

Micro resonant force gauges

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(Received September 5, 1991, accepted September 27, 1991)

Abstract

A review of micro resonant force gauges is presented. A theoretical description is given of gauges operating in a flexural mode of vibration, including a discussion of non-linear effects. Gauge factor and quality factor are defined and their relevance is discussed. Performance issues such as sensitivity, stability and resolution are addressed. Design aspects, including the means for excitation and detection of the vibration, and examples of silicon microfabrication technologies are described.

Introduction

A micro resonant force gauge comprises a (small) vibrating mechanical element, i.e., the resonator, which converts an externally applied (axial) force into a shift of the resonance frequency of the element. It is used as a sensing device for measuring quantities such as pressure, force (weight), mass flow, temperature or acceleration. The term micro refers to the method of realization, i.e., (silicon) microfabrication technologies. Resonant force gauges can be used directly as sensors to convert the unknown applied force into a frequency-shift output. They can also form the heart of a sensor, for instance, be applied as strain gauges, where the measurand is first converted into a strain, which is subsequently converted into a frequency-shift of the resonant gauge. Generally speaking, micro resonant force gauges belong to the class of resonant sensors [1, 2]. Resonant sensors are very attractive in the precision measurement field, because of their high sensitivity and resolution, and further because of their semi-digital output, i.e., a frequency shift, which eliminates problems such as intensity fluctuations associated with analog signals.

In general, the resonance frequency of a mechanical structure is affected by a perturbation of its potential or kinetic energy [3]. Potential energy perturbations can be caused by mechanically straining the resonator or by changing the shape,

and thus the stiffness, of the resonator. In a resonant force gauge, the frequency shift is a result of potential energy perturbations caused by mechanical strain. To avoid error readings, kinetic energy perturbations, e.g., caused by a change of the resonator mass or by changes of the density of the surrounding medium, should be eliminated. This can be done by hermetically sealing the resonator in an evacuated or inert cavity to provide a stable environment.

Although a resonant force gauge can have a variety of shapes and vibrate in various modes, the gauges considered in more detail in this paper are restricted to flexurally vibrating elements that are mounted at two end points. Special attention is paid to prismatic homogeneous beams that are clamped at both ends. Analytical expressions are reviewed for the resonance frequencies of the beam, including a quantitative large-deflection analysis. As a measure for the sensitivity of the gauge, gauge factors are defined and expressed in terms of dimensions and residual stress. Further, the mechanisms of energy losses are discussed and ways of reducing them are indicated. A discussion of the various means of excitation and detection of the vibration is also included. Finally, silicon fabrication technologies are briefly reviewed and state of the art examples are given on how to fabricate sealed resonators. For more information regarding applications and other aspects of resonant sensors, reference is made to a number of review articles.

written in recent years [1–6] Specifics of quartz resonating sensors are not a subject of this paper, but can be found in the literature [7–9]

Resonance frequencies

For an initially flat prismatic homogeneous beam, subjected to a (tensile) axial force N , the equation of motion governing the transverse deflection $w(x, t)$ as a function of the position x along the beam length and the time t is given by the following linear partial differential equation [10]

$$\hat{E}I \frac{\partial^4 w(x, t)}{\partial x^4} - N \frac{\partial^2 w(x, t)}{\partial x^2} + \rho A \frac{\partial^2 w(x, t)}{\partial t^2} = q(x, t) \quad (1)$$

where \hat{E} and ρ are the 'effective' Young's modulus [11] and specific mass of the beam material, A and I the cross-sectional area and second moment of inertia, respectively, and $q(x, t)$ indicates the driving force per unit length. To find the eigenfunctions or natural modes together with the corresponding eigenvalues or natural frequencies, the homogeneous part of eqn (1) is solved by employing a separation of variables approach in the form $w(x, t) = \phi(x) \exp(j\omega t)$. Or, in other words, it is assumed that the beam is oscillating at an angular frequency ω with a mode shape $\phi(x)$. For a clamped-clamped beam ($w(0, t) = w(l, t) = 0$ and $w'(0, t) = w'(l, t) = 0$, where l is the length of the beam), non-trivial solutions are obtained if the following condition, i.e., the characteristic equation, is satisfied

$$\cos(\lambda l) \cosh(\mu l) - \frac{1}{2} \left(\frac{\mu}{\lambda} - \frac{\lambda}{\mu} \right) \sinh(\mu l) \sin(\lambda l) = 1 \quad (2)$$

where

$$\lambda l = kI[(a^2 + 1)^{1/2} - a]^{1/2} \quad (3a)$$

$$\mu l = kI[(a^2 + 1)^{1/2} + a]^{1/2} \quad (3b)$$

and

$$a = N/2\hat{E}Ik^2 \quad (4a)$$

$$k^4 = \rho A \omega^2 / \hat{E}I \quad (4b)$$

This yields the following expression for the mode shape functions

$$\begin{aligned} \phi(x) = & \cos(\lambda x) - \cosh(\mu x) + \frac{\cos(\lambda l) - \cosh(\mu l)}{\frac{\lambda}{\mu} \sinh(\mu l) - \sin(\lambda l)} \\ & \times \left(\sin(\lambda x) - \frac{\lambda}{\mu} \sinh(\mu x) \right) \end{aligned} \quad (5)$$

The characteristic eqn (2) is satisfied for a discrete set of solutions yielding a discrete number of values for k , i.e., k_n for $n = 1, 2, \dots$. The corresponding natural frequencies or eigenfrequencies ω_n are found from eqn (4) and the associated mode shapes ϕ_n from eqn (5). Because of the transcendental nature of the characteristic equation, a closed-form expression for the natural frequencies as a function of the axial load N and the beam parameters cannot be obtained. Approximate solutions can be found, for example, by employing Rayleigh's energy method [12]. The following expression for the natural frequencies can be obtained this way

$$\omega_n(N) \approx \omega_n(0) \left(1 + \gamma_n \frac{NI^2}{12\hat{E}I} \right)^{1/2} \quad (6)$$

where

$$\omega_n(0) = \frac{\alpha_n^2}{l^2} \left(\frac{\hat{E}I}{\rho A} \right)^{1/2} \quad (7)$$

and the coefficients α_n and γ_n can be found from

$$\alpha_n^2 = l^2 \left(\int_0^l \left(\frac{d^2 \tilde{\phi}_n(x)}{dx^2} \right)^2 dx \right) / \left(\int_0^l (\tilde{\phi}_n(x))^2 dx \right)^{1/2} \quad (8a)$$

$$\gamma_n = \frac{12}{l^2} \left(\int_0^l \left(\frac{d \tilde{\phi}_n(x)}{dx} \right)^2 dx \right) / \left(\int_0^l \left(\frac{d^2 \tilde{\phi}_n(x)}{dx^2} \right)^2 dx \right) \quad (8b)$$

where $\tilde{\phi}_n(x)$ represents an approximate shape function for a particular mode n . When $\tilde{\phi}_n(x)$ corresponds to the exact shape function, eqn (6) yields the exact value for the natural frequency, otherwise the result of eqn (6) will always be an upper bound of the natural frequency [12]. A good approximation for the natural frequencies of a beam subjected to a non-zero axial load can be obtained if the shape functions of the same beam for zero applied axial load are substituted for $\tilde{\phi}_n(x)$. For a clamped-clamped beam, these functions are given by eqn (5) for $\lambda = \mu = k$, where k is determined from eqn (2), which for $N = 0$ reduces to $\cos(kl) \cosh(kl) = 1$. For the fundamental mode this yields $\alpha_1 = 4.730$ and $\gamma_1 = 0.295$, and for the first harmonic, $\alpha_2 = 7.853$ and $\gamma_2 = 0.145$. This is

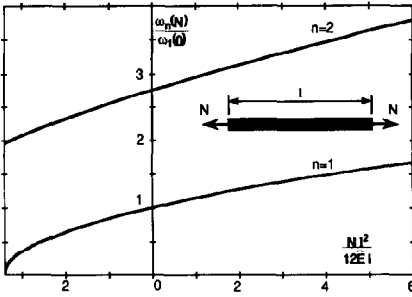


Fig 1 Normalized angular resonance frequency of the fundamental mode and the first harmonic as a function of the normalized axial force for an initially flat prismatic clamped-clamped beam, see also eqn (6)

graphically illustrated in Fig 1. The error in the approximation for the natural frequency is smaller than 0.5% if $\gamma_n NI^2/12EI < 1$ [13]. An empirical correction in the form of an additional quadratic term in the axial force under the square root has been proposed by van Mullem *et al* [14].

In micromechanical devices, very often beams with a rectangular cross section and a large width ($b > 5h$ [15]) are used and eqns (6)–(7) can conveniently be written as

$$\omega_n(N) = \frac{\alpha_n^2}{\sqrt{12}} \left(\frac{E}{\rho(1-\nu^2)} \right)^{1/2} \times \frac{h}{l^2} \left(1 + \gamma_n \frac{N}{Ebh} (1-\nu^2) \left(\frac{l}{h} \right)^2 \right)^{1/2} \quad (9)$$

where ν and E are Poisson's ratio and Young's modulus of the beam material, respectively, and b and h are the width and thickness of the beam, respectively.

In the model described above, effects due to shear deformation and rotary inertia are not taken into account. These effects are negligible for slender beams, i.e., beams with a large length/thickness ratio and for small values of the mode number n [12, 16]. Besides the shift in the resonance frequency as a result of the induced axial force, the frequency also changes slightly as a result of changes in the dimensions of the beam. The latter effect, however, is small compared to the effect of the induced axial force (see also Section on gauge factors). Further, the model does not apply for beams with a non-zero initial deflection, e.g., beyond the Euler buckling point.

In this case, additional terms have to be included in the equation of motion [13, 17]. The effect of an elastic support on the resonance frequencies was discussed by Bouwstra and Geijselaers [13], and the analysis showed that the support forms a reasonable stiffness against bending, but not against axial elongations. The latter implies that, in the case of an elastic support, the frequency shifts are smaller than predicted by the equations above. Torsional modes were discussed by Geijselaers and Tijdsman [18]. The effects of damping terms and non-linear (large deflection) deformation are not accounted for here, but will be briefly discussed below.

Force, stress or strain?

The resonance frequencies of doubly supported beams respond to the applied axial force N . This is easily understood from an inspection of the equation of motion of the beam, eqn (1). The frequency dependence is expressed by eqn (6). If the beam is used as a measuring device it can therefore be designated as a 'resonant force gauge'. An illustrative example is the vibrating string of Wyman [19], where the external force, e.g., a weight, comprises the axial force responsible for the frequency shift of the string. The force in this case is the independent variable, which induces an axial elongation of the string. If the cross-sectional area A does not change under the applied load, the gauge could also be designated as a 'resonant stress gauge', since the axial stress σ in this case is directly related to the axial force N : $\sigma = N/A$.

In many applications, however, the axial force is a result of a displacement of the end points or elongation of the gauge, e.g., see [20–29]. Here, the induced axial force is directly related to the elongation Δl or the strain $\Delta l/l$ of the gauge: $N = EA(\Delta l/l)$, where l is the length of the gauge. The gauge truly senses a deformation of the supporting structure and is therefore referred to as a 'resonant elongation gauge' or 'resonant strain gauge' to emphasize the measuring principle and the origin of the axial force. It also links devices employing resonant strain gauges to devices employing the more conventional (piezo)resistive strain gauges. In these applications, the gauges are embedded into a supporting structure, the so-called 'load cell', e.g.,

a diaphragm [24], or a supporting frame [14, 26], which converts the externally applied load, e.g., a pressure, into a strain in the gauge. The contribution of the stiffness of the gauge to the overall stiffness of the device is generally negligible.

Gauge factors

The gauge factor of a resonant gauge provides a measure of the gauge to the applied axial load. The gauge factor G_{Nn} , describing the sensitivity of the gauge, vibrating at $\omega = \omega_n$, to changes in the axial force N , and in the vicinity of the operating point $N = N_0$, caused by the biaxial residual stress σ_0 or residual strain ε_0 , is defined by

$$G_{Nn} \equiv \left[\frac{1}{\omega_n} \frac{\partial \omega_n}{\partial N} \right]_{N=N_0=(1-\nu)\sigma_0 A = EA\varepsilon_0} \quad (10)$$

or, for a (wide) beam with a rectangular cross section (see eqn (9))

$$G_{Nn} = \frac{1}{2} \left[\frac{\gamma_n \frac{(1-\nu^2)}{Ebh} \left(\frac{l}{h} \right)^2}{1 + \gamma_n \varepsilon_0 (1-\nu^2) \left(\frac{l}{h} \right)^2} \right] \quad (11)$$

If the axial force is a result of an axial elongation of the beam, it is more useful to define a gauge factor $G_{\varepsilon n}$, describing the sensitivity of mode n to changes in the strain ε in the vicinity of the operating point $\varepsilon_0 = (1-\nu)\sigma_0/E$

$$G_{\varepsilon n} \equiv \left[\frac{1}{\omega_n} \frac{\partial \omega_n}{\partial \varepsilon} \right]_{\varepsilon=\varepsilon_0} \quad (12)$$

or using eqn (9) with $N/Ebh = \varepsilon$,

$$G_{\varepsilon n} = \frac{1}{2} \left[\frac{\gamma_n (1-\nu^2) \left(\frac{l}{h} \right)^2}{1 + \gamma_n \varepsilon_0 (1-\nu^2) \left(\frac{l}{h} \right)^2} \right] \quad (13)$$

If the effects of geometrical deformations are taken into account $l' = l(1 + \varepsilon)$ and $h' = h(1 - \nu\varepsilon)$, the gauge factor would be given by

$$G'_{\varepsilon n} = -(2 + \nu) + \frac{1}{2}(1 + 2\varepsilon_0(1 + \nu)) \times \left[\frac{\gamma_n (1-\nu^2) \left(\frac{l}{h} \right)^2}{1 + \gamma_n \varepsilon_0 (1-\nu^2) \left(\frac{l}{h} \right)^2} \right] \quad (14)$$

The gauge factors $G_{\varepsilon n}$ and $G'_{\varepsilon n}$ are approximately the same. For zero residual strain ($\varepsilon_0 = 0$), $\nu = 0.3$ and an aspect ratio $l/h = 200$, they differ by 0.04%. Or in other words, the shift in the resonance frequency as a result of geometrical deformation of the gauges is small compared to the shift caused by the axial stiffening. This has an important consequence for the behaviour of resonant gauges that are subject to creep. If creep occurs under a constant state of stress, for instance as in the experiment described by Bethe *et al* [30], the resonance frequency will only be slightly affected. On the other hand, if the input load of the gauge is an elongation, creep will seriously limit the performance of the device. Also a possible relaxation of the residual stress during operation will cause error readings. Study of the relaxation of residual stress in thin films used for the fabrication of microresonators should therefore be an important topic of future research.

Large gauge factors are achieved at low residual strain/stress levels and/or for slender beams. Also, the gauge factor decreases with increasing mode number. This implies a larger contribution of geometrical deformations to the shift in the resonance frequency for the higher-order modes. For the fundamental mode, the gauge factor given by eqn (13) is graphically shown in Fig. 2.

Quality factor

The mechanical quality factor Q is a measure of the energy losses of the resonator or, in other

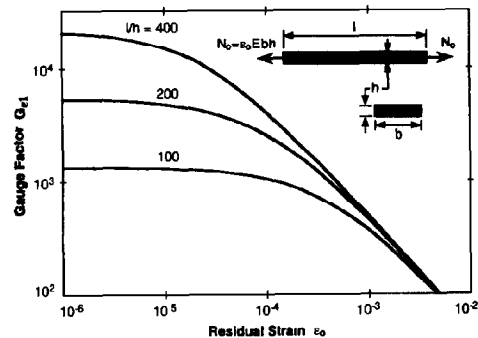


Fig. 2 Gauge factor $G_{\varepsilon 1}$ of the fundamental mode vs. residual tensile strain ε_0 for a clamped-clamped beam with a rectangular cross section for three values of the slenderness ratio l/h and $\nu = 0.3$, see also eqn (13)

words, a measure of the mechanical damping. The Q -factor is defined as

$$Q \equiv 2\pi \frac{\text{maximum energy stored in one period}}{\text{dissipated energy per period}} \quad (15)$$

Low energy losses imply a high Q -factor. The Q -factor cannot be determined directly, but instead can be deduced from the response characteristics of the resonator. One common method of determining Q is from the steady-state frequency response plot of a resonator excited by a harmonic force with constant amplitude

$$Q \cong \frac{\omega_{\text{res}}}{\Delta\omega_{-3\text{ dB}}} \quad (16)$$

where ω_{res} is the resonance frequency, defined as the frequency of maximum amplitude response, and $\Delta\omega_{-3\text{ dB}}$ is the half-power bandwidth of the frequency response. Equation (16) indicates that Q is a measure of the sharpness or the frequency selectivity of the resonator. A high Q -factor means a sharp resonance peak. A high Q -factor for a resonant force gauge has several advantages. The energy required to maintain oscillation is kept low, which reduces heat generation and opens up the possibility of powering the resonant gauges from alternative sources, e.g., solar energy. Further, a high Q means a good frequency stability and the effects on the oscillation frequency of the electronic circuitry used to sustain the oscillation are minimized.

Several mechanisms of energy loss can be identified: (a) losses into the surrounding (fluid) medium, caused by acoustic radiation and viscous drag, (b) losses into the mount used to support the resonator due to motion of the mount, and (c) intrinsic damping caused by energy losses inside the material of the resonator. The energy loss of each loss mechanism separately can be described by a corresponding quality factor Q_i , and the overall quality factor Q_{tot} can be found from

$$\frac{1}{Q_{\text{tot}}} = \sum_i \frac{1}{Q_i} \quad (17)$$

It is obvious from eqn (17) that Q_{tot} cannot exceed the value of the smallest Q_i . The discussion below mainly deals with vibrating beams. Quality factors of vibrating diaphragms are discussed elsewhere [31].

The losses into the surrounding fluid are due to viscous damping and/or radiation of sound waves propagating in a direction normal to the surface. The latter effect will only be significant if the acoustic wavelength becomes equal to or less than a typical dimension of the resonator [32, 33]. Acoustic radiation can generally be ignored for micromechanical resonators. Viscous damping is characterized by two contributions [34–36]. One is due to the usual Stokes drag force for a body in uniform motion through a viscous fluid. The second (dynamic) part, the so-called shear wave effect, is characterized by a boundary layer around the vibrating structure and is dependent on the frequency of vibration ω , and further on the density ρ_0 and viscosity η of the fluid medium. The quality factor Q_{viscous} caused by viscous damping can be expressed as [37]

$$Q_{\text{viscous}} = \frac{\rho A \omega}{c \left(\frac{R}{\delta(\eta, \rho_0, \omega)}, \eta \right)} \quad (18)$$

where c is the coefficient of the dissipative part of the drag force, R represents the relevant linear dimension and $\delta = (2\eta/\rho_0\omega)^{1/2}$ is the characteristic width of the boundary layer. If δ is much larger than the linear dimensions of the resonator, the shear-wave effects can be ignored and c is a given constant, dependent only on η . $Q_{\text{viscous}} = \rho A \omega / c(\eta)$, stating that in this case the quality factor is linearly proportional to the frequency of vibration. The viscous quality factor of a wide beam with a rectangular cross section and for zero applied axial force can then be expressed as (see also eqn (9))

$$Q_{\text{viscous}, \eta} = \frac{\rho A \omega_n}{c(\eta)} = \frac{\alpha_n^2 b}{c(\eta) \sqrt{12}} \left(\frac{h}{l} \right)^2 \left(\frac{\rho E}{(1-\nu^2)} \right)^{1/2} \quad (\delta \gg R) \quad (19)$$

From the above expression it is seen that the viscous quality factor is inversely proportional to the aspect ratio (l/h) of the beam. Assuming $c(\eta) \approx 24\eta$ for a prismatic beam with a rectangular cross section [38], a viscous quality factor in air ($\eta = 1.8 \times 10^{-5} \text{ N s/m}^2$) of approximately 30 is found for the fundamental mode of a clamped-clamped silicon beam $1 \mu\text{m}$ wide with an aspect ratio of 100. If shear-wave effects cannot be ignored, the quality factor will be lower and will become directly proportional to $\omega^{1/2}$. This dependence has

been experimentally observed by Lammerink *et al* [39] and Blom *et al* [37]

In the discussion above it was assumed that the resonator is isolated in space. If the flexurally vibrating resonator is close to another stationary surface, damping forces increase due to a pressure built-up in the intervening space, i.e., the (air) gap [38, 40, 41]. This so-called squeeze-film damping effect becomes significant if the gap spacing approaches or becomes less than the width of the vibrating beam. Whereas the viscous quality factor would be of the order of 100–2000 for an isolated beam, it rapidly drops below 1 if the gap spacing is too small. This has been experimentally observed by Howe and Muller [41]. Squeeze-film damping can be slightly reduced by making ventilation holes in the vibrating beam [41, 42] or practically eliminated by placing the beam in an evacuated cavity [24, 27, 43].

The energy coupled into the supporting structure can be minimized by mechanically isolating the resonator from the mount [1, 7]. An example of a geometry providing a means of decoupling a flexurally vibrating single beam from the support is an isolation system in between the beam and the support. This consists of a large mass and an isolator beam, acting as a soft spring-mass system with a natural frequency much lower than the frequency of the beam and of the support [44, 45]. In this design, moment and shear reactions are isolated from the support, resulting in a reduction of energy losses. The mass has to be large to give it enough rotary inertia to form an efficient clamping edge for the resonating beam. A decoupling method for a torsional resonator was reported by Buser and de Rooij [46]. In their structure, a frame was designed around the resonator which itself can vibrate in a torsional mode. Again, the aim of the design was to have a high ratio of the resonance frequencies of the resonator and the mounting frame in order to minimize the energy losses. Quality factors in vacuum as high as 600 000 were measured for a structure made out of single-crystalline silicon. Another way of lowering the energy losses into the support is to use a specific resonator design. A well-known example is the double-ended tuning fork (DETF), consisting of two beams vibrating 180° out of phase, thereby cancelling moment reactions at the beam roots and resulting in a reduction of energy losses, see Fig 3(a) [7, 47]. The triple beam structure

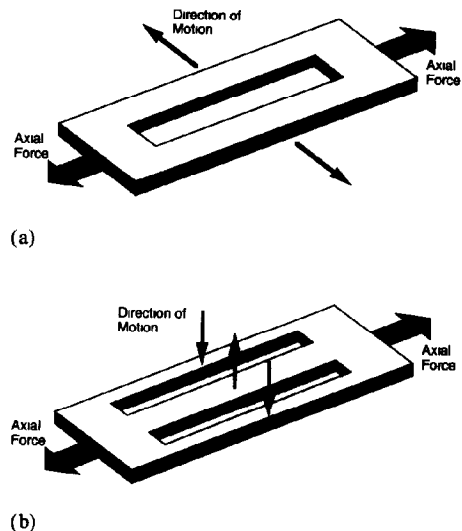


Fig 3 (a) Double-ended tuning fork [47], (b) triple beam structure [48]

provides yet another way of cancelling moments and shear forces at the clamped ends, see Fig 3(b) [48, 49]. It consists of three beams, the middle beam being twice the width of the outer beams. The middle beam and the two outer beams vibrate 180° out of phase, resulting in the desired cancellation of moments and shear forces. This structure is very attractive from a fabrication point of view. It can easily be fabricated with planar micromachining technologies and the excitation/detection of the flexural transverse (perpendicular to the substrate) vibrations does not mean any more difficulties than for the single-beam approach. This is in contrast to the DETF, which requires in-plane excitation/detection schemes. Another structure, consisting of a balanced dual-diaphragm, was reported by Stemme and Stemme [42]. Here, a balanced torsional mode of vibration is excited, where energy losses into the mount are small because of the stationary centre of mass and because the vibrating element is suspended at the nodal lines, which minimizes the movement of the mount. Balanced structures were reviewed by Stemme [5].

Besides the external sources of energy losses described above, there still remains a large number of mechanisms through which vibrational energy can be dissipated within the material that is cyclically deformed. They include magnetic effects

(magnetoelastic hysteresis), thermal effects (thermoelastic internal friction [50] and atomic reconstructions (dislocations, stress relaxation at grain boundaries) [51] A way of describing viscoelastic material losses or structural damping is by introducing a complex Young's modulus $E^* = E(1 + i\gamma)$, where $i = \sqrt{-1}$ and γ is the structural damping factor [52, 53] The quality factor Q_{int} associated with structural damping is simply given by $Q_{\text{int}} = 1/\gamma$ Single-crystal materials, such as quartz and single-crystalline silicon, seem to have lower intrinsic losses compared to amorphous or polycrystalline materials, and are therefore more attractive as resonator materials [9, 54] However, a lot of work remains in investigating the damping properties of materials

In describing the air-pressure dependence of the overall quality factor Q_{tot} , three main pressure regions can be distinguished [37, 38] The transition points of these regions depend on the shape and material properties of the resonator and also on the way the resonator is supported In general, viscous damping is the dominating mechanism near atmospheric pressure This region can be divided into two sub-regions, depending on the relative width of the boundary layer δ as discussed before At high pressures and for high frequencies, shear-wave effects dominate and Q_{tot} will be proportional to δ and thus to $1/p^{1/2}$, where p is the air pressure At lower pressures and/or frequencies, Q_{tot} will be independent of δ and thus independent of p Lowering the pressure even further, the Knudsen gas region is reached and the air no longer acts as a viscous fluid Energy losses are now caused by individual collisions of the gas molecules with the resonator In this region, Q_{tot} is proportional to $1/p$ [37, 55] At very low pressures (e.g., < 1 Pa) air damping can be ignored and the quality factor is determined by losses into the support and by the intrinsic losses, making Q_{tot} independent of p Thus, in order to obtain a Q -factor as high as possible, vacuum encapsulation of the resonator is necessary

Non-linear (large-amplitude) effects

In the derivation of eqn (1), small amplitudes of the vibration w_{max} were assumed If w_{max} becomes comparable to the radius of gyration,

$r = (I/A)^{1/2}$, of the cross section of the beam, the dependence of the axial force on the amplitude of the vibration has to be taken into account, resulting in a non-linear term in eqn (1) [56] If the distance between the ends of the beam is rigidly fixed, a tensile axial force will be developed by the transverse deflection This will result in an increase of the resonance frequencies of the beam and is known in the literature as the 'hard-spring effect' [56–61] To get some idea of the impact of this effect on the natural frequencies, an additional potential energy term is included in Rayleigh's quotient The additional stretching of the mid-plane of the beam results in a potential energy change U_{NL} given by

$$U_{\text{NL}} = \frac{1}{2} \int_0^l \frac{EA}{4} \left(\frac{dw}{dx} \right)^4 dx \quad (20)$$

Including this term in Rayleigh's quotient results in a modified expression of eqn (6)

$$\omega_n(N, w_{\text{max}}) = \omega_n(0, 0) \times \left(1 + \gamma_n \frac{NI^2}{12EI} + \beta_n \frac{EA}{12EI} w_{\text{max}}^2 \right)^{1/2} \quad (21)$$

where $\omega_n(0, 0)$ is the natural frequency of mode n for zero axial load and ignoring non-linear effects, w_{max} is the amplitude of the vibration and β_n is a constant given by

$$\beta_n = \frac{3}{\tilde{\phi}_{n, \text{max}}^2} \left(\int_0^l \left(\frac{d\tilde{\phi}_n(x)}{dx} \right)^4 dx \right) / \left(\int_0^l \left(\frac{d^2\tilde{\phi}_n(x)}{dx^2} \right)^2 dx \right) \quad (22)$$

where $\tilde{\phi}_{n, \text{max}}$ is the maximum value of the approximate shape function $\tilde{\phi}_n$ For prismatic wide beams with a rectangular cross section and $N = bhE\varepsilon$, eqn (21) can be written as (compare eqn (9))

$$\omega_n(N, w_{\text{max}}) = \frac{\alpha_n^2}{\sqrt{12}} \left(\frac{E}{\rho(1 - v^2)} \right)^{1/2} \times \frac{h}{l^2} \left[1 + \gamma_n \varepsilon (1 - v^2) \left(\frac{l}{h} \right)^2 + \beta_n (1 - v^2) \left(\frac{w_{\text{max}}}{h} \right)^2 \right]^{1/2} \quad (23)$$

Note that the large-amplitude effect requires a (slight) correction of the expressions of the gauge factors given previously

The dependence of the resonance frequency on the amplitude of vibration given by eqn (23) is similar in form to the frequency dependence of a simple spring-mass system with a restoring force having a cubic dependence on the vibration amplitude. An estimate for the coefficients β_1 and β_2 of the fundamental mode and first harmonic, respectively, can be found by substituting the mode shapes for zero axial force into eqn (22). This yields $\beta_1 = 0.528$ and $\beta_2 = 1.228$ for a prismatic clamped-clamped beam with a rectangular cross section. The coefficient β_n depends on the edge conditions of the beam, e.g., for simply supported edges β_n will be higher. In the case of movable axial end supports, the hardening effect will be smaller and can even revert to a softening effect for beams with a sufficiently small aspect ratio l/h [57]. The dependence of the resonance frequency on the vibrational amplitude of the fundamental mode of a rigidly clamped-clamped beam, together with a typical large-amplitude forced response plot, is shown in Fig 4. This Figure also indicates the effect of the magnitude of the driving force on the response plot [61]. If the magnitude of the driving force exceeds a critical value F_{crit} , the amplitude becomes three-valued within a range of frequencies. This frequency interval defines the region of hysteresis, with two stable points, one at a large amplitude and the other at a small amplitude. To avoid hysteresis, the

magnitude of the driving force should be smaller than the critical load. It can be shown that the critical load is inversely proportional to $Q^{3/2}$, where Q is the quality factor of the resonator [61]. At the critical load, the amplitude of vibration is defined as the critical amplitude $w_{\text{max crit}}$, being inversely proportional to $Q^{1/2}$. Considering a clamped-clamped beam to behave as a simple spring-mass system with a restoring force having a cubic dependence on the amplitude, it can be shown [61] that the critical amplitude can be approximated by

$$w_{\text{max crit}}/h \approx [2/(Q\beta_n(1-\nu^2))]^{1/2}$$

Hence, even though a high Q has several advantages as indicated in the previous Section, it enhances the chance of hysteresis occurring.

Noise or other instabilities of the vibrational amplitude will limit the ultimate frequency resolution or stability of the gauge. Any frequency change caused by an amplitude change must be small compared to the minimum frequency change one wishes to resolve. It can be derived from eqns (23) and (12) that a condition, which defines an upper limit for the variations Δw_{max} in the amplitude, is given by

$$\left(\frac{\Delta w_{\text{max}}}{w_{\text{max}}}\right) \ll \left(\frac{\gamma_n}{2\beta_n G_{\text{en}}}\right) \left(\frac{l}{w_{\text{max}}}\right)^2 \left(\frac{\Delta \omega}{\omega}\right)_{\text{min}} \quad (w_{\text{max}} < w_{\text{max crit}}) \quad (24)$$

where $(\Delta \omega/\omega)_{\text{min}}$ is the minimum resolution required. For a clamped-clamped beam with an aspect ratio $l/h = 200$, $l/w_{\text{max}} = 10^5$, zero residual strain ($\epsilon_0 = 0$) and a minimum frequency resolution of 10^{-6} , eqn (24) demands a relative variation of the maximum amplitude much smaller than 0.5. If the beam thickness $h = 1 \mu\text{m}$, this means that $w_{\text{max}} = 2 \text{ nm}$ and $\Delta w_{\text{max}} \ll 0.5 \text{ nm}$. The critical amplitude in this case is approximately equal to 20 nm for $Q = 10,000$.

Excitation and detection of the vibration

To measure the resonance frequency of a vibrating beam, it must first be excited into vibration and subsequently the vibrational motion must be detected. Mathematically, the driving load $q(x, t)$ used to excite the resonator can be accounted for in the inhomogeneous part of the differential equation of motion, as indicated by eqn (1). In

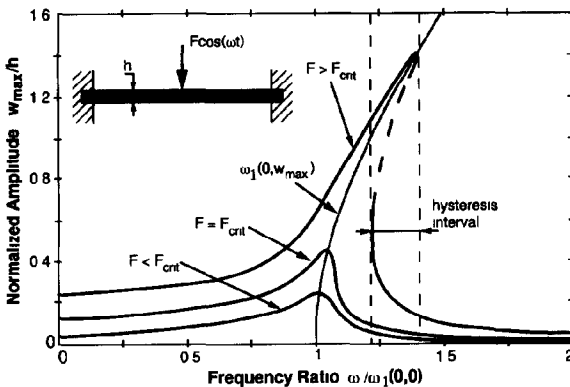


Fig 4 Forced response plots, showing the normalized amplitude vs the normalized frequency for a clamped-clamped beam with a rectangular cross section, illustrating the effect of a large vibrational amplitude. If the magnitude F of the excitation force exceeds a critical value F_{crit} , the amplitude becomes three-valued for a particular frequency interval. The dashed part of the curve in this interval indicates unstable points [61].

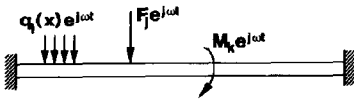


Fig 5 Schematic representation of excitation loads

general, for flexurally vibrating structures the load $q(x, t)$ represents (harmonically varying) bending moments or transverse forces

$$q(x, t) = q(x) \exp(i\omega t) = \left[\sum_i q_i(x) + \sum_j F_j \delta(x - x_j) + \sum_k M_k \delta_{-1}(x - x_k) \right] \exp(i\omega t) \quad (25)$$

where $q_i(x)$ is a distributed force per unit length, F_j is a point force applied at $x = x_j$, M_k is a point moment applied at $x = x_k$, ω is the frequency of excitation and δ_{-1} is the derivative of the Dirac function (see also Fig 5)

An expression for the overall response can be obtained from a modal analysis [62–64]. The distribution of the driving load along the beam length determines the efficiency of excitation of a particular mode of vibration. For instance, if the driving load is symmetric with respect to the centre of the beam, it is (theoretically) impossible to excite an anti-symmetric mode, e.g., the first harmonic ($n = 2$). A measure for the efficiency of excitation of a particular mode is the generalized load P_n , given by the inner product of the shape function $\phi_n(x)$ of mode n and of the driving load $q(x)$ [64]

$$P_n \equiv \int_0^l q(x) \phi_n(x) dx \quad (26)$$

A large value for P_n implies a large contribution of mode n to the overall response of the resonator

Several excitation/detection schemes have been described in the literature

electrostatic excitation/capacitive detection [21, 25, 41, 42, 65–67]

magnetic excitation/magnetic detection [19, 24, 68]

piezoelectric/piezoelectric [14, 26, 69, 70]

electrothermal/piezoresistive [49, 71–74]

optothermal/optical [23, 75–82]

dielectric/capacitive [83]

For the first two methods the driving load can be modelled as a distributed transverse force $q_i(x)$ and the remaining four methods are modelled as a number of point moments $M_k \delta_{-1}(x - x_k)$. Since a discussion of the various means of excitation and detection has been given in the recent literature [5, 79, 84], only a brief summary will be given here

In the case of *electrostatic excitation*, the driving load is simply the attractive force between the two plates or electrodes of a capacitor. One electrode is formed by (a part of) the beam and the other by a (stationary) surface located at a close distance from the beam. *Capacitive detection* is based on the fact that an a.c. current will flow through a d.c.-biased capacitor if the distance between the capacitor plates, and therefore also the capacitance, fluctuates. This scheme is very attractive from a technological point of view, fabrication of micromechanical resonators and integration with electronics is relatively easy [41, 66, 67]. However, if the electrical feedthrough and/or parasitic loads are too large, these effects will obscure the detection signal of the mechanical resonance. As a consequence, on-chip buffering and/or amplification is generally necessary. Furthermore, for proper operation, a d.c. polarization voltage is required. This voltage will reduce the dynamic stiffness of the structure and will therefore result in a lowering of the resonance frequency [65, 85]. Also, instability will occur if the polarization voltage exceeds the so-called pull-in voltage [65, 85]. For precision measurements, the dependence of the resonance frequency on the polarization voltage and the instability problem require very stable voltages and amplitudes of vibration.

The Lorentz force experienced by a current-carrying wire in the presence of a magnetic field forms the driving force for a *magnetically excited* resonator. Due to a change in area of the current loop, the magnetic flux passing through the loop will change if the beam vibrates. This will induce a voltage in the loop, providing the detection signal. Fabrication is relatively simple, but problems arise with packaging. A magnet needs to be positioned close to the resonator. Another way to develop the static magnetic field is by means of an electrical current flowing through a wire (or coil) that is in close proximity to the resonator, e.g., a design employing a double-ended tuning

fork [68] Problems arise with heat generation, resulting in a temperature difference between the beam and the support, which will induce compressive axial forces and thus results in a lowering of the resonance frequency [13, 73]

Piezoelectric excitation and piezoelectric detection are based on the inverse piezoelectric effect and the direct piezoelectric effect, respectively [86] The inverse piezoelectric effect manifests itself by a mechanical deformation in the material subjected to an electric field If the piezoelement is rigidly fixed on top of the beam, a bending moment will be developed which is used to excite the beam Conversely, through the direct piezoelectric effect a mechanical stress or strain will generate a dielectric displacement in the material, which can be detected as an electric current in an external circuit This method of excitation/detection has been widely used for quartz resonators, since quartz itself is piezoelectric [7] Thin films of piezoelectric materials such as zinc oxide (ZnO) or aluminium nitride (AlN) are very attractive for use in silicon-based resonators ZnO has been investigated extensively for applications as an actuation material [87–91] Due to its strong piezoelectric coupling efficiency, it is a very attractive material for excitation and detection of the vibrational motion of a resonator A problem, however, is created because of the high d.c. conductivity, which prevents the build-up of an electric field Applications at low frequencies (<1 MHz) therefore require special configurations, such as the use of insulating layers or a depleted MOS-like structure [90], which make the fabrication process more complicated and the composite resonator more susceptible to temperature fluctuations as a result of differential thermal expansion effects Furthermore, ZnO is not an IC-compatible material and special precautions such as encapsulation of the ZnO layer in silicon nitride layers [92] are necessary to avoid zinc contamination and to protect the ZnO layer against the different etchants used Also, a lot of effort is necessary to study the reproducibility and the effects of heat treatment, humidity and deposition conditions on the mechanical and electrical properties of the ZnO film

Electrothermal excitation is based on the thermal expansion of a resistive material due to heat generation by an electrical current If the resistor is located in the upper fibres of the beam, a

temperature gradient in the thickness direction will develop This in turn creates a bending moment, which is used to excite the beam The motion is detected by piezoresistors, made of doped polycrystalline silicon for example This method is very attractive from a technological point of view Standard IC processing technologies can be used to fabricate the resonator An inherent problem is the static heat generation causing compressive axial forces, which will affect the resonance frequency [13, 73] For precision measurements this requires a good control of the heat flow to the surroundings

The basic principle of *optothermal excitation* is the same as for electrothermal excitation The difference is the heat source, which is now formed by the absorption of light by bare silicon or an absorbing layer, e.g., aluminium [93] Several techniques are used for *optical detection*, such as intensity modulation by means of a shutter controlled by the resonator [81], use of an optical proximity or displacement sensor [94], or interferometric techniques [23, 58, 78, 80] Optical sensors are very attractive for applications where there is no reliable electrical solution, such as under extreme environmental or hazardous conditions Fabrication of the resonator is relatively simple, but the integration with the optical (fibre) system makes the realization more complicated Further, there is a frequency dependence on the optical drive power as a result of thermally induced axial forces [73, 95]

Dielectric excitation is based on the lateral deformation of a dielectric thin film, sandwiched between a top and bottom electrode, due to an electrostatic force arising if a voltage is applied across the electrodes The lateral deformation will cause bending moments that are used to drive the structure The *detection* is capacitive, based on the change of the capacitance of a dielectric capacitor if the dielectric is deformed So far, the method seems promising, but the signals appear to be extremely small Only if materials with a very high permittivity, such as PZT, having a reported permittivity as large as 2500 for a thin film [96], are used is this method interesting for future applications

It is clear that none of the excitation/detection methods described above is perfect They all have certain advantages and disadvantages The choice of a particular method is determined by several

criteria first of all, the kind and number of materials that are required for fabrication. In this respect, considerations concerning aging of material properties, fatigue, yield strength, stress relaxation, etc., and differential thermal expansion effects are important. A homogeneous structure, preferably consisting of a single-crystalline material, seems to be ideal. Another relevant aspect is the signal-to-noise ratio. A big problem is caused by noise and other interference signals (e.g., electrical feed-through), which can obscure the mechanical resonance. This also requires special attention to the overall design of the structure, including shielding, minimization of parasitic loads, on-chip electronics for buffering, etc. An efficient transduction mechanism, e.g., using ZnO, is preferred to obtain a large signal level. Another constraint is formed by the complexity of the fabrication process with respect to cost, yield and through-put, and further by the technology that is available, or whether it can be used in an IC environment or not.

Fabrication technology

The technology described in this Section refers to the micromachining of silicon, silicon-based materials, metals and special transducer materials such as ZnO. A global overview will be given and for processing details, reference is made to the literature.

Several technologies have been developed over the past three decades to fabricate micromechanical resonators. In general, two main technologies can be distinguished: bulk micromachining [97–99] and surface micromachining [100–102]. Combinations of both have also been used.

In the case of bulk machining, a piece of silicon is sculptured into a three-dimensional structure using sophisticated etching techniques such as anisotropic etching [103–107], high boron etch stops [105, 108], electrochemical etching [109–114] or HF anodic etching [115, 116]. Examples of resonating structures built this way are resonating pressure sensors [21, 23, 28, 29, 72, 81, 94], a resonating force sensor [14, 26], resonating accelerometers [49, 80, 117], a resonating mass-flow sensor [118, 119] and a vibration sensor [120].

Surface micromachining is generally associated with the deposition of thin films and sacrificial layer

etching techniques [102, 121]. The first prototype of a resonator fabricated this way was demonstrated by Nathanson *et al.* in 1967 [65]. They used metal films for both the construction material and the sacrificial layer. More recently, ‘construction material/sacrificial layer’ combinations of polysilicon/oxide [41, 43, 66, 122, 123, 124], polysilicon/nitride [124], nitride/(poly)silicon [118, 119, 125–127], oxide/silicon [128] and polyimide/aluminium [129] have been used. Prototypes of resonating structures include a resonant vapour sensor [41], a resonating mass-flow sensor [118], a resonant force sensor [25, 60], a resonating accelerometer [117] and resonating polysilicon microbridges [41, 43, 66, 123].

As mentioned before, resonant sensors are very attractive in the precision measurement field. However, in order to exploit the advantageous properties, unwanted disturbances have to be eliminated and a high Q -factor must be obtained. This requires vacuum encapsulation. An elegant way of accomplishing this was first demonstrated by Ikeda *et al.* in 1988 [24, 130]. Figure 6 shows the basic structure of a differential pressure sensor using a sealed resonator as the strain-sensing element. This new concept requires an extended definition of the gauge. The term resonant force/strain gauge not only includes the vibrating element itself, but also the evacuated cavity and the shell surrounding the cavity. The shell forms an integral part of a resonant force gauge.

The fabrication process of sealed resonators as described by Ikeda *et al.* is based on selective epitaxial growth of boron-doped single-crystalline silicon [131], high boron etch stops and selective electrochemical anisotropic etching. Very heavily boron-doped (p^{++}) silicon layers are used as the construction material and heavily boron-doped (p^+) silicon layers as the sacrificial layer. The p^{++} layers are not attacked by the anisotropic etchant.

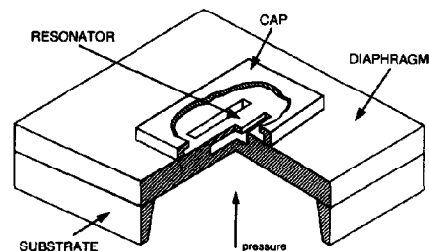
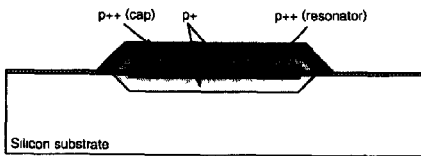


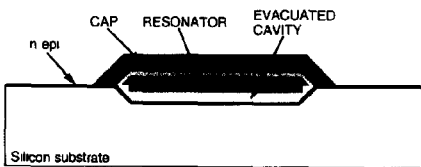
Fig. 6 Example of a mechanical sensor consisting of a diaphragm with an encapsulated built-in resonator that can be used as a differential pressure sensor.



(a)

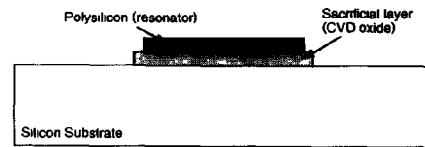


(b)

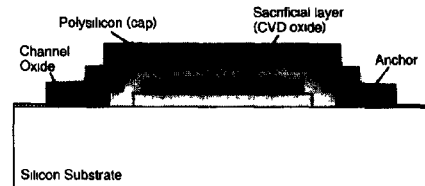


(c)

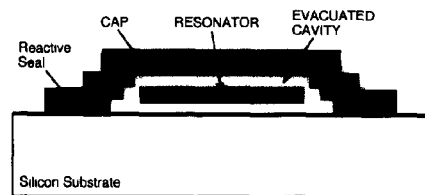
Fig 7 Fabrication process of sealed resonant force gauges using selective epitaxy [130] (a) After oxidation, patterning and HCl etching of silicon, (b) after subsequent selective epitaxial growth of p^+ , p^{++} , p^+ and p^{++} silicon, (c) after removing the oxide, selective etching of p^+ silicon, reactive sealing with n-epi and annealing in N_2



(a)



(b)



(c)

Fig 8 Fabrication process of sealed resonant force gauges using LPCVD polysilicon [43] (a) After deposition and patterning of the first sacrificial layer (CVD or thermal oxide) and the first polysilicon layer, (b) after deposition and patterning of the second sacrificial layer (CVD oxide or nitride), thin thermal oxide for the etch channels and the second polysilicon layer, (c) after the sacrificial layer etch in HF and reactive sealing with polysilicon or silicon nitride

(a mixture of hydrazine and water) due to the high boron concentration [108]. The n-type silicon substrate is protected from the etchant through electrochemical passivation. The cavity is sealed by closing off the etch channels with n-epi. Subsequent high-temperature annealing in a nitrogen atmosphere produces a vacuum cavity (< 1 mTorr) by out-diffusion of the residual hydrogen through the silicon cavity walls. The basic steps of the process are illustrated in Fig 7(a)–(c).

An alternative way of fabricating sealed resonators has been described by Guckel *et al* [43]. Their process is based on sacrificial layer etching and reactive sealing techniques [132]. In this way a hermetically sealed cavity can be formed with a low residual pressure, as indicated by the obtained quality factors of around 35 000. Fine-grained tensile polysilicon, grown using low-pressure chemical vapour deposition (LPCVD) [133, 134], is used as a construction material and silicon oxide and/or nitride can be used as a sacrificial layer. The

sacrificial etchant used is hydrofluoric acid. 'Sticking' of the resonator and the sealing cap to the substrate is avoided by freeze–sublimation procedures [124]. The basic steps for the formation of sealed polysilicon resonators are schematically shown in Fig 8.

A third way of fabricating sealed resonators [135] is based on HF anodic etching [115, 116] and silicon fusion bonding [136]. The results are preliminary but very encouraging.

In deciding which technology to use for the fabrication of sealed resonators, several aspects are worth considering. In the case of selective epitaxy and HF anodic etching, single-crystalline silicon is used as the resonator material. It is expected that a single-crystalline material is more

suitable than polycrystalline materials due to the superior material properties with respect to aging, drift, hysteresis, fatigue, creep, yielding, etc., of the former. A definite statement, however, cannot be made at this point since the study of the material properties of polysilicon is still in a preliminary stage. Selective epitaxy seems to be more complicated and less flexible. For instance, the sealing cap always closely surrounds the resonator. This precludes the sealing of more than one resonator in a single cavity, e.g., as proposed for a differential design for common-mode rejection purposes [137]. In addition, as a result of the high deposition rate (300 nm/min) of epitaxially grown silicon, it will be difficult to realize very thin ($< 1 \mu\text{m}$) resonators in an accurately controlled and reproducible way. For very thin resonators, LPCVD polysilicon (deposition rate of the order of 7 nm/min) seems to be the best candidate. On the other hand, the low deposition rate for polysilicon means long deposition times, which makes this technology less attractive. If the resonator thickness exceeds $2\text{--}3 \mu\text{m}$, LPCVD polysilicon is no longer practical.

It is pointed out here that in the process descriptions given above, no special attention is paid to the excitation/detection mechanism used. Ikeda's resonator is driven magnetically and no additional processing on the resonator is required, since the p^{++} resonator is already conductive enough. Guckel's resonator is driven electrothermally or electrostatically and detection is done piezoresistively. This requires additional processing on the resonator to form the polyresistors and the electrodes. This can be done in a convenient way by means of local implantation of impurities, e.g., boron. The fabrication of a piezoelectrically driven resonator, on the other hand, creates new challenges to the process engineer. A question that arises is how subsequent heat treatments affect the properties of the piezoelectric layer. This might exclude epitaxial growth of silicon, since this is done at relatively high temperatures ($1000\text{--}1150^\circ\text{C}$). Also, the piezoelectric layer should either be resistant to the sacrificial layer etchant, or it should be protected against the etchant by encapsulating the piezomaterial in a passivation layer.

Another relevant aspect is the final stress state of the (composite) resonator caused by the residual stresses in the applied materials. In general, it is

preferred to have the resonator under small tension. This minimizes the chance of buckling and allows long beams to be fabricated. A large tension is not attractive, since this will lower the gauge factor and thus the sensitivity of the device, see Fig. 2.

Design aspects and performance issues

The sensitivity of a resonant force/strain gauge to an applied (mechanical) load depends on the gauge factor of the resonator. Large gauge factors require slender beams with a low residual strain.

In a sensor system, the resonant force gauge will be the frequency-determining building block of an electronic oscillator. As indicated by eqn (24), automatic gain control (AGC) is necessary to minimize error readings due to a variable amplitude of vibration. Improved behaviour of a feedback oscillator as a result of AGC has been experimentally demonstrated by Ikeda *et al* [59].

Unwanted frequency shifts are not only caused by spreads in the vibrational amplitude, but can also be caused by a variety of physical and chemical loads, e.g., mass loading due to surrounding fluid, temperature, humidity, vapour adsorption, dust, etc. Most of these disturbing loads can be eliminated by isolating the gauge from its surroundings, e.g., through vacuum encapsulation. Temperature very often remains as a major source of errors. Material properties such as Young's modulus and the resonator dimensions are all temperature dependent and, as a result, a temperature change will induce a shift of the resonance frequency. Moreover, differential thermal expansion effects within the composite resonator or between the sensor chip and the mount can strongly degrade the performance of the device. Solutions to this problem are found in electronic temperature compensation (requiring an on-chip temperature sensor), accurate temperature regulation of the sensor environment and/or by employing a differential resonator design [137]. Other common-mode errors that are suppressed in a differential design are variations in the reference clock frequency, aging of material properties, even-order non-linearity effects and, last but not least, mounting or package-induced stresses. A further reduction of mounting strains is achieved

if stress-free assembly techniques [138] or mechanical decoupling zones [139] are used

Factors that might limit the resolution are the excitation/detection scheme used and, of course, the noise in the system [140]. If the resonator is regarded as a simple harmonic oscillator with an angular frequency of resonance ω_0 , and if the feedback oscillator is locked at the frequency where the phase shift is $\pi/2$ radians, i.e., at $\omega = \omega_0$, the minimum relative frequency resolution is given by

$$(\Delta\omega/\omega)_{\min} = (1/2Q) \Delta\phi_{\min}$$

where Q is the mechanical quality factor of the resonator and $\Delta\phi_{\min}$ the minimum phase shift that can be detected by the oscillator. Hence, the resolution is inversely proportional to the quality factor Q . The minimum phase shift that can be resolved is determined by the resolution of the detection mechanism and by the noise in the entire system.

As already indicated above, the ultimate resolution of the resonant force gauge is determined by several factors: temperature sensitivity and variations, stability of electrical components of the feedback oscillator, stability of the environment and the quality factor of the resonator. These factors actually determine the short-term resolution or stability $(\Delta\omega/\omega)_{s, \min}$, which can be expressed mathematically as

$$\left(\frac{\Delta\omega}{\omega}\right)_{s, \min} = \max \left[\left(\frac{\Delta w_{\max}}{w_{\max}} \right)^2 \left(\frac{w_{\max}}{l} \right)^2 \left(\frac{2\beta_n G_{en}}{\gamma_n} \right), \right. \\ \left. \frac{1}{2Q} \Delta\phi_{\min}, G_T \Delta T_{\min}, G_L \Delta L_{\min}, \right] \quad (27)$$

where max is the 'maximum' function, the first argument between the brackets can be obtained from eqn (24), $G_T = (1/\omega)(\partial\omega/\partial T)$, the relative temperature sensitivity of the gauge and $G_L = (1/\omega)(\partial\omega/\partial L)$, the relative sensitivity of the gauge to any other unwanted load L , e.g., humidity, ΔT_{\min} and ΔL_{\min} are the minimum variations in temperature and other unwanted loads seen by the resonator, respectively. The resolution Δp_{\min} , defined as the smallest change in load, e.g., a pressure change, that can be distinguished by the sensor structure (e.g., the pressure sensor as shown in Fig. 6) is given by

$$\Delta p_{\min} = (1/G_p)(\Delta\omega/\omega)_{s, \min}$$

where $G_p = (1/\omega)(\partial\omega/\partial p)$, the relative frequency sensitivity of the sensor to the applied mechanical load p .

In speaking of long-term resolution or stability, aging phenomena, creep and stress relaxation become relevant. Long-term drift requires frequent recalibration of the system. This generally concerns drift of material properties and it is expected that single-crystalline materials have more stable properties than polycrystalline or amorphous materials. Therefore, single-crystalline materials are preferred. Also, the intrinsic quality factor of these materials is higher.

According to Karrer and Ward [141], the response time is determined by (1) the time the resonator is maintained at the old load, (2) the magnitude of the load change, and (3) the desired degree of stability. It is expected that the response time is small compared to the time required for counting the frequency shift, especially in high-precision sensors.

Finally, mode interference, or in other words interference of unwanted modes with the desired mode, is a relevant issue. For complex resonator shapes, the frequencies of the different modes of vibration can be very close to each other and they all have different sensitivities to the axial load, e.g., [49, 142]. The dynamic range or measurement window of the gauge will be limited to the frequency range where modes do not interfere, since only here will the frequency be a single-valued function of the axial load. The best way to increase the dynamic range is to keep the resonator structure simple and, moreover, to design and place the excitation/detection elements in such a way that the unwanted modes are not excited (see also eqn (26)) and/or cannot be detected.

Conclusions

Resonant force gauges are very attractive for precision measurements because of their high sensitivity, high stability and frequency output. Micro-machining of the gauges allows batch fabrication to take place, with possible on-chip electronics, manufacturing costs to be reduced and reproducibility to be improved.

To be effectively employed in high-performance sensors, resonant force gauges must be isolated from the environment to eliminate frequency shifts caused by unwanted loads. A very promising way of doing this, which might define the direction of future research, is by means of local vacuum encapsulation of the gauge in a batch fabrication process. From this point of view the cavity and the enclosing shell form an integral part of the gauge. Temperature will always remain as a disturbing load and special attention must be given not only to the force gauge, but also to the design of the entire sensor chip, including packaging aspects to reduce differential thermal expansion effects.

Single-crystalline materials such as single-crystalline silicon and quartz have highly stable properties with low hysteresis and creep, which makes them very suitable for the fabrication of resonant force/strain gauges. The potential application of other materials such as thin films of polycrystalline silicon and silicon nitride should be further investigated with respect to stability and repeatability of mechanical properties, because they are very attractive from a micromachining point of view. Complex mechanical structures, including sealed resonators, can relatively easily (as compared to quartz and single-crystalline silicon) be fabricated. Furthermore, the thin-film/sacrificial layer technology is very flexible and versatile. Also, more effort must be put into the development of new technologies for micromachining single-crystalline silicon, such as dopant-selective electrochemical etching and HF anodic etching. A challenge is formed by the proper selection and implementation of a suitable excitation/detection scheme that has a minimal degrading effect on the resonator performance.

The feasibility of silicon resonant force gauges has already been demonstrated by a large number of laboratory prototypes, but as indicated in this paper, a long way still has to be gone to demonstrate their applicability in a real environment.

Acknowledgements

The authors would like to thank Dr Siebe Bouwstra for many fruitful discussions and his valuable comments on the manuscript.

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