

$$\text{In[5]:= } V = -ma * g * la * \text{Cos}[qb] - mb * g * (wa * \text{Cos}[qb] + lb * \text{Cos}[qb])$$

$$\text{Out[5]= } -g \, la \, ma \, \text{Cos}[qb] - g \, mb \, (lb \, \text{Cos}[qb] + wa \, \text{Cos}[qb])$$

$$\text{In[6]:= } T = 1/2 * (ma * la * ((qa)'[t])^2 + mb * (wb^2 * ((qa)'[t])^2 + lb^2 * ((qb)'[t])^2 + 2 * wa * lb * (qa)'[t] * (qb)'[t] * \text{Cos}[qa - qb]))$$

$$\text{Out[6]= } \frac{1}{2} (la \, ma \, qa'[t]^2 + mb \, (wb^2 \, qa'[t]^2 + 2 \, lb \, wa \, \text{Cos}[qa - qb] \, qa'[t] \, qb'[t] + lb^2 \, qb'[t]^2))$$

$$\text{In[7]:= } dLdqap = ma * la^2 * x2 + mb * wa^2 * x2 + wa * lb * x5 * \text{Cos}[x1 - x4]$$

$$\text{Out[7]= } la^2 \, ma \, x2 + mb \, wa^2 \, x2 + lb \, wa \, x5 \, \text{Cos}[x1 - x4]$$

$$\text{In[8]:= } dLdqbp = mb * lb^2 * x5 * \text{Cos}[x1 - x4]$$

$$\text{Out[8]= } lb^2 \, mb \, x5 \, \text{Cos}[x1 - x4]$$

$$\text{In[9]:= } dtdLdqa = x3 * (ma * la^2 + mb * wb^2) + wa * lb * x6 * \text{Cos}[x1 - x4] + wa * lb * x5^2 * \text{Sin}[x1 - x4] - wa * lb * x2 * x5 - wa * lb * x1 * x5 * \text{Sin}[x1 - x4]$$

$$\text{Out[9]= } (la^2 \, ma + mb \, wb^2) \, x3 - lb \, wa \, x2 \, x5 + lb \, wa \, x6 \, \text{Cos}[x1 - x4] - lb \, wa \, x1 \, x5 \, \text{Sin}[x1 - x4] + lb \, wa \, x5^2 \, \text{Sin}[x1 - x4]$$

$$\text{In[10]:= } dtdLdqb = mb * lb * x6 + wa * lb * x3 * \text{Cos}[x1 - x4] + wa * lb * x2 * x5 * \text{Sin}[x1 - x4] - wa * lb * x2^2 * \text{Sin}[x1 - x4]$$

$$\text{Out[10]= } lb \, mb \, x6 + lb \, wa \, x3 \, \text{Cos}[x1 - x4] - lb \, wa \, x2^2 \, \text{Sin}[x1 - x4] + lb \, wa \, x2 \, x5 \, \text{Sin}[x1 - x4]$$

$$\text{In[13]:= } \text{eqns} = \{ \\ dtdLdqa - dLdqap == 2 * T1 + 2 * w1 / l2 * T2 - k1 * x2, \\ dtdLdqb - dLdqbp == 2 * T2 - k2 * x5 \\ \}$$

$$\text{Out[13]= } \left\{ -la^2 \, ma \, x2 - mb \, wa^2 \, x2 + (la^2 \, ma + mb \, wb^2) \, x3 - lb \, wa \, x2 \, x5 - lb \, wa \, x5 \, \text{Cos}[x1 - x4] + lb \, wa \, x6 \, \text{Cos}[x1 - x4] - lb \, wa \, x1 \, x5 \, \text{Sin}[x1 - x4] + lb \, wa \, x5^2 \, \text{Sin}[x1 - x4] == 2 \, T1 + \frac{2 \, T2 \, w1}{l2} - k1 \, x2, \right. \\ \left. lb \, mb \, x6 + lb \, wa \, x3 \, \text{Cos}[x1 - x4] - lb^2 \, mb \, x5 \, \text{Cos}[x1 - x4] - lb \, wa \, x2^2 \, \text{Sin}[x1 - x4] + lb \, wa \, x2 \, x5 \, \text{Sin}[x1 - x4] == 2 \, T2 - k2 \, x5 \right\}$$

In[14]:= **Solve[eqns, {x3, x6}]**

Out[14]= $\left\{ \left\{ x3 \rightarrow \frac{-\left(\left(-lb\,wa\,\cos[x1-x4] \left(-2\,T2+k2\,x5-lb^2\,mb\,x5\,\cos[x1-x4]-lb\,wa\,x2^2\,\sin[x1-x4]+lb\,wa\,x2\,x5\,\sin[x1-x4] \right) + lb\,mb \left(-2\,T1-\frac{2\,T2\,w1}{l2}+k1\,x2-la^2\,ma\,x2-mb\,wa^2\,x2-lb\,wa\,x2\,x5-lb\,wa\,x5\,\cos[x1-x4]-lb\,wa\,x1\,x5\,\sin[x1-x4]+lb\,wa\,x5^2\,\sin[x1-x4] \right) \right) \right) }{(lb\,mb\,(la^2\,ma+mb\,wb^2)-lb^2\,wa^2\,\cos[x1-x4]^2)}, x6 \rightarrow \frac{-\left((2\,l2\,la^2\,ma\,T2+2\,l2\,mb\,T2\,wb^2-k2\,l2\,la^2\,ma\,x5-k2\,l2\,mb\,wb^2\,x5-2\,l2\,lb\,T1\,wa\,\cos[x1-x4]-2\,lb\,T2\,w1\,wa\,\cos[x1-x4]+k1\,l2\,lb\,wa\,x2\,\cos[x1-x4]-l2\,la^2\,lb\,ma\,wa\,x2\,\cos[x1-x4]-l2\,lb\,mb\,wa^3\,x2\,\cos[x1-x4]+l2\,la^2\,lb^2\,ma\,mb\,x5\,\cos[x1-x4]+l2\,lb^2\,mb^2\,wb^2\,x5\,\cos[x1-x4]-l2\,lb^2\,wa^2\,x2\,x5\,\cos[x1-x4]-l2\,lb^2\,wa^2\,x5\,\cos[x1-x4]^2+l2\,la^2\,lb\,ma\,wa\,x2^2\,\sin[x1-x4]+l2\,lb\,mb\,wa\,wb^2\,x2^2\,\sin[x1-x4]-l2\,la^2\,lb\,ma\,wa\,x2\,x5\,\sin[x1-x4]-l2\,lb\,mb\,wa\,wb^2\,x2\,x5\,\sin[x1-x4]-l2\,lb^2\,wa^2\,x1\,x5\,\cos[x1-x4]\times\sin[x1-x4]+l2\,lb^2\,wa^2\,x5^2\,\cos[x1-x4]\times\sin[x1-x4]) \right)}{(l2\,lb\,(-la^2\,ma\,mb-mb^2\,wb^2+lb\,wa^2\,\cos[x1-x4]^2))} \right\} \right\}$