C2_W4_Assignment

October 31, 2020

1 Assignment 4: Word Embeddings

Welcome to the fourth (and last) programming assignment of Course 2!

In this assignment, you will practice how to compute word embeddings and use them for sentiment analysis. - To implement sentiment analysis, you can go beyond counting the number of positive words and negative words. - You can find a way to represent each word numerically, by a vector. - The vector could then represent syntactic (i.e. parts of speech) and semantic (i.e. meaning) structures.

In this assignment, you will explore a classic way of generating word embeddings or representations. - You will implement a famous model called the continuous bag of words (CBOW) model.

By completing this assignment you will:

- Train word vectors from scratch.
- Learn how to create batches of data.
- Understand how backpropagation works.
- Plot and visualize your learned word vectors.

Knowing how to train these models will give you a better understanding of word vectors, which are building blocks to many applications in natural language processing.

1.1 Outline

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1. The Continuous bag of words model

Let's take a look at the following sentence: >'I am happy because I am learning'.

- In continuous bag of words (CBOW) modeling, we try to predict the center word given a few context words (the words around the center word).
- For example, if you were to choose a context half-size of say C = 2, then you would try to predict the word **happy** given the context that includes 2 words before and 2 words after the center word:

C words before: [I, am]

C words after: [because, I]

• In other words:

$$context = [I, am, because, I]$$

 $target = happy$

The structure of your model will look like this:

Figure 1

Where \bar{x} is the average of all the one hot vectors of the context words.

Figure 2

Once you have encoded all the context words, you can use \bar{x} as the input to your model.

The architecture you will be implementing is as follows:

$$h = W_1 X + b_1 \tag{1}$$

$$a = ReLU(h) \tag{2}$$

$$z = W_2 a + b_2 \tag{3}$$

$$\hat{y} = softmax(z) \tag{4}$$

(1)

In []: # Import Python libraries and helper functions (in utils2)
 import nltk

from nltk.tokenize import word_tokenize
import numpy as np

from collections import Counter

from utils2 import sigmoid, get_batches, compute_pca, get_dict

```
In []: # Load, tokenize and process the data
        import re
                                                                           # Load the Regex-
       with open('shakespeare.txt') as f:
            data = f.read()
                                                                            # Read in the dat
       data = re.sub(r'[,!?;-]', '.',data)
                                                                            # Punktuations ar
       data = nltk.word_tokenize(data)
                                                                           # Tokenize string
       data = [ ch.lower() for ch in data if ch.isalpha() or ch == '.'] # Lower case and
       print("Number of tokens:", len(data),'\n', data[:15])
                                                                           # print data samp
In []: # Compute the frequency distribution of the words in the dataset (vocabulary)
       fdist = nltk.FreqDist(word for word in data)
       print("Size of vocabulary: ",len(fdist) )
       print("Most frequent tokens: ",fdist.most_common(20)) # print the 20 most frequent wo
```

Mapping words to indices and indices to words We provide a helper function to create a dictionary that maps words to indices and indices to words.

1.1.1 Initializing the model

You will now initialize two matrices and two vectors. - The first matrix (W_1) is of dimension $N \times V$, where V is the number of words in your vocabulary and N is the dimension of your word vector. - The second matrix (W_2) is of dimension $V \times N$. - Vector b_1 has dimensions $N \times 1$ - Vector b_2 has dimensions $V \times 1$. - b_1 and b_2 are the bias vectors of the linear layers from matrices W_1 and W_2 .

The overall structure of the model will look as in Figure 1, but at this stage we are just initializing the parameters.

Exercise 01 Please use numpy.random.rand to generate matrices that are initialized with random values from a uniform distribution, ranging between 0 and 1.

Note: In the next cell you will encounter a random seed. Please **DO NOT** modify this seed so your solution can be tested correctly.

```
Outputs:
                W1, W2, b1, b2: initialized weights and biases
            np.random.seed(random seed)
            ### START CODE HERE (Replace instances of 'None' with your code) ###
            # W1 has shape (N, V)
            W1 = np.random.rand(N,V)
            # W2 has shape (V,N)
            W2 = np.random.rand(V,N)
            # b1 has shape (N,1)
            b1 = np.random.rand(N,1)
            # b2 has shape (V,1)
            b2 = np.random.rand(V,1)
            ### END CODE HERE ###
            return W1, W2, b1, b2
In []: # Test your function example.
        tmp_N = 4
        tmp_V = 10
        tmp_W1, tmp_W2, tmp_b1, tmp_b2 = initialize_model(tmp_N,tmp_V)
        assert tmp_W1.shape == ((tmp_N,tmp_V))
        assert tmp_W2.shape == ((tmp_V,tmp_N))
        print(f"tmp_W1.shape: {tmp_W1.shape}")
        print(f"tmp_W2.shape: {tmp_W2.shape}")
        print(f"tmp_b1.shape: {tmp_b1.shape}")
        print(f"tmp_b2.shape: {tmp_b2.shape}")
  Expected Output
tmp_W1.shape: (4, 10)
```

tmp_W1.shape: (4, 10)
tmp_W2.shape: (10, 4)
tmp_b1.shape: (4, 1)
tmp_b2.shape: (10, 1)

2.1 Softmax Before we can start training the model, we need to implement the softmax function as defined in equation 5:

softmax
$$(z_i) = \frac{e^{z_i}}{\sum_{i=0}^{V-1} e^{z_i}}$$
 (5)

- Array indexing in code starts at 0.
- *V* is the number of words in the vocabulary (which is also the number of rows of *z*).
- *i* goes from 0 to |V| 1.

Exercise 02 **Instructions**: Implement the softmax function below.

• Assume that the input *z* to softmax is a 2D array

- Each training example is represented by a column of shape (V, 1) in this 2D array.
- There may be more than one column, in the 2D array, because you can put in a batch of examples to increase efficiency. Let's call the batch size lowercase m, so the z array has shape (V, m)
- When taking the sum from $i = 1 \cdots V 1$, take the sum for each column (each example) separately.

Please use - numpy.exp - numpy.sum (set the axis so that you take the sum of each column in z)

```
In [ ]: # UNQ_C2 (UNIQUE CELL IDENTIFIER, DO NOT EDIT)
        # GRADED FUNCTION: softmax
        def softmax(z):
            ,,,
            Inputs:
                z: output scores from the hidden layer
            Outputs:
                yhat: prediction (estimate of y)
            ### START CODE HERE (Replace instances of 'None' with your own code) ###
            # Calculate yhat (softmax)
            e_z = np.exp(z)
            yhat = e_z/np.sum(e_z,axis=0)
            ### END CODE HERE ###
            return yhat
In [ ]: # Test the function
        tmp = np.array([[1,2,3],
                        [1,1,1]
                       ])
        tmp_sm = softmax(tmp)
        display(tmp_sm)
  Expected Ouput
```

```
array([[0.5 , 0.73105858, 0.88079708], [0.5 , 0.26894142, 0.11920292]])
```

2.2 Forward propagation

Exercise 03 Implement the forward propagation z according to equations (1) to (3).

$$h = W_1 X + b_1 \tag{1}$$

$$a = ReLU(h) \tag{2}$$

$$z = W_2 a + b_2 \tag{3}$$

(2)

For that, you will use as activation the Rectified Linear Unit (ReLU) given by:

$$f(h) = \max(0, h) \tag{6}$$

Hints

You can use numpy.maximum(x1,x2) to get the maximum of two values Use numpy.dot(A,B) to matrix multiply A and B

```
In [ ]: # UNQ_C3 (UNIQUE CELL IDENTIFIER, DO NOT EDIT)
        # GRADED FUNCTION: forward_prop
        def forward_prop(x, W1, W2, b1, b2):
            Inputs:
                x: average one hot vector for the context
                W1, W2, b1, b2: matrices and biases to be learned
             Outputs:
                z: output score vector
            ### START CODE HERE (Replace instances of 'None' with your own code) ###
            # Calculate h
           h = np.dot(W1,x)+b1
            # Apply the relu on h (store result in h)
           h = np.maximum(0,h)
            # Calculate z
            z = np.dot(W2,h)+b2
            ### END CODE HERE ###
           return z, h
In [ ]: # Test the function
        # Create some inputs
        tmp_N = 2
        tmp_V = 3
        tmp_x = np.array([[0,1,0]]).T
        tmp_W1, tmp_W2, tmp_b1, tmp_b2 = initialize_model(N=tmp_N,V=tmp_V, random_seed=1)
       print(f"x has shape {tmp_x.shape}")
       print(f"N is {tmp_N} and vocabulary size V is {tmp_V}")
        # call function
        tmp_z, tmp_h = forward_prop(tmp_x, tmp_W1, tmp_W2, tmp_b1, tmp_b2)
        print("call forward_prop")
       print()
```

```
print("z has values:")
        print(tmp_z)
        print()
        print(f"h has shape {tmp_h.shape}")
        print("h has values:")
        print(tmp_h)
  Expected output
x has shape (3, 1)
N is 2 and vocabulary size V is 3
call forward_prop
z has shape (3, 1)
z has values:
[[0.55379268]
[1.58960774]
[1.50722933]]
h has shape (2, 1)
h has values:
[[0.92477674]
[1.02487333]]
  ## 2.3 Cost function
  • We have implemented the cross-entropy cost function for you.
In [ ]: # compute_cost: cross-entropy cost functioN
        def compute_cost(y, yhat, batch_size):
            # cost function
            logprobs = np.multiply(np.log(yhat),y) + np.multiply(np.log(1 - yhat), 1 - y)
            cost = - 1/batch_size * np.sum(logprobs)
            cost = np.squeeze(cost)
            return cost
In [ ]: # Test the function
        tmp_C = 2
        tmp_N = 50
        tmp_batch_size = 4
        tmp_word2Ind, tmp_Ind2word = get_dict(data)
        tmp_V = len(word2Ind)
        tmp_x, tmp_y = next(get_batches(data, tmp_word2Ind, tmp_V,tmp_C, tmp_batch_size))
```

Look at output

print(f"z has shape {tmp_z.shape}")

```
print(f"tmp_x.shape {tmp_x.shape}")
print(f"tmp_y.shape {tmp_y.shape}")

tmp_W1, tmp_W2, tmp_b1, tmp_b2 = initialize_model(tmp_N,tmp_V)

print(f"tmp_W1.shape {tmp_W1.shape}")
print(f"tmp_w2.shape {tmp_W2.shape}")
print(f"tmp_b1.shape {tmp_b1.shape}")
print(f"tmp_b2.shape {tmp_b2.shape}")

tmp_z, tmp_h = forward_prop(tmp_x, tmp_W1, tmp_W2, tmp_b1, tmp_b2)
print(f"tmp_z.shape: {tmp_z.shape}")
print(f"tmp_h.shape: {tmp_h.shape}")

tmp_yhat = softmax(tmp_z)
print(f"tmp_yhat.shape: {tmp_yhat.shape}")

tmp_cost = compute_cost(tmp_y, tmp_yhat, tmp_batch_size)
print("call_compute_cost")
print(f"tmp_cost {tmp_cost:.4f}")
```

Expected output

```
tmp_x.shape (5778, 4)
tmp_y.shape (5778, 4)
tmp_W1.shape (50, 5778)
tmp_W2.shape (5778, 50)
tmp_b1.shape (50, 1)
tmp_b2.shape (5778, 1)
tmp_z.shape: (5778, 4)
tmp_h.shape: (50, 4)
tmp_yhat.shape: (5778, 4)
call compute_cost
tmp_cost 9.9560
```

2.4 Training the Model - Backpropagation

Exercise 04 Now that you have understood how the CBOW model works, you will train it. You created a function for the forward propagation. Now you will implement a function that computes the gradients to backpropagate the errors.

```
W1, W2, b1, b2: matrices and biases
                batch_size: batch size
             Outputs:
                grad_W1, grad_W2, grad_b1, grad_b2: gradients of matrices and biases
            ### START CODE HERE (Replace instanes of 'None' with your code) ###
            # Compute l1 as W2^T (Yhat - Y)
            # Re-use it whenever you see W2^T (Yhat - Y) used to compute a gradient
            11 = np.dot(W2.T,(yhat-y))
            # Apply relu to 11
            11 = np.max(0,11)
            # Compute the gradient of W1
            grad_W1 = (1/batch_size)*np.dot(l1,x.T)
            # Compute the gradient of W2
            grad_W2 = (1/batch_size)*np.dot(yhat-y,h.T)
            # Compute the gradient of b1
            grad_b1 = np.sum((1/batch_size)*np.dot(11,x.T),axis=1,keepdims=True)
            # Compute the gradient of b2
            grad b2 = np.sum((1/batch size)*np.dot(yhat-y,h.T),axis=1,keepdims=True)
            ### END CODE HERE ###
           return grad_W1, grad_W2, grad_b1, grad_b2
In []: # Test the function
       tmp C = 2
        tmp N = 50
        tmp_batch_size = 4
        tmp_word2Ind, tmp_Ind2word = get_dict(data)
        tmp_V = len(word2Ind)
        # get a batch of data
        tmp_x, tmp_y = next(get_batches(data, tmp_word2Ind, tmp_V,tmp_C, tmp_batch_size))
       print("get a batch of data")
       print(f"tmp_x.shape {tmp_x.shape}")
       print(f"tmp_y.shape {tmp_y.shape}")
       print()
       print("Initialize weights and biases")
        tmp_W1, tmp_W2, tmp_b1, tmp_b2 = initialize_model(tmp_N,tmp_V)
       print(f"tmp_W1.shape {tmp_W1.shape}")
        print(f"tmp_W2.shape {tmp_W2.shape}")
       print(f"tmp_b1.shape {tmp_b1.shape}")
       print(f"tmp_b2.shape {tmp_b2.shape}")
       print()
```

```
print("Forwad prop to get z and h")
tmp_z, tmp_h = forward_prop(tmp_x, tmp_W1, tmp_W2, tmp_b1, tmp_b2)
print(f"tmp_z.shape: {tmp_z.shape}")
print(f"tmp_h.shape: {tmp_h.shape}")
print()
print("Get yhat by calling softmax")
tmp_yhat = softmax(tmp_z)
print(f"tmp_yhat.shape: {tmp_yhat.shape}")
tmp_m = (2*tmp_C)
tmp_grad_W1, tmp_grad_W2, tmp_grad_b1, tmp_grad_b2 = back_prop(tmp_x, tmp_yhat, tmp_y,
print()
print("call back_prop")
print(f"tmp_grad_W1.shape {tmp_grad_W1.shape}")
print(f"tmp_grad_W2.shape {tmp_grad_W2.shape}")
print(f"tmp_grad_b1.shape {tmp_grad_b1.shape}")
print(f"tmp_grad_b2.shape {tmp_grad_b2.shape}")
```

Expected output

```
get a batch of data
tmp_x.shape (5778, 4)
tmp_y.shape (5778, 4)
Initialize weights and biases
tmp_W1.shape (50, 5778)
tmp_W2.shape (5778, 50)
tmp_b1.shape (50, 1)
tmp_b2.shape (5778, 1)
Forwad prop to get z and h
tmp_z.shape: (5778, 4)
tmp_h.shape: (50, 4)
Get yhat by calling softmax
tmp_yhat.shape: (5778, 4)
call back_prop
tmp_grad_W1.shape (50, 5778)
tmp_grad_W2.shape (5778, 50)
tmp_grad_b1.shape (50, 1)
tmp_grad_b2.shape (5778, 1)
```

Gradient Descent

Exercise 05 Now that you have implemented a function to compute the gradients, you will implement batch gradient descent over your training set.

Hint: For that, you will use initialize_model and the back_prop functions which you just created (and the compute_cost function). You can also use the provided get_batches helper function:

```
for x, y in get_batches(data, word2Ind, V, C, batch_size):
  Also: print the cost after each batch is processed (use batch size = 128)
In [ ]: # UNQ_C5 (UNIQUE CELL IDENTIFIER, DO NOT EDIT)
        # GRADED FUNCTION: gradient_descent
        def gradient_descent(data, word2Ind, N, V, num_iters, alpha=0.03):
            ,,,
            This is the gradient_descent function
              Inputs:
                data:
                          text
                word2Ind: words to Indices
                           dimension of hidden vector
                V:
                           dimension of vocabulary
                num_iters: number of iterations
             Outputs:
                W1, W2, b1, b2: updated matrices and biases
            111
            W1, W2, b1, b2 = initialize_model(N,V, random_seed=282)
            batch size = 128
            iters = 0
            for x, y in get_batches(data, word2Ind, V, C, batch_size):
                ### START CODE HERE (Replace instances of 'None' with your own code) ###
                # Get z and h
                z, h = forward_prop(x, W1, W2, b1, b2)
                # Get yhat
                yhat = softmax(z)
                # Get cost
                cost = compute_cost(y, yhat, batch_size)
                if ( (iters+1) % 10 == 0):
                    print(f"iters: {iters + 1} cost: {cost:.6f}")
                # Get gradients
                grad_W1, grad_W2, grad_b1, grad_b2 = back_prop(x, yhat, y, h, W1, W2, b1, b2,
                # Update weights and biases
                W1 -= alpha*grad_W1
                W2 -= alpha*grad_W2
                b1 -= alpha*grad_b1
                b2 -= alpha*grad_b2
                ### END CODE HERE ###
```

```
iters += 1
    if iters == num_iters:
        break
    if iters % 100 == 0:
        alpha *= 0.66

    return W1, W2, b1, b2

In []: # test your function
    C = 2
    N = 50
    word2Ind, Ind2word = get_dict(data)
    V = len(word2Ind)
    num_iters = 150
    print("Call gradient_descent")
    W1, W2, b1, b2 = gradient_descent(data, word2Ind, N, V, num_iters)
```

Expected Output

```
iters: 10 cost: 0.789141
iters: 20 cost: 0.105543
iters: 30 cost: 0.056008
iters: 40 cost: 0.028868
iters: 50 cost: 0.023237
iters: 70 cost: 0.019444
iters: 80 cost: 0.016716
iters: 90 cost: 0.014660
iters: 100 cost: 0.012133
iters: 110 cost: 0.012133
iters: 120 cost: 0.011370
iters: 130 cost: 0.010100
iters: 140 cost: 0.010100
iters: 150 cost: 0.009566
```

Your numbers may differ a bit depending on which version of Python you're using. ## 3.0 Visualizing the word vectors

In this part you will visualize the word vectors trained using the function you just coded above.

```
X = embs[idx, :]
    print(X.shape, idx) # X.shape: Number of words of dimension N each
In []: result= compute_pca(X, 2)
    pyplot.scatter(result[:, 0], result[:, 1])
    for i, word in enumerate(words):
        pyplot.annotate(word, xy=(result[i, 0], result[i, 1]))
    pyplot.show()
```

You can see that man and king are next to each other. However, we have to be careful with the interpretation of this projected word vectors, since the PCA depends on the projection – as shown in the following illustration.