Intro to ACF and PACF

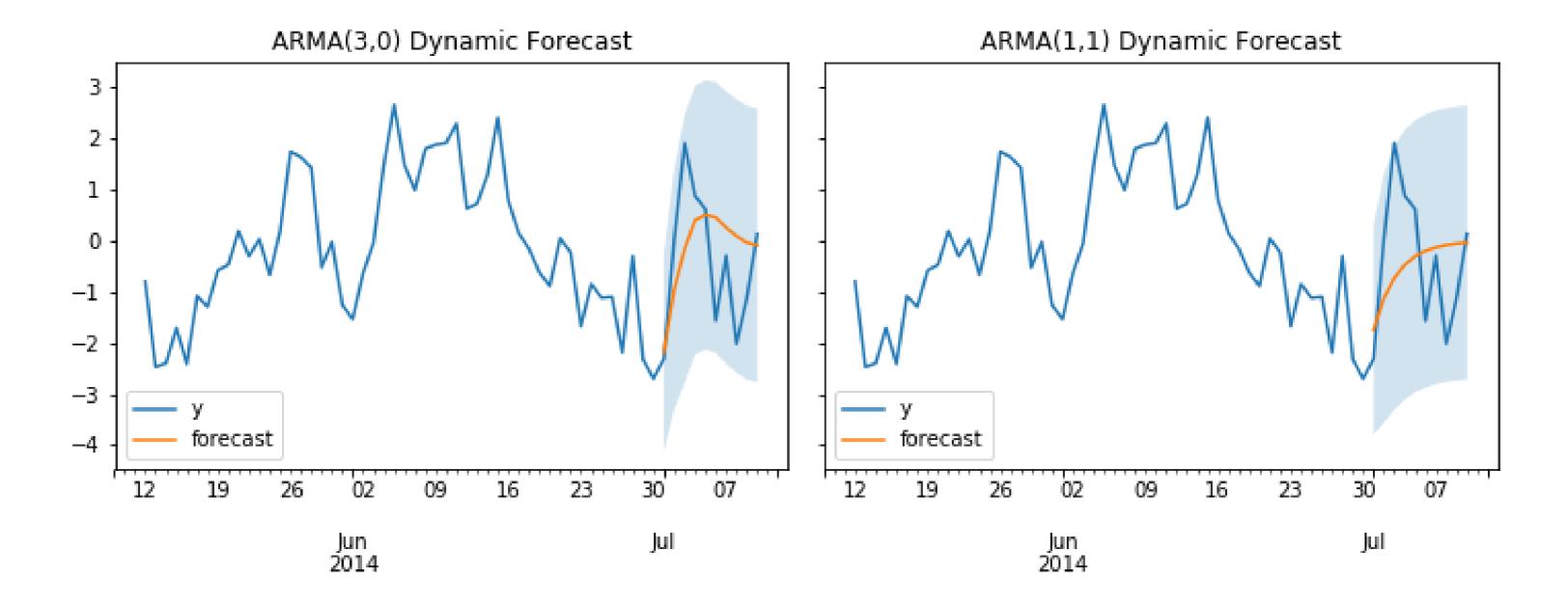
FORECASTING USING ARIMA MODELS IN PYTHON



James Fulton
Climate informatics researcher



Motivation



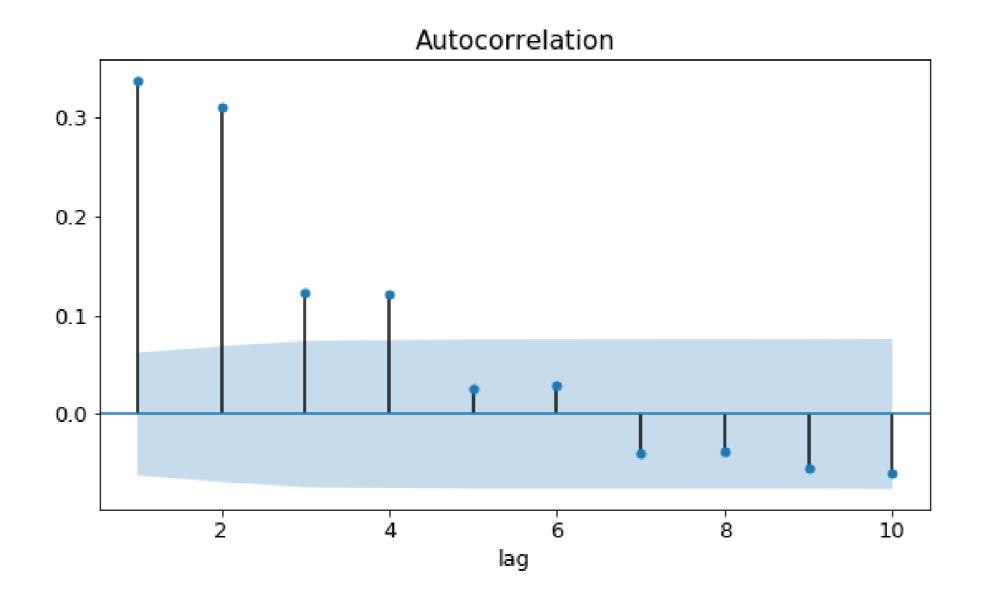
ACF and **PACF**

- ACF Autocorrelation Function
- PACF Partial autocorrelation function

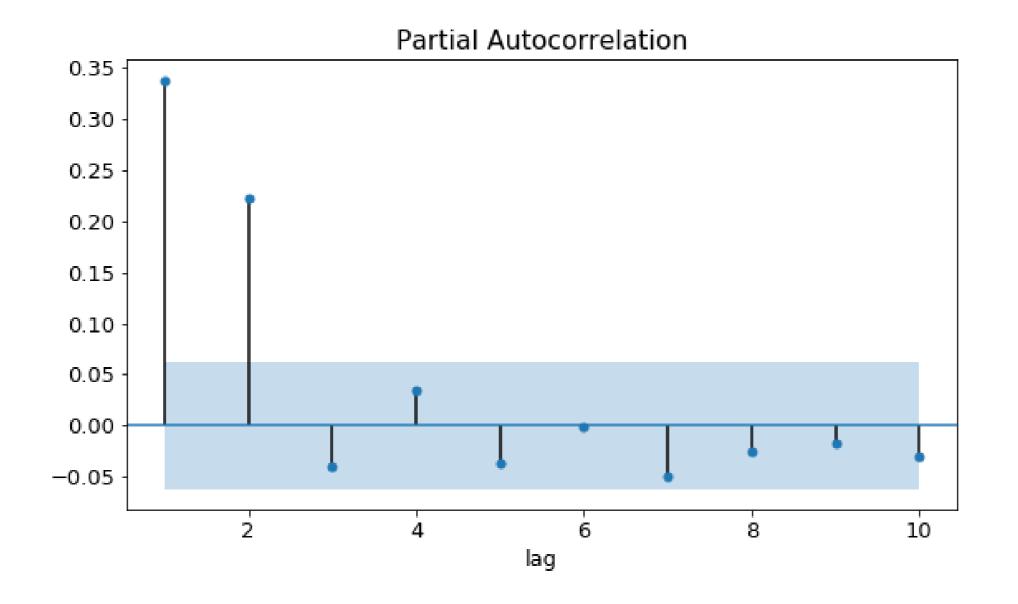
What is the ACF

- lag-1 autocorrelation $ightarrow corr(y_t, y_{t-1})$
- lag-2 autocorrelation $ightarrow corr(y_t,y_{t-2})$
- ...
- ullet lag-n autocorrelation $ightarrow corr(y_t,y_{t-n})$

What is the ACF

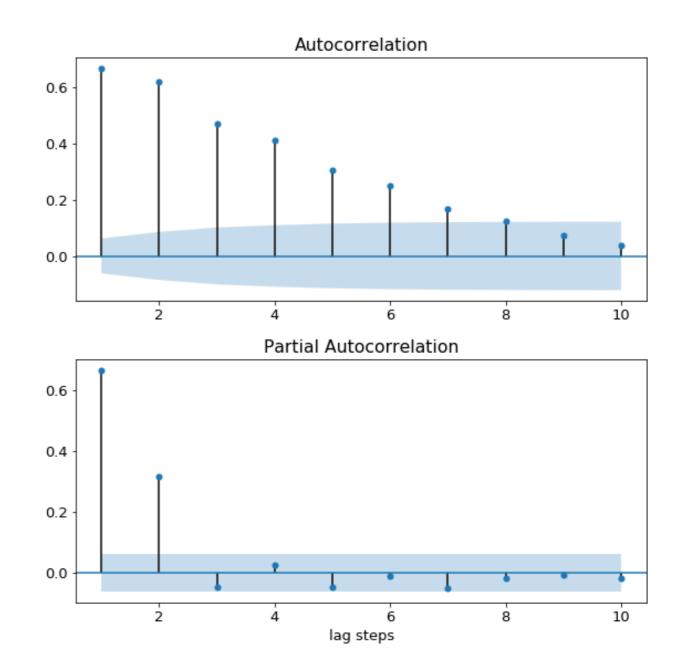


What is the PACF



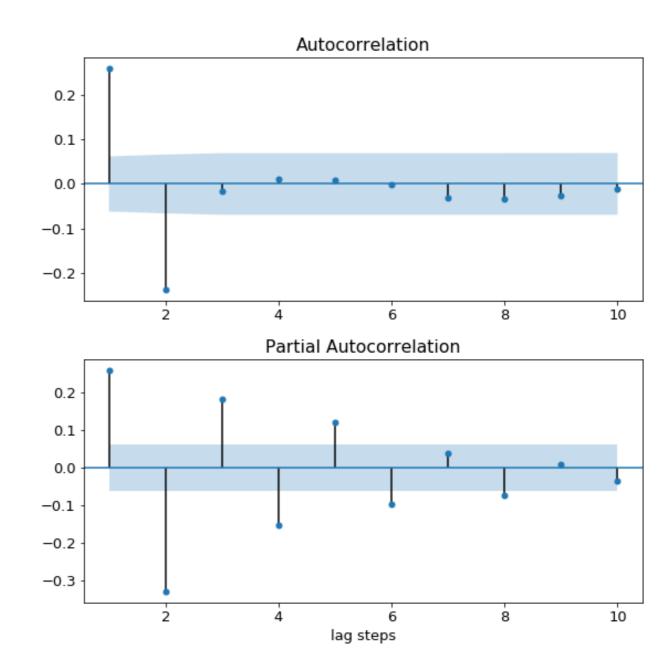
	AR(p)
ACF	Tails off
PACF	Cuts off after lag p

ullet AR(2) model o



	MA(q)
ACF	Cuts off after lag q
PACF	Tails off

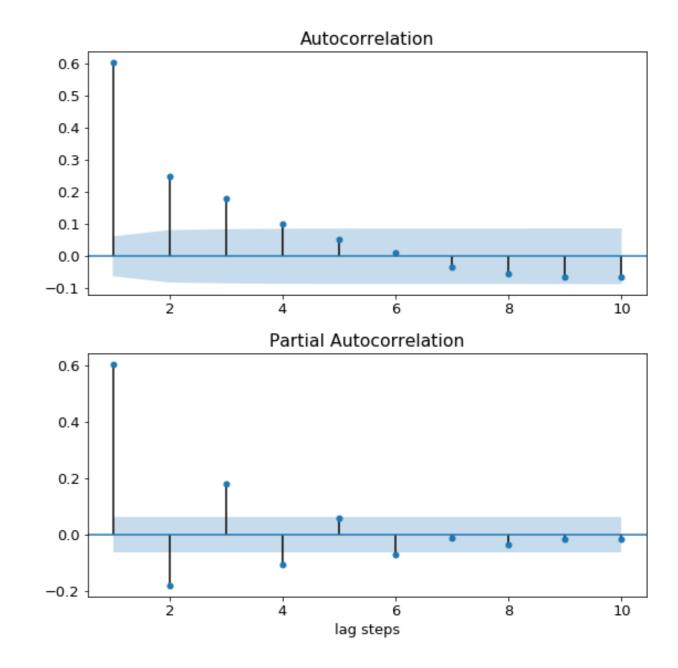
• MA(2) model \rightarrow



ARMA(p,q)

ACF Tails off

PACF Tails off



	AR(p)	MA(q)	ARMA(p,q)
ACF	Tails off	Cuts off after lag q	Tails off
PACF	Cuts off after lag p	Tails off	Tails off

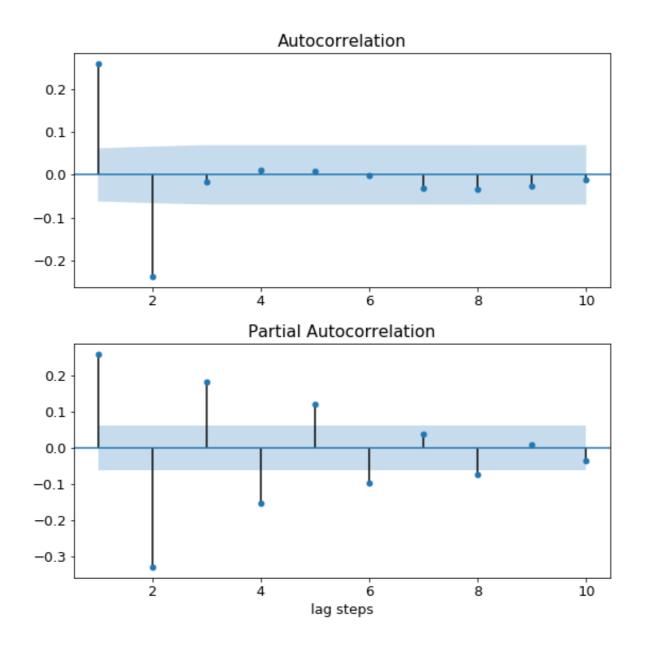
Implementation in Python

from statsmodels.graphics.tsaplots import plot_acf, plot_pacf

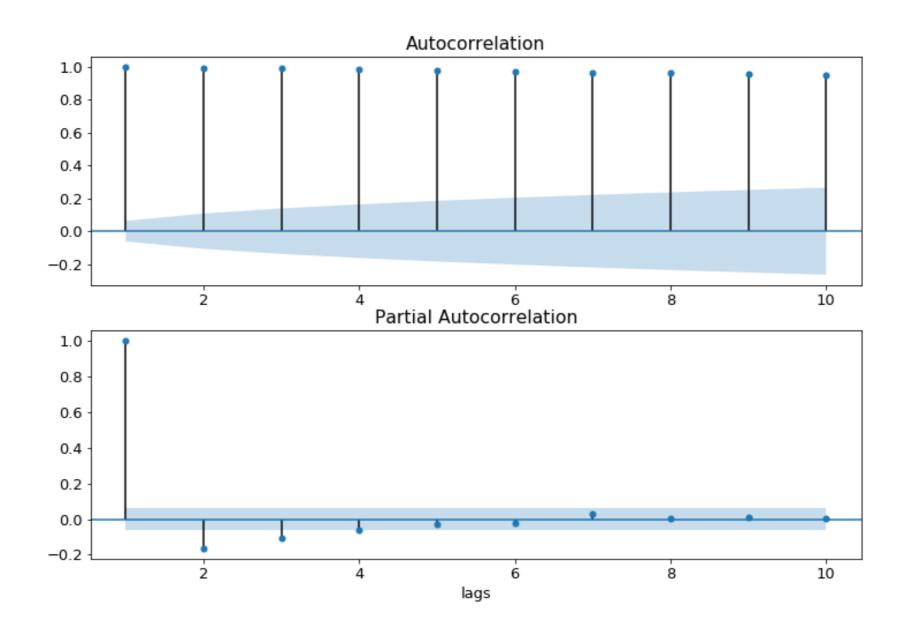
```
# Create figure
fig, (ax1, ax2) = plt.subplots(2,1, figsize=(8,8))
# Make ACF plot
plot_acf(df, lags=10, zero=False, ax=ax1)
# Make PACF plot
plot_pacf(df, lags=10, zero=False, ax=ax2)
plt.show()
```



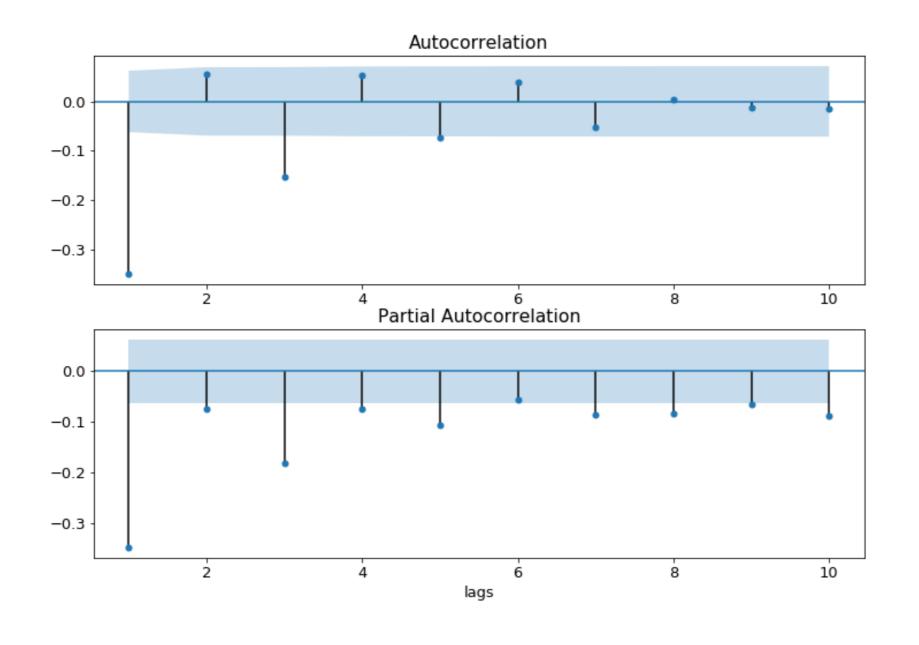
Implementation in Python



Over/under differencing and ACF and PACF



Over/under differencing and ACF and PACF



Let's practice!

FORECASTING USING ARIMA MODELS IN PYTHON



AIC and BIC

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James Fulton
Climate informatics researcher



AIC - Akaike information criterion

- Lower AIC indicates a better model
- AIC likes to choose simple models with lower order

BIC - Bayesian information criterion

- Very similar to AIC
- Lower BIC indicates a better model
- BIC likes to choose simple models with lower order

AIC vs BIC

- BIC favors simpler models than AIC
- AIC is better at choosing predictive models
- BIC is better at choosing good explanatory model

AIC and BIC in statsmodels

```
# Create model
model = SARIMAX(df, order=(1,0,1))
# Fit model
results = model.fit()
# Print fit summary
print(results.summary())
```

```
Statespace Model Results
Dep. Variable:
                                        No. Observations:
                                                                          1000
                    SARIMAX(2, 0, 0) Log Likelihood
Model:
                                                                     -1399.704
                    Fri, 10 May 2019
                                      AIC
Date:
                                                                      2805.407
                             01:06:11
Time:
                                        BIC
                                                                      2820.131
Sample:
                           01-01-2013
                                        HOIC
                                                                      2811.003
                         - 09-27-2015
Covariance Type:
                                  opg
```

AIC and BIC in statsmodels

```
# Create model
model = SARIMAX(df, order=(1,0,1))
# Fit model
results = model.fit()
# Print AIC and BIC
print('AIC:', results.aic)
print('BIC:', results.bic)
```

AIC: 2806.36

BIC: 2821.09



Searching over AIC and BIC

```
# Loop over AR order
for p in range(3):
    # Loop over MA order
    for q in range(3):
        # Fit model
        model = SARIMAX(df, order=(p,0,q))
        results = model.fit()
        # print the model order and the AIC/BIC values
        print(p, q, results.aic, results.bic)
```

```
0 0 2900.13 2905.04

0 1 2828.70 2838.52

0 2 2806.69 2821.42

1 0 2810.25 2820.06

1 1 2806.37 2821.09

1 2 2807.52 2827.15

...
```



Searching over AIC and BIC

```
order_aic_bic =[]
# Loop over AR order
for p in range(3):
    # Loop over MA order
    for q in range(3):
        # Fit model
        model = SARIMAX(df, order=(p,0,q))
        results = model.fit()
        # Add order and scores to list
        order_aic_bic.append((p, q, results.aic, results.bic))
```

```
# Make DataFrame of model order and AIC/BIC scores
order_df = pd.DataFrame(order_aic_bic, columns=['p','q', 'aic', 'bic'])
```

Searching over AIC and BIC

```
p q aic bic
7 2 1 2804.54 2824.17
6 2 0 2805.41 2820.13
4 1 1 2806.37 2821.09
2 0 2 2806.69 2821.42
...
```

print(order_df.sort_values('aic'))

```
# Sort by BIC
print(order_df.sort_values('bic'))
```

```
p q aic bic
3 1 0 2810.25 2820.06
6 2 0 2805.41 2820.13
4 1 1 2806.37 2821.09
2 0 2 2806.69 2821.42
...
```

Sort by AIC

Non-stationary model orders

```
# Fit model
model = SARIMAX(df, order=(2,0,1))
results = model.fit()
```

```
ValueError: Non-stationary starting autoregressive parameters found with `enforce_stationarity` set to True.
```

When certain orders don't work

```
# Loop over AR order
for p in range(3):
   # Loop over MA order
   for q in range(3):
        # Fit model
        model = SARIMAX(df, order=(p,0,q))
        results = model.fit()
        # Print the model order and the AIC/BIC values
        print(p, q, results.aic, results.bic)
```

When certain orders don't work

```
# Loop over AR order
for p in range(3):
    # Loop over MA order
    for q in range(3):
        try:
            # Fit model
            model = SARIMAX(df, order=(p,0,q))
            results = model.fit()
            # Print the model order and the AIC/BIC values
            print(p, q, results.aic, results.bic)
        except:
            # Print AIC and BIC as None when fails
            print(p, q, None, None)
```

Let's practice!

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Model diagnostics

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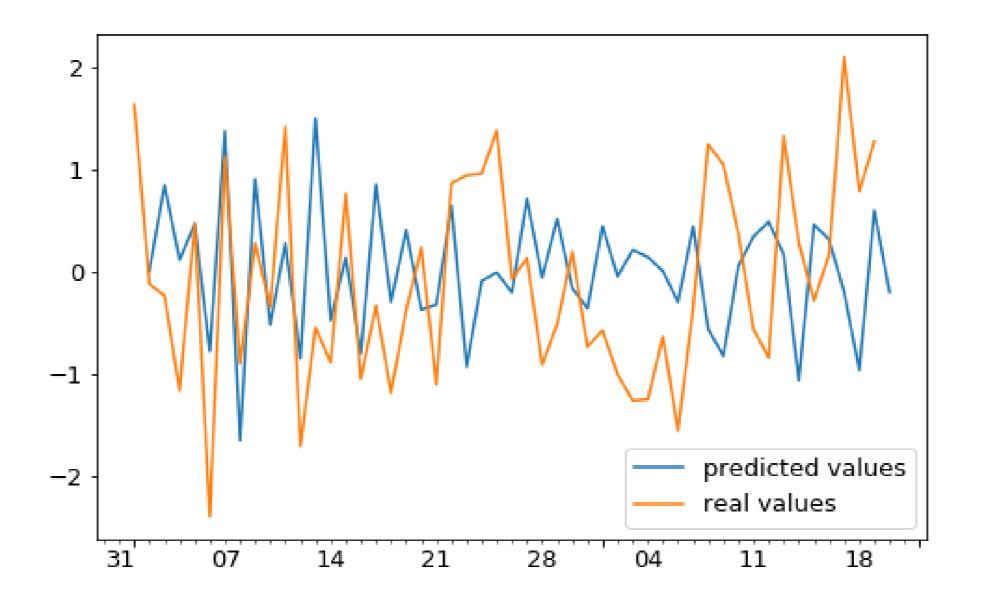
James Fulton
Climate informatics researcher



Introduction to model diagnostics

How good is the final model?

Residuals



Residuals

```
# Fit model
model = SARIMAX(df, order=(p,d,q))
results = model.fit()
# Assign residuals to variable
residuals = results.resid
```

Mean absolute error

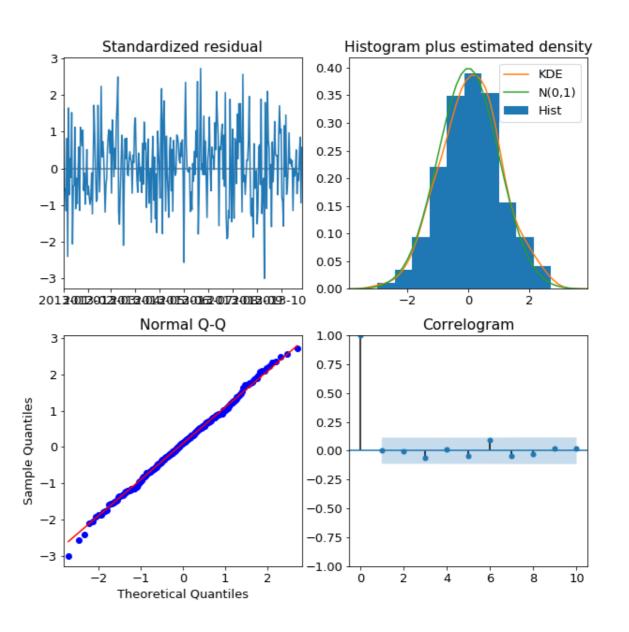
How far our the predictions from the real values?

```
mae = np.mean(np.abs(residuals))
```

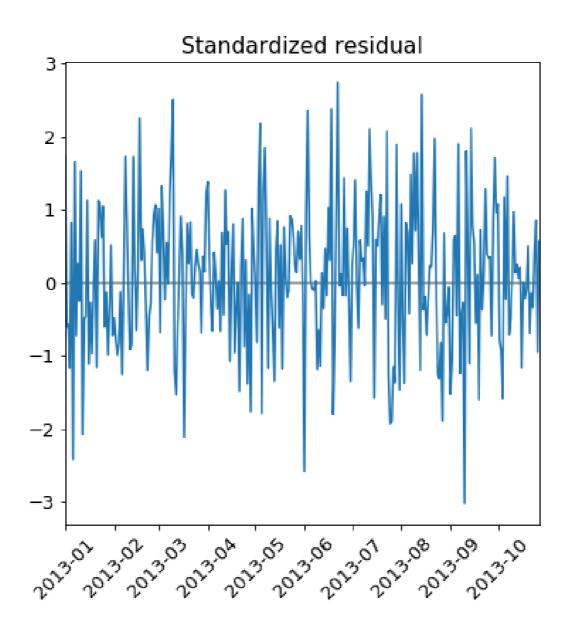
Plot diagnostics

If the model fits well the residuals will be white Gaussian noise

```
# Create the 4 diagostics plots
results.plot_diagnostics()
plt.show()
```

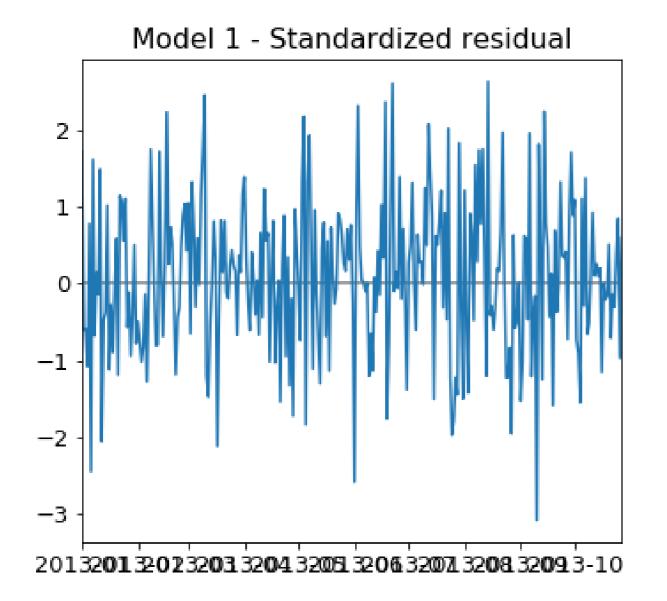


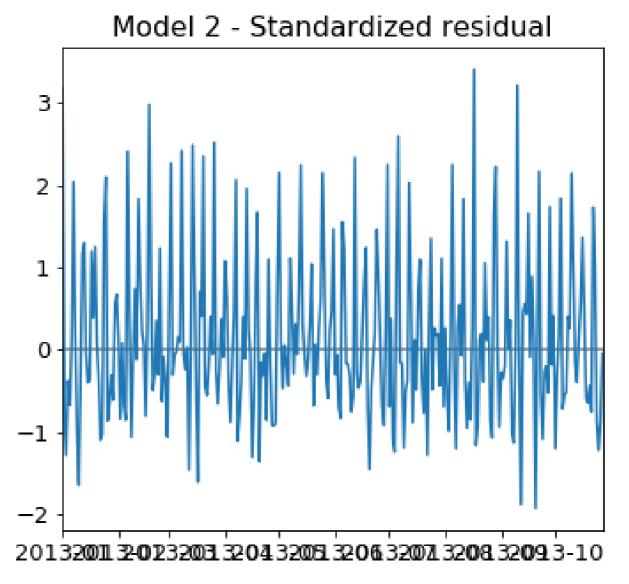
Residuals plot



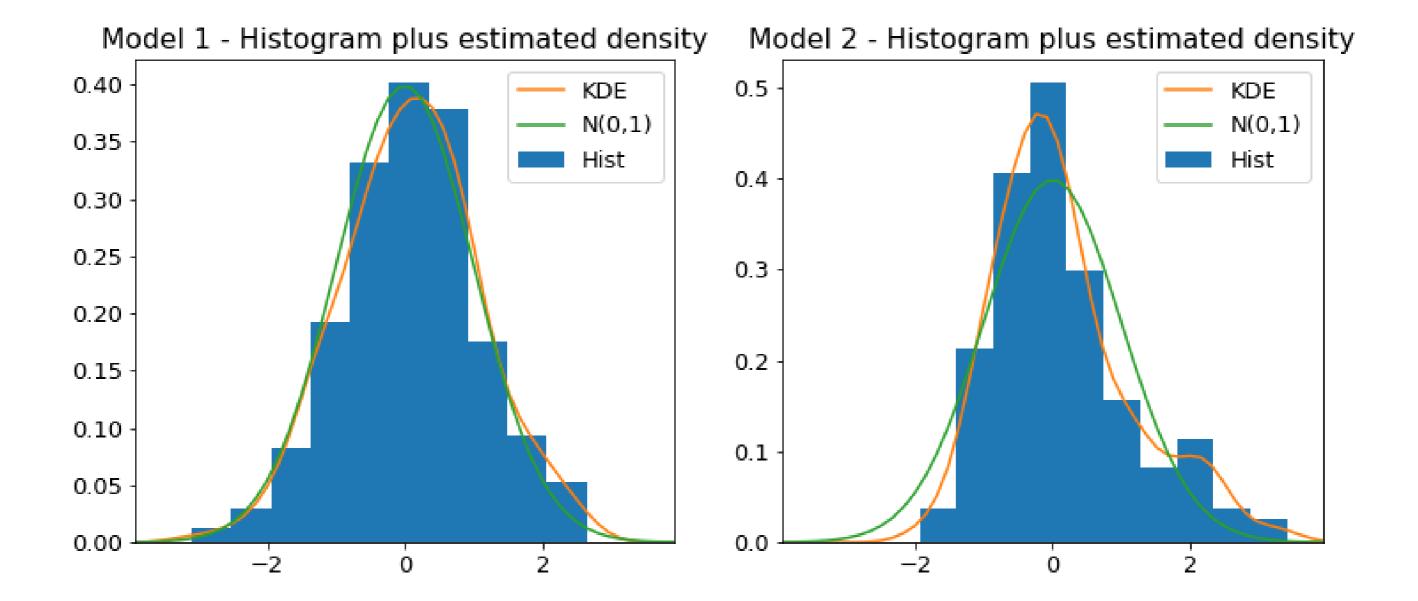


Residuals plot

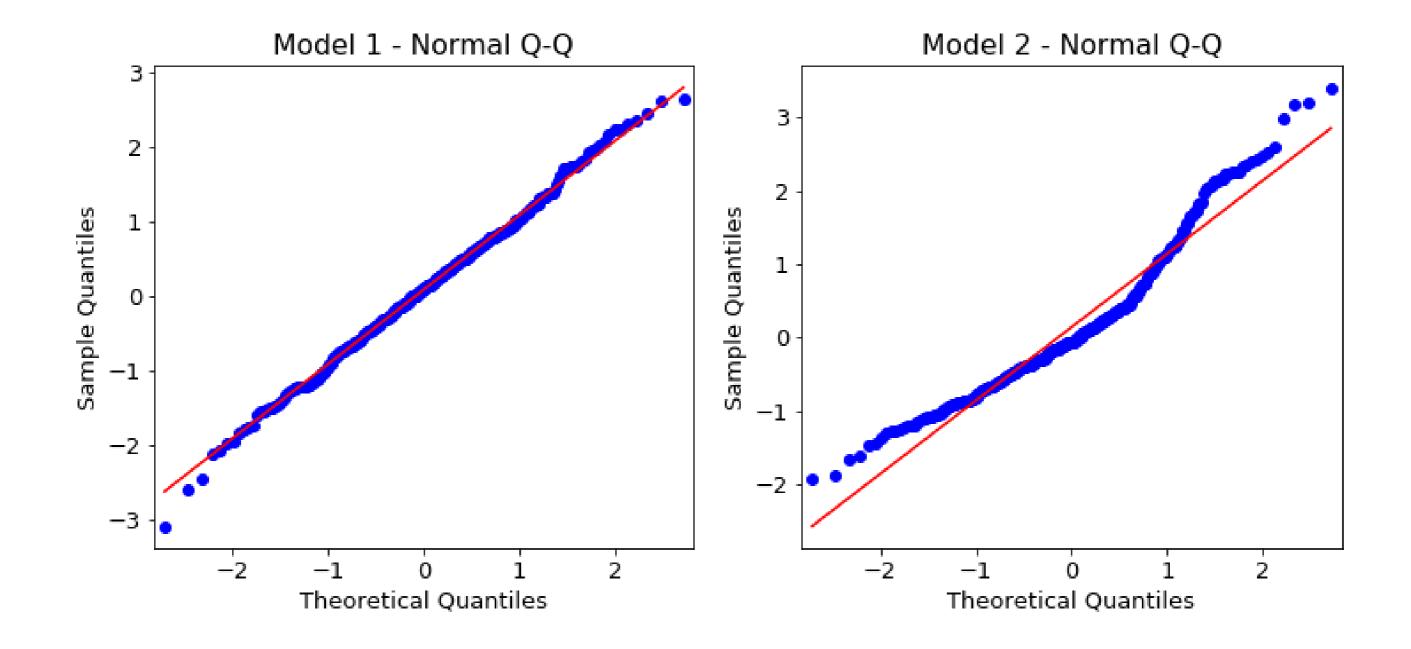




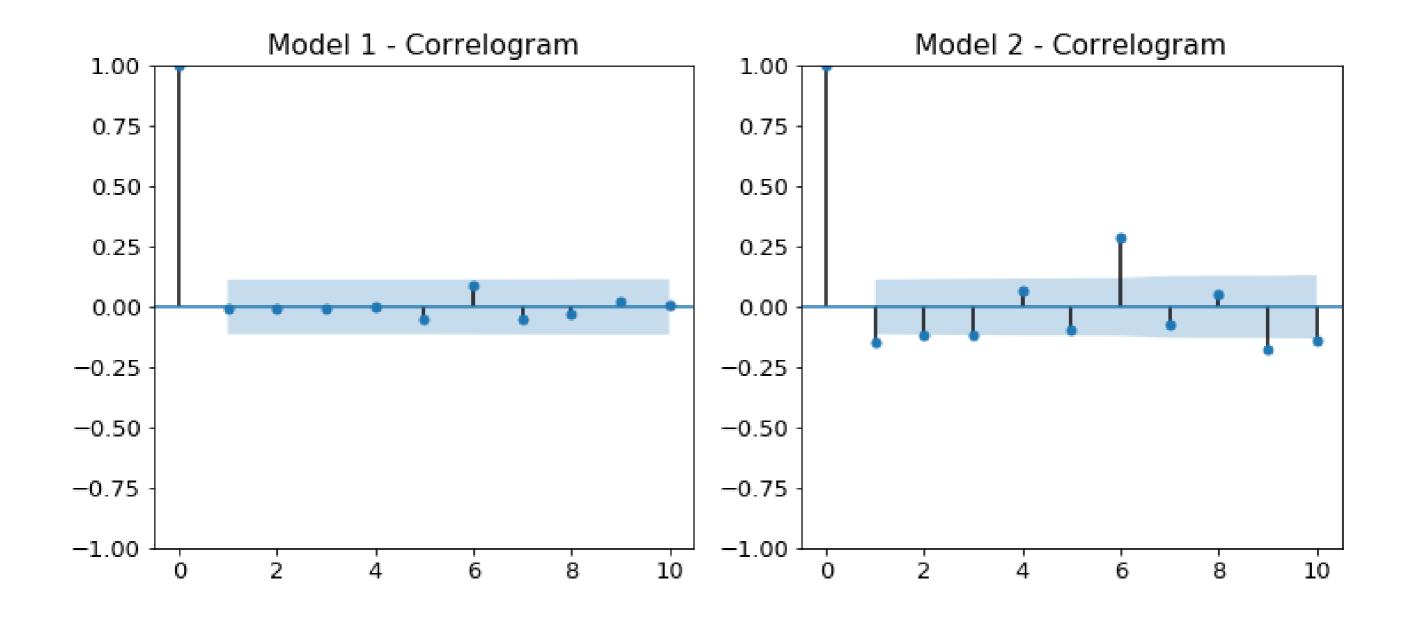
Histogram plus estimated density



Normal Q-Q



Correlogram



Summary statistics

```
print(results.summary())
```

```
Ljung-Box (Q):
                                              Jarque-Bera (JB):
                                     32.10
                                                                                 0.02
Prob(Q):
                                              Prob(JB):
                                       0.81
                                                                                 0.99
Heteroskedasticity (H):
                                      1.28
                                            Skew:
                                                                                -0.02
Prob(H) (two-sided):
                                              Kurtosis:
                                       0.21
                                                                                 2.98
```

- Prob(Q) p-value for null hypothesis that residuals are uncorrelated
- Prob(JB) p-value for null hypothesis that residuals are normal



Let's practice!

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Box-Jenkins method

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James Fulton
Climate informatics researcher



The Box-Jenkins method

From raw data \rightarrow production model

- identification
- estimation
- model diagnostics

Identification

- Is the time series stationary?
- What differencing will make it stationary?
- What transforms will make it stationary?
- What values of p and q are most promising?



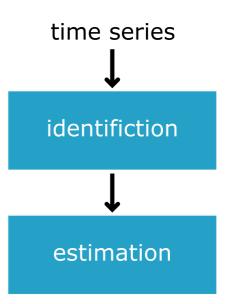
Identification tools

- Plot the time series
 - o df.plot()
- Use augmented Dicky-Fuller test
 - o adfuller()
- Use transforms and/or differencing
 - o df.diff() , np.log() , np.sqrt()
- Plot ACF/PACF
 - plot_acf() , plot_pacf()



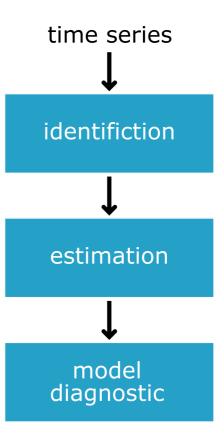
Estimation

- Use the data to train the model coefficients
- Done for us using model.fit()
- Choose between models using AIC and BIC
 - o results.aic , results.bic

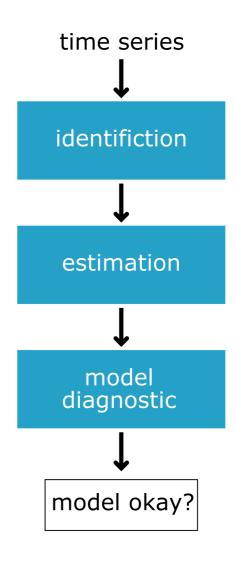


Model diagnostics

- Are the residuals uncorrelated
- Are residuals normally distributed
 - results.plot_diagnostics()
 - o results.summary()

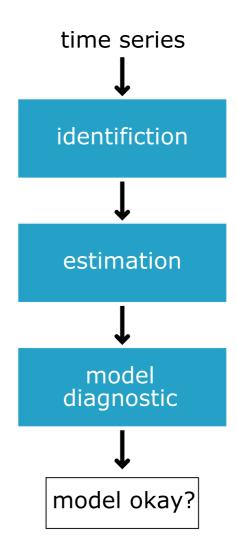


Decision



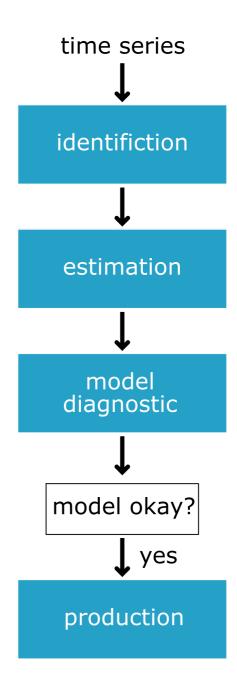
Repeat

- We go through the process again with more information
- Find a better model

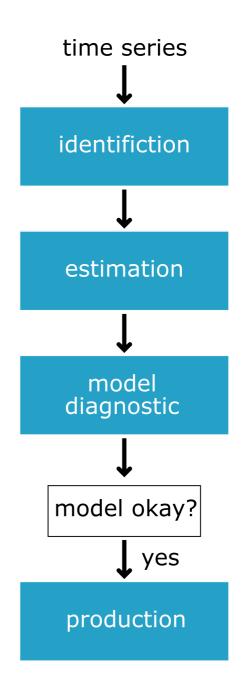


Production

- Ready to make forecasts
 - o results.get_forecast()



Box-Jenkins



Let's practice!

FORECASTING USING ARIMA MODELS IN PYTHON

