DEPARTMENT OF ELECTRICAL AND ELECTRONIC ENGINEERING EXAMINATIONS 2008

EEE/ISE PART II: MEng, BEng and ACGI

COMMUNICATIONS 2

Monday, 9 June 2:00 pm

Time allowed: 2:00 hours

There are FOUR questions on this paper.

Q1 is compulsory. Answer Q1 and any two of questions 2-4. Q1 carries 40% of the marks. Questions 2 to 4 carry equal marks (30% each).

Any special instructions for invigilators and information for candidates are on page 1.

C. Ling

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Second Marker(s): J.A. Barria, J.A. Barria

EXAM QUESTIONS

- 1. This question is compulsory.
 - Answer the following questions about probability and random processes.
 - Explain what is meant by a wide-sense stationary random process and what the Wiener-Khinchine theorem says about it.

[3]

ii) Given two statistically independent Gaussian random variables with zeros means and the same variances, how would you generate a Rayleigh random variable and a Ricean random variable?

[4]

iii) Explain what is meant by the term "ergodicity". Is the sinusoid $X(t) = A\cos(\omega_c t + \Theta)$ with random phase Θ uniformly distributed on $[0, 2\pi]$ ergodic? (There is no justification required.)

[3]

- b) Answer the following questions about modulation and demodulation.
 - Explain the terms "synchronous detection", "envelope detection", "coherent detection", and "noncoherent detection".

[4]

ii) Draw a diagram for the demodulation of single-sideband (SSB) amplitudemodulated signals where the carrier is suppressed. Indicate the bandwidth of the bandpass filter.

[3]

iii) Can the regular phase shift-keying (PSK) signal be noncoherently detected? Explain what is meant by differential phase shift-keying (DPSK).

[3]

- c) Answer the following questions about information theory and coding.
 - i) Explain how Shannon defines and measures information.

[5]

 Explain what is meant by mutual information, how channel capacity is defined, and write down the Shannon capacity formula for the additive white Gaussian noise channel.

[5]

- d) Answer the following questions about noise.
 - i) Explain what the term "additive white Gaussian noise" means. Is Gaussian noise always white?

[4]

[Continued on the following page.]

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ii) A bandpass noise signal n(t) can be expressed as $n(t) = n_c(t) \cos \omega_c t + n_s(t) \sin \omega_c t$. Consider bandpass noise n(t) having the power spectral density shown below in Fig. 1.1. Draw the power spectral density of $n_s(t)$ if the center frequency $\omega_c/2\pi$ is 8 MHz.

[6]

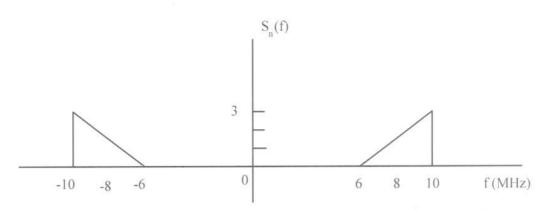


Figure 1.1 Power spectral density of n(t).

2. Analogue communications.

 A single-sideband (SSB) signal is transmitted over a noisy channel, with the power spectral density of the noise

$$\mathbb{S}(f) = \begin{cases} N_o \left(1 - \frac{|f|}{B} \right), & |f| < B \\ 0, & \text{otherwise} \end{cases}$$
 (2.1)

where $B=200~\rm kHz$ and $N_o=10^{-9}~\rm W/Hz$. The message has bandwidth 10 kHz and average power 10 W. The carrier amplitude at the transmitter is 1 V. Assume the channel attenuates the signal power by a factor of 1000, i.e., 30 decibel (dB). Assume the lower sideband (LSB) is transmitted and a suitable bandpass filter is used at the receiver to limit the out-of-band noise. Determine the predetection SNR at the receiver if

i) the carrier frequency is 100 kHz;

[8]

ii) the carrier frequency is 200 kHz.

[6]

b) In practice, the de-emphasis filter in an FM receiver is often a simple resistancecapacitance (RC) circuit with transfer function

$$H_{de}(f) = \frac{1}{1 + j2\pi fRC}$$
 (2.2)

i) Calculate the 3-dB bandwidth and equivalent bandwidth.

[4]

Suppose the modulating signal has bandwidth W, the carrier amplitude is A, and the single-sided power spectral density of the white Gaussian noise is N_0 . Compute the noise power at the output of the de-emphasis filter.

[6]

iii) Compute the noise power without the de-emphasis filter.

[3]

iv) Now suppose $RC = 6 \times 10^{-5}$, and W = 15 kHz. Compute the improvement in the output signal-to-noise ratio (SNR) provided by the de-emphasis filter. Express it in decibel (dB).

[3]

- 3. Digital communications.
 - a) A uniform quantizer for PCM has 2^n levels. The input signal is $m(t) = A_m[\cos(\omega_m t) + \sin(\omega_m t)]$. Assume the dynamic range of the quantizer matches that of the input signal.
 - i) Write down the expressions for the signal power, quantization noise power, and the SNR in dB at the output of the quantizer.

[6]

Determine the value of n such that the output SNR is about 62 dB.

[4]

- b) Consider a binary digital modulation system, where the carrier amplitude at the receiver is 1 V, and the white Gaussian noise has standard deviation 0.2. Assume that symbol 0 and symbol 1 occur with equal probabilities.
 - Compute the bit error rates for ASK, FSK, and PSK with coherent detection. Use the following approximation to the Q-function

$$Q(x) \lesssim \frac{1}{\sqrt{2\pi} \cdot x} e^{-x^2/2}, \quad x \ge 0$$
 (3.1)

[5]

 Compute the bit error rates for ASK, FSK, and DPSK with noncoherent detection.

[5]

The Q-function is widely used in performance evaluation of digital communication systems. More precisely, Q(x) is defined as the probability that a standard normal random variable X exceeds the value x:

$$Q(x) \triangleq \int_{x}^{\infty} \frac{1}{\sqrt{2\pi}} e^{-t^{2}/2} dt, \quad x \ge 0$$
 (3.2)

i) It is known that Q(x) admits an alternative expression

$$Q(x) = \frac{1}{\pi} \int_0^{\pi/2} e^{-\frac{x^2}{2\sin^2\theta}} d\theta, \quad x \ge 0$$
 (3.3)

Using this alternative expression, show the upper bound $Q(x) \le \frac{1}{2}e^{-x^2/2}$.

[4]

ii) By the definition (3.2), show that (3.1) is an upper bound on Q(x), i.e.,

$$Q(x) \le \frac{1}{\sqrt{2\pi} \cdot x} e^{-x^2/2}, \quad x \ge 0$$
 (3.4)

[Hint: use integration by parts for $e^{-t^2/2}$ in (3.2).]

[6]

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4. Information theory and coding.

a) Consider an information source generating the random variable *X* with probability distribution

x_k	x_1	x_2	<i>x</i> ₃	<i>x</i> ₄	<i>X</i> 5
$P(X = x_k)$	0.3	0.1	0.15	0.15	0.3

i) Construct a binary Huffman code for this information source. The encoded bits for the symbols should be shown.

[6]

ii) Compute the efficiency η of this code, where the efficiency is defined as the ratio between the entropy and the average codeword length:

$$\eta = \frac{H(X)}{\overline{L}} \tag{4.1}$$

[6]

- b) A (7,4) cyclic code has a generator polynomial $g(z) = g_0 z^3 + g_1 z^2 + g_2 z + 1 = z^3 + z^2 + 1$.
 - i) Write down the generator matrix in the systematic form.

[6]

ii) Find the parity check polynomial associated with this generator polynomial.

[4]

iii) What is the minimum Hamming distance? [Justification is required.] How many errors can this code detect and correct respectively?

[4]

iv) Is this a "perfect" code in the sense of the Hamming bound? [Justification is required.]

[4]