

The **Do-Operator** ( $\text{do}(X = x)$ ) represents an **intervention**: it forces the variable  $X$  to take the value  $x$ , **breaking its natural causes**.



**The Do-Operator allows to test out counterfactuals:**

- For this historical figure, what if they had received a classical education instead of a religious one? What if it had been a man instead of a woman?
- For this manuscript, what if it had been printed with a movable type press rather than hand-copied?
- For this region, what if the dominant language in the 13th century had been Czech instead of German? What if  **Přemysl Otakar II**  had kicked Rudolf of Habsburg's butt?

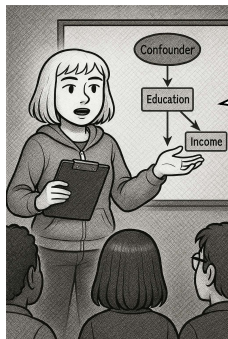
To understand the do-Operator:

- In `simulate_data()`, a causal graph with a confounder is simulated.
- In `estimate_adjusted_model(data)` we control the confounder by regression.
- In `predict_do_intervention()` we use the regressed values, to produce input-data (as if the confounder was fixed). We are now able to predict the effect of education on income, as if there was no confounder.



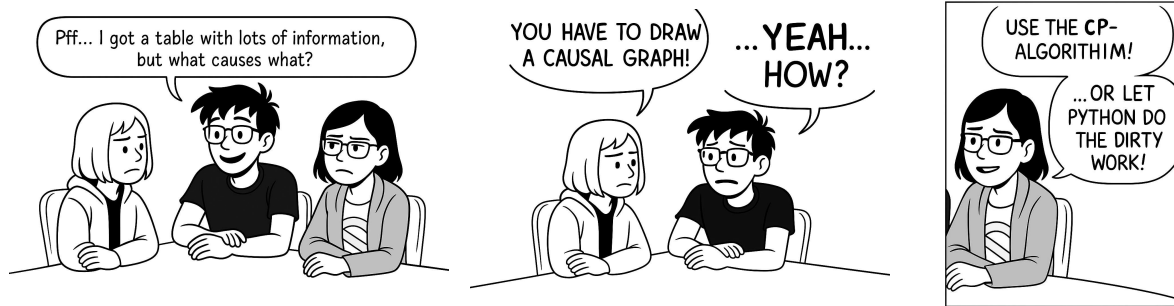
Do-Operator notation:  $P(a_i | \text{do}(B = b_i), \beta, \gamma, c_i)$

$b_i$  = controlled variable  
 $\beta, \gamma$  = other variables  
 $c_i$  = treatment variable

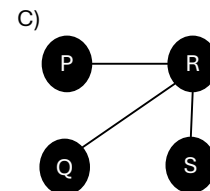
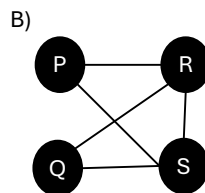
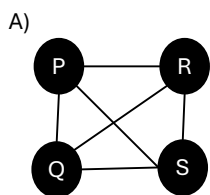


- The do-Operator can simulate a world, where a confounder has no influence on the data.
- We can also simulate and then compare two different worlds: One, where something happens – and one where it does not (ATE).
- We can simulate two versions of an individual (ITE).
- We can average impact of a treatment on those that are treated (ATT)

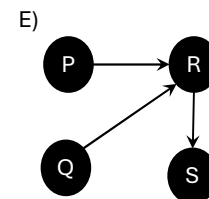
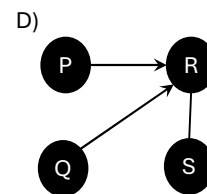
- Run `doOperator.py`.
- Explain the visualization.
- In your own words: What is the do-Operator *doing*?



- File causalLearn.py simulates a collider graph with Nodes Q,P,R,S and stores information in a pandas data frame (a table).
- The PC-algorithm is applied using significance test, to find depended nodes
- It calculates the resulting graph.



- 1. Start with a fully connected undirected graph** (between all observed variables)
- 2. Remove edges for unconditional independence** (i.e., if two variables are marginally independent)
- 3. Remove more edges using conditional independence**
  1. For each pair A-B, check all subsets C of adjacent variables
  2. If  $A \perp\!\!\!\perp B \mid C$ , remove the edge between A and B
- 4. Orient v-structures (colliders):**
  1. If  $A-B-C$ , and A and C are not connected, and A is **not** independent of C given B  $\rightarrow$  then orient as  $A \rightarrow B \leftarrow C$
- 5. Propagate orientation using Meek's rules**
  1. For example: avoid cycles, prevent new colliders, etc.



- Run causalLearn.py.
- Identify nodes of the “real” graph in the resulting graph.
- Imagine running PC-algorithm on real world data. What could be the benefits?