Course 02402 Introduction to Statistics Lecture 13:

A course summary

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Agenda - the 12 lectures

1. Chapter 1: Simple Graphics and Summary Statistics
2. Chapter 2: Discrete Distributions
3. Chapter 2: Continuous Distributions
4. Chapter 3: One sample confidence intervals
5. Chapter 3: One sample hypothesis testing
6. Chapter 3: Two Sample statistics
7. Chapter 4: Statistics by simulation
8. Chapter 5: Simple linear Regression Analysis
9. Chapter 6: Multiple linear Regression Analysis
10. Chapter 8: One-way Analysis of Variance
11. Chapter 8: Two-way Analysis of Variance
12. Chapter 7: Inferences for Proportions

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Chapter 1: Simple Graphics and Summary Statistics

- Look at data as it is! (descriptive statistics)
- Summary Statistics
  - Mean $\bar{x}$
  - Standard deviation s, variance s^2
  - Median, upper- and lower quartiles
- Simple graphics
  - Scatter plot (xy plot)
  - Histogram, cumulative distribution
  - Boxplots, Bar charts, Pie charts

Agenda

Chapter 2: Discrete Distributions

- General concepts:
  - Definition of a stochastic variable
  - Density function
  - Distribution function
  - Mean and variance
- Specific distributions:
  - The binomial distribution
  - The hypergeometric distribution
  - The Poisson distribution

Agenda

Chapter 2: Continuous Distributions

- General concepts:
  - Density function, distribution function
  - Mean, variance
  - Calculation rules for stochastic variables
- Specific distributions:
  - Normal
  - Log-Normal, Uniform, Exponential

Agenda

Chapter 3: One sample confidence intervals

- General concepts
  - Estimation, confidence intervals
  - Population and a random sample
  - Sampling distributions (t and χ^2)
  - Central Limit Theorem
- Specific methods, one sample:
  - Confidence intervals for the mean
  - Confidence intervals for the variance (and standard deviation)

Agenda

Chapter 3: One sample hypothesis testing

- General concepts:
  - Hypotheses, p-value, Significance level
  - Type I and Type II error, Power
- Specific methods, One sample:
  - t-test for mean difference
  - Sample size for wanted power
  - Normal qq-plot

Agenda

Chapter 3: Two Samples

- Specific methods, two samples:
  - Test and confidence interval for the mean difference (t-test)
- Specific methods, two PAIRED samples:
  - "Take difference" $\Rightarrow$ "One sample"
- Planning for precision and/or power
  - One-sample Confidence interval: sample size for wanted precision
  - One-sample hypothesis test: sample size for wanted power (or other combinations)
  - Two-sample hypothesis test: sample size for wanted power (or other combinations)

Agenda

Chapter 4, Statistics by simulation

- Introduction to simulation
- Error propagation rules
- Bootstrapping
  - Parametric
  - Non-parametric
  - Confidence intervals (and hence also hypothesis testing)
- Specific situations: (4 versions of confidence intervals)
  - One-sample and Two-sample data
  - Parametric and Non-parametric

Agenda

Chapter 5: Simple linear Regression Analysis

- Two quantitative variables, x and y.
- Calculating least squares line
- Inferences for a simple linear regression model
  - Statistical model: $y_i = \beta_0 + \beta_1 x_i + \varepsilon_i$
  - Interval estimation and test for β_0 and β_1.
  - Confidence interval for the expected line.
  - Prediction interval.
- r and r^2
  - r describes the strength of a linear relation.
  - r^2 expresses the proportion of the y variability explained by the linear relation.

Agenda

Chapter 6: Multiple linear Regression Analysis

- Many quantitative variables, x_1, x_2 and y.
- Calculating least squares fit
- Inferences for a the multiple linear regression model
  - Statistical model: $y_i = \beta_0 + \beta_1 x_{1,i} + \beta_2 x_{2,i} \varepsilon_i$
  - Interval estimation and test for β_0 and β_i.
  - Confidence interval for the expected fit.
  - Prediction interval.
- r^2 expresses the proportion of the y variability explained by the linear relation.

Agenda

Chapter 8: One-way Analysis of Variance

- Specific methods, k INDEPENDENT samples
- One-way analysis of variance
  - Compares the means of the groups
  - ANOVA-table: $SST = SS(Tr) + SSE$
  - F-test.
  - Post hoc test: pairwise t-test with/without Bonferroni correction

Agenda

Chapter 8: Two-way Analysis of Variance

- Block design - two-way analysis of variance
- ANOVA-tabel: $SST = SS(Tr) + SS(Bl) + SSE$
  - SST, $SS(Tr)$ and $SS(Bl)$ calculated as one-way ANOVA
  - $SSE = SST - SS(Tr) - SS(Bl)$
- F-test.
- Post hoc test: pairwise t-test with/without Bonferroni correction

Agenda

Chapter 7: Inferences for Proportions

- Specific methods, one, two and $k > 2$ samples
  - Binary/categorical response
- Estimation and confidence interval of proportions
  - Large sample vs. small sample methods
- Hypotheses for one proportion
- Hypotheses for two proportions
- Analysis of contingency tables (χ^2-test) (All expected > 5)

Agenda