Transactional Logic

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0.0 Introduction

I talked about my original idea called *propositional stability-* roughly, when a truth-value for a proposition or sentence remains bound by the same range of truth-values after being *transacted* between two logics regardless of the range of truth-values available within the second logic.

So, no proposition or sentence assigned true or false under a classical logic can be assigned say both true and false within say a Kleene 3-valued so-called logic of contradiction (Priest's logic of paradox where a third-truth value is understood as standing for both true and false rather than as indeterminate which was proposed as a solution to Alethic paradox).

I'd like to take some time to elaborate that concept, discuss two related concepts, and then talk briefly about <u>combined modal logics</u> which have just begun to be studied.

Again, importantly, a lot of this discussion fits within the larger <u>logical pluralism</u> debate which regards the feasibility of at least one of the following three theses:

- (1) There is no one, sole and universal, logic that structures, limits, defines, or describes all of reality.
- (2) There are either multiple truth-predicates/operators, conceptions of truth, and/or alethic inferences underpinning truth-predicates/operators.
- (3) There are multiple truth-properties.

That thesis is not as radical as it might at first seem -abductive reasoning is common in law, medicine, and science and requires something like a non-monotonic logical framework to truly represent and understand the types of valid inference patterns allowed. Classical logic (Boolean Algebra), however, is monotonic.

1.0 Definitions

Meta-language: (following <u>Tarski</u>) a language *L* sufficient for First-Order Logic within which object languages are constructed.

Object-language: a language O constructed within a meta-language L - the target language to

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be specified or built.

Cross Logics: two object languages O1 and O2 so-constructed in a meta-language L such that they comprise a transactional logic are each referred to as the cross logic of the other.

Logical Transaction: a time-based mechanism or procedure by which a proposition *P* in a metalanguage *L* also residing in an object language *O* in *L* is assigned a new truth-value within the cross logic of *L*.

Transactional Logic: a meta-language L implements a transactional logic if-and-only-if L contains languages O1, ... that are cross logics of each other supporting logical transactions between them.