



# Correlations

## Correlation

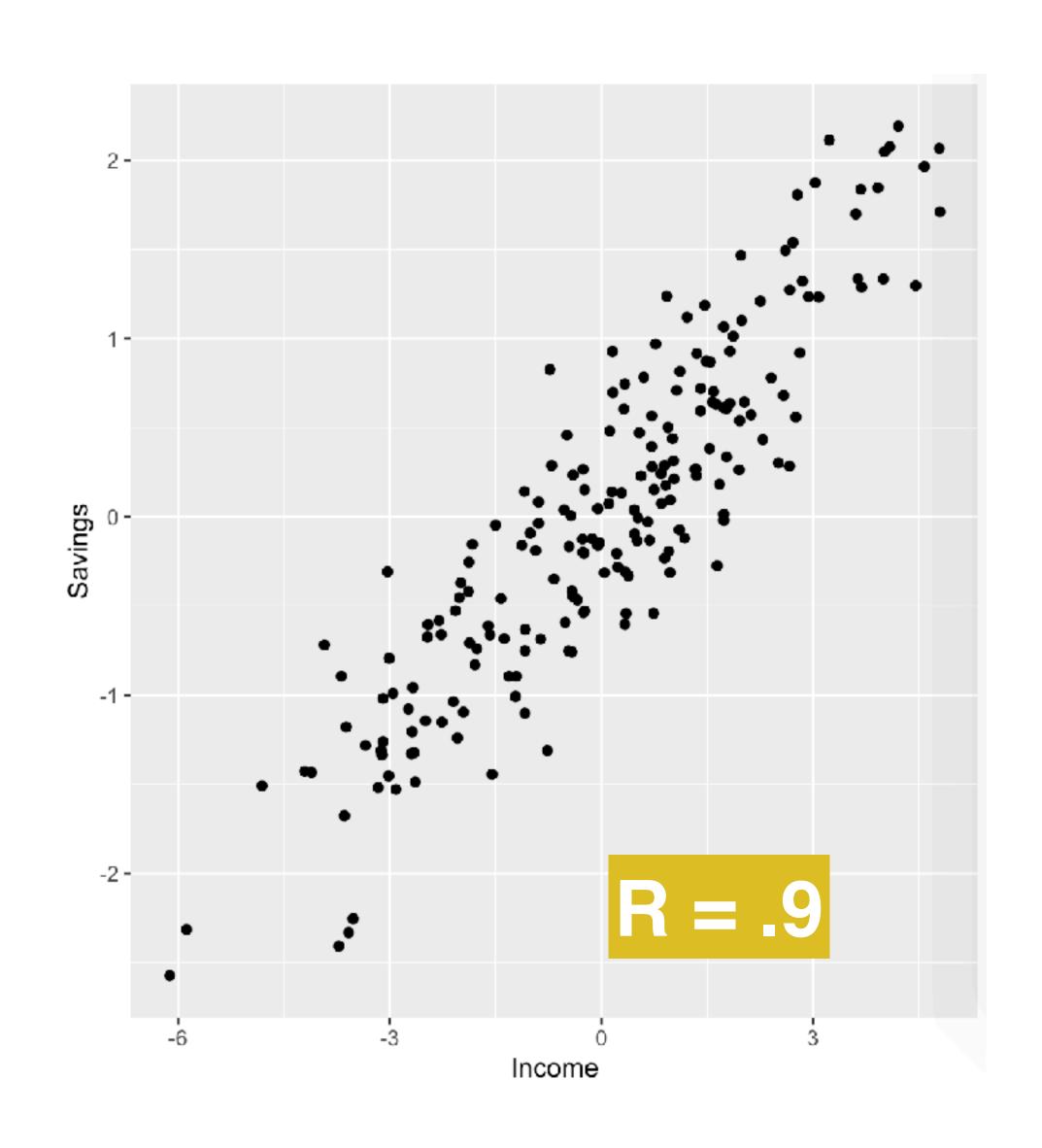
How closely two variables related

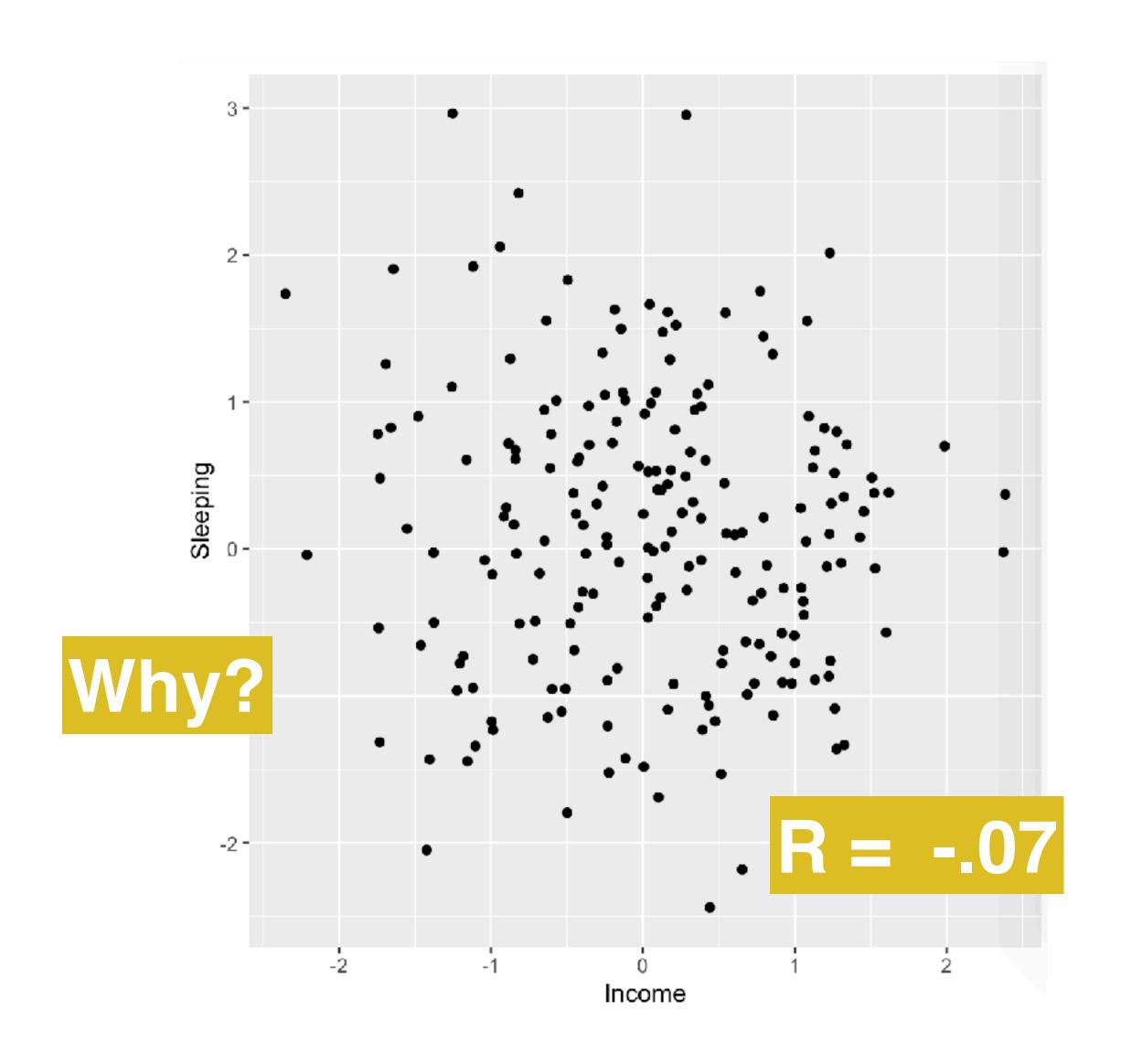
Direction of the relationship

-1 to 1

-1 and 1 = perfectly correlated 0 = perfectly uncorrelated

# Relationships between variables





#### GENERAL GUIDELINES

0

0.01 - 0.19

0.20 - 0.29

0.30 - 0.39

0.40 - 0.69

0.70 - 0.99

No relationship

Little to no relationship

Weak relationship

Moderate relationship

Strong relationship

Very strong relationship

Perfect relationship

Can be positive or negative

## Guess the Correlation

http://guessthecorrelation.com/

### Math

https://www.khanacademy.org/math/ap-statistics/bivariate-data-ap/correlation-coefficient-r/v/calculating-correlation-coefficient-r

$$r_{xy} = \frac{\sum_{i=1}^{n} (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\sum_{i=1}^{n} (x_i - \bar{x})^2 \sum_{i=1}^{n} (y_i - \bar{y})^2}}$$

## Interpretation

As the value of X goes up, Y tends to go up (or down)

A lot / a little / not at all

### Relations between variables

What do we mean by strong "relationship"?

If X is high/low then
Y is high/low

Having information about X = you know something about Y

# Drawing Lines

# Drawing Lines

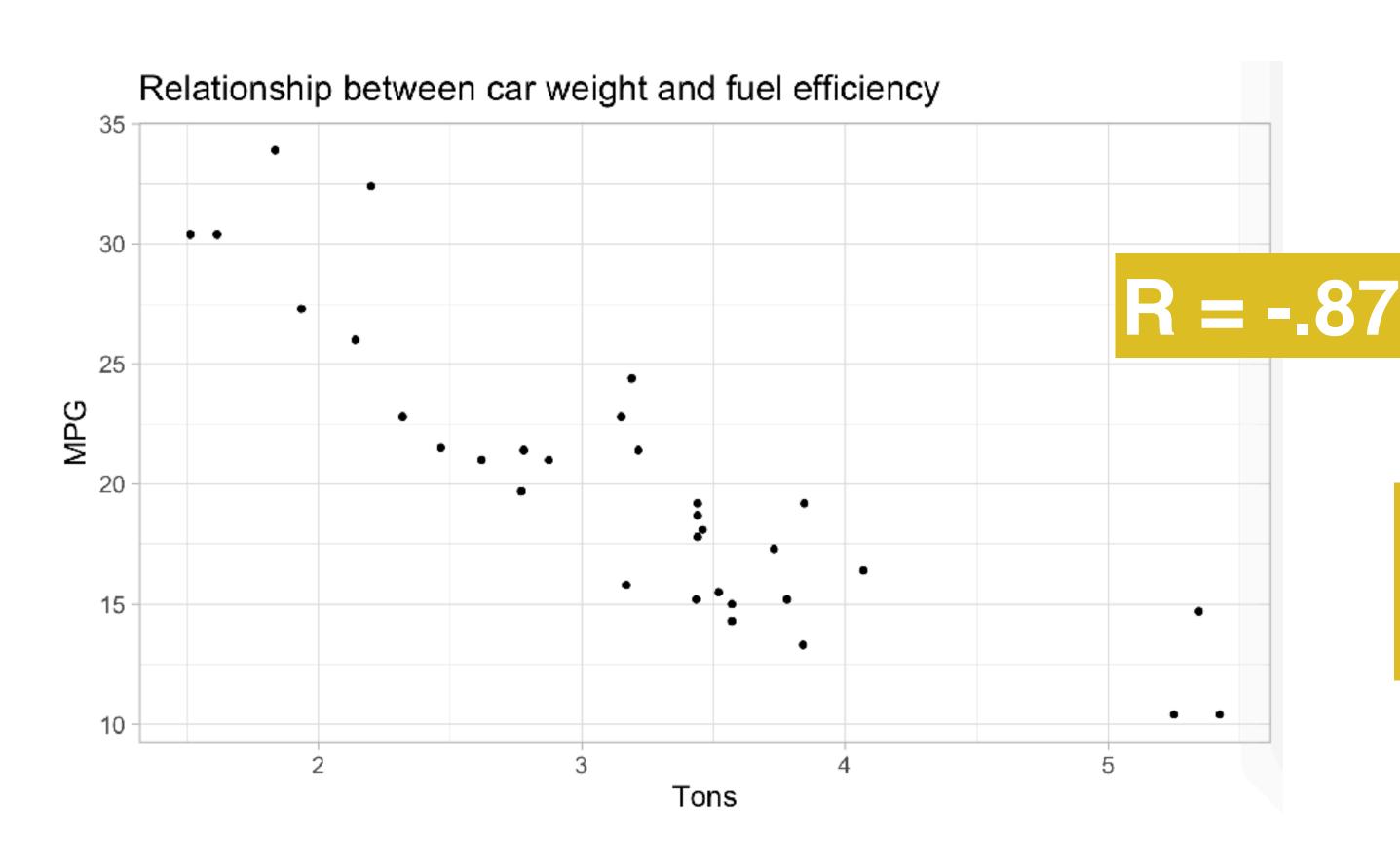


# Why lines?

Correlation just gives us direction and strength of relationship

But what if we wanted to know what level of health we should expect given a level of wealth?

Cars



If we took a ton off a car, how does MPG change?

What MPG should we expect given: a weight of 3 tons, A weight of 6 tons?

# Alternative approaches

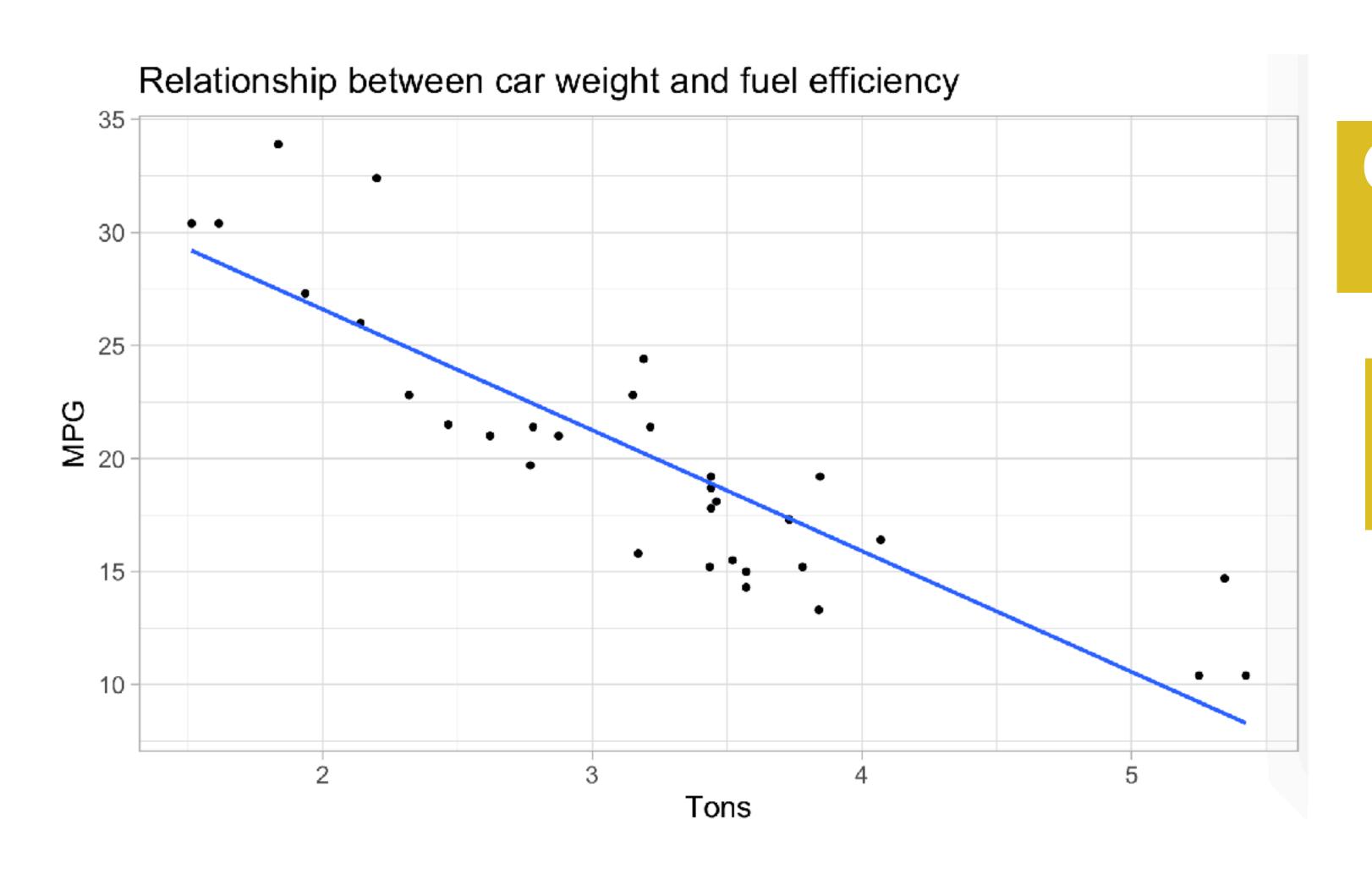
```
# average MPG per weight
mtcars %>%
  group_by(wt) %>%
  summarise(avg_mpg = mean(mpg))
```

```
wt avg_mpg
       <dbl>
1.51
        30.4
        30.4
1.62
1.84
        33.9
        27.3
1.94
2.14
        26
        32.4
2.32
        22.8
        21.5
2.62
        19.7
2.77
with 19 more rows
```

```
# average MPG per weight categories
mtcars %>%
  mutate(wt_cat = cut_number(wt, n = 3)) %>%
  group_by(wt_cat) %>%
  summarise(avg_mpg = mean(mpg))
```

Strengths vs. weaknesses?

.....



# Guess MPG even where no data on weight

Slope of line gives me general rate of change

# Speaking the language

Y

Outcome variable

Response variable

Dependent variable

What you want to explain or predict

X

Explanatory variable

Predictor variable

Independent variable

What you use to explain changes in Y

# Identify the parts

A car company determining the effect of weight on fuel efficiency

Weather channel using changes in temperature, pressure, humidity, etc., to predict rain or no rain for tomorrow

Do students who get tutoring tend to get higher grades?

Amazon using your browsing history, past purchases, demographics, etc., to suggest purchases

## Steps

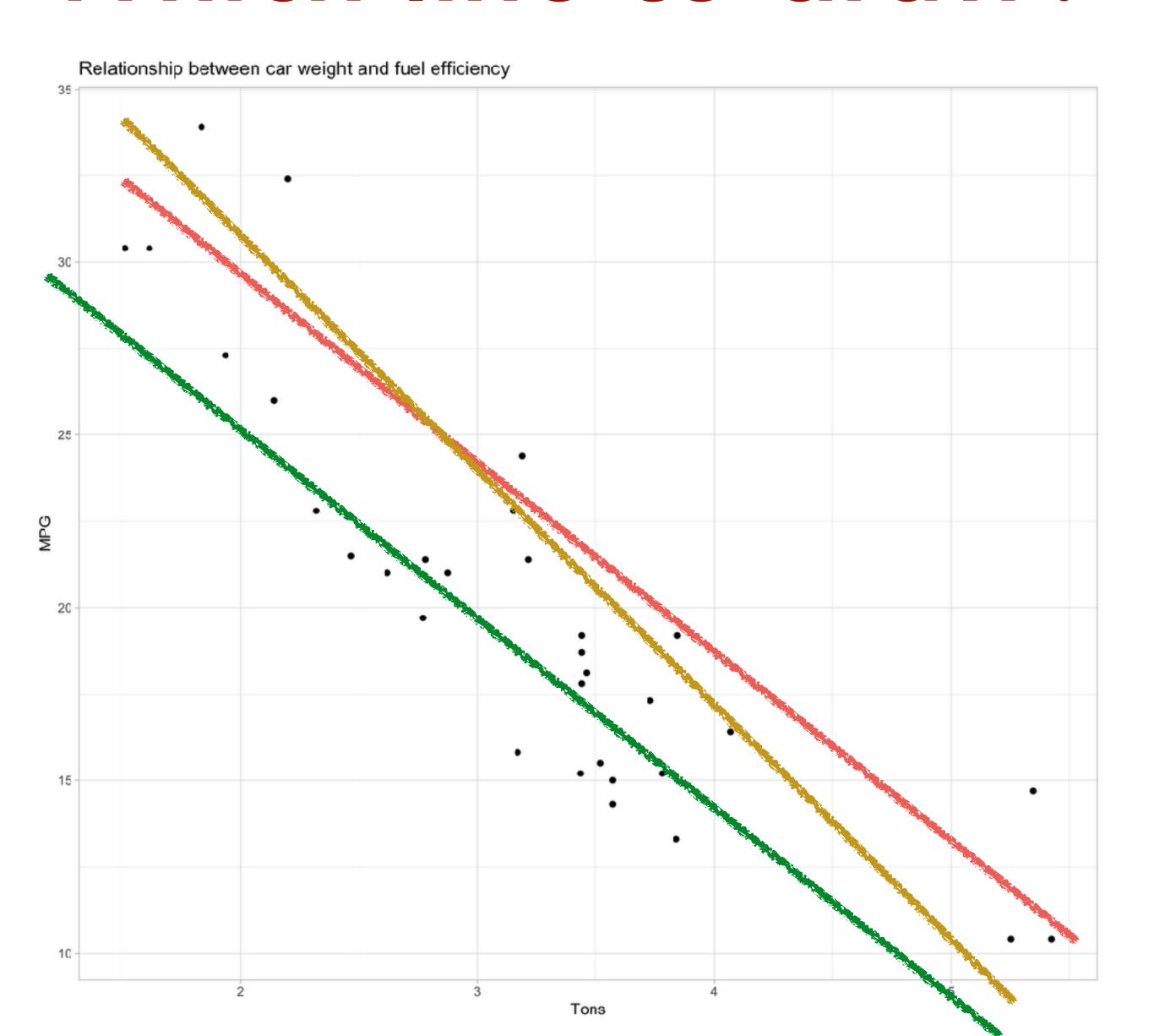
Plot X and Y

Draw line to approximate relationship

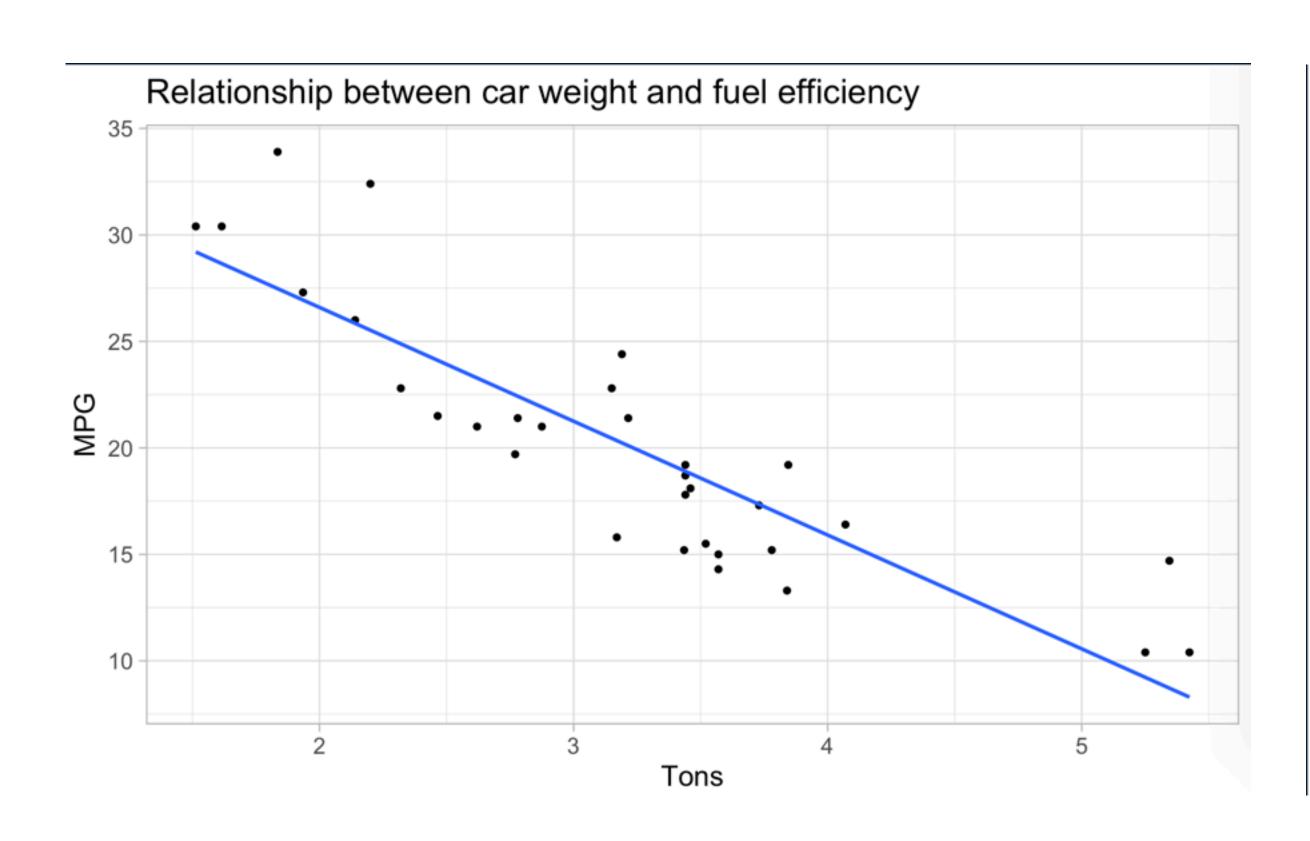
Find "math-y" parts of line

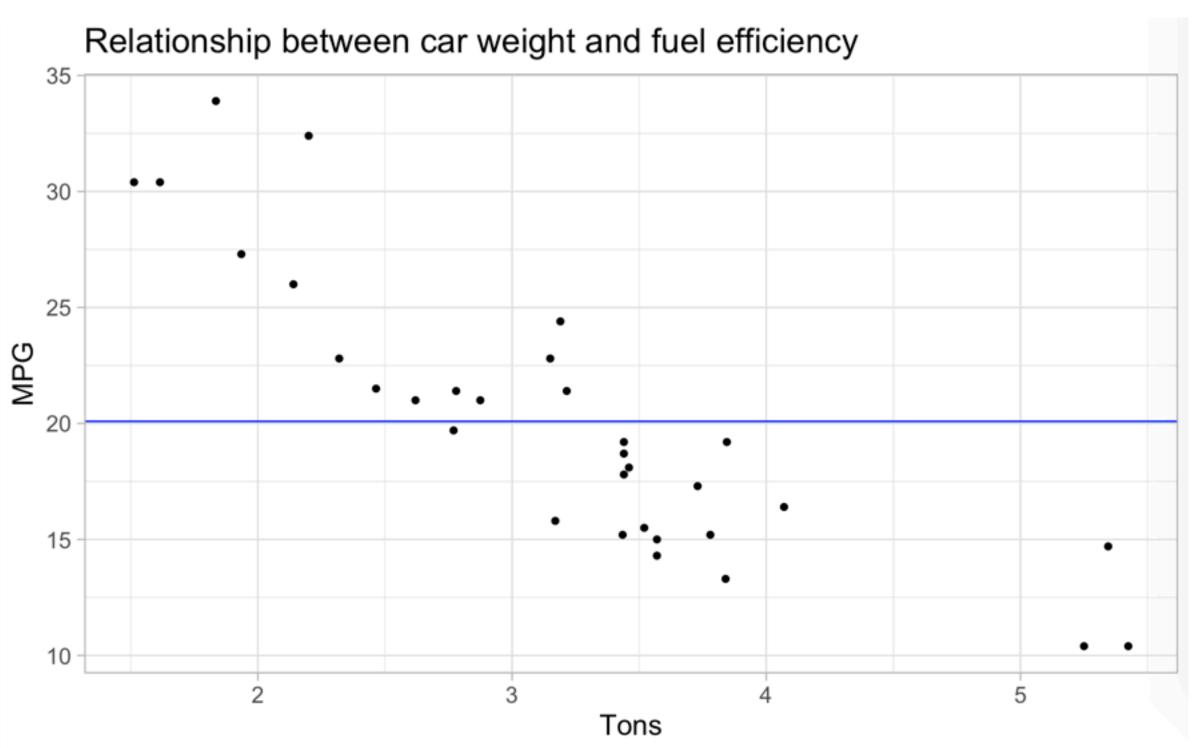
Interpret the math

## Which line to draw?

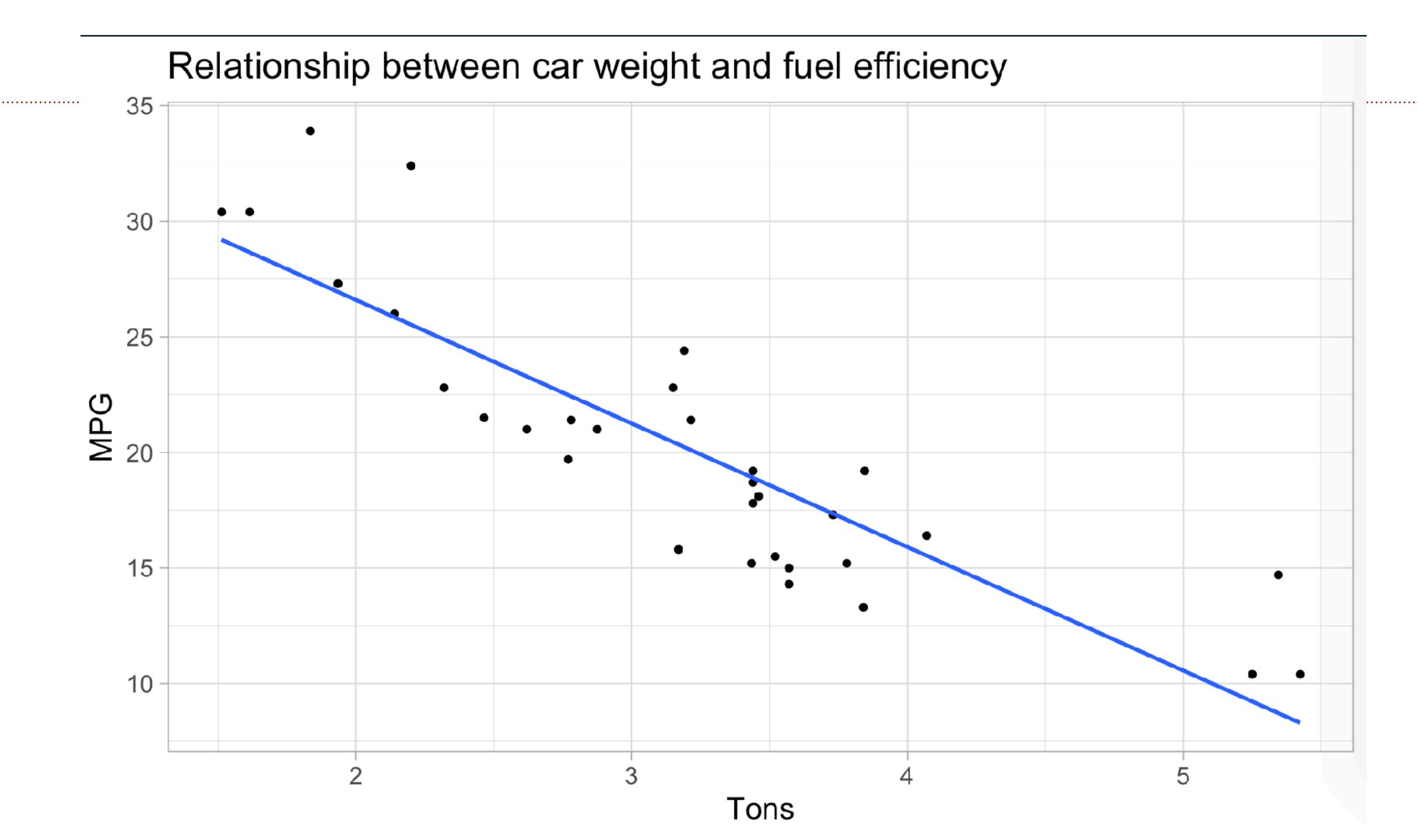


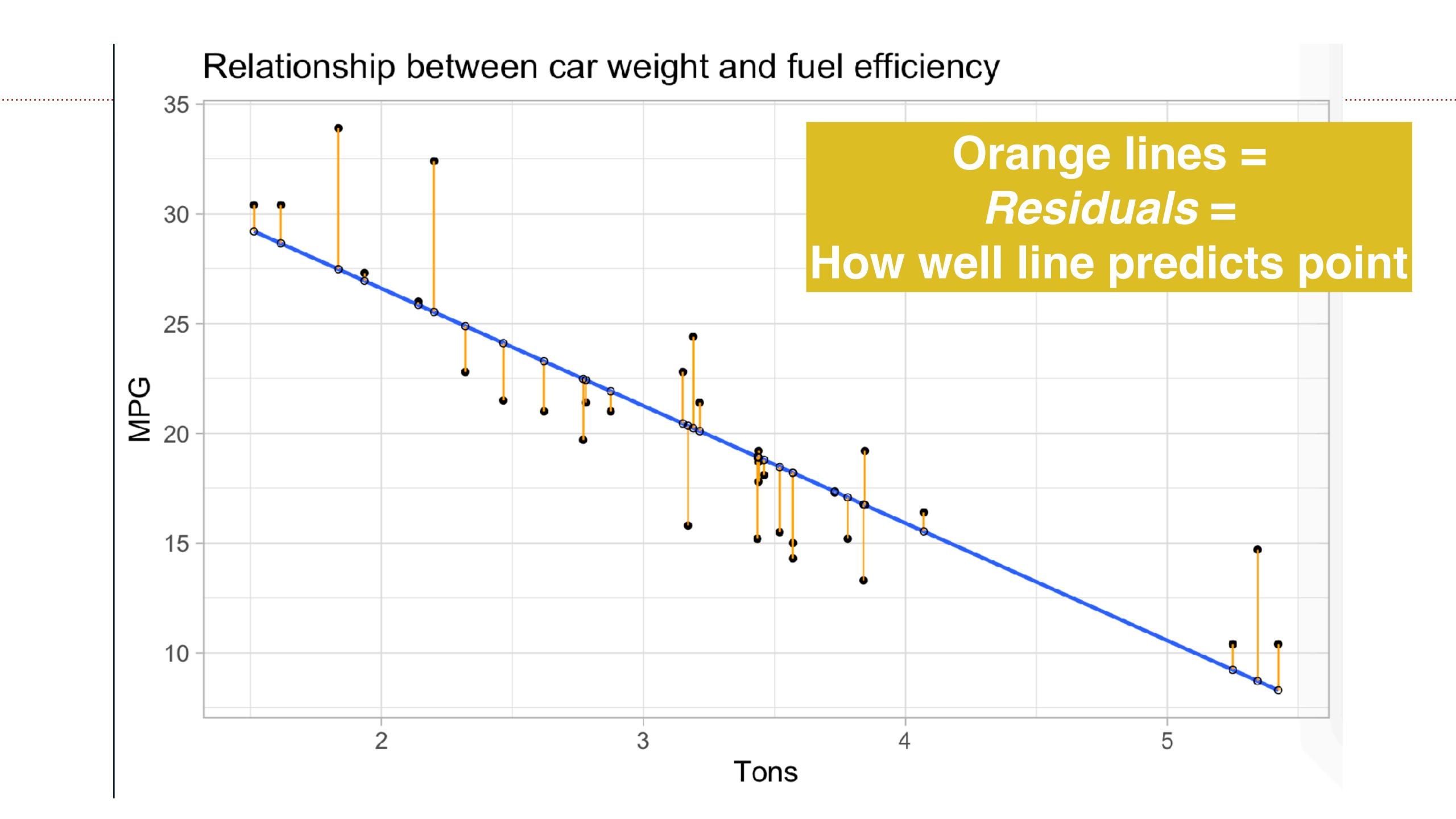
## Compare two lines

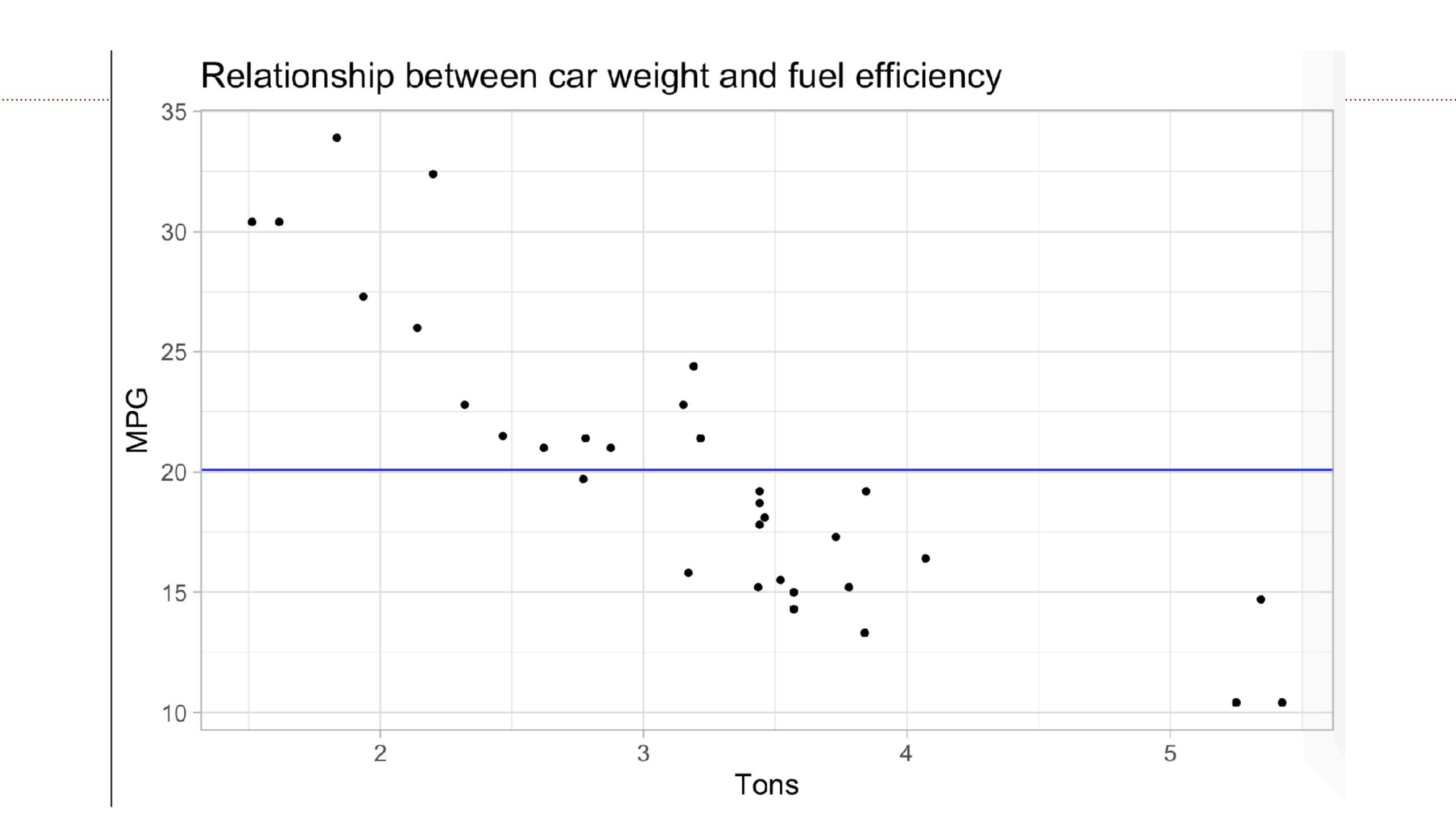


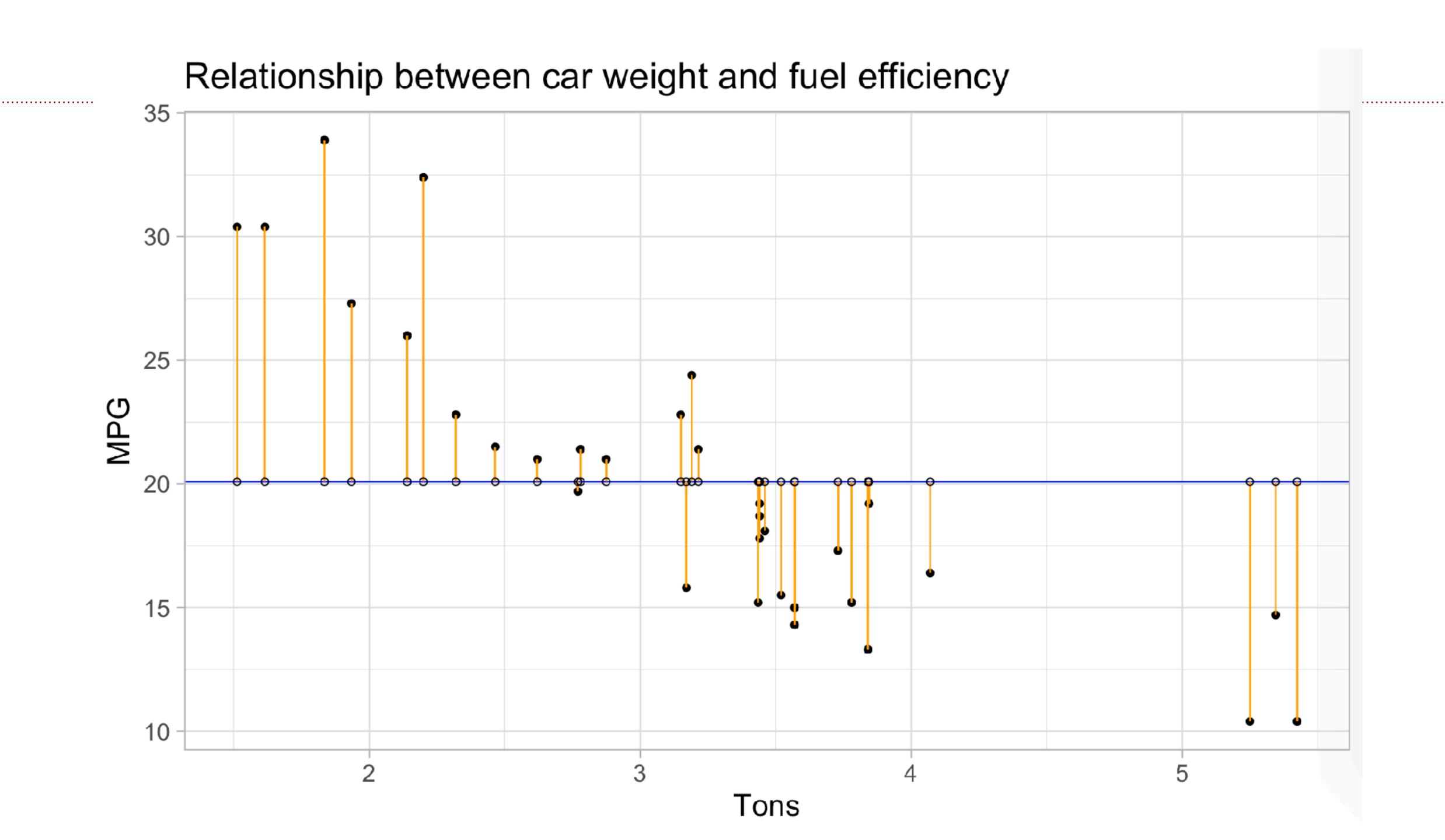


Which line fits better? Why?

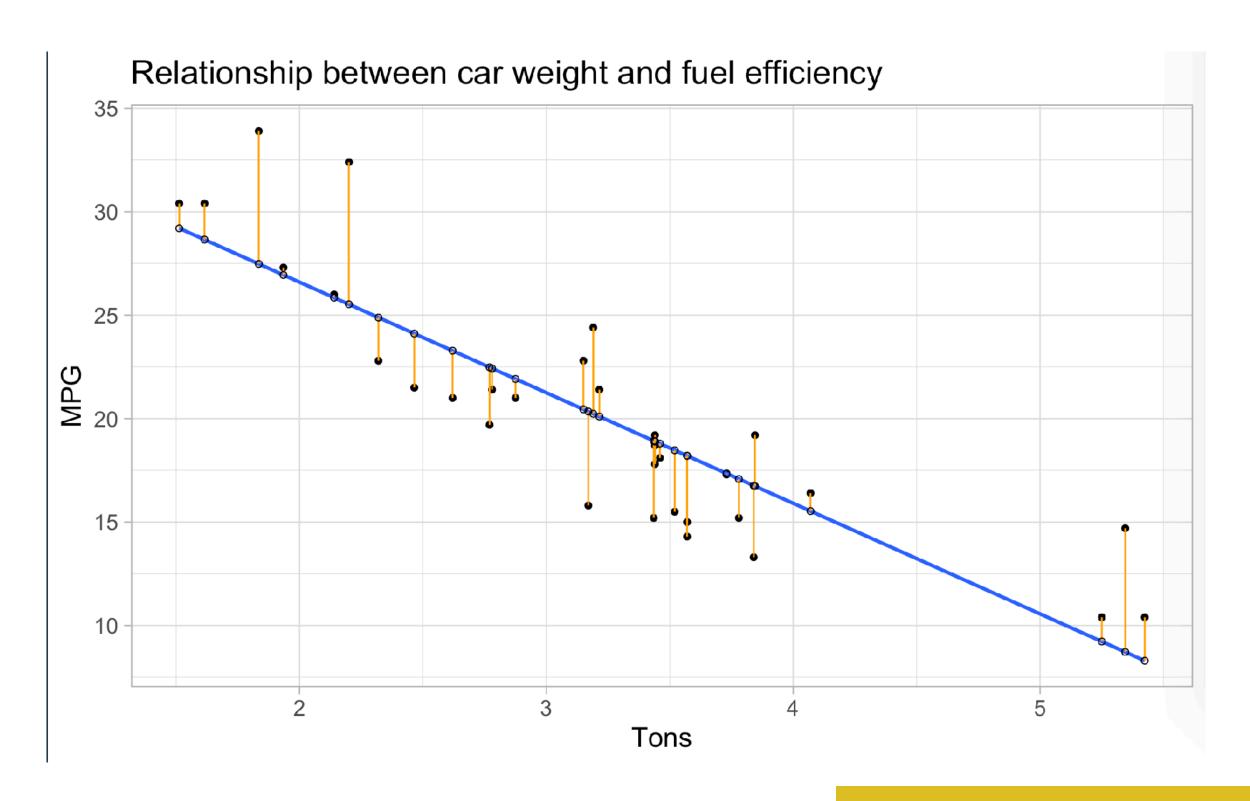


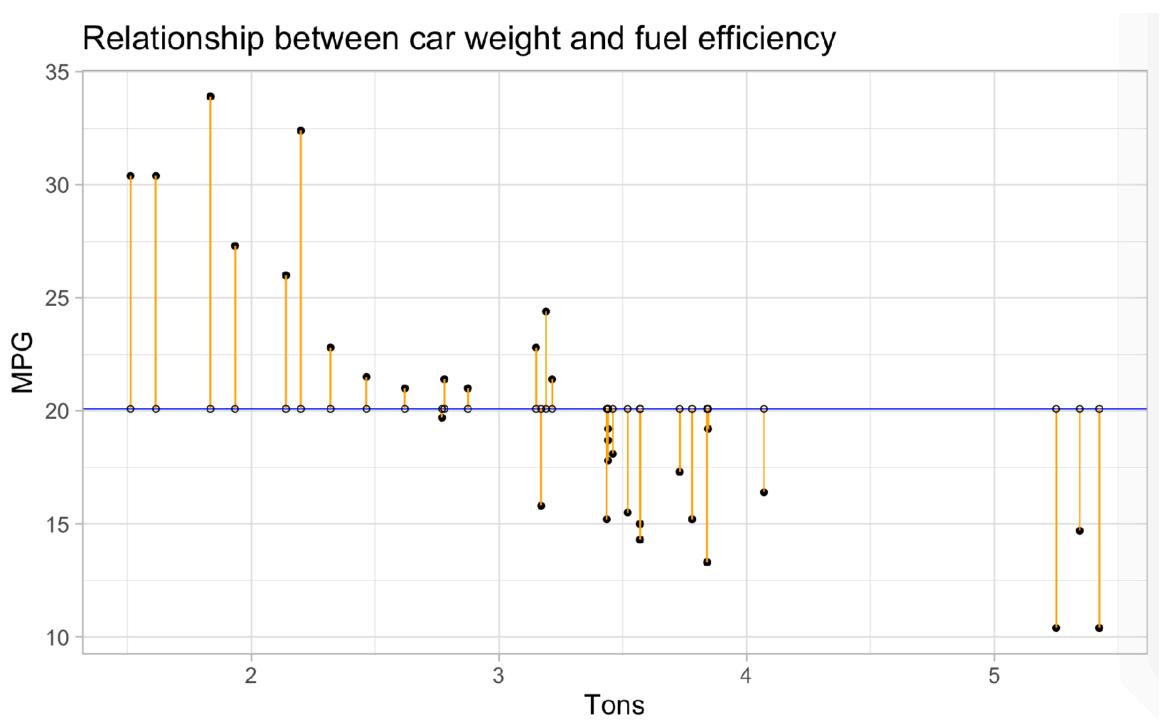






### Which is better?





SSR = 278

For each potential line:
Square distances from line,
Add them all up
Pick line with lowest sum

SSR = 1126

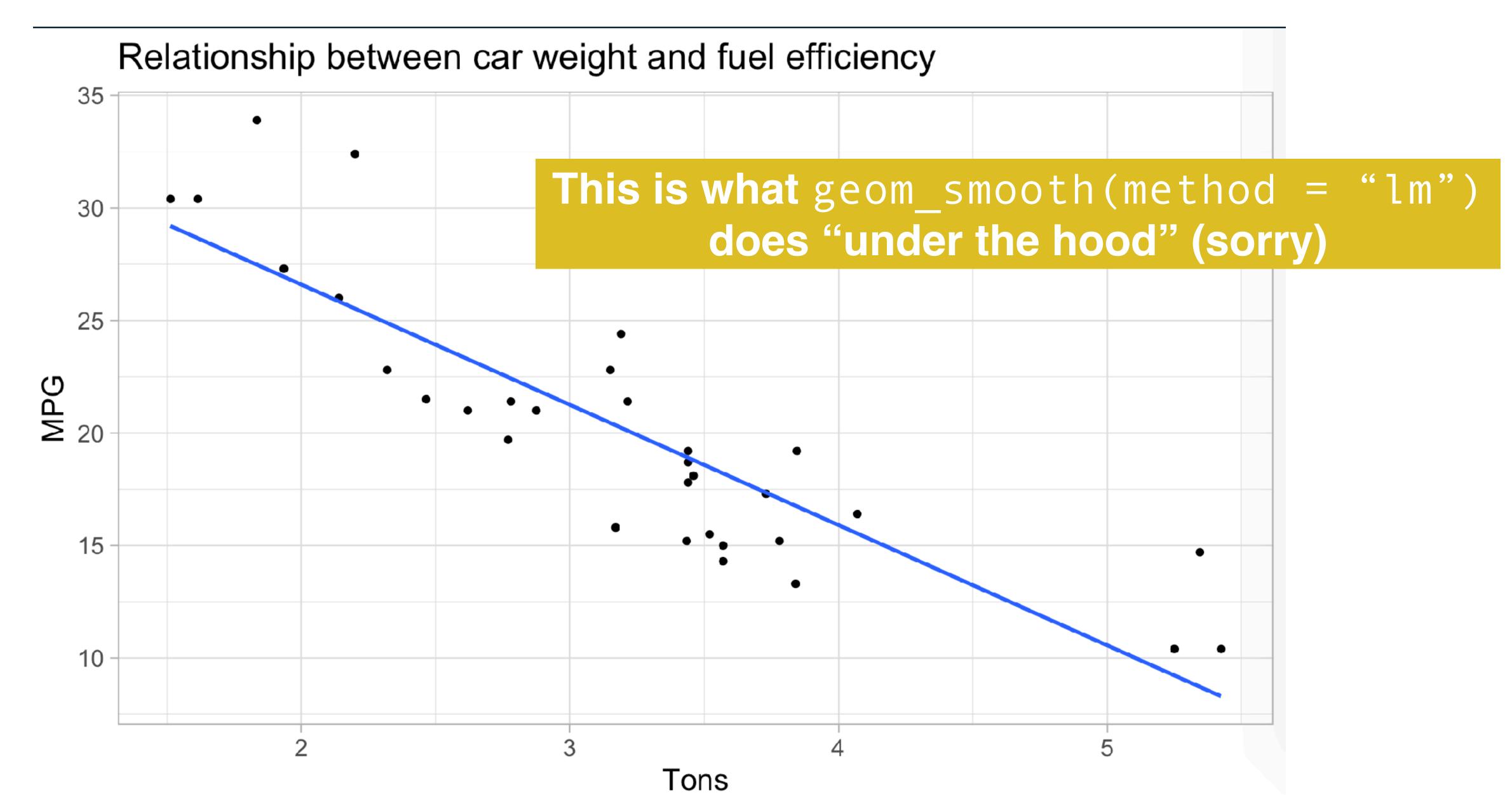
### The best line

Ordinary Least Squares (OLS) is one way of getting "best" line

Minimize sum of the squares of the differences between the observed and predicted values

$$\hat{\boldsymbol{\beta}} = (\mathbf{X}^{\mathrm{T}}\mathbf{X})^{-1}\mathbf{X}^{\mathrm{T}}\mathbf{y}.$$

## OLS



# Getting the line

$$Y = mx + b$$

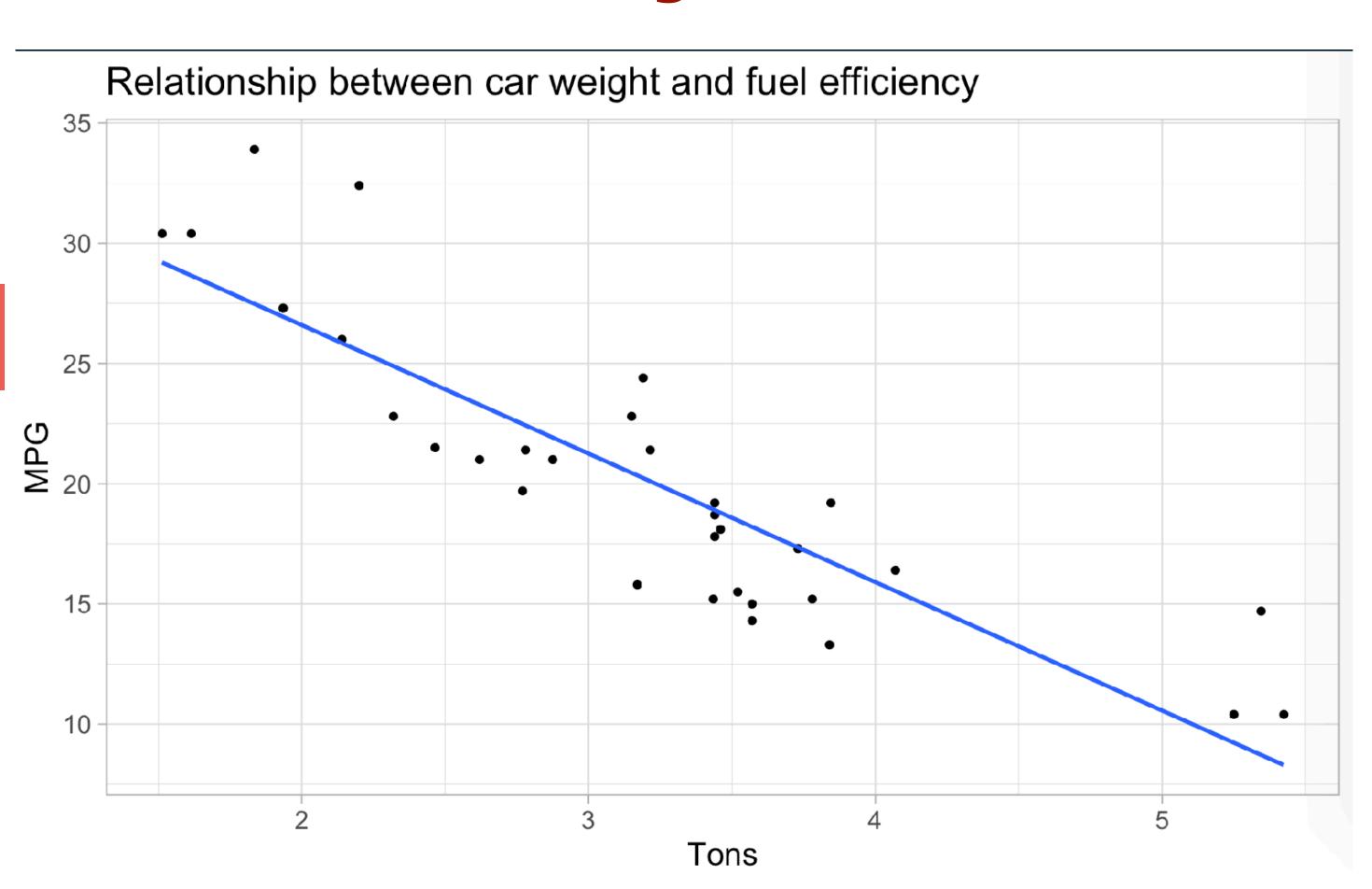


# From 6th grade algebra to Statistics

# Modeling car weight and fuel efficiency

$$\hat{y} = \beta_0 + \beta_1 x_1 + \epsilon$$

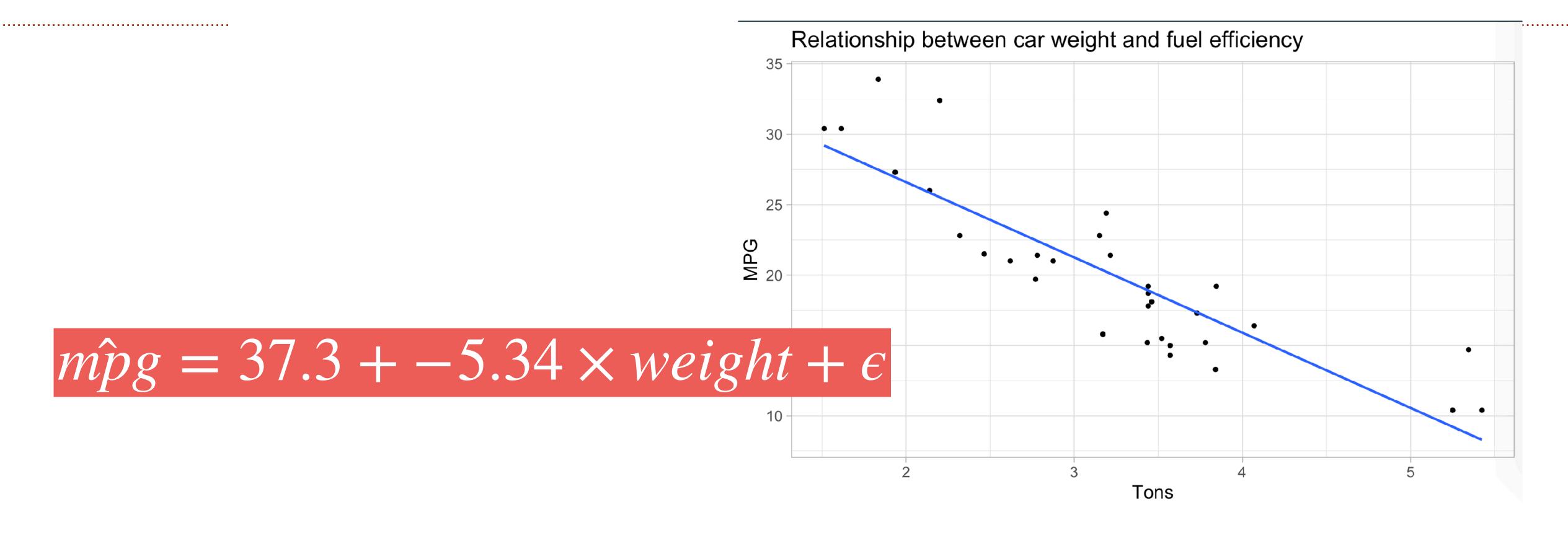
$$m\hat{p}g = \beta_0 + \beta_1 weight + \epsilon$$



# Modeling car weight and fuel efficiency

```
mpg_model = lm(mpg ~ wt, data = mtcars)
mpg_model %>%
   get_regression_table()
```

```
A tibble: 2 \times 7
        estimate std_error statistic p_value lower_ci upper_ci
 term
       <dbl>
 <chr>
 intercept 37.3
                         19.9
                                 0 33.4
                 1.88
                                           41.1
2 wt
                                           -4.20
          -5.34
                  0.559
                         -9.56
                                 0
                                     -6.49
```



```
# A tibble: 2 x 7

term estimate std_error statistic p_value lower_ci upper_ci

<chr> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> </dbl>

1 intercept 37.3

2 wt -5.34

NOT YET; end of semester
```

# Why doesn't it look right?



## Interpretation

A one unit increase in X is associated with a  $\beta_1$  increase (or decrease) in Y, on average

$$m\hat{p}g = 37.3 + -5.34 \times weight + \epsilon$$

Put the above in human words