

A hands-on tutorial on R and R Studio

A tutorial that might get used for lots of stuff

Tiago A. Marques

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Disclaimer: in this document I copy paste freely from other documents that I have written. Therefore, if you have read these words elsewhere by me, though luck. I claim the right to plagiarize myself here!

Introduction

This tutorial was created as a gentle introduction to the **R** environment via the **RStudio** interface to R. While it could be a general introduction to R, the primary objective of this document is to serve as a “hands-on-tutorial” for courses delivered by me (TAM). I use it for both Ecologia Numérica and Modelação Ecológica, at FCUL, as well as for some other courses. It does not assume any previous knowledge about R, but some basic logic and programming notions would be desirable.

This .Rmd is the main document in the github repository located at:

<https://github.com/TiagoAMarques/AnIntro2RTutorial>

To facilitate the interaction with R we leverage on **RStudio**, a piece of software which allows users to have at a click’s distance many useful features in R. In the following sections of the tutorial you will be guided through a first session of R via RStudio.

The tutorial is intended to follow a brief presentation about R and RStudio, their interaction and capabilities (“Quick introduction to R and R Studio.pptx”, also in this git repository). It assumes that R and RStudio have been previously installed in the computer you are using. The latest version of both software packages is recommended. Both are free and open source.

Preliminaries about R

There is an extensive community revolving around R, and abundant courses, tutorials, books, blogs, list servers, etc, are freely available online.

R might seem frightening at first, but even monsters can make something look more pleasant if you look from the right angle. It is all a matter of perspective :) So I will use the help of some monsters here to convince you that this is the right thing to do!

The amazing images in this document are all by Allison Horst, Artwork by '@allison_horst, and I recommend you visit Allison’s github repository filled up with amazing stats and maths illustrations (<https://github.com/allisonhorst/stats-illustrations>), including so many amazing resources to make R look less frightening. To be honest, this section is actually also an homage to Allison’s outstanding work.

And it is not just about stats. If you do not understand how to find the derivative of a function after looking at Artwork by Allison Horst and her amazing visualization series on the topic, take it as a sign: just give it up, as I suspect you will never will!

Nowadays learning R by example is easy to do, with so many free online resources available to do so.

I recommend that you do it via the RStudio environment, since it provides an integrated environment to integrate with all R things. And there are many! And if you do so, I can guarantee that in no time you will be having fRun.

The advantages of mastering R are priceless, but the learning curve can be daunting at first.

This document is written in RMarkdown, a tool that allows you to build dynamic reports based on R code, providing integrated documents that contain all that is required for a given project, from reading the data in to final results and discussion, passing through all the analysis and results. If you want a gentle introduction to RMarkdown using a hands on tutorial based on a versatile template that will do many of the things you’ll need to get started, look for no more, there is also one here:

<https://github.com/TiagoAMarques/RMarkdownTemplate>



Figure 1: Illustrating R Monsters: Artwork by '@allison_horst

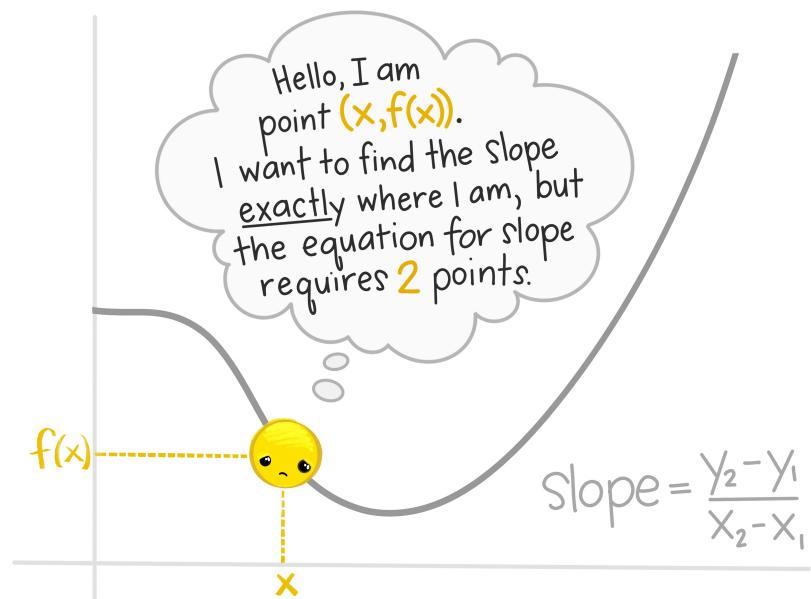


Figure 2: Illustrating a Derivative: Artwork by '@allison_horst

remote R learners,

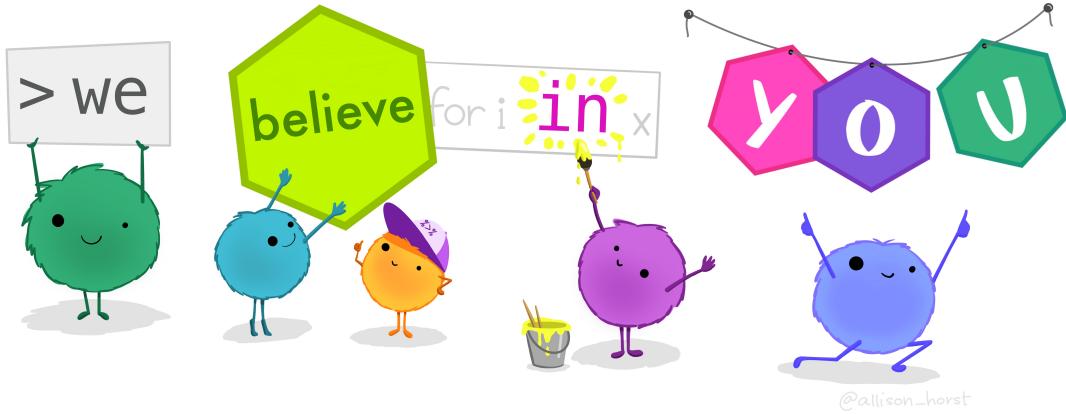


Figure 3: Illustrating learning R online: Artwork by '@allison_horst

Go out and explore, little grasshopper. You will conquer many great things if you do. You will become a code giant one day. But never forget, you need to be thankful to an entire community, and you are standing on the shoulders of giants!

External R resources that might be helpful

We provide here a small list of these that might be particularly helpful for beginners:

- [R webpage](#) - the main R webpage, including links to downloading R, manuals, tutorials, dedicated search engines, etc.
- [Swirl](#) - if you want to learn R interactively from the command line, you might want to try this package. Your own R tutor at your fingertips. Try it!
- [R video tutorials](#) - video how to's in R
- [Online tutorial](#) - a course with interactive exercises
- [Online course](#) - notes for a two-day course in R
- [Reference card](#) - A very handy list of useful R functions
- [Short reference card](#) - A longer reference card with most commonly used R functions
- [Cheat sheets](#) - an incredible useful set of resources from the R Studio team, where self contained subject specific sets of functions are provided for different common tasks

At the end of this tutorial there is a longer list of less introductory/general resources on R that might just have what you were looking for. Disclaimer: this is a random non-exhaustive list of resources I have read and were useful to me at some point. I make no claims they might be useful to you :)



Figure 4: Illustrating having funR: Artwork by '@allison_horst



Figure 5: Illustrating R's learning curve: Artwork by '@allison_horst'

Introduction to R Studio

Typically, if I am using this tutorial in a class room, the student will have been exposed to the PowerPoint [Quick introduction to R and R Studio.pptx](#). If you are not in a class room, you might want to take a look at it. This is also available at the repository

<https://github.com/TiagoAMarques/AnIntro2RTutorial>

right about [here](#).

Nowadays most users (except perhaps die hard command line users) will use some sort of graphical user interface (GUI) to R. While the basic R installation comes with a simple GUI, here we adopt the use of R Studio, which considerably facilitates an introduction to R by providing many shortcuts and convenient features which we introduce next.

A major advantage of RStudio is that it makes it easy for you to type your R code into a script window, which you can easily save, and then send individual lines or blocks of code to the R command line to be acted upon. This way, you have a record of what you have done, in the saved script file, and can easily reproduce it any time you like. We strongly recommend that you save your code script.

Given RStudio has been installed, when you double-click on a R workspace it should open in RStudio. Note that, if this fails, you might have to first associate .Rdata files with RStudio. After the presentation on R and RStudio you just sat through, from within RStudio you should be able to know where to find:

- the command line (bottom left pane ¹)
- the code scripts (top left pane)
- the workspace objects (top right pane)
- the loaded packages and how to load them (bottom right pane)

¹All the tab positions are the RStudio defaults, but this can be customized by the user later.



Figure 6: Illustrating standing on the shoulders of giants: Artwork by '@allison_horst

- the created plots (bottom right pane)
- the help files (bottom right pane)
- a file navigator system akin to windows explorer (bottom right pane)

Note that you can customize the aspect of RStudio (e.g. font size and colors of the smart syntax highlighting scheme) via “Tools|Global options”.

A very handy feature of R Studio is that you can preview the possible arguments of functions, as well as their description, directly when you are inserting the code. Let’s try doing that. Type say `seq()` in the command line or the script window and then place the cursor between the parenthesis and press the “Tab” key... Is this a nice feature or what?

Now we have met RStudio and we know how it can make our life simpler, let’s move on.

Dynamic reports and reproducible research

One of the most amazing features of the integration of R and R Studio is how simple it becomes to work with dynamic reports, built on RMarkdown. This will take you to the next level in data analysis! Actually, this document was itself created as a dynamic report, using RMarkdown. You should explore some of the basics of R Markdown, and you can do so here: https://rmarkdown.rstudio.com/authoring_basics.html. You can find additional details here: <https://rmarkdown.rstudio.com/>. You can read an entire free book on the topic here: <https://bookdown.org/yihui/rmarkdown/>.

Experiment yourself to create one. In R Studio, select File -> New file -> R Markdown..., then just add a title, something like “My first dynamic report” and see what happens. Explore the content of the file just created and see what happens when you press the R Studio button `knit`. Experiment with the created document to try and change some of the output.

Actually, a good way to learn and get up and running fast in RMarkdown is by example. Hence, I have prepared a template that you can use to create without effort a nice dynamic report. Feel free to explore the material here:

<https://github.com/TiagoAMarques/RMarkdownTemplate>

Just download all the files into a folder, `knit` the file `RMarkdownTemplate.Rmd` and off you go.

Imagine the potential when you are analyzing real data, and the data changes after your report is written!

A recent (well, on the 15th January 2021 it was recent. This wording might not age well!) note about latest features in RMarkdown is [here](#).

A first quick session in R Studio

Here we present a brief introduction to R inside R Studio, using a script and the command line. In the coming sections we will mostly consider analysis using dynamic reports via RMarkdown documents (.Rmd), but it is useful to start with a session where you can see objects being created in the global environment.

Open RStudio. By default an empty workspace should appear. If you have an existing workspace, you can open it by selecting `File|Open File`. We recommend that you begin by creating a script file (`Ctrl+Shift+N`, RStudio Shortcut) and use that to save and comment all your code that will be executed during the tutorial. In this way you will have a record of everything you did.

You know that R is ready to receive a command when you see the R prompt on the command line (on the bottom left tab by default in R Studio): `>`. If you type a line of code that is not complete, R presents the `+` character, so that the user knows it expects the conclusion of the current line.

Important note: while the prompt `>` and `+` might not be shown in this tutorial’s code, they are often present in material online. You should not try to add either `>` nor `+` to the command line: this is something that R does for you and will complain if you try to do it yourself! Past experience tells us that more than

one person will have problems because they forgot to delete a > and/or + from code when they copy paste the code into their own R sessions. Avoid being that person!

On the top right corner tab, where objects available in the Environment are listed, you currently have no objects.

Here we just create a couple of objects and use them, but below we will do it again in more detail. Now we just want to create some objects so that we can then save them and retrieve them again.

```
# assign the value 3 to the object hh2
hh2<-3
# assign the value 5 to the object hh3
hh3<-5
# multiply them up
hh2*hh3

## [1] 15
# add them up
hh2+hh3

## [1] 8
#note how you can write comments in R by using "#"
#anything in front of # is not interpreted by R
#and treated as a comment
#you should have the good habit of extensively commenting
#all your code so that you know what you've done
#when you return to it even months or years later
```

We can print an object to the screen by simply typing its name and press enter (despite the fact that currently you can actually see the values on these objects Environment tab - but that is because they are simple objects and the workspace is almost empty.)

```
hh2

## [1] 3
#same as
print(hh2)
```

```
## [1] 3
```

R is a very powerful calculator! Try some simple maths, say for example (you need to press enter after each line so that the line is evaluated)

```
4+3

## [1] 7
log(8)

## [1] 2.079442
sin(pi)

## [1] 1.224606e-16
1234*sqrt(234)-12/23*4^(0.12-0.4)

## [1] 18876.22
```

Tip: There is actually a simpler way to do sourcing from the script file in RStudio. CTRL-Enter is a keyboard shortcut for “source the current line of code in my script file and move the cursor to the next line”. In general

if you like keyboard shortcuts, look in RStudio under the menu **Help | Keyboard shortcuts** - there are probably many more than those you will be able to remember!

It is now time to end our first R session. At this point you need to decide what to do, as all objects created so far are in the memory, but this will be wiped out unless we explicitly save it to a file. The easiest way to do so is by calling the `save.image` function

```
save.image(file="my1stR.Rdata")
```

Note the unusual extension name `.Rdata` associated with R workspaces (an R file is called a workspace). We could now load up this workspace in a new R session, or typically we will load up that workspace by starting R by double clicking on the file created. Do this to see that you retrieve the above created objects. Note that if you already have an R session open, you can load up any previously saved workspace via function `load`.

Finally, just to avoid clutter later, we will delete all the objects created so far

```
#deletes all objects in the dynamic report temporary memory  
rm(list = ls())
```

Note that you have saved your workspace in some directory but you have not defined the directory explicitly. By default, this is your working directory. You can check what that directory currently is by using the following command

```
getwd()
```

```
## [1] "C:/Users/tam2/Dropbox/GithubProjects/AnIntro2RTutorial"
```

You can always change the directory you are working on by setting it up explicitly to your desired location, using

```
#set the working directory - but remember to use your own path!!!  
setwd("C:/Users/tiago/Desktop/mycourse")
```

It is a very good habit to make sure that you are working in the directory you think you are working. Many errors might occur if R can't find some object or file because it is looking on the wrong place.

Now you have used R in RStudio, let's use the power of their integration to work directly in a dynamic report.

Working through R via a dynamic report

Create a new dynamic report using a RMarkdown file, as described above. Comment all you do in the appropriate place. At the end you will have a record that makes it easy to track everything you did, and a template you can use in future classes.

Once you created the RMarkdown from scratch, we can start by creating a new variable.

Note that all the code must go inside code chunks, and you can get them by doing **Code | InsertChunk** or the shortcut **Ctrl+Alt+I**.

An empty code chunk (in the image with a comment added to it!) looks like this:

```
```{r}  
this is just a code comment - code will go here
```
```

We will create a variable called `myvar1` which we will assign the value of 4. This is typically done using the assign operator `<-`.

```
myvar1<-4
```

There are typically multiple ways to do the same thing in R, and this is sometimes referred to as a disadvantage. For simplicity, we deliberately avoid presenting the several alternatives for each action, and concentrate on the ones we prefer. This is not the same as saying these are the best, and if you continue to work with R you will likely get used to doing things your way - for now we do it our way!

An object should have been created in your workspace. You can list all objects in a given workspace using

```
ls()
```

```
## [1] "myvar1"
```

You can also remove any object by using the `rm` function, so here we remove `myvar1`.

```
rm(myvar1)
```

and hence our workspace is empty again.

Task 0: Create some objects and assign numbers to them. Then try to make some basic calculations with the objects you just created. Finally, clean up the workspace again.

Note a key difference between the functions `ls` and `rm`. While the first function does not need any arguments, the second requires at least one argument (but can take several). This can be easily seen by checking their help files and noting that `rm` needs at least 1 explicit argument while `ls` can work with defaults

```
?rm
```

This is a convenient way to obtain more information about a given function. If one does not know what the name of the function might be, one can search for functions containing a given string. The following command lists all the functions with the string `mean` in them.

```
apropos("mean")
```

```
## [1] ".colMeans"      ".rowMeans"      "colMeans"       "kmeans"  
## [5] "mean"           "mean.Date"     "mean.default"   "mean.diffftime"  
## [9] "mean.POSIXct"   "mean.POSIXlt"  "rowMeans"       "weighted.mean"
```

Not surprisingly, most if not all of these functions will be used for some kind of calculation involving a mean. You can look into any one of them using the `?` as above. We have assigned a number to a variable , but we can actually more generally have vectors (strictly, `myvar1` was a numeric vector of length 1) containing a large number of values “inside” them.

The following code assigns some numbers to 5 different vectors.

```
x2<-c(1,2,0.12,4,-22)  
x3<-seq(1,8,by=2)  
# : useful shortcut for sequences with the by argument = 1  
x1<-1:5  
z1<-10:8  
z2<-10:10
```

Take a peak at the objects just created:

```
x1
```

```
## [1] 1 2 3 4 5
```

```
x2
```

```
## [1] 1.00 2.00 0.12 4.00 -22.00
```

```
x3
```

```
## [1] 1 3 5 7
```

```

z1
## [1] 10 9 8
z2
## [1] -10 -9 -8 -7 -6 -5 -4 -3 -2 -1 0 1 2 3 4 5 6 7 8
## [20] 9 10

```

The function `seq` is very useful for setting sequences of numbers. The optional arguments `length.out` and `along.with` provide extra flexibility. Look at `?seq` to find out what the function does and the consequences of using these different arguments.

We can use the usual mathematical operators over vectors. A few examples follow:

```

x1+x2
## [1] 2.00 4.00 3.12 8.00 -17.00
x4<-x1+x2
x5<-x1-x2
x6<-x1*x2
x7<-x1/x2

```

Note by default you do not see results, you need to print them to the report to see them. As an example

```

print(x4)
## [1] 2.00 4.00 3.12 8.00 -17.00

```

it is actually simpler than using `print`, because if you just use the name of the object on the console it gets printed by default

```

x4
## [1] 2.00 4.00 3.12 8.00 -17.00
x5
## [1] 0.00 0.00 2.88 0.00 27.00
x6
## [1] 1.00 4.00 0.36 16.00 -110.00
x7
## [1] 1.0000000 1.0000000 25.0000000 1.0000000 -0.2272727

```

Note that if the vectors are of the same length, R performs the operation element-wise. Another useful (but possibly dangerous) feature is that R recycles vectors if they are not the same length

```

x8<-c(1,2,3,4)
x8+2

```

```

## [1] 3 4 5 6

```

However, if one of the vectors is smaller, unexpected behavior can happen, because R recycles elements regardless (so be careful, a warning is typically produced)

```

x9<-c(3,4,5)
x10<-c(0.7,0.9,1.3)
x9+x10

```

```

## [1] 3.7 4.9 6.3

```

```
x8+x9
```

```
## Warning in x8 + x9: longer object length is not a multiple of shorter object
## length
## [1] 4 6 8 7
```

As expected, a warning message was produced when `x8` and `x9` were added. Usually *these messages are important and should be read!* Quite often the answer to your current question lies in the previous error or warning message.

Another useful function is `rep`, which allows one to create repetitions of patterns. As examples, see the difference between the next two lines of code

```
rep(c(1,2,3,4),times=3)

## [1] 1 2 3 4 1 2 3 4 1 2 3 4

rep(c(1,2,3,4),each=3)

## [1] 1 1 1 2 2 2 3 3 3 4 4 4
```

We have just started R, created and removed some objects, and used simple functions like `ls`, `seq` or `save`. R is an object oriented language, and functions and vectors are just examples of types of objects available in R. In the next section we go through the most commonly used classes of objects in R.

Types and classes of objects

Objects can have classes, which allow functions to interact with them. Objects can be of several classes. We already used the class `numeric`, which is used for general numbers, but there are also additional very commonly used classes:

- `integer`, for integer numbers
- `character`, just for character strings
- `factor`, used to represent levels of a categorical variable
- `logical`, the values TRUE and FALSE

While many others exist, these are the more commonly used. Another type of object which we have already used are functions.

```
class(mean)

## [1] "function"
```

While there are thousands of available functions inside R, later we will learn how to create our own functions.

Outputs of some analyses have special classes, as an example, the output of a call of function `lm` is an object of class `lm`, i.e., a linear model. Many packages introduce special classes for objects, so that functions know how to behave when those objects are used as arguments. Typically, functions behave differently according to the class of an object. As an example, note how `summary` treats differently an object of class `factor` or one of class `numeric`, producing a table of counts per level for a factor but a 6 number summary for numeric values.

```
obj1<-factor(c(rep("a",12),rep("b",4),rep("c",2)))
summary(obj1)

##   a   b   c
## 12  4  2

obj2<-c(2,5,-0.2,89,12,-3,-5.4)
summary(obj2)
```

```
##      Min. 1st Qu. Median     Mean 3rd Qu.    Max.
##     -5.4    -1.6    2.0    14.2    8.5    89.0
```

We can check the class of an object using function `class`, as in the following examples

```
class(obj1)
```

```
## [1] "factor"
```

```
class(obj2)
```

```
## [1] "numeric"
```

```
class(TRUE)
```

```
## [1] "logical"
```

It is sometimes useful to coerce, i.e. force, objects into different classes, but care should be used when doing so. Some examples are presented below. Can you describe in your own words what R did below?

```
as.integer(c(3,-0.3,0.4,0.6,0.9,13.2,12))
```

```
## [1] 3 0 0 0 0 13 12
```

```
as.numeric(c(TRUE,FALSE,TRUE))
```

```
## [1] 1 0 1
```

```
as.numeric(obj1)
```

```
## [1] 1 1 1 1 1 1 1 1 1 1 1 2 2 2 2 3 3
```

A common way to organize multiple vectors together is in the form of a matrix. Here we create such an object

```
mat1<-matrix(1:12,nrow=3,ncol=4)
```

```
mat1
```

```
##      [,1] [,2] [,3] [,4]
```

```
## [1,]    1    4    7   10
```

```
## [2,]    2    5    8   11
```

```
## [3,]    3    6    9   12
```

Note that by default R fills the first column (with 1,2,3) then the second column (4,5,6) etc. If you want it to fill the first row, then the second, you can use the optional argument `byrow=TRUE`, like this:

```
matrix(1:12,nrow=3,ncol=4,byrow=TRUE)
```

```
##      [,1] [,2] [,3] [,4]
```

```
## [1,]    1    2    3    4
```

```
## [2,]    5    6    7    8
```

```
## [3,]    9   10   11   12
```

R also allows data structures with more than 2 dimensions – we don't cover those here, but look up the help on “array” if you're interested. A matrix is just a two dimensional array.

Arrays are useful objects, but can be complex to visualize due to their potential high dimensionality. Another common type of object is a `data.frame`. This is essentially a matrix but for which each column can be of a different type. These are what we would typically associate with an excel spreadsheet or a table in a database. Typically columns correspond to variables observed in a number of subjects, each subject recorded in its own row. A simple example with 3 variables and 5 subjects follows:

```
mysex<-c("male","female","female","male","male")
```

```
myage<-c(34,23,56,45,12)
```

```
myhei<-c(185,178,167,165,148)
```

```

df1<-data.frame(ID=1:5,sex=mysex,age=myage,height=myhei)
df1

##   ID   sex age height
## 1  1 male  34    185
## 2  2 female 23    178
## 3  3 female 56    167
## 4  4 male  45    165
## 5  5 male  12    148

```

Typically, `data.frames` are used to store the data we subsequently analyse. Usually the data are not manually imputed as above, but read into R from other software, using R functions addressed in a later section.

A data frame is just a special type of `list`. A `list` can contain objects of different types and dimensions. An example is here

```

list1<-list(Note="whatever I want here",X2=4,age=1:4)
list1

## $Note
## [1] "whatever I want here"
##
## $X2
## [1] 4
##
## $age
## [1] 1 2 3 4

```

Lists are typically used to store outputs of computations which require different kinds of objects to be recorded. Note the use of `$` to access the sub components of a list or a `data.frame`.

```
list1$X2+10
```

```
## [1] 14
```

Alternatively, one might use index to retrieve elements of a list

```
list1[[3]]+5
```

```
## [1] 6 7 8 9
```

In the next section we will learn more about using indexes to access subsets of data.

Subsetting data

One useful feature of R relates to how we can index subsets of data. The indexing information is included within square brackets: `[]`. As an example, we can select the 3rd element of a vector

```
x<-c(1,3.5,7,8,-7,0.43,-1)
x[3]
```

```
## [1] 7
```

but we can also select all except the second and third elements of the same vector

```
x[-c(2,3)]
```

```
## [1] 1.00 8.00 -7.00 0.43 -1.00
```

We can also select only the objects which follow a given condition, say only those that are positive

```
x[x>0]
## [1] 1.00 3.50 7.00 8.00 0.43
or those between (-1,1)
x[(x>-1) & (x<1)]
```

```
## [1] 0.43
```

Note the subtle difference between the previous and next statements

```
x[(x>=-1) & (x<=1)]
## [1] 1.00 0.43 -1.00
```

which reminds us we should be careful when setting these logical conditions, especially when working with integer boundaries which might be on the limits of those conditions. Note indexing can be done using additional information. As an example, we select here the elements in `x` such that the corresponding elements in `y` are positive:

```
#rnorm(k) produces k Gaussian random deviates
x<-rnorm(10)
y<-rnorm(10)
x2<-x[y>0]
```

When working on a matrix the indexing is done by row and column, therefore for selecting the value that is in the third row and second column of a matrix we use

```
mat1[3,2]
```

```
## [1] 6
```

but we can also select all the elements in the second row

```
mat1[2,]
```

```
## [1] 2 5 8 11
```

or the fourth column

```
mat1[,4]
```

```
## [1] 10 11 12
```

We are often interested in subsetting a dataset by some characteristic of one (or several) of its columns. Here we illustrate with the dataset `iris` (check `?iris` for data details)

```
head(iris)
```

```
##   Sepal.Length Sepal.Width Petal.Length Petal.Width Species
## 1          5.1         3.5         1.4         0.2  setosa
## 2          4.9         3.0         1.4         0.2  setosa
## 3          4.7         3.2         1.3         0.2  setosa
## 4          4.6         3.1         1.5         0.2  setosa
## 5          5.0         3.6         1.4         0.2  setosa
## 6          5.4         3.9         1.7         0.4  setosa
str(iris)
## 'data.frame': 150 obs. of 5 variables:
## $ Sepal.Length: num 5.1 4.9 4.7 4.6 5 5.4 4.6 5 4.4 4.9 ...
## $ Sepal.Width : num 3.5 3 3.2 3.1 3.6 3.9 3.4 3.4 2.9 3.1 ...
```

```
## $ Petal.Length: num  1.4 1.4 1.3 1.5 1.4 1.7 1.4 1.5 1.4 1.5 ...
## $ Petal.Width : num  0.2 0.2 0.2 0.2 0.2 0.4 0.3 0.2 0.2 0.1 ...
## $ Species      : Factor w/ 3 levels "setosa","versicolor",...: 1 1 1 1 1 1 1 1 1 1 ...
```

that contains information about 3 species: setosa, versicolor and virginica. Imagine that we want to do something just with those from species virginica. Then we can create an object holding just that information as

```
iris.3 <- iris[iris$Species=="virginica",]  
summary(iris.3)
```

```
##   Sepal.Length   Sepal.Width    Petal.Length   Petal.Width
## Min.   :4.900   Min.   :2.200   Min.   :4.500   Min.   :1.400
## 1st Qu.:6.225   1st Qu.:2.800   1st Qu.:5.100   1st Qu.:1.800
## Median :6.500   Median :3.000   Median :5.550   Median :2.000
## Mean    :6.588   Mean    :2.974   Mean    :5.552   Mean    :2.026
## 3rd Qu.:6.900   3rd Qu.:3.175   3rd Qu.:5.875   3rd Qu.:2.300
## Max.   :7.900   Max.   :3.800   Max.   :6.900   Max.   :2.500
##           Species
## setosa   : 0
## versicolor: 0
## virginica:50
##
```

Mathematical functions

Within R there are a number of mathematical operators but also mathematical and statistical functions. As any other functions, many of these have required parameters and optional parameters. It would take a very long time to describe even the most basic functions. Therefore, we prefer to let you try hands on explore a number of these.

Task 1: Take your time to explore the functions below: `sum(x)`, `sqrt(x)`, `log(x)`, `log(x,n)`, `exp(x)`, `choose(n,x)`, `factorial(x)`, `floor(x)`, `ceiling(x)`, `round(x,digits)`, `abs(x)`, `cos(x)`, `sin(x)`, `tan(x)`, `acos(x)`, `acosh(x)`, `max(x)`, `min(x)`, `mean(x)`, `median(x)`, `range(x)`, `var(x)`, `cor(x,y)`, `quantile(x)`.

(Tip: do not forget that you can get a full description what each function can be used for, what arguments it takes, and what kind of output it produces, using ?. Further, the help of most functions includes examples of their use, which proves invaluable to understand their usage.)

Importing and exporting data

Rather than importing data into R manually, typically the data we work with are imported from some external source. Typically this might be some simple file format, like a txt or a csv file, but while not covered here, direct import from say Excel files or Access data bases is possible. Such more specialized inputs often require additional packages.

R Studio includes a useful dedicated shortcut **Import dataset**, by default available through the top right window of R Studio's interface. Note this shortcut essentially just calls the appropriate functions required for each import. Here we present a couple of examples just for practicing.

First, we load up a data frame which exists in R (note R includes a large variety of example data sets which are useful to illustrate the use of code) and contains an example data set, with variables measured in 150 flowers of 3 varieties. This is in object `iris`, and we use the function `data` to load it so that we have access to it.

```
data(iris)
```

we can take a look at what this data set contains

```
#example of head use: see the first 4 rows in iris  
head(iris,4)
```

```
##   Sepal.Length Sepal.Width Petal.Length Petal.Width Species  
## 1         5.1      3.5       1.4      0.2   setosa  
## 2         4.9      3.0       1.4      0.2   setosa  
## 3         4.7      3.2       1.3      0.2   setosa  
## 4         4.6      3.1       1.5      0.2   setosa
```

```
#example of str use  
str(iris)
```

```
## 'data.frame': 150 obs. of 5 variables:  
## $ Sepal.Length: num 5.1 4.9 4.7 4.6 5 5.4 4.6 5 4.4 4.9 ...  
## $ Sepal.Width : num 3.5 3 3.2 3.1 3.6 3.9 3.4 3.4 2.9 3.1 ...  
## $ Petal.Length: num 1.4 1.4 1.3 1.5 1.4 1.7 1.4 1.5 1.4 1.5 ...  
## $ Petal.Width : num 0.2 0.2 0.2 0.2 0.2 0.4 0.3 0.2 0.2 0.1 ...  
## $ Species     : Factor w/ 3 levels "setosa","versicolor",...: 1 1 1 1 1 1 1 1 1 1 ...  
#example of summary use  
summary(iris)
```

```
##   Sepal.Length   Sepal.Width   Petal.Length   Petal.Width  
## Min.    :4.300  Min.    :2.000  Min.    :1.000  Min.    :0.100  
## 1st Qu.:5.100  1st Qu.:2.800  1st Qu.:1.600  1st Qu.:0.300  
## Median  :5.800  Median  :3.000  Median  :4.350  Median  :1.300  
## Mean    :5.843  Mean    :3.057  Mean    :4.358  Mean    :1.587  
## 3rd Qu.:6.400  3rd Qu.:3.300  3rd Qu.:5.100  3rd Qu.:1.800  
## Max.    :7.900  Max.    :4.400  Max.    :5.700  Max.    :2.500  
##  
##   Species  
##   setosa    :50  
##   versicolor:50  
##   virginica:50  
##  
##  
##
```

Now we create a new data frame which we then modify to include a new variable

```
mydata<-iris  
mydata$total<-mydata$Sepal.Length+mydata$Sepal.Width+  
mydata$Petal.Length+mydata$Petal.Width
```

Now, we are going to export this data set as a txt, named `mydatafile.txt`

```
write.table(mydata,file="mydatafile.txt",row.names=FALSE)
```

Note the use of the optional argument `row.names=FALSE`, otherwise some arbitrary row names would be added to the file. If you look in the folder you are working in, you should now have a new file there. Open it and check that it looks as you would expect. Next, we are going to import it back into R, into an object named `indat`.

```
indat<-read.table(file="mydatafile.txt",header=TRUE)
```

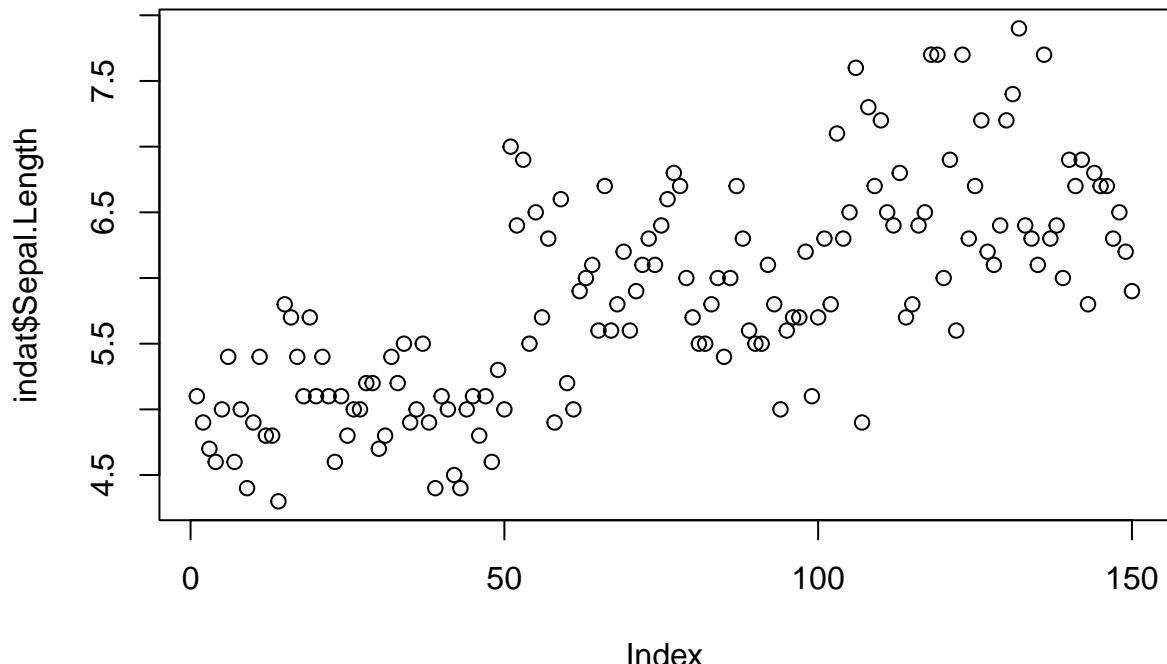
So now we have our data back in R.

Task 2: Import the file `dados1.csv` into R, giving it the name `newfile`. Tips: Explore the possible options including (1) Import Dataset shortcut in the Environment tab, (2) the optional argument `sep=","` in function `read.table` or (3) consider using function `read.csv`.

Graphics

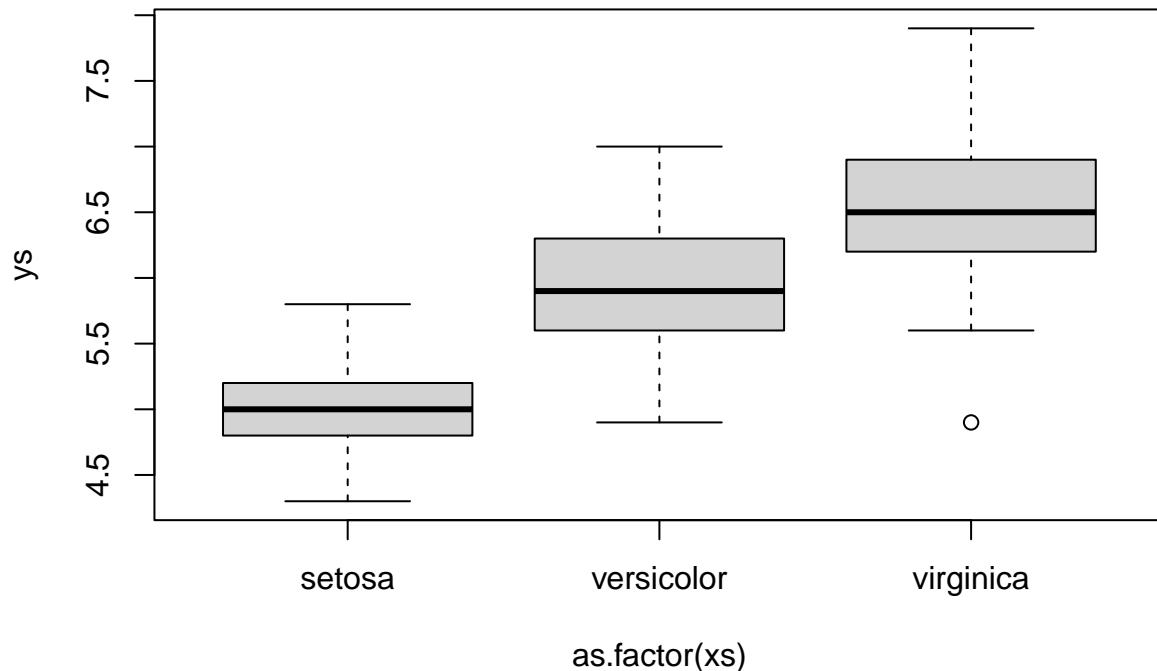
One of the most amazing R capabilities are its graphics customization properties. One can create pretty much any graphic output desirable. The `plot` function is, as we have seen before for function `summary`, a function that attempts to do something smart depending on the type of arguments used. Using the data set `iris` previously considered, plot examples are implemented below, with some optional arguments being used to show some of the possibilities to customize plots.

```
#default use  
plot(indat$Sepal.Length)
```



In the following example, R evaluates the class of one of the arguments as being a factor and hence tries to give you a sensible result, which is producing a boxplot of a numerical variable as a function of a factor.

```
ys<-indat$Sepal.Length  
xs<-indat$Species  
#note use of ~ to represent "as a function of"  
plot(ys~as.factor(xs))
```

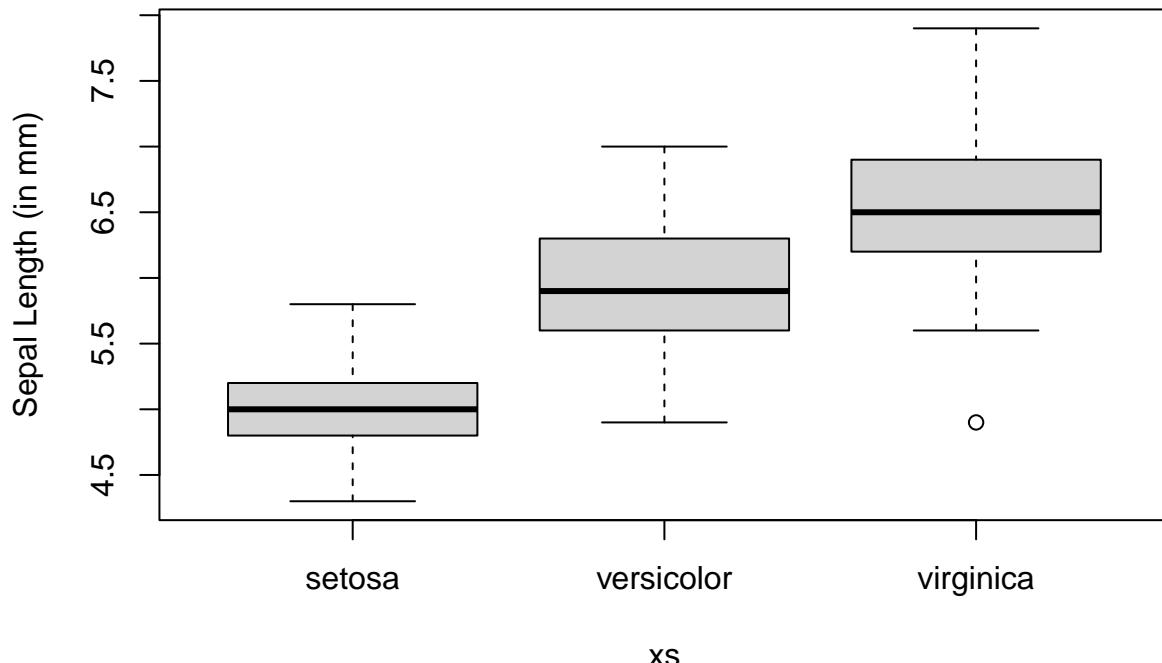


Note the use of `~` to mean “as a function of”; this is also used below when specifying regression models, where the object on the left of `~` will be the response variable and the objects on the right explanatory variables.

We now add some labels to a new plot, using directly function `boxplot` (which in the background `plot` above called), of sepal length as a function of species

```
ys<-indat$Sepal.Length
xs<-indat$Species
#note use of ~ to represent "as a function of"
boxplot(ys~xs,ylab="Sepal Length (in mm)",main="Sepal length by species")
```

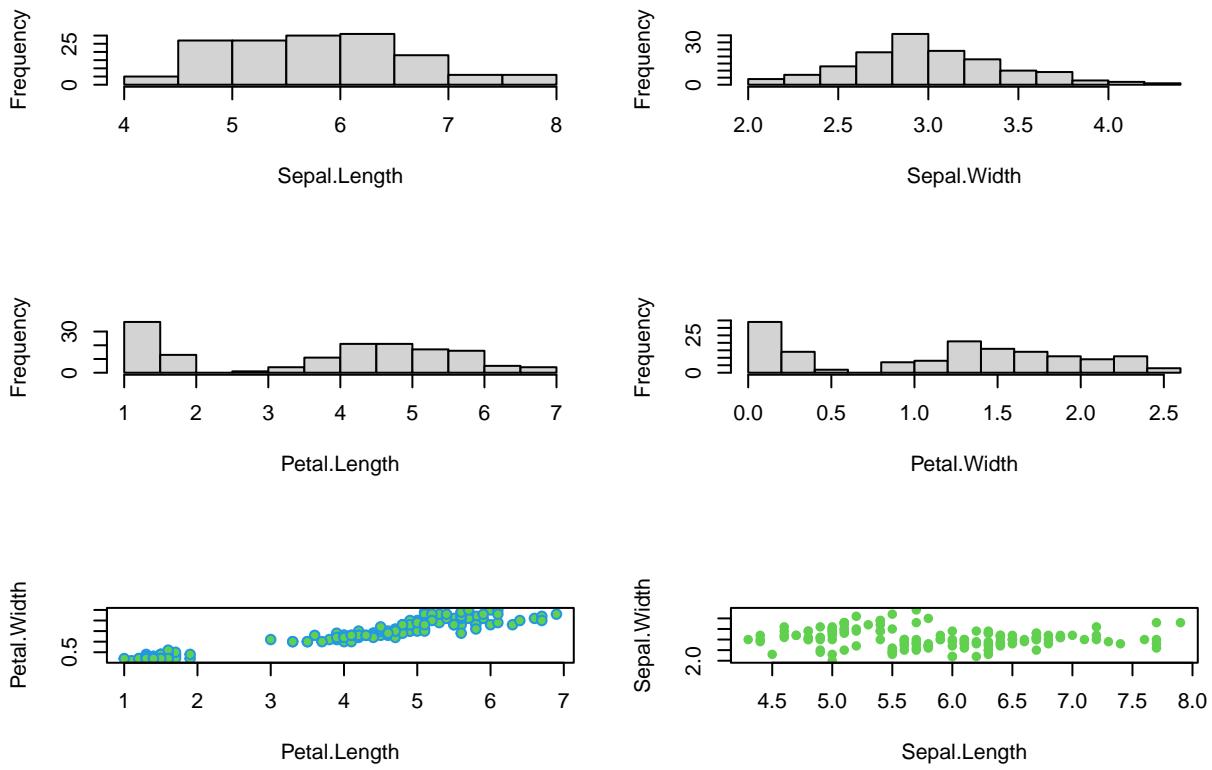
Sepal length by species



```
#compare with this code - next line returns an error
#plot(ys~xs,ylab="Sepal Length (in mm)",main="Sepal length by species")
#making species be a factor - allows the plot below to work well
#xs<-as.factor(indat$Species)
#plot(ys~xs,ylab="Sepal Length (in mm)",main="Sepal length by species")
```

We can also set the graphic window to hold multiple plots. This is obtained via argument `mfrow`, one of the arguments in function. Note this function controls a much larger number of graphical parameters. You can take a look at its help file to get a feel for how many and what kind of control it allows you. An example follows, in which we leverage on the use of function `with` to avoid having to constantly use `indat$` to tell R where the data can be found.

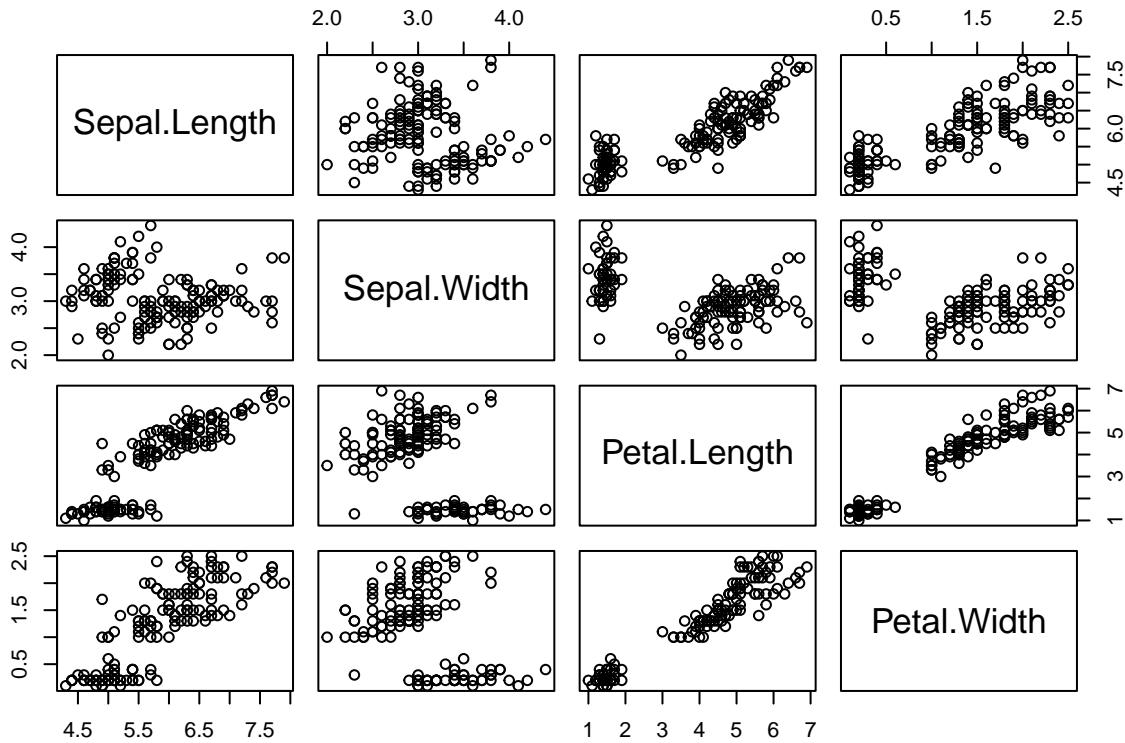
```
#define 3 rows and 2 columns of plots
par(mfrow=c(3,2))
with(indat,hist(Sepal.Length,main=""))
with(indat,hist(Sepal.Width,main=""))
with(indat,hist(Petal.Length,main=""))
with(indat,hist(Petal.Width,main=""))
with(indat,plot(Petal.Length,Petal.Width,pch=21,col=12,bg=3))
with(indat,plot(Sepal.Length,Sepal.Width,pch=16,col=3))
```



We used argument `mfrw`, but looking at the help for function `par` gives you an insight to the level of customization one can reach with respect to these graphical parameters, via dozens of different arguments.

We can look at the correlation structure between all variables using function `pairs`.

```
#note selection of just the first 4 columns, since the last is not numeric
pairs(indat[,1:4])
```



Task 3: Using data `cars`, create a plot that represents the stopping distances as a function of the speed of cars. Use the `points` function to add a special symbol to points corresponding to cars with speed lower than 15 mph, but distance larger than 70m. Check out the function `text` to add text annotations to plots. Customize axis labels.

Extending basic capabilities via packages

While R base installation includes enough functions that getting acquainted with them could take several years, many more are available via the installation of additional packages available online. A package is just a set of functions and data sets (and the corresponding documentation plus some additional required files) which usually have some specific goal. As examples, in our course we will be using packages `vegan` and `mgcv`, which allow the implementation of a variety of numerical ecology techniques and generalized additive models (GAM), respectively.

Note packages cover a very wide range of applications, and chances are that at least a package, often more than one, already exists to implement most kinds of statistical or data processing tasks we might imagine.

Installing a new package in R requires a call to function `install.packages`. A RStudio shortcut is simply to follow the `Tools | Install packages...` shortcut.

After a package is installed it needs to be loaded to be available. In R this is done calling function `library` with the package name as an argument. In RStudio this becomes simpler by checking the boxes under the RStudio tab packages (by default this tab is available on the bottom right window, along with the Files, Plots, Help and Viewer tabs).

We use `vegan` as an example. Notice to begin with that `vegan` is not available yet

```
#  
?vegan
```

Next, we install the package.

```
#  
install.packages("vegan")
```

Then, we load the package

```
#  
library("vegan")
```

```
## Loading required package: permute  
## Loading required package: lattice  
## This is vegan 2.6-4
```

and finally we check that the functions in it are now loaded

```
#  
?vegan
```

We would now be ready to do all sorts of classification and ordination techniques, say.

Task 4: Run the example code available in the help page from package `cca`. Try to understand what is happening.

```
#here are the relevant lines of code to run  
data(varespec)  
data(varechem)  
## Common but bad way: use all variables you happen to have in your  
## environmental data matrix  
vare.cca <- cca(varespec, varechem)  
vare.cca  
plot(vare.cca)
```

Analysis example: regression

One of the most common type of data analysis is a regression model. Despite common and conceptually simple, it is a very powerful way to understand which (and how) of a number of candidate variables, sometimes referred to covariates, independent or explanatory variables, might influence a dependent variable, also often referred as the response. There are many flavors of regression models, from a simple linear regression to complicated generalized additive mixed models. We do not wish to present these in any detail, but to introduce you to some functions that implement these models and the syntax that R uses to describe them.

Let's start with the basics. You have used the `cars` data set above. We use it here again to try to explain the distance a car takes to stop as a function of its speed. We start with a linear model using function `lm`.

```
data(cars)  
mylm1<-lm(dist~speed,data=cars)
```

We have stored the result of fitting the model in object `mylm1`. The function `summary` can be used to print a summary of the fit

```
summary(mylm1)
```

```
##  
## Call:
```

```

## lm(formula = dist ~ speed, data = cars)
##
## Residuals:
##    Min      1Q  Median      3Q     Max 
## -29.069 -9.525 -2.272  9.215 43.201 
## 
## Coefficients:
##             Estimate Std. Error t value Pr(>|t|)    
## (Intercept) -17.5791   6.7584  -2.601   0.0123 *  
## speed        3.9324   0.4155   9.464 1.49e-12 *** 
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1 
## 
## Residual standard error: 15.38 on 48 degrees of freedom
## Multiple R-squared:  0.6511, Adjusted R-squared:  0.6438 
## F-statistic: 89.57 on 1 and 48 DF,  p-value: 1.49e-12

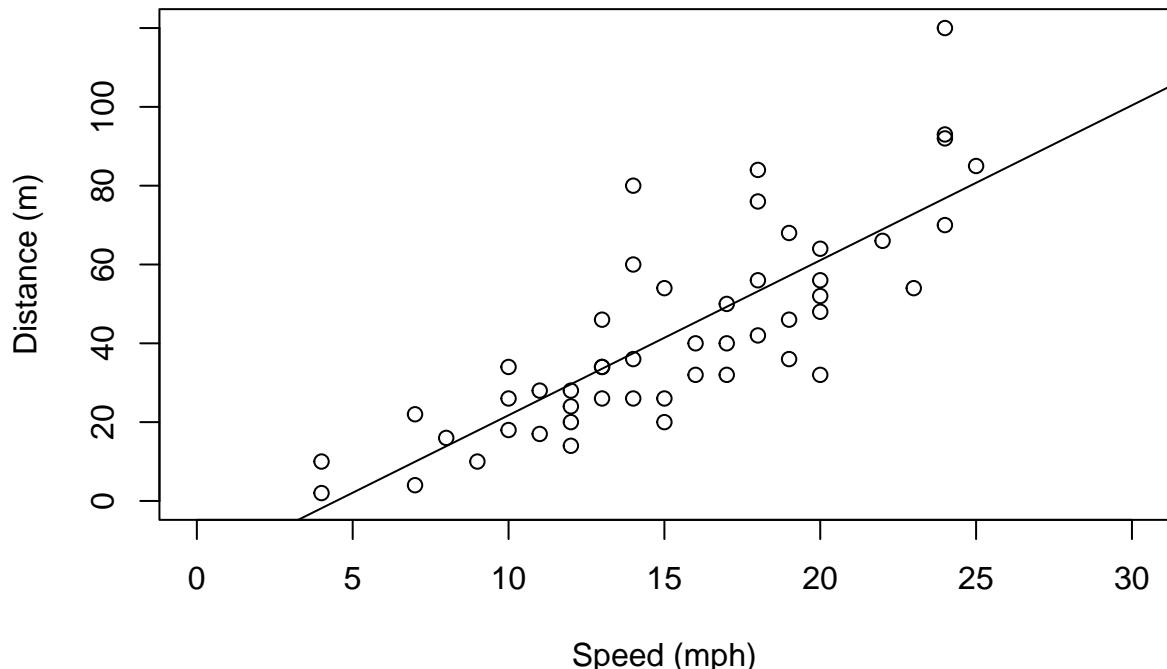
```

Do not get frightened about all the output. The coefficient associated with speed tells us what intuition alone would anticipate, the higher the speed, the larger the distance a car takes to stop. The easier way to see the relationship is by adding a line to the plot (note this is a similar plot to what you should have created in task 3 above!). The predicted relationship is shown in figure ??.

```

xl<-"Speed (mph)"
yl<-"Distance (m)"
plot(cars$speed,cars$dist,xlab=xl,ylab=yl,ylim=c(0,120),xlim=c(0,30))
abline(mylm1)

```



Note how function `abline` is used with a linear model as its first argument and it uses the parameters in said object to add a line to the plot. The optional arguments `v` and `h` are often very useful to draw vertical and horizontal lines in plots.

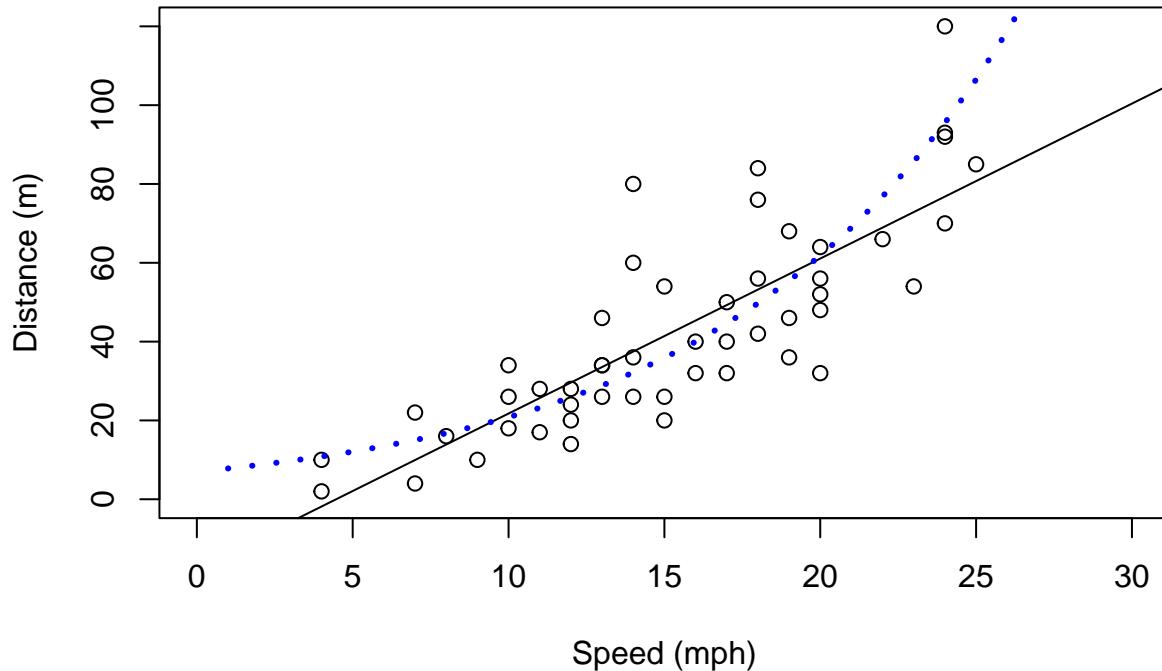
Task 5: Use `abline` to draw dashed lines (tip, use optional argument `lty=2`) representing the estimated distance that a car moving at 16 mph would take to stop.

Note that the line added to the plot represents the distance a car would take to stop given its speed. Oddly enough, it seems like a car going at 3 mph might take a negative time to stop, which is just plain nonsense. Why? Because we used a model which does not respect the features of the data. A stopping distance can't be negative! However, implicit in the linear model we used, distance is a Gaussian (=normal) random variable. We can avoid this by using a generalized linear model (GLM). Now the response can have a range of distributions. An example of such distribution that takes only positive values is the gamma distribution. We implement a gamma GLM next

```
#fit the GLM
myglm1<-glm(dist~speed,data=cars,family=Gamma(link=log))
#predict using the GLM for speeds between 1 and 30
predmyglm1<-predict.glm(myglm1,
newdata<-data.frame(speed=1:30),type="response")
```

Our model now assumes the response has a gamma distribution, and the link function is the logarithm. The link function allows you to change how the mean value is related to the covariates. This becomes rather technical rather fast. Details about GLMs are naturally beyond the scope of this tutorial. References like Faraway (2006) or Zuur *et al.* (2009) will provide further details in an applied context. The predicted relationship is shown in the next figure.

```
#create a plot
plot(cars$speed,cars$dist,xlab="Speed (mph)",
ylab="Distance (m)",ylim=c(0,120),xlim=c(0,30))
#add the linear fit
abline(myglm1)
#and now add the glm predictions
lines(1:30,predmyglm1,col="blue",lwd=3,lty=3)
```



However, this GLM still requires that the response is linear at some scale (in this case, on the scale of the link function). Sometimes, non-linear effects are present. These can be fitted using generalized additive models. A good introduction to GAMs is provided by Wood (2006) and Zuur *et al.* (2009).

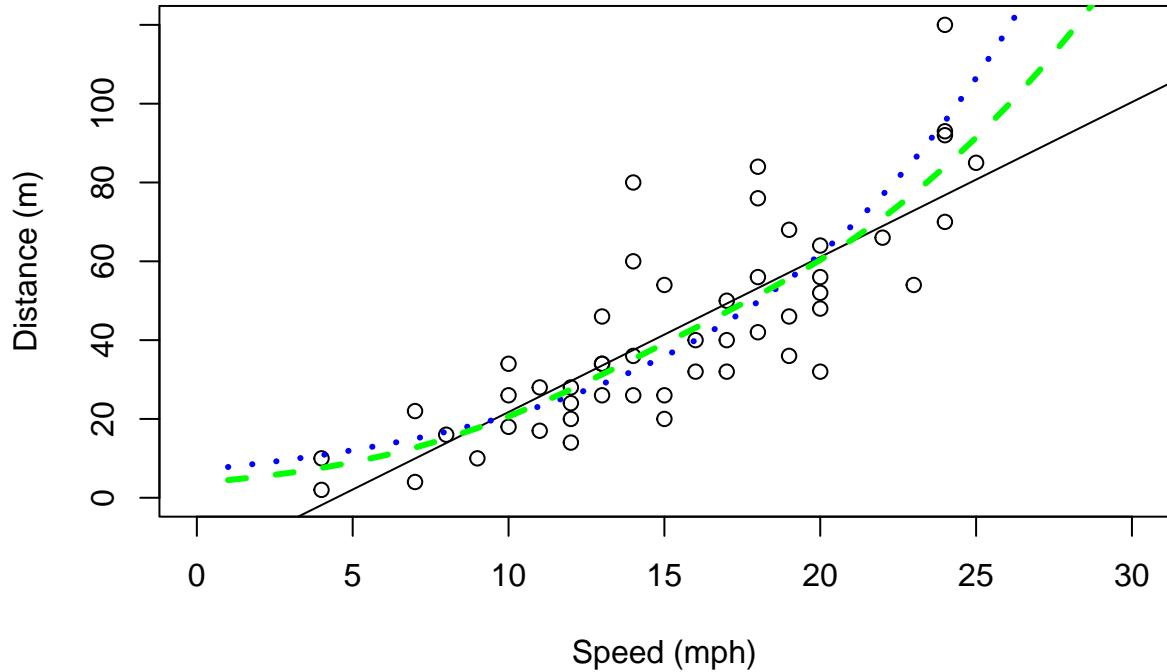
So finally we fit a GAM model to the same data set. For that we require library `mgcv`. The outcome is shown below. Here the fit is not very different from the GLM fit, but under many circumstances a GAM might be required over a GLM. We will see such an example in the next few days, when we model the detectability of beaked whale clicks as a function of distance and angle (with respect to hydrophones).

```
#load the mgcv library
library(mgcv)

## Loading required package: nlme
## This is mgcv 1.8-41. For overview type 'help("mgcv-package")'.
#fit the GAM
mygam1<-gam(dist~s(speed),data=cars,family=Gamma(link=log))
#predict using the GAM for speeds between 1 and 30
predmygam1<-predict(mygam1,newdata=data.frame(speed=1:30),
type="response")

#create a plot
plot(cars$speed,cars$dist,xlab="Speed (mph)",
ylab="Distance (m)",ylim=c(0,120),xlim=c(0,30))
#add the linear fit
abline(mylm1)
#and now add the GLM predictions
lines(1:30,predmyglm1,col="blue",lwd=3,lty=3)
```

```
lines(1:30,predmygam1,col="green",lwd=3,lty=2)
```



Simulation and random number generation

Another powerful use of R is for simulation. To this end, R has the ability to simulate random deviates from a large number of distributions. Perhaps the more useful and commonly used are the uniform and the Gaussian distributions. We now create 50 random deviates from each of these, as well as some Poisson deviates, for illustration

```
#generate 50 pseudo-random Gaussian numbers with mean 20 and standard deviation 3
rnorm<-rnorm(50,mean=20,sd=3)
#generate 50 pseudo-random 50 uniform numbers between 3 and 6
rdunif<-runif(50,min=3,max=6)
#generate 50 pseudo-random 50 Poisson numbers with mean 6
rpois<-rpois(50,lambda=6)
```

R can create random numbers from many different distributions (see `help(Distributions)` for a list) – the relevant functions generally start with `r` and then an abbreviated distribution name (`rbinom`, `rexp`, `rgeom`, etc). Additionally, R also includes the ability to obtain the density function, distribution function and quantile function via the `d+name`, `p+name` and `q+name` functions. As an example, the Gaussian function usage of these functions is presented below

```
dnorm(0,mean=0,sd=1)
```

```
## [1] 0.3989423
```

```

pnorm(0,mean=0,sd=1)

## [1] 0.5

qnorm(0.975,mean=0,sd=1)

## [1] 1.959964

```

Task 6: Using what you have learnt here, create two histograms, one of 50, another of 5000, random deviates from a Gaussian distribution (you can choose the mean and standard deviation you prefer!), using the optional argument `freq=FALSE` (leading to an estimate of the density function). Then add a line to the plot that represents the true underlying density (tip, you can use function `dnorm`), and comment on the results. You can also do similar experiments with other distributions. How weird are a $\text{beta}(1,1)$, a $\text{beta}(1,5)$ and a $\text{beta}(0.5,0.5)$ distributions. Can you guess which one is sometimes referred to as bath tub distribution. What might be a beta useful for?

Programming tricks

Some very useful programming structures are those required to evaluate conditional statements and those used to repeat statements many times. These are fundamental for implementing simulations. In R we have `if` statements and `for` loops, respectively.

As an example, see how an `if` statement works

```

X=2
if (X>0) print(X+3)

## [1] 5

```

One can also use an `if-else` statement, which executes either (1) something or (2) something else, depending on the condition being TRUE or FALSE. Here's an example:

```

X=2
if (X>0)
  {Y=abs(X)} else
  {Y=X^2}
Y

## [1] 2

X=-5
if (X>0)
  {Y=abs(X)} else
  {Y=X^2}
Y

## [1] 25

```

on the other side, here's how a `for` loop works

```

n=4
X=1:n
for (i in 1:n) print(i+3)

## [1] 4
## [1] 5
## [1] 6
## [1] 7

```

note there is nothing special about the use of `i` for an index; you can use any index that you might want

```
n=4
X=1:n
for (j in 1:n) print(sum(c(j,j+3)))
```

```
## [1] 5
## [1] 7
## [1] 9
## [1] 11
```

or even

```
n=4
X=1:n
for (i in X) {
  cat(paste("The i currently is:",i),sep="\n")
  cat(paste("The i+3 currently is:",i+3),sep="\n")
}
```

```
## The i currently is: 1
## The i+3 currently is: 4
## The i currently is: 2
## The i+3 currently is: 5
## The i currently is: 3
## The i+3 currently is: 6
## The i currently is: 4
## The i+3 currently is: 7
```

See above, explore R. Change the code. Repeat. Check for yourself what `cat` and `paste` can be used for!

Task 7: Create 9 histograms of samples of Gaussian random variables, adding the mean value on the plot as a vertical dashed line, in blue if the mean of the observations is positive and in red if the mean of the observations is negative.

Other interesting structures for “control flow” are the `while`, `repeat` and `break`. Look into the help, `?if`, to see details.

Writing your own functions

While the above functions, and the many more available, make R a very useful tool, there are sometimes problems which require a special tool. For these, we can create our own functions. Note this is an advanced topic.

The way of doing that follows a specific syntax

```
> name <- function(arg1,arg2,...) {what the function does goes here}
```

As an example, we create a function that returns the sum of its 2 arguments:

```
myfun<-function(i,j){
  myres<-i+j
  return(myres)
}
```

You can now see the function in the works

```
myfun(3,5)
```

```
## [1] 8
```

Note a function could have many arguments, none, or just one.

Task 7: create a function called `mystats` which returns the mean, variance, maximum and minimum of the first, and only, argument (a vector). Then, update your function such that it can also return the mean excluding the negative numbers. Then, create some other function you might think could be useful.

Creating your own functions will unleash strong R power, increasing significantly your ability to manipulate, analyze and simulate data.

A final task integrating all of the above

This task is only intended for the students in Modelação Ecológica. If you are a Ecologia Numérica student you can try it at your own risk! If you are neither of those, then feel free to work through the material regardless.

Here we will implement an exercise were we pretend we are sampling an animal population, using some (very basic) simulations to understand the process better. Create plots that represent all the steps of your task, with proper legends, labels, colors, etc, and add all your comments to the dynamic report.

This exercise simulates a distance sampling survey. If you want to know more about it, you can check this 2 page introduction paper on the topic [here](#). It is one of the most often used methods to estimate the abundance and/or density of wildlife populations.

1. Simulate the positions of 10000 animals in a study area, with length 10km and width 1km. Assume that any animal has an equal chance to be at any location in the study area (this corresponds to a uniform density surface).
2. Generate a transect at a random location along the study area.
3. Assume that you can potentially detect at most animals up to 500 meters from your transect. Count all the animals that you would detect if detection was perfect across your transect.
4. Consider that animals far from your transect are harder to detect - yes, you are doing distance sampling! Define a function that represents a distance sampling half-normal detection function. If you do not know what that looks like check [here](#), around slide 9. Assume that sigma=200m.
5. Simulate the detection process and get a sample of those animals detected. This is the hard bit, creating an animal detector. Tip: using `rnorm` will help. Ask me for details if you need them.
6. Create a plot that allows you to estimate (at this stage just a visual guess is needed) the detection probability.
7. Repeat the sampling process 500 times, and store the number of animals detected in each one of your simulated surveys.
8. plot the distribution of the number of animals that you would detect each new survey.

Take your own conclusions about all that you did.

Wrap up

A full introduction to R course could take an entire week. A full course in regression modelling with R could take an entire semester. A full course of data analysis in R could take a life time.

Our objective with this tutorial was simply to introduce you to R such that when we use R in the next few days, the commands do not look too esoteric. Nonetheless, this material, as well as the references provided, should constitute a good basis to learn R further if you so desire.

Beginners find the R learning curve is often steep, but once mastered, R simplifies enormously the task of statistical data analysis.

Finally, to promote good habits, we clean the workspace. An organized workspace is very important!

```
#cleaning the workspace  
rm(list = ls())
```

Random R stuff I used and might be worth exploring

This is a non-exhaustive, non-comprehensive and quite random list of R (and related) resources that I found useful at some point. Feel free to explore at your own risk. No real order in the list I am afraid.

- [Ten awesome R Markdown tricks](#): R Markdown is more versatile than you might think by Keith McNulty (Dec 18, 2020, 8 min read). A preview: “Though I code in both R and Python, R Markdown is my only route for writing reports, blogs or books. It is incredibly flexible, has many beautiful design options and supports many output formats really nicely. If you have never worked in R Markdown, I highly recommend it. If you have worked in it before, here are ten little tricks I’ve learned which have served me well in numerous projects, and which highlight how flexible it is.”
- [A course on GAM’s](#) by Noam Ross
- [Introduction to Linear, Generalized, and Mixed/Multilevel models with R](#) by Francisco Rodriguez-Sanchez (the first couple of slides are fantastic introduction to modern statistical analysis in a unified GLM framework). Found about this via a [tweet](#).
- [GIS and mapping in R: Introduction to the sf package](#) by Olivier Gimenez
- [R for biologists](#) - the name says it all
- [Introduction to R for Biologists](#) by Maria Doyle, Jessica Chung, Vicky Perreau
- [Introduction to R for Biologists](#) by Sheri Sanders
- [Fundamentals of R for Biologists](#) Fundamentals of R for Biologists is a self-guided crash course in how to use R specifically geared for those working in the biological sciences. All of the lessons in this course are bundled together into a single PDF textbook: Fundamentals of R for Biologists. You can easily access this text [here](#)
- [A short thread of rstats resources made freely available online](#) by Danielle Navarro

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References

- Faraway, J.J. (2006). *Extending the linear model with r*. Chapman & Hall / CRC.
Wood, S.N. (2006). *Generalized additive models: An introduction with r*. CRC/Chapman & Hall.
Zuur, A.F., Ieno, E.N., Walker, N., Saveliev, A.A. & Smith, G.M. (2009). *Mixed effects models and extensions in ecology with r*. Springer.