

age > 40, income = low  
 +  
 want to know  $P(\text{buy?} \mid \text{age} > 40, \text{income} = \text{high})$

age	income	student	credit_rating	buys_computer
<=30	high	no	fair	no
<=30	high	no	excellent	no
31...40	high	no	fair	yes
>40	medium	no	fair	yes
>40	low	yes	fair	yes
>40	low	yes	excellent	no
31...40	low	yes	excellent	yes
<=30	medium	no	fair	no
<=30	low	yes	fair	yes
>40	medium	yes	fair	yes
<=30	medium	yes	excellent	yes
31...40	medium	no	excellent	yes
31...40	high	yes	fair	yes
>40	medium	no	excellent	no

Sol

$$P(\text{buy: Yes}) = 9/14 = 0.643$$

$$P(\text{buy: No}) = 5/14 = 0.357$$

$$P(\text{age} > 40 \mid \text{buy: Yes}) = 3/9 = 0.33$$

$$P(\text{age} > 40 \mid \text{buy: No}) = 2/5 = 0.4$$

$$P(\text{income = low} \mid \text{buy: Yes}) = 2/9 = 0.22$$

$$P(\text{income = low} \mid \text{buy: No}) = 1/5 = 0.2$$

$$P(\text{age} > 40, \text{income} = \text{low} \mid \text{buy: Yes}) = 0.0226$$

$$P(\text{age} > 40, \text{income} = \text{low} \mid \text{buy: No}) = 0.08$$

$$P(\text{buy: Yes}) \cdot P(\text{age} > 40, \text{income} = \text{low} \mid \text{buy: Yes}) = 0.0476$$

$$P(\text{buy: No}) \cdot P(\text{age} > 40, \text{income} = \text{low} \mid \text{buy: No}) = 0.028$$

## Laplacian

Sol  $P(\text{buy} \mid \text{age } 31-40, \text{income} = \text{high})$

$$P(\text{buy: Yes}) = 9/14$$

$$P(\text{buy: No}) = 5/14$$

$$P(31-40 \mid \text{buy: Yes}) = 4/9 + 3 = 5/12$$

$$P(31-40 \mid \text{buy: No}) = 1/5 + 3 = 1/8$$

$$P(\text{income high} \mid \text{buy: Yes}) = 2/9$$

$$P(\text{income high} \mid \text{buy: No}) = 2/5$$

$$P(31-40, \text{income high} \mid \text{buy: Yes}) = \frac{5}{12} \times \frac{2}{9}$$

$$P(31-40, \text{income high} \mid \text{buy: No}) = \frac{1}{8} \times \frac{2}{5}$$

$$P(\text{buy: Yes}) \cdot P(31-40, \text{income high} \mid \text{buy: Yes}) = \frac{5}{12} \times \frac{2}{9} \times \frac{9}{14} = 0.0596$$

$$P(\text{buy: No}) \cdot P(31-40, \text{income high} \mid \text{buy: No}) = \frac{1}{8} \times \frac{2}{5} \times \frac{5}{14} = 0.179$$