

13/10/25

Lab - 7

Unification AlgorithmAlgorithm: Unify.

Solve the following

ii) Find Most General Unifier (MGU) of $\{Q(a, g(x, a), f(x))$
and $Q(a, g(f(b), a), x)\}$

Sol $\Rightarrow a = a$

$$g(x, a) = g(f(b), a) \rightarrow x = f(b)$$

$$f(x) = x$$

~~$$\{x/f(b), f(y)/x\}$$~~

$$x \rightarrow f(b)$$

$$y \rightarrow b$$

$$\text{MGU: } \{x/f(b), y/b\}$$

iii) Find MGU of $\{f(f(a), g(y)), f(x, x)\}$

$$f(a) = x$$

$$g(y) = x$$

 $\therefore f$ and g are different, so no unifier existsiv) unify $\{\text{prime}(11)$ and $\text{prime}(y)\}$

$$\text{prime}(11) = \text{prime}(y)$$

~~$$y = 11$$~~
$$y = 11$$

$$\text{MGU: } \{y/11\}$$

v) unify: $\{ \text{knows}(\text{John}, x), \text{knows}(y, \text{mother}(y)) \}$
 $\text{knows}(\text{John}) = y$
 $y = \text{John} \rightarrow \text{John} = y$

$\text{knows}(x) = \text{knows}(\text{mother}(y))$
 $x = \text{mother}(\text{John})$
 MGU: $\{ y/\text{John}, x/\text{mother}(\text{John}) \}$

vi) unify: $\{ \text{knows}(\text{John}, x), \text{knows}(y, \text{Bill}) \}$
 $\text{knows}(\text{John}) = \text{knows}(y)$
 $y = \text{John}$

$\text{knows}(x) = \text{knows}(\text{Bill})$
 $x = \text{Bill}$
 MGU: $\{ y/\text{John}, x/\text{Bill} \}$

i) Find MGU of $\{ p(b, x, f(g(z))) \}$ and $p(z, f(y), f(y))$
 $b = z \rightarrow z = b$

$x \rightarrow f(y)$
 $f(g(z)) = f(y) \rightarrow g(z) = y$
 MGU: $\{ z/b, x/f(y), y/g(z) \}$

Algorithm

Algorithm: unify(ψ_1, ψ_2)

Step 1: If ψ_1 or ψ_2 is a variable or constant, then:

- If ψ_1 or ψ_2 are identical, then return NIL
- Else if ψ_1 is a variable,
 - then if ψ_1 occurs in ψ_2 , then return FAILURE

b. Else return $\{(\psi_2/\psi_1)\}$

c) Else if ψ_2 is a variable,
a. If ψ_2 occurs in ψ_1 then return FAILURE,
b. Else return $\{(\psi_1/\psi_2)\}$

d) Else return FAILURE

step 2: If the initial Predicate symbol in ψ_1 and ψ_2 are not same, then return FAILURE

step 3: IF ψ_1 and ψ_2 have a different number of arguments, then return FAILURE

step 4: Set substitution set (SUBST) to NIL

step 5: For $i=1$ to the number of elements in ψ_1 ,

a) Call unify function with the i th element of ψ_1 and i th element of ψ_2 , and put the result into s

b) If $s = \text{failure}$ then returns Failure

c) If $s \neq \text{NIL}$ then do,

a. Apply s to the remainder of both $L1$ and $L2$

b. $\text{SUBST} = \text{APPEND}(s, \text{SUBST})$

step 6: Return SUBST

output (i)

MGU: $\{ 'b': 'z', 'x': ('f', 'y'), 'y': ('g', 'z') \}$