

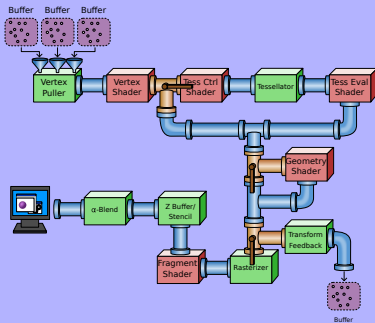
Tessellation Shaders

Motivation

- ▶ We've seen tessellation shaders for lines
- ▶ Now we'll discuss using them with triangles

Review

► Recall GPU pipeline



TCS & TES

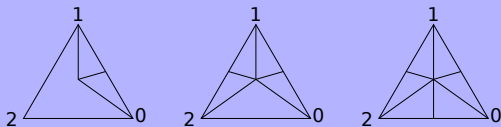
- ▶ Recall: TCS and TES work together to direct tessellator actions
- ▶ TCS says how much subdivision to do
- ▶ TES says what kind of subdivision to do
- ▶ For this discussion, we'll assume triangular tessellation

TCS

- ▶ TCS must write to `gl_TessLevelOuter[0...2]`
 - ▶ Tells how much to subdivide each edge of the triangle
- ▶ Also must write to `gl_TessLevelInner[0]`
 - ▶ Tells how much to subdivide interior of triangle
- ▶ If zero written to any of these: Entire patch is discarded

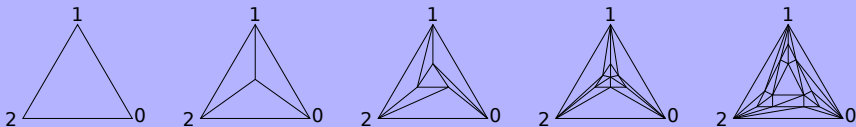
Examples

- ▶ `gl_TessLevelInner` is 1 in all of these
- ▶ `gl_TessLevelOuter` is $\{2,1,1\}$, $\{2,2,1\}$, $\{2,2,2\}$ here



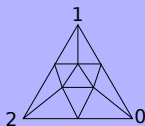
Examples

- ▶ `glTessLevelOuter` is $\{1,1,1\}$ for all of these
- ▶ `gl_TessLevelInner` is 1, 2, 3, 4, and 5



Example

- ▶ Outer is $\{2,2,2\}$ and inner is 3



TES

- ▶ TES should begin with line:
`layout(triangles)in;`

Code

- ▶ First, we'll develop program that just draws input mesh
- ▶ C++ code:

```
void draw(){  
    cam->setUniforms();  
    glClear(GL_COLOR_BUFFER_BIT | GL_DEPTH_BUFFER_BIT );  
    Program::setUniform("worldMatrix", mat4::identity() );  
    meshprog->use();  
    glPatchParameteri(GL_PATCH_VERTICES,3);  
    M->draw(GL_PATCHES);  
    fpsText->draw();  
}
```

VS

► Vertex shader: Just a passthrough:

```
layout(location=0) in vec3 position;  
layout(location=1) in vec2 texCoord;  
layout(location=2) in vec3 normal;
```

```
out vec2 v_texCoord;  
out vec3 v_normal;  
out vec3 v_position;
```

```
void main(){  
    v_texCoord = texCoord;  
    v_normal = normal;  
    v_position = position;  
}
```

TCS

- ▶ TCS: Notice vertices=3
- ▶ Since patch size is 3, system will pull 3 vertices off input, run TCS 3 times, then feed result to tessellator

```
layout(vertices=3) out;
```

```
in vec3 v_position[];  
in vec2 v_texCoord[];  
in vec3 v_normal[];
```

```
out vec3 tcs_position[];  
out vec3 tcs_normal[];  
out vec2 tcs_texCoord[];
```

```
void main(){  
    gl_TessLevelOuter[0] = 1;  
    gl_TessLevelOuter[1] = 1;  
    gl_TessLevelOuter[2] = 1;  
    gl_TessLevelInner[0] = 1;  
    tcs_position[gl_InvocationID] = v_position[gl_InvocationID];  
    tcs_normal[gl_InvocationID] = v_normal[gl_InvocationID];  
    tcs_texCoord[gl_InvocationID] = v_texCoord[gl_InvocationID];  
}
```

TES

- For TES, we'll need to define some helper functions:

```
vec3 interpolate(float u, float v, float w, vec3 a, vec3 b, vec3
c ){
    //simple barycentric interpolation
    vec3 p0 = u * a;
    vec3 p1 = v * b;
    vec3 p2 = w * c;
    return (p0+p1+p2);
}
vec2 interpolate(float u, float v, float w, vec2 a, vec2 b, vec2
c ){
    vec2 p0 = u * a;
    vec2 p1 = v * b;
    vec2 p2 = w * c;
    return (p0+p1+p2);
}
```

TES

- ▶ Now for the declarations.
- ▶ Notice we have this declared as taking triangles (first line):

```
layout(triangles) in;
```

```
in vec3 tcs_position[];
```

```
in vec3 tcs_normal[];
```

```
in vec2 tcs_texCoord[];
```

```
out vec3 tes_worldPos;
```

```
out vec2 tes_texCoord;
```

```
out vec3 tes_normal;
```

```
void main(){
```

```
    ...
```

```
}
```

TES

- Determine position of points:

```
vec3 p1 = interpolate(  
    gl_TessCoord[0], gl_TessCoord[1], gl_TessCoord[2],  
    tcs_position[0], tcs_position[1], tcs_position[2] );  
vec3 n1 = interpolate(  
    gl_TessCoord[0], gl_TessCoord[1], gl_TessCoord[2],  
    tcs_normal[0], tcs_normal[1], tcs_normal[2] );  
tes_texCoord = interpolate(  
    gl_TessCoord[0], gl_TessCoord[1], gl_TessCoord[2],  
    tcs_texCoord[0], tcs_texCoord[1], tcs_texCoord[2] );
```

TES

- ▶ Rest of the code would look very familiar in a vertex shader:

```
vec4 p = vec4(p1,1.0);  
p = p * worldMatrix;  
tes_worldPos = p.xyz;  
p = p * viewMatrix;  
p = p * projMatrix;  
gl_Position = p;
```

```
vec4 n = vec4(n1,0.0);  
n = n * worldMatrix;  
tes_normal = n.xyz;
```


TES

- ▶ `gl_TessCoord[0...2]` will have the u,v,w barycentric coordinates
- ▶ We need to interpolate all three items (position, normal, texture coordinates)
- ▶ Also output data for FS

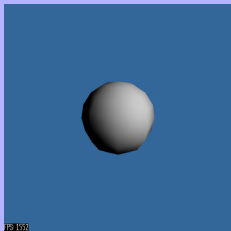
FS

► Standard FS:

```
in vec2 tes_texCoord;  
in vec3 tes_normal;  
in vec3 tes_worldPos;  
  
out vec4 color;  
layout(binding=0) uniform sampler2DArray tex;  
  
void main(){  
    vec4 c = texture( tex, vec3(tes_texCoord,0.0) );  
    vec3 L = normalize(lightPosition - tes_worldPos);  
    vec3 N = normalize(tes_normal);  
    float dp = max( dot(L,N), 0.0 );  
    color.rgb = dp * diffuse * c.rgb;  
    color.a = c.a;  
}
```

Result

- ▶ We're using a fairly coarse mesh here with smoothed normals:



Applications

- ▶ What can we do with triangle tessellation?
- ▶ One use: Adaptive surface refinement
- ▶ First method we'll look at: Implicit Surfaces

Implicit Surfaces

- ▶ Implicit surface: Surface is described by mathematical equation
- ▶ Example: Sphere of radius 1
- ▶ We begin by rendering an octahedron
- ▶ TCS sets subdivision level
- ▶ TES pushes each resulting vertex to correct distance from origin and computes radius

VS

- ▶ Nothing special here: Just pass data through
- ▶ We've already seen this, so no need to show it again.

TCS

- ▶ TCS copies data and defines tessellation level
- ▶ `main()` is the only change from what we had previously:

```
void main(){  
    //tessFactor is a uniform  
    gl_TessLevelOuter[0] = tessFactor;  
    gl_TessLevelOuter[1] = tessFactor;  
    gl_TessLevelOuter[2] = tessFactor;  
    gl_TessLevelInner[0] = tessFactor;  
    tcs_position[gl_InvocationID] = v_position[gl_InvocationID];  
    tcs_normal[gl_InvocationID] = v_normal[gl_InvocationID];  
    tcs_texCoord[gl_InvocationID] = v_texCoord[gl_InvocationID];  
}
```

TES

- ▶ TES is where the main work happens

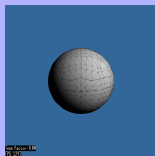
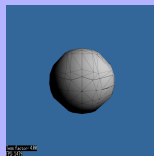
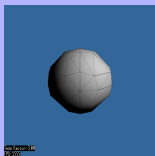
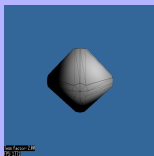
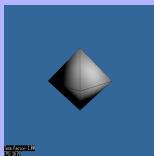
```
void main(){
    vec3 p1 = interpolate(gl_TessCoord[0], gl_TessCoord[1],
        gl_TessCoord[2],
        tcs_position[0], tcs_position[1], tcs_position[2] );
    p1 = normalize(p1);
    vec3 n1 = p1;
    tes_texCoord = interpolate(gl_TessCoord[0], gl_TessCoord[1],
        gl_TessCoord[2],
        tcs_texCoord[0], tcs_texCoord[1], tcs_texCoord[2] );
    ...multiply p1 with worldMatrix, viewMatrix, projMatrix...
    ...write p1 to gl_Position...
    ...multiply n with worldMatrix, write to tes_normal
}
```


FS

- ▶ FS is as usual

Results

- Tessellation levels of 1, 2, 3, 4, 8



Problem

- ▶ Usually, we'd use a lower level of tessellation for model when it's far away and switch to more detailed level as it gets closer
- ▶ Problem: Can cause “popping” effect when levels change
 - ▶ Very distracting visually
- ▶ We can solve this with fractional tessellation values
 - ▶ Make sure first line of TES is:
layout(triangles,fractional_odd_spacing) in;
- ▶ Now, fractional values give intermediate positions
- ▶ Allows smooth transition
- ▶ fractional.orgv

Phong Tessellation

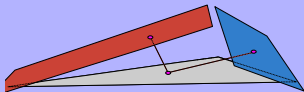
- ▶ Implicit surfaces work well if object can be described via simple mathematical formula
 - ▶ Ex: Sphere, rounded cube, cone, cylinder, ...
- ▶ But what if we have a more complex object? (Such as a mesh)
- ▶ Another method of refinement: Phong tessellation

Phong Tessellation

- ▶ Given: Three vertices of triangle, v_0, v_1, v_2 with normals n_0, n_1, n_2
- ▶ Recall: We can define a plane using a point and a normal
 - ▶ Plane equation: $Ax+By+Cz+D=0$
 - ▶ At vertex i : $A, B, C = n_i$ and $D = -(n_i \cdot v_i)$
- ▶ So we can define three planes, one at each vertex of the triangle
- ▶ We project original surface point to each plane then interpolate its position

Idea

- ▶ Each vertex has a smooth normal
- ▶ That normal + the vertex location define a plane
- ▶ Project surface point to that plane (do three times: Once for each vertex)
- ▶ Here, only two planes are shown.



Projection

- ▶ How to project a point p to an arbitrary plane (A,B,C,D) ?
- ▶ We know distance of p from plane is given by
$$\delta = Ap_x + Bp_y + Cp_z + D$$
 - ▶ This is a standard property of plane equation, assuming A,B,C is unit vector
- ▶ So if we compute $p - \delta n$ units (where n = plane normal), we have projected p to the plane
- ▶ Why subtraction? If we are 4 units in front of plane, we need to move 4 units in negative normal direction

Projection

- We can wrap this in a GLSL function:

```
vec3 project( vec3 v, vec3 n, vec3 p ){  
    //project p to plane defined by point v and normal n  
    vec4 planeEquation = vec4(n, -dot(v,n) );  
    float pdistance = dot( vec4(p,1),planeEquation );  
    return p - pdistance * n;  
}
```


Procedure

- ▶ Once we've computed three projected points, take barycentric average of their positions
- ▶ This gives final surface location
- ▶ Note: Original developers of PT technique recommended taking $\frac{3}{4}/\frac{1}{4}$ mix of new point and old point
- ▶ Normal is just the usual interpolated normal (also using barycentric interpolation)

TES

- ▶ TES is where the main Phong tessellation work happens

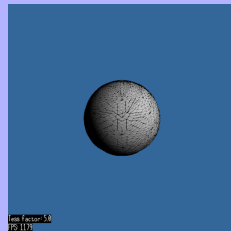
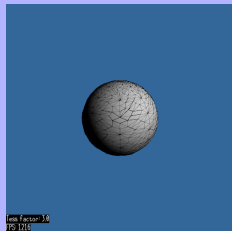
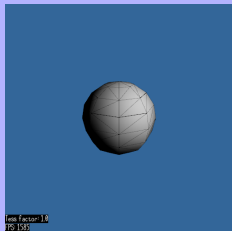
```
vec3 p1 = interpolate(  
    gl_TessCoord[0], gl_TessCoord[1], gl_TessCoord[2],  
    tcs_position[0], tcs_position[1], tcs_position[2] );
```

```
vec3 pr1 = project( tcs_position[0], tcs_normal[0], p1 );  
vec3 pr2 = project( tcs_position[1], tcs_normal[1], p1 );  
vec3 pr3 = project( tcs_position[2], tcs_normal[2], p1 );  
vec3 p1a = interpolate(  
    gl_TessCoord[0], gl_TessCoord[1], gl_TessCoord[2],  
    pr1,pr2,pr3 );
```

```
float alpha=0.75;  
p1 = (1.0-alpha)*p1 + alpha * p1a;  
...interpolate normal and texcoord as before...  
...multiply by world/view/proj matrices...
```

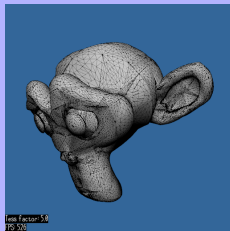
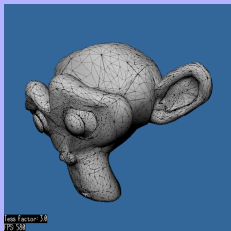
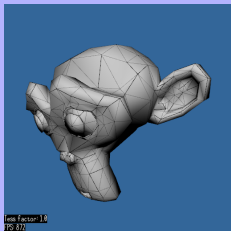
Results

- Sphere with tessFactor=1, 3, 5



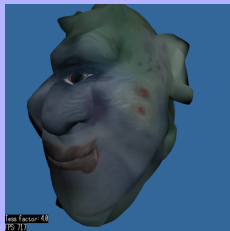
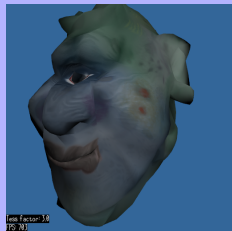
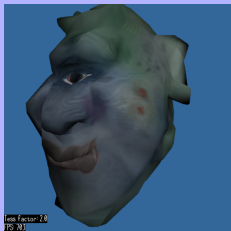
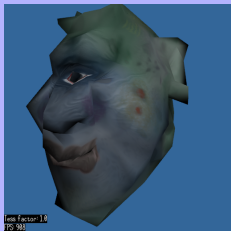
Results

- Using the Suzanne model from Blender, tessFactor=1, 3, 5



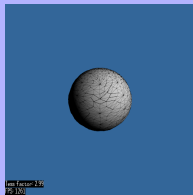
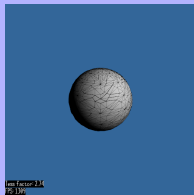
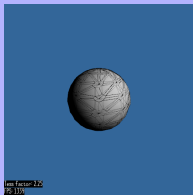
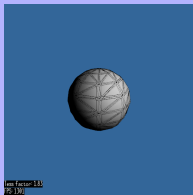
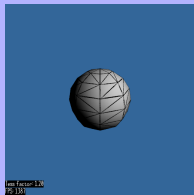
Results

- ▶ Using a decimated version of Keenan Crane's Jerry model:
tessFactor=1, 2, 3, 4



Fractional Spacing

- ▶ We can use fractional spacing here to reduce popping
- ▶ Example of fractional tessellations: 1.2, 1.8, 2.25, 2.75, 3.0



Note

- ▶ We could apply more subdivision to silhouette edges vs faces viewed head-on
- ▶ This can improve appearance of model without imposing too much rendering cost

Sources

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- ▶ <http://onrendering.blogspot.com/2011/12/tessellation-on-gpu-curved-pn-triangles.html>
- ▶ <http://www.ludicon.com/castano/blog/2009/01/10-fun-things-to-do-with-tessellation/>
- ▶ Brandon Wang. Smooth GPU Tessellation. https://people.eecs.berkeley.edu/~sequin/CS284/PROJ_12/Brandon/Smooth%20GPU%20Tessellation.pdf
- ▶ Tomas Akenine-Möller, Eric Haines, Naty Hoffman, Angelo Pesce, Michał Iwanicki, Sébastien Hillaire. Real-Time Rendering (Fourth Edition). CRC Press.

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