University Of Portsmouth
BSc (Hons) Computer Science
First Year

Architecture and Operating Systems (Maths)

M30943
September 2022 - May 2023
20 Credits

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Contents

S.1. Introduction To Module

27-09-2022 10:00 Zhaojie Zoom

The goal of this module is to: help with maths involved in programming; prepare for other technical units (including: databases, functional programming; discrete maths; theoretical computer science; computer vision; and more); and to gain confidence.
The maths element (this element) is 30% of the Architecture and Operating Systems module. The two components are independent until the final grade for the module is produced.

Assessments

There are two components to the assessments for this element of the module.

Online Tests

Throughout the year, there are 7 online tests which will be completed through the Pearson MyMathsLab. Overall, these tests will equal 15% of the overall module score. Each test should last for 20 minutes and has a practice test available which can be accessed anytime in the year, and as many times as you wish. The real test can only be attempted once. After you submit the test, you will get an instant score.
Calculators are permitted, however it may not always be advisable to use one.

End Of Year Test

At the end of the year, there will be an end of year test. This is equal to 15% of the overall module score.

Staff & Support

Jhaojie is the main lecturer for the module. He will be assisted by Bryan.
Outside of class, Xia and Kirsten are available from the academic tutors office to help where needed. They can be booked through Moodle.
A MathsCafe runs during term-time for drop in Maths support. It is held at the following times

- Monday 12:00-14:00, LG learning and teaching space;
- Tuesday 12:00-14:00, LG learning and teaching space;
- Wednesday, 12:00-14:00, Zoom;
- Wednesday 14:00-16:00, Library 0.36;
- Thursday 12:00-14:00, LG learning and teaching space;
- Friday 12:00-14:00, LG learning and teaching space.

When writing working out for questions, full steps should be written down. This allows errors to be found and corrected.
Take a pen and paper to practical classes.

S.2. Basic Numeracy and Basic Algebra

27-09-22 10:20 Zhaojie Zoom

Negative Numbers

Subtracting a negative number is equivalent to adding a positive number. This can be seen in the following example.

$$\begin{aligned} 2-(-5) &= \\ 2+5 &= \\ &= 7 \end{aligned}$$

The result of multiplying or dividing two numbers of the same sign is always positive.
The result of multiplying of dividing two numbers of opposing signs is always negative.

BIDMAS

The order in which to carry out operations in complex mathematical expressions is defined by the following priority list

1 Brackets

2 Indices

3 Division

3 Multiplication

4 Addition

4 Subtraction

Fractions

The names of different components of a fraction are as follows: $fraction = \dfrac{numerator}{denominator} = \dfrac{p}{q}$

Addition & Subtraction of Fractions

To add or subtract two fractions, their denominator needs to be the same. Then the addition/subtraction is performed just to the numerator. The fraction is usually then simplified.

Multiplication of Fractions

To multiply two fractions together: first, multiply the numerators together then multiply the denominators together.

Division of Fractions

To divide one fraction by another, multiply the first fraction by the inverse (reciprocal) of the second fraction. Simplify where necessary.

Simplification Of Fractions

A fraction is in its simplest form where there are no factors other than one to both the numerator and the denominator.

Algebra

The use of letters in maths is called Algebra. It defines the rules of how to manipulate with symbols.

Addition & Subtraction of like terms

Term

Either a single umber or variable, or the product of several and/or variables, for example $3y$.

Constant

A term without a symbol, for example, 2.

Like terms are multiples of the same variables; they can be added/ subtracted.

Multi-variable simplification

$$24y^2 + 7x + 12xy - 4x - 5y^2 + 3xy =$$
$$19y^2 + 15xy + 3x =$$

Multiplication algebraic expressions

The fundamental concept behind multiplication of terms is to multiply the numbers and multiply the variables (using the rules for multiplication of indices if possible), taking into account the sign rules where multiplying terms with different signs.

Multiplying algebra example

$(2a)(6ab^2) = 12a^2b^2$

Expressions

Removing Brackets

In the expression $a(b+c)$, a is multiplies by all the bracketed terms to give $ab+ac$.
In the expression $(a+b)(c+d)$, $(a+b)$ is multiplied by the other pair of brackets as individual terms. Giving the answer as $ac+ad+bc+bd$
This principle along with the principle of simplifying algebra can be used to remove brackets fromm more complex expressions.

Removing brackets from a more-complex expression

$$\begin{aligned}(x+6)(x-3) &= x(x+6) + (-3)(x+6) \\ &= x^2 + 6x - 3x - 18 \\ &= x^2 + 3x - 18\end{aligned}$$

Substitution

Where letters are replaced by actual numerical values.

Simple Linear Equations

Equations state that two quantities, usually one is known and one is not, are equal. We can use this information to solve the equation - to work out what the unknown quantity is.
A linear equation comes in the form of $ax + b = c$ where a, b and c are given numbers and x is an unknown quantity.

Solve $4x + 8 = 0$ **for** x

We can start by removing one of the known values, by subtracting 8 from both sides. This results in $4x = -8$ We can then divide both sides by 4 to get $x = -2$, which is our solution.

Basic Numeracy & Algebra Worksheet 1

02-10-22 Worksheet

1. Calculate:

$$\begin{aligned}\frac{18}{6} \times 3 - 18 + 2 \times (-4) = & \\ =&\frac{18}{6} \times 3 - 18 - 8 \\ =&3 \times 3 - 18 - 8 \\ =&9 - 18 - 8 \\ =&-9 - 8 \\ =&17\end{aligned}$$

2. Calculate:

$$\begin{aligned}\frac{12}{6} + \frac{12}{-4} + (-2) \times (-1) = & \\ =&\frac{12}{6} + \frac{12}{-4} + 2 \\ =&2 - 3 + 2 \\ =&1\end{aligned}$$

3. Calculate:

$$\begin{aligned}(-3) \times (-1) - 2 - 6 + 8 = & \\ =&3 - -4 + 8 \\ =&3 + 4 + 8 \\ =&15\end{aligned}$$

4. Calculate:

$$\begin{aligned}(3^2 \times 2 - 2) \div 2^3 = & \\ =&(9 \times 2 - 2) \div 2^3 \\ =&(18 - 2) \div 2^3 \\ =&(16) \div 2^3 \\ =&16 \div 8 \\ =&2\end{aligned}$$

5. Solve $2x - 8 = 3x - 7$ for x.

$$\begin{aligned}2x - 8 &= 3x - 7 \\ 2x - 1 &= 3x \\ -1 &= 1x\end{aligned}$$

6. Solve $4x - 8 = 2(x + 3) + 10$ for x.

$$\begin{aligned}4x - 8 &= 2x + 6 + 10 \\ 4x - 8 &= 2x + 16 \\ 4x &= 2x + 24 \\ 2x &= 24 \\ x &= 12\end{aligned}$$

7. Evaluate the expression $\frac{5}{3} - \frac{1}{3} \times \frac{9}{2}$ and write in its simplest form.

$$\begin{aligned}\frac{5}{3} - \frac{1}{3} \times \frac{9}{2} &= \\ &= \frac{5}{3} - \frac{9}{6} \\ &= \frac{30}{18} - \frac{27}{18} \\ &= \frac{3}{18} \\ &= \frac{1}{6}\end{aligned}$$

8. Evaluate the expression $\frac{7}{2} - \frac{1}{4} + \frac{6}{8}$ and write it in its simplest form.

$$\begin{aligned}\frac{7}{2} - \frac{1}{4} + \frac{6}{8} &= \\ &= \left(\frac{7}{2} - \frac{1}{4}\right) + \frac{6}{8} \\ &= \left(\frac{28}{8} - \frac{2}{8}\right) + \frac{6}{8} \\ &= \left(\frac{28}{8}\right) + \frac{6}{8} \\ &= \frac{32}{8} \\ &= \frac{16}{4} \\ &= \frac{4}{1}\end{aligned}$$

9. Simplify.

(i) $3(-7y)$
$=-21y$

(ii) $(2y)(y^2)$
$=3y^3$

(iii) $3y^2(-2y)$
$=6y^3$

(iv) $(-2y)(-2y)$
$=-4y^2$

10. Expand the following expression

$$\begin{aligned}2x(4x - \frac{1}{2}) - 4x(5 - \frac{x}{2}) &= \\ &= \ldots\end{aligned}$$

11. Expand the following expression

$$\begin{aligned}6(4x + \frac{3}{2}) - 4x(5 + \frac{x}{2} + x^2) &= \\ &= \ldots\end{aligned}$$

12. Expand the following expression

$$\begin{aligned}(x+3)(2x-6)+2 &= \\ &= (2x^2-6x+6x-18)+2 \\ &= 2x-16\end{aligned}$$

13. Expand and fully simplify the following expression

$$\begin{aligned}(2y-3)^2 &= \\ &= (2y-3)(2y-3) \\ &= 4y^2-6y-6y+9 \\ &= 4y^2-12y+9\end{aligned}$$

14. Simplify the following expression.

$$\begin{aligned}3x(x-y^2)+3(x^2+1)-7x^2y &= \\ &= 3x^2-3xy^2+3x^2+3-7x^y \\ &= 6x^2-3xy^2+3-7x^2y\end{aligned}$$