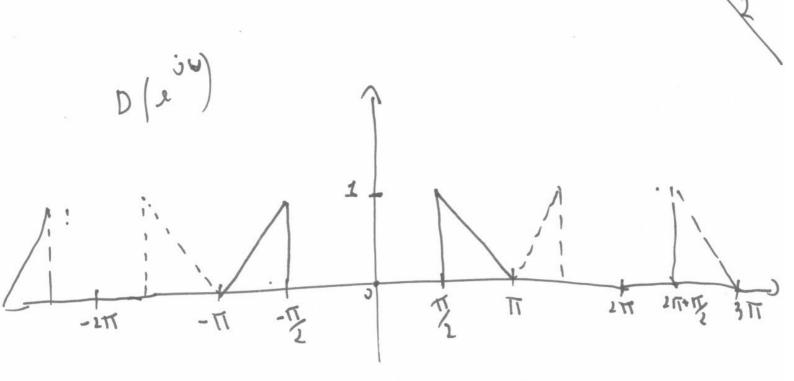
QUESTION 1 SOLUTIONS ZOOS

a)
$$C(7) = \frac{1}{2} \left[H(7^{1/2}) \chi(7^{1/2}) + H(-7^{1/2}) \chi(-7^{1/2}) \right] \frac{1}{2} \left[\frac{1}{2} \chi(7^{1/2}) + \frac{1}{2} \chi(7^{1/2}) \right] \frac$$

$$D(\underline{t}) = X(\underline{t}) - \lambda(\underline{t})$$

DEPEND ON H(7).



C) THE SYSTEM IS NOT IDEMPOTENT : PT +P

IN FACT THE SYSTEM IS IDEMPOTENT IF

THAT 15 \$[-]= x[-]

CHECK :

$$\overline{X}(z) = \left\{ H(z)C(z)X(z^{1}) \right\}_{z}^{z}$$

$$= X(\overline{z})\left(H(z^{1/2})C(z^{1/2}) + H(-z^{1/2})C(-z^{1/2})\right)$$

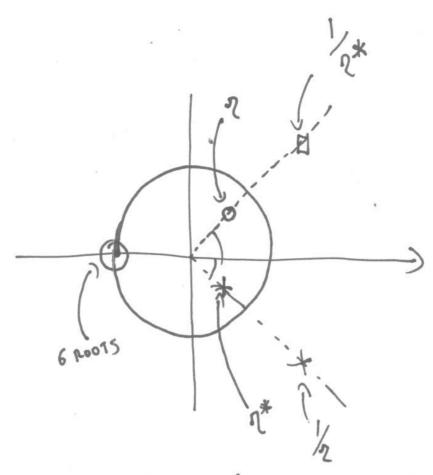
d) THE SYSTEM IS IDEMPOTENT IF AND ONLY IF

$$H(7) \cdot G(7) + H(-7) G(-7) = 2$$
 (3)

THE COEFFICIENTS & AND 5 HUST BE SUCH THAT CONDITION (1) 15 SATISFIED.

THUS
$$a = \frac{1}{4}$$
 AND $b = -\frac{1}{16}$.

NOTICE THAT THE UPPER-BRANCH
IS NOW PERFORMING AN OBLIQUE
PROJECTION WHICH IS GOOD NEWS.
HOWEVER, THE PROJECTION IS NOT
OPTIMAL IN THAT IT IS NOT
ONTHOGONAL.



$$P(t) = (1+t)^{3}(1+t^{-1})^{3}(t-t^{-1})$$

THEREFORE U, (7) HAS A TENO OF ORDER 3 POOR AT W =0:

NOW

POSSIBLE FACTORIFATION!

$$H^{o}(f) = (1+f)(1+f_{-1})(b(f))$$

 $e^{o}(f) = (1+f)_{f}(1+f_{-1})_{f}$

TWO-SCALE EQUATIONS:

MUNEOVER:

USING THE TWO-SCALE EQUATIONS AND THE LINEARITY OF INNER PHODUCT, WE OBTAIN:

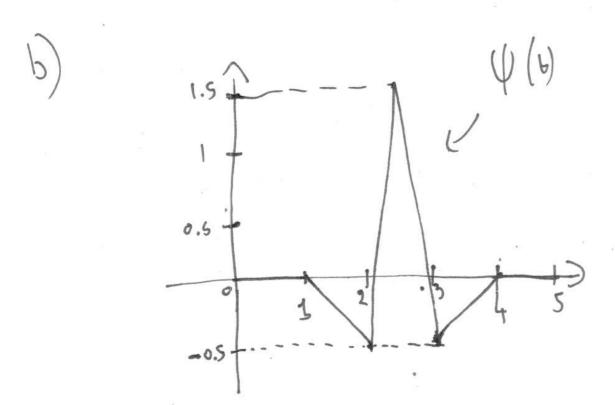
$$\frac{1}{2} \left(\frac{1}{2} \right) \left(\frac{1}{2} \right) \left(\frac{1}{2} \right) = \frac{1}{2} \left(\frac{1}{2} \right) \left(\frac{1}{2$$

WHERE IN THE LAST EQUALITY WE HANE REPLACED 2+ WITH X.

BELOUSE OF (1) WE HAVE THAT 2 4 (4-11) , 4 (x-2m-2))= 8 [16-(2m+2)]

EQ. 2 , THENEFORE BECOMES ".

BY CONDANING THIS LAST TERM ABOVE WITH EQ. (1) WE OBTAIN THE DESIDED RESULT:



SINCE Co(t) HAS TWO REMOS AT II)
THIS MEANS THAT H₁(t) HAS TWO
ZENOS AT WEO.

$$\psi$$
 $(\omega) = \frac{1}{\sqrt{2}} H_1(z^{\frac{3\omega}{2}}) \tilde{\varphi}(\frac{\omega}{2})$

THUS $\widetilde{\psi}(H)$ HAS TWO VAMISHING MONEWTS.

d)

WHERE P. to(t) IS A POLYHONIAL OF

DEGREE 1 m= Ld)

DEGREE 1 c | f-to| d

(3)

THE WAVELET (DEFFICIENTS IN THE CONE OF INFLUENCE OF & ARE THEN GIVEN 137:

2 P, Vm, ~) = < P(+), Vm, ~ (+) >+ < E(+), (m, m)

SINCE L=1.8 THEN m=1AND

SINCE V(+) RAS TWO VANISHING MONENTS

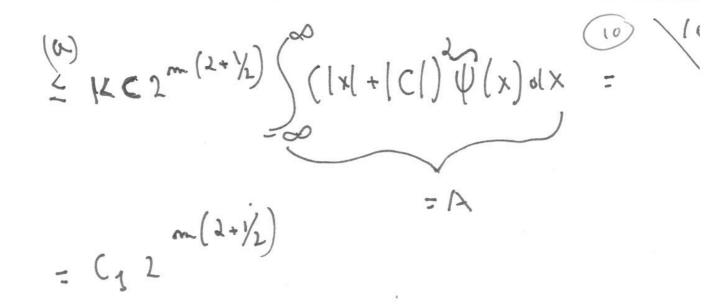
LPG(+), V~,~(+) D=0

CSING EQ. I WE HAVE:

- m/2 (| f-r₃| Ψ(z^mf-m) with

2 f, Ψ m, m > = < ε(t), Ψ m, m ≥ ≤ | (2) | (x) dx

= 12 2 m/2 (| x 2^m + m 2^m - t₀| Ψ(x) dx

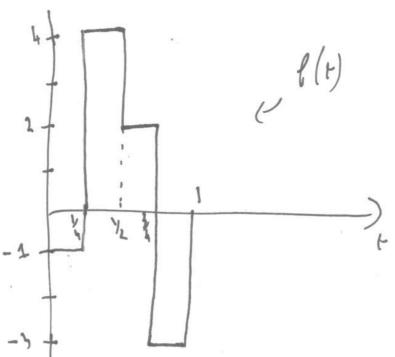


WHENE (a) FOLLOWS FROM THE FACT THAT

WE ARE IN THE CONE OF INFLUENCE OF 6,

THEREFORE | M2^m-to | \leq C2^m. HERE 'C' IS

THE COMPACT SUPPORT OF \$\text{\$\partial}(t)\$.



a)
$$Y_{-2,m}(t) = 2 \varphi(kt-m)$$
, $(s,m= \langle \beta(t), \varphi_{i,m}(t) \rangle$.
 $S_{-2,m} = -\frac{1}{2}$
 $C_{-2,1} = 2$
 $C_{-2,2} = 3$

(., m = 0 m + 0, 1, 2, 3

62,3:-3/

$$\begin{cases} c_{0,0} = -\frac{1}{4} + \frac{1}{2} - \frac{1}{2} \\ c_{0,m} = 0, \quad m \neq 0 \end{cases}$$

$$\begin{cases} \begin{cases} 0 & -1, 0 = -\frac{5}{4} \cdot \sqrt{2} \\ 0 & -1, 1 = \frac{5}{4} \cdot \sqrt{2} \\ 0 & -1, 1 = \frac{5}{4} \cdot \sqrt{2} \end{cases}$$

$$0 & -1, 1 = \frac{5}{4} \cdot \sqrt{2}$$

$$0 & -1, 1 = \frac{5}{4} \cdot \sqrt{2}$$

$$0 & -1, 1 = \frac{5}{4} \cdot \sqrt{2}$$

PARSEVAL = D || || || = \(\frac{1}{2} \) | (m, 0| \(\frac{1}{2} \) \(\frac{1}{2} 1111= 1 + 16 + 4 + 9 = 15 1 Co, 0 + | do, 0 | + | d-1, 0 | + | d-1, 2 | = -1 + 1 + 25.1 + 25.1 = 15