

ASSIGNMENT-3

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Download all python codes from

<https://github.com/ThurpuNaveena/ASSIGNMENT-3/tree/main/CODES>

and latex-tikz codes from

<https://github.com/ThurpuNaveena/ASSIGNMENT-3/tree/main>

Row reducing the augmented matrix,

$$\begin{pmatrix} 1 & 1 & -1 & 1 \\ 6 & 4 & -5 & 1 \\ -4 & -2 & 3 & 1 \end{pmatrix} \xleftrightarrow{R_2 \rightarrow R_2 - 6R_1} \begin{pmatrix} 1 & 1 & -1 & 1 \\ 0 & -2 & 1 & -5 \\ -4 & -2 & 3 & 1 \end{pmatrix} \quad (2.0.4)$$

$$\xleftrightarrow{R_3 \rightarrow R_3 + 4R_1} \begin{pmatrix} 1 & 1 & -1 & 1 \\ 0 & -2 & 1 & -5 \\ 0 & 2 & -1 & 5 \end{pmatrix} \quad (2.0.5)$$

$$\xleftrightarrow{R_2 \rightarrow \frac{-R_2}{2}} \begin{pmatrix} 1 & 1 & -1 & 1 \\ 0 & 1 & \frac{-1}{2} & \frac{5}{2} \\ 0 & 2 & -1 & 5 \end{pmatrix} \quad (2.0.6)$$

$$\xleftrightarrow{R_1 \rightarrow R_1 - R_2} \begin{pmatrix} 1 & 0 & \frac{-1}{2} & \frac{-3}{2} \\ 0 & 1 & \frac{-1}{2} & \frac{5}{2} \\ 0 & 2 & -1 & 5 \end{pmatrix} \quad (2.0.7)$$

$$\xleftrightarrow{R_3 \rightarrow R_3 - 2R_2} \begin{pmatrix} 1 & 0 & \frac{-1}{2} & \frac{-3}{2} \\ 0 & 1 & \frac{-1}{2} & \frac{5}{2} \\ 0 & 0 & 0 & 0 \end{pmatrix} \quad (2.0.8)$$

$$\begin{pmatrix} 1 & 0 & -0.5 & -1.5 \\ 0 & 1 & -0.5 & 2.5 \\ 0 & 0 & 0 & 0 \end{pmatrix} \quad (2.0.9)$$

1 QUESTION No-2.36 (A) (LINEAR FORMS)

Find the equation of the planes that passes through three points $\begin{pmatrix} 1 \\ 1 \\ -1 \end{pmatrix}, \begin{pmatrix} 6 \\ 4 \\ -5 \end{pmatrix}, \begin{pmatrix} -4 \\ -2 \\ 3 \end{pmatrix}$

2 SOLUTION

$$\mathbf{R} = \begin{pmatrix} 1 \\ 1 \\ -1 \end{pmatrix}, \mathbf{S} = \begin{pmatrix} 6 \\ 4 \\ -5 \end{pmatrix} \text{ and } \mathbf{T} = \begin{pmatrix} -4 \\ -2 \\ 3 \end{pmatrix} \quad (2.0.1)$$

If the equation of the plane is given by

$$\mathbf{n}^T \mathbf{x} = 1 \quad (2.0.2)$$

$$\begin{pmatrix} 1 & 1 & -1 \\ 6 & 4 & -5 \\ -4 & -2 & 3 \end{pmatrix} \mathbf{n} = \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix} \quad (2.0.3)$$

Number of Non zero row =2. Rank of Matrix =2
For the linear equation to have infinite solution.
Rank(coefficient matrix) = Rank(Augmented matrix) and both not equal to Rank (Full matrix)

$$\begin{pmatrix} 1 & 1 & -1 \\ 6 & 4 & -5 \\ -4 & -2 & 3 \end{pmatrix} \quad (2.0.10)$$

Row reduced matrix

$$\begin{pmatrix} 1 & 0 & -0.5 \\ 0 & 1 & -0.5 \\ 0 & 0 & 0 \end{pmatrix} \quad (2.0.11)$$

Rank of matrix =3

Rank of coefficient matrix = 0

since the given matrix has infinite solutions, there

are infinitely many planes passing through the points which means that they lie on a straight line.

Equation of the line

$$\mathbf{A} = \begin{pmatrix} 1 \\ 6 \\ -4 \end{pmatrix}, \mathbf{B} = \begin{pmatrix} 1 \\ 4 \\ -2 \end{pmatrix} \quad (2.0.12)$$

$$\mathbf{x} = \mathbf{A} + \lambda (\mathbf{B} - \mathbf{A}) \quad (2.0.13)$$

$$\mathbf{x} = \begin{pmatrix} 1 \\ 6 \\ -4 \end{pmatrix} + \lambda \begin{pmatrix} 0 \\ -2 \\ 2 \end{pmatrix} \quad (2.0.14)$$

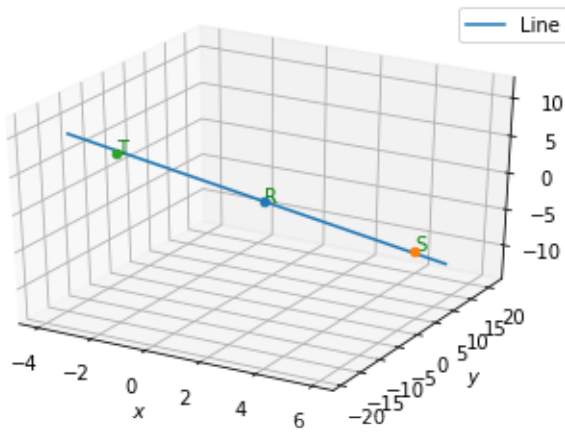


Fig. 2.1: plot of the line