

W25 201-8 lab 1 lecture summary doc

For all three parts to turn in the first few steps are the same:

- 1) Title the graph and label the axes
- 2) Determine the scale for the axes
- 3) Plot the points from the tables given in the handout
- 4) Draw a best fit line that has half the points above and half below
- 5) Pick one point on the best fit line near the bottom of the graph (q_1) and one near the top of the graph (q_2)

The first two calculations (slope and y-intercept) also have the same starting place for all three:

Slope:

$$m_s = \frac{\Delta y}{\Delta x} = \frac{y_2 - y_1}{x_2 - x_1}$$

y-intercept (b in this equation):

$$y = m_s x + b$$

Where $q_1 = (x_1, y_1)$ & $q_2 = (x_2, y_2)$

This is all that is needed for R vs v , however there is another value, q , you are asked to calculate for graphs 2 and 3.

We are given the nominal equation $m = \frac{1}{2}qt^2$ and we discussed in class how if we want to be able to draw a best fit curve that is a straight line we will have to either square the time data or take the square root of the mass data.

In order to calculate q we take the equation that we plotted and assume that the parts of it match up with our equation for the best fit line:

$$\begin{aligned} m &= \frac{1}{2}qt^2 + 0 \\ y &= \frac{m}{m_s}x + b \end{aligned}$$

Below I have written the same equation but I have isolated the parts that we assume match up with each other with parentheses and the part we most care about with square brackets.

$$\begin{pmatrix} m \\ y \end{pmatrix} = \left[\frac{1}{2}q \right] \begin{pmatrix} t^2 \\ x \end{pmatrix} + \begin{pmatrix} 0 \\ b \end{pmatrix}$$

For #2 we looked at m vs t^2 . In the given equation t^2 already appears the way that we graphed it (i.e. raised to the 2nd power) and so we don't need to make any modifications to the equation before we set $m_s = \frac{1}{2}q$ and find our q value by solving for q and plugging in our value for m_s .

This is not the case for #3. We need a \sqrt{m} term to be in the equation. We still start with $m = \frac{1}{2}qt^2$ and modify it until the term we need is present.

Things to remember when doing the math for this lab and on the upcoming quiz:

- All the values that we plot on our graphs or read off our graphs have units attached to them.
 - This means that the ordered pairs for our points q_1 & q_2 will have units.
 - The 1st value has the same units as the horizontal axis
 - the 2nd value has the same units as the vertical axis
 - It helps to always write them as we do our math so that we remember any operations that we perform on them along the way to getting our answers.
 - This also helps me give you as much partial credit as I can justify giving.
- Whatever you do to one side of an equation you do to the other also
 - This applies to constants(numbers), variables and units
- When distributing exponents to fractions they affect both the top and the bottom in the same way
 - This applies to units too:

$$\left(\frac{\text{miles}}{\text{hour}^3}\right)^2 \equiv \frac{\text{miles}^{1 \cdot 2}}{\text{hours}^{3 \cdot 2}} \equiv \frac{\text{miles}^2}{\text{hours}^6}$$

- Square roots are canceled by squaring them and vice versa both for numbers and units:

$$(\sqrt{x})^2 = \sqrt{x^2} = x$$