

1) c

Probabilistic Interpretation in slide 11:

$$L(w) = \left(\frac{1}{\sqrt{2\pi}\sigma} \right)^N \exp \left(- \frac{\sum_{n=1}^N (y_n - w^T x_n)^2}{2\sigma^2} \right)$$

1. First Step: Let's assume we have bias:

$$L(w) = \left(\frac{1}{\sqrt{2\pi}\sigma} \right)^N \exp \left(- \frac{\sum_{n=1}^N (y_n - w_0 - w^T x_n)^2}{2\sigma^2} \right)$$

2. Apply log:

$$\ell(w) = \frac{1}{2\sigma^2} \sum_{n=1}^N (y_n - w_0 - w^T x_n)^2 - N \left(\frac{1}{2} \log \sigma^2 - \log \sqrt{2\pi} \right) =$$

$$= \left\{ \frac{1}{2\sigma^2} \sum_{n=1}^N (y_n - w_0 - w^T x_n)^2 - \frac{N}{2} \log \sigma^2 \right\} - \underbrace{\log \sqrt{2\pi}}_{\text{constant term!}}$$

$$= \frac{1}{2} \left(\frac{1}{\sigma^2} \sum_{n=1}^N (y_n - w_0 - w^T x_n)^2 - N \log \sigma^2 \right) + \text{constant}$$

$$= \frac{1}{2} \left(\underbrace{\sum_{n=1}^N \frac{1}{\sigma^2} (y_n - w_0 - w^T x_n)^2}_{=C_N} - N \log \sigma^2 \right) + \text{constant}$$

$= C_N$, this means that the cost may vary according to N size (we can check the term $\boxed{N \log \sigma^2}$).

Also, if N size varies, one may expect that sigma also varies, thus, influencing the error function.