

# **Radio Frequency Circuits & Antenna**

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**Homework: 5**

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# 1 Complete the entries in the following table:

Remarks on general equations:

$$VSWR = \frac{1 + |\Gamma|}{1 - |\Gamma|} \iff |\Gamma| = \left| \frac{1 - VSWR}{1 + VSWR} \right| \quad (1)$$

$$|\Gamma| = \sqrt{P_r/P_f} \quad (2)$$

$$T = \sqrt{1 - |\Gamma|^2} \iff |\Gamma| = \sqrt{1 - T^2} \quad (3)$$

$$RL(dB) = 10 \log_{10} \frac{P_i}{P_r} = -20 \log_{10} |\Gamma| \iff |\Gamma| = 10^{-RL/20} \quad (4)$$

$$IL(dB) = 10 \log_{10} \frac{P_T}{P_R} = -20 \log_{10} (|T|) \iff |T| = \sqrt{1 - 10^{-IL/10}} \quad (5)$$

$VSWR$	$ \Gamma $	$RL(dB)$	$ T $	$IL(dB)$
1.02	0.01	40	0.99995	0.000434
1.1	0.05	26	0.99874	0.011
1.22	0.099	20.078	0.995	0.04286
1.49687	0.1989997	14.023	0.98	0.17547
1.86	0.3	10.5	0.954	0.41
2.337	0.40067	7.944	0.91622	0.76
3	0.5	6.02	0.866	1.249587
4	0.6	4.437	0.8	1.9382
9	0.8	1.9365	0.6	4.44

## 2 Complete the entries in the following table:

Remarks on general equations:

$$P[dBm] = 10 \log_{10} P[mW] \quad (6)$$

$$P[W] = 10^3 P[mW] \quad (7)$$

$P[W]$	$P[mW]$	$P[dBm]$
$10^{-4}$	0.1	-10
$10^{-3}$	1	0
$10^{-2}$	10	10
0.015	15	11.76
0.02	20	13.01
0.1	100	20

## 3 An amplifier with a gain of 11[dB], a bandwidth of 150[MHz], and a noise figure of 3.8[dB] feeds a receiver with a noise temperature of 935[K]. Find the noise figure of the overall system.

$$F_{tot} = F_1 + \frac{F_2 - 1}{G_1} \quad (8)$$

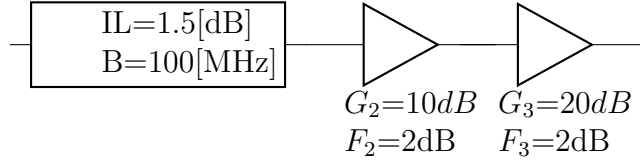
$$= 3.8[dB] + \frac{1 + T_e/T_o - 1}{11[dB]} \quad (9)$$

$$= 10^{0.38} + \frac{T_e}{10^{1.1} T_o} \quad (10)$$

$$= 2.4 + \frac{935}{12.59 \cdot 290} = 2.4 + 0.2561 \quad (11)$$

$$F_{tot} = 2.656 \rightarrow 4.242[dB] \quad (12)$$

- 4 Consider the wireless local area network (WLAN) receiver front-end shown below, where the bandwidth of the bandpass filter is  $100[MHz]$  centered at  $2.4[GHz]$ . The system is at the room temperature.



- a) Find the noise figure of the overall system.

$$L = 10^{1.5/10} = 1.41 \quad \wedge \quad G_1 = L^{-1} \quad (13)$$

$$F_2 = 10^{2/10} = 1.585 \quad \wedge \quad G_2 = 10^{10/10} = 10 \quad (14)$$

$$F_3 = 10^{2/10} = 1.585 \quad \wedge \quad G_3 = 10^{20/10} = 100 \quad (15)$$

$$F_{tot} = F_1 + \frac{F_2 - 1}{G_1} + \frac{F_3 - 1}{G_1 G_2} \quad (16)$$

$$= 1.41 + \frac{1.585 - 1}{1/1.41} + \frac{1.585 - 1}{10/1.41} \quad (17)$$

$$F_{tot} = 2.317 \rightarrow 3.65[dB] \quad (18)$$

- b) What is the resulting signal-to-noise ratio at the output, if the input signal power level is -86 dBm?

$$P_{in} = -86[dBm] = 2.512 \cdot 10^{-9}mW \quad (19)$$

$$P_{out} = (P_{in} + G_2 + G_3 - L)[dBm] = \quad (20)$$

$$= -86 + 10 + 20 - 1.5 \quad (21)$$

$$= -57.5[dBm] \quad (22)$$

$$= 1.78 \cdot 10^{-6}mW \quad (23)$$

Noise effect:

$$N = G \cdot K \cdot T \cdot B \quad (24)$$

$$G = -1.5 + 10 + 20 = 28.5[dB] \rightarrow 10^{2.85} = 707.95 \quad (25)$$

$$K = 1.38 \cdot 10^{-23}[J/K] \quad (26)$$

$$T = (F_{tot} - 1)T_0 = (2.317 - 1)290 = 381.9[K] \quad (27)$$

$$B = 100[MHz] = 10^8[Hz] \quad (28)$$

$$\therefore N = 707.95 \cdot 1.38 \cdot 10^{-23} \cdot 381.9 \cdot 10^8 \quad (29)$$

$$= 3.73 \cdot 10^{-7}[mW] \rightarrow -64.3[dBm] \quad (30)$$

$$SNR = \frac{P_{out}}{N_{out}} = -57.5 - (-64.3) = 6.8[dB] \rightarrow 4.79 \quad (31)$$

c) Can the components be arranged to give a better noise figure?

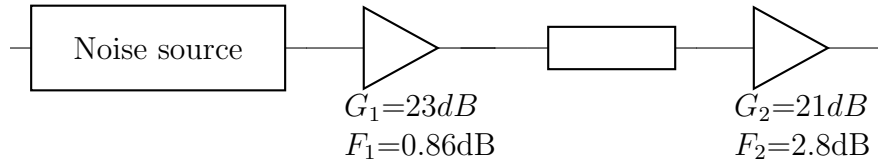
Yes, by reversing the order of the system we would get:

$$F_{tot} = F_1 + \frac{F_2 - 1}{G_1} + \frac{F_3 - 1}{G_1 G_2} \quad (32)$$

$$= 1.585 + \frac{1.585 - 1}{100} + \frac{1.41 - 1}{1000} \quad (33)$$

$$F_{tot} = 1.59 \rightarrow 2.02[dB] \quad (34)$$

## 5 Consider the next system:



a) Find the equivalent noise temperature and the noise figure of the system (without the noise of the source).

$$G_1 = 23[dB] \rightarrow 199.5 \quad \wedge \quad F_1 = 0.86[dB] \rightarrow 1.22 \quad (35)$$

$$L = 0.9[dB] \rightarrow 1.23 \quad \wedge \quad T = 315 \quad (36)$$

$$G_2 = 21[dB] \rightarrow 125.9 \quad \wedge \quad F_2 = 2.8[dB] \rightarrow 1.91 \quad (37)$$

$$T_1 = (F_1 - 1)T_0 = (1.22 - 1)290 = 63.8[K] \quad (38)$$

$$T_2 = (F_2 - 1)T_0 = (1.91 - 1)290 = 263.9[K] \quad (39)$$

$$T_L = (L - 1)T_0 = (1.23 - 1)315 = 72.45[K] \quad (40)$$

$$T_{tot} = T_1 + \frac{T_L}{G_1} + \frac{T_2 \cdot L}{G_1} \quad (41)$$

$$= 63.8 + \frac{72.45}{199.5} + \frac{263.9 \cdot 1.23}{199.5} \quad (42)$$

$$T_{tot} = 65.8[K] \quad (43)$$

$$F_T = 1 + T_{tot}/T_0 \quad (44)$$

$$= 1 + 65.8/290 = 1.23 \quad (45)$$

$$F_T = 0.89[dB] \quad (46)$$

- b) Find the output noise power of the system, if it's bandpass is  $103MHz$  and the noise power of the source is  $N_i = -92[dBm]$ .

$$N_{in} = -92[dBm] \quad (47)$$

$$= 10^{-9.2} \rightarrow 6.31 \cdot 10^{-10}[mW] \quad (48)$$

$$G_{tot} = (23 - 0.9 + 21)[dB] \quad (49)$$

$$= 43.1[dB] \rightarrow 10^{4.31} = 20417.38 \quad (50)$$

$$N_{out} = N_{in}G_{tot} + KBT_{tot}G_{tot} \quad (51)$$

$$= (N_{in} + KBT_{tot})G_{tot} \quad (52)$$

$$= (6.31 \cdot 10^{-10} + 1.38 \cdot 10^{-23} \cdot 103 \cdot 10^6 \cdot 65.8)20417.38 \quad (53)$$

$$= 1.34 \cdot 10^{-5}mW = 48.7[dBm] \quad (54)$$

- 6 A certain transmission line has a noise figured  $F = 1.2[dB]$  at a temperature of  $T_0 = 290[K]$ . Calculate and plot in "Matlab" the noise figure of this line (in dB) as its physical temperature ranges from  $T = 0 \rightarrow 1200[K]$ .

$$F(T) = 1 + (L - 1)T/T_0 \quad (55)$$

$$F(T_0) = L = 1.2[dB] \rightarrow 1.318 \quad (56)$$

