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A Complete Tutorial on Ridge and Lasso Regression in Python

AARSHAY JAIN (HTTPS://WWW.ANALYTICSVIDHYA.COM/BLOG/AUTHOR/AARSHAY/), JANUARY 28, 2016



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Introduction

When we talk about Regression, we often end up discussing Lineareand Logistics Regression. But, that's not the end. Do you know there are 7 types of Regressions (https://www.analyticsvidhya.com/blog/2015/08/comprehensive-guide-regression/)?

Contact Number Linear and logistic regression is just the most loved members from the family of regressions. Last week, I saw a recorded talk at NYC Data Science Academy (http://nycdatascience.com/featured-talk-1-kaggle-datascientist-owen-zhang/) from Owen Zhang, current Kaggle rank 3 (https://www.kaggle.com/owenzhang1) and Chief Product Officer at DataRobot. He said, 'if you are using regression without regularization, you have to be very special!'. I hope you get what a person of his stature referred to.

I understood it very well and decided to explore regularization techniques in detail.

In this article, I have explained the complex science behind 'Ridge Regression' and 'Lasso Regression' which are the most fundamental regularization techniques, sadly still not used by many.

The overall idea of regression remains the same. It's the way in which the model coefficients are determined which makes all the difference. I strongly encourage you to go through multiple regression before reading this. You can take help from https://www.analyticsvidhya.com/blog/2015/10/regression-python-beginners/) or any other preferred material.



(https://www.analyticsvidhya.com/wp-content/uploads/2016/01/ridge.jpg)

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- 6. Conclusion Comparing Ridge and Lasso Regression

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1. Brief Overview

Ridge and Lasso regression are powerful techniques generally used for creating parsimonious models in presence of a 'large' number of features. Here 'large' can typically mean either of two things:

- 1. Large enough to enhance the *tendency of a model to overfit* (as low as 10 variables might cause overfitting)
- 2. Large enough to *cause computational challenges*. With modern systems, this situation might arise in case of millions or billions of features

Though Ridge and Lasso might appear to work towards a common goal, the inherent properties and practical use cases differ substantially. If you've heard of them before, you must know that they work by penalizing the magnitude of coefficients of features along with minimizing the error between predicted and actual observations. These are called 'regularization' techniques. The key difference is in how they assign penalty to the coefficients:

1. Ridge Regression:

- Performs L2 regularization, i.e. adds penalty equivalent to square of the magnitude of coefficients
- Minimization objective = LS Obj + α * (sum of square of coefficients)

2. Lasso Regression:

- Performs L1 regularization, i.e. adds penalty equivalent to absolute value of the magnitude of coefficients
- Minimization objective = LS Obj + α * (sum of absolute value of coefficients)

Note that here 'LS Obj' refers to 'least squares objective', i.e. the linear regression objective without regularization.

If terms like 'penalty' and 'regularization' seem very unfamiliar to you, don't worry we'll talk about these in more detail through the course of this article. Before digging further into how they work, lets try to get some intuition into why penalizing the magnitude of coefficients should work in the first place.

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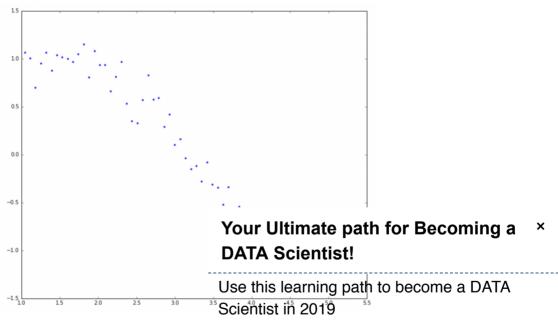
2. Why Penalize the Magnitude of Coefficients (See this learning path to become a DATA Scientist in 2019

Lets try to understand the impact of model complexity on the magnitude of coefficients. As an example, I have simulated a **sine curve** (between 60° and 300°) and added some random noise using the following code:

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```
#Importing libraries. The same will be used throughout the article.
import numpy as np
import pandas as pd
import random
import matplotlib.pyplot as plt
%matplotlib inline
from matplotlib.pylab import rcParams
rcParams['figure.figsize'] = 12, 10
#Define input array with angles from 60deg to 300deg converted to radians
x = np.array([i*np.pi/180 for i in range(60,300,4)])
np.random.seed(10) #Setting seed for reproducability
y = np.sin(x) + np.random.normal(0,0.15,len(x))
data = pd.DataFrame(np.column_stack([x,y]),columns=['x','y'])
plt.plot(data['x'],data['y'],'.')
```

The input-output looks like:



(https://www.analyticsvidhya.com/wp-content/uploads/2016/01/1.sine-curve.png)

Name

This resembles a sine curve but not exactly because of the noise. We'll use this as an example to test different scenarios in this article. Lets try to estimate the sinferfeind on using polynomial regression with powers of x form 1 to 15. Lets add a column for each power upto 15 in our dataframe. This can be accomplished using the following code:

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The dataframe looks like:

```
0
   1.047198
              1.065763
                         1.096623
                                   1.148381
                                                         1.259340
                                              1.202581
                                                                    1.318778
1
   1.117011
              1.006086
                         1.247713
                                   1.393709
                                              1.556788
                                                         1.738948
                                                                    1.942424
2
   1.186824
                                                         2.354677
              0.695374
                         1.408551
                                   1.671702
                                              1.984016
                                                                    2.794587
   1.256637
              0.949799
                         1.579137
                                   1.984402
                                                         3.133642
                                                                    3.937850
3
                                              2.493673
   1.326450
              1.063496
                         1.759470
                                   2.333850
                                              3.095735
                                                         4.106339
                                                                    5.446854
                                          x 10
        x 7
                   x 8
                               x 9
                                                      x 11
                                                                  x 12
                                                                              x 13
   1.381021
0
              1.446202
                          1.514459
                                      1.585938
                                                  1.660790
                                                              1.739176
                                                                          1.821260
   2.169709
              2.423588
                          2.707173
                                      3.023942
                                                  3.377775
                                                              3.773011
                                                                          4.214494
1
2
   3.316683
              3.936319
                          4.671717
                                      5.544505
                                                  6.580351
                                                              7.809718
                                                                          9.268760
3
   4.948448
              6.218404
                          7.814277
                                      9.819710
                                                 12.339811
                                                             15.506664
                                                                         19.486248
   7.224981
              9.583578
                         12.712139
                                     16.862020
                                                22.366630
                                                             29.668222
                                                                         39.353420
        x 14
                    x 15
                1.997235
    1.907219
0
1
    4.707635
                5.258479
   11.000386
               13.055521
   24.487142
               30.771450
   52.200353
               69.241170
```

(https://www.analyticsvidhya.com/wp-content/uploads/2016/01/1.2-15-powers.png)

Now that we have all the 15 powers, lets make 15 different linear regression models with each model containing variables with powers of x from 1 to the particular model number. For example, the feature set of model 8 will be $-\{x, x_2, x_3, ..., x_8\}$.

First, we'll define a generic function which takes in the real parts of the parts o

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'Residual Sum of Squares' which is nothing but the sum of **square ভিন্তা ভারতি কিন্তা ভারতি কিন্তি কিন্তি কিন্তি কিন্তা ভারতি কিন্তা**

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```
#Import Linear Regression model from scikit-learn.
from sklearn.linear_model import LinearRegression
def linear_regression(data, power, models_to_plot):
   #initialize predictors:
   predictors=['x']
   if power>=2:
        predictors.extend(['x_%d'%i for i in range(2,power+1)])
   #Fit the model
   linreg = LinearRegression(normalize=True)
   linreq.fit(data[predictors],data['y'])
   y_pred = linreg.predict(data[predictors])
   #Check if a plot is to be made for the entered power
    if power in models_to_plot:
        plt.subplot(models_to_plot[power])
        plt.tight_layout()
        plt.plot(data['x'],y_pred)
        plt.plot(data['x'],data['y'],'.')
        plt.title('Plot for power: %d'%power)
   #Return the result in pre-defined format
    rss = sum((y_pred-data['y'])**2)
   ret = [rss]
    ret.extend([linreg.intercept_])
    ret.extend(linreg.coef_)
                                                 Your Ultimate path for Becoming a
    return ret
                                                 DATA Scientist!
```

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Note that this function will not plot the model fit for all the powers but with return the RSS and coefficients for all the models. I'll skip the details of the code for now to maintain brevity. I'll be happy to discuss the same through comments below if required.

Name

Now, we can make all 15 models and compare the results. For each analysis, we'll store all the results in a Pandas dataframe and plot 6 models to get an idea of the trend. Consider the following code:

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```
#Initialize a dataframe to store the results:
col = ['rss','intercept'] + ['coef_x_%d'%i for i in range(1,16)]
ind = ['model_pow_%d'%i for i in range(1,16)]
coef_matrix_simple = pd.DataFrame(index=ind, columns=col)

#Define the powers for which a plot is required:
models_to_plot = {1:231,3:232,6:233,9:234,12:235,15:236}

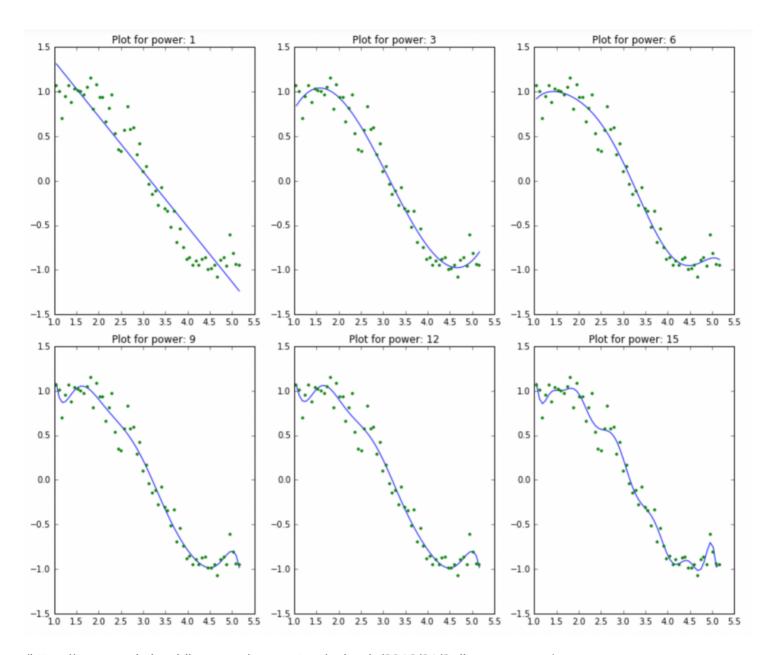
#Iterate through all powers and assimilate results
for i in range(1,16):
    coef_matrix_simple.iloc[i-1,0:i+2] = linear_regression(data, power=i, models_to_plot=m)
odels_to_plot)
```

We would expect the models with increasing complexity to better fit the data and result in lower RSS values. This can be verified by looking at the plots generated for 6 models:

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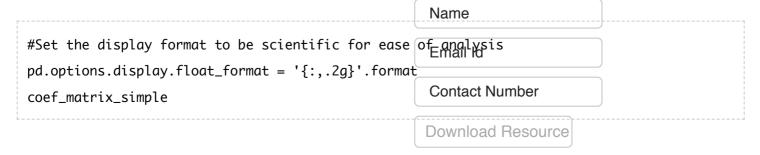
(https://www.analyticsvidhya.com/wp-content/uploads/2016/01/2.-lin-reg-op.png)

This clearly aligns with our initial understanding. As the reven smaller deviations in the training data set. Though the some time and come to our main objective, i.e. the impanalysed by looking at the data frame created above.

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Python Code:



The output looks like:

	rss	intercept	coef_x_1	coef_x_2	coef_x_3	coef_x_4	coef_x_5	coef_x_6	coef_x_7	coef_x_8	coef_x_9	coef_x_10	coef_x_11
model_pow_1	3.3	2	-0.62	NaN	NaN								
model_pow_2	3.3	1.9	-0.58	-0.006	NaN	NaN							
model_pow_3	1.1	-1.1	3	-1.3	0.14	NaN	NaN						
model_pow_4	1.1	-0.27	1.7	-0.53	-0.036	0.014	NaN	NaN	NaN	NaN	NaN	NaN	NaN
model_pow_5	1	3	-5.1	4.7	-1.9	0.33	-0.021	NaN	NaN	NaN	NaN	NaN	NaN
model_pow_6	0.99	-2.8	9.5	-9.7	5.2	-1.6	0.23	-0.014	NaN	NaN	NaN	NaN	NaN
model_pow_7	0.93	19	-56	69	-45	17	-3.5	0.4	-0.019	NaN	NaN	NaN	NaN
model_pow_8	0.92	43	-1.4e+02	1.8e+02	-1.3e+02	58	-15	2.4	-0.21	0.0077	NaN	NaN	NaN
model_pow_9	0.87	1.7e+02	-6.1e+02	9.6e+02	-8.5e+02	4.6e+02	-1.6e+02	37	-5.2	0.42	-0.015	NaN	NaN
model_pow_10	0.87	1.4e+02	-4.9e+02	7.3e+02	-6e+02	2.9e+02	-87	15	-0.81	-0.14	0.026	-0.0013	NaN
model_pow_11	0.87	-75	5.1e+02	-1.3e+03	1.9e+03	-1.6e+03	9.1e+02	-3.5e+02	91	-16	1.8	-0.12	0.0034
model_pow_12	0.87	-3.4e+02	1.9e+03	-4.4e+03	6e+03	-5.2e+03	3.1e+03	-1.3e+03	3.8e+02	-80	12	-1.1	0.062
model_pow_13	0.86	3.2e+03	-1.8e+04	4.5e+04	-6.7e+04	6.6e+04	-4.6e+04	2.3e+04	-8.5e+03	2.3e+03	-4.5e+02	62	-5.7
model_pow_14	0.79	2.4e+04	-1.4e+05	3.8e+05	-6.1e+05	6.6e+05	-5e+05	2.8e+05	-1.2e+05	3.7e+04	-8.5e+03	1.5e+03	-1.8e+02
model_pow_15	0.7	-3.6e+04	2.4e+05	-7.5e+05	1.4e+06	-1.7e+06	1.5e+06	-1e+06	5e+05	-1.9e+05	5.4e+04	-1.2e+04	1.9e+03

(https://www.analyticsvidhya.com/wp-content/uploads/2016/01/3-linear output modIFIED.png)

It is clearly evident that the size of coefficients increase exponentially with increase in model complexity. I hope this gives some intuition into why putting a constraint on the magnitude of coefficients can be a good idea to reduce model complexity.

Lets try to understand this even better.

What does a large coefficient signify? It means that we're putting a lot of emphasis on that feature, i.e. the particular feature is a good predictor for the outcome. When it becomes too large, the algorithm starts modelling intricate relations to estimate the output and ends up overfitting to the particular training data.

I hope the concept is clear. I'll be happy to discuss further in comments if needed. Now. lets understand ridge and lasso regression in detail and see how well they work Your Ultimate path for Becoming a ×

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3. Ridge Regression

As mentioned before, ridge regression performs '**L2 regular** izations, i.e. it adds a factor of sum of squares of coefficients in the optimization objective. Thus, ridge regression optimizes the following:

Objective = RSS + a * (sum of square of coefficients)

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Here, α (alpha) is the parameter which balances the amount of emphasis given to minimizing RSS vs minimizing sum of square of coefficients. α can take various values:

1. a = 0:

- The objective becomes same as simple linear regression.
- We'll get the same coefficients as simple linear regression.

2. **a** = ∞:

• The coefficients will be zero. Why? Because of infinite weightage on square of coefficients, anything less than zero will make the objective infinite.

3. **0 < a < ∞**:

- The magnitude of α will decide the weightage given to different parts of objective.
- The coefficients will be somewhere between 0 and ones for simple linear regression.

I hope this gives some sense on how α would impact the magnitude of coefficients. One thing is for sure that any non-zero value would give values less than that of simple linear regression. By how much? We'll find out soon. Leaving the mathematical details for later, lets see ridge regression in action on the same problem as above.

First, lets define a generic function for ridge regression similar to the one defined for simple linear regression. The Python code is:

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```
from sklearn.linear_model import Ridge
def ridge_regression(data, predictors, alpha, models_to_plot={}):
    #Fit the model
    ridgereg = Ridge(alpha=alpha,normalize=True)
    ridgereg.fit(data[predictors],data['y'])
    y_pred = ridgereg.predict(data[predictors])
    #Check if a plot is to be made for the entered alpha
    if alpha in models_to_plot:
        plt.subplot(models_to_plot[alpha])
        plt.tight_layout()
        plt.plot(data['x'],y_pred)
        plt.plot(data['x'],data['y'],'.')
        plt.title('Plot for alpha: %.3g'%alpha)
    #Return the result in pre-defined format
    rss = sum((y_pred-data['y'])**2)
    ret = [rss]
    ret.extend([ridgereg.intercept_])
    ret.extend(ridgereg.coef_)
    return ret
```

Note the 'Ridge' function used here. It takes 'alpha' as a parameter on initialization. Also, keep in mind that normalizing the inputs is generally a good idea in every type of regression and should be used in case of ridge regression as well.

Now, lets analyze the result of Ridge regression for 10 di values have been chosen so that we can easily analyze however differ from case to case.

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Note that each of these 10 models will contain all the 15 variables and only the value of alpha would differ. This is different from the simple linear regression case where each model had a subset of features.

Python Code:

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```
#Initialize predictors to be set of 15 powers of x
predictors=['x']
predictors.extend(['x_%d'%i for i in range(2,16)])

#Set the different values of alpha to be tested
alpha_ridge = [1e-15, 1e-10, 1e-8, 1e-4, 1e-3,1e-2, 1, 5, 10, 20]

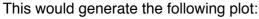
#Initialize the dataframe for storing coefficients.
col = ['rss','intercept'] + ['coef_x_%d'%i for i in range(1,16)]
ind = ['alpha_%.2g'%alpha_ridge[i] for i in range(0,10)]
coef_matrix_ridge = pd.DataFrame(index=ind, columns=col)

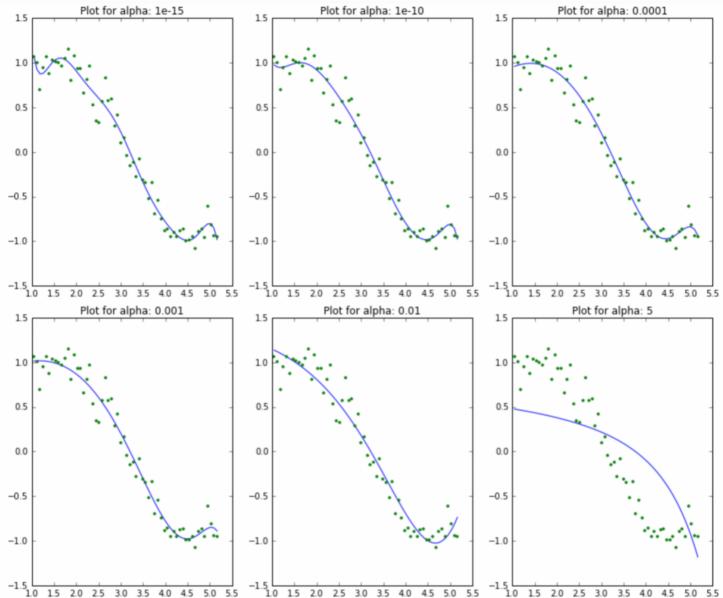
models_to_plot = {1e-15:231, 1e-10:232, 1e-4:233, 1e-3:234, 1e-2:235, 5:236}
for i in range(10):
    coef_matrix_ridge.iloc[i,] = ridge_regression(data, predictors, alpha_ridge[i], models_to_plot)
```

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(https://www.analyticsvidhya.com/wp-content/uploads/2016/01/4.-ridge-output.png)

Here we can clearly observe that **as the value of alpha ir** higher values of alpha reduce overfitting, significantly high

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5). Thus alpha should be chosen wisely. A widely accept tease is a range of values and the one giving higher stream is iterated over a range of values and the one giving higher stream is the stream of the contract of the stream of

Lets have a look at the value of coefficients in the ab	ove models: Name
Python Code:	Email Id
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#Set the display format to be scientific for ease of analysis
pd.options.display.float_format = '{:,.2g}'.format
coef_matrix_ridge

The table looks like:

	rss	intercept	coef_x_1	CC	pef_x_2	coef_x_3	coef_x_4	coef_x_5	coef_x_6	coef_x_7	coef_x_8	С	oef_x_9	coef_x_10	coef_x_11	CO
alpha_1e-15	0.87	95	-3e+02	3.	8e+02	-2.4e+02	66	0.96	-4.8	0.64	0.15	-1	0.026	-0.0054	0.00086	0.0
alpha_1e-10	0.92	11	-29	31		-15	2.9	0.17	-0.091	-0.011	0.002	0	.00064	2.4e-05	-2e-05	-4.2
alpha_1e-08	0.95	1.3	-1.5	4.	7	-0.68	0.039	0.016	0.00016	-0.00036	-5.4e-05 4	4	2.9e-07	1.1e-06	1.9e-07	2e-
alpha_0.0001	0.96	0.56	0.55	-0	.13	-0.026	-0.0028	-0.00011	4.1e-05	1.5e-05	3.7e-06	7	.4e-07	1.3e-07	1.9e-08	1.9
alpha_0.001	1	0.82	0.31	-0	.087	-0.02	-0.0028	-0.00022	1.8e-05	1.2e-05	3.4e-06	7	.3e-07	1.3e-07	1.9e-08	1.7
alpha_0.01	1.4	1.3	-0.088	-0	.052	-0.01	-0.0014	-0.00013	7.2e-07	4.1e-06	1.3e-06	3	e-07	5.6e-08	9e-09	1.1
alpha_1	5.6	0.97	-0.14	-0	.019	-0.003	-0.00047	-7e-05	-9.9e-06	-1.3e-06	-1.4e-07	-9	9.3e-09	1.3e-09	7.8e-10	2.4
alpha_5	14	0.55	-0.059	-0	.0085	-0.0014	-0.00024	-4.1e-05	-6.9e-06	-1.1e-06	-1.9e-07	4	3.1e-08	-5.1e-09	-8.2e-10	-1.0
alpha_10	18	0.4	-0.037	-0	.0055	-0.00095	-0.00017	-3e-05	-5.2e-06	-9.2e-07	-1.6e-07	-;	2.9e-08	-5.1e-09	-9.1e-10	-1.6
alpha_20	23	0.28	-0.022	-0	.0034	-0.0006	-0.00011	-2e-05	-3.6e-06	-6.6e-07	-1.2e-07	-	2.2e-08	-4e-09	-7.5e-10	-1.4

(https://www.analyticsvidhya.com/wp-content/uploads/2016/01/5.-ridge-table_modified.png)

This straight away gives us the following inferences:

- 1. The RSS increases with increase in alpha, this model complexity reduces
- 2. An alpha as small as 1e-15 gives us significant reduction in magnitude of coefficients. How? Compare the coefficients in the first row of this table to the last row of simple linear regression table.
- 3. High alpha values can lead to significant underfitting. Note the rapid increase in RSS for values of alpha greater than 1
- 4. Though the coefficients are very very small, they are NOT zero.

The first 3 are very intuitive. But #4 is also a crucial obsernumber of zeros in each row of the coefficients data set:						
Python Code:	Your Ultimate path for Becoming a × DATA Scientist!					
coef_matrix_ridge.apply(lambda x: sum(x.values==	Use this learning path to become a DATA ₌ଡ\$çi়e្តកូដូ <u>ន</u> t jn 2019					
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Output:

_(https://www.analyticsvidhya.com/wp-content/uploads/2016/01/6ridge-
_(III)PER WITHALIA J. III STALL

<u>zeros.png)</u>

This confirms that all the 15 coefficients are greater than zero in magnitude (can be +ve or -ve). Remember this observation and have a look again until its clear. This will play an important role in later while comparing ridge with lasso regression.

4. Lasso Regression

LASSO stands for *Least Absolute Shrinkage and Selection Operator*. I know it doesn't give much of an idea but there are 2 key words here – 'absolute' and 'selection'.

Lets consider the former first and worry about the latter later.

Lasso regression performs L1 regularization, i.e. it adds the optimization objective. Thus, lasso regression optimize DATA Scientist!

Objective = RSS + a * (sum of absolute value of coefficients) earning path to become a DATA Scientist in 2019

Here, α (alpha) works similar to that of ridge and provides a trade-off between balancing RSS and magnitude of coefficients. Like that of ridge, α can take various values. Lets iterate it here briefly:

1. α = 0: Same coefficients as simple linear regression

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2. $\alpha = \infty$: All coefficients zero (same logic as before)

3. $0 < \alpha < \infty$: coefficients between 0 and that of simple line and the simple line an

Yes its appearing to be very similar to Ridge till now. But just hang on with me and you'll know the difference by the time we finish. Like before, lets run lasso regression on the same problem as above. First we'll define a generic function:

```
from sklearn.linear_model import Lasso
def lasso_regression(data, predictors, alpha, models_to_plot={}):
    #Fit the model
    lassoreg = Lasso(alpha=alpha,normalize=True, max_iter=1e5)
    lassoreg.fit(data[predictors],data['y'])
    y_pred = lassoreg.predict(data[predictors])
    #Check if a plot is to be made for the entered alpha
    if alpha in models_to_plot:
        plt.subplot(models_to_plot[alpha])
        plt.tight_layout()
        plt.plot(data['x'],y_pred)
        plt.plot(data['x'],data['y'],'.')
        plt.title('Plot for alpha: %.3g'%alpha)
    #Return the result in pre-defined format
    rss = sum((y_pred-data['y'])**2)
    ret = [rss]
    ret.extend([lassoreg.intercept_])
    ret.extend(lassoreg.coef_)
    return ret
```

Notice the additional parameters defined in Lasso funciterations for which we want the model to run if it doesn't of setting this to a higher than default value was required in this case Why? I'll come to this in next section, just keep it in the back of the envelope.

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Lets check the output for 10 different values of alpha using the following code:

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```
#Initialize predictors to all 15 powers of x
predictors=['x']
predictors.extend(['x_%d'%i for i in range(2,16)])

#Define the alpha values to test
alpha_lasso = [1e-15, 1e-10, 1e-8, 1e-5,1e-4, 1e-3,1e-2, 1, 5, 10]

#Initialize the dataframe to store coefficients
col = ['rss','intercept'] + ['coef_x_%d'%i for i in range(1,16)]
ind = ['alpha_%.2g'%alpha_lasso[i] for i in range(0,10)]
coef_matrix_lasso = pd.DataFrame(index=ind, columns=col)

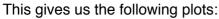
#Define the models to plot
models_to_plot = {1e-10:231, 1e-5:232,1e-4:233, 1e-3:234, 1e-2:235, 1:236}

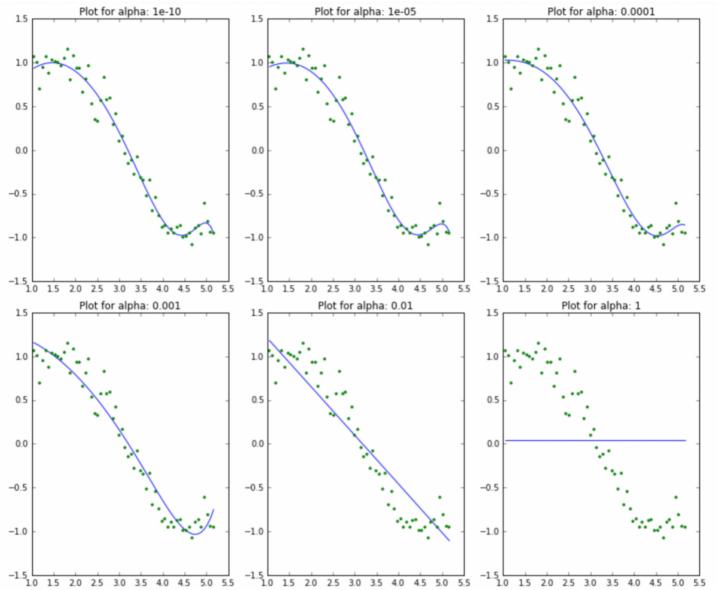
#Iterate over the 10 alpha values:
for i in range(10):
    coef_matrix_lasso.iloc[i,] = lasso_regression(data, predictors, alpha_lasso[i], models_to_plot)
```

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(https://www.analyticsvidhya.com/wp-content/uploads/2016/01/7.-lasso-output1.png)

This again tells us that the model complexity decreases w straight line at alpha=1. Appears a bit strange to me. Let's

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	rss	intercept	coef_x_1	coef_x_2	coef_x_3	coef_x_4	coef_x_5	coef_x_6	coef_x_7	coef_x_8	coef_x_9	coef_x_10	coef_x_11	COE
alpha_1e-15	0.96	0.22	1.1	-0.37	0.00089	0.0016	-0.00012	-6.4e-05	-6.3e-06	1.4e-06	7.8e-07	2.1e-07	4e-08	5.4
alpha_1e-10	0.96	0.22	1.1	-0.37	0.00088	0.0016	-0.00012	-6.4e-05	-6.3e-06	1.4e-06	7.8e-07	2.1e-07	4e-08	5.4
alpha_1e-08	0.96	0.22	1.1	-0.37	0.00077	0.0016	-0.00011	-6.4e-05	-6.3e-06	1.4e-06	7.8e-07	2.1e-07	4e-08	5.3
alpha_1e-05	0.96	0.5	0.6	-0.13	-0.038	-0	0	0	0	7.7e-06	1e-06	7.7e-08	0	0
alpha_0.0001	1	0.9	0.17	-0	-0.048	-0	-0	0	0	9.5e-06	5.1e-07	0	0	0
alpha_0.001	1.7	1.3	-0	-0.13	-0	-0	-0	0	0	0	0	0	1.5e-08	7.5
alpha_0.01	3.6	1.8	-0.55	-0.00056	-0	-0	-Вісн с	PARSITY	-0	-0	-0	0	0	0
alpha_1	37	0.038	-0	-0	-0	-0	-0	-0	-0	-0	-0	-0	-0	-0
alpha_5	37	0.038	-0	-0	-0	-0	-0	-0	-0	-0	-0	-0	-0	-0
alpha_10	37	0.038	-0	-0	-0	-0	-0	-0	-0	-0	-0	-0	-0	-0

(https://www.analyticsvidhya.com/wp-content/uploads/2016/01/8.-lasso-table_modified.png)

Apart from the expected inference of higher RSS for higher alphas, we can see the following:

- 1. For the same values of alpha, the coefficients of lasso regression are much smaller as compared to that of ridge regression (compare row 1 of the 2 tables).
- 2. For the same alpha, lasso has higher RSS (poorer fit) as compared to ridge regression
- 3. Many of the coefficients are zero even for very small values of alpha

Inferences #1,2 might not generalize always but will hold for many cases. The real difference from ridge is coming out in the last inference. Lets check the number of coefficients which are zero in each model using following code:

```
coef_matrix_lasso.apply(lambda x: sum(x.values==0),axis=1)
```

Output:

alpha_1e-15 alpha_1e-10 alpha_1e-08 alpha 1e-05	0 0 0 8	Your Ultimate path for Becoming a × DATA Scientist!
alpha_1e-03 alpha_0.0001 alpha_0.001 alpha_0.01 alpha_1 alpha_5 alpha_10	10 12 13 15 15	Use this learning path to become a DATA Scientist in 2019 (https://www.analyticsvidhya.com/wp-content/uploads/2016/01/9 Name Email Id Contact Number
dtype: int64 lasso-zeros.png)		Download Resource

We can observe that **even for a small value of alpha, a significant number of coefficients are zero**. This also explains the horizontal line fit for alpha=1 in the lasso plots, its just a baseline model! This phenomenon of most of the coefficients being zero is called '**sparsity**'. Although lasso performs feature selection, this level of sparsity is achieved in special cases only which we'll discuss towards the end.

This has some really interesting implications on the use cases of lasso regression as compared to that of ridge regression. But before coming to the final comparison, lets take a **bird's eye view** of the mathematics behind why coefficients are zero in case of lasso but not ridge.

5. Sneak Peak into Statistics (Optional)

I personally love statistics but many of you might not. That's why I have specifically marked this section as '**OPTIONAL**'. If you feel you can handle the algorithms without going into the maths behind them, I totally respect the decision and you can feel free to skip this section.

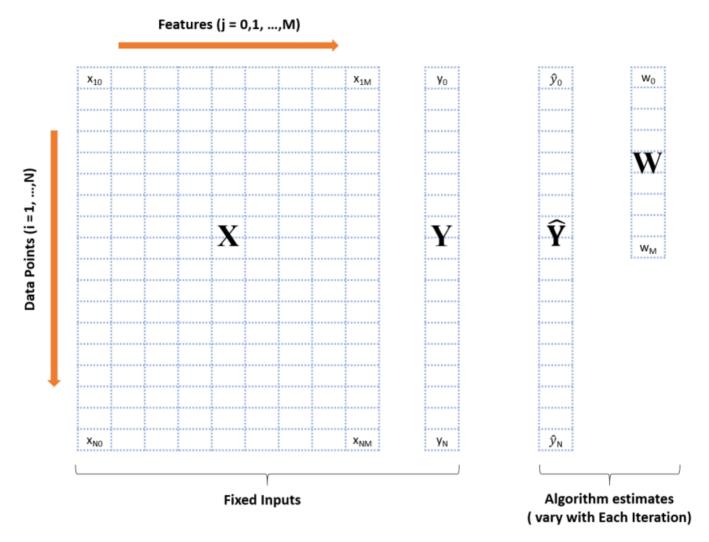
But I personally feel that getting some elementary understanding of how the thing works can be helpful in the long run.

As promised, I'll keep it to a bird's eye view. If you wish to get into the details, I recommend taking a good statistics textbook. One of my favorites is the <u>Elements of Statistical Learning (https://web.stanford.edu/~hastie/Papers/ESLII.pdf)</u>. The best part about this is that it has been made available for free by the authors.

Let's start by reviewing the basic structure of data in a regression problem.

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Regression Data Representation



(https://www.analyticsvidhya.com/wp-content/uploads/2016/01/fig31.png)

In this infographic, you can see there are 4 data elements:

- 1. **X**: the matrix of input features (nrow: N, ncol: M+1)
- 2. **Y**: the actual outcome variable (length:N)
- 3. Yhat: these are predicted values of Y (length:N)
- 4. **W**: the weights or the coefficients (length: M+1)

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Here, N is the total number of data points available and M is the total number of features. X has M+1 columns because of M features and 1 intercept.

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The predicted outcome for any data point i is:

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$$\hat{y}_i = \sum_{j=0}^M w_j * x_{ij}$$

(https://www.analyticsvidhya.com/wp-content/uploads/2016/01/eq1.png)

It is simply the weighted sum of each data point with coefficients as the weights. This prediction is achieved by finding the optimum value of weights based on certain criteria, which depends on the type of regression algorithm being used. Lets consider all 3 cases:

1. Simple Linear Regression

The objective function (also called as the cost) to be minimized is just the RSS (Residual Sum of Squares), i.e. the sum of squared errors of the predicted outcome as compared to the actual outcome. This can be depicted mathematically as:

Cost (W) = RSS(W) =
$$\sum_{i=1}^{N} \{y_i - \hat{y}_i\}^2 = \sum_{i=1}^{N} \left\{ y_i - \sum_{j=0}^{M} w_j x_{ij} \right\}^2$$

(https://www.analyticsvidhya.com/wp-content/uploads/2016/01/eg2.png)

In order to minimize this cost, we generally use a 'gradient descent' algorithm. I'll not go into the details right now but you can refer this. The overall algorithm works as:

- initialize weights (say w=0)
- 2. iterate till not converged
 - 2.1 iterate over all features (j=0,1...M)
 - 2.1.1 determine the gradient

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2.1.2 update the jth weight by subtracting Scientist in 2019 times the gradient

w(t+1) = w(t) - learning rate * gradient

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Here the important step is #2.1.1 where we compute the gradient is nothing but a partial differential of the cost with respect to a particular weight (denoted as w_i). The gradient for the j^{th} weight will be:

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$$\frac{\partial}{\partial w_j} Cost(W) = -2 \sum_{i=1}^N x_{ij} \left\{ y_i - \sum_{k=0}^M w_k x_{ik} \right\}$$

(https://www.analyticsvidhya.com/wp-content/uploads/2016/01/eg3_updated.png)

This is formed from 2 parts:

- 1. 2*{..}: This is formed because we've differentiated the square of the term in {..}
- 2. $-w_j$: This is the differentiation of the part in $\{..\}$ wrt w_j . Since its a summation, all other would become 0 and only w_i would remain.

Step #2.1.2 involves updating the weights using the gradient. This update step for simple linear regression looks like:

$$w_j^{t+1} = w_j^t + 2\eta \sum_{i=1}^N x_{ij} \left\{ y_i - \sum_{k=0}^M w_k x_{ik} \right\}$$

(https://www.analyticsvidhya.com/wp-content/uploads/2016/01/eq4-1.png)

I hope you are able to follow along. Note the +ve sign in the RHS is formed after multiplication of 2 -ve signs. I would like to explain point #2 of the gradient descent algorithm mentioned above 'iterate till not converged'. Here convergence refers to attaining the optimum solution within pre-defined limit.

It is checked using the value of gradient. If the gradient is small enough, that means we are very close to optimum and further iterations won't have a substantial impact on coefficients. The lower-limit on gradient can be changed using the 'tol' parameter.

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Lets consider the case of ridge regression now.

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2. Ridge Regression

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The objective function (also called the cost) to be minimized 18 PSS plus the sum of square of the magnitude of weights. This can be depicted mathematically as:

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$$Cost(W) = RSS(W) + \lambda * (sum of squares of weights)$$

$$= \sum_{i=1}^{N} \left\{ y_i - \sum_{j=0}^{M} w_j x_{ij} \right\}^2 + \lambda \sum_{j=0}^{M} w_j^2$$

(https://www.analyticsvidhya.com/wp-content/uploads/2016/01/eq5-1.png)

In this case, the gradient would be:

$$\frac{\partial}{\partial w_j} Cost(W) = -2 \sum_{i=1}^N x_{ij} \left\{ y_i - \sum_{k=0}^M w_k x_{ik} \right\} + 2\lambda w_j$$

(https://www.analyticsvidhya.com/wp-content/uploads/2016/01/eq6-1.png)

Again in the regularization part of gradient, only w_j remains and all other would become zero. The corresponding update rule is:

$$w_j^{t+1} = w_j^t - \eta \left[-2\sum_{i=1}^N x_{ij} \left\{ y_i - \sum_{k=0}^M w_k * x_{ik} \right\} + 2\lambda w_j \right]$$

$$w_j^{t+1} = (1 - 2\lambda \eta) w_j^t + 2\eta \sum_{i=1}^N x_{i:i} \left\{ v_i - \sum_{k=0}^M w_k * x_{ik} \right\}$$
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Here we can see that second part of the RHS is same as Nthate of simple linear regression. Thus, ridge regression is equivalent to reducing the weight by a factor of (1-2\lambda) first and then applying the same update rule as simple linear regression. I hope this gives some intuition why the coefficients get reduced to small numbers but never become zero.

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Note that the criteria for convergence in this case remains similar to simple linear regression, i.e. checking the value of gradients. Lets discuss Lasso regression now.

3. Lasso Regression

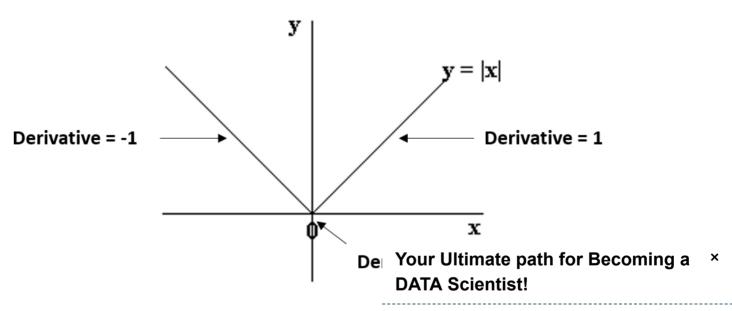
The objective function (also called the cost) to be minimized is the RSS plus the sum of absolute value of the magnitude of weights. This can be depicted mathematically as:

$$Cost(W) = RSS(W) + \lambda * (sum of absolute value of weights)$$

$$= \sum_{i=1}^{N} \left\{ y_i - \sum_{j=0}^{M} w_j x_{ij} \right\}^2 + \lambda \sum_{j=0}^{M} |w_j|$$

(https://www.analyticsvidhya.com/wp-content/uploads/2016/01/eq8-1.png)

In this case, the gradient is not defined as the absolute function is not differentiable at x=0. This can be illustrated as:



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(https://www.analyticsvidhya.com/wp-content/uploads/2016/8di/eigtisting)2019

We can see that the parts on the left and right side of 0 are straight lines with defined derivates but the function can't be differentiated at x=0. In this case, we have to use a different technique called as **coordinate** descent which is based on the concept of sub-gradients. One to the default in sklearn):

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- 1. initialize weights (say w=0)
- 2. iterate till not converged
 - 2.1 iterate over all features (j=0,1...M)
 - 2.1.1 update the jth weight with a value which minimizes the cost

#2.1.1 might look too generalized. But I'm intentionally leaving the details and jumping to the update rule:

$$w_{j} = \begin{cases} g(w_{-j}) + \frac{\lambda}{2}, & \text{if } g(w_{-j}) < -\frac{\lambda}{2} \\ 0, & \text{if } -\frac{\lambda}{2} \le g(w_{-j}) \le \frac{\lambda}{2} \end{cases}$$
$$g(w_{-j}) - \frac{\lambda}{2}, & \text{if } g(w_{-j}) > \frac{\lambda}{2} \end{cases}$$

(https://www.analyticsvidhya.com/wp-content/uploads/2016/01/eg9.png)

Here $g(w_{-j})$ represents (but not exactly) the difference between actual outcome and the predicted outcome considering all EXCEPT the j^{th} variable. If this value is small, it means that the algorithm is able to predict the outcome fairly well even without the jth variable and thus it can be removed from the equation by setting a zero coefficient. This gives us some intuition into why the coefficients become zero in case of lasso regression.

In coordinate descent, checking convergence is another issue. Since gradients are not defined, we need an alternate method. Many alternatives exist but the simplest one is to check the step size of the algorithm. We can check the maximum difference in weights in any property Your Ultimate path for Becoming a above).

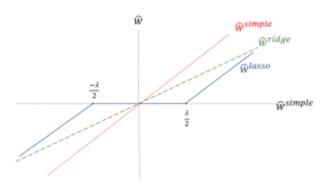
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If this is lower than 'tol' specified, algo will stop. The convergence specified specified and we might have to set the 'max_iter' parameter if a warning capplest in saying that the algo stopped before convergence. This is why I specified this parameter in the Lasso generic function.

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Lets summarize our understanding by comparing the coefficients in all the three cases using the following visual, which shows how the ridge and lasso coefficients believe in comparison to the simple linear regression case.

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(https://www.analyticsvidhya.com/wp-content/uploads/2016/01/fig2.png)

Apologies for the lack of visual appeal. But I think it is good enough to re-inforced the following facts:

- 1. The ridge coefficients are a reduced factor of the simple linear regression coefficients and thus never attain zero values but very small values
- 2. The lasso coefficients become zero in a certain range and are reduced by a constant factor, which explains there low magnitude in comparison to ridge.

Before going further, one important issue in case of both ridge and lasso regression is **intercept handling**. Generally, regularizing the intercept is not a good idea and it should be left out of regularization. This requires slight changes in the implementation, which I'll leave for you to explore.

If you're still confused and things are a bit fuzzy, I recommend taking the course on Regression which is part of the <u>Machine Learning Specialization (https://www.coursera.org/specializations/machine-learning)</u> by University of Washington at Coursera.

Now, lets come to the concluding part where we compare the Ridge and Lasso techniques and see where these can be used

6. Conclusion

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Now that we have a fair idea of how ridge and lat understanding by comparing them and try to appreciate the last specific learning as at the last some alternate approaches. Lets analyze these under three some last in 2019

1. Key Difference

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- Ridge: It includes all (or none) of the features in the major advantage of ridge regression is coefficient shrinkage and reducing model complexity.
- Lasso: Along with shrinking coefficients, lasso performentestule before as well. (Remember the 'selection' in the lasso full-form?) As we observed earlier, some of the coefficients become exactly zero, which is equivalent to the particular feature being excluded from the model.

Traditionally, techniques like **stepwise regression** were used to perform feature selection and make parsimonious models. But with advancements in Machine Learning, ridge and lasso regression provide very good alternatives as they give much **better output**, require **fewer tuning parameters** and can be **automated** to a large extend.

2. Typical Use Cases

- **Ridge:** It is majorly used to *prevent overfitting*. Since it includes all the features, it is not very useful in case of exorbitantly high #features, say in millions, as it will pose computational challenges.
- Lasso: Since it provides sparse solutions, it is generally the model of choice (or some variant of this
 concept) for modelling cases where the #features are in millions or more. In such a case, getting a
 sparse solution is of great computational advantage as the features with zero coefficients can simply be
 ignored.

Its not hard to see why the stepwise selection techniques become practically very cumbersome to implement in high dimensionality cases. Thus, lasso provides a significant advantage.

3. Presence of Highly Correlated Features

- **Ridge:** It generally works well even in presence of highly correlated features as it will include all of them in the model but the coefficients will be distributed among them depending on the correlation.
- Lasso: It arbitrarily selects any one feature among the highly correlated ones and reduced the coefficients of the rest to zero. Also, the chosen variable changes randomly with change in model parameters. This generally doesn't work that well as compared to ridge regression.

This disadvantage of lasso can be observed in the example we discussed above. Since we used a polynomial regression, the variables were highly correlate

Thus, we saw that even small values of alpha were giving

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Along with Ridge and Lasso, Elastic Net is another useful techniques which combines both L1 and L2 regularization. It can be used to balance out the pros and cons of ridge and lasso regression. I encourage you to explore it further.

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In this article, I gave an overview of regularization using ridge and lasso regression. Then, I focused on reasons behind penalizing the magnitude of coefficients should give us passimonious models. Next, we went into details of ridge and lasso regression and saw their advantages over simple linear regression. We got

some intuition into why they should work and also how they work. If you read the optional mathematical part, you probably understood the underlying fundamentals.

Regularization techniques are really useful and I encourage you to implement them. If you're ready to take the challenge, why not try them on the <u>BigMart Sales Prediction</u> (http://datahack.analyticsvidhya.com/contest/practice-problem-bigmart-sales-prediction) problem and share your results in the <u>discussion forum (http://discuss.analyticsvidhya.com)</u>.

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m/biog/2018/10/understanding-Neural Network & Deep Learning inception-network-from-scratch/) (https://www.analyticsvidhya.co m/blog/2015/07/top-youtube

python-beginner duite old and you mightidage machine plears it is a the author. We request you to post this comment on Analytics Vidhya's provided in the comment of Analytics Vidhya's vidh queries resolved

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52 COMMENTS



NILABHRA ROY CHOWDHURY (HTTP://CHAOTICSENSES.WORDPRESS.COM) Reply

January 28, 2016 at 8:26 pm (https://www.analyticsvidhya.com/blog/2016/01/complete-tutorial-ridge-lasso-regression-

python/#comment-104807)

Good read, liked the way you explained why weight constraining is essential for regularization. Can you also perform the same experiments on Elastic Net and update this blog?



AARSHAY JAIN

Reply

January 29, 2016 at 4:11 am (https://www.analyticsvidhya.com/blog/2016/01/complete-tutorial-ridge-lasso-regressionpython/#comment-104833)

Hi Nilabhra,

Thanks for reaching out. Yes it would be a good idea to discuss Elastic Net but I'll probably take this up in a separate article. I suppose there is sufficient content here to digest and I can discuss Elastic Net along with other regression techniques in future. Stay tuned!

Cheers



DR.D.K.SAMUEL

Reply

January 29, 2016 at 5:21 am (https://www.analyticsvidhya.com/blog/2016/01/complete-tutorial-ridge-lasso-regressionpython/#comment-104836)

Beautiful, I will like this article ported to R please (I am somehow more happy in R than python)



AARSHAY JAIN

Reply

January 29, 2016 at 10:29 am (https://www.analyticsvidhya.com/blog/2016/01/complete-tutorial-ridge-lasso-regression-

python/#comment-104862)

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Thanks for reaching out. I'll try to put together the R codes

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AARSHAY JAIN

Reply

February 12, 2016 at 1:06 pm (https://www.analyticsvidhya.com/plog/2016/01/complete-tutorial-ridge-lasso-regression-

python/#comment-105579)

Email Id

Hello Dr. Samuel,

Contact Number

My apologies for not being able to stand upto my commitment for delivering the R-codes. I'm a bit crunched for bandwidth but I have this in the pipeline. Not sure when I'll be able to come back.

If you have any juniors working under you on this, please feel free to ask them to reach to me for help through our discussion portal. Thank you!



PROF RAVI VADLAMANI

Reply

January 29, 2016 at 5:40 am (https://www.analyticsvidhya.com/blog/2016/01/complete-tutorial-ridge-lasso-regression-python/#comment-104840)

Hi.

It was a good post detailing the Ridge and Lasso regression. Great effort.

However, it could have been complete, had the concept of multicollinearity been discussed in the context of Ridge regression. This is because to address this ticklish issue of multicollinearity, we have two alternative remedies in the form of ridge regression and principal component regression.

Bests



AARSHAY JAIN

Reply

<u>January 29, 2016 at 10:46 am (https://www.analyticsvidhya.com/blog/2016/01/complete-tutorial-ridge-lasso-regression-python/#comment-104864)</u>

Hello professor,

Thanks for your valuable feedback. I suppose it'll be better if I discuss multi-collinearity in a separate article. You can expect it in future. Please stay tuned!

Cheers!



ALPHA (HTTP://ALPLHABETA)

Reply

<u>January 29, 2016 at 6:39 am (https://www.analyticsvidhya.com/blog/2016/01/complete-tutorial-ridge-lasso-regression-python/#comment-104844)</u>

You are an excellent teacher my friend, keep up the good

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AARSHAY JAIN

Use this learning path to become a DATA Reply

January 29, 2016 at 10:46 am (https://www.analyticsvidhya.com/signation/signation-independent of the python/#comment-104865)

Thanks! I'll try my best..

Name

Email Id



TUHIN (HTTP://WWW.TUHINCHATTOPADH YAY COM) Number

Reply

January 29, 2016 at 1:06 pm (https://www.analyticsvidhya.com/blog/2016/01/complete-tutorial-ridge-lasso-regression-python/#comment-104872)

Excellent write-up Aarshay. Deeply appreciate.



AARSHAY JAIN

Reply

January 29, 2016 at 7:52 pm (https://www.analyticsvidhya.com/blog/2016/01/complete-tutorial-ridge-lasso-regressionpython/#comment-104887)

Thanks Tuhin!



SHUVAYAN DAS

Reply

January 29, 2016 at 1:28 pm (https://www.analyticsvidhya.com/blog/2016/01/complete-tutorial-ridge-lasso-regressionpython/#comment-104874)

Awesome arshay, keep up the learning and good work



AARSHAY JAIN

<u>Reply</u>

January 29, 2016 at 7:53 pm (https://www.analyticsvidhya.com/blog/2016/01/complete-tutorial-ridge-lasso-regressionpython/#comment-104888)

For sure





SHAN

Reply

February 2, 2016 at 10:05 am (https://www.analyticsvidhya.com/blog/2016/01/complete-tutorial-ridge-lasso-regressionpython/#comment-105065)

Informative article. I understand LASSO shrunk coefficients to zero. Just wondering, after shrinkage, can any coefficient regain value. If yes, under what conditions it may happen so., Thanks.



AARSHAY JAIN

python/#comment-105068)

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I believe it can regain value. Actually it should depend on the selection of feature (step #2.1) in coordinate descent algorithm. Step #2.1 says that the algo will cycle through all features and optimize for one particular

feature at a time. So, it might be possible that a non-zero optimetable exist in a future iteration which will cause the weight to regain value.

Contact Number

It might be helpful to look into the contour plots of coordinate descent steps. There you can observe that it works in steps with a step along one particular dimension (in terms of weights) at a time. So a step in one direction can result in the algorithm choosing a non-zero step in another dimension even though it choose a zero step for the same dimension earlier. It might not be very intuitive but its possible. I have observed this happening.

If we don't want this to happen. We can use a different method to select the feature to optimize in step#2.1. For instance, we might set a rule that once a feature becomes zero, it will not be selected.

Hope this helps.



TIM

<u>Reply</u>

<u>February 7, 2016 at 2:57 pm (https://www.analyticsvidhya.com/blog/2016/01/complete-tutorial-ridge-lasso-regression-python/#comment-105325)</u>

Hello,

really good and illustrative article. Gives a good impression of ridge and Lasso regression and definitely very helpful.

Keep up the good work!

p.s.

Just two small corrections:

- 1) a \$lambda\$ got lost in the second line of the cost function for ridge regression.
- 2) I think that \$w_j\$ in the associated gradient expression of the cost function should be replaced by \$x_ij\$ and the whole expression multiplied by (-2)



AARSHAY JAIN

<u>Reply</u>

<u>February 7, 2016 at 7:35 pm (https://www.analyticsvidhya.com/blog/2016/01/complete-tutorial-ridge-lasso-regression-python/#comment-105337)</u>

Hi Tim,

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I'm glad you liked it. 🙂

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And thanks for pointing out the typing errors. I've updated the same to 2019

Cheers!

Name

Email Id



SURYA1987

Reply

March 2, 2016 at 1:52 pm (https://www.analyticsvidhya.com/blog/2016401fdshrphthertutorial-ridge-lasso-regression-

python/#comment-106485)

Really a nice article to understand lasso and ridge regression. However here in this article why are you reffering to simple linear regression instead of multiple linear regression. Any specific reason?



AARSHAY JAIN

Reply

March 2, 2016 at 3:55 pm (https://www.analyticsvidhya.com/blog/2016/01/complete-tutorial-ridge-lasso-regressionpython/#comment-106489)

Thanks 🙂



I'm sorry I didn't get you simple linear regression point. I've used a polynomial regression example here with 15 variables. Please elaborate.



SURYA PRAKASH

Reply

March 2, 2016 at 7:34 pm (https://www.analyticsvidhya.com/blog/2016/01/complete-tutorial-ridge-lasso-regressionpython/#comment-106494)

I mean to say that you were comparing ridge and lasso model coefficients with simple linear regression coefficients. I.e you have mentioned (Compare the coefficients in the first row of this table to the last row of simple linear regression table.) ... Nothing wrong but it's just to correct my understanding.



SURYA PRAKASH

Reply

March 2, 2016 at 7:36 pm (https://www.analyticsvidhya.com/blog/2016/01/complete-tutorial-ridge-lasso-regressionpython/#comment-106495)

I mean to say that you were comparing ridge and lasso model coefficients with simple linear regression coefficients. I.e you have mentioned (Compare the coefficients in the first row of this table to the last row of simple linear regression table.) ... Nothing wrong but it's just to correct my understanding.



AARSHAY JAIN

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March 3, 2016 at 3:26 am (https://www.analyticsvidhya.cor python/#comment-106505)

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Contact Number

My bad. I used an incorrect term. By 'simple' here I meant the regression without regularization and not the 'simple' in terms of single variable. Thanks for reaching out and for reading this in such depth.

Please feel free to reach out in case you face any other challenges il



Reply

April 22, 2016 at 12:06 pm (https://www.analyticsvidhya.com/blog/2016/01/complete-tutorial-ridge-lasso-regressionpython/#comment-109850)

When writing the formula for #2.1.1, why did you introduce `k` and not just use `j`?



AARSHAY JAIN

Reply

April 25, 2016 at 5:55 pm (https://www.analyticsvidhya.com/blog/2016/01/complete-tutorial-ridge-lasso-regressionpython/#comment-110008)

i'm sorry I didn't get which part are you referring to.



JIM

Reply

April 22, 2016 at 7:25 pm (https://www.analyticsvidhya.com/blog/2016/01/complete-tutorial-ridge-lasso-regressionpython/#comment-109866)

Is the equation for predicted value of linear correction correct? (http://i1.wp.com/www.analyticsvidhya.com/wp-content/uploads/2016/01/eq1.png (http://i1.wp.com/www.analyticsvidhya.com/wp-content/uploads/2016/01/eq1.png)) Should there not be a bias added that is not multiplied by the weight?



AARSHAY JAIN

Reply

April 25, 2016 at 5:56 pm (https://www.analyticsvidhya.com/blog/2016/01/complete-tutorial-ridge-lasso-regressionpython/#comment-110009)

Here 'i' is starting with 0. So the bias term is included in matrix for easy vectorization of calculation. The weight should be 1 always.



SANOJ KUMAR

Reply

May 16, 2016 at 4:08 pm (https://www.analyticsvidhya.com/blog/2016/01/complete-tutorial-ridge-lasso-regression-

python/#comment-111061)

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Hello,

Lasso code. If I specify a static range of lambda and apply of throws me very less number of features for some models while so many for other models. I want to calculate lambda(max) for each model then specify the range of lambda based on that and do cross validation to get appropriate number of features. My intention is feature selection here. I am using python.

Email Id



AARSHAY JAIN

Contact Number

<u>Reply</u>

July 1, 2016 at 1:41 pm (https://www.analyticsvidhya.com/blog/2016/01/complete-tutorial-ridge-lasso-regression-Download Resource

python/#comment-112908)

I'm not sure if I understood your concern currently. I'll explain a strategy which I would use to select the best value of lambda. First you should check for say 10 values which are separated by a good margin, say 1e-15, 1e-12, 1e-9 and so on upto say 1e5 or so. Once you do cross-validation on these, you'll get a sense of the range in which optimum value will lie. Then you can go for closer values in that range.

Talking about the #features, you should choose the model with best CV score. If you think its not making sense, you should also try a higher number of folds and check the variance of error in different folds and not just the mean error. Hope this helps.



ARUN KHATTRI

<u>Reply</u>

<u>July 1, 2016 at 1:09 pm (https://www.analyticsvidhya.com/blog/2016/01/complete-tutorial-ridge-lasso-regression-python/#comment-112904)</u>

Refer Lasso regression, am using py 3.5, I changed the value of max_iter to 1e7, even then am getting a ConvergenceWarning that Objective did not converge. You might want to increase the number of iterations. Will appreciate if you can throw some light on this....



AARSHAY JAIN

Reply

<u>July 1, 2016 at 1:36 pm (https://www.analyticsvidhya.com/blog/2016/01/complete-tutorial-ridge-lasso-regression-python/#comment-112907)</u>

This might happen for some of the alpha values. If you read carefully, I have mentioned this towards the end of the lasso section. Some alpha values can result in a poor fit and thus the least square objective will not converge to the minimum value. One solution is to choose higher #iterations but if the problem persists for even high values, you should consider leaving that specific alpha value.

Note that the alpha values causing this will vary from case to case and you should not keep any universal values of alpha in your mind. Hope this helps.



DINA G

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July 7, 2016 at 5:08 pm (https://www.analyticsvidhya.com/bldd/201th/0s/deapreingupathritgebessomegressibATA python/#comment-113190)

Scientist in 2019

Thanks for the article, this was very helpful.

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One point is a little unclear to me, however. I can see that the lessal regression will produce zero values where ridge regression will likely produce just small weights. However, it is unclear to me whether this is a result of the differently defined cost function or of the different communication makes or in the different produce zero values where ridge regression will produce zero values where ridge regression ridge regression will regression will regression ridge regression ridge regression ridge regression ridge regression ridge ridge regression ridge ridge ridge ridge ridge ridge ridge ridge r

since the gradient is undefined. But, couldn't you use coordinate descent with ridge regression? And would that not produce zeros at a higher rate than gradient descent? Also, the function g(w_j) is a little mysterious to me.



AARSHAY JAIN

Reply

<u>July 7, 2016 at 5:21 pm (https://www.analyticsvidhya.com/blog/2016/01/complete-tutorial-ridge-lasso-regression-python/#comment-113191)</u>

I think you're getting mixed up here. Coordinate descent is not something applied by choice. The contour plot in case of lasso regression is such that coordinate descent has to be applied. That's not the case for ridge. If you go a little deeper into the mathematics, you'll understand better. There's a Machine Learning specialization on coursera which you can check out if you're interested in digging deeper! Hope this helps..



DINA G

<u>July 7, 2016 at 5:24 pm (https://www.analyticsvidhya.com/blog/2016/01/complete-tutorial-ridge-lasso-regression-python/#comment-113192)</u>

But couldn't you use coordinate descent with ridge? I understand that you don't have to.



AARSHAY JAIN

Reply

Reply

<u>July 7, 2016 at 5:36 pm (https://www.analyticsvidhya.com/blog/2016/01/complete-tutorial-ridge-lasso-regression-python/#comment-113194)</u>

Actually coordinate descent is not as good as gradient descent because a closed form solution does not exist as the gradient is not defined at all points. Its more of an iterative, random approach. So gradient descent will always be preferred.

I haven't tried using coordinate descent in ridge, but I reck be less than lasso. This is because intersection of the two much lower than lasso because of the shape of the contout through that lecture from the Coursera course I mentioned

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through that lecture from the Coursera course I mentioned above his learning planted become a DATA

Scientist in 2019

Hope this helps.



DINA G

Email Id

Name

Reply

<u>July 7, 2016 at 6:14 pm (https://www.analyticsvidhya.com/blog/2016/01/complete-tutorial-ridge-lasso-regression-python/#comment-113197)</u>

Contact Number

My point is that you are conflating two things – the cost function and minimization algorithm – that are actually separate.

Also, why do you use alpha in the main text and lambda in the statistics section? Aren't they the same thing?



RAMA KRISHNA

Reply

<u>August 19, 2016 at 5:16 am (https://www.analyticsvidhya.com/blog/2016/01/complete-tutorial-ridge-lasso-regression-python/#comment-114945)</u>

Excellent piece of work my friend. Please publish more.



RYAN Reply

<u>August 25, 2016 at 9:20 am (https://www.analyticsvidhya.com/blog/2016/01/complete-tutorial-ridge-lasso-regression-python/#comment-115124)</u>

Thanks a lot Aarshay for this excellent tutorial. Now I understand better why I should use LASSO instead of forward stepwise regression for shrinking an ODE system.



SAM

Reply

<u>September 9, 2016 at 6:57 am (https://www.analyticsvidhya.com/blog/2016/01/complete-tutorial-ridge-lasso-regression-python/#comment-115837)</u>

Hello,

Thanks for your article, very useful.

Not sure if it's a mistake but, on the graph showing the comparison between simple linear, Lasso and Ridge regression. you labeled the x-axis as "w simple", whereas "w simple" is already labeled for the red line. Should the x-axis not be labeled as "lambda"?



VAN AUSLOOS XAVIER (HTTP://LADONN

October 3, 2016 at 7:55 am (https://www.analyticsvidhya.cupython/#comment-116708)

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Perfect and clear. Thanks a lot



JASON

Name

<u>Reply</u>

October 19, 2016 at 5:00 pm (https://www.analyticsvidhya.com/blog/20/16/01/complete-tutorial-ricge-lasso-regression-python/#comment-117312)

Contact Number

Hi, Thanks for sharing.

I am wondering how to formulate g(w-j) in Lasso regression here.wnload Resource Could you please provide some information?

Many thanks!



VAIBHAV SAHU

Reply

November 1, 2016 at 5:24 pm (https://www.analyticsvidhya.com/blog/2016/01/complete-tutorial-ridge-lasso-regressionpython/#comment-117788)

Thanks for making it easy to understand!



RAHUL Reply

November 3, 2016 at 5:59 am (https://www.analyticsvidhya.com/blog/2016/01/complete-tutorial-ridge-lasso-regressionpython/#comment-117860)

Hi Aarshay,

I have a couple of questions w.r.t. regularized regression (Lasso & Ridge). Hope you could answer them

- 1.) In unregularized regression, we use adjusted R2. Similarly, what are the model evaluation parameters that we can use for regularized models?
- 2.) Basically, regularized model is min(error term + regularization term). So in this case, will Mean Square Error (MSE) for regularized models will always be higher than that of unregularized model?



MS

Reply

November 14, 2016 at 12:00 pm (https://www.analyticsvidhya.com/blog/2016/01/complete-tutorial-ridge-lasso-regressionpython/#comment-118348)

Great article...helped me a lot !!



KISHORE

Your Ultimate path for Becoming a **DATA Scientist!**

December 9, 2016 at 10:28 am (https://www.analyticsvidhya.lcbse/bl/bi/s/046/04/irognplatthtutorlateriolganlasaof/ba/risonpython/#comment-119475) Scientist in 2019

Hello Aarshay Jain,

Really a nice stuff. Thank you for sharing.

Name

Email Id



EMRAH

Contact Number

<u>Reply</u>

May 29, 2017 at 2:21 pm (https://www.analyticsvidhya.com/blog/2016/01/complete-tutorial-ridge-lasso-regression-Download Resource

python/#comment-129409)

Thank you for clarification about regularized regression model.



EVANGELOS KATSAROS

Reply

November 5, 2017 at 9:31 pm (https://www.analyticsvidhya.com/blog/2016/01/complete-tutorial-ridge-lasso-regressionpython/#comment-142328)

Excellent read, excellent explanation even of the maths. Keep up the good work!



HOLLY <u>Reply</u>

February 28, 2018 at 10:22 am (https://www.analyticsvidhya.com/blog/2016/01/complete-tutorial-ridge-lasso-regressionpython/#comment-151633)

such a great article! thanks



MOHAMMED SUNASRA

<u>Reply</u>

April 19, 2018 at 4:05 pm (https://www.analyticsvidhya.com/blog/2016/01/complete-tutorial-ridge-lasso-regressionpython/#comment-152691)

"It is clearly evident that the size of coefficients increase exponentially with increase in model complexity. I hope this gives some intuition into why putting a constraint on the magnitude of coefficients can be a good idea to reduce model complexity."

This above statement cleared my whole doubt. Nice writeup. Cheers!



AISHWARYA SINGH

Reply

April 20, 2018 at 11:56 am (https://www.analyticsvidhya.com/blog/2016/01/complete-tutorial-ridge-lasso-regression-

python/#comment-152710)

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Hi Mohammed,

Happy learning!

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JEZA

Glad you found this helpful!

Email Id

Name

Reply

May 4, 2018 at 10:37 pm (https://www.analyticsvidhya.com/blog/2016/01/complete-tutorial-ridge-lasso-regression-

python/#comment-153049)

Contact Number

Thanks ever so much for your explanation



BIN

Reply

May 17, 2018 at 7:49 am (https://www.analyticsvidhya.com/blog/2016/01/complete-tutorial-ridge-lasso-regression-python/#comment-153325)

Hello, that url "http://statweb.stanford.edu/~tibs/ElemStatLearn/" can not open.



AISHWARYA SINGH

Reply

May 17, 2018 at 11:14 am (https://www.analyticsvidhya.com/blog/2016/01/complete-tutorial-ridge-lasso-regression-python/#comment-153330)

Hi,

Thank you for pointing it out. We have updated the same in the article.



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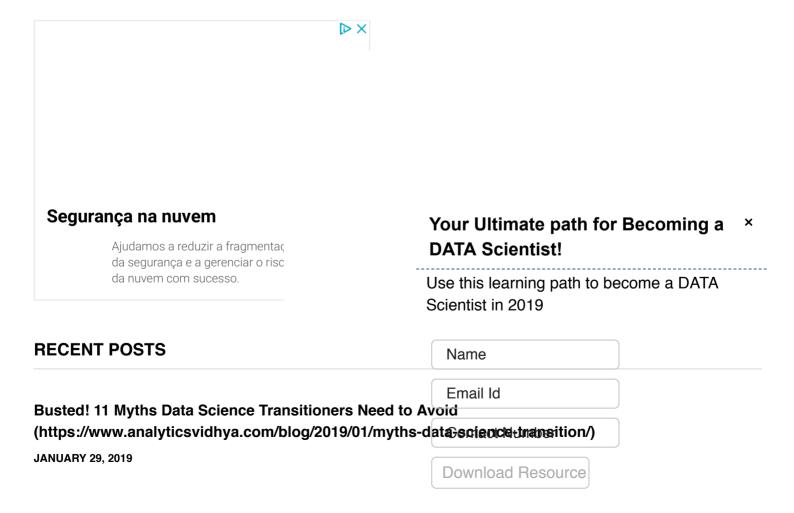
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(http://www.edvancer.in/certified-data-scientist-with-python-

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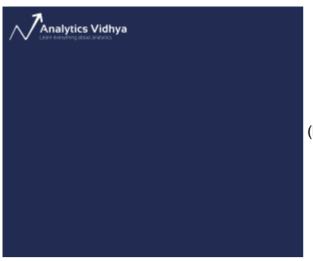
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v1:AnalyticsVidhya+CVDL101+CVDL101_T1/about? utm_source=AVStickyBanner2&utm_medium=display2&utm_campaign=cv10percent)

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