

Nature-inspired computing

- Nature has always served as a source of inspiration for engineers and scientists
- The best problem solver known in nature is:
 - **the (human) brain** that created “the wheel, New York, wars and so on” (after Douglas Adams’ Hitch-Hikers Guide)
 - **the evolution mechanism** that created the human brain (after Darwin’s Origin of Species)
- Answer 1 → neurocomputing
 - Today
- Answer 2 → evolutionary computing
 - Weeks 7 + 8

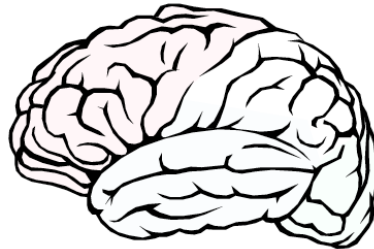
Presentation Outline

- Artificial Neural Networks
 - Perceptron
 - Perceptron Training Algorithm
 - Back Propagation
- Deep Learning

Supervised Learning using Artificial Neural Networks

Neural Networks

- Human brain consists of around 86 billion interconnected “neurons”
- Each neuron is connected to about 1000+ neighbouring neurons
- Each neuron responds to stimuli and passes output to other neurons
- In ML, artificial neural networks are loosely modelled on the human brain



Biological Networks of Neurons

- A neuron receives inputs (electrochemical signals) from its neighbours
- If enough inputs are received at the same time, it gets *activated*
- Once activated, a neuron fires, giving an output that may (in turn) activate connected neurons
- The behaviour of a biological network of neurons is dependent on connection types and activation strength (*synaptic function*)

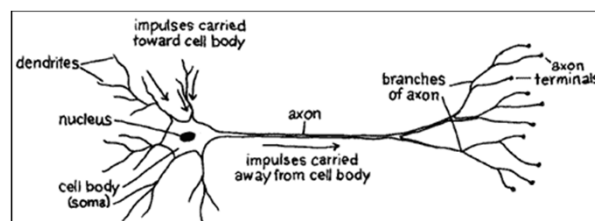


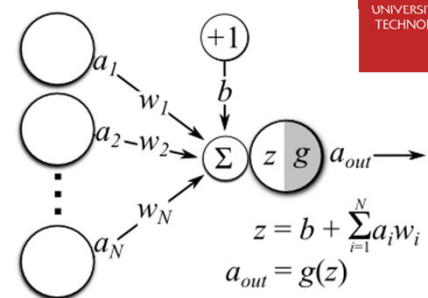
Image Source: <https://science.education.nih.gov/supplements/webversions/BrainAddiction/guide/lesson2-1.html>

Artificial Neural Networks

- Loosely modelled on the brain
- Consist of many processing units (neurons) connected together.
- As a collection, they have sophisticated behaviour
 - “Connectionist model” – emergent process of interconnected networks of simple units,
 - “Parallel distributed processing”
- Many different kinds of neural networks exist
- Mainly used for learning & reasoning
- Can be treated as a *black-box* for inputs and outputs

Artificial Neuron

- A neuron has a bunch of weighted inputs (take inputs $a_1, a_2 \dots a_n$ and multiply by the weight $w_1, w_2, \dots w_n$)
- A bias is then added to the total (as a control parameter)
- If final result is greater than a threshold, then the **activation function** is used to compute the output
 - Strength of output depends upon the activation function chosen
- The output is then fed to other neurons
- The weights and bias are determined through **training** (i.e., the ANN **learns** a **model**)

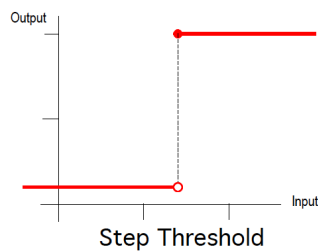


<https://theclevermachine.wordpress.com/2014/09/11/a-gentle-introduction-to-artificial-neural-networks/>

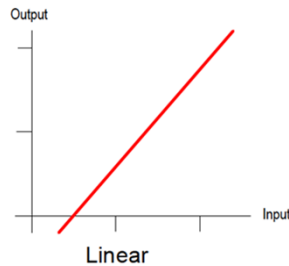
Activation Functions

- step, linear, sigmoid, tanH, Gaussian, ReLU

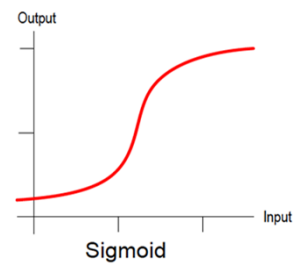
$$y = \begin{cases} A_1, & \text{if } w \cdot x + b > 0 \\ A_0, & \text{otherwise} \end{cases}$$



$$y = \sum_{i=1}^N x_i w_i$$

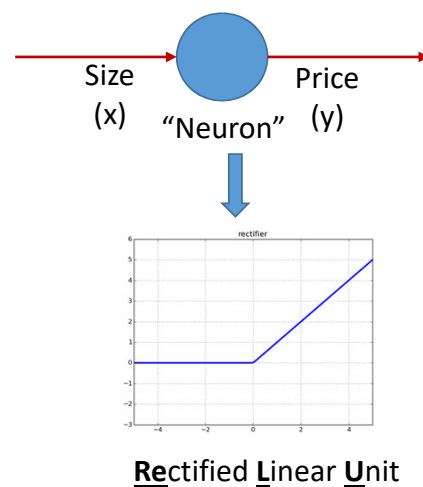
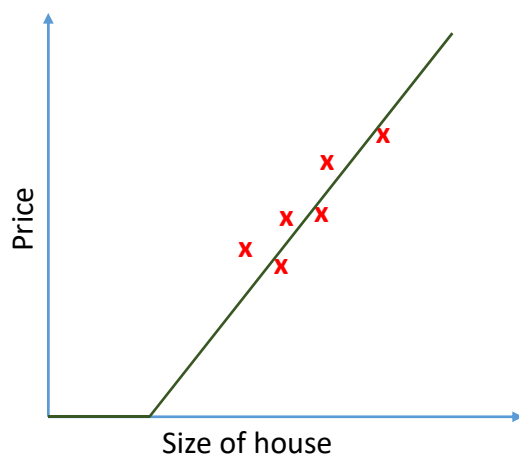


$$y = \frac{1}{1 + e^{-x}}$$



Learn more about activation functions - <https://medium.com/the-theory-of-everything/understanding-activation-functions-in-neural-networks-9491262884e0>

Price Prediction –Single Neuron

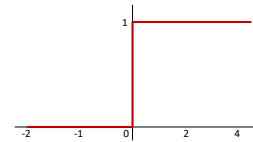


Perceptron

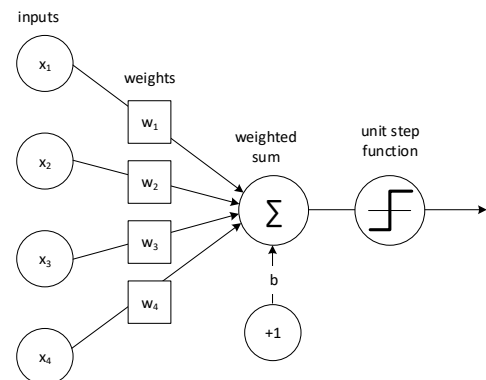
- Simplest neural network possible
- Single neuron that performs binary classification
- Uses a *step activation function*
 - Also referred to as *Heaviside Step Function*

$$f(x) = \begin{cases} 1, & \text{if } w \cdot x + b > t \\ 0, & \text{otherwise} \end{cases}$$

where $w \cdot x$ is the dot product $\sum_{i=1}^N x_i w_i$ and t is the threshold



Step Activation Function

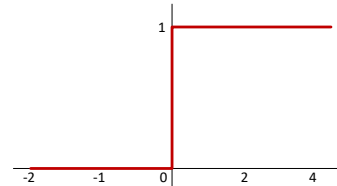


Training a Perceptron

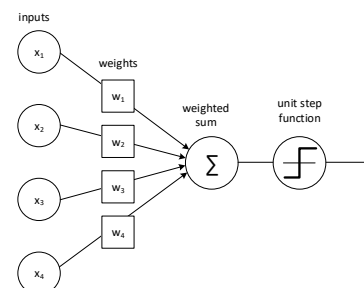
- Initialize model with random weights (usually between -0.5 and 0.5)
- Iteratively adjust weights on the basis of training examples that pair inputs with targets
- Modify weights at each step according to the perceptron training rule

$$w_i \leftarrow w_i + \alpha(t - o) * x_i$$

where t = target output, o = observed output, α = learning rate, and x_i = input

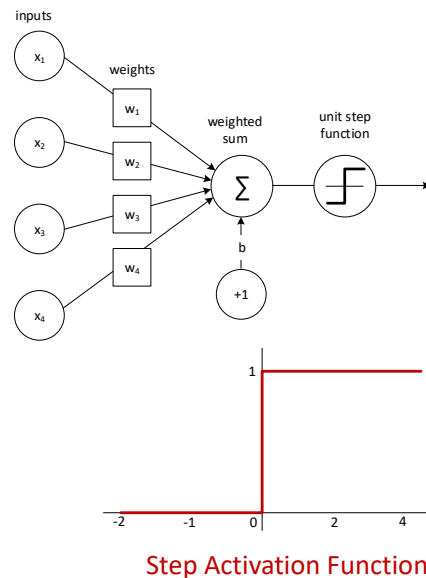


Step Activation Function



Training a Perceptron

- Randomly initialise all weights
- **Loop** through training set
 - If *actual output* is 1 and *target output* is 0 (**false positive**), decrement active weights
 - If *actual output* is 0 and *target output* is 1 (**false negative**), increment active weights
- **Until** Network gives the correct outputs (or some time/step limit is exceeded)
- The perceptron training rule will converge if the training set is linearly separable



Prediction using Perceptron

Old Training Data						
#	Student	HD (2010)	Male	Works Hard	Drinks	HD (2011)
1	Bob	yes	yes	no	yes	No
2	Howard	yes	yes	yes	no	Yes
3	Natasha	yes	no	yes	yes	Yes
4	Bush	no	yes	no	yes	No
5	Blair	no	yes	yes	yes	No
6	Mary	no	no	yes	no	Yes

New Test Data						
1	Tony	yes	yes	yes	no	?

- Can we predict the grade of a student based on historical data?
 - Learn using the example data where input and expected output is known
 - Adjust weights of active connections if the expected output does not match input

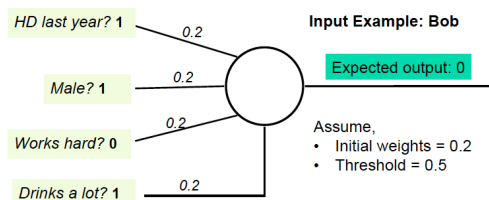
Training the Perceptron (1) - Bob

Old Training Data

#	Student	HD (2010)	Male	Works Hard	Drinks	HD (2011)
1	Bob	yes	yes	no	yes	No
2	Howard	yes	yes	yes	no	Yes
3	Natasha	yes	no	yes	yes	Yes
4	Bush	no	yes	no	yes	No
5	Blair	no	yes	yes	yes	No
6	Mary	no	no	yes	no	Yes

New Test Data

1	Tony	yes	yes	yes	no	?
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- Initial weights = 0.2, Threshold = 0.5
- Start with the first record in the training set
- Weighted sum = $(0.2 * 1 + 0.2 * 1 + 0.2 * 0 + 0.2 * 1) = 0.6$
- Check weighted sum against threshold
- Since $0.6 > \text{threshold } (0.5)$, Output = 1 (**Incorrect**)
- Hence, weights need to be adjusted

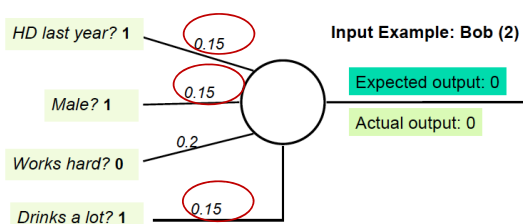
Training the Perceptron (2) - Bob

Old Training Data

#	Student	HD (2010)	Male	Works Hard	Drinks	HD (2011)
1	Bob	yes	yes	no	yes	No
2	Howard	yes	yes	yes	no	Yes
3	Natasha	yes	no	yes	yes	Yes
4	Bush	no	yes	no	yes	No
5	Blair	no	yes	yes	yes	No
6	Mary	no	no	yes	no	Yes

New Test Data

1	Tony	yes	yes	yes	no	?
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- Update the active connection weights
 - **Decrement weight by 0.05** (domain dependent)
- Weighted sum = $0.15 + 0.15 + 0 + 0.15 = 0.45$
- Since $0.45 < \text{threshold } (0.5)$, Output = 0 (**Correct**)
- Hence, weights do not need any further adjustments
- Perceptron is able to correctly predict the output for the first record

Training the Perceptron (3) - Howard

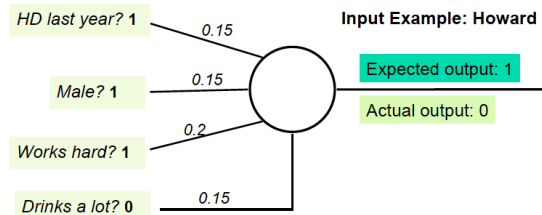
- Train the perceptron using new training data
- Weighted sum $(0.15 + 0.15 + 0.2) = 0.5$
- $0.5 < \text{threshold } (0.5)$, Output = 0 (**Incorrect**)
- **Active weights need adjustment**

Old Training Data

#	Student	HD (2010)	Male	Works Hard	Drinks	HD (2011)
1	Bob	yes	yes	no	yes	No
2	Howard	yes	yes	yes	no	Yes
3	Natasha	yes	no	yes	yes	Yes
4	Bush	no	yes	no	yes	No
5	Blair	no	yes	yes	yes	No
6	Mary	no	no	yes	no	Yes

New Test Data

1	Tony	yes	yes	yes	no	?
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Training the Perceptron (4) - Howard

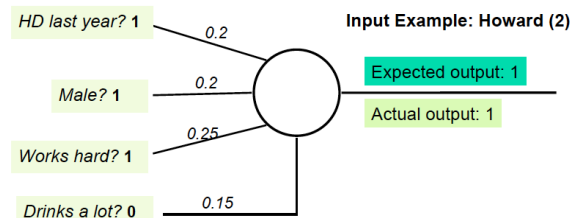
- **Increasing weights of active connections by 0.05**
- Weighted sum $(0.2 + 0.2 + 0.25) = 0.65$
- $0.65 > \text{threshold } (0.5)$, Output = 1 (**Correct**)
- Weights do not need any further adjustments

Old Training Data

#	Student	HD (2010)	Male	Works Hard	Drinks	HD (2011)
1	Bob	yes	yes	no	yes	No
2	Howard	yes	yes	yes	no	Yes
3	Natasha	yes	no	yes	yes	Yes
4	Bush	no	yes	no	yes	No
5	Blair	no	yes	yes	yes	No
6	Mary	no	no	yes	no	Yes

New Test Data

1	Tony	yes	yes	yes	no	?
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Training the Perceptron (5) - Natasha

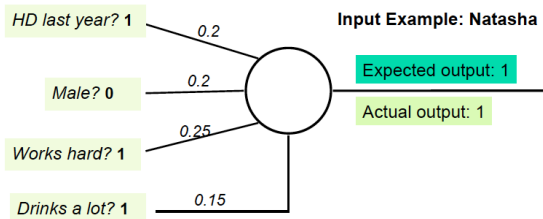
- Weighted sum $(0.2 + 0 + 0.25 + 0.25) = 0.6$
- $0.6 > \text{threshold } (0.5)$, Output = 1 (**Correct**)
- Weights are left unchanged**

Old Training Data

#	Student	HD (2010)	Male	Works Hard	Drinks	HD (2011)
1	Bob	yes	yes	no	yes	No
2	Howard	yes	yes	yes	no	Yes
3	Natasha	yes	no	yes	yes	Yes
4	Bush	no	yes	no	yes	No
5	Blair	no	yes	yes	yes	No
6	Mary	no	no	yes	no	Yes

New Test Data

1	Tony	yes	yes	yes	no	?
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Training the Perceptron (6) - Bush

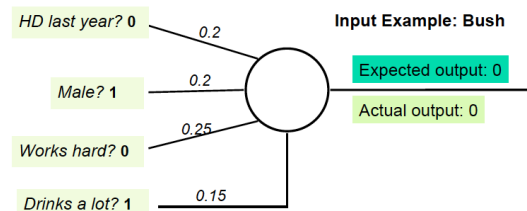
- Weighted sum $(0 + 0.2 + 0 + 0.15) = 0.35$
- $0.35 < \text{threshold } (0.5)$, Output = 0 (**Correct**)
- Weights are left unchanged**

Old Training Data

#	Student	HD (2010)	Male	Works Hard	Drinks	HD (2011)
1	Bob	yes	yes	no	yes	No
2	Howard	yes	yes	yes	no	Yes
3	Natasha	yes	no	yes	yes	Yes
4	Bush	no	yes	no	yes	No
5	Blair	no	yes	yes	yes	No
6	Mary	no	no	yes	no	Yes

New Test Data

1	Tony	yes	yes	yes	no	?
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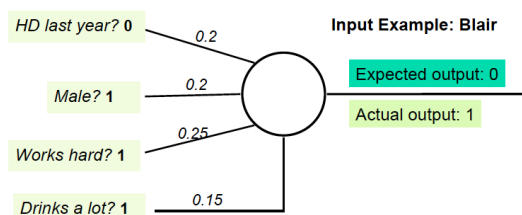


Training the Perceptron (7) - Blair

- Weighted sum ($0 + 0.2 + 0.25 + 0.15$) = 0.6
- $0.6 > \text{threshold } (0.5)$, Output = 1 (**Incorrect**)
- **Weights need to be changed**

Old Training Data						
#	Student	HD (2010)	Male	Works Hard	Drinks	HD (2011)
1	Bob	yes	yes	no	yes	No
2	Howard	yes	yes	yes	no	Yes
3	Natasha	yes	no	yes	yes	Yes
4	Bush	no	yes	no	yes	No
5	Blair	no	yes	yes	yes	No
6	Mary	no	no	yes	no	Yes

New Test Data						
1	Tony	yes	yes	yes	no	?

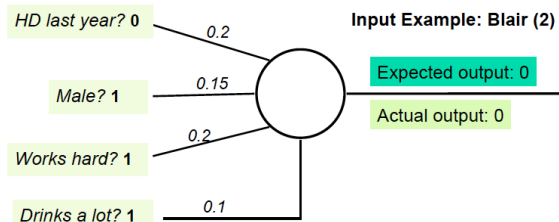


Training the Perceptron (8) - Blair

- New weights - 0.2, 0.15, 0.2, 0.1
- Weighted sum ($0 + 0.15 + 0.2 + 0.1$) = 0.45
- $0.45 < \text{threshold } (0.5)$, Output = 0 (**Correct**)
- **Weights need not be changed**

Old Training Data						
#	Student	HD (2010)	Male	Works Hard	Drinks	HD (2011)
1	Bob	yes	yes	no	yes	No
2	Howard	yes	yes	yes	no	Yes
3	Natasha	yes	no	yes	yes	Yes
4	Bush	no	yes	no	yes	No
5	Blair	no	yes	yes	yes	No
6	Mary	no	no	yes	no	Yes

New Test Data						
1	Tony	yes	yes	yes	no	?



Training the Perceptron (9) - Mary

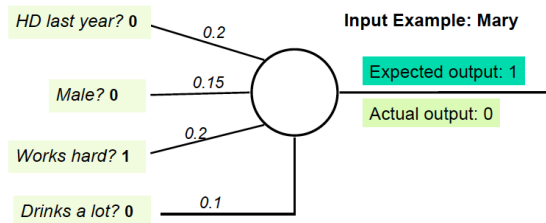
- Weighted sum $(0 + 0 + 0.2 + 0) = 0.2$
- $0.2 < \text{threshold } (0.5)$, Output = 0 (**Incorrect**)
- Weights need to be changed (for 'works hard')**

Old Training Data

#	Student	HD (2010)	Male	Works Hard	Drinks	HD (2011)
1	Bob	yes	yes	no	yes	No
2	Howard	yes	yes	yes	no	Yes
3	Natasha	yes	no	yes	yes	Yes
4	Bush	no	yes	no	yes	No
5	Blair	no	yes	yes	yes	No
6	Mary	no	no	yes	no	Yes

New Test Data

1	Tony	yes	yes	yes	no	?
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Training the Perceptron (10) - Mary

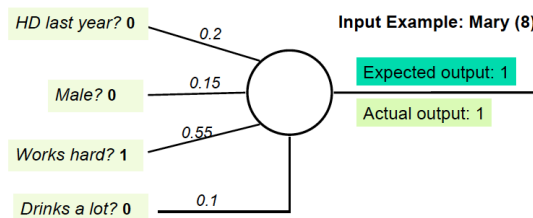
- After multiple adjustments, the weight for "Works hard" is set to 0.55
- $0.55 < \text{threshold } (0.5)$, Output = 1 (**Correct**)
- Weights need not be changed any more**

Old Training Data

#	Student	HD (2010)	Male	Works Hard	Drinks	HD (2011)
1	Bob	yes	yes	no	yes	No
2	Howard	yes	yes	yes	no	Yes
3	Natasha	yes	no	yes	yes	Yes
4	Bush	no	yes	no	yes	No
5	Blair	no	yes	yes	yes	No
6	Mary	no	no	yes	no	Yes

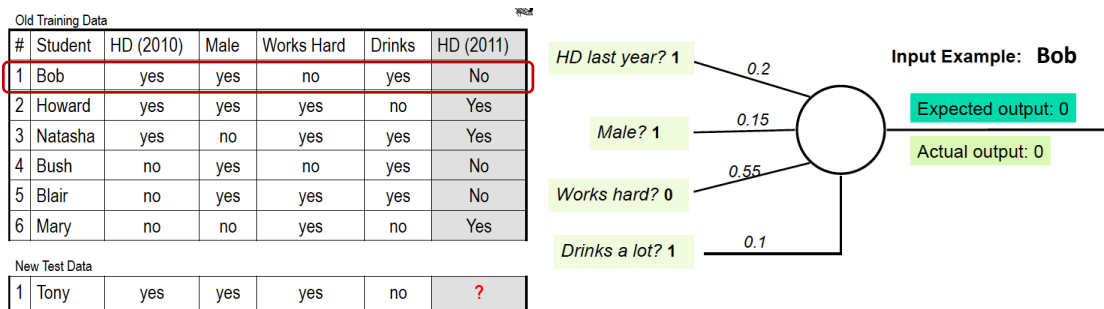
New Test Data

1	Tony	yes	yes	yes	no	?
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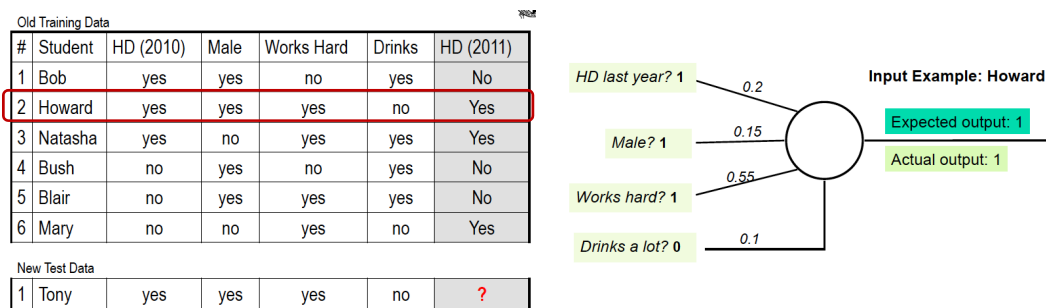
Training the Perceptron (11) - Bob

- The process is repeated starting with Bob again
Weighted sum $(0.2 + 0.15 + 0.1) = 0.45$
- $0.45 < \text{threshold } (0.5)$, Output = 0 (**Correct**)
- Process is repeated until sufficient accuracy has been achieved**



Training the Perceptron (12) - Howard

- We test the perceptron with Howard
Weighted sum $(0.2 + 0.15 + 0.55) = 0.9$
- $0.9 < \text{threshold } (0.5)$, Output = 1 (**Correct**)



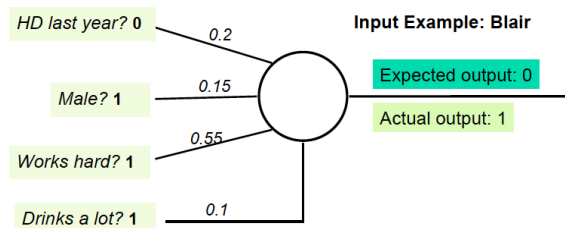
- This setting works fine for Natasha, Bush and Mary as well

Training the Perceptron (13) - Blair

- We test the perceptron with Blair
- Weighted sum ($0 + 0.15 + 0.55 + 0.1$) = 0.8
- $0.9 < \text{threshold } (0.5)$, Output = 1 (**Incorrect**)

Old Training Data						
#	Student	HD (2010)	Male	Works Hard	Drinks	HD (2011)
1	Bob	yes	yes	no	yes	No
2	Howard	yes	yes	yes	no	Yes
3	Natasha	yes	no	yes	yes	Yes
4	Bush	no	yes	no	yes	No
5	Blair	no	yes	yes	yes	No
6	Mary	no	no	yes	no	Yes

New Test Data						
1	Tony	yes	yes	yes	no	?



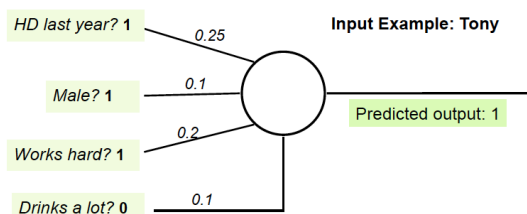
- Weights will be adjusted a lot to bring down the factor on 'Works hard'
- Eventually, the perceptron will settle down (Do we get 100% accuracy?)

Trained Perceptron - Prediction

- The trained perceptron can now predict if Tony will do well

Old Training Data						
#	Student	HD (2010)	Male	Works Hard	Drinks	HD (2011)
1	Bob	yes	yes	no	yes	No
2	Howard	yes	yes	yes	no	Yes
3	Natasha	yes	no	yes	yes	Yes
4	Bush	no	yes	no	yes	No
5	Blair	no	yes	yes	yes	No
6	Mary	no	no	yes	no	Yes

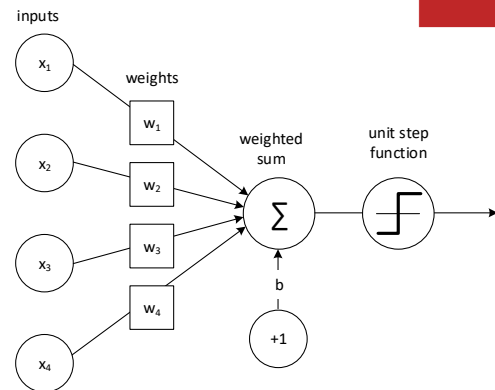
New Test Data						
1	Tony	yes	yes	yes	no	?



- Weighted sum ($0.25 + 0.1 + 0.2 + 0.1$) = 0.65
- $0.65 > \text{threshold } (0.5)$, Output = 1
- The perceptron predicts that **Tony will get a HD**

Perceptron - Summary

- Perceptron → single neuron that classifies a set of inputs into one of two categories
- Uses a step activation function
- Learning involves choosing values for the weights w_1, \dots, w_n so that the actual output o matches the target output t
- The learning procedure will converge if the data is linearly separable and a sufficiently small learning rate is used



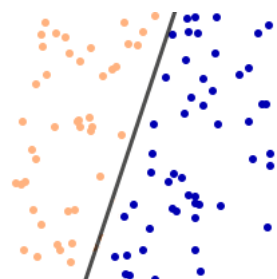
Perceptrons & Linearly Separable Regions

- Perceptrons can only classify linearly separable functions
 - The two axes are the inputs which can take values of 0 and 1
 - Numbers on the graph are the expected output for a particular input
 - AND, OR and NOT are linearly separable
- XOR is not linearly separable
- However, XOR function can be represented using a multilayer network

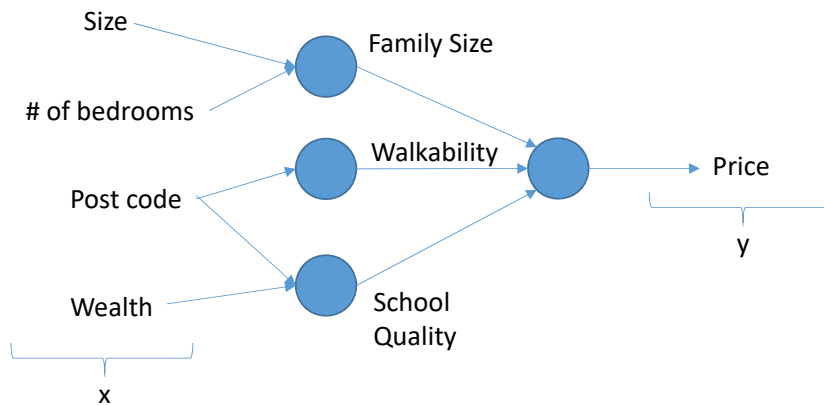
1	0	1
0	0	0
AND	0	1

1	1	0
0	1	0
NOT	0	1

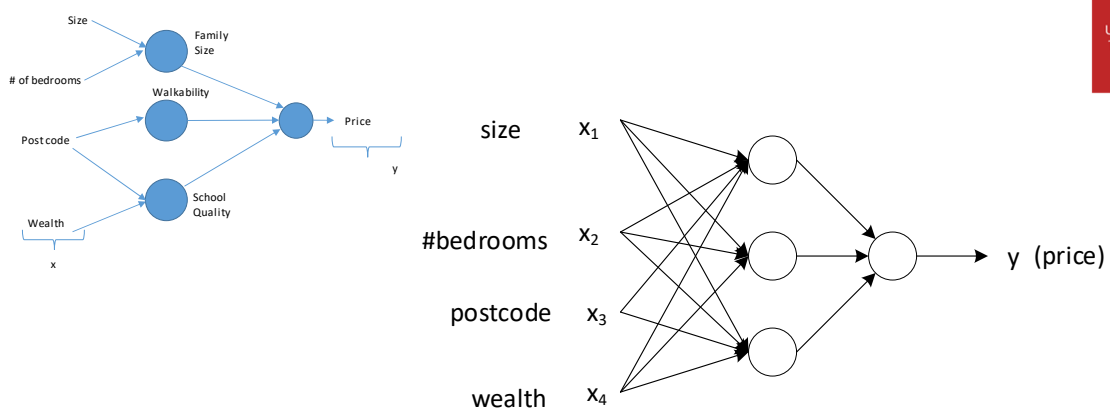
1	1	0
0	0	1
XOR	0	1



Price Prediction – Bigger Neural Network

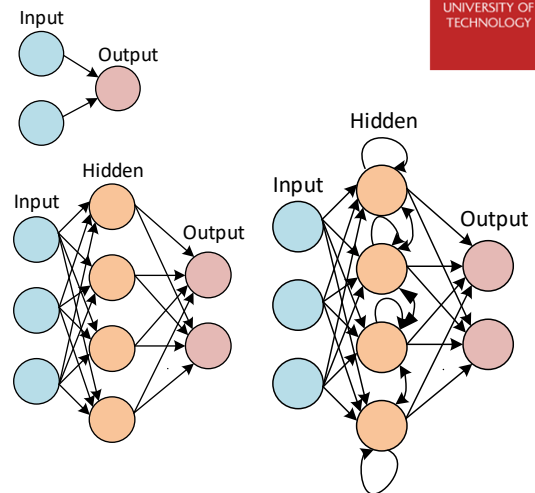


Price Prediction – Bigger Neural Network



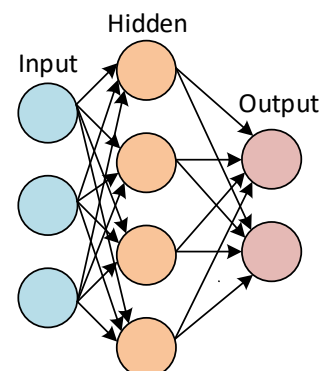
Complex Neural Network - Structures

- There are 2 main categories of neural network structures
- **Acyclic/Feed-Forward Networks** – no loops, no internal state
 - Single-layer perceptron
 - Multi-layer perceptron
- **Cyclic/Recurrent Networks** – feeds its outputs back into its own inputs, directed cycles, supports short-term memory



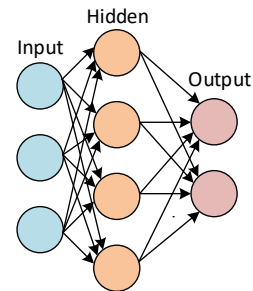
Multiple-Layer Neural Networks

- A complex neural network involves a set of neurons (e.g. perceptrons) interconnected in layers to solve more complex problems
 - Input layer neurons connect to hidden layer neurons
 - Hidden layer neurons connect to output layer neurons
 - Output layer can have multiple outputs
- Multilayer neural networks can classify a range of functions including non-linearly separable ones

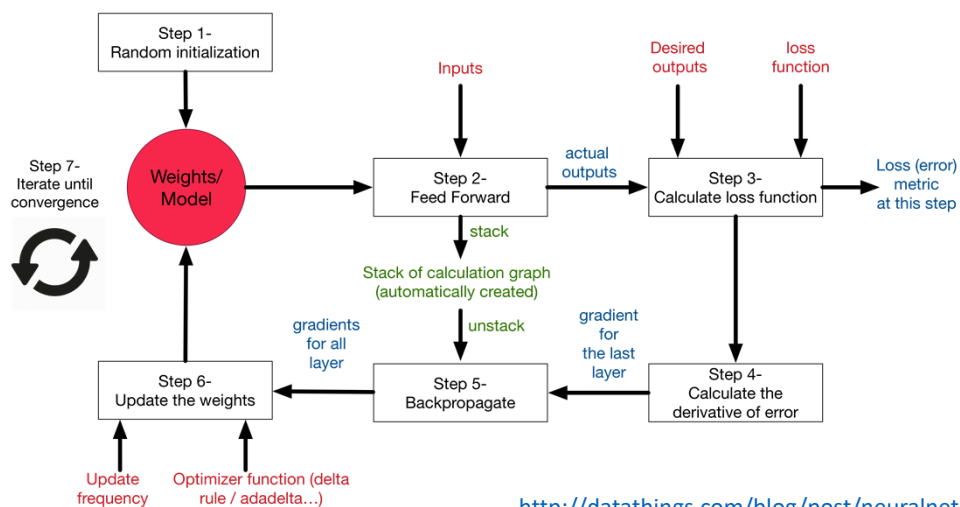


Learning in Multiple-Layer Neural Networks

- Multilayer NN learn the same way as perceptrons
- **Forward pass** – compute the values from input to output
- **Backward pass** – propagate errors backwards to adjust the connection weights
- Error occurs when expected output \neq actual output
- **Cost/Loss function** – a measure of “how good or bad” a NN did w.r.t its given training sample and the expected output



Learning in Multiple-Layer Neural Networks



Backpropagation

- An approach for training a ANN
 - used to optimize weights in a multi-layer NN so that it can learn to correctly map arbitrary inputs to outputs
 - Objective of training the network is to *minimize* value of the *cost function* by adjusting the weights

$$W := W - \alpha \frac{\partial J}{\partial W}$$

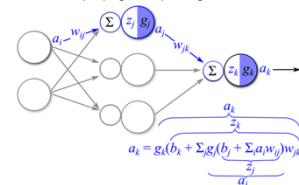
- α – learning rate, W - weight, J – cost function
- $\frac{\partial J}{\partial W}$ - Partial derivative of J w.r.t W

NOTE: partial derivative of a function of several variables is its derivate with respect to one variable keeping every other variable constant

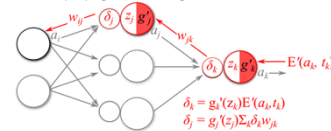
Back Propagation Algorithm

- **Feedforward** – input signals are forward propagated though the network towards the outputs
 - The output is a composite function of the weights, inputs and activation function(s)
- **Verification** - Actual output value is compared with expected output.
 - ERROR = Desired output – Actual output
- **Backpropagation** – Network errors are back propagated backwards towards to the inputs

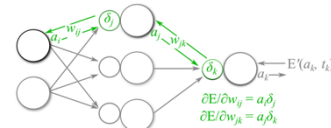
I. Forward-propagate Input Signal



II. Back-propagate Error Signals



III. Calculate Parameter Gradients



IV. Update Parameters

$$w_{ij} = w_{ij} - \eta (\partial E / \partial w_{ij})$$

$$w_{jk} = w_{jk} - \eta (\partial E / \partial w_{jk})$$

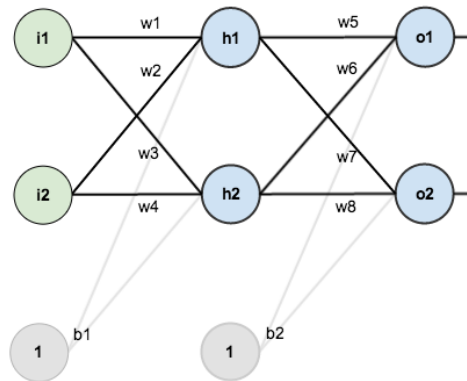
for learning rate η

<https://theclevermachine.wordpress.com/2014/09/11/a-gentle-introduction-to-artificial-neural-networks/>

Back Propagation – Step by Step Example

Neural Network Structure

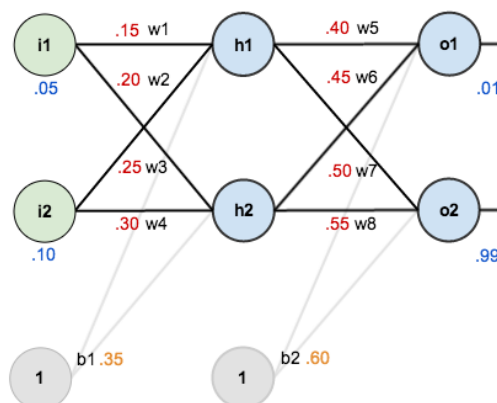
- Neural network with two inputs, two hidden neurons, and two output neurons
- Hidden and output neurons have a bias



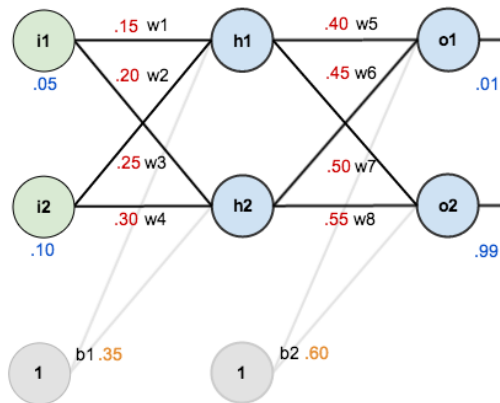
<https://mattmazur.com/2015/03/17/a-step-by-step-backpropagation-example/>

Back Propagation – Step by Step Example

Initial Weights, Biases and Training Inputs/Outputs



Back Propagation – Step by Step Example



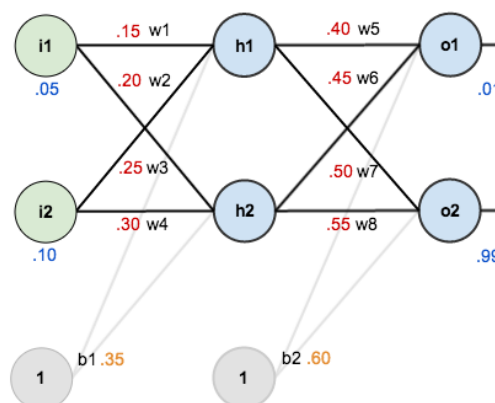
Goal of Back Propagation

- Optimize weights so that neural network can learn to correctly map arbitrary inputs to outputs
- Given the inputs 0.05 and 0.10, the neural network should output 0.01 and 0.99

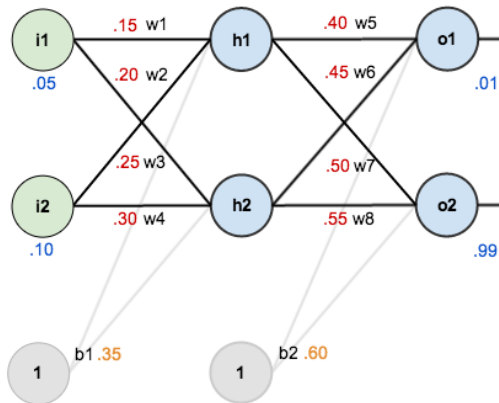
Back Propagation – Step by Step Example

Forward Pass

- Feed the inputs forward through the network
- Compute net input to each hidden neuron, apply activation function to it, repeat process with output layer neurons



Back Propagation – Step by Step Example



Forward Pass – 1:

Calculate total net input net_{h1} for $h1$

$$net_{h1} = w_1 * i_1 + w_2 * i_2 + b_1$$

$$net_{h1} = 0.15 * 0.05 + 0.2 * 0.1 + 0.35$$

$$net_{h1} = 0.3775$$

Apply activation function to calculate output out_{h1} of $h1$

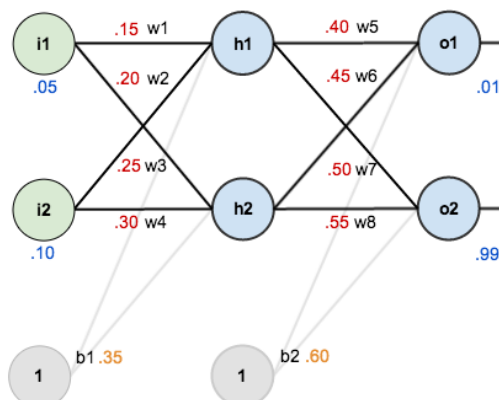
$$out_{h1} = \frac{1}{1 + e^{-net_{h1}}} \text{ (logistic function)}$$

$$= \frac{1}{1 + e^{-0.3775}} = 0.59329992$$

Do the same for h_2

$$out_{h2} = 0.596884378$$

Back Propagation – Step by Step Example



Forward Pass - 2

Calculate net input net_{o1} for $o1$

$$net_{o1} = w_5 * out_{h1} + w_6 * out_{h2} + b_2$$

$$= 0.40 * 0.59329992 + 0.45 * 0.596884378 + 0.60$$

$$= 1.105905967$$

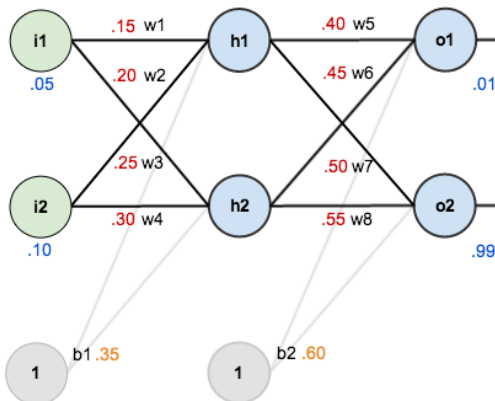
Apply activation function to calculate output out_{o1} of $o1$

$$out_{o1} = 0.75136507$$

Do the same for o_2

$$out_{o2} = 0.772928465$$

Back Propagation – Step by Step Example



Calculate Error

Calculate the total error of each output neuron using the *Squared Error Function*

$$E = \sum \frac{1}{2}(\text{target} - \text{output})^2$$

Error E_{o1} for output neuron $o1$

$$E_{o1} = \frac{1}{2}(\text{target}_{o1} - \text{out}_{o1})^2$$

$$E_{o1} = \frac{1}{2}(0.01 - 0.7514)^2$$

$$E_{o1} = 0.274811083$$

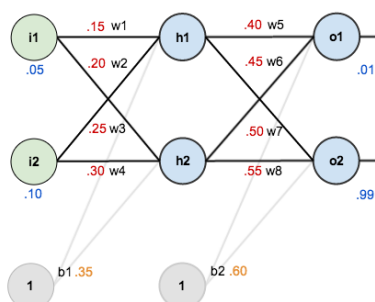
Error E_{o2} for output neuron $o2$

$$E_{o2} = 0.023560026$$

Total Error is the sum of the errors

$$E_{\text{total}} = 0.274811083 + 0.023560026 = 0.298371109$$

Back Propagation – Step by Step Example



Backward Pass

We want to determine how much a change in w_5 contributes to the total error E_{total}

$$\frac{\partial E_{\text{total}}}{\partial w_5} = \left[\frac{\partial E_{\text{total}}}{\partial \text{out}_{o1}} \right] * \frac{\partial \text{out}_{o1}}{\partial \text{net}_{o1}} * \frac{\partial \text{net}_{o1}}{\partial w_5}$$

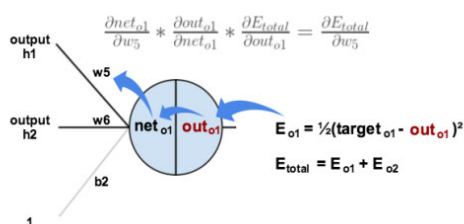
How much does the error change w.r.t out_{o1} ?

$$E_{\text{total}} = \frac{1}{2}(\text{target}_{o1} - \text{out}_{o1})^2 + \frac{1}{2}(\text{target}_{o2} - \text{out}_{o2})^2$$

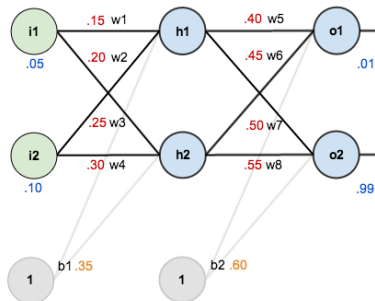
$$\frac{\partial E_{\text{total}}}{\partial \text{out}_{o1}} = 2 * \frac{1}{2} (\text{target}_{o1} - \text{out}_{o1})^{2-1} * -1 + 0$$

$$\frac{\partial E_{\text{total}}}{\partial \text{out}_{o1}} = -(\text{target}_{o1} - \text{out}_{o1})$$

$$\frac{\partial E_{\text{total}}}{\partial \text{out}_{o1}} = -(0.01 - 0.75136507) = 0.74136507$$



Back Propagation – Step by Step Example



Backward Pass

We want to determine how much a change in w_5 contributes to the total error E_{total}

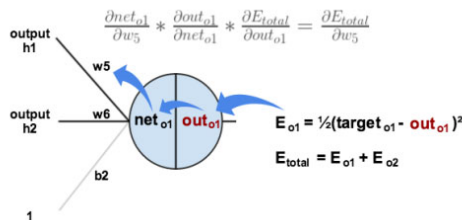
$$\frac{\partial E_{total}}{\partial w_5} = \frac{\partial E_{total}}{\partial out_{o1}} * \left[\frac{\partial out_{o1}}{\partial net_{o1}} \right] * \frac{\partial net_{o1}}{\partial w_5}$$

How much does the output out_{o1} change w.r.t net_{o1} ?

$$out_{o1} = \frac{1}{1 + e^{-net_{o1}}}$$

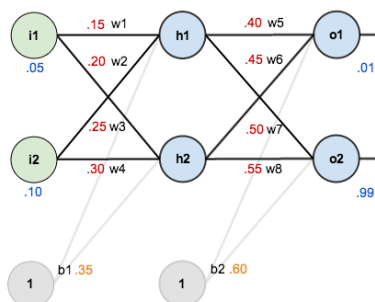
$$\frac{\partial out_{o1}}{\partial net_{o1}} = out_{o1} (1 - out_{o1}) = 0.775136507 (1 - 0.75136507)$$

$$\frac{\partial out_{o1}}{\partial net_{o1}} = 0.186815602$$



1

Back Propagation – Step by Step Example



Backward Pass

We want to determine how much a change in w_5 contributes to the total error E_{total}

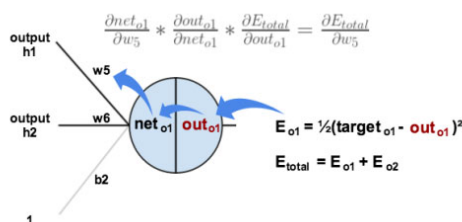
$$\frac{\partial E_{total}}{\partial w_5} = \frac{\partial E_{total}}{\partial out_{o1}} * \frac{\partial out_{o1}}{\partial net_{o1}} * \left[\frac{\partial net_{o1}}{\partial w_5} \right]$$

How much does the net input net_{o1} change w.r.t w_5 ?

$$net_{o1} = w_5 * out_{h1} + w_6 * out_{h2} + b_2 * 1$$

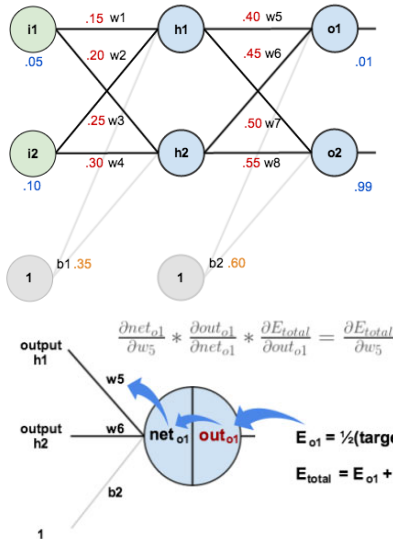
$$\frac{\partial net_{o1}}{\partial w_5} = out_{h1} + 0 + 0 = 0.593269992$$

$$\frac{\partial E_{total}}{\partial w_5} = 0.74136507 * 0.186815602 * 0.59327 = 0.082167041$$



1

Back Propagation – Step by Step Example



Update weight

Calculating new weight (using an optional learning rate α of 0.5)

$$w_5^+ = w_5 - \alpha * \frac{\partial E_{total}}{\partial w_5}$$

$$w_5^+ = 0.4 - 0.5 * 0.082167041 = 0.35891648$$

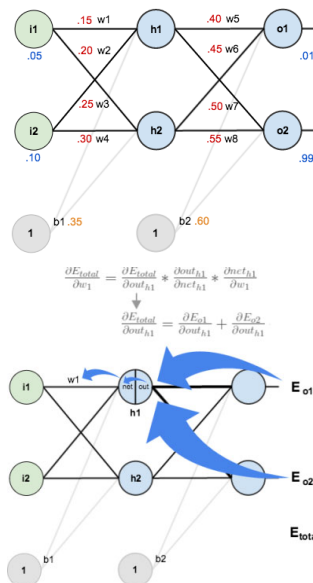
Similarly, we can calculate new weights for w_6 , w_7 and w_8

$$w_6^+ = 0.408666186$$

$$w_7^+ = 0.511301270$$

$$w_8^+ = 0.561370121$$

Back Propagation – Step by Step Example



Backward Pass - 2

We calculate the new value for the weight w_1 , w_2 , w_3 , w_4

$$\frac{\partial E_{total}}{\partial w_1} = \frac{\partial E_{total}}{\partial out_{h1}} * \frac{\partial out_{h1}}{\partial net_{h1}} * \frac{\partial net_{h1}}{\partial w_1}$$

$$\frac{\partial E_{total}}{\partial out_{h1}} = \frac{\partial E_{o1}}{\partial out_{h1}} + \frac{\partial E_{o2}}{\partial out_{h1}}$$

Skipping a few steps....

$$\frac{\partial E_{total}}{\partial w_1} = 0.036350306 * 0.241300709 * 0.05 = 0.000438568$$

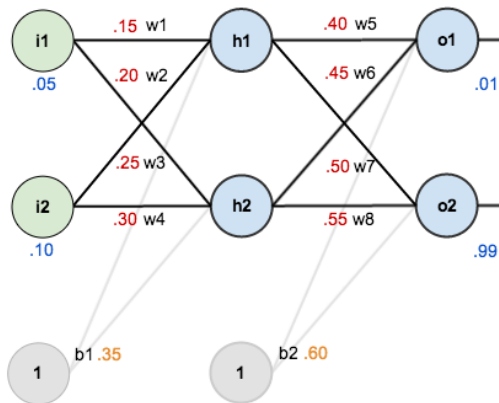
Updating the weights.... $w_1^+ = w_1 - \alpha * \frac{\partial E_{total}}{\partial w_1}$

$$w_1^+ = 0.15 - 0.5 * 0.000438568 = 0.149780716$$

$$w_2^+ = 0.19956143, \quad w_3^+ = 0.24975114$$

$$w_4^+ = 0.29950229$$

Back Propagation – Step by Step Example



- After updating all the weights, the total error of the network is reduced to **0.298371109**
- The original error was **0.291027924**
- If this process is repeated 10000 times, the error is reduced to **0.0000351085**
- At this point, the inputs of **0.05** and **0.1** produce outputs of **0.015912196** (vs 0.01 target) and **0.984065734** (vs 0.99 target)

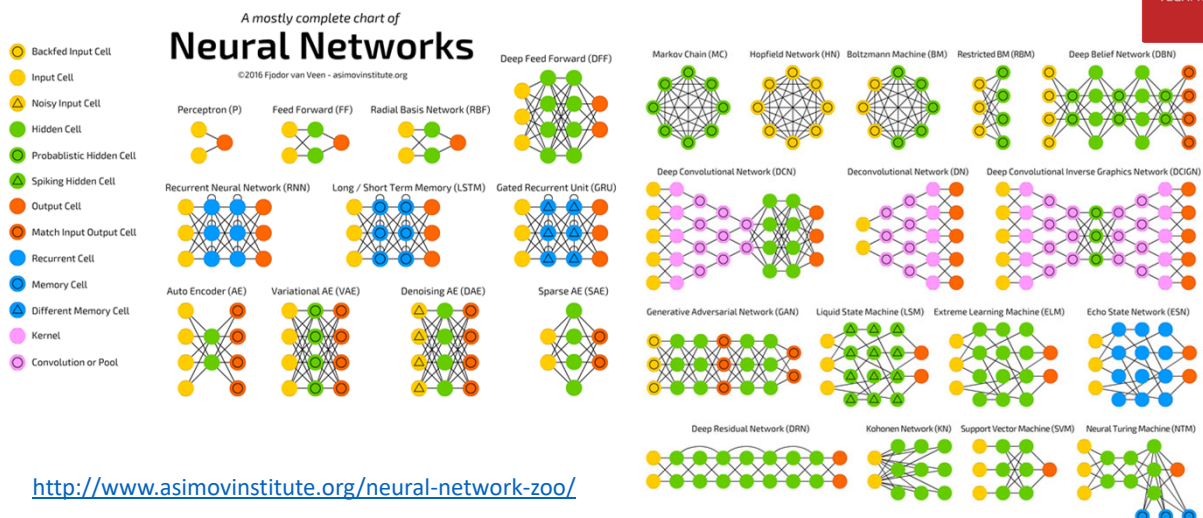
Developing a Neural Network

- Needs a fair degree of mathematical competence
- Not simple (also very time consuming)
- Considerations include:
 - Identification of features in the problem domain worth mapping into inputs/outputs (Problem Representation)
 - Determining the number of hidden layers and nodes
 - Setting up initial parameters – weights, thresholds, increments
 - What learning method to use?
- No rules exist, based on experience (and solid understanding of problem domain)

Weakness of Neural Networks

- Neural networks are *opaque* – it is very hard to check that the weights after training are sensible
- A neural network can never explain how it arrived at a particular conclusion
- Loss of human control, lack of trust since AI cannot explain all decisions and actions, or take responsibility – **Black Box AI**
- Some work is being done on combating the opacity problem
- Partnership on AI (<https://www.partnershiponai.org>) is a step towards safe and trustworthy AI technologies – supported by tech giants including Google, IBM and Microsoft

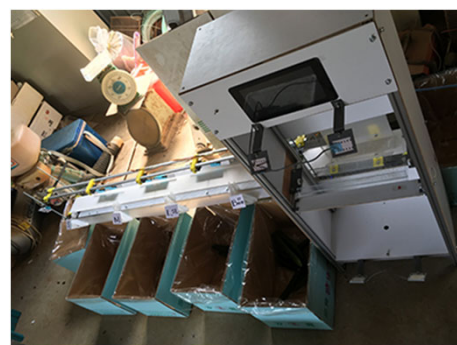
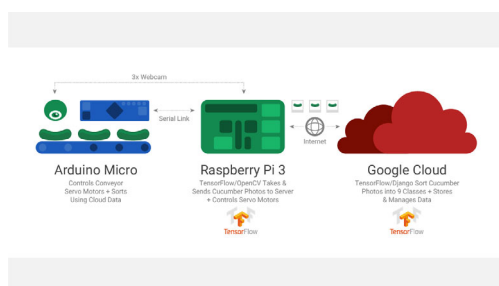
Types of Neural Networks



Machine Learning as a Service

- Machine learning is no longer for experts only
- Software developers can use cutting-edge, commercially usable machine learning frameworks
 - Scikit-learn
 - Google Tensorflow
 - PyTorch
 - Microsoft Cognitive Toolkit
 - Theano
 - Caffe
 - Deeplearning4j
- Major cloud providers including Amazon, Google and Microsoft offer machine learning as a service

Cucumber Farming & TensorFlow



- Cucumber classification into 9 different classes using Tensorflow based on size, thickness, color, texture, small scratches, whether they are crooked, whether they have prickles,

<https://cloud.google.com/blog/big-data/2016/08/how-a-japanese-cucumber-farmer-is-using-deep-learning-and-tensorflow>