

# ASM 2

## Motivation

- ▶ Develop the full hierarchy of expressions for arithmetic and relational operators

# Arithmetic

- ▶ What happens if we want to do arithmetic?

- ▶ Ex:

$$x = y + 4$$

- ▶ Seems easy:

```
mov rax, [y]
add rax, 4
mov [x], rax
```

## Arithmetic

- ▶ What if the expression is a bit more complex?

$$x = (y+4) * (z-2)$$

- ▶ We can do this using a second register to hold a temporary value:

```
mov rax,[y]
add rax,4
mov rbx,[z]
sub rbx,2
imul rax,rbx
mov [x],rax
```

# Problem

- ▶ What happens when we run out of registers?
  - ▶ There are only 16
- ▶ Solution: The *stack*

## Stack

- ▶ When program starts up, OS allocates some RAM as a stack
- ▶ `rsp` register points to topmost item on the stack
- ▶ We can store temporaries to the stack with `push`:  
`push rax`
- ▶ And we can remove them with `pop`:  
`pop rax`
- ▶ **Important:** Change `return-stmt`, `loop`, and `cond` to get their values from the stack, not from `rax`!
  - ▶ It's as easy as just adding a "`pop rax`" in the right places

# Stack

- ▶ We can discard items from the stack:  
`add rsp,8`
  - ▶ This works because stack grows down in memory
  - ▶ Each item is 64 bits (=8 bytes)
- ▶ We can read items from the stack without popping:
  - ▶ `mov rax, [rsp]` ;get topmost item
  - ▶ `mov rax, [rsp+8]` ;get next item down
  - ▶ `mov rax, [rsp+16]` ;get third-from-top

# Code

- ▶ We need to define some semantics
- ▶ Change the `expr` production and add additional nonterminals for various mathematical and relational operations:

`expr`  $\rightarrow$  `orexp`

`orexp`  $\rightarrow$  ~~`orexp OR andexp`~~ | `andexp`

`andexp`  $\rightarrow$  ~~`andexp AND notexp`~~ | `notexp`

`notexp`  $\rightarrow$  ~~`NOT notexp`~~ | `rel`

`rel`  $\rightarrow$  ~~`sum RELOP sum`~~ | `sum`

`sum`  $\rightarrow$  `sum ADDOP term` | `sum MINUS term` | `term`

`term`  $\rightarrow$  `term MULOP neg` | `neg`

`neg`  $\rightarrow$  ~~`MINUS neg`~~ | `factor`

`factor`  $\rightarrow$  `ID` | `NUM` | `LP expr RP` | ~~`func call`~~ | ~~`ID LB expr list RB`~~

~~`STRING CONSTANT`~~

- ▶ For now, we'll ignore the parts of the grammar that are struck out



# Attributes

- ▶ Recall: Synthesized attributes and inherited attributes
- ▶ sum, term, factor produce synthesized attributes
  - ▶ Value: The value of the arithmetic operation
    - ▶ This will always be on top of the stack
  - ▶ Type: What's the type of the result
    - ▶ For now, this is always a number, but later we'll add additional types
- ▶ We'll define an enumeration:  
`enum VarType{ NUMBER };`

# Code

- ▶ Suppose we write some functions to process the various tree nodes
- ▶ Some of them are just stubs for now...

```
void exprNodeCode(TreeNode n, out VarType type){  
    return orexpNodeCode(n, out type);  
}  
void orexpNodeCode(TreeNode n, out VarType type){  
    return andexpNodeCode(n, out type);  
}  
void notexpNodeCode(TreeNode n, out VarType type){  
    return relNodeCode(n, out type);  
}  
void relNodeCode(TreeNode n, out VarType type){  
    return sumNodeCode(n, out type);  
}  
void negNodeCode(TreeNode n, out VarType type){  
    return factorNodeCode(n, out type);  
}
```

# Factor

- ▶ We're ready to write the code for factor
- ▶ Only two possibilities in our cut-down grammar

```
static void factorNodeCode(TreeNode n, out VarType type){  
    //factor -> NUM | LP expr RP  
    var child = n.Children[0];  
    switch( child.Symbol ){  
        case "NUM":  
            double d = Convert.ToDouble(child.Lexeme);  
            string ds = d.ToString("f");  
            if(ds.IndexOf(".") == -1 )  
                ds += ".0";  
            emit("mov rax, __float64__({0})", ds);  
            emit("push rax");  
            type = VarType.NUMBER;  
            break;  
        case "LP":  
            exprNodeCode( n.Children[1], out type );  
            break;  
        default:  
            throw new Exception("?");  
    }  
}
```

# Mathematics

- ▶ Next, we'll look at the code for sum
- ▶ We now need to decide: Will we do integer math or floating point math?
  - ▶ Floating point is often very useful for users
  - ▶ So we'll use floating point operations here
  - ▶ This also allows us to show how FP numbers are processed

# Floating Point

- ▶ FP operations use different registers from integer operations
- ▶ Sixteen registers: xmm0, xmm1, ... , xmm15

**Load** movsd xmm0, [x]

**Store** movsd [x], xmm0

**Add** addsd xmm0, xmm1 ;  $xmm0 \leftarrow xmm0 + xmm1$

**Subtract** subsd xmm0, xmm1 ;  $xmm0 \leftarrow xmm0 - xmm1$

**Multiply** mulsd xmm0, xmm1 ;  $xmm0 \leftarrow xmm0 * xmm1$

**Divide** divsd xmm0, xmm1 ;  $xmm0 \leftarrow xmm0 \div xmm1$

**Int→FP** cvtsi2sd xmm0, rax ; Converts integer value to double

**FP→Int** cvtsd2si rax, xmm0 ; Truncates double to integer

**XMM→GPR** movq rax, xmm0 ; rax gets bit pattern for double

**GPR→XMM** movq xmm0, rax ; bit pattern moved unchanged to xmm0

**XMM→Mem** movsd [x], xmm0

**Mem→XMM** movsd xmm0, [x]

# Stack

- ▶ We can't use PUSH or POP with xmm's directly
- ▶ We need to do one of these for push:
  - ▶ `movq rax, xmm0`  
`push rax`
  - ▶ `sub rsp,8`  
`movsd [rsp], xmm0`
- ▶ We do one of these for pop:
  - ▶ `pop rax`  
`movq xmm0, rax`
  - ▶ `movsd xmm0, [rsp]`  
`add rsp,8`

## Note

- ▶ Pay careful attention to the difference between `cvtsi2sd` and `movq`!
  - ▶ `cvtsi2sd` *converts an integer to a double precision number*
  - ▶ `movq` moves the bit pattern unchanged

## Sum

```
void sumNodeCode(TreeNode n, out VarType type){  
    //sum -> sum ADDOP term | sum MINUS term | term  
    switch( n.Children[0].Symbol ){  
        case "term":  
            termNodeCode(n.Children[0], out type);  
            return;  
        case "sum":  
            ...more code...  
        default:  
            error  
    }  
}
```



## Sum

- ▶ If we're processing sum  $\rightarrow$  sum ADDOP term or sum  $\rightarrow$  sum MINUS term we must first evaluate the two child nodes to get their values

```
VarType t0,t1;  
sumNodeCode( n.Children[0], out t0 );  
termNodeCode( n.Children[2], out t1 );
```

## Sum

- ▶ Next, we verify the types

```
if( t0 != VarType.NUMBER || t1 != VarType.NUMBER )  
    error!
```

## Sum

- ▶ We can now move the two operands from the stack to xmm registers so we can perform FP math

```
emit("pop rax");    //second operand
emit("movq xmm1, rax");
emit("pop rax");    //first operand
emit("movq xmm0, rax");
```

## Sum

- ▶ We then decide whether to do addition or subtraction

```
switch( n.Children[1].Lexeme ){  
    case "+":  
        emit("addsd xmm0,xmm1");  
        break;  
    case "-":  
        emit("subsd xmm0,xmm1");  
        break;  
    default:  
        ICE  
}
```

## Sum

- ▶ We defined the math operations to leave their results on the stack, so we must now move the value from xmm0 to the stack

```
emit("movq rax, xmm0");  
emit("push rax");
```

- ▶ We can then return our synthesized attribute

```
type = VarType.NUMBER;  
return;
```

## Question

- ▶ What if the parse tree was generated with an LL parser?
- ▶ In that case, the grammar rules are probably more like this:  
 $\text{sum} \rightarrow \text{term sum'}$   
 $\text{sum'} \rightarrow \text{ADDOP term sum'} \mid \text{MINUS term sum'} \mid \lambda$
- ▶ The logic for sum would be tweaked a bit

## Sum

```
void sumNodeCode(TreeNode n, out VarType type){  
    //sum -> term sum'  
    VarType type1;  
    termNodeCode(n.Children[0], out type1);  
    sumprimeNodeCode( n.Children[1], type1, out type);  
}
```

# Sum'

```
void sumprimeNodeCode( TreeNode n, VarType type1, out VarType type){
    //sum' -> ADDOP term sum' | MINUS term sum' | lambda
    if( n.Children.Count == 0 ){
        type = type1;
        return;
    }
    VarType type2;
    termNodeCode( n.Children[1], out type2);
    if( type1 != type2 )
        error
    emit("pop rax");    //second operand
    emit("movq xmm1, rax");
    emit("pop rax");    //first operand
    emit("movq xmm0, rax");
    switch( n.Children[0].Lexeme ){
        case "+":
            emit("addsd xmm0,xmm1");
            break;
        case "-":
            emit("subsd xmm0,xmm1");
            break;
        default:
            ICE
    }
    emit("movq rax, xmm0");
    emit("push rax");
    type = VarType.NUMBER;
}
```



## Term

- ▶ The logic for term is similar, so it's left as an exercise for you

## Comparisons

- ▶ What about logical operators?  
rel  $\rightarrow$  sum RELOP sum | sum
  - ▶ RELOP is one of  $>$ ,  $<$ ,  $>=$ ,  $<=$ ,  $!=$ ,  $==$
- ▶ Notice sum is on both sides of the operator so things like “ $x > y > z$ ” are not valid
- ▶ We need to define semantics of relational operators
  - ▶ We'll do like C: True is nonzero value; false is zero

## rel

- ▶ We can begin with an outline that's very similar to the code that we've seen before for sum
- ▶ Evaluate the two operands and move them to registers

```
void relNodeCode(TreeNode n, out VarType type){
    //rel -> sum RELOP sum | sum
    if( n.Children.Count == 1 )
        return sumNodeCode(n.Children[0]);
    VarType t0,t1;
    sumNodeCode( n.Children[0], out t0 );
    sumNodeCode( n.Children[2], out t1 );
    ...check types of t0 and t1...
    emit("pop rax");
    emit("movq xmm1, rax"); //right hand operand
    emit("pop rax");
    emit("movq xmm0, rax"); //left hand operand
    ...more code...
}
```

## rel

- ▶ Floating point compare is implemented via the `cmpXXsd` mnemonics
- ▶ Takes two registers to compare
- ▶ First operand gets either `0x0` or `0xffffffffffffffff` for true or false
- ▶ Instructions:
  - ▶ `cmpeqsd (=)`
  - ▶ `cmpltsd (<)`
  - ▶ `cmpleqd (<=)`
  - ▶ `cmpneqsd ( $\neq$ )`
  - ▶ `cmpnltsd ( $\geq$  i.e., “not less than”)`
  - ▶ `cmpnleqd ( $>$  i.e., “not less than or equal to”)`

## rel

- We can use a switch statement:

```
string mnemonic;  
switch(n.Children[1].Lexeme){  
    case "==": mnemonic = "cmpeqsd"; break;  
    case "<": mnemonic = "cmpltsd"; break;  
    case "<=": mnemonic = "cmpllesd"; break;  
    case "!=": mnemonic = "cmpneqsd"; break;  
    case ">=": mnemonic = "cmpnltsd"; break;  
    case ">": mnemonic = "cmpnlesd"; break;  
    default:      throw new Exception("?");  
}  
emit("{0} xmm0,xmm1",mnemonic);
```

## Problem

- ▶ 0xffffffffffffffff doesn't correspond to a valid floating point number
- ▶ Doubles are stored as:
  - ▶ 1 sign bit
  - ▶ 11 exponent bits
  - ▶ 52 mantissa bits
- ▶ If all exponent bits are 1's: The number represents either a NaN or infinity, depending on pattern in mantissa
- ▶ The value 1.0 is represented by sign=0, exponent = 01111111111, mantissa = 0
- ▶ So we'll do a bitwise AND to convert the NaN to 1.0

rel

```
emit("movq rax, xmm0");  
emit("mov rbx, __float64__(1.0)");  
emit("and rax,rbx");  
emit("push rax");  
type = VarType.NUMBER;
```

## Boolean

- ▶ The only part left is the boolean operations (and, or, not)  
orexp  $\rightarrow$  orexp OR andexp | andexp  
andexp  $\rightarrow$  andexp AND notexp | notexp  
notexp  $\rightarrow$  NOT notexp | rel



## Evaluation

- ▶ Most modern languages implement *short circuit evaluation*
- ▶ Idea: As soon as result of boolean expression is known, stop evaluating
- ▶ If short circuit evaluation was not implemented, we couldn't write things like:  
`if( x != 0 and y/x > 10 ){ ... }`
  - ▶ We'd get divide by zero even though we're trying to prevent that

## orexp

- ▶ We'll examine orexp; andexp and notexp are similar
- ▶ First, we deal with the easy case...

```
void orexpNodeCode(TreeNode n, out VarType type){  
    //orexp -> orexp OR andexp | andexp  
    if( n.Children.Count == 1 )  
        andexpNodeCode(n.Children[0], out type);  
    ...more code...  
}
```

## orexp

- ▶ We then evaluate the left side of the OR

```
VarType t0;  
orexpNodeCode(n.Children[0], out t0);  
...verify t0 is correct type...  
emit("pop rax");  
emit("cmp rax,0");
```

- ▶ We're ready to do the comparison

## orexpr

- ▶ If rax holds a nonzero value:
  - ▶ We don't want to evaluate child 2; we want value of entire orexp to be nonzero
- ▶ If rax holds zero value, we must evaluate child 2 in case it ends up being true
  - ▶ The result of the entire orexp is whatever child 2 produces
- ▶ This is going to involve some jump operations

## orexp

- ▶ Create a label and pop result from evaluating first child

```
string lbl = label();  
emit("pop rax");
```

## orexp

- ▶ If first child gave nonzero, skip over the second child's code
- ▶ Otherwise, fall through and execute code for second child, leaving result in rax

```
emit("cmp rax,0");  
emit("jne "+lbl);  
VarType t1;  
andexpNodeCode(n.Children[2], out t1);  
...verify t1 is correct type...  
emit("pop rax");  
emit(lbl+":");
```

## orexp

- ▶ Final step: Make sure the stack gets the result of the entire expression and return our attributes

```
emit("push rax");  
type = VarType.NUMBER ;
```

## Notice

- ▶ This is not very efficient: We could have a pop immediately followed by a push of that exact same thing
- ▶ Here's the assembly code written in one place:

```
...code for first child...  
pop rax  
cmp rax,0  
jne lbl12345  
...code for second child...  
pop rax  
lbl12345:  
push rax
```
- ▶ Push-Then-Pop going to be a no-op for us
- ▶ So we can tweak the code to eliminate that pop-then-push...



# Code

```
void orexpNodeCode(TreeNode n, VarType type){
    //orexp -> orexp OR andexp | andexp
    if( n.Children.Count == 1 )
        andexpNodeCode(n.Children[0], out type);
    VarType t0;
    orexpNodeCode(n.Children[0], out t0);
    ...verify t0 is OK...
    string lbl = label();
    emit("mov rax, [rsp]");
    emit("cmp rax, 0");
    emit("jne {0}",lbl);
    emit("add rsp,8");
    VarType t1;
    andexpNodeCode(n.Children[2], out t1);
    ...verify t1 is OK...
    emit("{0}:", lbl);
    type = VarType.NUMBER;
}
```

## Explanation

- ▶ Suppose the evaluation of child 0 leaves value  $v$  on the stack
- ▶ We copy  $v$  to `rax` and compare to zero
- ▶ Suppose  $v$  is zero
  - ▶ We do not take the branch
  - ▶ We pop the stack (by adding 8 to `rsp`) and fall through to the `andexp` node's code
  - ▶ That will leave its result on top of the stack, so this becomes the result of the entire `orexpr`
- ▶ What if  $v$  is nonzero?
  - ▶ We take the branch. The result of child 0 is still on top of the stack
  - ▶ We are at the end of the `orexpr` code, so we're done.

## Optimizing

- ▶ This last example shows the concept of *optimizing* code
- ▶ We'll discuss optimization in more detail later, but essentially amounts to trying to choose fastest code sequence
- ▶ In general, register operations are fastest
- ▶ Accessing RAM is much slower (ex: variable access; push/pop)
- ▶ We'd prefer to keep as many operations as possible in registers

## Alteration

- ▶ The code as we've described it is not very good: It uses memory (the stack) heavily
- ▶ We could modify our code to *spill* values to the stack only when necessary
- ▶ Ex: Maybe we devote registers r8-r15 to temporaries
- ▶ We keep track of which registers are in use and which are free
- ▶ When we need a temporary, we use one of the registers if one is available
- ▶ Otherwise, use the stack
- ▶ We'd need our Attributes structure to also tell where we put the value

## Analysis

- ▶ This can make generated code much more efficient
- ▶ But: It's also more complex!

## Assignment

- ▶ Complete the code for the rest of the arithmetic hierarchy (except for factor: Leave it as just NUM and LP expr RP)
- ▶ If you want to be impressive, use registers instead of the stack for temporaries
- ▶ Use the test harness: [Main.cs](#), [ExeTools.cs](#), [GrammarData.cs](#), and [inputs.txt](#)
- ▶ As before, you can't assume the existence of grammar.txt, but you can embed the full grammar in your executable as a C# string

## Sources

- ▶ Intel Corp. Intel Reference Manual.

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