Diffusion Generative Flow Samplers: Improving Learning Signals Through Partial Trajectory Optimization

Dinghuai Zhang*, Ricky T. Q. Chen, Cheng-Hao Liu, Aaron Courville & Yoshua Bengio

Thomas Mousseau

October 23, 2025

Overview

Introduction

1. Introduction

- 1.1 Problem Statement
- 1.2 Stochastic Optimal Control

2. Stochastic Optimal Control to GFlowNets

- 2.1 Target Process
- 2.2 GFlowNet

3. Diffusion Generative Flow Sampler Results

- 3.1 Gradients variance, Z estimation and mode coverage
- 3.2 Convergence Guarantees

4. Conclusion

- 4.1 Summary
- 4.2 Q&A

Diffusion Generative Flow Sampler Results

Introduction

0000

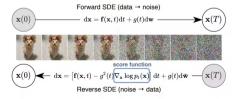
Generative Modeling

Task

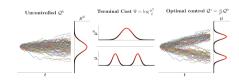
Sample from a complex (high-dimensional and multimodal) distribution D.

D can be given under the form of:

• A dataset of samples $\{x_i\}_{i=1}^N \sim D$ (e.g., images, text. audio)



An unnormalized density $\mu(x)$ where D has density $\pi(x) \propto \mu(x)$ (e.g., energy-based models, physics/chemistry)



Sampling from Unnormalized Densities

Context. Sample from a *D*-dimensional target with unnormalized density $\mu(x)$ where $\mathbb{R}^D \to \mathbb{R}^+$.

$$\pi(x) = \frac{\mu(x)}{Z}, \qquad Z = \int_{\mathbb{R}^D} \mu(x) \, dx \text{ (unknown)}.$$

We assume we can evaluate $\mu(x)$, but we have no samples from π and do not know Z.

Goal. We seek a *sampler* (similar to MCMC/VI) that produces calibrated samples and, ideally, estimates Z without any dataset from π .

Chemistry (molecule conformers).

Different 3D conformations have a formation energy from force-field terms (bonds, angles, dihedrals, nonbonded). A low energy means a higher probability of being sampled. A well-calibrated sampler is needed to draw conformers in proportion to these probabilities, which is important in binding-pose ranking, free-energy estimation and generating diverse realistic 3D conformers for screening.

Diffusion Generative Flow Samplers

Idea. We will reframe sampling from an unnormalized target $\pi(x) \propto \mu(x)$ as a stochastic optimal control (SOC) problem. This means learning a control function that steers a diffusion process so its terminal marginal matches π .

Why this helps.

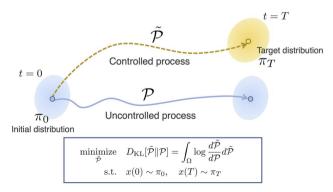
- Gives a path-space training objective/metric: a KL on trajectories $\mathrm{KL}(Q \parallel P)$ where P is the reference paths reweighted by $\mu(x_T)$.
- The partition function Z cancels inside this objective, so we can train using only μ (and optionally $\nabla \log \mu$).
- Lets us optimize without samples from π and still measure closeness to the true normalized endpoint.

Caveat (sets up DGFS). This path-KL places supervision *only at the terminal time* \Rightarrow poor *credit assignment* and high-variance gradients.

DGFS fix (preview). Inject *intermediate* learning signals via a GFlowNet-inspired *learned flow* and *subtrajectory balance*, enabling partial-trajectory training and more stable learning.

Diffusion Generative Flow Samplers v2

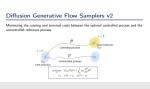
Minimizing the running and terminal costs between the optimal controlled process and the uncontrolled reference process.



Diffusion Generative Flow Samplers: Improving Learning Signals Through Partial Trajectory Optimization

Introduction
Problem Statement

Diffusion Generative Flow Samplers v2



refaire cette illustration avec le controlled, uncontrolled et target (optimal controlled) processus

Controlled and Reference Processes

Controlled forward transition (learned drift).

$$P_F(x_{n+1} | x_n) = \mathcal{N}(x_{n+1}; x_n + h f_{\theta}(x_n, n), h\sigma^2 I)$$

Controlled process.

$$Q(x_{0:N}) = p_0^{\mathsf{ref}}(x_0) \prod_{n=0}^{N-1} P_F(x_{n+1} \mid x_n)$$

Uncontrolled/Reference forward transition (zero drift).

$$P_E^{\text{ref}}(x_{n+1} \mid x_n) = \mathcal{N}(x_{n+1}; x_n, h\sigma^2 I)$$

Uncontrolled/Reference process and marginals.

$$Q^{\text{ref}}(x_{0:N}) = p_0^{\text{ref}}(x_0) \prod_{n=0}^{N-1} P_F^{\text{ref}}(x_{n+1} \mid x_n),$$

$$p_n^{\text{ref}}(x) = \mathcal{N}\left(x; \mu_0, \Sigma_0 + nh\sigma^2 I\right)$$
, is closed form.

Goal. Learn f so that the terminal marginal $Q(x_N)$ matches $\pi(x) = \mu(x)/Z$ (no data, Z unknown.).

Diffusion Generative Flow Samplers: Improving Learning Signals
Through Partial Trajectory Optimization
Introduction
Stochastic Optimal Control
Controlled and Reference Processes

Controlled and Reference Processes

Consider to and spositive, formed all θ_0 . $P(t_{t+1}|t_t) = P(t_{t+1}|t_t) + P(t_{t+1}|t_t)$ Consider proces. $P(t_{t+1}|t_t) = P(t_{t+1}|t_t) + P(t_{t+1}|t_t)$ Unconsider (finiteness traces transitive (cons. All θ_0).

Unconsider (finiteness proces and requiries.

Unconsider (finiteness proces and requiries. $P(t_{t+1}|t_t) = P(t_{t+1}|t_t) + P(t_{t+1}|t_t)$ $P(t_{t+1}|t_t) = P(t_{t+1}|t_t) + P(t_{t+1}|t_t)$ $P(t_{t+1}|t_t) = P(t_{t+1}|t_t) + P(t_{t+1}|t_t)$ $P(t_{t+1}|t_t) = P(t_{t+1}|t_t) + P(t_{t+1}|t_t)$ Get in our facility in the sum of $P(t_t) = P(t_t) + P(t_t)$ is a finite former.

Why closed form for uncontrolled but not controlled? The uncontrolled reference process has no drift, so each transition is a simple Gaussian convolution, leading to Gaussian marginals with closed-form means and variances $(e.g., p_n^{ref}(x) = N(x; mu_0, cov_0 + nh\sigma^2 I))$. The controlled process includes a learned drift $f(x_n, n)$, which makes transitions non-Gaussian and dependent on f, preventing a closed-form marginal expression without solving the integral numerically or via simulation.

je dois refaire cette slide, on ne voit meme comment xn est sample (par rapport a la SDE) et aussi d'ou sort sigma mu et la closed form expliquer et c'est une convolution de gaussienne

Stochastic Optimal Control

Path space KL objective

Target path measure via terminal reweighting.

$$P(x_{0:N}) \propto Q^{\operatorname{ref}}(x_{0:N-1}|x_N)\mu(x_N) \propto Q^{\operatorname{ref}}(x_{0:N}) \frac{\mu(x_N)}{p_N^{\operatorname{ref}}(x_N)} \Longrightarrow P(x_N) \propto \mu(x_N).$$

KL decomposition.

$$\mathrm{KL}(Q\|P) = \mathbb{E}_Q \bigg[\log \frac{Q}{P} \bigg] = \mathbb{E}_Q \bigg[\log \frac{Q}{Q^{\mathsf{ref}}} \bigg] + \mathbb{E}_Q \bigg[\log \frac{p_N^{\mathsf{ref}}(\mathsf{x}_N)}{\mu(\mathsf{x}_N)} \bigg] + \log Z.$$

Running control cost (Gaussian mean-shift) Girsanov theorem.

$$\mathbb{E}_{Q}\left[\log \frac{Q}{Q^{\mathsf{ref}}}\right] = \mathbb{E}_{Q} \sum_{n=0}^{N-1} \frac{h}{2\sigma^{2}} \|f_{\theta}(x_{n}, n)\|^{2}.$$

Terminal cost.

$$\mathbb{E}_{Q}\left[\log\frac{p_{N}^{\mathsf{ref}}(x_{N})}{\mu(x_{N})}\right] = \mathbb{E}_{Q}\left[\log p_{N}^{\mathsf{ref}}(x_{N}) - \log \mu(x_{N})\right]$$

Diffusion Generative Flow Samplers: Improving Learning Signals Through Partial Trajectory Optimization

—Introduction

Stochastic Optimal Control
Path space KL objective



Je devrais avoir une slide complete a explier d'ou vient le foward target process P parce que c'est le coeur de mon algorithme

Target Path Measure via Importance Sampling

Importance Sampling Basics. Importance sampling is a technique to estimate expectations under a hard-to-sample target distribution P using samples from an easy-to-sample proposal distribution Q. The key formula is:

$$\mathbb{E}_{x \sim Q} [f(x) \cdot w(x)] = \mathbb{E}_{x \sim P} [f(x)],$$

where the *importance weight* $w(x) = \frac{P(x)}{Q(x)}$ corrects the samples from Q to behave as if they were from P. **Intuition.** Q provides "biased" samples; w(x) upweights samples that are likely under P and downweights those that aren't, effectively resampling from P without directly sampling it.

Application to Path Measures. In our case, the "samples" are entire trajectories $x_{0:N}$, and we want the path measure P to have the correct terminal marginal $\pi(x_N) \propto \mu(x_N)$. We use the reference path measure Q^{ref} (easy to sample, e.g., Gaussian paths) as the proposal. The reweighted path measure is:

$$P(x_{0:N}) \propto Q^{\mathsf{ref}}(x_{0:N}) \cdot w(x_{0:N}),$$

where the weight $w(x_{0:N}) = \frac{\pi(x_N)}{p_N^{\text{ref}}(x_N)}$. This ensures $P(x_N) \propto \mu(x_N)$, as the weight depends only on the endpoint.

Credit Assignment Problem in SOC objective

SOC Discrete-time objective

$$\min_{f_{\theta}} \mathbb{E}_{Q} \left[\underbrace{\sum_{n=0}^{N-1} \frac{h}{2\sigma^{2}} \|f_{\theta}(x_{n}, n)\|^{2}}_{\text{Running cost}} + \underbrace{\log p_{N}^{\mathsf{ref}}(x_{N}) - \log \mu(x_{N})}_{\text{Terminal cost}} \right]$$

This objective is used on the seminar paper *Path Integral Sampler: Diffusion-based Sampling for Unnormalized Densities* by Dinghuai Zhang et al which presented the sampling from unnormalized densities as a stochastic optimal control problem.

Explanation. The SOC objective provides feedback signal only at the terminal step, making credit assignment difficult via backpropagation through time. This causes high-variance gradients, weak feedback for early actions, poor mode discovery, and inefficient optimization of the drift f without intermediate signals.

SOC as a GFlowNet

Comparison Table: GFlowNet vs. SOC Framework

Concept	GFlowNet	SOC		
Forward Process	Trajectory sampling on DAG	Controlled diffusion path		
Forward Transition Probability	$P_{F}(s' s)$	$P_F(x_{n+1} x_n) = \mathcal{N}(x_{n+1}; x_n + hf(x_n), h\sigma^2 I)$		
Backward Transition Probability	$P_B(s s')$	$P_B^{ref}(x_n x_{n+1})$ (known)		
Reward Function	R(x) (unnormalized)	$\mu(x)$ (unnormalized density)		
Terminal Marginal Distribution	$P_T(x) \propto R(x)$	$Q(x_{N}) \propto \mu(x_{N})$		
Flow State	Flow $F(s)$ at states	Learned flow $F_n(x)$		

Insight. Since SOC can be viewed as a GFlowNet, we can apply GFlowNet tools (e.g., detailed balance loss, subtrajectory balance) to solve the credit assignment problem in diffusion sampling.

Diffusion Generative Flow Samplers: Improving Learning Signals
Through Partial Trajectory Optimization

Stochastic Optimal Control to GFlowNets
Target Process

SOC as a GFlowNet

omparison Table: GFlowNet vs. SOC Framework							
oncept	GFlowNet	soc					
orward Process	Trajectory sampling on DAG	Controlled diffusion path					
orward Transition Probability lackward Transition Probability	Pr(a' a) $P_{\alpha}(a a')$	$Pr(\mathbf{x}_{n+1} \mathbf{x}_n) = \mathcal{N}(\mathbf{x}_{n+1}; \mathbf{x}_n + hf(\mathbf{x}_n), h\sigma^2 I)$ $P_{\mathbf{x}_n}^{\text{res}}(\mathbf{x}_n \mathbf{x}_{n+1}) \text{ (known)}$					
loward Function ferminal Marginal Distribution low State	R(x) (unnormalized) $P_T(x) \propto R(x)$ Flow $F(x)$ at states	$\mu(x)$ (unnormalized density) $Q(x_0) \propto \mu(x_0)$ Learned flow $F_r(x)$					

make a mental note to comeback to professor hernandez comment on Tristan's Deleu presentation when someone asked: "The if GFlowNets are just Reinfrocement Learning, then why keep doing research on this framework?" Professor Hernandez reponded by proving the felxibility of GFN, he said that it was en entery point between RL, Diffusion models, Energy-based models and in this case we prove that it can also be used in Stochastic Optimal Control problems.

Decomposition of the Target Process

Target Process Decomposition. The target path measure can be decomposed into a product of conditional distributions:

$$P(x_{0:N}) \propto Q^{\mathsf{ref}}(x_{0:N}) \frac{\mu(x_N)}{p_N^{\mathsf{ref}}(x_N)} \implies P(x_N) \propto \mu(x_N).$$

Conditional Form. Since the reweighting only affects the terminal state, the joint can be written as:

$$P(x_{0:N}) = \pi(x_N) \prod_{n=0}^{N-1} P_B^{\mathsf{ref}}(x_n|x_{n+1}),$$

where $P_B^{\text{ref}}(\cdot|\cdot)$ is the backward transition probability (derived from the target joint). This is tractable because P_B^{ref} is known because they are Gaussian convolutions with a known mean and variance.



Diffusion Generative Flow Samplers: Improving Learning Signals
Through Partial Trajectory Optimization

Stochastic Optimal Control to GFlowNets

GFlowNet

Decomposition of the Target Process

Decomposition of the Target Process Teap Proce Demonstrate. The torp and neares on the description does not not not obtained administration of devictions: $F(u_n) = G^{*}(u_n) \frac{du^2}{du^2} = F(u_n) \times \rho(u_n)$ Confident From. Since the modeling only plants to the confident stars, the joint can be written as $F(u_n) = c(u_n) \prod_{i=1}^n F^{*}_{i}(u_i(u_{i+1}), \dots, u_n)$ where $F^{*}_{i}(v_i)$ is the behavior transition pointaint; (administration from the target point). This is transition from $F^{*}_{i}(v_n)$ is the behavior transition plants (in finite from the target point). This is transition from $F^{*}_{i}(v_n)$ is the behavior transition plants (in finite from the target point). The is transition of the finite from the target point $F^{*}_{i}(v_n)$ is the behavior transition plants (in Fig. 1) and $F^{*}_{i}(v_n)$ is the second transition of $F^{*}_{i}(v_n)$ in the finite from the target $F^{*}_{i}(v_n)$ is the finite from the finite from the support of $F^{*}_{i}(v_n)$ is the finite from the finite form of $F^{*}_{i}(v_n)$ is the finite form of $F^{*}_{i}(v_n)$ in the finite form of $F^{*}_{i}(v_n)$ is the finite form of $F^{*}_{i}(v_n)$ in the finite form of $F^{*}_{i}(v_n)$ in the finite form of $F^{*}_{i}(v_n)$ is the finite form of $F^{*}_{i}(v_n)$ in the finite form of F^{*

conditional form is exactly like the RHS of the trajectory balance equation in gfn. Lire le paper de Nikolay sur Trajectory Balance pour bien comprendre cette equation et comment elle se relie a DGFS

GFlowNet

If We Had Access to $p_n(x_n)$ we could write the partial joint which would allow training on subtrajectories and thus have better credit assignment:

$$P(x_{0:n}) = p_n(x_n) \prod_{k=0}^{n-1} P_B(x_k|x_{k+1}),$$

But There's No Closed Form for $p_n(x_n)$. To calculate $p_n(x_n)$, we would need to compute the integral:

$$p_n(x_n) = \int \pi(x_N) \prod_{n=1}^{N-1} P_B(x_n|x_{n+1}) dx_{n+1:N}.$$

Why Is $p_n(x_n)$ Hard to Compute? The reference marginal at step N is a simple Gaussian formula. But for the target marginal at earlier steps n < N, there's no easy formula because the target process depends on the terminal state $\pi(x_N)$, making it complex. Computing it needs integrating over many future states, which can't be done analytically for general targets. At n = N, it's just $\pi(x_N)$, but earlier steps are harder.

Solution: Learn an Approximation $F_n \approx p_n$. We introduce a learned flow function $F_n(x_n; \theta)$ parameterized by a neural network to approximate $p_n(x_n)$. This avoids computing the intractable integral at every training step.



Diffusion Generative Flow Samplers: Improving Learning Signals
Through Partial Trajectory Optimization

Stochastic Optimal Control to GFlowNets

GFlowNet

Rewriting the Target Process with Marginal

Fig. that According to the poly-level and the the part of pick and the dark for toxing an administration and the term could an against the term could an against the term could are against the pick of the pick

Rewriting the Target Process with Marginal

ne pas oublier de parler des MC quadrature method pour approximer l'integral mais c'est couteux en temps de calcul et pas scalable du tout

Trajectory Balance with Learned Flow

Proposed Amortized Approach. Train $F_n(\cdot; \phi)$ to satisfy the following constraint for all partial trajectories $x_{n:N}$:

$$F_n(x_n;\phi)\prod_{k=n}^{N-1}P_F(x_{k+1}|x_k;\theta)=\mu(x_N)\prod_{k=n}^{N-1}P_B(x_k|x_{k+1}).$$

Details.

- P_F (forward policy) and F_n are parameterized by deep neural networks, with parameters θ and ϕ respectively.
- We can view F_n as an approximation to the unknown marginal $p_n(x_n)$ thus an amortized way to estimate the intractable integral.
- We use only $\mu(\cdot)$ (no Z), so the unknown normalization is absorbed into F_n .

GFlowNet

Detailed Balance from Trajectory Balance condition. Comparing the constraint for n and n+1 gives a formula independent of μ which now only involves local transitions (signal subtrajectories instead of full trajectories)

$$F_n(x_n;\theta)P_F(x_{n+1}|x_n;\theta)=F_{n+1}(x_{n+1};\theta)P_B(x_n|x_{n+1}).$$

GFlowNet

Subtrajectory Balance Loss for Partial Trajectories.

$$\ell_{\mathsf{SubTB}}(x_{m:n}; \theta, \phi) = \left(\log \frac{F_m(x_m; \phi) \prod_{k=m}^{n-1} P_F(x_{k+1} | x_k; \theta)}{F_n(x_n; \phi) \prod_{k=m}^{n-1} P_B(x_k | x_{k+1})}\right)^2$$

Forward Process (Controlled). The learned forward transition depends on θ :

$$P_F(x_{n+1}|x_n;\theta) = \mathcal{N}\left(x_{n+1};x_n + hf_{\theta}(x_n,n),h\sigma^2I\right),$$

where $f(x_n, n)$ is the learned drift parameterized by θ .

Diffusion Generative Flow Samplers: Improving Learning Signals
Through Partial Trajectory Optimization

Stochastic Optimal Control to GFlowNets
GFlowNet
Subtrajectories Loss

Subtrajectories Loss Marijectories (Subtrajectories) $\frac{(x_{i+1}, x_{i+1}, \dots, x_{i+1})}{(x_{i+1}, x_{i+1}, \dots, x_{i+1})} \left(\left(\frac{x_{i+1}}{x_{i+1}} \frac{(x_{i+1}, x_{i+1})}{x_{i+1}} \frac{x_{i+1}}{x_{i+1}} \frac{x_{i+1}}{x_{i+1}} \right)^{1} \right)$ Formed Fromm (Cantenday). The former forest transition depends in it. $\frac{(x_{i+1}, x_{i+1}, \dots, x_{i+1})}{(x_{i+1}, x_{i+1})} \frac{x_{i+1}}{x_{i+1}} \frac{x_{i+1}$

a voir si je voudrais pas mettre une schema sur l'une des 3 derniers slides pour faire un recap de scrap la SOC objective, now we build DB loss with learned flow to solve credit assignment problem

Overall Training Objective

Recall SubTB Loss

$$\ell_{\mathsf{SubTB}}(x_{m:n}; \theta, \phi) = \left(\log \frac{F_m(x_m; \phi) \prod_{k=m}^{n-1} P_F(x_{k+1} | x_k; \theta)}{F_n(x_n; \phi) \prod_{k=m}^{n-1} P_B(x_k | x_{k+1})}\right)^2$$

Diffusion Generative Flow Sampler (DGFS) Loss

$$L(\tau;\theta;\phi) = \frac{\sum_{0 \leq m < n \leq N} \lambda^{n-m} \ell_{\mathsf{SubTB}}(x_{m:n})}{\sum_{0 \leq m < n \leq N} \lambda^{n-m}}, \quad \tau = (x_0, \dots, x_N)$$

This combines signals from all subtrajectory lengths, reducing variance and improving credit assignment

- τ : Full trajectory (x_0, \ldots, x_N) .
- λ: Positive scalar weighting different subtrajectory lengths (e.g., shorter subtrajectories get higher weight if λ < 1).
- The numerator sums SubTB losses over all subtrajectories $x_{m:n}$, weighted by λ^{n-m} (length-based weighting).
- The denominator normalizes to average the losses..

Algorithm 1 DGFS Training

Require: $\mu(\cdot)$, $\bar{\sigma}$, N, λ , B, η

- 1: Init $\theta = (\theta_f, \phi)$
- 2: repeat
- 3: Sample trajectories:
- 4: **for** b = 1 to B **do**
- 5: $\tau^{(b)} = (x_0^{(b)}, \dots, x_N^{(b)}) \text{ under } x_{n+1} = x_n + hf_{\theta_{\ell}}(x_n, n) + \sqrt{h}\bar{\sigma}\varepsilon_n, \ \varepsilon_n \sim \mathcal{N}(0, I)$
- 6: end for
- 7: Build subtrajectories: $S(\tau^{(b)})$ of (m, n) with $0 \le m < n \le N$
- 8: Compute SubTB loss:

$$\mathcal{L}(\tau^{(b)}; \theta) = \sum_{(m,n) \in \mathcal{S}(\tau^{(b)})} \lambda^{n-m} \left[\log \frac{F_{\phi}(x_m) \prod_{l=m}^{n-1} P_F(x_{l+1} \mid x_l; \theta_f)}{F_{\phi}(x_n) \prod_{l=m}^{n-1} P_B^{\text{ref}}(x_l \mid x_{l+1})} \right]^2$$

- 9: $g \leftarrow \nabla_{\theta} \frac{1}{B} \sum_{b=1}^{B} \mathcal{L}(\tau^{(b)}; \theta)$
- 10: $\theta \leftarrow \operatorname{Adam}(\theta, g, \eta)$
- 11: until convergence

Reduction of gradient variance

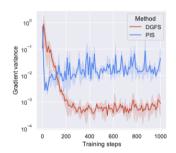


Figure: Gradient variance comparison between DGFS and PIS. DGFS shows significantly lower variance, leading to more stable training.

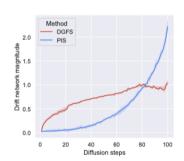


Figure: Drift network magnitude of DGFS and PIS

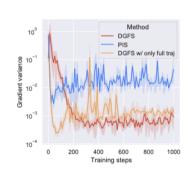


Figure: Gradient variance of DGFS, PIS, and DGFS trained with only full paths

Accurate partition function Z estimation

How to Estimate Z. The partition function $Z=\int \mu(x)\,dx$ normalizes the density. Since we sample trajectories from the learned process Q, we estimate Z using importance sampling on the terminal states. Log-partition function estimator:

$$\log \sum_{b=1}^{B} \exp(S(\tau^{(b)}; \theta)) - \log B \leq \log Z, \quad \tau^{(b)} \sim Q(\cdot; \theta).$$

Intuition (Simple).

Introduction

- $S(\tau;\theta)$: Weight showing how well the trajectory matches the target (higher if it ends in high- μ regions).
- Sample many trajectories from Q, compute their weights, and average in log space.
- This gives a lower bound on $\log Z$ because Q approximates the target, providing an estimate without direct π samples.

Partition function estimation results

	MoG	Funnel	MANYWELL	VAE	Cox
SMC VI-NF CRAFT FAB w/ Buffer ⁵	$\begin{array}{c} 0.289 {\pm} 0.112 \\ 1.354 {\pm} 0.473 \\ 0.348 {\pm} 0.210 \\ 0.003 {\pm} 0.0005 \end{array}$	$\begin{array}{c} 0.307 {\pm} 0.076 \\ 0.272 {\pm} 0.048 \\ 0.454 {\pm} 0.485 \\ 0.0022 {\pm} 0.0005 \end{array}$	$\begin{array}{c} 22.36 {\pm} 7.536 \\ 2.677 {\pm} 0.016 \\ 0.987 {\pm} 0.599 \\ 0.032 {\pm} 0.004 \end{array}$	$\begin{array}{c} 14.34{\pm}2.604 \\ 6.961{\pm}2.501 \\ 0.521{\pm}0.239 \\ \text{N/A} \end{array}$	$\begin{array}{c} 99.61 {\pm} 8.382 \\ 83.49 {\pm} 2.434 \\ 13.79 {\pm} 2.351 \\ 0.19 {\pm} 0.04 \end{array}$
PIS DDS DGFS	$\begin{array}{c} 0.036 {\pm} 0.007 \\ 0.028 {\pm} 0.013 \\ 0.019 {\pm} 0.008 \end{array}$	$0.305{\scriptstyle \pm 0.013} \\ 0.416{\scriptstyle \pm 0.094} \\ 0.274{\scriptstyle \pm 0.014}$	$\begin{array}{c} 1.391 {\pm} 1.014 \\ 1.154 {\pm} 0.626 \\ 0.904 {\pm} 0.067 \end{array}$	$\begin{array}{c} 2.049 {\pm} 2.826 \\ 1.740 {\pm} 1.158 \\ 0.180 {\pm} 0.083 \end{array}$	$11.28{\scriptstyle\pm1.365}\atop \text{N/A}^{6}\cr 8.974{\scriptstyle\pm1.169}$

Figure: The lower the better, DGFS achieves the lowest bias in estimating the partition function across various benchmarks compared to PIS and DDS.

Convergence Guarantees

Convergence Guarantees for DGFS.

- Previous studies De Bortoli et al. 2022; Chen et al. 2022; Lee et al. 2022 show that the terminal sample distribution of a diffusion model converges to the target under mild assumptions if the control term is well learned. These apply to DGFS since proofs are independent of training method.
- Zhang et al. 2022 prove that a perfectly learned score corresponds to zero GFlowNet training loss
 E. Bengio, Jain, et al. 2021; E. Bengio, S. Bengio, et al. 2023, ensuring a well-trained DGFS accurately samples from the target distribution.

Diffusion Generative Flow Samplers: Improving Learning Signals Through Partial Trajectory Optimization

— Diffusion Generative Flow Sampler Results

Convergence Guarantees
Convergence Guarantees

Convergence Guarantees

Convergence Guarantees for DGFS.

• Previous studies De Bortoli et al. 2022: Chen et al. 2022: Lee et al. 2022 show that the termina

sample distribution of a diffusion model converges to the target under mild assumptions if the control term is well learned. These apply to DGP's since proofs are independent of training method. 2. Thans et al. 2022 more that a perfectly learned score corresponds to zero. GPLowNet training loss

Zhang et al. 2022 prove that a parfectly learned score corresponds to zero GFlowNet training loss E. Benglo, Juln, et al. 2021; E. Benglo, S. Benglo, et al. 2023, ensuring a well-trained DGFS accurately samples from the target distribution.

Le but de montrer cette slide de garanties de convergences est pour prouver que malgrer les examples simples MoG, Manywell, etc (doivent etre simple pour avoir acces a la partition function Z , on peut garantir que DGFS va converger vers la bonne distribution cible pour des targets plus complexes.)

Mode coverage results

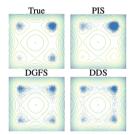


Figure: Manywell plots. DGFS and DDS but not PIS recover all modes

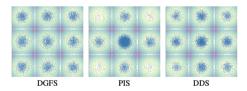


Figure: MoG visualization of DGFS and other diffusion-based samplers shows that DGFS could capture the diverse modes well. The contours display the landscape of the target density

Off-policy training capability (a voir si on garde cette slide)

Off-Policy Training in DGFS. Unlike previous KL-based methods restricted to on-policy training (high-variance off-policy via importance sampling), DGFS supports off-policy exploration without it, as its objectives (Eq. 9/14) don't require samples from a specific distribution malkin2023; lahlou2023.

Exploration Strategy. Use a larger variance coefficient $\tilde{\sigma} > \sigma$ in the forward process during rollouts to capture diverse modes, improving multimodal sampling.

Example: MoG+ Task. With distant modes, setting $\tilde{\sigma}=2$ (vs. $\sigma=1$) achieves better mode coverage and lower Z estimation bias.

DGFS+ Experiment. Linearly anneal $\tilde{\sigma}$ from 1.1 to 1 over first 1000 steps, enhancing performance in some scenarios as a tunable hyperparameter.

Conclusion

Introduction

Summary

Summary. Diffusion Generative Flow Sampler (DGFS), a novel algorithm that trains diffusion models to sample from given unnormalized target densities. Different from prior works (Path Integral Sampler and Denoising Diffusion Sampler) that could only learn from complete diffusion chains, DGFS can update its parameters with only partial specification of the stochastic process trajectory. These features help DGFS benefit from efficient credit assignment and thus achieve better partition function estimation bias in the sampling benchmarks while keeping the theoretical guarantees of convergence from diffusion-based samplers.

Questions and hopefully answers:)

Questions?

Q&A

Bengio, Emmanuel, Salem Bengio, et al. (2023). "GFlowNet Foundations". In: Journal of Machine Learning Research 24, pp. 1–55.

Diffusion Generative Flow Sampler Results

- Bengio, Emmanuel, Moksh Jain, et al. (2021). "Flow Network based Generative Models for Non-Iterative Diverse Candidate Generation". In: Advances in Neural Information Processing Systems 34, pp. 27381–27394.
- Chen, Nan et al. (2022). "On the convergence of score-based generative modeling". In: arXiv preprint arXiv:2206.04114.
- De Bortoli, Valentin et al. (2022). "Convergence of score-based generative modeling for general data distributions". In: Advances in Neural Information Processing Systems 35, pp. 21892-21904.



Q&A

Lee, Hyeontae et al. (2022). "Convergence of denoising diffusion models under the manifold hypothesis". In: arXiv preprint arXiv:2205.12551.



Zhang, Dinghuai et al. (2022). "Path Integral Sampler: Diffusion-based Sampling for Unnormalized Densities". In: *Advances in Neural Information Processing Systems* 35, pp. 11738–11751.