

1. Consider a complete undirected graph with vertex set  $V = \{0, 1, 2, 3, 4\}$ . Entry  $W[i][j]$  in the matrix  $W$  below is the weight of the edge  $(i, j)$ . What is the minimum possible weight of a spanning tree  $T$  in this graph such that vertex 0 is a leaf node in the tree  $T$ . Briefly explain your answer. (3p)

- a. 9
- b. 7
- c. 8
- d. 10

$$W = \begin{pmatrix} 0 & 1 & 8 & 1 & 4 \\ 1 & 0 & 12 & 4 & 9 \\ 8 & 12 & 0 & 7 & 3 \\ 1 & 4 & 7 & 0 & 2 \\ 4 & 9 & 3 & 2 & 0 \end{pmatrix}$$

2. If a graph has 92 vertices, how many edges are in the minimum spanning tree? Briefly explain your answer. (1p)

- a. 93
- b. 91
- c. 92
- d. 9
- e. Cannot be determined with the given information.

3. Given the weights and values of the items below, put these items in a knapsack of capacity  $W = 30$  to get the maximum total value in the knapsack. Which is the maximum value obtained? Illustrate the steps in Knapsack Problem algorithm to answer. (2p)

$val[] = \{ 60, 100, 120 \};$

$wt[] = \{ 10, 20, 30 \};$

4. Simulate Dijkstra's algorithm on the edge-weighted graph below, starting from vertex 0. (2p)

