Optical Communication 2014 Solutions

1. a)
$$\lambda_0 = 1330 \text{ nm} : f = c/\lambda_0 \quad \Delta f = .05 (c/\lambda_0)$$

$$\Delta f = .05 \times 3 \times 10^8 = 11,300 \text{ GHz}$$

$$1.33 \times 10^{-6} = 11,300 \text{ GHz}$$

- to III, which will be less, so shot noise will dominate.
- region of the LED (brightness theorem).

- e) The photon energy of do = 1550 nm is well below the bondgap energy of Si 50 Si connet absorb.
- f) The mode of lower n' (1475) his more light in the cladding, so is more weakly guided, will lesk more.

$$q$$
) $d \leq m k_0$ $m=1$ $d \leq 1.3 \mu m$ $= 2.64 \mu m$ $2\sqrt{1.52^2 - 1.6^2} = 2.64 \mu m$

- h) It's easier to align sources to fibres and fibres to each other. (Alternatively easier to launch light from homeomitter efficiently.

 1) $R = \left(\frac{1.5 1.3}{1.5 + 1.3}\right)^2 = 0.005$ in either direction
- i) Spreading loss gives a 1/R2 dependence which is not exponential and so not constant in 213/4m.

2. a)

a mode m is superfied if
$$J > ml_0$$
 ZNA
 ZNA

To
$$m = 1.519$$

For $m = 1$ (011) $Y = -X_{CO} + X \rightarrow S_{MX}/X = \frac{1}{2} \frac{1}{2} R$

By successive approx $X = 2.077$
 $K_{X} = 2X/L = 1.0385$ $N = 1.52^{2} - (1.0385 \times 1.3/217)^{2}$
 $N' = 1.505$

d) For an
$$m=1$$
 mode in the case, $E(x)=E_0 \sin(k_0 x)$ which pedes at $k_0 x_m = \pi / 2$, $x_m = \pi / 2 k_x$

$$k_{1x} = \int n_1^2 - n_1^2 k_0 \quad k_0 = 2\pi / k_0$$

$$x_m = \lambda_0 / 2 \int n_1^2 - n_1^2$$

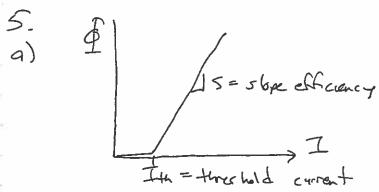
3. a) Material Dispersion - this is caused by the variation of n with I of the glasses making up the fibre.

Waveguide Dispersion - this is caused by the variation of mode shape with λ , and thus u' as the frechen in the core changes.

b)
$$n' = D_0 + D_1 (J_1 - J_{1-2})$$
 $V_5 = \frac{dU}{dR} = \frac{dW}{d(n'k_0)} = \frac{dW}{dJ_0} / \frac{d(n'k_0)}{dJ_0}$
 $|dw/dJ_0| = u/J_0 \cdot \frac{d(n'k_0)}{dJ_0} = \frac{d}{dJ_0} (2\pi n'/J_0)$
 $\frac{d(n'k_0)}{dJ_0} = 2\pi \left(-\frac{D_0}{J_0^2} + \frac{D_0}{J_0^2} \right)$
 $\frac{d(n'k_0)}{dJ_0} = 2\pi \left(-\frac{D_0}{J_0^2} + \frac{D_0}{J_0^2} \right)$
 $\frac{d(n'k_0)}{dJ_0} = \frac{2\pi}{J_0^2} \left(-\frac{D_0}{J_0^2} + \frac{D_0}{J_0^2} \right)$

$$C) \quad \overline{Z}_{g} = \frac{L}{V_{g}} = \frac{L}{C} \left(O_{o} - O_{i} \lambda_{c} \right)$$

I) Since T_{ij} does not depend an h_{ij} , there is no chromotic dispersion. This can also be carelided from $\frac{d^{2}u'}{dh^{2}} = 0$.



The threshold current arises because of the need to achieve sufficient photors in the cavity to ensure that stimulated enission becomes more likely than sponteneous emission. Its keel deads on the end reflection coefficients, internal loss, and not

b) If we neglect the artput up to Itm, then the artput.

$$\vec{T} = (I - I + 1) \leq \text{where } \leq = \frac{1}{2} \ln \frac{1}{2} \ln \frac{1}{2} + \frac{1}{2} \ln \frac{1}{2} + \frac{1}{2} \ln \frac{1}{2} \ln \frac{1}{2} + \frac{1}{2} \ln \frac{1}{2} \ln \frac{1}{2} \ln \frac{1}{2} + \frac{1}{2} \ln \frac$$

c) For boy Induct nodes, for cavity length L, we need $\frac{m_i h_i}{2} = L$ with m_i the mode ndex.

 $d_i = \lambda_{oi} / n'$ $f_i = c / \lambda_{ii} = c m_i / 2n' L$ then $\Delta f_i = c / 2n' L$) but the grap velocity it $\approx c / n'$ so $\Delta f_i = V_g / 2L$ $\Delta f_i^{-1} = (2L) / V_g = round-trip time$.

d) Pits the frechen of input electrons converted to photons
next is the frechen of generated photons reaching the autput.

The both LEDS and lasers, ni is limited by the relative
radiative and now redistrict recombination rates, but in lasors
this is largely regarded by showlated emission.

Mext is limited in LEDS by total internal reflection, surface (Fresnel)
reflection, re-adsorption, and propagation devinwards.

In lisers yest is much higher, limited by appropriate losses.

Vb = / Emax/(watwo) | Emax = e Nawp Wn = NA wp W= Watup 1. V2 = e N2 Wp (1+ N4/NO)

2 = e N2 W = 2 (1+ N4/NO)

2 \(\text{2} \) \(\text{1} + \text{N} \) \(\text{N} \) Ub = 1.1×10 +5×10° × (5×10°)2 2×12 ×8.85×1012 (1+5) = 1.57 V b) y = e-xx, -e-xx2 $x_i = h - w_p$ $x_i = h + w_n$ n= e-xh (xwp - -5dwp) 2h = 0.8×105 × 8×106 = 0.64 exp(-ah) = 0.527 0.80 = 1.52 = e + e - e = xwp Successive approximation: 0 = 0.48 Wp = 6.48 = 6 Mm W = 640 = 36 MM Vb = 1.57 (36)2 = BIV

(6) $|E_{max}| = \frac{E \times 10^{4}}{0.12} = 5.00 \times 10^{5} \text{ V/m}$ $|E_{mx}| = \frac{e N_{A} W_{P}}{0.12} = \frac{2 V_{b}}{W} = \sqrt{\frac{2 e N_{A} V_{b}}{2 (1 + N_{A}/N_{0})}}$ $|V_{b}| = |E_{max}|^{2} \times \frac{E_{c}}{E_{c}} (|V_{c}| + N_{A}/N_{0})$ $= (5.00 \times 10^{5})^{2} \times 12 \times 8.85 \times 10^{-12} (6)$ = 0.49 V