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Paper Number(s): **E2.1**

IMPERIAL COLLEGE OF SCIENCE, TECHNOLOGY AND MEDICINE UNIVERSITY OF LONDON

DEPARTMENT OF ELECTRICAL AND ELECTRONIC ENGINEERING **EXAMINATIONS 2008**

EEE/ISE PART II: MEng, BEng and ACGI

DIGITAL ELECTRONICS 2

Monday, 2 June 2:00 pm

There are FOUR questions on this paper.

Q1 is compulsory.

Answer Q1 and any two of questions 2-4.

Q1 carries 40% of the marks. Questions 2 to 4 carry equal marks (30% each).

Time allowed: 2:00 hours

Examiners responsible:

First Marker(s): D.M. Brookes D.M. Brookes

Second Marker(s): T.J.W. Clarke T.J.W. Clarke

Information for Candidates:

Notation: Unless explicitly indicated otherwise, digital circuits throughout this paper are

drawn with their inputs on the left and their outputs on the right. The notation X2:0 denotes the three-bit number X2, X1 and X0. The least significant bit of a binary number is always designated bit 0. Signed binary numbers use 2's

complement notation.

Digital Electronic II Page 1 of 7

- 1. (a) Figure 1.1 shows the state table for a state machine which has a single input A and a state that is represented by the value of the unsigned 2-bit number S1:0. The table entries are of the form D1,D0 / X,Y where D1:0 denotes the next state and X and Y are the output signals during the current state. State transitions occur on the rising edges of CLOCK which, for convenience, have been shown as numbered dashed lines in Figure 1.2.
 - (i) Draw the state diagram for the circuit

[5]

[3]

(ii) Complete the timing diagram shown in *Figure 1.2* by showing the state of the circuit during each clock cycle as a decimal number and the waveforms of X and Y. The state machine is initially in state 0 as shown.

S1,S0	A=0	A=1	
00	01/00	10/00	
01	01/11	11/11	
10	01/10	11/00	
11	00/01	11/01	

Figure 1.1

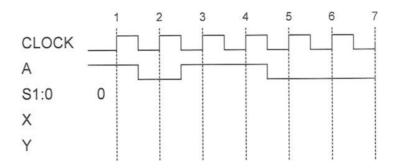


Figure 1.2

- (b) In the circuit of Figure 1.3 the propagation delays of the leftmost flipflop and the logic block are are t_p and t_d respectively. The rightmost flipflop has setup and hold times of t_s and t_h . The clock signal C is symmetrical with period T.
 - (i) Write the setup and hold inequalities that apply to the rightmost flip-flop. [5]
 - (ii) Find the maximum clock frequency for the circuit if the timing parameters (in ns) are: $t_p = 2$, $t_s = 11$, $t_h = 5$ and $t_d \leq 23$

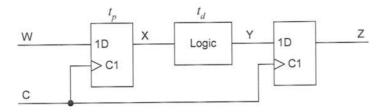


Figure 1.3

- (c) Figure 1.4 shows a digital-to-analogue converter whose input is a 3-bit unsigned binary number X2:0. Each of the three switches is labelled with the input bit that controls it and all switches are shown in the position corresponding to an input value of 0. The input voltage is $V_R = 1$ volt as shown.
 - (i) Determine the value of I_2 and explain why it is the same for both positions of the switch X2. [4]
 - (ii) Calculate the value of V_{OUT} when the input number X2:0 has the value 6. [4]

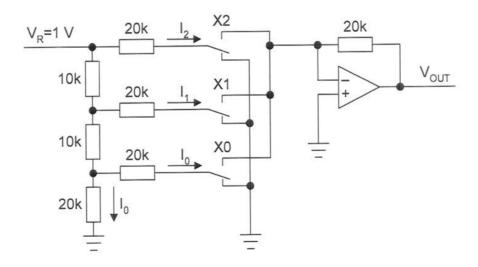


Figure 1.4

(d) A carry-lookahead adder is used to add together two 4-bit binary numbers X3:0 and Y3:0. The carry out of adder stage 1 is generated using either of the following equivalent expressions:

$$C1 = G1 + P1 \cdot G0 + P1 \cdot P0 \cdot CI$$
$$= G1 + P1 \cdot (G0 + P0 \cdot CI)$$

where CI is the carry into the least significant adder stage and Gn and Pn are defined by $Gn = Xn \cdot Yn$ and Pn = Xn + Yn.

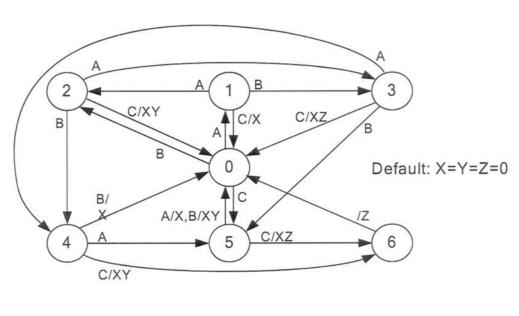
- (i) Determine the maximum propagation delay from any X or Y input to C1 separately for each of the two expressions given above. Assume that AND and OR gates each have a delay of 1 unit.
- (ii) Give a similar expression for C2, the carry out of stage 2, and determine the propagation delay from any X or Y input when it is implemented from an unfactorized expression. [4]
- (e) X7:0 is an 8-bit unsigned number in the range 0 to 255. Determine the decimal number range or ranges of values of X7:0 for which the following expressions are true:
 - (i) $X7 \cdot \overline{X6} \cdot X5$ [4] (ii) $X6 \oplus X5$

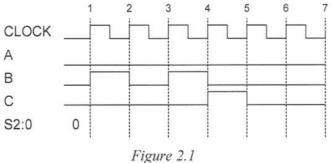
[4]

- 2. A state machine that controls a vending machine has three input signals A, B and C which go high for one clock cycle following the insertion of 10p, 20p and 50p coins respectively. At most one of A, B and C is ever high at a time and their transitions occur shortly after the CLOCK rising edge. The state machine has three outputs, X, Y and Z which respectively dispense a chocolate bar and give 10p and 20p coins as change. *Figure 2.1* shows the state diagram for the vending machine; the outputs are all low except where indicated on transition arrows.
 - (a) Complete the timing diagram shown in *Figure 2.1* showing the sequence of states, S2:0, as a decimal number and the waveforms of X, Y and Z.
 - (b) Deduce the cost of a chocolate bar. [3]

[7]

- (c) Give simplified Boolean expressions for X, Y and Z. [12]
- (d) Draw a revised state diagram for a state machine having the same input and output signals as before but with a chocolate bar price of 40p. The outputs Y and Z must never be high simultaneously. [8]





- 3. The circuit of *Figure 3.1* consists of an adder (Σ) , a subtractor (Δ) , a 2-bit counter (CTR2), an AND gate and three registers. The two registers that include a clock enable input ignore CLOCK edges whenever EN=0. The output of the subtractor is given by D=P-Q. The signals S, D, W, X, Y, Z represent multi-bit signed binary numbers whose decimal values during clock cycle n are denoted by $s(n), d(n), \dots, z(n)$ respectively. All signal transitions occur shortly after the rising edge of CLOCK.
 - (a) Complete the timing diagram of *Figure 3.1* by giving the value of B1:0 in each clock cycle, the waveform of EN and the values of x, y and z in each clock cycle. The vertical dashed lines denote CLOCK rising edges and the clock cycles are numbers 1 to 13 for convenience. The initial values of B1:0, x, y and z are zero as shown. You may assume that the adder and subtractor never overflow.
 - (b) The registers and counter have a propagation delay of 10 ns and setup/hold times of 5 ns and 2 ns respectively. The AND gate has a propagation delay of 3 ns and the adder/subtractor circuits have a propagation delay of 18 ns. Determine the maximum clock frequency. [4]
 - (c) Show that $x(k) = \sum_{n=1}^{k-1} w(n)$ and that y(4m) = x(4m-4) where k and m are [6] positive integers.
 - (d) Derive an expression for z(4m) in terms of w(n) and, for m = 3, compare your solution with the answer given in part (a).

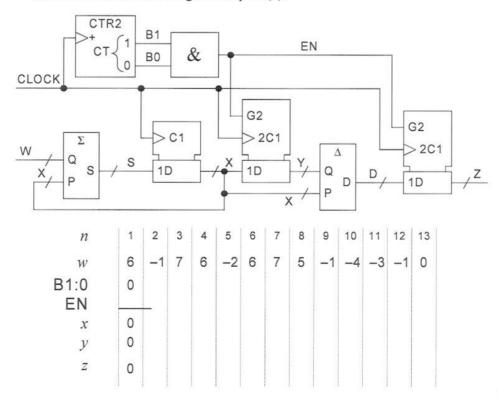


Figure 3.1

Digital Electronic II

4. Figure 4.1 shows a 4-bit analogue-to-digital converter (ADC). The circuit consists of a 2-bit flash ADC (labelled ADC1) whose output is used to select the reference voltages of a second, 3-bit, flash ADC consisting of a resistor chain, five comparators and a logic block. The unsigned values of R1:0 and P2:0 are r and p respectively. The logic block outputs are: P2 = B·C·D, P1 = A·B·D+B·D·E and P0 = A⊕B⊕C⊕D⊕E. The output of the first ADC, r, and the resultant voltages at Y and Z are given by:

Input Voltage X (Volts)	X<-4	-4≤X<0	0≤X<+4	+4≤X
ADC1 Output, r	1	2	3	0
Voltages Y and Z (Volts)	-8, -4	0, -4	0, +4	+8, +4

(a) Complete a truth table giving the decimal value of *p* for the each of the following ten combinations of A, B, C, D, E: 00000, 10000, 11000, 11100, 11111, 01111, 00111, 00011, 00001.

[12]

[6]

- (b) If the switches are fixed in the position shown (i.e. Y=0 and Z=-4 volts) determine which of the combinations of A, B, C, D, E from part (a) might occur and the range of X voltages that will result in each. Hence show that, for $-5 \le X < 1$, the value of P2:0 is given by p = 5 + floor(X) where $floor(\bullet)$ denotes rounding down to the next lowest integer (e.g. floor(-1.5) = -2).
- (c) Find a similar expression for p if the switches are instead in the position corresponding to r = 3 (i.e. Y=0 and Z=+4 volts).
- (d) The final output of the ADC is given by the four least significant bits of the sum s = p + 4r + 3. Show how s may be generated from R1:0 and P2:0 using a single 4-bit adder. [6]

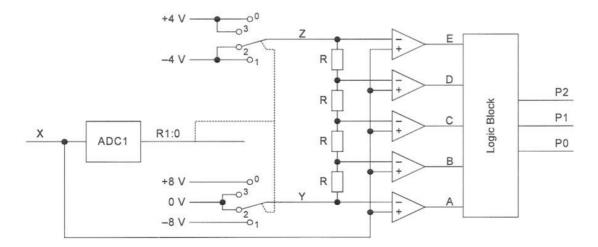


Figure 4.1

Digital Electronic II Page 7 of 7