Main

July 13, 2018

```
In [1]: import halotools
    import numpy as np
    import matplotlib.pyplot as plt
    from scipy.optimize import curve_fit
    %matplotlib inline
```

1 1) Import data

We begin with the analysis of a subsample of the Bolshoi simulation with Planck cosmology as of 2013 (h=0.7, Ω_{Λ} =0.69289, Ω_{m} = 0.30711, Ω_{b} = 0.048, n_{s} = 0.96, σ_{8} = 0.82). The simulation started at z_{ini} = 80 and followed 2048³ particles of mass M_{dm} = 1.55 × 10⁸ M_{sun}/h in their evolution in a volume of boxsize L=250 Mpc/h.

```
In [3]: #Catalog of halos itself
    halos = halocat.halo_table
    #To see what properties are available
    print(halos.keys())

['halo_vmax_firstacc', 'halo_dmvir_dt_tdyn', 'halo_macc', 'halo_scale_factor', 'hal
```

2 2) Organize the data into samples

```
In [4]: from halotools.utils import group_member_generator
    #Group halos by halo host id
    halos.sort('halo_hostid')
    grouping_key = 'halo_hostid'
    requested_columns = []
    group_gen = group_member_generator(halos, grouping_key, requested_columns)

#calculates the number of subalos per host
    nsub = np.zeros(len(halos))
    for first, last, member_props in group_gen:
```

```
In [5]: NumberHosthalos=0
        NumberSubhalos=0
        for i in range(0,len(halos)):
             if halos["halo_pid"][i]==-1:
                 NumberHosthalos= NumberHosthalos+1
             else:
                 NumberSubhalos = NumberSubhalos+1
        print("Number of halos in total, unfilterd bolplank catalog", len(halos))
        print("Number of hosthalos, unfilterd bolplank catalog", NumberHosthalos)
        print("Number of subhalos, unfilterd bolplank catalog", NumberSubhalos)
Number of halos in total, unfilterd bolplank catalog 1444262
Number of hosthalos, unfilterd bolplank catalog 1078614
Number of subhalos, unfilterd bolplank catalog 365648
In [9]: #Attribute Subhalos with the Positions of their respective host in order to
        #center of mass frame:
        halos.add_column(halos["halo_x"], name="Host_x")
        halos.add_column(halos["halo_y"], name="Host_y")
        halos.add_column(halos["halo_z"], name="Host_z")
        halos.add_column(halos["halo_vx"], name="Host_vx")
        halos.add_column(halos["halo_vy"], name="Host_vy")
        halos.add_column(halos["halo_vz"], name="Host_vz")
  The catalog is filtered by the following criteria. We generate two samples:
  Sample 1 consists of all host halos with M_{vir} < 10^{15} M_{sun} and with M_{vir}/M_{Dm,partcl} > 100
together with the subhalos with M_{vir}/M_{Dm,partel} > 100, M_{vir}/M_{Vir,Host} > 10^{-3} and with
M_{Vir,Host} < 10^{15} M_{sun}.
  Sample 2 is constrained under the same criteria as Sample 1, but one of the conditions on the
subhalos, namely M_{vir}/M_{Vir,Host} > 10^{-3}, is removed.
In [6]: ##We consider two main samples:
        ##Sample 1: Consider all halos consisting of more than 100 dm particles and
        ##Sample 2: Take into account all halos and still exclude hosts with less
        #The mask for the hosts
        M_dm_particle = 1.55e8
        host_maskSample1 = ((halos['halo_upid'] == -1) & (halos["halo_mvir"] < 1e15)</pre>
        hostsSample1 = halos[host_maskSample1]
        #mask for the subhalos
        sub_maskSample1 = ((halos["halo_upid"]>0) & ((halos['halo_mvir']/halos["halo_
```

#Adds a new column to the ith-row of the table which gives the number of su

nsub[first:last] = last - first - 1

halos['num_subhalos'] = nsub

```
subsSample1 = halos[sub_maskSample1]
sub_maskSample2 = ((halos["halo_upid"]>0)&(halos["halo_mvir_host_halo"]< 1e
subsSample2 = halos[sub_maskSample2]

print("Number of hosthalos in Sample 1 = ", len(hostsSample1))
print("The mean concentration of host halos in sample 1 is ", "r$ \bar{c}$?
print("Number of subhalos in Sample 1 = ", len(subsSample1))
print("Number of subhalos in Sample 2 = ", len(subsSample2))

C:\Users\ThimoPreis\Anaconda3\lib\site-packages\ipykernel\__main__.py:12: RuntimeWalos

Number of hosthalos in Sample 1 = 1071702
The mean concentration of host halos in sample 1 is r$ ar{c}$ = 16.0799

Number of subhalos in Sample 1 = 224818

Number of subhalos in Sample 2 = 289020

In []:</pre>
```

3 3) Radial density profile

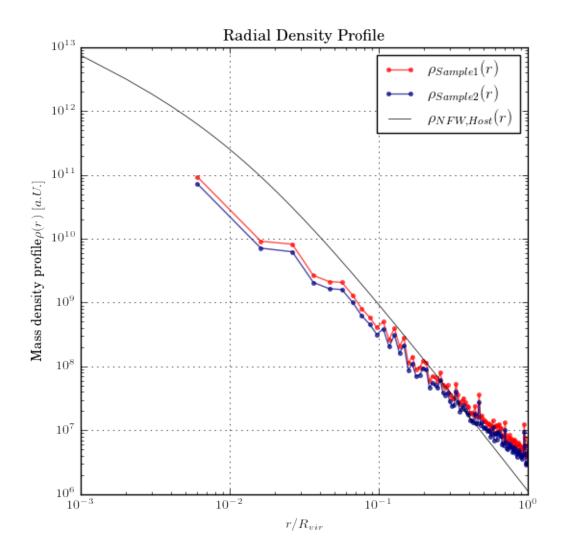
```
In [7]: from halotools.mock_observables import return_xyz_formatted_array
        host_pos_sample1 = return_xyz_formatted_array(hostsSample1['halo_x'], hosts
        sub_pos_sample1 = return_xyz_formatted_array(subsSample1['halo_x'], subsSample1
        sub_pos_sample2 = return_xyz_formatted_array(subsSample2['halo_x'], subsSample2
        hx1 = hostsSample1["halo_x"]
        hy1 = hostsSample1["halo_y"]
        hz1 = hostsSample1["halo_z"]
        sx1 = subsSample1["halo_x"]
        sy1 = subsSample1["halo_y"]
        sz1 = subsSample1["halo_z"]
        sx2 = subsSample2["halo_x"]
        sy2 = subsSample2["halo_y"]
        sz2 = subsSample2["halo_z"]
        hvx1 = hostsSample1["halo_vx"]
        hvy1 = hostsSample1["halo_vy"]
        hvz1 = hostsSample1["halo_vz"]
        svx1 = subsSample1["halo_vx"]
        svy1 = subsSample1["halo_vy"]
        svz1 = subsSample1["halo_vz"]
        svx2 = subsSample2["halo_vx"]
        svy2 = subsSample2["halo_vy"]
```

svz2 = subsSample2["halo_vz"]

```
In [9]: from halotools.mock_observables import radial_profile_3d
        rbins_normalized = np.linspace(0.001, 1, 100)
        rbins_midpoints = (rbins_normalized[:-1] + rbins_normalized[1:])/2
        Density_profileSample1, CountsSample1 = radial_profile_3d(host_pos_sample1,
                                    rbins_normalized = rbins_normalized,
                                    normalize_rbins_by = hostsSample1['halo_rvir'],
                                    period=halocat.Lbox, return_counts = True)
        Density_profileSample2, CountsSample2 = radial_profile_3d(host_pos_sample1,
                                    rbins_normalized = rbins_normalized,
                                    normalize_rbins_by = hostsSample1['halo_rvir'],
                                    period=halocat.Lbox,return_counts = True)
In [10]: shell_volumes = 4/3*np.pi*(rbins_normalized[1:]**3-rbins_normalized[:-1]**
         MeanNumberDensitySample1 = (CountsSample1/float(len(subsSample1)))/shell_v
         MeanNumberDensitySample2 = (CountsSample2/float(len(subsSample2)))/shell_v
In [19]: #Model NFW profil of the hosts
         #from halotools import empirical_models
         #from halotools.empirical_models import NFWProfile
         #nfw = NFWProfile(conc_mass_model='direct_from_halo_catalog', mdef='vir',
         #model_conc = nfw.conc_NFWmodel(table=hostsSample1)
         #Write NFW profile function yourself:
         from halotools.empirical_models import density_threshold
         from astropy import cosmology
         from astropy.cosmology import LambdaCDM
         cosmo = LambdaCDM(H0=70, Om0=0.3, Ode0=0.7)
         m_dm=1.55e8
         def NFW(r):
             return density_threshold(cosmo,0,mdef="vir") *0.3/3*np.mean(hostsSample
         rhocrit = cosmo.critical_density0
         #Another definition, completely equivalent to NFW, not neccessary to use I
         c=np.mean(hostsSample1["halo_nfw_conc"])
         def nfwProfile(r):
             return (200 \times \text{rhocrit} \times \text{c})/3/(\text{np.log}(1+\text{c-c}/(1+\text{c}))) / (\text{r/np.mean}(\text{hostsSample}))
         #r_values_hosts=np.linspace(0.001,1,len(hostsSample1))
```

#rho_nfw = nfw.dimensionless_mass_density(scaled_radius =r_values_hosts,co

```
In [25]: plt.rc('text', usetex=True)
         plt.rc('font', family='serif')
         r_values =np.linspace(0.001,1,1000)
         # Create a new figure
         fig = plt.figure(figsize=(6,6), dpi=80)
         plot_profile = fig.add_subplot(111)
         plot_profile.set_xscale('log')
         plot_profile.set_yscale('log')
         plot_profile.grid(True)
         #plot_ps.set_xlim(1.0e-5, 1.0e5)
         #plot_profile.set_ylim(0.001, 1e3)
         plot_profile.set_xlabel(r' $ r/R_{vir} $')
         plot_profile.set_ylabel(r'Mass density profile$\rho (r) \;[a.U.]$')
         plot_profile.plot(rbins_midpoints, Density_profileSample1/shell_volumes/fi
         plot_profile.plot(rbins_midpoints, Density_profileSample2/shell_volumes/fi
         #plot_profile.plot(r_values_hosts, rho_nfw, color="black", marker=".",labe
         plot_profile.plot(r_values, NFW(r_values)/4e3, color="black",lw=0.5,label=
         plot_profile.legend(prop={'size':12}, loc="best")
         plt.title("Radial Density Profile")
         # Save figure using 80 dots per inch
         plt.savefig("RadialDensityProfile.pdf",dpi=80)
```



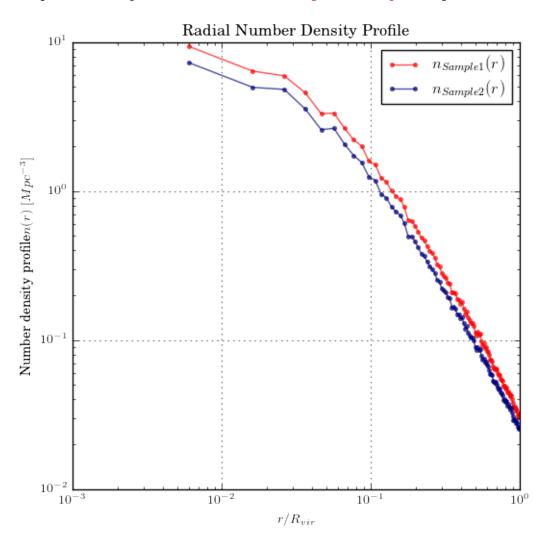
```
In [26]: # Create a new figure
    fig = plt.figure(figsize=(6,6), dpi=80)
    plot_profile = fig.add_subplot(111)
    plot_profile.set_xscale('log')
    plot_profile.set_yscale('log')
    plot_profile.grid(True)

#plot_ps.set_xlim(1.0e-5, 1.0e5)
    #plot_profile.set_ylim(0.001, 1e3)

plot_profile.set_xlabel(r' $ r/R_{vir} $')
    plot_profile.set_ylabel(r'Number density profile$n(r) \; [Mpc^{-3}]$')

plot_profile.plot(rbins_midpoints, MeanNumberDensitySample1, color="red", plot_profile.plot(rbins_midpoints, MeanNumberDensitySample2, color="navy",
```

```
plot_profile.legend(prop={'size':12}, loc="best")
plt.title("Radial Number Density Profile")
# Save figure using 80 dots per inch
plt.savefig("RadialNumberDensityProfile.pdf",dpi=80)
```



4 4) Velocity profiles

In []: #Replace every position and velocity of the subhalos by the the subh

for i in range(0, len(hostsSample1)):

```
for j in range(0, len(subsSample1)):
    if hostsSample1["halo_id"][i] == subsSample1["halo_hostid"][j]:
        sx1[j] = sx1[j]-hx1[i]
        sy1[j] = sy1[j]-hy1[i]
        sz1[j] = sz1[j]-hz1[i]
        svx1[j] = svx1[j]-hvx1[i]
        svy1[j] = svy1[j]-hvy1[i]
        svz1[j] = svz1[j]-hvz1[i]
    else:
        sx1[j] = 10000
        sy1[j] = 10000
        sz1[j] = 10000
        svx1[j] = 10000
        svy1[j] = 10000
        svz1[j] = 10000
for m in range(0, len(subsSample2)):
    if hostsSample1["halo_id"][i] == subsSample2["halo_hostid"][m]:
        sx2[m] = sx2[m]-hx2[i]
        sy2[m] = sy2[m]-hy2[i]
        sz2[m] = sz2[m]-hz2[i]
        svx2[m] = svx2[m]-hvx2[i]
        svy2[m] = svy2[m]-hvy2[i]
        svz2[m] = svz2[m]-hvz2[i]
    else:
        sx1[m] = 10000
        sy1[m] = 10000
        sz1[m] = 10000
        svx1[m] = 10000
        svy1[m] = 10000
        svz1[m] = 10000
```

5 Put every component to zero, when subhalo does not have a corresponding host halo

```
for i in range(0,len(subsSample1)): if indexReturn(subsSample1["halo_hostid"][i])=="NOT-
FOUND": sx1[i] = 0 sy1[i] = 0 sz1[i] = 0 svx1[i] = 0 svy1[i] = 0 svz1[i] = 0
else:
    sx1[i] = sx1[i] - hx1[indexReturn(subsSample1["halo_upid"][i])]
    sy1[i] = sy1[i] - hy1[indexReturn(subsSample1["halo_upid"][i])]
    sz1[i] = sz1[i] - hz1[indexReturn(subsSample1["halo_upid"][i])]
    svx1[i] = svx1[i] - hvx1[indexReturn(subsSample1["halo_upid"][i])]
    svy1[i] = svy1[i]- hvy1[indexReturn(subsSample1["halo_upid"][i])]
    svz1[i] = svz1[i]- hvz1[indexReturn(subsSample1["halo_upid"][i])]
  for k in range(0,len(subsSample2)):
if indexReturn(subsSample1["halo_hostid"][i]) == "NOTFOUND":
    sx2[k] = 0
    sy2[k] = 0
    sz2[k] = 0
    svx2[k] = 0
    svy2[k] = 0
    svz2[k] = 0
else:
    sx2[k] = sx2[k] - hx1[indexReturn(subsSample2["halo_upid"][k])]
    sy2[k] = sy2[k]- hy1[indexReturn(subsSample2["halo_upid"][k])]
    sz2[k] = sz2[k]- hz1[indexReturn(subsSample2["halo_upid"][k])]
    svx2[k] = svx2[k]- hvx1[indexReturn(subsSample2["halo_upid"][k])]
    svy2[k] = svy2[k] - hvy1[indexReturn(subsSample2["halo_upid"][k])]
    svz2[k] = svz2[k] - hvz1[indexReturn(subsSample2["halo_upid"][k])]
In [12]: #Go into spherical coordinates
         r_s1 = np.sqrt(sx1**2+sy1**2+sz1**2)
         r_s2 = np.sqrt(sx2**2+sy2**2+sz2**2)
         vr_s1 = (sx1*svx1+sy1*svy1+sz1*svz1)/r_s1
         vr_s2 = (sx2*svx2+sy2*svy2+sz2*svz2)/r_s2
         vphi_s1 = (svx1*sy1-sx1*svy1) / (sx1**2+sy1**2)
         vphi_s2 = (svx2*sy2-sx2*svy2)/(sx2**2+sy2**2)
         vth_s1 = (sz1*(sx1*svx1+sy1*svy1) - svz1*(sx1**2+sy1**2))/np.sqrt(sx1**2+sy1**2)
         vth_s2 = (sz2*(sx2*svx2+sy2*svy2) - svz2*(sx2**2+sy2**2)) / np.sqrt(sx2**2+sy2**2)
In [14]: #Average the radial velocity profiles
```

```
rbins_normalized = np.linspace(0.001, 1, 100)
         rbins_midpoints = (rbins_normalized[:-1] + rbins_normalized[1:])/2
         aver_vr_s1 = radial_profile_3d(host_pos_sample1, sub_pos_sample1, vr_s1,
                                    rbins_normalized = rbins_normalized,
                                    normalize_rbins_by = hostsSample1['halo_rvir'],
                                    period=halocat.Lbox)
         aver_vr_s2 = radial_profile_3d(host_pos_sample1, sub_pos_sample2, vr_s2,
                                    rbins_normalized = rbins_normalized,
                                    normalize_rbins_by = hostsSample1['halo_rvir'],
                                    period=halocat.Lbox)
         aver_vphi_s1 = radial_profile_3d(host_pos_sample1, sub_pos_sample1, vphi_s
                                    rbins_normalized = rbins_normalized,
                                    normalize_rbins_by = hostsSample1['halo_rvir'],
                                    period=halocat.Lbox)
         aver_vphi_s2 = radial_profile_3d(host_pos_sample1, sub_pos_sample2, vphi_s
                                    rbins_normalized = rbins_normalized,
                                    normalize_rbins_by = hostsSample1['halo_rvir'],
                                    period=halocat.Lbox)
         aver_vth_s1 = radial_profile_3d(host_pos_sample1, sub_pos_sample1, vth_s1,
                                    rbins_normalized = rbins_normalized,
                                    normalize_rbins_by = hostsSample1['halo_rvir'],
                                    period=halocat.Lbox)
         aver_vth_s2 = radial_profile_3d(host_pos_sample1, sub_pos_sample2, vth_s2,
                                    rbins_normalized = rbins_normalized,
                                    normalize_rbins_by = hostsSample1['halo_rvir'],
                                    period=halocat.Lbox)
In [24]: #Normalize by virial velocity
         np.max(sx2)
Out[24]: 0.0
In [16]: # Create a new figure
         fig = plt.figure(figsize=(6,6), dpi=80)
         plot_profile = fig.add_subplot(111)
         plot_profile.set_xscale('log')
         #plot_profile.set_yscale('log')
         plot_profile.grid(True)
```

from halotools.mock_observables import radial_profile_3d

```
#plot_ps.set_xlim(1.0e-5, 1.0e5)
     #plot_profile.set_ylim(0.001, 1e3)
     plot_profile.set_xlabel(r' $ r/R_{vir} $')
     plot_profile.set_ylabel(r'$<v(r)>/V_{vir}$')
     plot_profile.plot(rbins_midpoints, aver_vr_s1, color="red", marker=".", lak
     plot_profile.plot(rbins_midpoints, aver_vphi_s1, color="navy", marker=".",
     #plot_profile.plot(r_values_hosts, rho_nfw, color="black", marker=".",labe
     plot_profile.plot(rbins_midpoints, aver_vth_s1, color="black", lw=0.5, label
     plot_profile.legend(prop={'size':12}, loc="best")
     plt.title("Radial Average Velocity Profile Sample 1")
     # Save figure using 80 dots per inch
     plt.savefig("RadialVelocityProfilesSample1.pdf",dpi=80)
   ValueError
                                              Traceback (most recent call last)
    <ipython-input-16-e09fe14ad7b0> in <module>()
     12 plot_profile.set_ylabel(r'$<v(r)>/V_{vir}$')
---> 14 plot_profile.plot(rbins_midpoints, aver_vr_s1, color="red", marker=".",
     15 plot_profile.plot(rbins_midpoints, aver_vphi_s1, color="navy", marker="
     16 #plot_profile.plot(r_values_hosts, rho_nfw, color="black", marker=".",1
   C:\Users\ThimoPreis\Anaconda3\lib\site-packages\matplotlib\__init__.py in :
   1816
                            warnings.warn(msg % (label_namer, func.__name__),
  1817
                                          RuntimeWarning, stacklevel=2)
-> 1818
                    return func(ax, *args, **kwargs)
   1819
                pre_doc = inner.__doc__
   1820
                if pre_doc is None:
   C:\Users\ThimoPreis\Anaconda3\lib\site-packages\matplotlib\axes\_axes.py in
   1384
                    lines.append(line)
   1385
-> 1386
                self.autoscale_view(scalex=scalex, scaley=scaley)
   1387
                return lines
   1388
```

C:\Users\ThimoPreis\Anaconda3\lib\site-packages\matplotlib\axes_base.py in

```
2166 x1 += delta

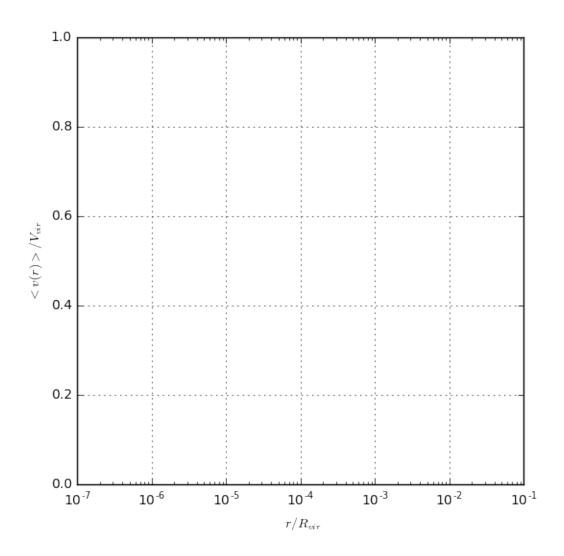
2167 if not _tight:

-> 2168 x0, x1 = xlocator.view_limits(x0, x1)

2169 self.set_xbound(x0, x1)

2170
```

ValueError: Data has no positive values, and therefore can not be log-scale



```
In [ ]: # Create a new figure
        fig = plt.figure(figsize=(6,6), dpi=80)
        plot_profile = fig.add_subplot(111)
        plot_profile.set_xscale('log')
        plot_profile.set_yscale('log')
        plot_profile.grid(True)
        #plot_ps.set_xlim(1.0e-5, 1.0e5)
        #plot_profile.set_ylim(0.001, 1e3)
        plot_profile.set_xlabel(r' $ r/R_{vir} $')
        plot_profile.set_ylabel(r'$<v(r)>/V_{vir}$')
        plot_profile.plot(rbins_midpoints, aver_vr_s1, color="red", marker=".",labe
        plot_profile.plot(rbins_midpoints, aver_vphi_s1, color="navy", marker=".",]
        #plot_profile.plot(r_values_hosts, rho_nfw, color="black", marker=".",label
        plot_profile.plot(rbins_midpoints, aver_vth_s1, color="black", lw=0.5, label=
        plot_profile.legend(prop={'size':12}, loc="best")
        plt.title("Radial Average Velocity Profile Sample 2")
        # Save figure using 80 dots per inch
        plt.savefig("RadialVelocityProfilesSample2.pdf",dpi=80)
In [ ]:
In [52]:
2821926828
1071307
243.125
243.142
0.0174408
In [ ]:
```