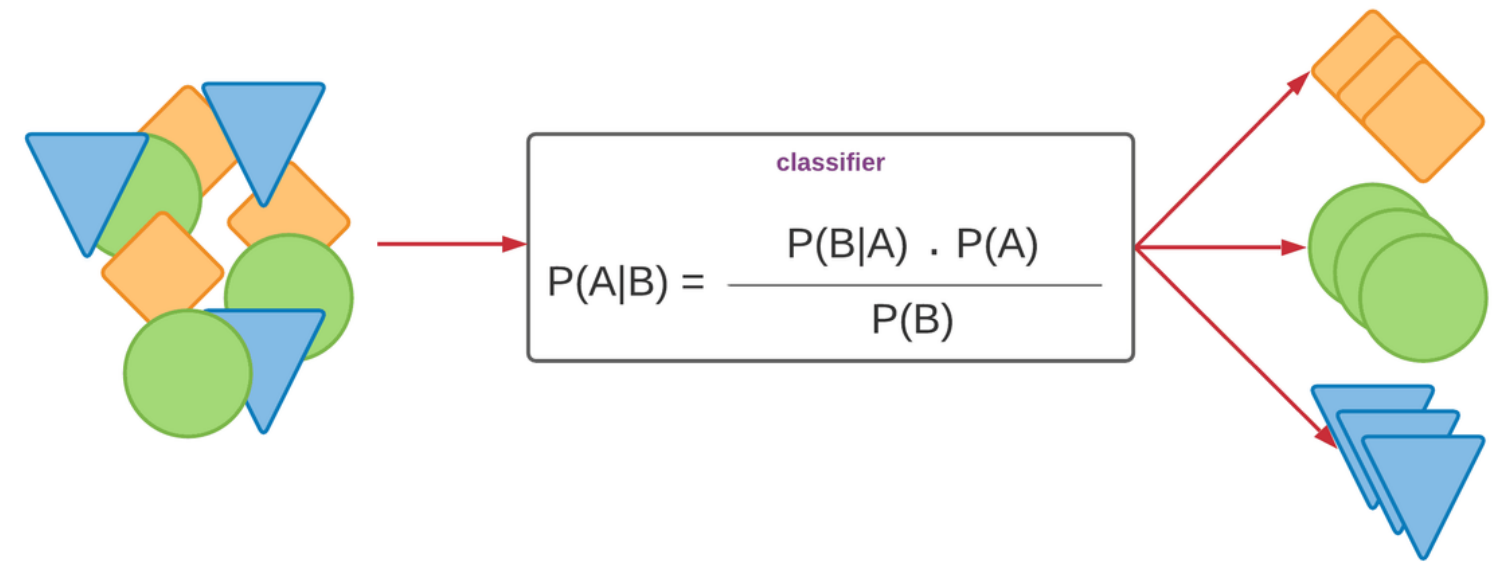





Multinomial Naive Bayes

Multinomial Naive Bayes



- The multinomial model captures word frequency information in documents
- Capturing frequency information of tokenization can help classification
- Require a small number of training sets but effective classification results
- The more applicable algorithm in text classification
- The most popular among naïve bayes classifiers

Conditional probabilities

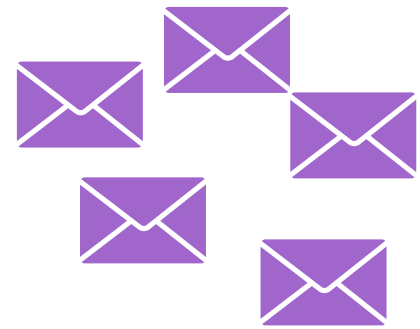


vector of words from message

$$P(\text{Spam}|x) = \frac{p(x|\text{Spam}) * P(\text{Spam})}{P(x)}$$

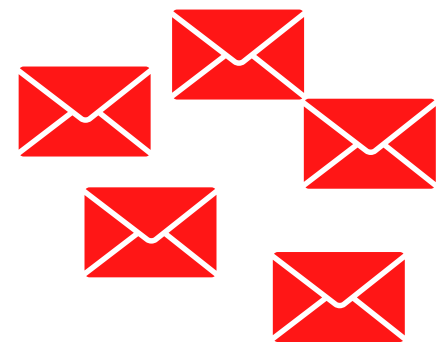
$x=[w_1, w_2, w_3, w_4, \dots, w_n]$

Conditional probabilities



Word	Count
Dear	9
Friend	6
Promotion	1
Free	1
Total	17

$$\begin{aligned}p(\text{Dear} | \text{normal}) &= 9/17 = 0.52 \\p(\text{Friend} | \text{normal}) &= 6/17 = 0.35 \\p(\text{promotion} | \text{normal}) &= 1/17 = 0.29 \\p(\text{free} | \text{normal}) &= 1/17 = 0.29\end{aligned}$$

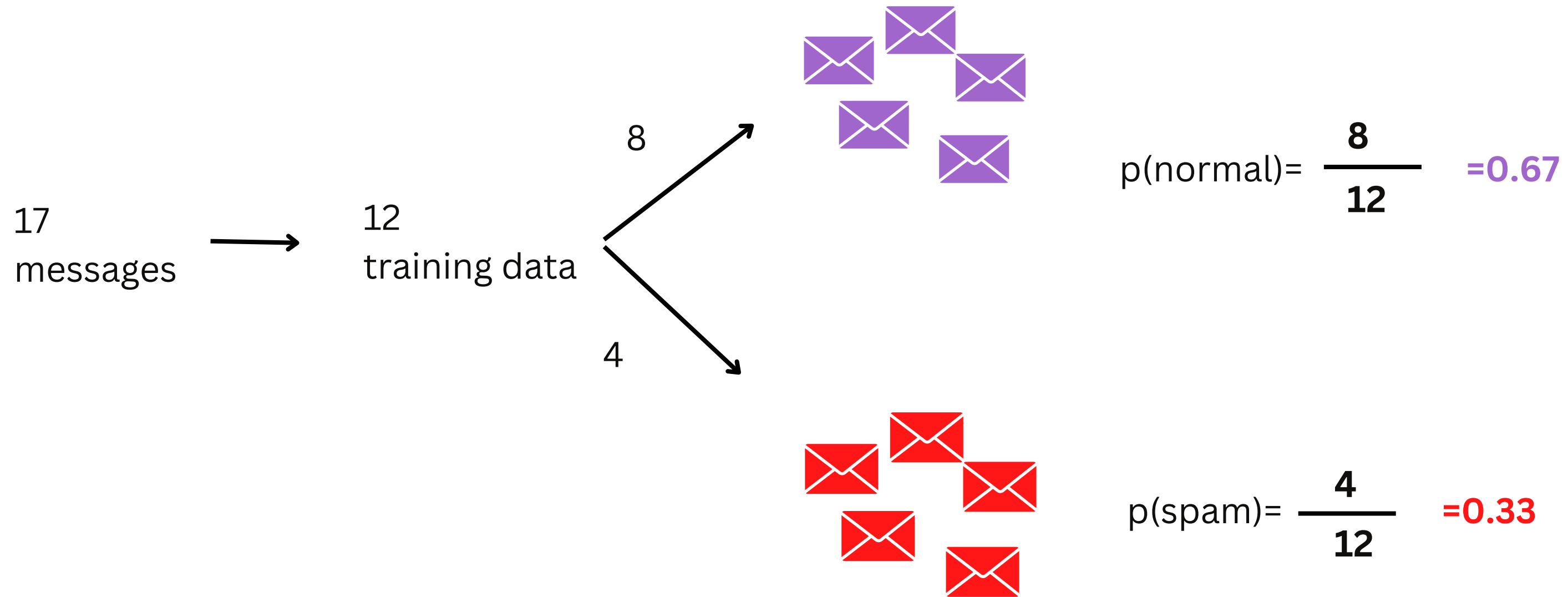


Word	Count
Dear	1
Friend	1
Promotion	1
Free	4
Total	7

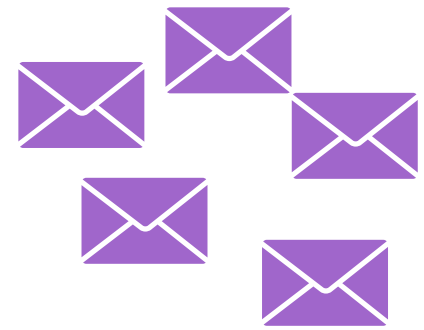
$$\begin{aligned}p(\text{Dear} | \text{spam}) &= 1/7 = 0.14 \\p(\text{Friend} | \text{spam}) &= 1/7 = 0.14 \\p(\text{promotion} | \text{spam}) &= 1/7 = 0.14 \\p(\text{free} | \text{spam}) &= 4/7 = 0.57\end{aligned}$$

likelihoods

Conditional probabilities



Conditional probabilities

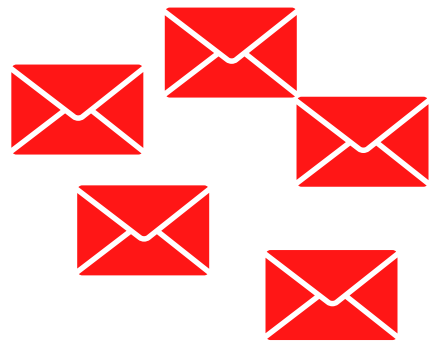


$$\begin{aligned} p(\text{Dear} | \text{normal}) &= 8/17 = 0.47 \\ p(\text{Friend} | \text{normal}) &= 5/17 = 0.29 \\ p(\text{promotion} | \text{normal}) &= 3/17 = 0.18 \\ p(\text{free} | \text{normal}) &= 1/17 = 0.06 \end{aligned}$$

Dear Friend

$$p(\text{normal}) = 0.67 \quad p(\text{normal}) * p(\text{Dear} | \text{normal}) * p(\text{Friend} | \text{normal})$$

$$0.67 * 0.47 * 0.29 = 0.091$$



$$\begin{aligned} p(\text{Dear} | \text{spam}) &= 1/7 = 0.14 \\ p(\text{Friend} | \text{spam}) &= 1/7 = 0.14 \\ p(\text{promotion} | \text{spam}) &= 1/7 = 0.14 \\ p(\text{free} | \text{spam}) &= 4/7 = 0.57 \end{aligned}$$

$$p(\text{spam}) = 0.33 \quad p(\text{spam}) * p(\text{Dear} | \text{spam}) * p(\text{Friend} | \text{spam})$$

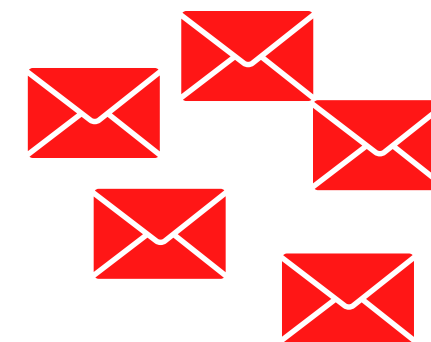
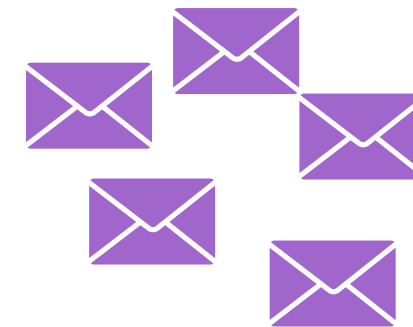
$$0.33 * 0.14 * 0.14 = 0.006$$

Conditional probabilities

$$0.67 * 0.47 * 0.29 = 0.091$$

$$0.33 * 0.14 * 0.14 = 0.006$$

Dear Friend



Conditional probabilities

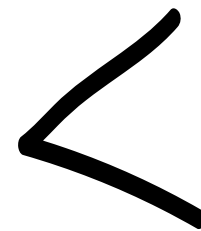
$p(\text{Dear} | \text{normal}) = 8/17 = 0.47$
 $p(\text{Friend} | \text{normal}) = 5/17 = 0.29$
 $p(\text{promotion} | \text{normal}) = 3/17 = 0.18$
 $p(\text{free} | \text{normal}) = 1/17 = 0.29$

Promotion Free
Free

$p(\text{Dear} | \text{spam}) = 1/7 = 0.14$
 $p(\text{Friend} | \text{spam}) = 1/7 = 0.14$
 $p(\text{promotion} | \text{spam}) = 1/7 = 0.14$
 $p(\text{free} | \text{spam}) = 4/7 = 0.57$

$p(\text{normal}) * p(\text{promotion} | \text{normal}) * p(\text{free} | \text{normal}) * p(\text{free} | \text{normal})$

$0.18 * 0.29 * 0.29 = 0.015$



$p(\text{spam}) * p(\text{promotion} | \text{spam}) * p(\text{free} | \text{spam}) * p(\text{free} | \text{spam})$

$0.14 * 0.57 * 0.57 = 0.045$

Promotion Free
Free