{i,t}) \ell(di) \right) L_t + \beta \mathbb{E}_t[\dots],$$

$$\pi_t^P (1 + \pi_t^P) = \frac{\varepsilon_P - 1}{\psi_P} \left(\frac{1}{Z_t} \frac{w_t}{(1 - \tau_t^L)(1 - \tau_t^S)(1 - \tau_t^E)} - 1 \right) + \beta \mathbb{E}_t[\dots],$$

$$(1 + \pi_t^W) \frac{w_{t-1}}{(1 - \tau_{t-1}^E)(1 - \tau_{t-1}^L)} = \frac{w_t}{(1 - \tau_t^E)(1 - \tau_t^L)} (1 + \pi_t^P)$$

Equivalence result

Proposition (An equivalence result)

When all instruments are available, the government implements an allocation with zero inflation for prices and wages in all periods.

- τ_t^E neutralizes the gap between mrs and wage \rightarrow turns off wage Phillips curve.
- τ_t^S neutralizes the gap between mpl and wage \rightarrow turns off price Phillips curve.

\Rightarrow inflation rates can be set to 0.

Remark. It *undoes* the union labor constraint. Higher welfare than in the flex-price allocation with union.

Other results

What about missing instruments?

Instruments	RA	HA
$\tau^L + \tau^S + \tau^E$	$\pi^P = 0$ and $\pi^W = 0$ (First-best)	$\pi^P = 0$ and $\pi^W = 0$ (optimal labor supply)
$\tau^L + \tau^S$	$\pi^P = 0$ and $\pi^W = 0$	$\pi^P = 0$ and $\pi^W \neq 0$ ("better" than flex P)
τ^L	$\pi^P \neq 0$ and $\pi^W = 0$	$\pi^P \neq 0$ and $\pi^W \neq 0$

- Compared to price rigidity only (Le Grand et al, 2022): +1 friction (sticky wages) but +2 tools to restore price-wage stability.
- When removing τ^E : flex-price allocation can be implemented but τ^S is used to partly undo the union labor constraint.
- Missing fiscal tools: Deviation from price-wage stability, but precise quantification is needed to assess the importance of fiscal tools.

Quantitative exercise: the numerical method

Three aspects of the method:

1. The reformulation: Lagrangian Approach (Marcet and Marimon, 2019; Le Grand and Ragot, 2022; Acikgoz et al. 2022).
 - Introduce Lagrange multipliers λ_t^i on Euler equations. $\lambda_t^i = 0$ if credit constraints bind for agents i .
 - Introduce Lagrange μ_t on the budget of the state.
 - Rearrange the Lagrangian before taking the first-order conditions.
2. Simulate the FOCs of the planner: Truncation methods.
3. Compute the weights by solving inverse optimum taxation problem, i.e., such that the **actual** fiscal system is **optimal** at the steady state.

Calibration

Parameter	Description	Value
Preference and technology		
β	Discount factor	0.99
σ	Curvature utility	2
\bar{a}	Credit limit	0
χ	Scaling param. labor supply	0.11
φ	Frisch elasticity labor supply	0.5
Shock process		
ρ_y	Autocorrelation idio. income	0.993
σ_y	Standard dev. idio. income	6%
Tax system		
τ^L	Labor tax	25%
τ^S	Labor subsidy	0%
Monetary parameters		
$(\varepsilon_p - 1)/\psi_p$	Price Phillips slope	5%
ε_w/ψ_w	Wage Phillips slope	5%
ε_p	Elasticity of sub. between goods	7
ε_w	Elasticity of sub. labor inputs	31

Quantitative assessment

Key instrument: time-varying wage tax τ_t^S .

In the *presence* of τ_t^S :

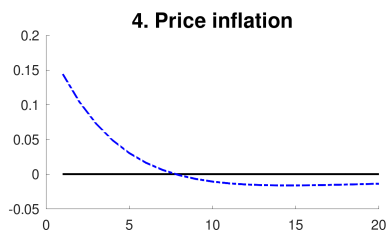
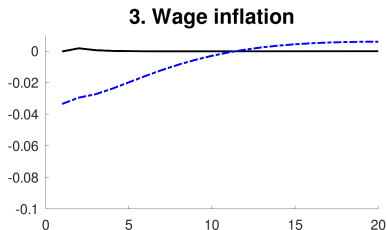
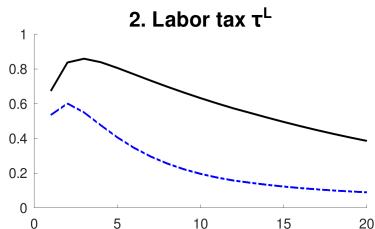
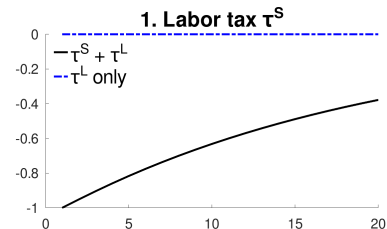
- small deviation from price-wage stability;
- quantitatively close predictions in HA and RA economies.

In the *absence* of τ_t^S :

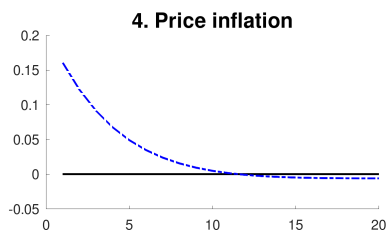
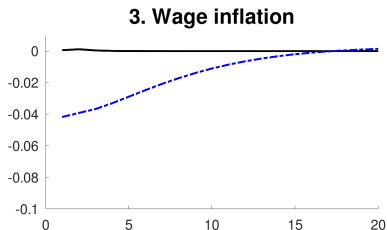
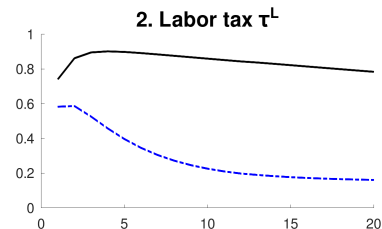
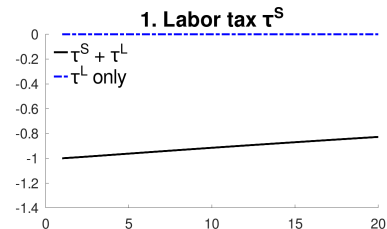
- sizable deviation from price-wage stability + (small) drop in consumption.
- Optimal policies quantitatively differ in RA and HA economies.

⇒ Relevant for fiscal and monetary policy making?

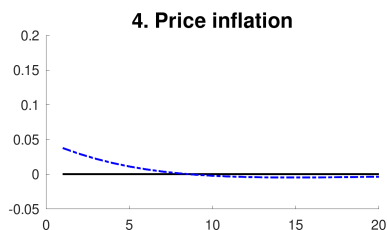
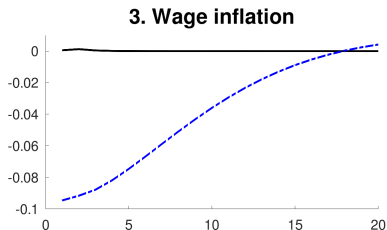
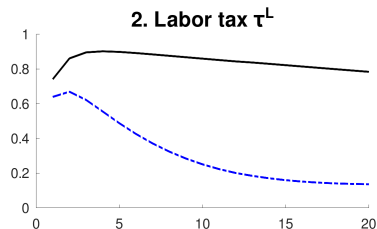
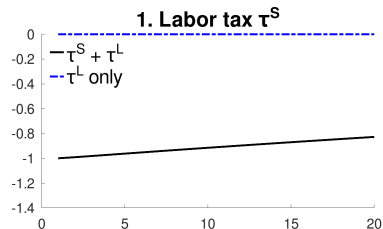
Simulation: Benchmark (0.95 persistence)



Simulation: Higher persistence (0.99)



Simulation: Role of Phillips curve slopes



Quantitative assessment (bis)

- Higher persistence increases the inflation responses (both for price and wage),...
 - ...and makes the lack of τ_t^S costlier.
 - Lowering the cost of wage inflation / increasing the cost of price inflation raises wage inflation and lowers price inflation, ...
 - ...and makes the lack of τ_t^S cheaper.
- Easier to substitute wage inflation to τ_t^S .

Conclusion

- Possible new identification of stabilization tools.
- Sticky prices + wages HANK may be a relevant environment.
- More to come on the quantitative side.