## An example sheet Question

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This is not a model tripos question, more the kind of thing you could find on an example sheet.

**EXERCISE 1** Define  $x \ll y$  by  $\mathcal{P}(x) \in \mathcal{P}(y)$ . Prove that  $\ll x$  is well-founded. Obviously you are not to use the axiom of foundation! Also it is artificially easy if you use the Axiom of Choice. The proof I have in mind is an elementary combinatorial one that does not use either of these axioms—tho' it does use replacement. It doesn't even use excluded middle.