S-061 Assignment 1

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Part 1: Classical Test Theory & Validation

1) On the basis of this correlation, the researcher states that the reliability of the ratings is 0.7. What *score* is she assuming is relevant, that has a reliability of 0.7? Is it the score from e-Rater A? The score from e-Rater B? Some combination of both scores? A score from any single e-Rater? Or other?

The researcher is referring to the reliability of the scores generated by the population of e-Raters (or equivalently, scoring algorithms) for this specific essay prompt, from which e-Raters A and B came. For example, we could imagine the company developing or acquiring another algorithm called e-Rater C, whose pairwise correlations with A and B should be 0.7.

2) If the researcher considers 0.7 to be the reliability, what is the replication that she assumes is relevant? What is random, and what is fixed?

The replication is the scoring process involving a random e-Rater (or, scoring algorithm). The e-Rater/scoring algorithm is random, but the students' abilities, form, and testing occasion are fixed.

3) Apply Spearman-Brown (actually perform a calculation) to estimate the reliability of the average these two e-Rater scores.

```
# create function to calculate Spearman-Brown
SB_Rho <- function(k, rho) {
    return(k * rho/(1 + (k - 1) * rho))
}

# conceptually, this is the corr between two sets of e-Raters A&B and C&D
pander(paste0("Spearman-Brown Rho: ", round(SB_Rho(2, 0.7), 2)))
```

Spearman-Brown Rho: 0.82

4) The company asks you what a valid use of the third score would be. Remember this score is available for only 10% of examinees. Should the company use this score alone? Should it use the unweighted average of the three scores (the two e-rater scores and the human score)? Should it ignore the score and use the average of the two e-Rater scores? Answer the following questions:

a) If you were an examinee with a high (well above average) true score, would you rather have the human score, the average of the two e-rater scores, or the average of all three scores?

We would want the average of all three scores to minimize the error variance. The more measurements we have of a given individual's score, the more likely it is that the average error will equal 0, (as the number of measurements approaches infinity, it should equal exactly 0), thus revealing the individual's true score.

b) If you were an examinee with a low (well below average) true score, would you rather have the human score, the average of the two e-rater scores, or the average of all three scores?

Because we can assume the human score is equally accurate and equally covarying with the e-Raters, we would rather have the single human score. This gives me a higher chance of having a large error to potentially mask my low "true score."

c) Weighing all considerations for the intended use of these scores for college admissions, what would be your recommendation to the company for how they should use this third score?

We recommend ignoring the third score and only use the average of the e-Raters for admissions purposes. Since this third score is only available for 10% of students, by averaging scores for that subgroup, we'd increase the precision (i.e., reduce the error variance) for their scores. That is, for 10% of people, they're more likely to be disadvantaged if their true score is low and more likely to be advantaged if their true score is high. Since this advantage/disadvantage is not available to the rest of the sample, it would be unfair.

Part 2: Classical Test Theory and Exploratory Analysis

```
# Read in data
data_raw <- read_dta("./Assignment1.dta")
```

5) Using Stata, calculate coefficient alpha for the first occasion and the second occasion separately. In a sentence or two, interpret coefficient alpha for the first occasion (see also Question 16).

```
# create variable lists
o1 <- paste0("x_o1_i", 1:12)
o2 <- paste0("x_o2_i", 1:12)
# subset data
data_o1 <- subset(data_raw, select = o1)
data_o2 <- subset(data_raw, select = o2)
# create alpha output
alpha1 <- alpha(data_o1)
alpha2 <- alpha(data_o2, keys = NULL, title = NULL, cumulative = FALSE, max = 10,
    na.rm = TRUE, check.keys = TRUE, n.iter = 1, delete = TRUE)
# get just the alpha numbers
alpha_time1 <- alpha1$total$std.alpha
alpha_time2 <- alpha2$total$std.alpha
# output alpha data alpha1 alpha2
```

Reliability analysis
raw_alpha std.alpha G6(smc) average_r S/N ase mean sd 0.88 0.87 0.94 0.36 6.9 0.033 2.6 0.91

Table 1: First occasion

raw_alpha	std.alpha	G6(smc)	average_r	S/N	ase	mean	sd
0.8804	0.8732	0.9384	0.3647	6.888	0.0332	2.557	0.9115

- **alpha.drop**:

	raw_alpha	std.alpha	G6(smc)	average_r	S/N	alpha se
x_o1_i1	0.857	0.849	0.9194	0.3382	5.621	0.04023
x_o1_i2	0.8665	0.8572	0.9172	0.353	6	0.03655
x_o1_i3	0.879	0.8718	0.9256	0.3821	6.803	0.03356
x_o1_i4	0.8587	0.8504	0.9219	0.3407	5.684	0.03957
x_o1_i5	0.8638	0.8555	0.9308	0.3499	5.92	0.03794
x_o1_i6	0.8669	0.8601	0.9257	0.3586	6.149	0.03708
x_o1_i7	0.8734	0.8641	0.9304	0.3664	6.36	0.03516
x_o1_i8	0.8744	0.8658	0.9324	0.3697	6.452	0.03503
x_o1_i9	0.8797	0.8706	0.9295	0.3794	6.725	0.03281
x_o1_i10	0.862	0.8545	0.9216	0.348	5.871	0.03863
x_o1_i11	0.8878	0.8871	0.9404	0.4166	7.855	0.0326
x_o1_i12	0.8756	0.8677	0.9223	0.3735	6.557	0.03455

Reliability analysis

raw_alpha std.alpha G6(smc) average_r S/N ase mean sd 0.85 0.85 0.92 0.33 5.8 0.042 2.8 0.85

Table 3: Second occasion

raw_alpha	std.alpha	G6(smc)	average_r	S/N	ase	mean	sd
0.8547	0.8539	0.9187	0.3276	5.845	0.04195	2.76	0.8516

- **alpha.drop**:

	raw_alpha	std.alpha	G6(smc)	average_r	S/N	alpha se
x_o2_i1	0.8413	0.8396	0.893	0.3224	5.234	0.04566
x_o2_i2	0.8386	0.8379	0.9067	0.3197	5.168	0.04698
x_o2_i3	0.8286	0.8289	0.899	0.3057	4.844	0.05015
x_o2_i4	0.8538	0.8533	0.9057	0.346	5.819	0.04223
x_o2_i5	0.8334	0.8325	0.8961	0.3113	4.972	0.04838
x_o2_i6	0.8298	0.8276	0.895	0.3039	4.802	0.04938
x_o2_i7	0.8401	0.8379	0.8998	0.3196	5.168	0.04629
x_o2_i8	0.8498	0.8499	0.9111	0.3398	5.662	0.04361
x_o2_i9	0.8298	0.8298	0.905	0.3072	4.877	0.04977
x_o2_i10	0.8533	0.852	0.9129	0.3435	5.755	0.04244
x_o2_i11	0.8637	0.8632	0.9098	0.3644	6.308	0.03957
x_o2_i12	0.8541	0.854	0.9086	0.3472	5.85	0.04241

For this sample $\alpha_1 = 0.873$ and $\alpha_2 = 0.854$

6) Using Stata, calculate the average score of participants from the first occasion, then calculate the average score of participants from the second occasion. Then, calculate the correlation between the two average scores using code like pwcorr avgscr1 avgscr2. Report this correlation and, in a sentence or two, provide an interpretation (see also Question 16).

```
avg_o1 <- rowMeans(data_o1)
avg_o2 <- rowMeans(data_o2)

cor(avg_o1, avg_o2)
```

```
## [1] 0.790936
```

This correlation represents the reliability of this grit scale across occasions. We would expect the correlation between any two administrations of this survey to have this value.

7) Reload the data and reshape it for analysis in Stata. Although it is a pain, I am requiring you to use some of the code that we have presented in the past .do files to reshape the data from "double-wide" format. See, for example, the Class03.do and Class04.do files. As one way to check your work, submit a screenshot of the output from code like table person item occasion, contents(mean score) and/or simply table person item occasion .

```
data_raw$person <- factor(data_raw$person)
colnames(data_raw) <- c("person", paste0("1_", 1:12), paste0("2_", 1:12))

data_long <- melt(data_raw, id.vars = c("person"))
data_long <- separate(data = data_long, col = variable, into = c("occasion", "item"),
    sep = "_")

data_long[1:20, ]
```

```
##    person occasion item value
## 1       1        1    1     4
## 2       2        1    1     5
## 3       3        1    1     1
## 4       4        1    1     4
## 5       5        1    1     2
## 6       6        1    1     5
## 7       7        1    1     5
## 8       8        1    1     3
## 9       9        1    1     5
## 10     10        1    1     5
## 11     11        1    1     4
## 12     12        1    1     5
## 13     13        1    1     5
## 14     14        1    1     3
## 15     15        1    1     4
## 16     16        1    1     5
## 17     17        1    1     5
## 18     18        1    1     1
## 19     19        1    1     3
## 20     20        1    1     4
```

8) Note the code available to you in the .do files, and include a) a discrete histogram of all 25x12x2 scores, b) a histogram of marginal person scores, c) a histogram of marginal item scores, and d) a histogram of marginal occasion scores. Use discrete histograms where you think they are appropriate, or substitute tables if histograms are not informative, for example, tabulate occasion, summarize(score) . Histograms of interactions are not necessary.

```
# (a) Discrete histogram of raw person-item-occasion scores
qplot(data_long$value, geom = "histogram", main = "Histogram of all 25p x 12i x 2o GRIT Scores",
    xlab = "Person-Item-Occasion Raw Score", ylab = "Frequency", ylim = c(0, 200),
    breaks = rep(1:5, each = 2) + c(-0.3, 0.3))
```

Histogram of all 25p x 12i x 2o GRIT Scores


```
# (b) person average score
marg_person <- ddply(data_long, "person", summarise, mean_p = mean(value))
qplot(marg_person$mean_p, geom = "histogram", main = "Histogram of Person Average GRIT Scores (over 12i
    xlab = "Person Average GRIT Score", ylab = "Frequency", ylim = c(0, 2), xlim = c(1,
        5))
```

Histogram of Person Average GRIT Scores (over 12i and 2o)


```
# (c) item average score
marg_item <- ddply(data_long, "item", summarise, mean_i = mean(value))
qplot(marg_item$mean_i, geom = "histogram", main = "Histogram of Item Average GRIT Scores (over 25p and
    xlab = "Item Average Score", ylab = "Frequency", ylim = c(0, 2), xlim = c(1,
        5))
```

Histogram of Item Average GRIT Scores (over 25p and 2o)


```
# (d) occasion average score
marg_occ <- ddply(data_long, "occasion", summarise, mean_o = mean(value))
pander(marg_occ)
```

occasion	mean_o
1	2.557
2	2.76

Part 3: The Generalizability Study

9) Write out the model implied by the data collection design under the tenets of Generalizability Theory. Draw the Venn diagram for this design.

The model implied here can be written as

$$X_{pi} = \mu + \nu_p + \nu_i + \nu_o + \nu_{pi} + \nu_{po} + \nu_{oi} + \nu_{pio,e}$$
$$\nu_p \sim N(0, \sigma_p^2)$$
$$\nu_i \sim N(0, \sigma_i^2)$$
$$\nu_o \sim N(0, \sigma_o^2)$$
$$\nu_{pi} \sim N(0, \sigma_{pi}^2)$$
$$\nu_{po} \sim N(0, \sigma_{po}^2)$$
$$\nu_{io} \sim N(0, \sigma_{io}^2)$$
$$\nu_{pio,e} \sim N(0, \sigma_{pio,e}^2)$$

The Venn diagram for the variances is seen below:
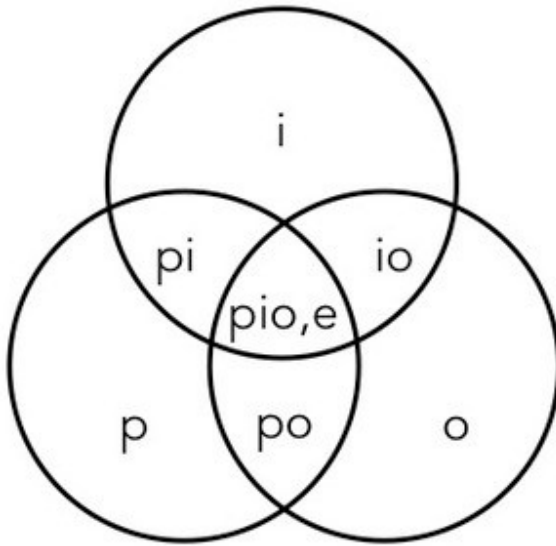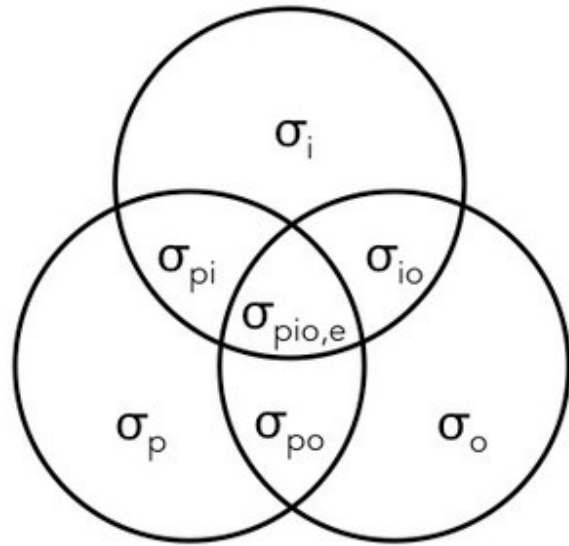
10) Estimate the variance components for this model using the mixed or xtmixed command. Feel free to go get coffee while this runs. Don't forget to create interactions using commands like egen pXi = group(person item). Include a table with four columns, the source of variance, the estimated variance components, their square roots, and their percentage of total score variance.

```
data_long$pxi <- as.factor(100 * as.numeric(data_long$person) + as.numeric(data_long$item))
data_long$pxo <- as.factor(100 * as.numeric(data_long$person) + as.numeric(data_long$occasion))
data_long$oxi <- as.factor(10 * as.numeric(data_long$occasion) + as.numeric(data_long$item))

mixed <- lmer(value ~ 1 + (1 | person) + (1 | item) + (1 | occasion) + (1 | pxi) +
    (1 | pxo) + (1 | oxi), data = data_long)

summary(mixed)
```

```
## Linear mixed model fit by REML ['lmerMod']
## Formula: value ~ 1 + (1 | person) + (1 | item) + (1 | occasion) + (1 |
##     pxi) + (1 | pxo) + (1 | oxi)
##    Data: data_long
##
## REML criterion at convergence: 1900
##
## Scaled residuals:
##      Min       1Q   Median       3Q      Max
## -2.42134 -0.58655 -0.02843  0.54729  2.64540
##
## Random effects:
##  Groups   Name        Variance Std.Dev.
##  pxi      (Intercept) 0.48748  0.6982
##  pxo      (Intercept) 0.10228  0.3198
##  person   (Intercept) 0.57337  0.7572
##  oxi      (Intercept) 0.09958  0.3156
##  item     (Intercept) 0.26306  0.5129
##  occasion (Intercept) 0.01380  0.1175
##  Residual             0.74172  0.8612
## Number of obs: 600, groups:
## pxi, 300; pxo, 50; person, 25; oxi, 22; item, 12; occasion, 2
##
## Fixed effects:
##             Estimate Std. Error t value
## (Intercept)   2.6562     0.2476   10.73
```

```
var_table <- as.data.frame(VarCorr(mixed))
var_table$var_comp <- var_table$sdcor^2
var_table$one <- 1
var_table <- ddply(var_table, "one", mutate, total = sum(var_comp), pct = var_comp/total)
var_table$percent <- paste0(round(var_table$pct * 100, 1), "%")

pander(var_table[, c("grp", "var_comp", "sdcor", "percent")])
```

grp	var_comp	sdcor	percent
pxi	0.4875	0.6982	21.4%
pxo	0.1023	0.3198	4.5%

grp	var_comp	sdcor	percent
person	0.5734	0.7572	25.1%
oxi	0.09958	0.3156	4.4%
item	0.2631	0.5129	11.5%
occasion	0.0138	0.1175	0.6%
Residual	0.7417	0.8612	32.5%

11) A novice psychometrician with no sense of the context observes from the percentages, "it looks like items are a much greater source of variance than occasions!" Explain the flaw in this reasoning.

The novice is not taking into account the fact that there are many more items than occasions. If you divide the variance components by the number of 'things' that comprise them, item level variance (.022) is only slightly higher than that of occasions (.0069). As a result, the difference between items and occasions is much closer and when taking into account the relative cost of increasing each, we would much rather add additional items rather than trying to offer the test an additional time.

12) Estimate the Mean Squares for this model using the anova command. You will first need to set the maximum matrix size to a large number, using code like set matsize 1000. Write out the equation for the estimated variance component, $\hat{\sigma}_p^2$, in terms of mean squares, MS, and confirm that this calculation corresponds to your results from mixed or xtmixed. Recall that $n_p = 25, n_i = 12$ and $n_o = 2$.

```
anovlm <- lm(value ~ person + item + occasion + pxi + pxo + oxi, data = data_long)

anova(anovlm)
```

```
## Analysis of Variance Table
##
## Response: value
##             Df Sum Sq Mean Sq F value    Pr(>F)
## person      24 400.92 16.7049 22.5668 < 2.2e-16 ***
## item        11 160.34 14.5762 19.6912 < 2.2e-16 ***
## occasion     1   6.20  6.2017  8.3779  0.004115 **
## pxi        264 453.20  1.7167  2.3191 8.453e-12 ***
## pxo         24  47.26  1.9690  2.6600 7.521e-05 ***
## oxi         11  39.62  3.6017  4.8655 7.547e-07 ***
## Residuals  264 195.42  0.7402
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

The equation for finding $\hat{\sigma}_p^2$ is

$$\frac{MS_p - MS_{pi} - MS_{po} + MS_{pio,e}}{n_i n_o}$$

plugging in the Mean Squares and ns from our ANOVA, we find that the estimated variance component is

$$\hat{\sigma}_p^2 = \frac{16.7 - 1.72 - 1.97 + .74}{12 \cdot 2} = .5729$$

This is basically the same as the answer we received from the mixed model.

13) Calculate and report the mean and standard deviation of marginal person scores, averaging over items and occasions. Following the code from class, you could obtain this using code like, summarize pmean if ptag . Explain why the term $\hat{\sigma}_p$, is less than the standard deviation of marginal person means.

```
# get marginal person scores

marg_person <- ddply(data_long, "person", summarise, mean_p = mean(value))

# mean person score
round(mean(marg_person$mean_p), 3)
```

```
## [1] 2.658
```

```
# variance of person scores
round(sd(marg_person$mean_p), 3)
```

```
## [1] 0.834
```

The estimate for σ_p is smaller than our calculated standard deviation here (.757 vs .834) because the variance across people also includes the variance of people interacted with items, people interacted with occasions, and people interacted with both (plus random error). The whole point of G-theory is to separate these components out and so we would be remiss to assume that this standard deviation of person scores is all attributable to true differences in their scores.

14) Describe the o, po, and io variance components in words, and include whether they are good, bad, or neutral with respect to relative error in a $p \times i \times o$ design. There is no need to reference the actual values, here.

The o variance component describes variance across occasions (constant across persons and items). This is ostensibly neutral as long as it affects all people equally. At the same time, we would prefer it to be smaller as it adds undesirable noise if we want to use the test score in an absolute setting. Additionally, the o variance component can cause problems if we want to use the test to compare cohorts across time. If we want to see whether successive cohorts of 5th graders are getting 'gritier', then o variation could lead us to make incorrect conclusions. In contrast, the po variance component is definitely bad, as it obfuscates both relative and absolute positions of persons across testing occasions. Finally, oi variance is fairly benign. While it's not a good thing that items change across time, if it does not affect different people differently, then it will not alter peoples' relative scores.

Part 4: The Decision Study

## 15) Write out the full equation for the relative error variance, σ_δ^2

As a rule, we know that any source of variability that intersects with the object of measurement (in this case persons) will change the measurement's relative position. In the case of a $p \times i \times o$ design, the relative error variance will include σ_{pi}^2, σ_{po}^2, and $\sigma_{pio,e}^2$ (see Figure). These variance components refer to single-unit replications, so we must divide by the relevant number of items and occasions to obtain error for average scores (over items and occasions). So the full equation for relative error variance is:

$$\sigma_\delta^2 = \frac{\sigma_{pi}^2}{n_i'} + \frac{\sigma_{po}^2}{n_o'} + \frac{\sigma_{pio,e}^2}{n_i' n_o'}$$

where $n'i$ and $n'o$ are the number of items and number of occasions of a hypothetical (') test design (what *could be* rather than what *was* in the G-study data).

From Question 10, we know that $\sigma_{pi}^2 = 0.487$, $\sigma_{po}^2 = 0.102$, and $\sigma_{pio,e}^2 = 0.741$. So we can calculate $\sigma_\delta^2 = \frac{0.487}{12} + \frac{0.102}{2} + \frac{0.741}{12 \times 2} = 0.122$ for 12 items and two occasions.

Variance Components for Relative Error
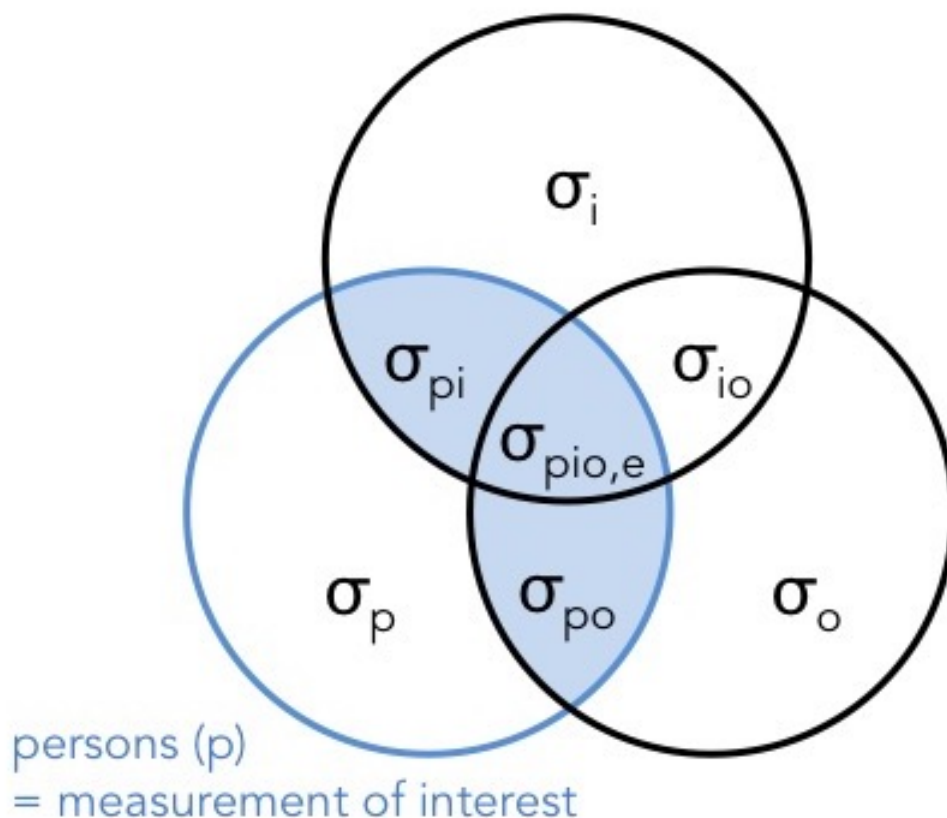
16) Calculate the generalizability coefficient for relative error, $E\hat{\rho}^2$, when there are 12 items administered on one occasion. Explain the differences between this coefficient, the coefficients from Question 5, and the coefficient from Question 6. Explain the differences between the questions that these different coefficients answer.

The generalization coefficient for relative error, $E\hat{\rho}^2 = \frac{\sigma_p^2}{\sigma_p^2 + \sigma_\delta^2}$.

And from Question 15, we know $\sigma_p^2 = 0.573$. Plugging in these numbers into the above equation we get:

$$E\hat{\rho}^2 = \frac{0.573}{0.573 + 0.122} = 0.824$$

The relative error does not include error terms σ_i^2 or σ_o^2 because variation across items or occasions, respectively, are the same for every person. Items that are more difficult will be more difficult for all persons and occasions with distractions will be more difficult for all persons. Therefore, they do not affect the relative position of one person to another. The same is true for variability for item-occasion interactions (σ_{io}^2).

17) Use the "$p \times i \times r$ D Study Template" to include a graph of a) the standard error of measurement and b) the generalizability coefficient for relative error. Relabel and rescale where appropriate.

```
## This is a function to generate the relative error coefficient given a model, a
## number of raters and a number of items. One weakness is that it presumes the
## names of your predictors and so is not suitable for general use. It does do the
## math correctly though and matches the output from Andrew's spreadsheet!

relative_error <- function(mod, raters, items) {

    sdvar <- as.data.frame(VarCorr(mod))
    sdvar$varComp <- sdvar$sdcor^2
    p <- sdvar$varComp[sdvar$grp == "person"]
    o <- sdvar$varComp[sdvar$grp == "occasion"]
    i <- sdvar$varComp[sdvar$grp == "item"]
    pxi <- sdvar$varComp[sdvar$grp == "pxi"]
    pxo <- sdvar$varComp[sdvar$grp == "pxo"]
    oxi <- sdvar$varComp[sdvar$grp == "oxi"]
    err <- sdvar$varComp[sdvar$grp == "Residual"]

    rel_err <- (pxi/items) + (pxo/raters) + (err/(items * raters))
    return(rel_err)
}

ggplot() + geom_line(aes(x = c(1:12), y = relative_error(mixed, 1, 1:12), colour = "1 Time")) +
    geom_line(aes(x = c(1:12), y = relative_error(mixed, 2, 1:12), colour = "2 Times")) +
    geom_line(aes(x = c(1:12), y = relative_error(mixed, 3, 1:12), colour = "3 Times")) +
    geom_line(aes(x = c(1:12), y = relative_error(mixed, 4, 1:12), colour = "4 Times")) +
    geom_line(aes(x = c(1:12), y = relative_error(mixed, 5, 1:12), colour = "5 Times")) +
    xlab("Number of Items") + ylab("Standard Error of Measurement") + ggtitle("Standard Error of Measure
```
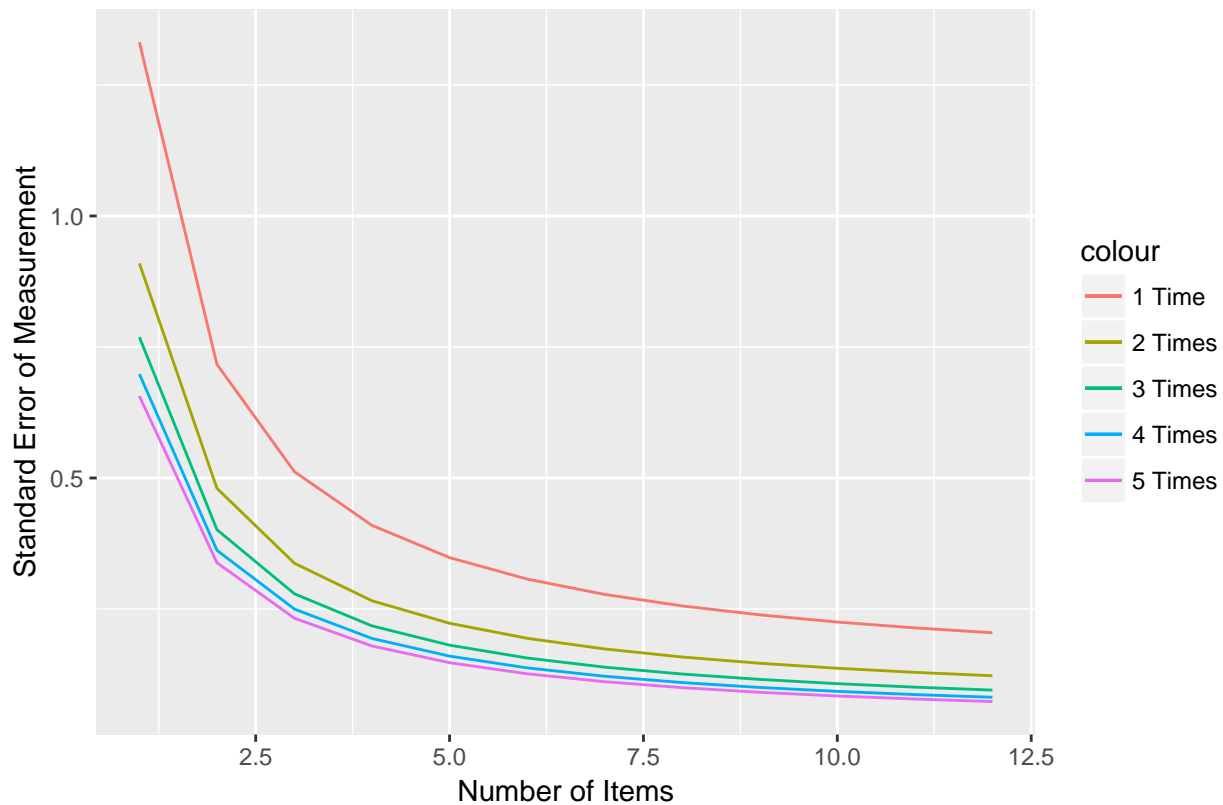
## Standard Error of Measurement Across Times and Items


```r
## This function opperates the same way as the one above, it just adds in the next
## step to generate the generalizability coefficient
rel_coeff <- function(mod, raters, items) {

    sdvar <- as.data.frame(VarCorr(mod))
    sdvar$varComp <- sdvar$sdcor^2
    p <- sdvar$varComp[sdvar$grp == "person"]
    o <- sdvar$varComp[sdvar$grp == "occasion"]
    i <- sdvar$varComp[sdvar$grp == "item"]
    pxi <- sdvar$varComp[sdvar$grp == "pxi"]
    pxo <- sdvar$varComp[sdvar$grp == "pxo"]
    oxi <- sdvar$varComp[sdvar$grp == "oxi"]
    err <- sdvar$varComp[sdvar$grp == "Residual"]

    rel_err <- (pxi/items) + (pxo/raters) + (err/(items * raters))
    gcoef <- (p/(p + rel_err))
    return(gcoef)
}


ggplot() + geom_line(aes(x = c(1:12), y = rel_coeff(mixed, 1, 1:12), colour = "1 Time")) +
    geom_line(aes(x = c(1:12), y = rel_coeff(mixed, 2, 1:12), colour = "2 Times")) +
    geom_line(aes(x = c(1:12), y = rel_coeff(mixed, 3, 1:12), colour = "3 Times")) +
    geom_line(aes(x = c(1:12), y = rel_coeff(mixed, 4, 1:12), colour = "4 Times")) +
    geom_line(aes(x = c(1:12), y = rel_coeff(mixed, 5, 1:12), colour = "5 Times")) +
    xlab("Number of Items") + ylab("Reliability Coefficient") + ggtitle("Reliability Coefficient Across
```

Reliability Coefficient Across Times and Items
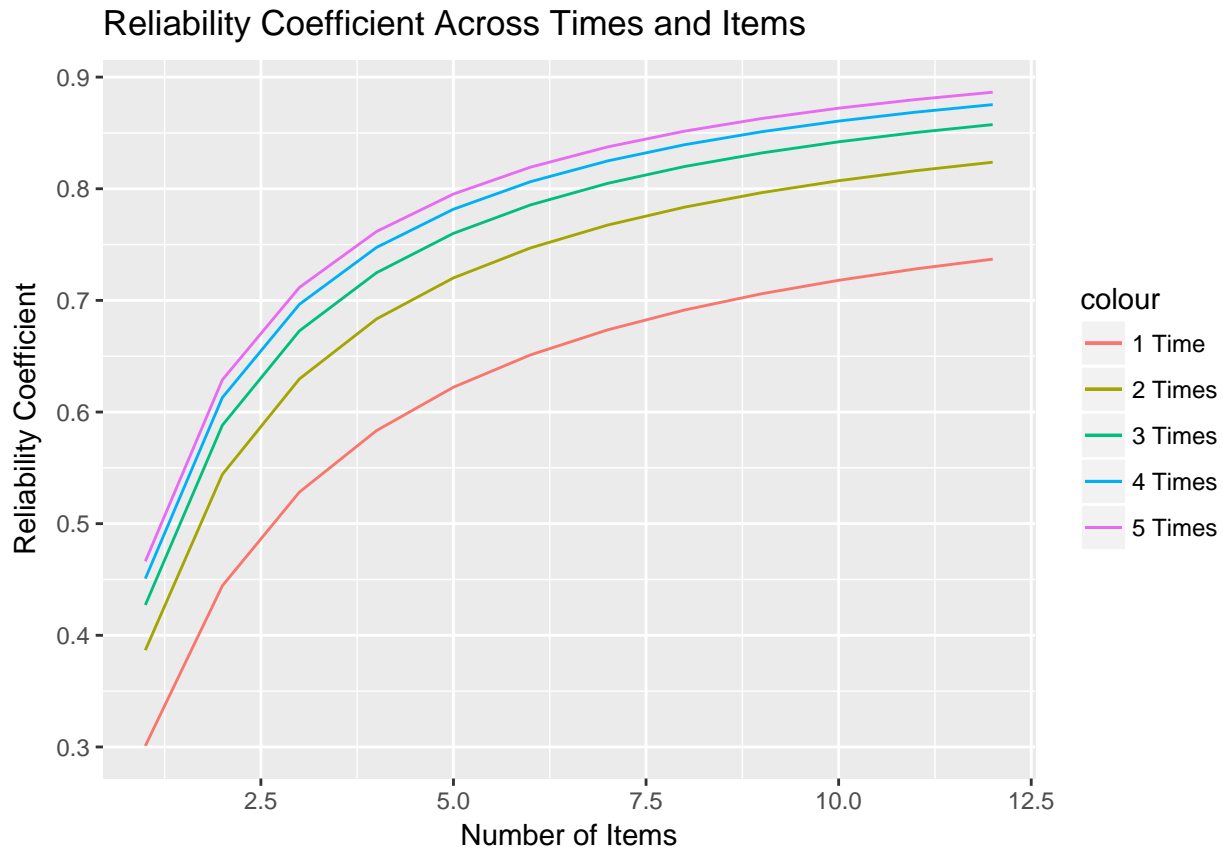
18) If the scale is administered on 1 occasion, how many items are required to achieve a reliability of 0.75? You can use the template to answer this.

```
rel_coeff(mixed, 1, 13)
```

```
## [1] 0.7444435
```

```
rel_coeff(mixed, 1, 14)
```

```
## [1] 0.7510293
```

Using the formula above, and starting with 13 items (seeing that the green line on the second graph doesn't reach .75), we found that 14 items would be needed to reach a reliability of .751.

19) Compare the benefits of doubling the number of items from 6 to 12 versus doubling the number of occasions from 1 to 2. Compare the benefits of doubling the number of items from 12 to 24 versus doubling the number of occasions from 1 to 2. How could you use this information to address the question of whether items are a greater source of error than occasions?

```
rel_coeff(mixed, 1, 6)
```

```
## [1] 0.6511777
```

```r
rel_coeff(mixed, 1, 12)
```

```
## [1] 0.7369047
```

```r
rel_coeff(mixed, 2, 6)
```

```
## [1] 0.7469992
```

In the above calculations, we examine the possibility of moving from 6 to twelve items (holding the occasions constant at 1), versus moving from 1 to 2 occasions (holding the items constant at 6). It seems clear that increasing the number of occasions yields greater benefits than increasing the number of items. At the same time, the cost of administering an additional test seems much higher than the cost of administering additional items.

```r
rel_coeff(mixed, 1, 12)
```

```
## [1] 0.7369047
```

```r
rel_coeff(mixed, 1, 24)
```

```
## [1] 0.788829
```

```r
rel_coeff(mixed, 2, 12)
```

```
## [1] 0.8237648
```

This second test, which involves a larger baseline of items provides similar results. Doubling the number of items results in a much smaller increase in reliability as compared to doubling occasions. In fact, it appears as though the marginal impact of going from 12-24 is smaller than the benefit of going from 6-12 (this makes sense given the shape of the graph from number 17). It seems clear that occasions are a much greater source of error — that is more error can be eliminated by increasing occasions — than items.

Authors

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