

ACM-ICPC World Finals 2017

Team Reference Document

University of Illinois at Urbana-Champaign: Time Limit Exceeded

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1 Data Structures

1.1 Segment Tree 2D

```
void build_y(int k_x, int k_y, int l, int r) {
   if (1 == r) {
       t[k_x][k_y] = 0;
       return:
   int mid = (1 + r) >> 1;
   build_y(k_x, k_y * 2, 1, mid);
   build_y(k_x, k_y * 2 + 1, mid + 1, r);
   t[k_x][k_y] = 0;
}
void build_x(int k, int l, int r) {
   build_y(k, 1, 1, n);
   if (1 == r) return;
   int mid = (1 + r) >> 1;
   build_x(k * 2, 1, mid);
   build_x(k * 2 + 1, mid + 1, r);
}
void update_y(int k_x, int l_x, int r_x, int k_y, int l_y, int
    r_y, int y, int v) {
   if (y < l_y || r_y < y) return;
   if (1_y == r_y) {
       if (1_x == r_x)
           t[k_x][k_y] += v;
           t[k_x][k_y] = t[k_x * 2][k_y] + t[k_x * 2 + 1][k_y];
    int mid = (l_y + r_y) >> 1;
    update_y(k_x, l_x, r_x, k_y * 2, l_y, mid, y, v);
    update_y(k_x, l_x, r_x, k_y * 2 + 1, mid + 1, r_y, y, v);
    t[k_x][k_y] = t[k_x][k_y * 2] + t[k_x][k_y * 2 + 1];
}
```

```
void update_x(int k, int l, int r, int x, int y, int v) {
    if (x < 1 \mid | r < x) return;
    if (1 == r) {
       update_y(k, l, r, 1, 1, n, y, v);
    int mid = (1 + r) >> 1;
    update_x(k * 2, 1, mid, x, y, v);
    update_x(k * 2 + 1, mid + 1, r, x, y, v);
    update_y(k, 1, r, 1, 1, n, y, v);
}
int get_y(int k_x, int k_y, int l, int r, int y1, int y2) {
    if (y2 < 1 || r < y1) return 0;
    if (y1 \le 1 \&\& r \le y2) return t[k_x][k_y];
    int mid = (1 + r) >> 1;
   return get_y(k_x, k_y * 2, 1, mid, y1, y2) +
          get_v(k_x, k_y * 2 + 1, mid + 1, r, v1, v2);
}
int get_x(int k, int l, int r, int x1, int x2, int y1, int y2) {
    if (r < x1 \mid | x2 < 1) return 0;
    if (x1 <= 1 && r <= x2)
       return get_y(k, 1, 1, n, y1, y2);
    int mid = (1 + r) >> 1;
    return get_x(k * 2, 1, mid, x1, x2, y1, y2) +
          get_x(k * 2 + 1, mid + 1, r, x1, x2, y1, y2);
```

1.2 Splay Tree

```
// Supports reversing a segment.
struct SplayTree {
    struct Node {
        Node *left, *right, *parent;
        int value, size;
        bool reversed;
    };
```

```
SplayTree() {
   nilt = new Node();
   nilt->left = nilt->right = nilt->parent = nilt;
   nilt->value = nilt->size = 0;
   nilt->reversed = false;
void set_left(Node* x, Node* y) {
   x \rightarrow left = y;
   y->parent = x;
}
void set_right(Node* x, Node* y) {
   x->right = y;
   y->parent = x;
}
void set_child(Node* x, Node* y, bool is_right) {
   if (is_right) set_right(x, y);
   else set_left(x, y);
}
void build_tree(vector < int >& arr) {
   root = nilt;
   for (int i = 0; i < arr.size(); ++i) {
       Node* x = new Node();
       x->size = arr[i];
       x->value = arr[i];
       x->reversed = false;
       set_left(x, root);
       x->parent = x->right = nilt;
       root = x;
   }
}
void propagate(Node* x) {
   if (x == nilt) return;
   if (x->reversed) {
       swap(x->left, x->right);
```

```
x->left->reversed = !x->left->reversed;
       x->right->reversed = !x->right->reversed;
       x->reversed = false;
   }
}
Node* locate(Node* x, int pos) {
   do {
       propagate(x);
       int num = x->left->size + 1;
       if (num == pos) return x;
       if (num > pos) x = x \rightarrow left;
           pos -= num, x = x->right;
   } while (true);
   return x;
}
void update(Node* x) {
   x->size = x->left->size + x->right->size + 1;
}
void uptree(Node* x) {
   Node* y = x->parent;
   Node* z = y->parent;
   if (x == y-)right) {
       Node* b = x->left;
       set_right(y, b);
       set_left(x, y);
   }
   else {
       Node* b = x->right;
       set_left(y, b);
       set_right(x, y);
   update(y);
   update(x);
   set_child(z, x, z->right == y);
```

```
void splay(Node* x) {
   do {
       Node* y = x-parent;
       if (y == nilt) return;
       Node* z = y->parent;
       if (z != nilt) {
           if ((x == y \rightarrow left) == (y == z \rightarrow left))
               uptree(y);
           else
               uptree(x);
       }
       uptree(x);
   } while (true);
}
void split(Node* t, int pos, Node*& t1, Node*& t2) {
   if (pos == 0) {
       t1 = nilt;
       t2 = t;
       return;
   }
   if (pos \geq t-\geqsize) {
       t1 = t:
       t2 = nilt;
       return;
   Node* x = locate(t, pos);
   splay(x);
   t1 = x;
   t2 = x->right;
   t1->right = nilt;
   t2->parent = nilt;
   update(t1);
Node* join(Node* t1, Node* t2) {
   if (t1 == nilt) return t2;
   t1 = locate(t1, t1->size);
   splay(t1);
   set_right(t1, t2);
```

```
update(t1);
   return t1;
}

Node *root, *nilt;
};
```

2 Graph Theory

2.1 Centroid Decomposition

```
void build(int u, int p) {
    sze[u] = 1;
   for (int v : adj[u])
       if (!elim[v] && v != p) build(v, u), sze[u] += sze[v];
}
int get_centroid(int u, int p, int num) {
    for (int v : adj[u])
       if (!elim[v] && v != p && sze[v] > num / 2)
           return get_centroid(v, u, num);
    return u;
}
void centroid_decomposition(int u) {
   build(u, -1);
    int root = get_centroid(u, -1, sze[u]);
   // Do stuffs here
    elim[root] = true;
   for (int v : adj[root])
       if (!elim[v]) centroid_decomposition(v, c + 1);
```

2.2 Heavy Light Decomposition

```
void build(int u) {
   size_tree[u] = 1;
   for (int i = 0; i < adj[u].size(); ++i) {</pre>
       int v = adj[u][i];
       if (parent[u] == v) continue;
       parent[v] = u;
       build(v);
       size_tree[u] += size_tree[v];
   }
}
void hld(int u) {
   if (chain_head[num_chain] == 0)
       chain_head[num_chain] = u;
   chain_idx[u] = num_chain;
   arr_idx[u] = ++num_arr;
   node_arr[num_arr] = u;
   int heavy_child = -1;
   for (int i = 0; i < adj[u].size(); ++i) {</pre>
       int v = adj[u][i];
       if (parent[u] == v) continue;
       if (heavy_child == -1 || size_tree[v] >
           size_tree[heavy_child])
           heavy_child = v;
   }
```

```
if (heavy_child != -1)
       hld(heavy_child);
   for (int i = 0; i < adj[u].size(); ++i) {</pre>
       int v = adj[u][i];
       if (v == heavy_child || parent[u] == v) continue;
       ++num_chain;
       hld(v);
   }
}
// u is an ancestor of v
int query_hld(int u, int v) {
   int uchain = chain_idx[u], vchain = chain_idx[v], ans = -1;
   while (true) {
       if (uchain == vchain) {
           get(..., arr_idx[u], arr_idx[v]);
           break;
       get(..., arr_idx[chain_head[vchain]], arr_idx[v]);
       v = parent[chain_head[vchain]];
       vchain = chain_idx[v];
   }
   return ans;
}
```