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1	Combinatorial optimization 1.1 Sparse max-flow	1 1	1.1 Sparse max-flow	
	1.2 Min-cost max-flow	2		
	1.3 Push-relabel max-flow	2	<pre>// Adjacency list implementation of Dinic's blocking flow algorithm. // This is very fast in practice, and only loses to push-relabel flow.</pre>	
	1.4 Min-cost matching	3		
	1.5 Max bipartite matchine	4	// O(V ^2 E) //	
	1.6 Global min-cut	4	// INPUT: // - graph, constructed using AddEdge()	
	1.7 Graph cut inference	5	// - source and sink //	
	The Graph Car Interested Control of the Control of		// OUTPUT: // - maximum flow value	
2	Geometry	6	<pre>// - To obtain actual flow values, look at edges with capacity > 0 // (zero capacity edges are residual edges).</pre>	
	2.1 Convex hull	6	#include <cstdio></cstdio>	
	2.2 Miscellaneous geometry	6	<pre>#include<vector> #include<queue></queue></vector></pre>	
	2.3 Slow Delaunay triangulation	8	using namespace std; typedef long long LL;	
			struct Edge {	
3	Numerical algorithms	8	int u, v; LL cap, flow;	
	3.1 Number theory (modular, Chinese remainder, linear Diophantine)	8	Eage (Inc a, Inc v, HE cap). a(a), v(v), cap(cap), IIow(o) ()	
	3.2 Systems of linear equations, matrix inverse, determinant	9);	
	3.3 Reduced row echelon form, matrix rank	10	<pre>struct Dinic { int N;</pre>	
	3.4 Fast Fourier transform	10		
	3.5 Simplex algorithm	11	<pre>vector<int> d, pt; Dinic(int N): N(N), E(0), g(N), d(N), pt(N) {}</int></pre>	
4	Graph algorithms	12	<pre>void AddEdge(int u, int v, LL cap) {</pre>	
_	4.1 Floyd's algorithm (C++)		<pre>if (u != v) { E.emplace_back(u, v, cap);</pre>	
	4.2 Fast Dijkstra's algorithm		E.emplace_back(v, u, 0);	
	4.3 Dijkstra's algorithm		g[v].empiace_back(E.Size() - 1),	
	4.4 Strongly connected components		,	
	4.5 Eulerian path		queue <ant> q((s));</ant>	
			d[s] = 0;	
5	Data structures	14		
	5.1 Suffix array	14	<pre>if (u == T) break; for (int k: g[u]) {</pre>	
	5.2 Binary Indexed Tree	14	Edge &e = $E[k]$; if (e.flow < e.cap && d[e.v] > d[e.u] + 1) {	
	5.3 Union-find set	14	<pre>d[e.v] = d[e.u] + 1; q.emplace(e.v);</pre>	
	5.4 KD-tree	15	}	
	5.5 Splay tree	16	return d[T] != N + 1;	
	5.6 Lowest common ancestor	17	LL DFS(int u, int T, LL flow = -1) {	
_	26. 11		<pre>if (u == T flow == 0) return flow; for (int fi = nt[u]: i < g[u] size(): ++i) {</pre>	
6	Miscellaneous	17	Edge &e = $E[g[u][i]]$;	
	6.1 Longest increasing subsequence		<pre>if (d[e.v] == d[e.u] + 1) { LL amt = e.cap - e.flow;</pre>	
	6.2 Dates		<pre>if (flow != -1 && amt > flow) amt = flow; if (LL pushed = DFS(e.v, T, amt)) {</pre>	
	6.3 Prime numbers		e.flow += pushed;	
	6.4 C++ input/output		return pushed;	
	6.5 Knuth-Morris-Pratt	18	3	

```
return 0;
  LL MaxFlow(int S, int T) {
    LL total = 0;
    while (BFS(S, T))
      fill(pt.begin(), pt.end(), 0);
      while (LL flow = DFS(S, T))
        total += flow;
    return total;
};
// The following code solves SPOJ problem #4110: Fast Maximum Flow (FASTFLOW)
  int N, E;
  scanf("%d%d", &N, &E);
  Dinic dinic(N);
  for (int i = 0; i < E; i++)
   int u, v;
    LL cap:
   scanf("%d%d%lld", &u, &v, &cap);
dinic.AddEdge(u - 1, v - 1, cap);
    dinic.AddEdge(v - 1, u - 1, cap);
  printf("%lld\n", dinic.MaxFlow(0, N - 1));
  return 0;
// END CUT
```

1.2 Min-cost max-flow

```
// Implementation of min cost max flow algorithm using adjacency
// matrix (Edmonds and Karp 1972). This implementation keeps track of
// forward and reverse edges separately (so you can set cap[i][j] !=
// cap[j][i]). For a regular max flow, set all edge costs to 0.
// Running time, O(|V|^2) cost per augmentation
      max flow:
                           O(|V|^3) augmentations
       min cost max flow: O(|V|^4 * MAX_EDGE_COST) augmentations
       - graph, constructed using AddEdge()
      - source
      - sink
       - (maximum flow value, minimum cost value)
       - To obtain the actual flow, look at positive values only.
#include <bits/stdc++.h>
using namespace std;
typedef vector<int> VI;
typedef vector<VI> VVI;
typedef long long L;
typedef vector<L> VL;
typedef vector<VL> VVL;
typedef pair<int, int> PII;
typedef vector<PII> VPII;
const L INF = numeric_limits<L>::max() / 4;
struct MinCostMaxFlow {
    int N;
    VVL cap, flow, cost;
    VI found;
    VL dist, pi, width;
    VPII dad;
    MinCostMaxFlow(int N) :
        N(N), cap(N, VL(N)), flow(N, VL(N)), cost(N, VL(N)),
        found(N), dist(N), pi(N), width(N), dad(N) {}
   void AddEdge(int from, int to, L cap, L cost) {
   this->cap[from][to] = cap;
   this->cost[from][to] = cost;
    void Relax(int s, int k, L cap, L cost, int dir) {
```

```
L val = dist[s] + pi[s] - pi[k] + cost;
        if (cap && val < dist[k]) {</pre>
            dist[k] = val;
            dad[k] = make_pair(s, dir);
            width[k] = min(cap, width[s]);
    L Dijkstra(int s, int t) {
        fill(found.begin(), found.end(), false);
        fill(dist.begin(), dist.end(), INF);
        fill(width.begin(), width.end(), 0);
        dist[s] = 0;
        width[s] = INF;
        while (s != -1) {
            int best = -1;
            found[s] = true;
            for (int k = 0; k < N; k++) {
                if (found[k]) continue;
                Relax(s, k, cap[s][k] - flow[s][k], cost[s][k], 1);
                Relax(s, k, flow[k][s], -cost[k][s], -1);
                if (best == -1 || dist[k] < dist[best]) best = k;</pre>
            s = best:
        for (int k = 0; k < N; k++)
           pi[k] = min(pi[k] + dist[k], INF);
        return width[t]:
    pair<L, L> GetMaxFlow(int s, int t) {
        L totflow = 0, totcost = 0;
        while (L amt = Dijkstra(s, t)) {
            totflow += amt;
            for (int x = t; x != s; x = dad[x].first) {
                if (dad[x].second == 1) {
                    flow[dad[x].first][x] += amt;
                    totcost += amt * cost[dad[x].first][x];
                else (
                    flow[x][dad[x].first] -= amt;
                    totcost -= amt * cost[x][dad[x].first];
        return make_pair(totflow, totcost);
};
// BEGIN CUT
// The following code solves UVA problem #10594: Data Flow
int main() {
    int N. M:
    while (scanf("%d%d", &N, &M) == 2) {
        VVL v(M, VL(3));
        for (int i = 0; i < M; i++)
           scanf("%Ld%Ld%Ld", &v[i][0], &v[i][1], &v[i][2]);
        scanf("%Ld%Ld", &D, &K);
        MinCostMaxFlow mcmf (N+1);
        for (int i = 0; i < M; i++)</pre>
            mcmf.AddEdge(int(v[i][0]), int(v[i][1]), K, v[i][2]);
            mcmf.AddEdge(int(v[i][1]), int(v[i][0]), K, v[i][2]);
        mcmf.AddEdge(0, 1, D, 0);
        pair<L, L> res = mcmf.GetMaxFlow(0, N);
        if (res.first == D) {
            printf("%Ld\n", res.second);
        } else {
           printf("Impossible.\n");
    return 0;
// END CUT
```

1.3 Push-relabel max-flow

```
// Adjacency list implementation of FIFO push relabel maximum flow // with the gap relabeling heuristic. This implementation is
```

```
// significantly faster than straight Ford-Fulkerson. It solves
// random problems with 10000 vertices and 1000000 edges in a few
// seconds, though it is possible to construct test cases that
// achieve the worst-case.
// Running time:
       0(|V|^3)
// INPUT:
       - graph, constructed using AddEdge()
       - source
      - sink
// OUTPUT:
       - maximum flow value
        - To obtain the actual flow values, look at all edges with
          capacity > 0 (zero capacity edges are residual edges).
#include <cmath>
#include <vector>
#include <iostream>
#include <queue>
using namespace std:
typedef long long LL;
struct Edge {
  int from, to, cap, flow, index;
  Edge(int from, int to, int cap, int flow, int index) :
    from(from), to(to), cap(cap), flow(flow), index(index) {}
struct PushRelabel {
  int N;
  vector<vector<Edge> > G;
  vector<LL> excess;
  vector<int> dist, active, count;
  queue<int> Q;
  PushRelabel(\textbf{int }N) \ : \ N(N) \, , \ G(N) \, , \ excess(N) \, , \ dist(N) \, , \ active(N) \, , \ count(2*N) \ \{\}
  void AddEdge(int from, int to, int cap) {
   G[from].push_back(Edge(from, to, cap, 0, G[to].size()));
   if (from == to) G[from].back().index++;
    G[to].push_back(Edge(to, from, 0, 0, G[from].size() - 1));
  void Enqueue(int v) {
    if (!active[v] && excess[v] > 0) { active[v] = true; Q.push(v); }
  void Push (Edge &e) {
    int amt = int(min(excess[e.from], LL(e.cap - e.flow)));
    if (dist[e.from] <= dist[e.to] || amt == 0) return;</pre>
    e.flow += amt:
    G[e.to][e.index].flow -= amt;
    excess[e.to] += amt;
    excess[e.from] -= amt;
    Enqueue (e.to);
  void Gap(int k) {
    for (int v = 0; v < N; v++) {
      if (dist[v] < k) continue;
count[dist[v]]--;</pre>
      dist[v] = max(dist[v], N+1);
      count[dist[v]]++;
      Enqueue(v);
  void Relabel(int v) {
    count[dist[v]]--;
    dist[v] = 2*N;
    for (int i = 0; i < G[v].size(); i++)</pre>
     if (G[v][i].cap - G[v][i].flow > 0)
        dist[v] = min(dist[v], dist[G[v][i].to] + 1);
    count[dist[v]]++;
    Enqueue (v);
  void Discharge(int v) {
   for (int i = 0; excess[v] > 0 && i < G[v].size(); i++) Push(G[v][i]);</pre>
    if (excess[v] > 0) {
      if (count[dist[v]] == 1)
        Gap(dist[v]);
        Relabel(v);
```

```
LL GetMaxFlow(int s, int t) {
    count[0] = N-1;
    count[N] = 1;
    dist[s] = N;
    active[s] = active[t] = true;
for (int i = 0; i < G[s].size(); i++) {
      excess[s] += G[s][i].cap;
      Push(G[s][i]);
    while (!Q.empty()) {
      int v = Q.front();
      Q.pop();
      active[v] = false;
      Discharge(v);
    LL totflow = 0;
    for (int i = 0; i < G[s].size(); i++) totflow += G[s][i].flow;</pre>
    return totflow;
};
// BEGIN CUT
// The following code solves SPOJ problem #4110: Fast Maximum Flow (FASTFLOW)
int main() {
 int n. m:
  scanf("%d%d", &n, &m);
  PushRelabel pr(n);
  for (int i = 0; i < m; i++) {
   int a, b, c;
    scanf("%d%d%d", &a, &b, &c);
    if (a == b) continue;
    pr.AddEdge(a-1, b-1, c);
    pr.AddEdge(b-1, a-1, c);
  printf("%Ld\n", pr.GetMaxFlow(0, n-1));
  return 0;
// END CUT
```

1.4 Min-cost matching

```
// Min cost bipartite matching via shortest augmenting paths
// This is an O(n^3) implementation of a shortest augmenting path
// algorithm for finding min cost perfect matchings in dense // graphs. In practice, it solves 1000x1000 problems in around 1
// second.
    cost[i][j] = cost for pairing left node i with right node j
    Lmate[i] = index of right node that left node i pairs with
    Rmate[j] = index of left node that right node j pairs with
// The values in cost[i][j] may be positive or negative. To perform
// maximization, simply negate the cost[][] matrix.
#include <algorithm>
#include <cstdio>
#include <cmath>
#include <vector>
using namespace std:
typedef vector<double> VD;
typedef vector<VD> VVD;
typedef vector<int> VI;
double MinCostMatching(const VVD &cost, VI &Lmate, VI &Rmate) {
  int n = int(cost.size());
  // construct dual feasible solution
  VD u(n);
  VD v(n);
  for (int i = 0; i < n; i++) {
    u[i] = cost[i][0];
    for (int j = 1; j < n; j++) u[i] = min(u[i], cost[i][j]);</pre>
  for (int j = 0; j < n; j++) {
    v[j] = cost[0][j] - u[0];
    for (int i = 1; i < n; i++) v[j] = min(v[j], cost[i][j] - u[i]);</pre>
```

```
// construct primal solution satisfying complementary slackness
Lmate = VI(n, -1);
Rmate = VI(n, -1);
int mated = 0;
for (int i = 0; i < n; i++) {
  for (int j = 0; j < n; j++) {
    if (Rmate[j] != -1) continue;
}</pre>
    if (fabs(cost[i][j] - u[i] - v[j]) < 1e-10) {
      Lmate[i] = j;
Rmate[j] = i;
       mated++;
      break;
VD dist(n);
VI dad(n);
// repeat until primal solution is feasible
while (mated < n) {</pre>
  // find an unmatched left node
  int s = 0:
  while (Lmate[s] != -1) s++;
  // initialize Diikstra
  fill(dad.begin(), dad.end(), -1);
  fill(seen.begin(), seen.end(), 0);
for (int k = 0; k < n; k++)</pre>
    dist[k] = cost[s][k] - u[s] - v[k];
  int j = 0;
  while (true) {
     // find closest
     for (int k = 0; k < n; k++) {
      if (seen[k]) continue;
       if (j == -1 || dist[k] < dist[j]) j = k;</pre>
     seen[j] = 1;
     // termination condition
     if (Rmate[j] == -1) break;
     // relax neighbors
     const int i = Rmate[j];
     for (int k = 0; k < n; k++) {
      if (seen[k]) continue;
       const double new_dist = dist[j] + cost[i][k] - u[i] - v[k];
       if (dist[k] > new_dist) {
         dist[k] = new_dist;
dad[k] = j;
   // update dual variables
  for (int k = 0; k < n; k++)
    if (k == j || !seen[k]) continue;
     const int i = Rmate[k];
     v[k] += dist[k] - dist[j];
    u[i] -= dist[k] - dist[j];
  u[s] += dist[j];
  // augment along path
while (dad[j] >= 0) {
  const int d = dad[j];
    Rmate[i] = Rmate[d];
     Lmate[Rmate[j]] = j;
    j = d;
  Rmate[j] = s;
  Lmate[s] = j;
  mated++;
double value = 0;
for (int i = 0; i < n; i++)</pre>
  value += cost[i][Lmate[i]];
return value:
```

1.5 Max bipartite matchine

```
// This code performs maximum bipartite matching.
// Running time: O(|E| |V|) -- often much faster in practice
      \mathit{INPUT:}\ w[i][j] = \mathit{edge}\ \mathit{between}\ \mathit{row}\ \mathit{node}\ \mathit{i}\ \mathit{and}\ \mathit{column}\ \mathit{node}\ \mathit{j}
     OUTPUT: mr[i] = assignment for row node i, -1 if unassigned mc[j] = assignment for column node j, -1 if unassigned
                function returns number of matches made
#include <vector>
using namespace std;
typedef vector<int> VI;
typedef vector<VI> VVI;
bool FindMatch(int i, const VVI &w, VI &mr, VI &mc, VI &seen) {
  for (int j = 0; j < w[i].size(); j++) {</pre>
     if (w[i][j] && !seen[j]) {
        seen[j] = true;
       if (mc[j] < 0 || FindMatch(mc[j], w, mr, mc, seen)) {
    mr[i] = j;
    mc[j] = i;</pre>
          return true;
  return false;
int BipartiteMatching(const VVI &w, VI &mr, VI &mc) {
  mr = VI(w.size(), -1);
  mc = VI(w[0].size(), -1);
  int ct = 0;
for (int i = 0; i < w.size(); i++) {</pre>
     VI seen(w[0].size());
if (FindMatch(i, w, mr, mc, seen)) ct++;
  return ct;
```

1.6 Global min-cut

```
// Adjacency matrix implementation of Stoer-Wagner min cut algorithm.
// Running time:
// INPUT:
       - graph, constructed using AddEdge()
// OUTPUT:
      - (min cut value, nodes in half of min cut)
#include <cmath>
#include <vector>
#include <iostream>
using namespace std;
typedef vector<int> VI;
typedef vector<VI> VVI;
const int INF = 1000000000;
pair<int, VI> GetMinCut(VVI &weights) {
  int N = weights.size();
  VI used(N), cut, best_cut;
  int best_weight = -1;
  for (int phase = N-1; phase >= 0; phase--) {
    VI w = weights[0];
    VI added = used;
    int prev, last = 0;
    for (int i = 0; i < phase; i++) {</pre>
      prev = last;
last = -1;
      for (int j = 1; j < N; j++)
  if (!added[j] && (last == -1 || w[j] > w[last])) last = j;
      if (i == phase-1) {
        for (int j = 0; j < N; j++) weights[prev][j] += weights[last][j];</pre>
```

```
for (int j = 0; j < N; j++) weights[j][prev] = weights[prev][j];</pre>
        used[last] = true;
        cut.push_back(last);
        if (best_weight == -1 || w[last] < best_weight) {</pre>
          best_cut = cut;
          best_weight = w[last];
      } else {
        for (int j = 0; j < N; j++)
          w[j] += weights[last][j];
        added[last] = true;
  return make_pair(best_weight, best_cut);
// The following code solves UVA problem #10989: Bomb, Divide and Conquer
int main() {
 int N;
 cin >> N;
  for (int i = 0; i < N; i++) {
   int n, m;
    cin >> n >> m;
    VVI weights(n, VI(n));
    for (int j = 0; j < m; j++) {
     int a, b, c;
     cin >> a >> b >> c:
      weights[a-1][b-1] = weights[b-1][a-1] = c;
   pair<int, VI> res = GetMinCut(weights);
cout << "Case #" << i+1 << ": " << res.first << endl;</pre>
// END CUT
```

1.7 Graph cut inference

```
// Special-purpose {0.1} combinatorial optimization solver for
// problems of the following by a reduction to graph cuts:
         \begin{array}{lll} & & & & & \\ & & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & \\ & \\ & & \\ & \\ & \\ & \\ & & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ & \\ 
                       psi_i : {0, 1} --> R
            phi_{ij} : {0, 1} x {0, 1} --> R
// \quad phi_{ij}(0,0) \ + \ phi_{ij}(1,1) \ <= \ phi_{ij}(0,1) \ + \ phi_{ij}(1,0) \quad (\star)
\ensuremath{//} This can also be used to solve maximization problems where the
// direction of the inequality in (*) is reversed.
// INPUT: phi -- a matrix such that phi[i][j][u][v] = phi_{ij}(u, v)
// psi -- a matrix such that psi[i][u] = psi_i(u)
                               x -- a vector where the optimal solution will be stored
 // OUTPUT: value of the optimal solution
// To use this code, create a GraphCutInference object, and call the
// DoInference() method. To perform maximization instead of minimization,
// ensure that #define MAXIMIZATION is enabled.
#include <vector>
#include <iostream>
using namespace std:
typedef vector<int> VI;
typedef vector<VI> VVI;
typedef vector<VVI> VVVI;
typedef vector<VVVI> VVVVI;
const int INF = 1000000000;
  // comment out following line for minimization
#define MAXIMIZATION
struct GraphCutInference {
      int N;
      VVI cap, flow;
       VI reached:
       int Augment(int s, int t, int a) {
            reached[s] = 1;
```

```
if (s == t) return a;
    for (int k = 0; k < N; k++) {
       if (reached[k]) continue;
       if (int aa = min(a, cap[s][k] - flow[s][k])) {
         if (int b = Augment(k, t, aa)) {
           flow[s][k] += b;
           flow[k][s] -= b;
           return b;
      }
    return 0;
  int GetMaxFlow(int s, int t) {
     N = cap.size();
    flow = VVI(N, VI(N));
    reached = VI(N);
    int totflow = 0;
     while (int amt = Augment(s, t, INF)) {
      totflow += amt;
       fill(reached.begin(), reached.end(), 0);
    return totflow:
  int DoInference(const VVVVI &phi, const VVI &psi, VI &x) {
    int M = phi.size();
    cap = VVI(M+2, VI(M+2));
     VI b(M);
    int c = 0;
     for (int i = 0; i < M; i++) {
      b[i] += psi[i][1] - psi[i][0];
       c += psi[i][0];
       for (int j = 0; j < i; j++)
      for (int j = 0, j < 1, j ...,
    b(i) += phi(i)[j](1](1) - phi(i)[j](0)[1];
for (int j = i+1; j < M; j++) {
    cap(i)[j] = phi(i)[j](0](1) + phi(i)[j](1](0) - phi(i)[j](0](0) - phi(i)[j](1](1);
    b(i) += phi(i)[j][1](0) - phi(i)[j](0)(0);</pre>
         c += phi[i][j][0][0];
#ifdef MAXIMIZATION
    for (int i = 0; i < M; i++) {
  for (int j = i+1; j < M; j++)
    cap[i][j] *= -1;
      b[i] *= -1;
    c *= -1;
#endif
    for (int i = 0; i < M; i++) {
      if (b[i] >= 0) {
         cap[M][i] = b[i];
       } else {
         cap[i][M+1] = -b[i];
         c += b[i];
    int score = GetMaxFlow(M, M+1);
    fill(reached.begin(), reached.end(), 0);
    Augment (M, M+1, INF);
    x = VI(M);
    for (int i = 0; i < M; i++) x[i] = reached[i] ? 0 : 1;</pre>
     score += c:
#ifdef MAXIMIZATION
     score \star = -1;
#endif
    return score;
};
int main() {
  // solver for "Cat vs. Dog" from NWERC 2008
  int numcases:
  cin >> numcases:
  for (int caseno = 0; caseno < numcases; caseno++) {
    int c. d. v:
    cin >> c >> d >> v;
     VVVVI phi(c+d, VVVI(c+d, VVI(2, VI(2))));
    VVI psi(c+d, VI(2));
    for (int i = 0; i < v; i++) {
       char p, q;
```

```
int u, v;
  cin >> p >> u >> q >> v;
  u-; v--;
  if (p == 'C') {
    phi[u][c+v][0][0]++;
    phi[c+v][u][0][0]++;
  } else {
    phi[v][c+u][1][1]++;
    phi[c+u][v][1][1]++;
    }
}

GraphCutInference graph;
VI x;
  cout << graph.DoInference(phi, psi, x) << endl;
}
return 0;</pre>
```

2 Geometry

2.1 Convex hull

```
// Compute the 2D convex hull of a set of points using the monotone chain
// algorithm. Eliminate redundant points from the hull if REMOVE_REDUNDANT is
// #defined.
// Running time: O(n log n)
    INPUT: a vector of input points, unordered.
    OUTPUT: a vector of points in the convex hull, counterclockwise, starting
             with bottommost/leftmost point
#include <cstdio>
#include <cassert>
#include <vector>
#include <algorithm>
#include <cmath>
// BEGIN CUT
#include <map>
// END CUT
using namespace std;
#define REMOVE_REDUNDANT
typedef double T;
const T EPS = 1e-7;
struct PT {
  T x, y;
  PT() {}
 PT(T x, T y) : x(x), y(y) {}
bool operator<(const PT &rhs) const { return make pair(y,x) < make pair(rhs.y,rhs.x); }</pre>
  bool operator==(const PT &rhs) const { return make_pair(y,x) == make_pair(rhs.y,rhs.x); }
T cross(PT p, PT q) { return p.x*q.y-p.y*q.x; }
T area2 (PT a, PT b, PT c) { return cross(a,b) + cross(b,c) + cross(c,a); }
bool between (const PT &a, const PT &b, const PT &c) {
  return (fabs(area2(a,b,c)) < EPS && (a.x-b.x)*(c.x-b.x) <= 0 && (a.y-b.y)*(c.y-b.y) <= 0);
#endif
void ConvexHull(vector<PT> &pts) {
 sort(pts.begin(), pts.end());
  pts.erase(unique(pts.begin(), pts.end()), pts.end());
  vector<PT> up, dn;
  for (int i = 0; i < pts.size(); i++) {
    while (up.size() > 1 && area2(up[up.size()-2], up.back(), pts[i]) >= 0) up.pop_back();
    while (dn.size() > 1 && area2(dn[dn.size()-2], dn.back(), pts[i]) <= 0) dn.pop_back();</pre>
    up.push_back(pts[i]);
    dn.push_back(pts[i]);
  pts = dn;
  for (int i = (int) up.size() - 2; i >= 1; i--) pts.push_back(up[i]);
#ifdef REMOVE_REDUNDANT
  if (pts.size() <= 2) return;</pre>
  dn.clear();
  dn.push_back(pts[0]);
  dn.push_back(pts[1]);
  for (int i = 2; i < pts.size(); i++) {</pre>
```

```
if (between(dn[dn.size()-2], dn[dn.size()-1], pts[i])) dn.pop_back();
    dn.push_back(pts[i]);
  if (dn.size() >= 3 && between(dn.back(), dn[0], dn[1])) {
    dn.pop_back();
  pts = dn;
#endif
// BEGIN CUT
// The following code solves SPOJ problem #26: Build the Fence (BSHEEP)
  scanf("%d", &t);
  for (int caseno = 0; caseno < t; caseno++) {</pre>
    int n;
    scanf("%d", &n);
    vector<PT> v(n);
    for (int i = 0; i < n; i++) scanf("%lf%lf", &v[i].x, &v[i].y);</pre>
    vector<PT> h(v);
    map<PT.int> index:
    for (int i = n-1; i >= 0; i--) index[v[i]] = i+1;
    ConvexHull(h):
    double len = 0;
    for (int i = 0; i < h.size(); i++) {</pre>
      double dx = h[i].x - h[(i+1)%h.size()].x;
      double dy = h[i].y - h[(i+1)%h.size()].y;
      len += sqrt (dx*dx+dy*dy);
    if (caseno > 0) printf("\n");
    printf("%.2f\n", len);
    for (int i = 0; i < h.size(); i++) {
  if (i > 0) printf(" ");
      printf("%d", index[h[i]]);
    printf("\n");
// END CUT
```

2.2 Miscellaneous geometry

```
// C++ routines for computational geometry.
#include <iostream>
#include <vector>
#include <cmath>
#include <cassert>
using namespace std;
double INF = 1e100;
double EPS = 1e-12;
  double x, y;
  PT(double x, double y) : x(x), y(y) {}
  PT(const PT &p) : x(p.x), y(p.y)
  PT operator + (const PT &p) const { return PT(x+p.x, y+p.y); }
  PT operator - (const PT &p) const { return PT(x-p.x, y-p.y); }
                              const { return PT(x*c, y*c );
  PT operator * (double c)
 PT operator / (double c)
                              const { return PT(x/c, y/c ); }
double dot (PT p, PT q)
                         { return p.x*q.x+p.y*q.y; }
double dist2(PT p, PT q)
                          { return dot(p-q,p-q); }
double cross(PT p, PT q) { return p.x*q.y-p.y*q.x; }
ostream &operator<<(ostream &os, const PT &p)
 return os << "(" << p.x << "," << p.y << ")";
// rotate a point CCW or CW around the origin
PT RotateCCW90 (PT p) { return PT (-p.y,p.x); }
PT RotateCW90(PT p)
                      { return PT(p.y,-p.x); }
PT RotateCCW(PT p, double t) {
 return PT(p.x*cos(t)-p.y*sin(t), p.x*sin(t)+p.y*cos(t));
// project point c onto line through a and b
// assuming a != b
```

```
PT ProjectPointLine(PT a, PT b, PT c) {
  return a + (b-a) *dot(c-a, b-a) /dot(b-a, b-a);
// project point c onto line segment through a and b
PT ProjectPointSegment (PT a, PT b, PT c) {
  double r = dot(b-a, b-a);
  if (fabs(r) < EPS) return a;</pre>
  r = dot(c-a, b-a)/r;
  if (r < 0) return a;
  if (r > 1) return b;
  return a + (b-a) *r;
// compute distance from c to segment between a and b
double DistancePointSegment (PT a, PT b, PT c) {
  return sqrt(dist2(c, ProjectPointSegment(a, b, c)));
// compute distance between point (x,y,z) and plane ax+by+cz=d
double DistancePointPlane(double x, double y, double z,
                           double a, double b, double c, double d)
  return fabs(a*x+b*y+c*z-d)/sqrt(a*a+b*b+c*c);
// determine if lines from a to b and c to d are parallel or collinear
bool LinesParallel(PT a, PT b, PT c, PT d) {
  return fabs(cross(b-a, c-d)) < EPS;
bool LinesCollinear (PT a, PT b, PT c, PT d) {
  return LinesParallel(a, b, c, d)
      && fabs(cross(a-b, a-c)) < EPS
      && fabs(cross(c-d, c-a)) < EPS;
// determine if line segment from a to b intersects with
// line segment from c to d
bool SegmentsIntersect(PT a, PT b, PT c, PT d) {
 if (LinesCollinear(a, b, c, d)) {
   if (dist2(a, c) < EPS || dist2(a, d) < EPS ||
      dist2(b, c) < EPS || dist2(b, d) < EPS) return true;</pre>
    if (dot(c-a, c-b) > 0 && dot(d-a, d-b) > 0 && dot(c-b, d-b) > 0)
      return false;
    return true:
  if (cross(d-a, b-a) * cross(c-a, b-a) > 0) return false;
  if (cross(a-c, d-c) * cross(b-c, d-c) > 0) return false;
  return true:
// compute intersection of line passing through a and b \,
// with line passing through c and d, assuming that unique
// intersection exists; for segment intersection, check if
// segments intersect first
PT ComputeLineIntersection(PT a, PT b, PT c, PT d) {
 b=b-a; d=c-d; c=c-a;
  assert(dot(b, b) > EPS && dot(d, d) > EPS);
  return a + b*cross(c, d)/cross(b, d);
// compute center of circle given three points
PT ComputeCircleCenter(PT a, PT b, PT c) {
  b = (a+b)/2;
  c = (a + c) / 2;
  return ComputeLineIntersection(b, b+RotateCW90(a-b), c, c+RotateCW90(a-c));
// determine if point is in a possibly non-convex polygon (by William
// Randolph Franklin); returns 1 for strictly interior points, 0 for // strictly exterior points, and 0 or 1 for the remaining points.
// Note that it is possible to convert this into an *exact* test using
// integer arithmetic by taking care of the division appropriately
// (making sure to deal with signs properly) and then by writing exact
// tests for checking point on polygon boundary
bool PointInPolygon(const vector<PT> &p, PT q) {
  bool c = 0;
  for (int i = 0; i < p.size(); i++) {</pre>
    int j = (i+1)%p.size();
    if ((p[i].y \le q.y \&\& q.y < p[j].y ||
      p[j].y \le q.y && q.y < p[i].y) &&
      q.x < p[i].x + (p[j].x - p[i].x) * (q.y - p[i].y) / (p[j].y - p[i].y))
      c = !c;
  return c:
   determine if point is on the boundary of a polygon
bool PointOnPolygon(const vector<PT> &p, PT q) {
  for (int i = 0; i < p.size(); i++)</pre>
    if (dist2(ProjectPointSegment(p[i], p[(i+1)%p.size()], q), q) < EPS)</pre>
```

```
return true;
    return false;
// compute intersection of line through points a and b with
// circle centered at c with radius r >
vector<PT> CircleLineIntersection(PT a, PT b, PT c, double r) {
  vector<PT> ret;
  b = b-a;
  a = a-c;
  double A = dot(b, b);
double B = dot(a, b);
double C = dot(a, a) - r*r;
  double D = B*B - A*C;
  if (D < -EPS) return ret;</pre>
  ret.push_back(c+a+b*(-B+sqrt(D+EPS))/A);
  if (D > EPS)
    ret.push_back(c+a+b*(-B-sqrt(D))/A);
  return ret:
// compute intersection of circle centered at a with radius r
// with circle centered at b with radius R
vector<PT> CircleCircleIntersection(PT a, PT b, double r, double R) {
  vector<PT> ret;
  double d = sqrt(dist2(a, b));
  if (d > r+R || d+min(r, R) < max(r, R)) return ret;
double x = (d*d-R*R+r*r)/(2*d);</pre>
  double v = sgrt(r*r-x*x):
  PT v = (b-a)/d;
  ret.push_back(a+v*x + RotateCCW90(v)*y);
  if(y > 0)
    ret.push_back(a+v*x - RotateCCW90(v)*y);
  return ret;
// This code computes the area or centroid of a (possibly nonconvex)
// polygon, assuming that the coordinates are listed in a clockwise or
// counterclockwise fashion. Note that the centroid is often known as // the "center of gravity" or "center of mass".
double ComputeSignedArea(const vector<PT> &p) {
  double area = 0:
  for(int i = 0; i < p.size(); i++) {</pre>
    int j = (i+1) % p.size();
    area += p[i].x*p[j].y - p[j].x*p[i].y;
  return area / 2.0;
double ComputeArea(const vector<PT> &p) {
  return fabs(ComputeSignedArea(p));
PT ComputeCentroid(const vector<PT> &p)
  PT c(0,0):
  double scale = 6.0 * ComputeSignedArea(p);
  for (int i = 0; i < p.size(); i++) {</pre>
    int j = (i+1) % p.size();
    c = c + (p[i]+p[j])*(p[i].x*p[j].y - p[j].x*p[i].y);
  return c / scale;
 // tests whether or not a given polygon (in CW or CCW order) is simple
bool IsSimple(const vector<PT> &p)
  for (int i = 0; i < p.size(); i++) {</pre>
    for (int k = i+1; k < p.size(); k++) {
      int j = (i+1) % p.size();
int l = (k+1) % p.size();
      if (i == 1 || j == k) continue;
if (SegmentsIntersect(p[i], p[j], p[k], p[l]))
        return false;
  return true;
int main() {
  // expected: (-5,2)
  cerr << RotateCCW90(PT(2,5)) << endl;</pre>
  // expected: (5,-2)
  cerr << RotateCW90(PT(2,5)) << endl;</pre>
  // expected: (-5,2)
  cerr << RotateCCW(PT(2,5),M_PI/2) << endl;</pre>
  // expected: (5,2)
  cerr << ProjectPointLine(PT(-5,-2), PT(10,4), PT(3,7)) << endl;</pre>
  // expected: (5,2) (7.5,3) (2.5,1)
```

```
cerr << ProjectPointSegment(PT(-5,-2), PT(10,4), PT(3,7)) << " "
     << ProjectPointSegment(PT(7.5,3), PT(10,4), PT(3,7)) << " "
     << ProjectPointSegment(PT(-5,-2), PT(2.5,1), PT(3,7)) << endl;
cerr << DistancePointPlane(4,-4,3,2,-2,5,-8) << endl;</pre>
// expected: 1 0 1
cerr << LinesParallel(PT(1,1), PT(3,5), PT(2,1), PT(4,5)) << " "
     << LinesParallel(PT(1,1), PT(3,5), PT(2,0), PT(4,5)) << " "
     << LinesParallel(PT(1,1), PT(3,5), PT(5,9), PT(7,13)) << endl;
cerr << SegmentsIntersect(PT(0,0), PT(2,4), PT(3,1), PT(-1,3)) << " "
     << SegmentsIntersect(PT(0,0), PT(2,4), PT(4,3), PT(0,5)) << " "
     << SegmentsIntersect(PT(0,0), PT(2,4), PT(2,-1), PT(-2,1)) << " "
     << SegmentsIntersect(PT(0,0), PT(2,4), PT(5,5), PT(1,7)) << endl;
// expected: (1.2)
cerr << ComputeLineIntersection(PT(0,0), PT(2,4), PT(3,1), PT(-1,3)) << endl;
// expected: (1.1)
cerr << ComputeCircleCenter(PT(-3,4), PT(6,1), PT(4,5)) << endl;
v.push_back(PT(0,0));
v.push_back(PT(5,0));
v.push_back(PT(5,5));
v.push_back(PT(0,5));
// expected: 1 1 1 0 0
cerr << PointInPolygon(v, PT(2,2)) << " "
     << PointInPolygon(v, PT(2,0)) << " "
     << PointInPolygon(v, PT(0,2)) << " "
     << PointInPolygon(v, PT(5,2)) << " "
     << PointInPolygon(v, PT(2,5)) << endl;
// expected: 0 1 1 1 1
cerr << PointOnPolygon(v, PT(2,2)) << " "</pre>
     << PointOnPolygon(v, PT(2,0)) << " "
     << PointOnPolygon(v, PT(0,2)) << " "
     << PointOnPolygon(v, PT(5,2)) << " "
     << PointOnPolygon(v, PT(2,5)) << endl;
// expected: (1,6)
             (5,4) (4,5)
             blank line
             (4,5) (5,4)
             hlank line
             (4.5) (5.4)
vector<PT> u = CircleLineIntersection(PT(0,6), PT(2,6), PT(1,1), 5);
for (int i = 0; i < u.size(); i++) cerr << u[i] << " "; cerr << endl;</pre>
u = CircleLineIntersection(PT(0,9), PT(9,0), PT(1,1), 5);

for (int i = 0; i < u.size(); i++) cerr << u[i] << " "; cerr << endl;
u = CircleCircleIntersection(PT(1,1), PT(10,10), 5, 5);
for (int i = 0; i < u.size(); i++) cerr << u[i] << " "; cerr << endl;
u = CircleCircleIntersection(PT(1,1), PT(8,8), 5, 5);
for (int i = 0; i < u.size(); i++) cerr << u[i] << " "; cerr << endl;</pre>
u = CircleCircleIntersection(PT(1,1), PT(4.5,4.5), 10, sqrt(2.0)/2.0);
for (int i = 0; i < u.size(); i++) cerr << u[i] << " "; cerr << endl;
// area should be 5.0 
// centroid should be (1.1666666, 1.166666) 
PT pa[] = { PT(0,0), PT(5,0), PT(1,1), PT(0,5) };
vector<PT> p(pa, pa+4);
PT c = ComputeCentroid(p);
cerr << "Area: " << ComputeArea(p) << endl;
cerr << "Centroid: " << c << endl;
return 0;
```

2.3 Slow Delaunay triangulation

```
// Slow but simple Delaunay triangulation. Does not handle // degenerate cases (from O'Rourke, Computational Geometry in C) // Running time: O(n^4) // // INPUT: x[] = x-coordinates
```

```
vfl = v-coordinates
               triples = a vector containing m triples of indices
                           corresponding to triangle vertices
#include<vector>
using namespace std;
typedef double T;
struct triple {
    int i, j, k;
    triple() {}
    triple(int i, int j, int k) : i(i), j(j), k(k) {}
1:
vector<triple> delaunayTriangulation(vector<T>& x, vector<T>& y) {
         vector<T> z(n);
         vector<triple> ret;
         for (int i = 0; i < n; i++)
              z[i] = x[i] * x[i] + y[i] * y[i];
         for (int i = 0; i < n-2; i++)
              for (int j = i+1; j < n; j++) {
   for (int k = i+1; k < n; k++) {</pre>
                       if (j == k) continue;
                       double xn = (y[j]-y[i])*(z[k]-z[i]) - (y[k]-y[i])*(z[j]-z[i]);
double yn = (x[k]-x[i])*(z[j]-z[i]) - (x[j]-x[i])*(z[k]-z[i]);
                       double zn = (x[j]-x[i])*(y[k]-y[i]) - (x[k]-x[i])*(y[j]-y[i]);
                       bool flag = zn < 0;
                        for (int m = 0; flag && m < n; m++)</pre>
                            flag = flag && ((x[m]-x[i])*xn +
                                               (z[m]-z[i])*zn <= 0);
                       if (flag) ret.push_back(triple(i, j, k));
         return ret;
int main()
    T xs[]={0, 0, 1, 0.9};
T ys[]={0, 1, 0, 0.9};
    vector<T> x(&xs[0], &xs[4]), y(&ys[0], &ys[4]);
vector<triple> tri = delaunayTriangulation(x, y);
    for(i = 0; i < tri.size(); i++)</pre>
         printf("%d %d %d\n", tri[i].i, tri[i].j, tri[i].k);
    return 0:
```

3 Numerical algorithms

3.1 Number theory (modular, Chinese remainder, linear Diophantine)

```
// This is a collection of useful code for solving problems that
// involve modular linear equations. Note that all of the
// algorithms described here work on nonnegative integers.
#include <iostream>
#include <vector>
#include <algorithm>
using namespace std;
typedef vector<int> VI;
typedef pair<int, int> PII;
// return a % b (positive value)
int mod(int a, int b) {
    return ((a%b) + b) % b;
}
// computes gcd(a,b)
```

```
int gcd(int a, int b) {
        while (b) { int t = a%b; a = b; b = t; }
// computes lcm(a,b)
int lcm(int a, int b) {
        return a / gcd(a, b) *b;
// (a^b) mod m via successive squaring
int powermod(int a, int b, int m)
        int ret = 1:
        while (b)
                 if (b & 1) ret = mod(ret*a, m);
                 a = mod(a*a, m);
        return ret;
// returns g = gcd(a, b); finds x, y such that d = ax + by
int extended_euclid(int a, int b, int &x, int &y) {
        int xx = y = 0;
        int yy = x = 1;
        while (b) {
                 int q = a / b;
                 int t = b; b = a%b; a = t;
                 t = xx; xx = x - q*xx; x = t;
                 t = yy; yy = y - q*yy; y = t;
        return a;
// finds all solutions to ax = b \pmod{n}
VI modular_linear_equation_solver(int a, int b, int n) {
        int x, y;
        VI ret;
        int g = extended_euclid(a, n, x, y);
        if (!(b%g)) {
                x = mod(x*(b / g), n);
for (int i = 0; i < g; i++)
                          ret.push_back(mod(x + i*(n / g), n));
// computes b such that ab = 1 \pmod{n}, returns -1 on failure
int mod_inverse(int a, int n) {
        int x, y;
        int g = extended_euclid(a, n, x, y);
        if (q > 1) return -1;
        return mod(x, n);
// Chinese remainder theorem (special case): find z such that
// z % m1 = r1, z % m2 = r2. Here, z is unique modulo M = lcm(m1, m2).
// Return (z, M). On failure, M = -1.
PII chinese_remainder_theorem(int m1, int r1, int m2, int r2) {
        int g = extended_euclid(m1, m2, s, t);
        if (r1%g != r2%g) return make_pair(0, -1);
        return make_pair(mod(s*r2*m1 + t*r1*m2, m1*m2) / g, m1*m2 / g);
// Chinese remainder theorem: find z such that
// z \circledast m[i] = r[i] for all i. Note that the solution is // unique modulo M = lcm_i (m[i]). Return (z, M). On // failure, M = -1. Note that we do not require the a[i]'s
// to be relatively prime.
PII chinese_remainder_theorem(const VI &m, const VI &r) {
        PII ret = make_pair(r[0], m[0]);
        for (int i = 1; i < m.size(); i++) {
    ret = chinese_remainder_theorem(ret.second, ret.first, m[i], r[i]);</pre>
                 if (ret.second == -1) break;
        return ret;
// computes x and y such that ax + by = c
// returns whether the solution exists
bool linear_diophantine(int a, int b, int c, int &x, int &y) {
        if (!a && !b)
                 if (c) return false;
                 x = 0; y = 0;
                 return true;
        if (!a)
```

```
if (c % b) return false;
                  x = 0; y = c / b;
                  return true;
        if (!b)
                  if (c % a) return false;
                  x = c / a; y = 0;
                  return true;
        int g = gcd(a, b);
        if (c % g) return false;
        x = c / g * mod_inverse(a / g, b / g);
        y = (c - a*x) / b;
        return true:
int main() {
        // expected: 2
        cout << gcd(14, 30) << endl;
         // expected: 2 -2 1
        int x, y;
int g = extended_euclid(14, 30, x, y);
cout << g << " " << x << " " << y << endl;</pre>
         // expected: 95 451
        VI sols = modular_linear_equation_solver(14, 30, 100);
        for (int i = 0; i < sols.size(); i++) cout << sols[i] << " ";</pre>
        cout << endl;
         // expected: 8
        cout << mod_inverse(8, 9) << endl;</pre>
         // expected: 23 105
                      11 12
        PII ret = chinese_remainder_theorem(VI({ 3, 5, 7 }), VI({ 2, 3, 2 })); cout << ret.first << " " << ret.second << endl;
        ret = chinese_remainder_theorem(VI({ 4, 6 }), VI({ 3, 5 }));
cout << ret.first << " " << ret.second << endl;
        return 0;
```

3.2 Systems of linear equations, matrix inverse, determinant

```
// Gauss-Jordan elimination with full pivoting.
// Uses:
    (1) solving systems of linear equations (AX=B)
    (2) inverting matrices (AX=I)
    (3) computing determinants of square matrices
// Running time: O(n^3)
// INPUT: a[][] = an nxn matrix
             b[][] = an nxm matrix
// OUTPUT: X
                  = an nxm matrix (stored in b[][])
             A^{-1} = an \ nxn \ matrix \ (stored in a[][])
             returns determinant of a[][]
#include <iostream>
#include <vector>
#include <cmath>
using namespace std;
const double EPS = 1e-10;
typedef vector<int> VI;
typedef double T;
typedef vector<T> VT;
typedef vector<VT> VVT;
T GaussJordan(VVT &a, VVT &b) {
 const int n = a.size();
const int m = b[0].size();
  VI irow(n), icol(n), ipiv(n);
  T \det = 1;
  for (int i = 0; i < n; i++) {
```

```
int pj = -1, pk = -1;
for (int j = 0; j < n; j++) if (!ipiv[j])
  for (int k = 0; k < n; k++) if (!ipiv[k])</pre>
       if (pj == -1 || fabs(a[j][k]) > fabs(a[pj][pk])) { pj = j; pk = k; }
  if (fabs(a[pj][pk]) < EPS) { cerr << "Matrix is singular." << endl; exit(0); }</pre>
  swap(a[pj], a[pk]);
  swap(b[pj], b[pk]);
  if (pj != pk) det *= -1;
  irow[i] = pj;
icol[i] = pk;
   \begin{array}{ll} T \ c = 1.0 \ / \ a[pk][pk]; \\ det \ \star = \ a[pk][pk]; \\ a[pk][pk] = 1.0; \\ \ for \ (int \ p = 0; \ p < n; \ p++) \ a[pk][p] \ \star = c; \end{array} 
  for (int p = 0; p < m; p++) b[pk][p] *= c;
  for (int p = 0; p < n; p++) if (p != pk) {
    c = a[p][pk];
     for (int q = 0; q < n; q++) a[p][q] -= a[pk][q] * c;
for (int q = 0; q < m; q++) b[p][q] -= b[pk][q] * c;
for (int p = n-1; p >= 0; p--) if (irow[p] != icol[p]) {
  for (int k = 0; k < n; k++) swap(a[k][irow[p]], a[k][icol[p]]);</pre>
return det:
const int n = 4;
const int m = 2;
double A[n][n] = \{ \{1,2,3,4\}, \{1,0,1,0\}, \{5,3,2,4\}, \{6,1,4,6\} \};
double B[n][m] = \{ \{1,2\}, \{4,3\}, \{5,6\}, \{8,7\} \};
VVT a(n), b(n);
for (int i = 0; i < n; i++) {
   a[i] = VT(A[i], A[i] + n);
   b[i] = VT(B[i], B[i] + m);</pre>
double det = GaussJordan(a, b);
// expected: 60
cout << "Determinant: " << det << endl;
// expected: -0.233333 0.166667 0.133333 0.0666667
                 0.166667 0.166667 0.333333 -0.333333
                  0.233333 0.833333 -0.133333 -0.0666667
                 0.05 -0.75 -0.1 0.2
cout << "Inverse: " << endl;
for (int i = 0; i < n; i++) {
  for (int j = 0; j < n; j++)
    cout << a[i][j] << ' ';</pre>
  cout << endl;
// expected: 1.63333 1.3
                 -0.166667 0.5
                  2.36667 1.7
                  -1.85 -1.35
cout << "Solution: " << endl;</pre>
for (int i = 0; i < n; i++)</pre>
  for (int j = 0; j < m; j++)
  cout << b[i][j] << ' ';</pre>
  cout << endl;
```

3.3 Reduced row echelon form, matrix rank

```
// Reduced row echelon form via Gauss-Jordan elimination
// with partial pivoting. This can be used for computing
// the rank of a matrix.
//
// Running time: O(n^3)
//
// INPUT: a[][] = an nxm matrix
//
// OUTPUT: rref[][] = an nxm matrix (stored in a[][])
    returns rank of a[][]

#include <iostream>
#include <vector>
#include <cmath>
```

```
using namespace std;
const double EPSILON = 1e-10;
typedef double T;
typedef vector<T> VT;
typedef vector<VT> VVT;
int rref(VVT &a) {
 int n = a.size();
  int m = a[0].size();
  int \mathbf{r} = 0;
  for (int c = 0; c < m && r < n; c++) {
    int j = r;
for (int i = r + 1; i < n; i++)</pre>
      if (fabs(a[i][c]) > fabs(a[j][c])) j = i;
    if (fabs(a[j][c]) < EPSILON) continue;</pre>
    swap(a[j], a[r]);
    T s = 1.0 / a[r][c];
    for (int j = 0; j < m; j++) a[r][j] *= s;
for (int i = 0; i < n; i++) if (i != r) {</pre>
       T t = a[i][c];
       for (int j = 0; j < m; j++) a[i][j] -= t * a[r][j];</pre>
    r++;
  return r:
int main() {
  const int n = 5, m = 4;
  double A[n][m] = {
    {16, 2, 3, 13},
    { 5, 11, 10, 8},
    { 9, 7, 6, 12},
    { 4, 14, 15, 1},
    {13, 21, 21, 13}};
  VVT a(n);
for (int i = 0; i < n; i++)</pre>
    a[i] = VT(A[i], A[i] + m);
  int rank = rref(a);
  // expected: 3
  cout << "Rank: " << rank << endl;</pre>
  // expected: 1 0 0 1
               0 1 0 3
                 0 0 1 -3
                 0 0 0 3.10862e-15
                0 0 0 2.22045e-15
  cout << "rref: " << endl;
  for (int i = 0; i < 5; i++) {
  for (int j = 0; j < 4; j++)
    cout << a[i][j] << ' ';
    cout << endl;
```

3.4 Fast Fourier transform

```
#include <cassert>
#include <cstdio>
#include <cmath>
struct cpx
  cpx(){}
  cpx (double aa):a(aa),b(0){}
  cpx(double aa, double bb):a(aa),b(bb){}
  double a;
  double b;
  double modsq(void) const
    return a * a + b * b;
  cpx bar(void) const
    return cpx(a, -b);
};
cpx operator + (cpx a, cpx b)
  return cpx(a.a + b.a, a.b + b.b);
```

```
cpx operator *(cpx a, cpx b)
  return cpx(a.a * b.a - a.b * b.b, a.a * b.b + a.b * b.a);
cpx operator / (cpx a, cpx b)
  cpx r = a * b.bar();
  return cpx(r.a / b.modsq(), r.b / b.modsq());
cpx EXP (double theta)
  return cpx(cos(theta), sin(theta));
const double two_pi = 4 * acos(0);
// in:
           input array
// out:
          output array
// step: {SET TO 1} (used internally)
// size: length of the input/output {MUST BE A POWER OF 2}
// dir: either plus or minus one (direction of the FFT)
// RESULT: out[k] = \sum_{j=0}^{size - 1} in[j] * exp(dir * 2pi * i * j * k / size)
void FFT(cpx *in, cpx *out, int step, int size, int dir)
  if(size < 1) return;</pre>
  if(size == 1)
    out[0] = in[0];
    return;
  FFT(in, out, step * 2, size / 2, dir);
  FFT(in + step, out + size / 2, step * 2, size / 2, dir);
  for(int i = 0; i < size / 2; i++)
    cpx even = out[i];
    cpx odd = out[i + size / 2];
    out[i] = even + EXP(dir * two_pi * i / size) * odd;
out[i + size / 2] = even + EXP(dir * two_pi * (i + size / 2) / size) * odd;
// Usage:
// f[0...N-1] and g[0..N-1] are numbers
// Want to compute the convolution h, defined by
// h[n] = sum \text{ of } f[k]g[n-k] \ (k = 0, ..., N-1).
// Here, the index is cyclic; f[-1] = f[N-1], f[-2] = f[N-2], etc.
// Let F[0...N-1] be FFT(f), and similarly, define G and H.
// The convolution theorem says H[n] = F[n]G[n] (element-wise product).
// To compute h[] in O(N \log N) time, do the following:
   1. Compute F and G (pass dir = 1 as the argument).
// 2. Get H by element-wise multiplying F and G.
    3. Get h by taking the inverse FFT (use dir = -1 as the argument) and *dividing by N*. DO NOT FORGET THIS SCALING FACTOR.
int main (void)
  printf("If rows come in identical pairs, then everything works.\n");
  cpx a[8] = \{0, 1, cpx(1,3), cpx(0,5), 1, 0, 2, 0\};
  cpx b[8] = \{1, cpx(0,-2), cpx(0,1), 3, -1, -3, 1, -2\};
  cpx A[8];
  cpx B[8];
  FFT(a, A, 1, 8, 1);
  FFT(b, B, 1, 8, 1);
  for(int i = 0; i < 8; i++)
    printf("%7.21f%7.21f", A[i].a, A[i].b);
  printf("\n");
  for (int i = 0; i < 8; i++)
    cpx Ai(0,0);
    for (int j = 0; j < 8; j++)
      Ai = Ai + a[j] * EXP(j * i * two_pi / 8);
    printf("%7.21f%7.21f", Ai.a, Ai.b);
  printf("\n");
  cpx AB[8]:
  for (int i = 0; i < 8; i++)
   AB[i] = A[i] * B[i];
  cpx aconvb[8];
  FFT (AB, aconvb, 1, 8, -1);
  for (int i = 0; i < 8; i++)
     aconvb[i] = aconvb[i] / 8;
  for (int i = 0; i < 8; i++)
```

```
{
    printf("%7.21f%7.21f", aconvb[i].a, aconvb[i].b);
}
printf("\n");
for(int i = 0; i < 8; i++)
{
    cpx aconvbi(0,0);
    for(int j = 0; j < 8; j++)
    {
        aconvbi = aconvbi + a[j] * b[(8 + i - j) % 8];
    }
    printf("%7.21f%7.21f", aconvbi.a, aconvbi.b);
}
printf("\n");
return 0;
}</pre>
```

3.5 Simplex algorithm

```
// Two-phase simplex algorithm for solving linear programs of the form
        maximize
        subject to Ax <= b
                        x >= 0
// INPUT: A -- an m x n matrix
           b -- an m-dimensional vector
            c -- an n-dimensional vector
            x -- a vector where the optimal solution will be stored
 // OUTPUT: value of the optimal solution (infinity if unbounded
             above, nan if infeasible)
// To use this code, create an LPSolver object with A, b, and c as
// arguments. Then, call Solve(x).
#include <iostream>
#include <iomanip>
#include <vector>
#include <cmath>
#include <limits>
using namespace std;
typedef long double DOUBLE;
typedef vector<DOUBLE> VD;
typedef vector<VD> VVD;
typedef vector<int> VI;
const DOUBLE EPS = 1e-9;
struct LPSolver {
  int m, n;
  VI B, N;
  VVD D
  LPSolver(const VVD &A, const VD &b, const VD &c) :
    m(b.size()), n(c.size()), N(n + 1), B(m), D(m + 2, VD(n + 2)) {
    for (int i = 0; i < m; i++) for (int j = 0; j < n; j++) D[i][j] = A[i][j];
for (int i = 0; i < m; i++) { B[i] = n + i; D[i][n] = -1; D[i][n + 1] = b[i]; }</pre>
     for (int j = 0; j < n; j++) { N[j] = j; D[m][j] = -c[j]; }</pre>
     N[n] = -1; D[m + 1][n] = 1;
  void Pivot(int r, int s) {
    double inv = 1.0 / D[r][s];
for (int i = 0; i < m + 2; i++) if (i != r)
    for (int j = 0; j < n + 2; j++) if (j != s)
    D[i][j] -= D[r][j] * D[i][s] * inv;</pre>
    for (int j = 0; j < n + 2; j++) if (j != s) D[r][j] *= inv;
for (int i = 0; i < m + 2; i++) if (i != r) D[i][s] *= -inv;
    D[r][s] = inv;
swap(B[r], N[s]);
  bool Simplex(int phase) {
     int x = phase == 1 ? m + 1 : m;
     while (true) {
       int s = -1;
       for (int j = 0; j <= n; j ++) {
    if (phase == 2 && N[j] == -1) continue;
    if (s == -1 || D[x][j] < D[x][s] || D[x][j] == D[x][s] && N[j] < N[s]) s = j;
       if (D[x][s] > -EPS) return true;
       for (int i = 0; i < m; i++) {
```

```
if (D[i][s] < EPS) continue;</pre>
        if (r == -1 || D[i][n + 1] / D[i][s] < D[r][n + 1] / D[r][s] ||</pre>
           (D[i][n+1] / D[i][s]) == (D[r][n+1] / D[r][s]) && B[i] < B[r]) r = i;
      Pivot(r, s);
  DOUBLE Solve(VD &x) {
    int r = 0;
    for (int i = 1; i < m; i++) if (D[i][n + 1] < D[r][n + 1]) r = i;
    if (D[r][n + 1] < -EPS) {
      Pivot(r, n);
      if (!Simplex(1) || D[m + 1][n + 1] < -EPS) return -numeric_limits<DOUBLE>::infinity();
      for (int i = 0; i < m; i++) if (B[i] == -1) {
        int s = -1;
        for (int j = 0; j \le n; j++)
          if (s == -1 || D[i][j] < D[i][s] || D[i][j] == D[i][s] && N[j] < N[s]) s = j;
    if (!Simplex(2)) return numeric_limits<DOUBLE>::infinity();
    for (int i = 0; i < m; i++) if (B[i] < n) x[B[i]] = D[i][n + 1];
    return D[m][n + 1];
1:
int main() {
  const int n = 3;
  DOUBLE _A[m][n] =
    { 6, -1, 0 },
    \{-1, -5, 0\},
    \{-1, -5, -1\}
  DOUBLE _b[m] = { 10, -4, 5, -5 };

DOUBLE _c[n] = { 1, -1, 0 };
  VVD A(m);
  VD b(_b, _b + m);
VD c(_c, _c + n);
  for (int i = 0; i < m; i++) A[i] = VD(_A[i], _A[i] + n);</pre>
  LPSolver solver(A, b, c);
  DOUBLE value = solver.Solve(x):
  cerr << "VALUE: " << value << endl; // VALUE: 1.29032
  cerr << "SOLUTION:"; // SOLUTION: 1.74194 0.451613 1
  for (size_t i = 0; i < x.size(); i++) cerr << " " << x[i];</pre>
  cerr << endl:
  return 0:
```

4 Graph algorithms

4.1 Floyd's algorithm (C++)

```
#include <bits/stdc++.h>
using namespace std;

typedef double T;
typedef vector<T> VT;
typedef vector<T> VT;
typedef vector<VT> VVT;

typedef vector<VT> VVI;

typedef vector<VI> VVI;

// This function runs the Floyd-Warshall algorithm for all-pairs
// shortest paths. Also handles negative edge weights. Returns true
// if a negative weight cycle is found.
/// Running time: O(|V|^3)
// INPUT: w[i][j] = weight of edge from i to j
// OUTPUT: w[i][j] = shortest path from i to j
// prev[i][j] = node before j on the best path starting at i
bool FloydWarshall (VVT &w, VVI &prev){
```

4.2 Fast Dijkstra's algorithm

```
// Implementation of Dijkstra's algorithm using adjacency lists
// and priority queue for efficiency.
// Running time: O(|E| log |V|)
#include <queue>
#include <cstdio>
using namespace std;
const int INF = 2000000000;
typedef pair<int, int> PII;
int main() {
        int N, s, t;
        scanf("%d%d%d", &N, &s, &t);
        vector<vector<PII> > edges(N):
        for (int i = 0; i < N; i++) {
                int M:
                scanf("%d", &M);
for (int j = 0; j < M; j++) {
                        int vertex, dist;
                        scanf("%d%d", &vertex, &dist);
                        edges[i].push_back(make_pair(dist, vertex)); // note order of arguments here
        // use priority queue in which top element has the "smallest" priority
        priority_queue<PII, vector<PII>, greater<PII> > Q;
        vector<int> dist(N, INF), dad(N, -1);
        Q.push (make pair (0, s));
        dist[s] = 0;
        while (!Q.empty()) {
                PII p = Q.top();
                Q.pop();
                int here = p.second;
                if (here == t) break;
                if (dist[here] != p.first) continue;
                for (vector<PII>::iterator it = edges[here].begin(); it != edges[here].end(); it++) {
                         if (dist[here] + it->first < dist[it->second]) {
                                 dist[it->second] = dist[here] + it->first;
                                 dad[it->second] = here;
                                 Q.push(make_pair(dist[it->second], it->second));
        printf("%d\n", dist[t]);
        if (dist[t] < INF)</pre>
                for (int i = t; i != -1; i = dad[i])
                        printf("%d%c", i, (i == s ? '\n' : ' '));
        return 0;
Sample input:
5 0 4 2 1 2 3 1
2 2 4 4 5
3 1 4 3 3 4 1
2 1 5 2 1
Expected:
```

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4.3 Dijkstra's algorithm

4.4 Minimum spanning trees using Prim

};

```
#include <bits/stdc++.h>
using namespace std;
// (u)int64, float
template<typename D>
struct Dijkstra {
    static constexpr D Inf = 11 << 60;
    struct Edge { size_t to; D len; };
        vector<Edge> outs;
        D dist = Inf;
#ifdef DIJKSTRA_RECORD_ROUTE
        size\_t prev = -1;
#endif
    size_t N;
    vector<Vertex> vs;
    // n nodes
    Dijkstra(size t n) : N(n) {
        vs.resize(n);
    void add(size_t from, size_t to, D len) {
        assert (from < N);
        assert (to < N);
        assert(len >= 0);
        vs[from].outs.push_back({ to, len });
   void add_u(size_t a, size_t b, D len) {
        add(a, b, len);
        add(b, a, len);
    D solve(size_t from, size_t to) {
        vs[from].dist = 0;
#ifdef DIJKSTRA_RECORD_ROUTE
        vs[from].prev = from;
#endif
        auto comp = [&](size_t x, size_t y) {
           return vs[x].dist < vs[y].dist || (vs[x].dist == vs[y].dist && x < y);</pre>
        set<size_t, decltype(comp)> q { comp };
        for (size_t i = 0; i < N; ++i) {
           q.insert(i);
        while (!q.empty()) {
           size_t i;
                auto it = q.begin();
                q.erase(it);
            if (i == to) {
               goto RETURN;
            for (Edge const& e : vs[i].outs) {
                if (vs[e.to].dist > vs[i].dist + e.len) {
                    if (q.find(e.to) != q.end()) {
                        q.erase(e.to);
                        vs[e.to].dist = vs[i].dist + e.len;
#ifdef DIJKSTRA_RECORD_ROUTE
                        vs[e.to].prev = i;
#endif
                        q.insert(e.to);
        return vs[to].dist;
```

```
#include <bits/stdc++.h>
using namespace std;
// (u)int64, float
template<typename D>
struct Prim {
    static constexpr D Inf = 11 << 60;</pre>
    struct Edge { size_t to; D len; };
    struct Vertex (
        vector<Edge> outs;
        D dist = Inf;
        size_t prev = -1;
    size_t N;
    vector<Vertex> vs;
    // n nodes
    Prim(size_t n) : N(n) {
        vs.resize(n);
    void add(size_t from, size_t to, D len) {
        assert (from < N);
        assert (to < N);
        assert(len >= 0);
        vs[from].outs.push_back({ to, len });
    void add_u(size_t a, size_t b, D len) {
        add(a, b, len);
        add(b, a, len);
    D solve(size_t from) {
        vs[from].dist = 0:
        vs[from].prev = from:
        auto comp = [&](size_t x, size_t y) {
    return vs[x].dist < vs[y].dist || (vs[x].dist == vs[y].dist && x < y);</pre>
        set<size_t, decltype(comp)> q { comp };
        for (size_t i = 0; i < N; ++i) {
            q.insert(i);
        while (!q.empty()) {
            size_t i;
                 auto it = q.begin();
i = *it;
                 q.erase(it);
             if (vs[i].dist == Inf) {
                 vs[i].dist = 0;
             for (Edge const& e : vs[i].outs) {
                 if (vs[e.to].dist > e.len) {
                     if (q.find(e.to) != q.end()) {
                          q.erase(e.to);
                         vs[e.to].dist = e.len;
vs[e.to].prev = i;
                         q.insert(e.to);
        D result = 0;
        for (size_t i = 0; i < N; ++i)</pre>
            result += vs[i].dist;
        return result;
};
```

4.5 Minimum spanning trees using Kruskal

```
#include <algorithm>
#include <cassert>
#include <cstdint>
#include <set>
#include <unordered_map>
#include <vector>
using namespace std;
// (u)int64, float
template <typename D>
struct Kruskal {
    static constexpr D Inf = 11 << 60;</pre>
    struct Edge {
        size_t n1, n2;
        D len;
        bool operator<(Edge const& o) const noexcept {</pre>
            return len < o.len || (len == o.len && (n1 < o.n1 || (n1 == o.n1 && (n2 < o.n2))));
    };
    typedef unordered_map<size_t, vector<Edge>> Forest;
    vector<Edge> edges;
    // n nodes
    Kruskal(size_t n) : N(n) {}
    void add(size_t n1, size_t n2, D len) {
        assert (n1 < N);
        assert (n2 < N);
        assert(len >= 0);
        if (n1 > n2) swap(n1, n2);
        edges.push_back({ n1, n2, len });
    void solve(Forest& forest) {
        sort(edges.begin(), edges.end());
        vector<size_t> _ufs(N);
        for (size_t i = 0; i < N; i++)
    _ufs[i] = i;</pre>
        auto ufs_p = [&](size_t i) -> size_t* {
            auto p = i:
            while (_ufs[p] != p)
             p = _ufs[p];
_ufs[i] = p;
            return &_ufs[i];
        for (Edge const& e : edges) {
            auto* ufs_n1p = ufs_p(e.n1);
auto* ufs_n2p = ufs_p(e.n2);
            if (*ufs_n1p != *ufs_n2p) {
                 if (*ufs_n1p > *ufs_n2p)
                     swap(*ufs_n1p, *ufs_n2p);
                 auto it = forest.find(*ufs_n2p);
                 if (it != forest.end()) {
                     forest[*ufs_nlp].insert(forest[*ufs_nlp].end(), it->second.begin(), it->second.end
                     forest.erase(it);
                 forest[*ufs_n1p].push_back(e);
                 *ufs_n2p = *ufs_n1p;
        return:
};
```

4.6 Strongly connected components

```
#include<memory.h>
struct edge{int e, nxt;};
```

```
int V, E;
edge e[MAXE], er[MAXE];
int sp[MAXV], spr[MAXV];
int group_cnt, group_num[MAXV];
bool v[MAXV];
int stk[MAXV];
void fill_forward(int x)
 int i;
  for(i=sp[x];i;i=e[i].nxt) if(!v[e[i].e]) fill_forward(e[i].e);
  stk[++stk[0]]=x;
void fill_backward(int x)
 v[x]=false;
  group_num[x]=group_cnt;
  for(i=spr[x];i;i=er[i].nxt) if(v[er[i].e]) fill_backward(er[i].e);
void add_edge(int v1, int v2) //add edge v1->v2
  e [++E].e=v2; e [E].nxt=sp [v1]; sp [v1]=E;
  er[ E].e=v1; er[E].nxt=spr[v2]; spr[v2]=E;
void SCC()
 int i:
  stk[0]=0;
  memset(v, false, sizeof(v));
  for(i=1;i<=V;i++) if(!v[i]) fill_forward(i);</pre>
  group_cnt=0;
  for(i=stk[0];i>=1;i--) if(v[stk[i]]) {group_cnt++; fill_backward(stk[i]);}
```

4.7 Eulerian path

```
typedef list<Edge>::iterator iter;
struct Edge
        int next_vertex;
        iter reverse_edge;
        Edge(int next_vertex)
                 :next_vertex(next_vertex)
};
const int max_vertices = ;
list<Edge> adj[max_vertices];
vector<int> path;
void find_path(int v)
        while(adj[v].size() > 0)
                 adj[v].front().next_vertex;
adj[v].erase(adj[v].front().reverse_edge);
adj[v].pop_front();
find_path(vn);
                  int vn = adj[v].front().next_vertex;
        path.push_back(v);
void add_edge(int a, int b)
         adj[a].push_front(Edge(b));
        iter ita = adj[a].begin();
        adj[b].push_front(Edge(a));
        iter itb = adj[b].begin();
        ita->reverse edge = itb:
        itb->reverse_edge = ita;
```

5 Data structures

5.1 Suffix array

```
// Suffix array construction in O(L log^2 L) time. Routine for
// computing the length of the longest common prefix of any two
// suffixes in O(log L) time.
// TNPUT: string s
// OUTPUT: array suffix[] such that suffix[i] = index (from 0 to L-1)
            of substring s[i...L-1] in the list of sorted suffixes.
            That is, if we take the inverse of the permutation suffix[],
            we get the actual suffix array.
#include <vector>
#include <iostream>
#include <string>
using namespace std;
struct SuffixArray {
  const int L;
  string s;
  vector<vector<int> > P:
  vector<pair<pair<int,int>,int> > M;
  SuffixArray(const string &s) : L(s.length()), s(s), P(1, vector<int>(L, 0)), M(L) {
    for (int i = 0; i < L; i++) P[0][i] = int(s[i]);
for (int skip = 1, level = 1; skip < L; skip *= 2, level++) {</pre>
      P.push_back(vector<int>(L, 0));
      for (int i = 0; i < L; i++)
       M[i] = make\_pair(make\_pair(P[level-1][i], i + skip < L ? P[level-1][i + skip] : -1000), i);
      sort(M.begin(), M.end());
      for (int i = 0; i < L; i++)
         P[level][M[i].second] = (i > 0 \&\& M[i].first == M[i-1].first) ? P[level][M[i-1].second] : i; 
  vector<int> GetSuffixArray() { return P.back(); }
  // returns the length of the longest common prefix of s[i...L-1] and s[j...L-1]
  int LongestCommonPrefix(int i, int j) {
    int len = 0;
    if (i == j) return L - i;
    for (int k = P.size() - 1; k >= 0 && i < L && j < L; k--) {
      if (P[k][i] == P[k][j]) {
         j += 1 << k;
        len += 1 << k;
    return len:
};
// The following code solves UVA problem 11512: GATTACA.
#define TESTING
#ifdef TESTING
int main() {
  for (int caseno = 0; caseno < T; caseno++) {</pre>
    string s;
    cin >> s:
    SuffixArray array(s);
    vector<int> v = array.GetSuffixArray();
    int bestlen = -1, bestpos = -1, bestcount = 0;
    for (int i = 0; i < s.length(); i++) {</pre>
     int len = 0, count = 0;
      for (int j = i+1; j < s.length(); j++) {</pre>
        int 1 = array.LongestCommonPrefix(i, j);
        if (1 >= len) {
          if (1 > len) count = 2; else count++;
      if (len > bestlen || len == bestlen && s.substr(bestpos, bestlen) > s.substr(i, len)) {
        bestlen = len;
        bestcount = count:
        bestpos = i;
    if (bestlen == 0) {
     cout << "No repetitions found!" << endl;</pre>
```

```
} else {
      cout << s.substr(bestpos, bestlen) << " " << bestcount << endl;</pre>
#else
// END CUT
int main() {
  // bobocel is the O'th suffix
  // obocel is the 5'th suffix
     bocel is the 1'st suffix
       ocel is the 6'th suffix
        cel is the 2'nd suffix
         el is the 3'rd suffix
          1 is the 4'th suffix
  SuffixArray suffix("bobocel");
  vector<int> v = suffix.GetSuffixArray();
  // Expected output: 0 5 1 6 2 3 4
  for (int i = 0; i < v.size(); i++) cout << v[i] << " ";
  cout << endl:
  cout << suffix.LongestCommonPrefix(0, 2) << endl;</pre>
// BEGIN CUT
#endif
// END CUT
```

5.2 Binary Indexed Tree

```
#include <iostream>
using namespace std;
#define LOGSZ 17
int tree[(1<<LOGSZ)+1];</pre>
int N = (1 << LOGSZ);
// add v to value at x
void set(int x, int v) {
  while (x <= N) {
    tree[x] += v;
    x += (x & -x);
// get cumulative sum up to and including x
int get(int x) {
 int res = 0:
  while(x) {
   res += tree[x];
   x -= (x & -x);
// get largest value with cumulative sum less than or equal to x;
// for smallest, pass x-1 and add 1 to result
int getind(int x) {
 int idx = 0, mask = N;
  while (mask && idx < N)
   int t = idx + mask;
   if(x >= tree[t]) {
     idx = t:
     x -= tree[t];
   mask >>= 1;
  return idx;
```

5.3 Union-find set

```
#include <bits/stdc++.h>
using namespace std;
struct UnionFind {
  vector<int> C;
  UnionFind(int n) : C(n) { for (int i = 0; i < n; i++) C[i] = i; }
  int find(int x) { return (C[x] == x) ? x : C[x] = find(C[x]); }
  void merge(int x, int y) { C[find(x)] = find(y); }
};</pre>
```

5.4 KD-tree

```
// A straightforward, but probably sub-optimal KD-tree implmentation
// that's probably good enough for most things (current it's a
// 2D-tree)
// - constructs from n points in O(n lg^2 n) time
// - handles nearest-neighbor query in O(lg n) if points are well
    distributed
// - worst case for nearest-neighbor may be linear in pathological
     Case
// Sonny Chan, Stanford University, April 2009
#include <iostream>
#include <vector>
#include <limits>
#include <cstdlib>
using namespace std;
// number type for coordinates, and its maximum value
typedef long long ntype;
const ntype sentry = numeric_limits<ntype>::max();
// point structure for 2D-tree, can be extended to 3D
struct point {
    ntype x, y;
   point(ntype xx = 0, ntype yy = 0) : x(xx), y(yy) {}
};
bool operator==(const point &a, const point &b)
    return a.x == b.x && a.y == b.y;
// sorts points on x-coordinate
bool on_x(const point &a, const point &b)
    return a.x < b.x:
   sorts points on v-coordinate
bool on_y(const point &a, const point &b)
    return a.y < b.y;</pre>
// squared distance between points
ntype pdist2(const point &a, const point &b)
    ntype dx = a.x-b.x, dy = a.y-b.y;
    return dx*dx + dy*dy;
// bounding box for a set of points
struct bbox
    ntype x0, x1, y0, y1;
    bbox(): x0(sentry), x1(-sentry), y0(sentry), y1(-sentry) {}
    // computes bounding box from a bunch of points
    void compute(const vector<point> &v) {
        for (int i = 0; i < v.size(); ++i) {
  x0 = min(x0, v[i].x);     x1 = max(x1, v[i].x);</pre>
            y0 = min(y0, v[i].y); y1 = max(y1, v[i].y);
    // squared distance between a point and this bbox, 0 if inside
    ntype distance (const point &p) {
        if (p.x < x0) {
            if (p.y < y0)
                                 return pdist2(point(x0, y0), p);
            else if (p.y > y1) return pdist2(point(x0, y1), p);
            else
                                 return pdist2(point(x0, p.y), p);
        else if (p.x > x1) {
                                return pdist2(point(x1, y0), p);
            if (p.y < y0)
            else if (p.y > y1) return pdist2(point(x1, y1), p);
            else
                                 return pdist2(point(x1, p.y), p);
        else
                                return pdist2(point(p.x, y0), p);
            if (p.y < y0)
            else if (p.y > y1) return pdist2(point(p.x, y1), p);
            else
                                 return 0;
```

```
// stores a single node of the kd-tree, either internal or leaf
struct kdnode
    bool leaf;
                     // true if this is a leaf node (has one point)
    point pt;
                     // the single point of this is a leaf
    bbox bound;
                     // bounding box for set of points in children
    kdnode *first. *second: // two children of this kd-node
    kdnode() : leaf(false), first(0), second(0) {}
    ~kdnode() { if (first) delete first; if (second) delete second; }
    // intersect a point with this node (returns squared distance)
    ntype intersect(const point &p) {
        return bound.distance(p);
    // recursively builds a kd-tree from a given cloud of points
    void construct(vector<point> &vp)
         // compute bounding box for points at this node
        bound.compute(vp);
        // if we're down to one point, then we're a leaf node
        if (vp.size() == 1) {
            leaf = true;
            pt = vp[0];
        else {
              split on x if the bbox is wider than high (not best heuristic...)
             if (bound.x1-bound.x0 >= bound.y1-bound.y0)
                 sort(vp.begin(), vp.end(), on_x);
             // otherwise split on y-coordinate
            else
                 sort(vp.begin(), vp.end(), on_y);
            // divide by taking half the array for each child
// (not best performance if many duplicates in the middle)
            int half = vp.size()/2;
            vector<point> vl(vp.begin(), vp.begin()+half);
vector<point> vr(vp.begin()+half, vp.end());
            first = new kdnode(); first->construct(vl);
            second = new kdnode(); second->construct(vr);
};
// simple kd-tree class to hold the tree and handle queries
struct kdtree
    kdnode +root:
    // constructs a kd-tree from a points (copied here, as it sorts them)
    kdtree(const vector<point> &vp) {
        vector<point> v(vp.begin(), vp.end());
        root = new kdnode();
        root->construct(v);
    "kdtree() { delete root; }
    // recursive search method returns squared distance to nearest point
    ntype search(kdnode *node, const point &p)
        if (node->leaf) {
            // commented special case tells a point not to find itself
              if (p == node->pt) return sentry;
              else
                return pdist2(p, node->pt);
        ntype bfirst = node->first->intersect(p);
        ntype bsecond = node->second->intersect(p);
        // choose the side with the closest bounding box to search first
         // (note that the other side is also searched if needed)
        if (bfirst < bsecond) {</pre>
             ntype best = search(node->first, p);
            if (bsecond < best)</pre>
                best = min(best, search(node->second, p));
            return best:
        else {
            ntype best = search(node->second, p);
            if (bfirst < best)</pre>
                best = min(best, search(node->first, p));
            return best:
```

```
// squared distance to the nearest
ntype nearest(const point &p) {
    return search(root, p);
};

// some basic test code here

int main()
{
    // generate some random points for a kd-tree
    vector<point> vp;
    for (int i = 0; i < 100000; ++i) {
        vp.push_back(point(rand()%100000, rand()%100000));
    }
    kdtree tree(vp);

    // query some points
    for (int i = 0; i < 10; ++i) {
        point q(rand()%100000, rand()%10000);
        cout << "Closest squared distance to (" << q.x << ", " << q.y << ")"
        << " is " << tree.nearest(q) << endl;
}

return 0;
}</pre>
```

5.5 Splay tree

```
#include <cstdio>
#include <algorithm>
using namespace std;
const int N_MAX = 130010;
const int oo = 0x3f3f3f3f3f;
struct Node
  Node *ch[2], *pre;
  int val, size;
  bool isTurned;
} nodePool[N_MAX], *null, *root;
Node *allocNode(int val)
  static int freePos = 0;
  Node *x = &nodePool[freePos ++];
  x->val = val, x->isTurned = false;
  x->ch[0] = x->ch[1] = x->pre = null;
  x->size = 1;
  return x;
inline void update (Node *x)
  x->size = x->ch[0]->size + x->ch[1]->size + 1;
inline void makeTurned(Node *x)
  if(x == null)
    return;
  swap(x->ch[0], x->ch[1]);
x->isTurned ^= 1;
inline void pushDown(Node *x)
  if(x->isTurned)
    makeTurned(x->ch[0]);
    makeTurned(x->ch[1]);
    x->isTurned ^= 1;
inline void rotate(Node *x, int c)
  Node *y = x->pre;
  x->pre = y->pre;
if(y->pre != null)
  11(y=>pre := null)
y->pre->ch[y == y->pre->ch[1]] = x;
y->ch[!c] = x->ch[c];
if(x->ch[c] != null)
    x->ch[c]->pre = y;
```

```
x->ch[c] = y, y->pre = x;
  update(y);
  if(y == root)
    root = x;
void splay (Node *x, Node *p)
  while(x->pre != p)
    if(x->pre->pre == p)
      rotate(x, x == x->pre->ch[0]);
    else
      Node *y = x->pre, *z = y->pre;
if(y == z->ch[0])
           rotate(y, 1), rotate(x, 1);
        else
          rotate(x, 0), rotate(x, 1);
      else
        if(x == y->ch[1])
          rotate(y, 0), rotate(x, 0);
        else
          rotate(x, 1), rotate(x, 0);
  update(x);
void select(int k, Node *fa)
  Node *now = root;
  while(1)
    pushDown (now);
    int tmp = now->ch[0]->size + 1;
    if(tmp == k)
     break:
    else if(tmp < k)</pre>
      now = now -> ch[1], k -= tmp;
    else
     now = now -> ch[0];
  splay(now, fa);
Node *makeTree(Node *p, int 1, int r)
 if(1 > r)
    return null:
  int mid = (1 + r) / 2:
 Node *x = allocNode(mid);
 x->pre = p;
x->ch[0] = makeTree(x, 1, mid - 1);
x->ch[1] = makeTree(x, mid + 1, r);
  update(x);
  return x;
int main()
  int n, m;
 null = allocNode(0);
 null->size = 0;
  root = allocNode(0):
  root->ch[1] = allocNode(oo);
  root->ch[1]->pre = root;
  update (root);
  scanf("%d%d", &n, &m);
  root->ch[1]->ch[0] = makeTree(root->ch[1], 1, n);
  splay(root->ch[1]->ch[0], null);
  while (m --)
    int a, b;
    scanf("%d%d", &a, &b);
    a ++, b ++;
select(a - 1, null);
    select(b + 1, root);
    makeTurned(root->ch[1]->ch[0]);
  for(int i = 1; i <= n; i ++)</pre>
    select(i + 1, null);
    printf("%d ", root->val);
```

return 0;
}

5.6 Lowest common ancestor

```
const int max_nodes, log_max_nodes;
int num_nodes, log_num_nodes, root;
vector<int> children[max_nodes];
                                          // children[i] contains the children of node i
int A[max_nodes][log_max_nodes+1];
                                         // A[i][j] is the 2^j-th ancestor of node i, or -1 if that
      ancestor does not exist
int L[max_nodes];
                                          // L[i] is the distance between node i and the root
// floor of the binary logarithm of n
int lb(unsigned int n)
    if(n==0)
       return -1;
    int p = 0;
    if (n >= 1<<16) { n >>= 16; p += 16; }
    if (n >= 1<< 8) { n >>= 8; p += 8;
    if (n >= 1<< 4) { n >>= 4; p += 4;
    if (n >= 1 << 2) { n >>= 2; p += 2; }
    if (n >= 1<< 1) {
    return p;
void DFS(int i, int 1)
    L[i] = 1;
    for(int j = 0; j < children[i].size(); j++)</pre>
        DFS(children[i][j], 1+1);
int LCA(int p, int q)
    // ensure node p is at least as deep as node q
    if(L[p] < L[q])
        swap(p, q);
    // "binary search" for the ancestor of node p situated on the same level as q for(int i = log_num_nodes; i \ge 0; i--)
        if(L[p] - (1<<i) >= L[q])
            p = A[p][i];
    if(p == q)
        return p;
    // "binary search" for the LCA
    for(int i = log_num_nodes; i >= 0; i--)
        if(A[p][i] != -1 && A[p][i] != A[q][i])
            p = A[p][i];
            q = A[q][i];
    return A[p][0];
int main(int argc,char* argv[])
    // read num_nodes, the total number of nodes
    log_num_nodes=1b(num_nodes);
    for(int i = 0; i < num_nodes; i++)</pre>
        // read p, the parent of node i or -1 if node i is the root
        A[i][0] = p;
        if(p != -1)
            children[p].push_back(i);
            root = i;
    // precompute A using dynamic programming
    for(int j = 1; j <= log_num_nodes; j++)</pre>
        for(int i = 0; i < num_nodes; i++)</pre>
            if(A[i][j-1] != -1)
                A[i][j] = A[A[i][j-1]][j-1];
            else
                A[i][j] = -1;
    // precompute L
    DFS(root, 0);
```

6 Miscellaneous

6.1 Longest increasing subsequence

```
// Given a list of numbers of length n, this routine extracts a
// longest increasing subsequence.
// Running time: O(n log n)
    INPUT: a vector of integers
    OUTPUT: a vector containing the longest increasing subsequence
#include <iostream>
#include <vector>
#include <algorithm>
using namespace std;
typedef vector<int> VI;
typedef pair<int, int> PII;
typedef vector<PII> VPII;
#define STRICTLY INCREASING
VI LongestIncreasingSubsequence(VI v) {
 VPII best;
 VI dad(v.size(), -1);
  for (int i = 0; i < v.size(); i++) {</pre>
#ifdef STRICTLY_INCREASNG
    PII item = make_pair(v[i], 0);
    VPII::iterator it = lower_bound(best.begin(), best.end(), item);
    item.second = i;
#else
    PII item = make_pair(v[i], i);
    VPII::iterator it = upper_bound(best.begin(), best.end(), item);
#endif
    if (it == best.end()) {
      dad[i] = (best.size() == 0 ? -1 : best.back().second);
      best.push_back(item);
   } else {
     dad[i] = it == best.begin() ? -1 : prev(it)->second;
      *it = item;
  for (int i = best.back().second; i >= 0; i = dad[i])
   ret.push_back(v[i]);
  reverse(ret.begin(), ret.end());
  return ret:
```

6.2 Dates

```
// Routines for performing computations on dates. In these routines,
// months are expressed as integers from 1 to 12, days are expressed
// as integers from 1 to 31, and years are expressed as 4-digit
// integers.

#include <iostream>
#include <string>
using namespace std;

string dayOfWeek[] = {"Mon", "Tue", "Wed", "Thu", "Fri", "Sat", "Sun"};

// converts Gregorian date to integer (Julian day number)
int dateToInt (int m, int d, int y){
    return
    1461 * (y + 4800 + (m - 14) / 12) / 4 +
    367 * (m - 2 - (m - 14) / 12 + 12) / 12 -
    3 * ((y + 4900 + (m - 14) / 12) / 100) / 4 +
    d - 32075;
}

// converts integer (Julian day number) to Gregorian date: month/day/year
```

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```
void intToDate (int jd, int &m, int &d, int &y) {
  int x, n, i, j;
  x = jd + 68569;
 n = 4 * x / 146097;
  x = (146097 * n + 3) / 4;
  i = (4000 * (x + 1)) / 1461001;
x -= 1461 * i / 4 - 31;
j = 80 * x / 2447;
  d = x - 2447 * j / 80;
 x = j / 11;

m = j + 2 - 12 * x;
  y = 100 * (n - 49) + i + x;
// converts integer (Julian day number) to day of week
string intToDay (int jd) {
  return dayOfWeek[jd % 7];
int main (int argc, char **argv) {
 int jd = dateToInt (3, 24, 2004);
  int m, d, y;
  intToDate (jd, m, d, y);
  string day = intToDay (jd);
  // expected output:
       2453089
        3/24/2004
       Wed
  cout << jd << endl
    << m << "/" << d << "/" << y << endl
    << day << end1;
```

6.3 Prime numbers

```
// O(sqrt(x)) Exhaustive Primality Test
#include <cmath>
#define EPS 1e-7
typedef long long LL:
bool IsPrimeSlow (LL x)
  if(x<=1) return false;</pre>
  if(x<=3) return true;</pre>
  if (!(x%2) || !(x%3)) return false;
  LL s=(LL) (sqrt((double)(x))+EPS);
  for(LL i=5;i<=s;i+=6)
    if (!(x%i) || !(x%(i+2))) return false;
  return true;
// Primes less than 1000:
                               11
59
                                     13
                                     61
                                           67
                                                             79
                                                                   83
                         5.3
                        107
                              109
                                    113
                                          127
                                                131
                                                            139
                                                                  149
                                                                        151
                        173
                              179
                                    181
                                          191
                                                193
                                                      197
                                                            199
           163
                  167
                                                                  211
                                    251
317
                                          257
                                                            271
                  233
                        239
                              241
                                                263
                                                      269
                        311
                              313
                                          331
                                                337
                  379
                              389
                                    397
                                          401
                                                409
      439
                  449
                        457
                              461
                                    463
                                          467
                                                479
                                                      487
                                                            491
      509
                  523
                        541
                              547
                                    557
                                          563
                                                569
                                                      571
                                                            577
                                                                   587
      599
            601
                  607
                        613
                              617
                                    619
                                          631
                                                641
                                                      643
                                                            647
                                                                   653
      661
            673
                  677
                        683
                              691
                                    701
                                          709
                                                719
                                                      727
                                                            733
                                                                   739
                                                                         743
     751
829
                  761
853
                        769
857
                                    787
                                          797
                                                809
                                                            821
                              859
                                          877
            839
                                    863
                                                881
                                                      883
                                                            887
                                                                  907
                                                                         911
                             947
                  937
                       941
                                    953
// Other primes:
     The largest prime smaller than 10 is 7.
      The largest prime smaller than 100 is 97.
     The largest prime smaller than 1000 is 997.
      The largest prime smaller than 10000 is 9973.
     The largest prime smaller than 100000 is 99991
      The largest prime smaller than 1000000 is 999983.
      The largest prime smaller than 10000000 is 9999991.
      The largest prime smaller than 100000000 is 99999989.
      The largest prime smaller than 1000000000 is 999999937.
     The largest prime smaller than 10000000000 is 9999999967. The largest prime smaller than 10000000000 is 99999999977.
     The largest prime smaller than 100000000000 is 99999999989. The largest prime smaller than 100000000000 is 999999999971.
      The largest prime smaller than 1000000000000 is 9999999999973.
      The largest prime smaller than 10000000000000 is 9999999999999999.
      The largest prime smaller than 100000000000000 is 999999999999937
```

6.4 C++ input/output

```
#include <bits/stdc++.h>
using namespace std:
int main()
    // Ouput a specific number of digits past the decimal point,
    // in this case 5
    cout.setf(ios::fixed); cout << setprecision(5);</pre>
    cout << 100.0/7.0 << endl;</pre>
    cout.unsetf(ios::fixed);
    // Output the decimal point and trailing zeros
    cout.setf(ios::showpoint);
    cout << 100.0 << end1:
    cout.unsetf(ios::showpoint);
    // Output a '+' before positive values
    cout.setf(ios::showpos);
    cout << 100 << " " << -100 << endl;
    cout.unsetf(ios::showpos);
    // Output numerical values in hexadecimal
    cout << hex << 100 << " " << 1000 << " " << 10000 << dec << endl;
```

6.5 Knuth-Morris-Pratt

```
Finds all occurrences of the pattern string p within the
text string t. Running time is O(n + m), where n and m
are the lengths of p and t, respecitvely.
#include <iostream>
#include <string>
#include <vector>
using namespace std;
typedef vector<int> VI:
void buildPi(string& p, VI& pi)
  pi = VI(p.length());
  int k = -2:
  for(int i = 0; i < p.length(); i++) {</pre>
    while (k \ge -1) && p[k+1] != p[i])

k = (k == -1) ? -2 : pi[k];
    pi[i] = ++k;
int KMP (string& t, string& p)
  VI pi;
  buildPi(p, pi);
  int k = -1;
  for(int i = 0; i < t.length(); i++) {
  while(k >= -1 && p[k+1] != t[i])
      k = (k == -1) ? -2 : pi[k];
    k++;
    if(k == p.length() - 1) {
     // p matches t[i-m+1, ..., i]
      cout << "matched at index " << i-k << ": ";
      cout << t.substr(i-k, p.length()) << endl;</pre>
      k = (k == -1) ? -2 : pi[k];
  return 0:
int main()
  string a = "AABAACAADAABAABA", b = "AABA";
  KMP(a, b); // expected matches at: 0, 9, 12
  return 0:
```

6.6 Latitude/longitude

```
{\it Converts from rectangular coordinates to latitude/longitude \ and \ vice}
versa. Uses degrees (not radians).
#include <iostream>
#include <cmath>
using namespace std;
struct 11
  double r, lat, lon;
struct rect
  double x, y, z;
};
11 convert (rect& P)
  11 Q;
  Q.r = sqrt(P.x*P.x+P.y*P.y+P.z*P.z);
  Q.lat = 180/M_PI*asin(P.z/Q.r);
Q.lon = 180/M_PI*acos(P.x/sqrt(P.x*P.x+P.y*P.y));
  return Q;
rect convert(11& Q)
 P.x = Q.r*cos(Q.lon*M_PI/180)*cos(Q.lat*M_PI/180);
P.y = Q.r*sin(Q.lon*M_PI/180)*cos(Q.lat*M_PI/180);
P.z = Q.r*sin(Q.lat*M_PI/180);
  return P;
int main()
  rect A;
  11 B;
  A.x = -1.0; A.y = 2.0; A.z = -3.0;
  B = convert(A);
cout << B.r << " " << B.lat << " " << B.lon << endl;</pre>
  A = convert(B);
cout << A.x << " " << A.y << " " << A.z << endl;
```

6.7 Vim settings

```
set enc=utf-8
set fenc=utf-8
scriptencoding utf-8
set fencs=utf-8,ucs-bom,gb18030,gbk,gb2312,cp936
```

```
syntax on
filetype plugin on
filetype indent on
set mouse=a
set nocompatible
set tabstop=4
set shiftwidth=4
set expandtab
set smarttab
set autoindent
set textwidth=1000
set showmatch
set ruler
set hlsearch
set incsearch
set ignorecase
set smartcase
set number
set relativenumber
set fdm=marker
set scrolloff=10
set showcmd
set backspace=indent,eol,start
set formatoptions=q,r
set nowrap
set foldmethod=indent
set foldlevelstart=10
set wildmenu
set omnifunc=syntaxcomplete#Complete
"the trail config failed in generate latex
"remember to add in the site"
set list listchars=tab:>-.trail:
set t_Co=256
set background=dark
nnoremap ; :
inoremap <silent> jj <ESC>
nnoremap <silent> <HOME>
inoremap <silent> <HOME> <ESC>^i
vnoremap <silent> <HOME> 0w
nnoremap <silent> <F9> :set nowrap<CR>
nnoremap <silent> <F10> :set wrap<CR>
```