```
1: \exists x. \forall y. ((R(y,x) \rightarrow \neg \exists z. (R(y,z) \land R(z,y))) \land (\neg \exists z. (R(y,z) \land R(z,y)) \rightarrow R(y,x)))
                                                                                                                                          assumption
  2: ||\operatorname{actual}|, \forall y.((R(y,i) \rightarrow \neg \exists z.(R(y,z) \land R(z,y))) \land (\neg \exists z.(R(y,z) \land R(z,y)) \rightarrow R(y,i)))|
                                                                                                                                          assumptions
  \exists : \| (R(i,i) \rightarrow \neg \exists z. (R(i,z) \land R(z,i))) \land (\neg \exists z. (R(i,z) \land R(z,i)) \rightarrow R(i,i)) \|
                                                                                                                                          ∀ elim 2.2,2.1
  4: || \neg \exists z. (R(i,z) \land R(z,i)) \rightarrow R(i,i)
                                                                                                                                          Λ elim 3
  5: ||R(i,i)\rightarrow \neg \exists z.(R(i,z) \land R(z,i))||
                                                                                                                                          Λ elim 3
 6: \parallel \exists z. (R(i,z) \land R(z,i))
                                                                                                                                          assumption
  7: | actual i1, R(i,i1) \(\lambda R(i1,i)\)
                                                                                                                                          assumptions
        R(i,i1)
  8: ||
                                                                                                                                          ۸ elim 7.2
        R(i1,i)
                                                                                                                                          ۸ elim 7.2
  9:
        R(i1,i) \wedge R(i,i1)
10:
                                                                                                                                          Λ intro 9,8
        |(R(i1,i)\rightarrow \neg \exists z.(R(i1,z)\land R(z,i1)))\land (\neg \exists z.(R(i1,z)\land R(z,i1))\rightarrow R(i1,i))|
11:
                                                                                                                                          ∀ elim 2.2,7.1
        \neg \exists z.(R(i1,z) \land R(z,i1)) \rightarrow R(i1,i)
12: |
                                                                                                                                          Λ elim 11
        R(i1,i) \rightarrow \neg \exists z.(R(i1,z) \land R(z,i1))
                                                                                                                                          Λ elim 11
13:
        \neg \exists z. (R(i1,z) \land R(z,i1))
14: ||
                                                                                                                                          → elim 13,9
        \exists z.(R(i1,z) \land R(z,i1))
15:
                                                                                                                                          ∃ intro 10,2.1
                                                                                                                                          ¬ elim 15,14
16: ||
      17:
                                                                                                                                          3 elim 6,7-16
18: \| \neg \exists z. (R(i,z) \land R(z,i))
                                                                                                                                          ¬ intro 6-17
19: || R(i,i)
                                                                                                                                          → elim 4,18
20: \|\neg \exists z. (R(i,z) \land R(z,i))
                                                                                                                                          \rightarrow elim 5,19
21: \|R(i,i) \wedge R(i,i)\|
                                                                                                                                          Λ intro 19,19
22: \exists z.(R(i,z) \land R(z,i))
                                                                                                                                          ∃ intro 21,2.1
23:|| 上
                                                                                                                                          ¬ elim 22.20
24: R(i,i)
                                                                                                                                          → elim 4,20
25:|| 上
                                                                                                                                          hyp 23
26: | 丄
                                                                                                                                          ∃ elim 1,2-25
27: \neg \exists x. \forall y. ((R(y,x) \rightarrow \neg \exists z. (R(y,z) \land R(z,y))) \land (\neg \exists z. (R(y,z) \land R(z,y)) \rightarrow R(y,x)))
                                                                                                                                          ¬ intro 1-26
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