

ASSIGNMENT-8

T.Naveena

Download all python codes from

<https://github.com/ThurpuNaveena/Assignment8/tree/main/Assignment8>

and latex-tikz codes from

<https://github.com/ThurpuNaveena/Assignment8/tree/main/Assignment8>

1 QUESTION No-2.48(INEQUALITIES)

Solve: $2x+y \geq 6$, $3x+4y \leq 12$.

2 SOLUTION

Let $2x+y \geq 6$, $-3x-4y \geq -12$

Let $u_1 \geq 0, u_2 \geq 0$. This may be expressed as

$$\mathbf{u} = \begin{pmatrix} u_1 \\ u_2 \end{pmatrix} \geq \mathbf{0} \quad (2.0.1)$$

Now we have,

$$\begin{pmatrix} 2 & 1 \\ -3 & -4 \end{pmatrix} \mathbf{x} \geq \begin{pmatrix} 6 \\ -12 \end{pmatrix} + \mathbf{u} \quad (2.0.2)$$

$$\mathbf{x} = \begin{pmatrix} 2 & 1 \\ -3 & -4 \end{pmatrix}^{-1} \begin{pmatrix} 6 \\ -12 \end{pmatrix} + \begin{pmatrix} 2 & 1 \\ -3 & -4 \end{pmatrix}^{-1} \mathbf{u} \quad (2.0.3)$$

$$\Rightarrow \mathbf{x} = \begin{pmatrix} \frac{4}{5} & \frac{1}{5} \\ \frac{3}{5} & \frac{2}{5} \end{pmatrix} \begin{pmatrix} 6 \\ -12 \end{pmatrix} + \frac{1}{5} \begin{pmatrix} 4 & 1 \\ -3 & -2 \end{pmatrix} \mathbf{u} \quad (2.0.4)$$

$$\mathbf{x} = \begin{pmatrix} \frac{12}{5} \\ \frac{6}{5} \end{pmatrix} + \frac{1}{5} \begin{pmatrix} 4 & 1 \\ -3 & -2 \end{pmatrix} \mathbf{u} \quad (2.0.5)$$

Thus the solution of the system of inequalities can be determined graphically and the desired region is the shaded triangle. Which is represented in the below figure,

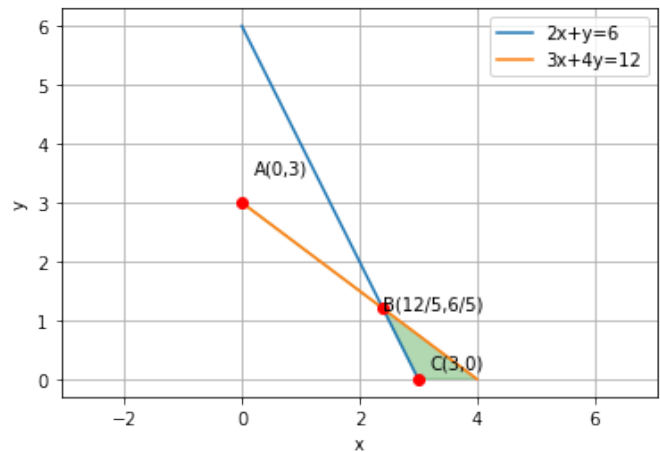


Fig. 2.1: Graphical solution