### DEPARTMENT OF ELECTRICAL AND ELECTRONIC ENGINEERING **EXAMINATIONS 2005**

MSc and EEE PART IV: MEng and ACGI

Corrected Copy

#### TRAFFIC THEORY & QUEUEING SYSTEMS

Thursday, 28 April 10:00 am

Time allowed: 3:00 hours

There are FIVE questions on this paper.

**Answer FOUR questions.** 

All questions carry equal marks

Any special instructions for invigilators and information for candidates are on page 1.

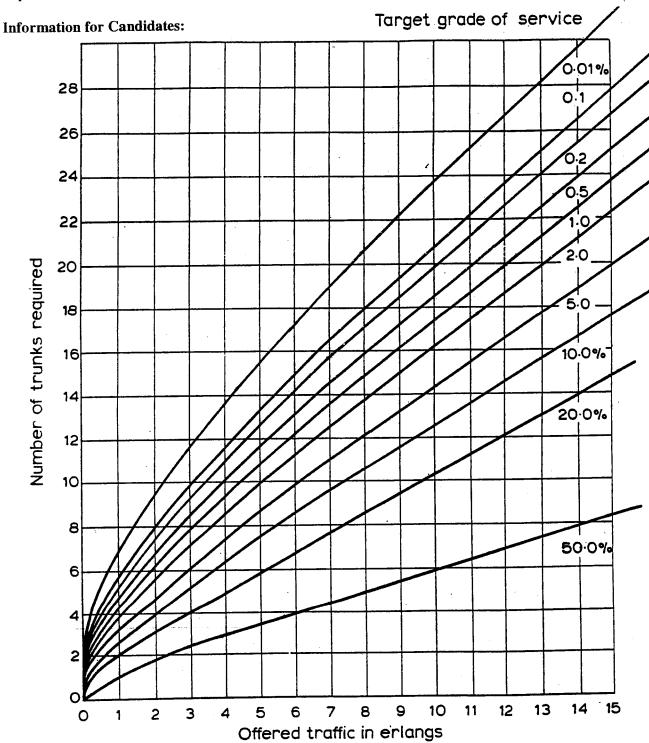
Examiners responsible

First Marker(s):

J.A. Barria

Second Marker(s): P. De Wilde

### Especial Information for Invigilators: NIL



Traffic capacity on basis of Erlang B. formula.

a)

-

- i) Describe and discuss underlying assumptions made when formulating the Erlang model.
- ii) For the case of finite capacity system derive the probability of link saturation.

[10]

- b) An N-channel link system is being offered  $\rho$  Erlangs of pure chance traffic.
  - Show that if the search for a free channel is always sequential (i.e. 1, 2, 3, ..., N) the mean occupancy of channel number j is given by

$$\eta_i = \rho [E_{i-1}(\rho) - E_i(\rho)]$$

ii) Derive the average value of the channel occupancy in part (b) i). Discuss your results.

a)

2

- i) Describe and discuss the usefulness of an Interrupted Poisson Process to describe an overflow link state.
- ii) Define and discuss an overflow link traffic model using the on-off source model of Figure 2.1.
- iii) Explain the meaning of  $\alpha$ ,  $\beta$  and  $\lambda$ .
- Derive the expressions of the global balance equations of an overflow link composed of one (1) channel.

[10]

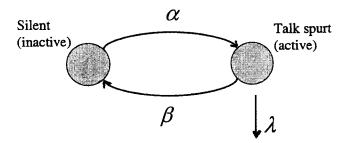


Figure 2.1.

- b) A communications link with 8 channels is grouped so that half the incoming traffic have access to the first 4 channels and the other half have access to the other 4 channels. If the total offered traffic is 8 Erlangs of pure chance traffic
  - i) Determine the call congestion of the system.
  - ii) Determine the link occupancy distribution.

3.

- a) Using mean-value analysis
  - i) Explain the meaning of and derive the expected residual time of an M/G/1 system.
  - ii) Derive the expression for the expected waiting time of an M/G/1 system.

State clearly all assumptions made. Explain clearly all steps of your derivations.

[10]

b)

- i) For a k-class priority queueing system, define and explain non-preemptive priority and pre-emptive priority mechanisms.
- ii) Explain and derive an expression for the expected transit time in a pre-emptive priority system.
- Describe and discuss a priority mechanism that would reduce the system expected waiting time (E(W)).

4

a)

- i) Explain the importance of access control in ATM networks.
- ii) The user parameter control technique proposed by the ATM forum has a number of equivalent representations. Explain the operation of one of such equivalent algorithms.
- iii) Derive a simple approximation model of an access control algorithm known to you.

[10]

- b) In an operation support system contact centre all incoming calls are handled on a delay basis by a group of 10 operators. Assume that incoming traffic is pure chance with a level of 8 Erlangs.
  - Determine the mean delay experienced by calls which are accepted but delayed for buffer capacity B = 5.
  - ii) Determine the mean delay experienced by calls which are accepted but delayed for buffer capacity B = 10.

a)

5

- i) Describe a multimedia traffic source model. Clearly define and describe all parameters of the model.
- ii) Derive and depict a Markov model representation of a N on-off source multiplexor.
- iii) Assuming that the service rate is  $\nu$  and the arrival rate of cells is  $\beta$  cells/s. Derive the maximum number of multiplexed sources that the system can cope with.

[10]

b) For the fault tolerant system represented in Figure 5.1.

Assume that the repair time and time to failure are exponentially distributed and:

 $R_p$ ; is the failure rate of each processor (assume it to be independent of the failure rate of the state of the other processors)

 $R_b$ ; is the failure rate of the data base (assume that any failure in the data base results in the loss of the entire system) and

 $j/R_r$ ; is the time to repair j faulty components

i) Obtain the Markov chain representing the fault tolerant system of Figure 5.1.

State clearly and discuss any assumptions made in your derivations.

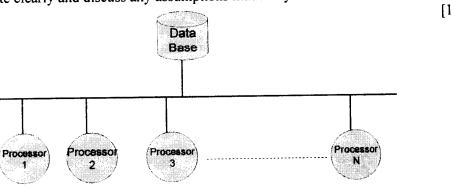


Figure 5.1:

TRAFFIC THEORY ( GUEUEING SYSTEMS 2005 2004-5 Confidential Examinations: Session MODEL ANSWER and MARKING SCHEME E405/ Paper Code First Examiner Page 1 out of 11 Question Second Examiner Marks allocations in right margin Question labels in left margin troloup hedd Assumptions The toles amos stream is a Poisson presen with it The channel helder the are meliperature exponented ice with mea holdp the of 1/1 it) The accent switch given july availability i.e with traffic source has account all the channel A For NESS P [ Link Sutreation ) = P [ No = 40] - TN = (p''h!) = Eh(p)

5

Examinations: Session Confidential MODEL ANSWER and MARKING SCHEME Paper Code First Examiner Page 2\_out of Question Second Examiner Marks allocations in right margin Question labels in left margin 100 C, -> C; - = link g size 1-1 ovalle to 19+1, --, col= p = 1 (p) Thefree bound by Cj = P[Ej-1(p)-Ej(p)] ラグニアレモューシーモックリ Average of My over all chaund Good 一方三八二十三八三十三八 = L TEO-EN) = 1 [1-130] = 4

	Examinations:	Session		Confid	ential
	MODEL ANSWER and MAI	RKING SC	HEME		·
First Ex	miner	Paper Code	D 1	out of	1
Second 1	Examiner	Question	Page 4		
Question	labels in left margin		Marks alloca	tions in right	margm
2(5)	3c = P [aurod is blodded]  = P [aurod is on A] P  + P [aurod is on A] P  = \frac{1}{2} \tag{4} + \frac{1}{3} \tag{5} \tag{6}  = \frac{1}{2} \tag{4} + \frac{1}{3} \tag{7} \tag{6}  The = P [Hr of hosy A cho  = P [Hr of hosy B ch  To = \tag{7} = 2\tag{7} \tag{7}  To = \tag{7} = 2\tag{7} \tag{7}	Call A  [all 3  4) =  than  channe  unel.	chand 0.311 h = i]	wsy	5
	$T_3' = 2(T_0T_3 + T_1T_2)$ $T_0' = (T_2)^2 + 2(T_0T_4 + T_1T_3)$				
	73 = 2 (Ti, Ta = Te T3)				
The Arithment is an arithment in the Arithment is an arithment in the Arithment in the Arithment is an arithment in the Arithment in the Arithment is an arithment in the Arithm	$\frac{76}{114} = \frac{(73)^2 + 27(2)^4}{27(3)^7}$ $\frac{76}{114} = \frac{27(3)^7}{27(4)^7}$ $= \frac{1}{27(4)^7}$				5

## Confidential Examinations: 1999 Session MODEL ANSWER and MARKING SCHEME Paper Code First Examiner Page 5 out of Question Second Examiner Marks allocations in right margin Question labels in left margin - reviewed service time = the until the first lecenture seem by the arrival څې eta - fint departure RE = periodul service tino recen my a vintral muricip at the there at equilibrium filey is a continuous time stockers or pracen which book ish The American ussuming that ERRY is Especial (in mean) E(Ce) = lin - for Redt = lim + \frac{1}{2} (\frac{1}{2} \frac{5}{12}) My = mag completed services in [0,T] HULL = Line 1: (MT) [ Tr [ 2 52]

A E(52)

EULE ) = = = 1 1 = (43)

5

# Confidential Examinations: Session MODEL ANSWER and MARKING SCHEME Paper Code First Examiner Page 6 out of Question Second Examiner Marks allocations in right margin Question labels in left margin we a waiting the found on arrival arrival m = [14 + 255] ELWI) = = [2 56] $= E(\Omega i) + E[E(\frac{Qi}{ZSi-j}|Qi)]$ $= c(\Omega i) + E[E(\frac{Qi}{ZSi-j}|Qi)]$ $= c(\Omega i) + c(\Omega i)$ $= c(\Omega i)$ $= c(\Omega i) + c(\Omega i)$ $= c(\Omega i)$ == E(N) + E(Qi) E(G) Time Poisson and old see unhand sample of quere perowiour =(W) = E(Q) + E(Q) E(G) by wittes E(Q)= ) E(H) E(W) = (R)

Examinations :	Session	Confide	ential	
MODEL ANSWER and MARKING SCHEME				
First Examiner	Paper Code	Page 7 out of		
Second Examiner	Question	Marks allocations in right	margin	
Question labels in left margin		Marks anocadons in right		
More-emptive priority:  More-emptive priority:  My higher-priority:  My higher-priority:  Pre-emptive remove remov	savice is in anived.  are 2 pess  we start  (1-0K)  i E(SK)ESi	tempted by	3	
E(Sk) = E(Sk) = E(Sk)	SK)  - JR-1  (NUK) + E(S)  the priority  the storter extends  a queue d	gure exted source	4 7	

Examinations: Session Confidential				
MODEL ANSWER and M		неме		
First Examiner	Paper Code			
Second Examiner	Question	Page 3 out of		
Question labels in left margin		Marks allocations in right mar	gin	
Agonp a cell han been a consent or each to ensure it is proceeding of accur with a proper position. It is not each accurate to a consent to the accurate to the following of the framework involves to be transported involves to be transported. It is not per D Sec, and not foll. At this tree no further treased throughout the position of positions of positions.	recensory actually represent a  control and to a  redict	to monitor generated by to the traffic  Use parameter anaperat or  technique equivalent the leading retate of a "toher" toher waite agranded hope in generated from the land		
	induced leaving	( ) that is the control of	5	

Examinations : 3	Session	Confid	ential
MODEL ANSWER as		HEME	
First Examiner	Paper Code	<b>.</b>	
Second Examiner	Question	Page $\mathcal{G}$ out of	
Question labels in left margin		Marks allocations in right	margin
$4(6)$ $\frac{2}{16}$ $$	Cond (	K=10)	
120937 = [ (1-1) p = 1	11-pa) = 12 (Kg		
$E_{k}(k_{0}) = 0.122$ $F_{k}(k_{0}) = 0.030$ $= 0.009$ $= 0.009$	= 5		5
PEQ=i) = (ifa)	)pi i =	0,1,B-1	
E (Qt   W>0). =	2.8c B=	5	
Usip little	- P[lies]	,	
= 0.10	35 See! 257 See!	B=5 B=10	
E(W(Deloy) =	E (at 1)		
	= 15 Sec = 26.5 Sec	73 = S 13 = 10	

Examinations:	Session		ential
MODEL ANSWER	and MARKING SC	HEME	
First Examiner	Paper Code Question	Page   O out of	
Second Examiner		Marks allocations in right	margin
Question labels in left margin			
Sa 1 ON-OH SOUNU			
	) Vp padreti	15.	
disassin	<i>[</i>		3
(0.1)	)	0,10	
1000		Now (Apr) D	
20 21)		1 (SID)	3
ni) kunge Alls/5	per 3571.6 =	$\int_{-\infty}^{\infty} \frac{\lambda}{\alpha + \lambda}$	
Average allest	I multiplexed.	sources = $\frac{490}{44}$	*3*
Cepacity of Sythe			
94 d		·	
	0(846)		4

